

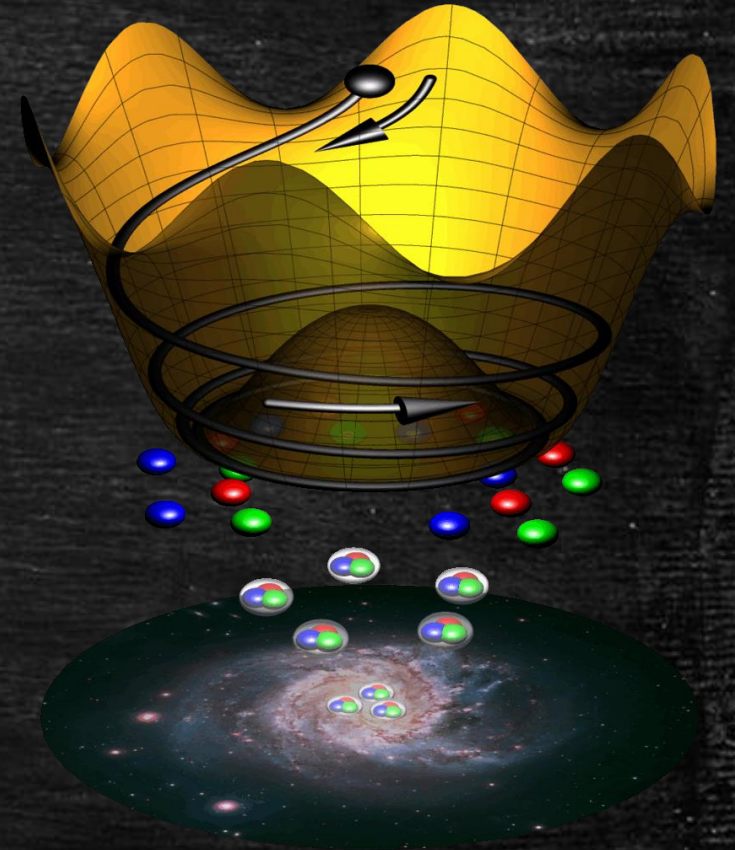
Axion Rotation as the Icing on the Cosmic Cake

Axion in Seoul
Seoul National University

July 28th, 2026

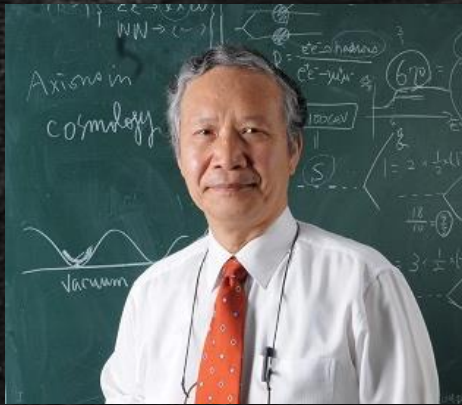
Raymond Co

Indiana University



2510.01308 RC, Fernandez, A. Ghalsasi, K. Harigaya, and J. Shelton
2608.IHope RC, T. Lee, S.C. Lam

In Two Days

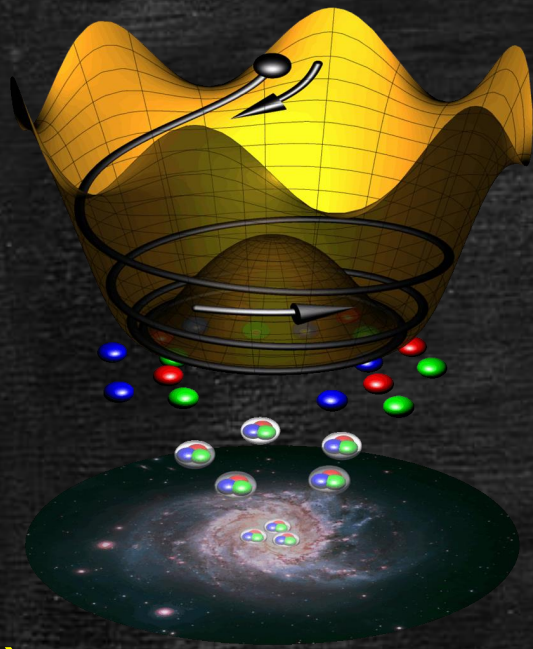


...
Top Scientist and Technologist Award of Korea 2003

Jihn Eui Kim

born on
July 30th 1946

Summary of the Talk

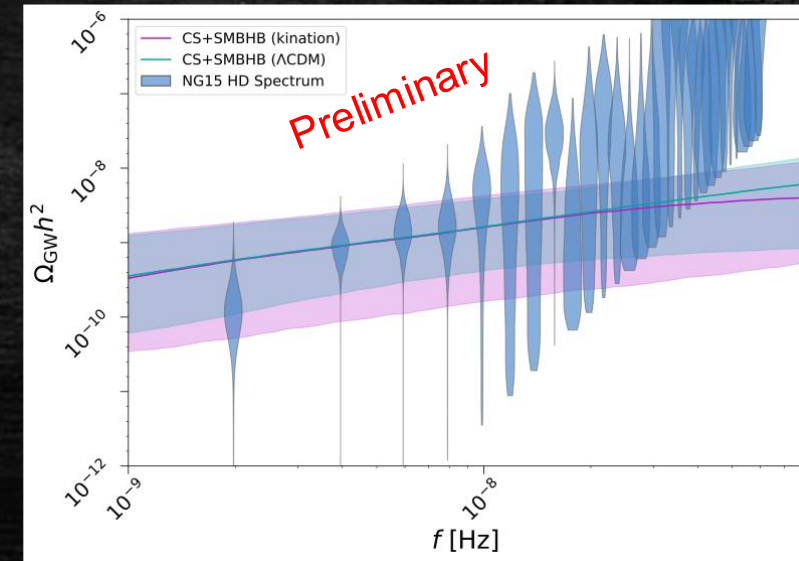
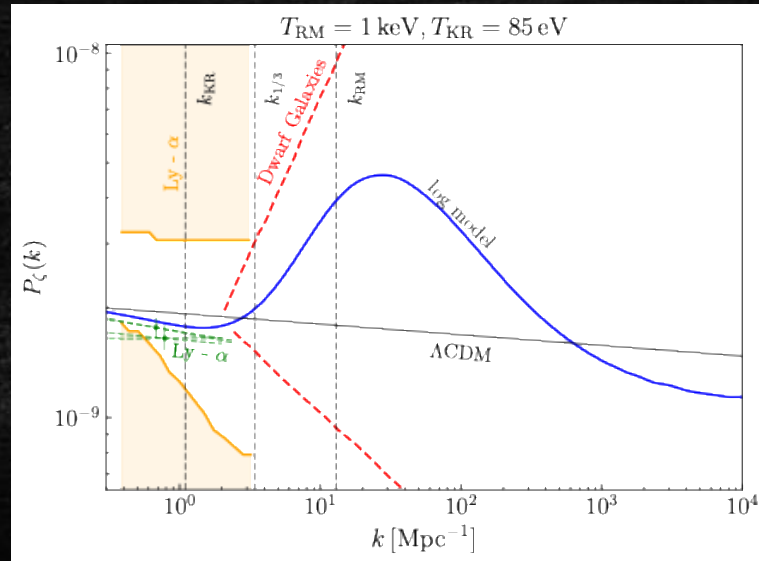
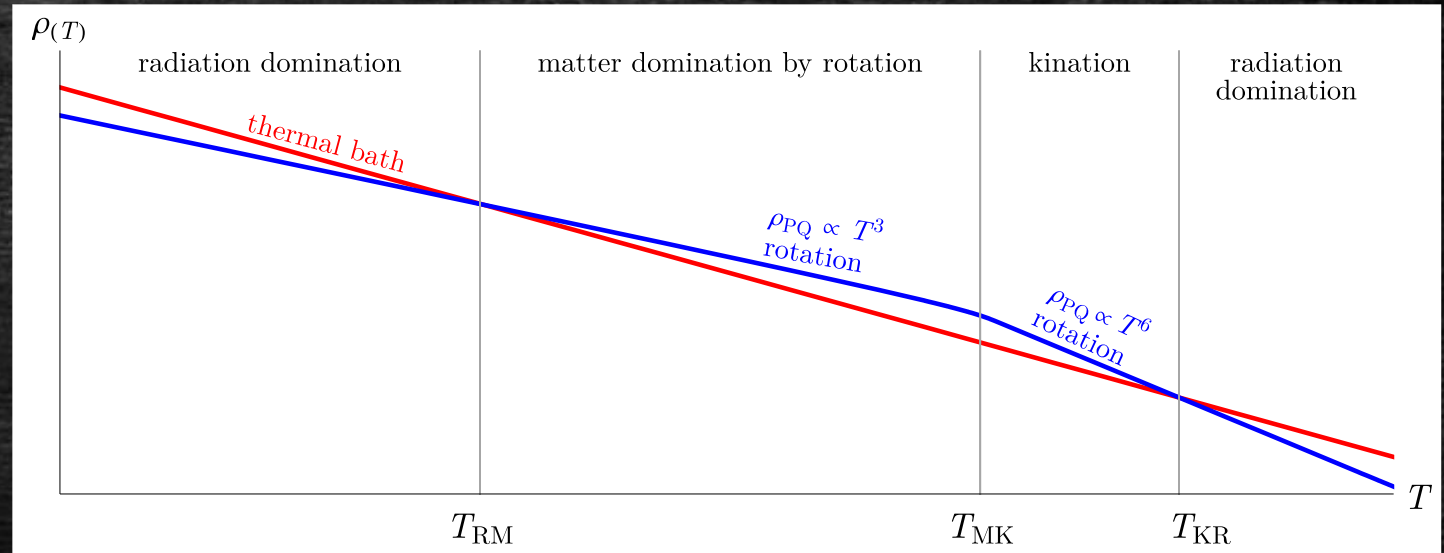


2) Kination cosmology

1) Axion Rotation

3) Enhanced matter power spectrum

Enhanced gravitational waves



Axion Rotation

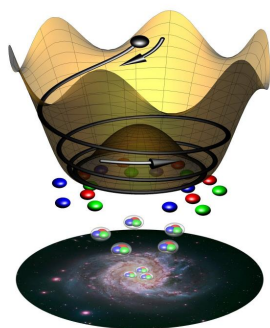
$$\mathcal{L} \supset \frac{\alpha_s}{8\pi} \frac{a}{f_a} G_b^{\mu\nu} \tilde{G}_{b\mu\nu}$$

$$P = \frac{S + f_a}{\sqrt{2}} e^{i \frac{a}{f_a}}$$



Paper sheds light on infant universe and origin of matter

10 March 2020



The rotation of the QCD axion (black ball) produces an excess of matter (colored balls) over antimatter, allowing galaxies and human beings to exist. Credit: Graphic: Harigaya and Co; Photo: NASA

A new study, conducted to better understand the origin of the universe, has provided insight into some of the most enduring questions in fundamental physics: How can the Standard Model of particle physics be extended to explain the cosmological excess of matter over antimatter? What is dark matter? And what is the theoretical origin of an unexpected but observed symmetry in the force that binds protons and neutrons together?

In the paper "Axiogenesis," scheduled to be published in *Physical Review Letters* on March 17, 2020, researchers Keisuke Harigaya, Member in

the School of Natural Sciences at the Institute for Advanced Study, and Raymond T. Co of the University of Michigan, have presented a compelling case in which the quantum chromodynamics (QCD) axion, first theorized in 1977, provides several important answers to these questions.

"We revealed that the rotation of the QCD axion can account for the excess of matter found in the universe," stated Harigaya. "We named this mechanism axiogenesis."

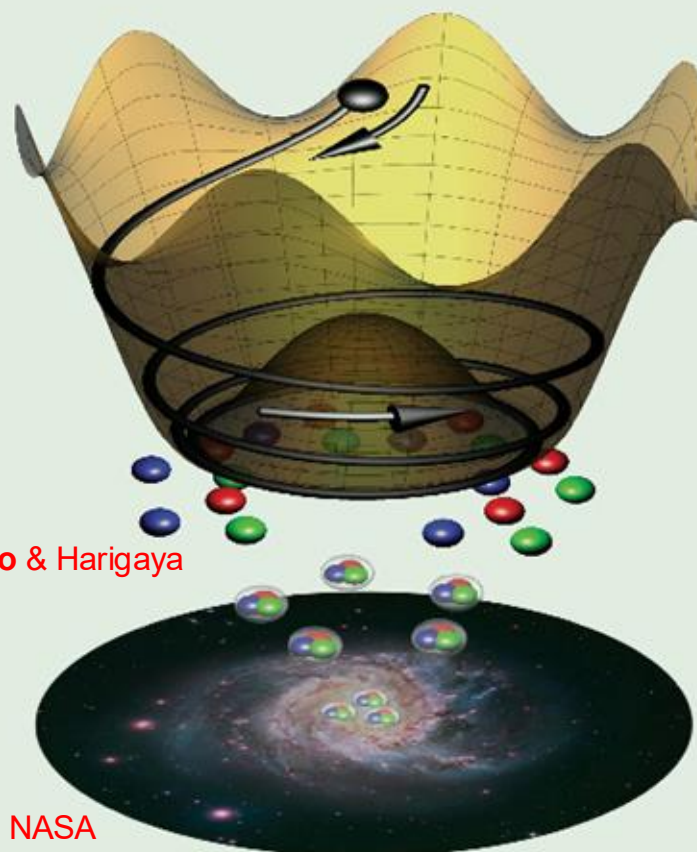
Infinitesimally light, the QCD axion—at least one billion times lighter than a proton—is nearly ghost-like. Millions of these particles pass through ordinary matter every second without notice. However, the subatomic level interaction of the QCD axion can still leave detectable signals in experiments with unprecedented sensitivities. While the QCD axion has never been directly detected, this study provides added fuel for experimentalists to hunt down the elusive particle.

"The versatility of the QCD axion in solving the mysteries of fundamental physics is truly amazing," stated Co. "We are thrilled about the unexplored theoretical possibilities that this new aspect of the QCD axion can bring. More importantly, experiments may soon tell us whether the mysteries of nature truly hint towards the QCD axion."

Harigaya and Co have reasoned that the QCD axion is capable of filling three missing pieces of the physics jigsaw puzzle simultaneously. First, the QCD axion was originally proposed to explain the so-called strong CP problem—why the strong force, which binds protons and neutrons together, unexpectedly preserves a symmetry called the Charge Parity (CP) symmetry. The CP symmetry is inferred from the observation that a neutron does not react with an electric field despite its charged constituents. Second, the QCD axion was found to

Articles published week ending

20 MARCH 2020



Graphic: Co & Harigaya

Photo: NASA



Quanta magazine

Physics

Mathematics

Bio

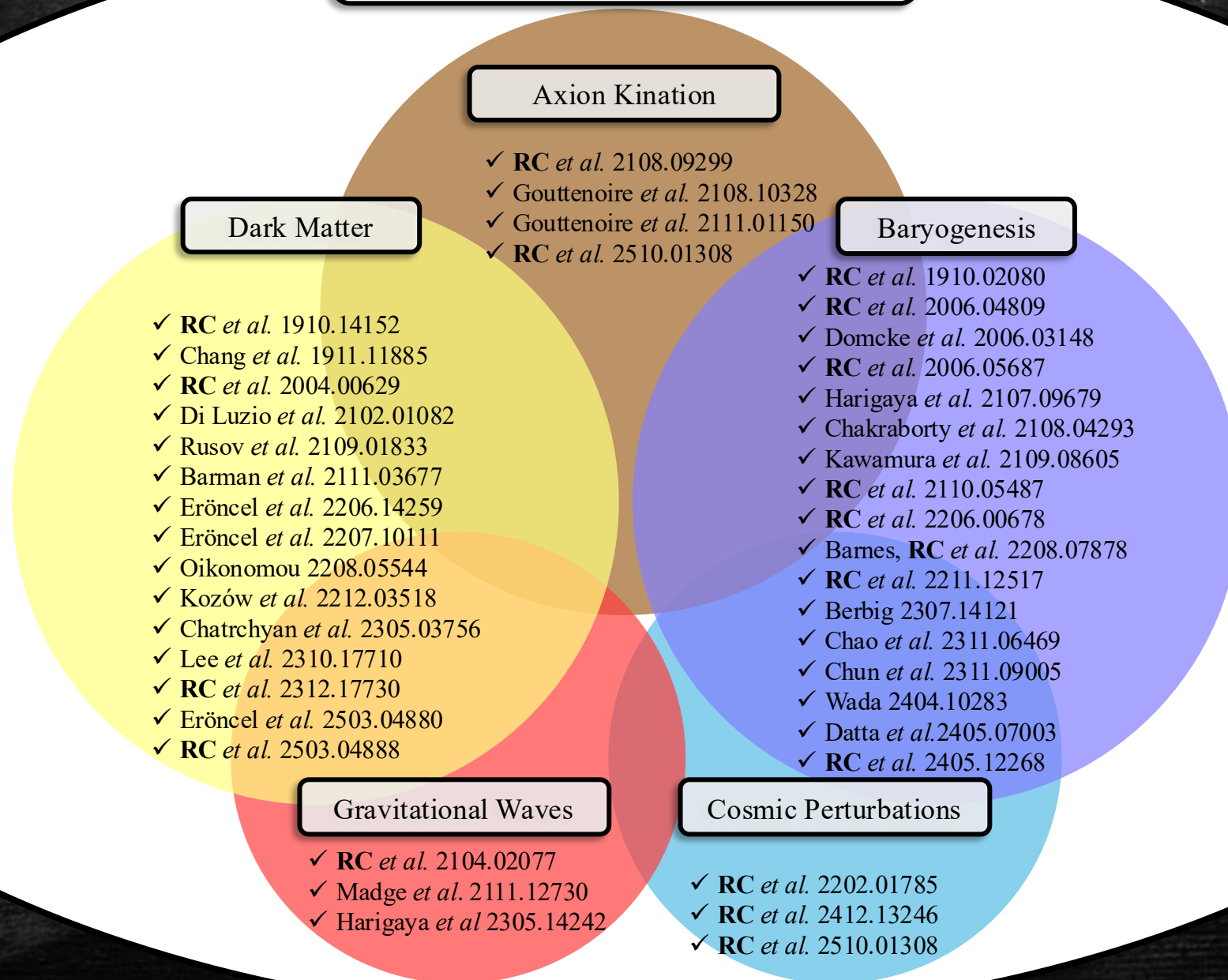
ABSTRACTS BLOG

Axions Would Solve Another Major Problem in Physics

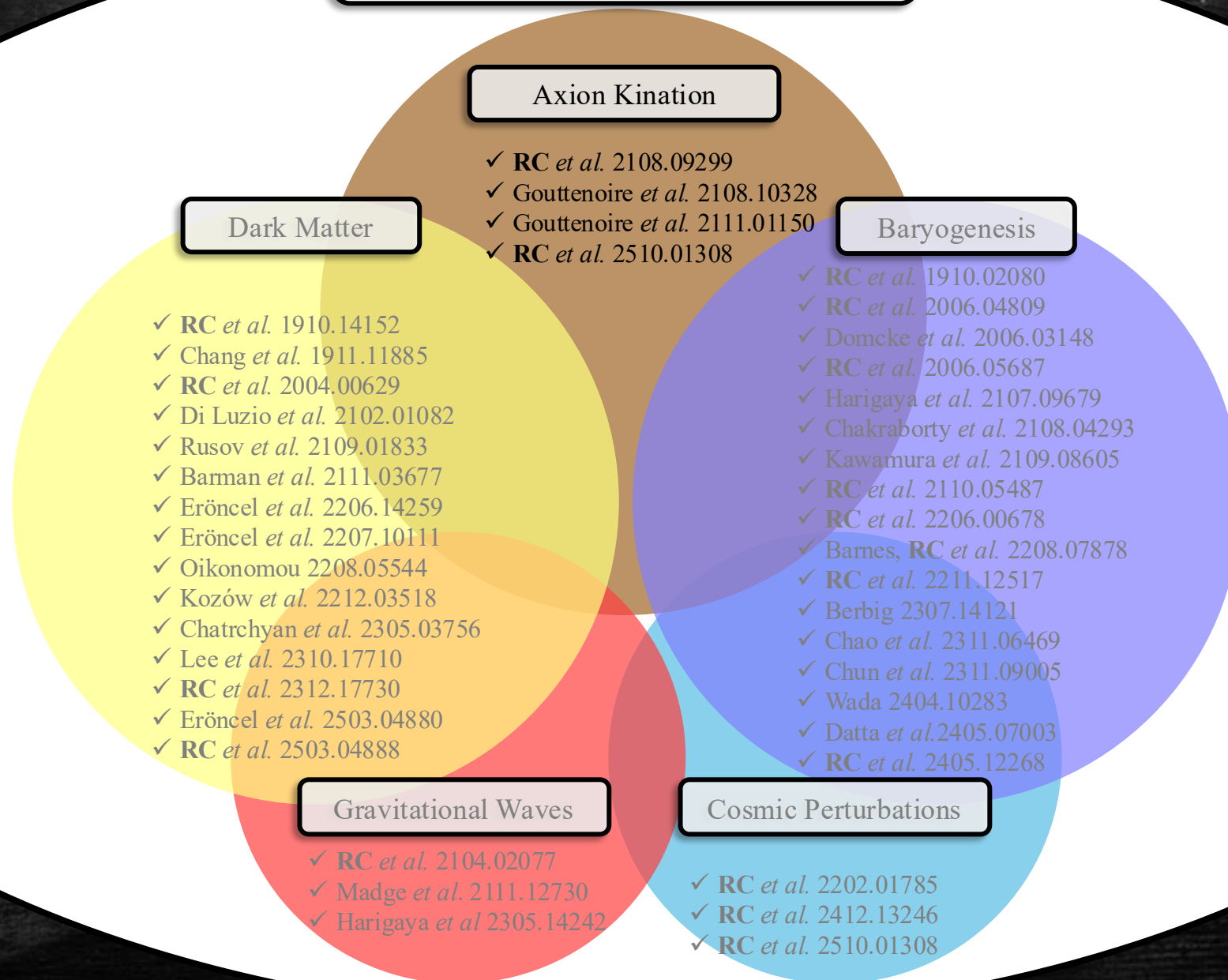
6 |

In a new paper, physicists argue that hypothetical particles called axions could explain why the universe isn't empty.

Axion Rotations

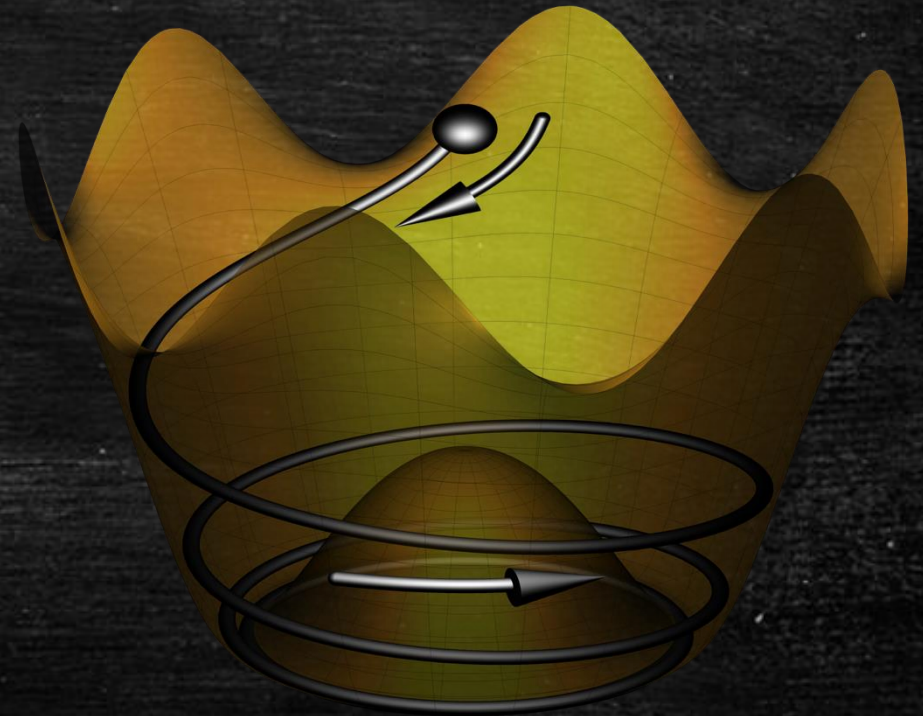


Axion Rotations



Why Rotation?

$$P = \frac{S + f_a}{\sqrt{2}} e^{i \frac{a}{f_a}}$$



Dynamics analogous to that in Affleck-Dine baryogenesis

I. Affleck and M. Dine 1991

PRL 92, 011301 (2004) T. Chiba, F. Takahashi, M. Yamaguchi
[PRL 124, 111602 \(2020\)](#) RC and K. Harigaya

Why Rotation?

Wiggles :

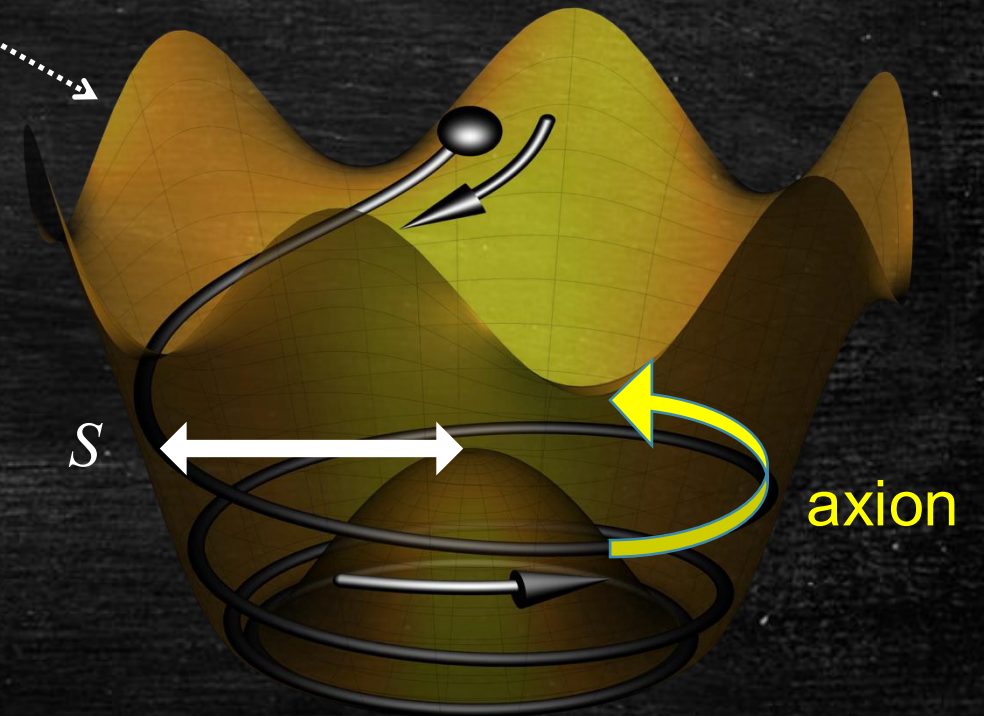
$$V(P) \sim \frac{P^n}{M^{n-4}} e^{i\varphi} + \text{h.c.} \sim \frac{|P|^n}{M^{n-4}} \cos \left(n \frac{a}{f_a} + \varphi \right)$$

$$P = \frac{S + f_a}{\sqrt{2}} e^{i \frac{a}{f_a}}$$

Explicit PQ breaking

expected from quantum gravity
or PQ as an accidental symmetry

S. Giddings et al. 1988
S. Coleman 1988
G. Gilbert 1988



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Large field value :

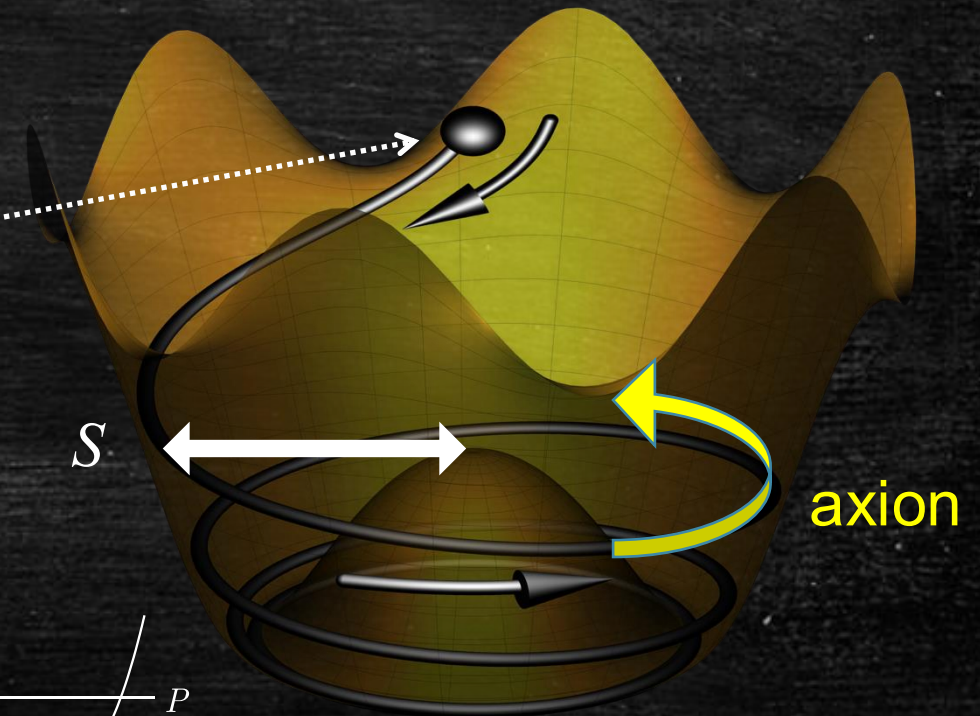
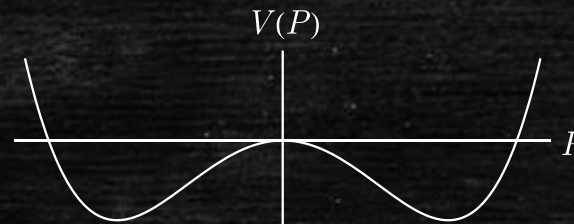
Flat potential

For example, as an initial condition or
set dynamically by inflationary dynamics

$$V(|P|) \sim -H_I^2 |P|^2 + \frac{|P|^d}{M^{d-4}}$$

Hubble-induced mass

M. Dine, L. Randall, and S. D. Thomas 1991



Dynamics analogous to that in Affleck-Dine baryogenesis

I. Affleck and M. Dine 1991

PRL 92, 011301 (2004) T. Chiba, F. Takahashi, M. Yamaguchi
PRL 124, 111602 (2020) RC and K. Harigaya

Axion Kination

Asymmetry of PQ Charge

Noether charge associated with the shift symmetry

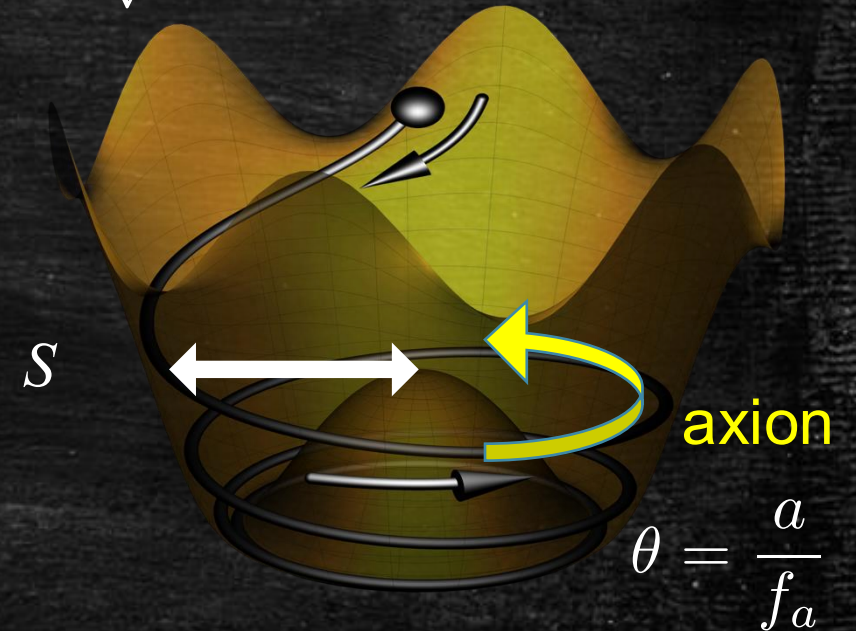
$$n_\theta = S^2 \dot{\theta}$$

this is nothing but
"angular momentum" $r^2 \omega$

$$P = \frac{S + f_a}{\sqrt{2}} e^{i \frac{a}{f_a}}$$

PQ asymmetry
PQ charge density = Rotation of PQ field

This is conserved soon after the initial kick.



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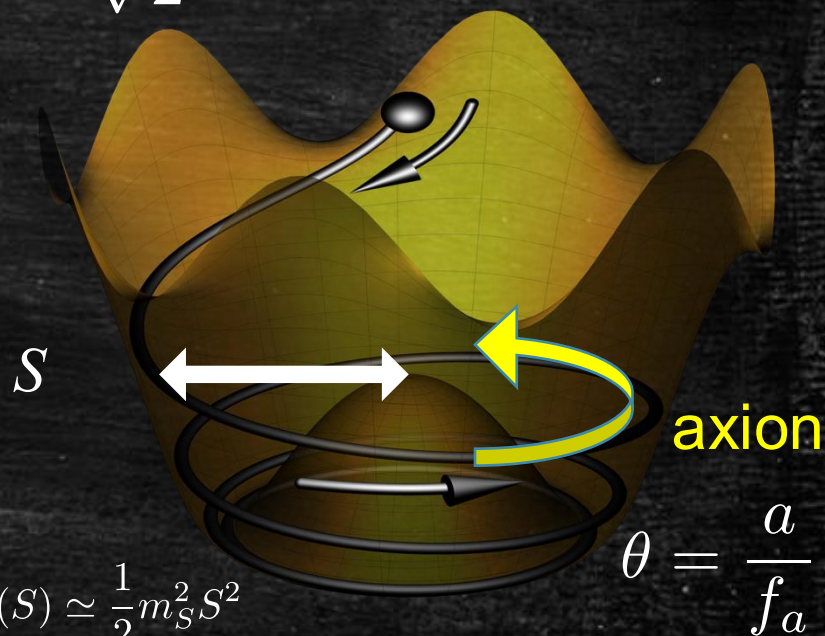
This is conserved soon after the initial kick.

What determines $\dot{\theta}$? Centripetal force!

$$\begin{aligned} F_c &= m a_c \\ V'(S) &= S \dot{\theta}^2 \\ m_S^2 S &= S \dot{\theta}^2 \end{aligned}$$

$\dot{\theta} = m_S$ which is in turn set by supersymmetry scale.

$$P = \frac{S + f_a}{\sqrt{2}} e^{i \frac{a}{f_a}}$$



$$V(S) \simeq \frac{1}{2} m_S^2 S^2$$

from supersymmetry

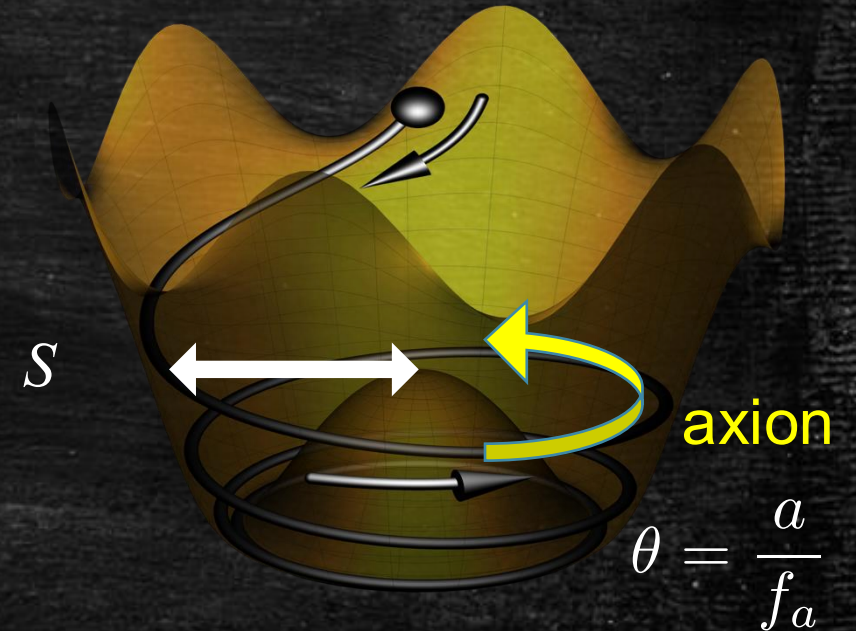
$$\theta = \frac{a}{f_a}$$

PQ Charge Evolution

Charge conservation:

$$n_\theta = S^2 \dot{\theta} \propto \underbrace{R^{-3}}_{\text{dilution due to cosmic expansion}}$$

scale factor of the universe



PQ Charge Evolution

Charge conservation:

$$n_\theta = S^2 \dot{\theta} \propto \underbrace{R^{-3}}_{\substack{\text{scale factor of the universe} \\ \text{dilution due to} \\ \text{cosmic expansion}}}$$

Large field ($S \gg f_a$):

$$S^2 \propto R^{-3}$$

for quadratic potential
 $V(S) \simeq \frac{1}{2} m_S^2 S^2$

$$\dot{\theta} = \text{constant}$$

$$\rho_\theta = \dot{\theta}^2 S^2 \propto R^{-3}$$

matter

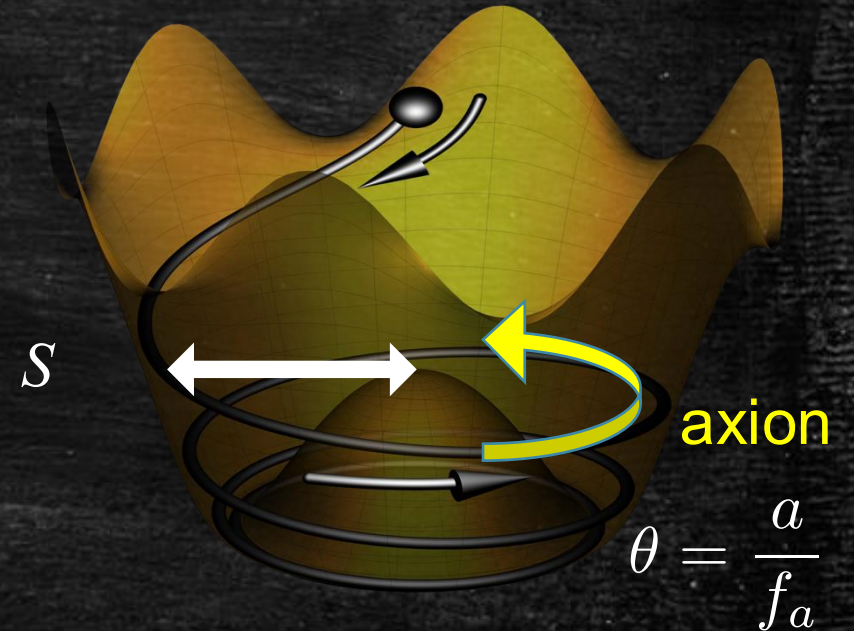
At the minimum:

$$S^2 = f_a^2$$

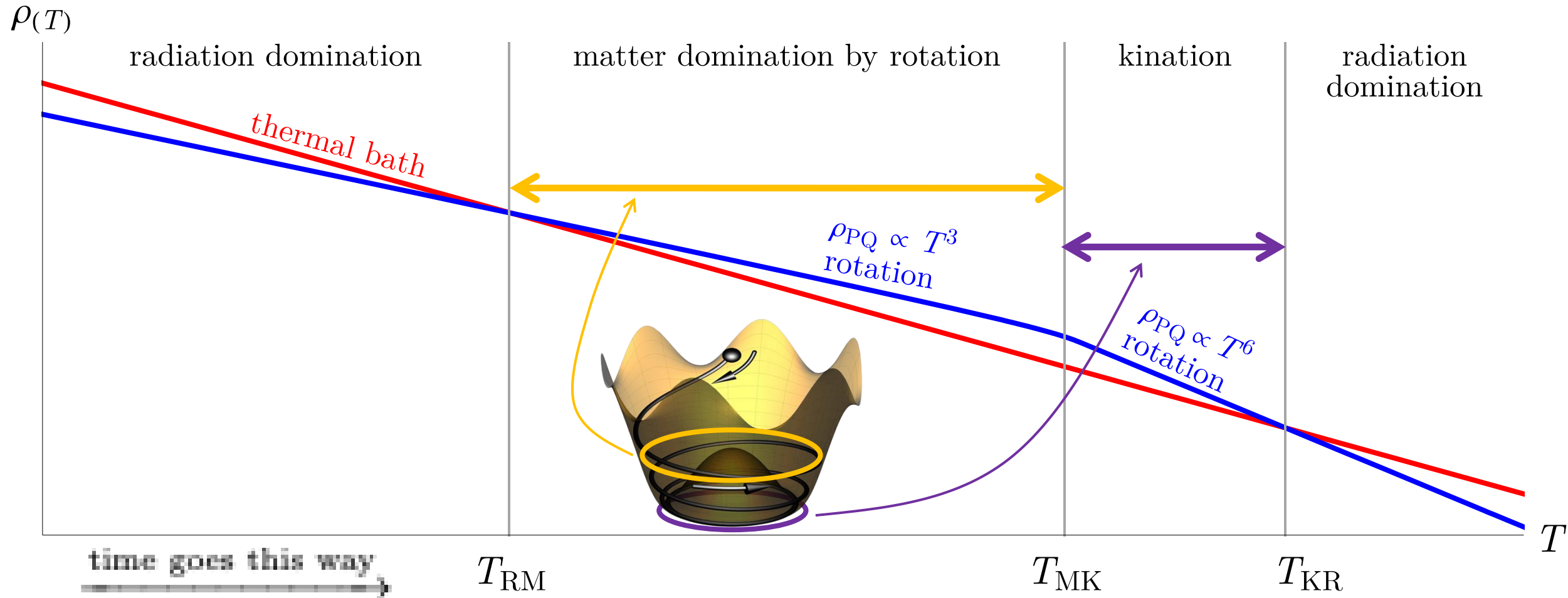
$$\dot{\theta} \propto R^{-3}$$

$$\rho_\theta = \dot{\theta}^2 f_a^2 \propto R^{-6}$$

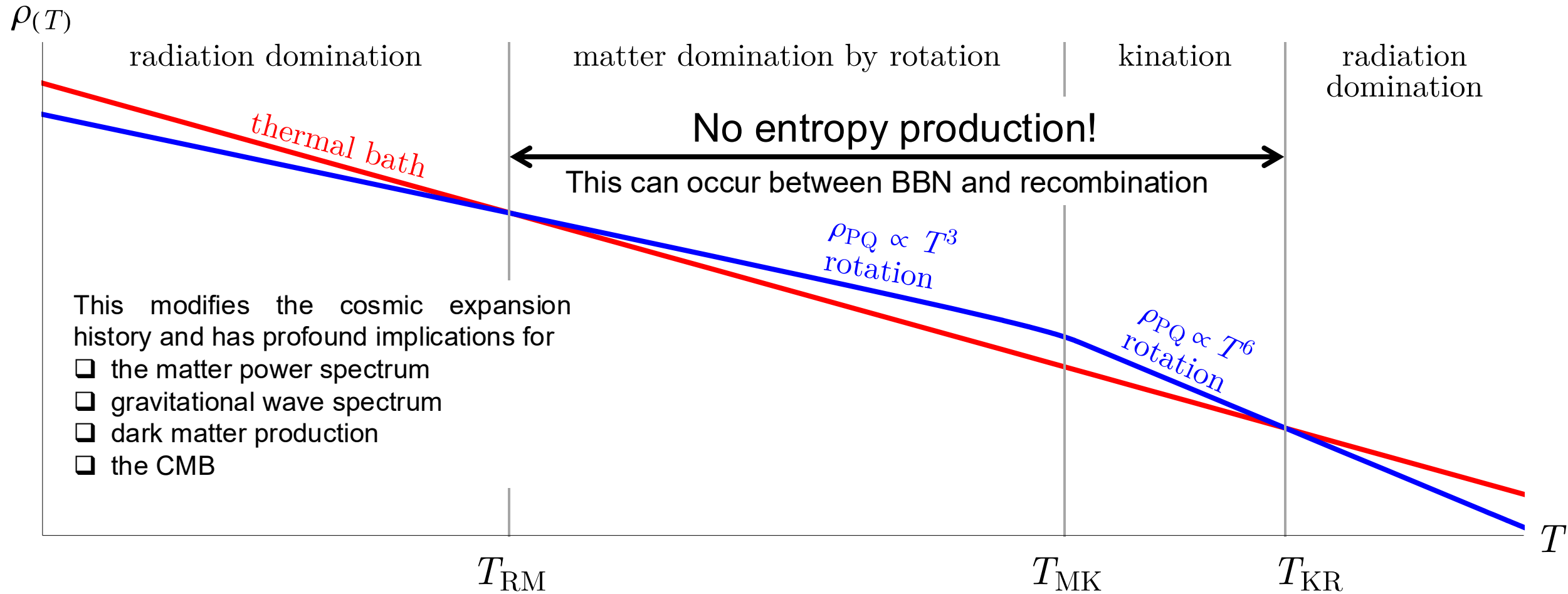
kination



Axion Rotations



Evolution of Energy Densities



PQ-breaking Potential

Piecewise approximation

$$\rho_\theta \propto \begin{cases} R^{-3} & \text{for } S \gg f_a \text{ i.e. } T \gg T_{\text{MK}} \\ R^{-6} & \text{for } S \simeq f_a \text{ i.e. } T \ll T_{\text{MK}} \end{cases}$$

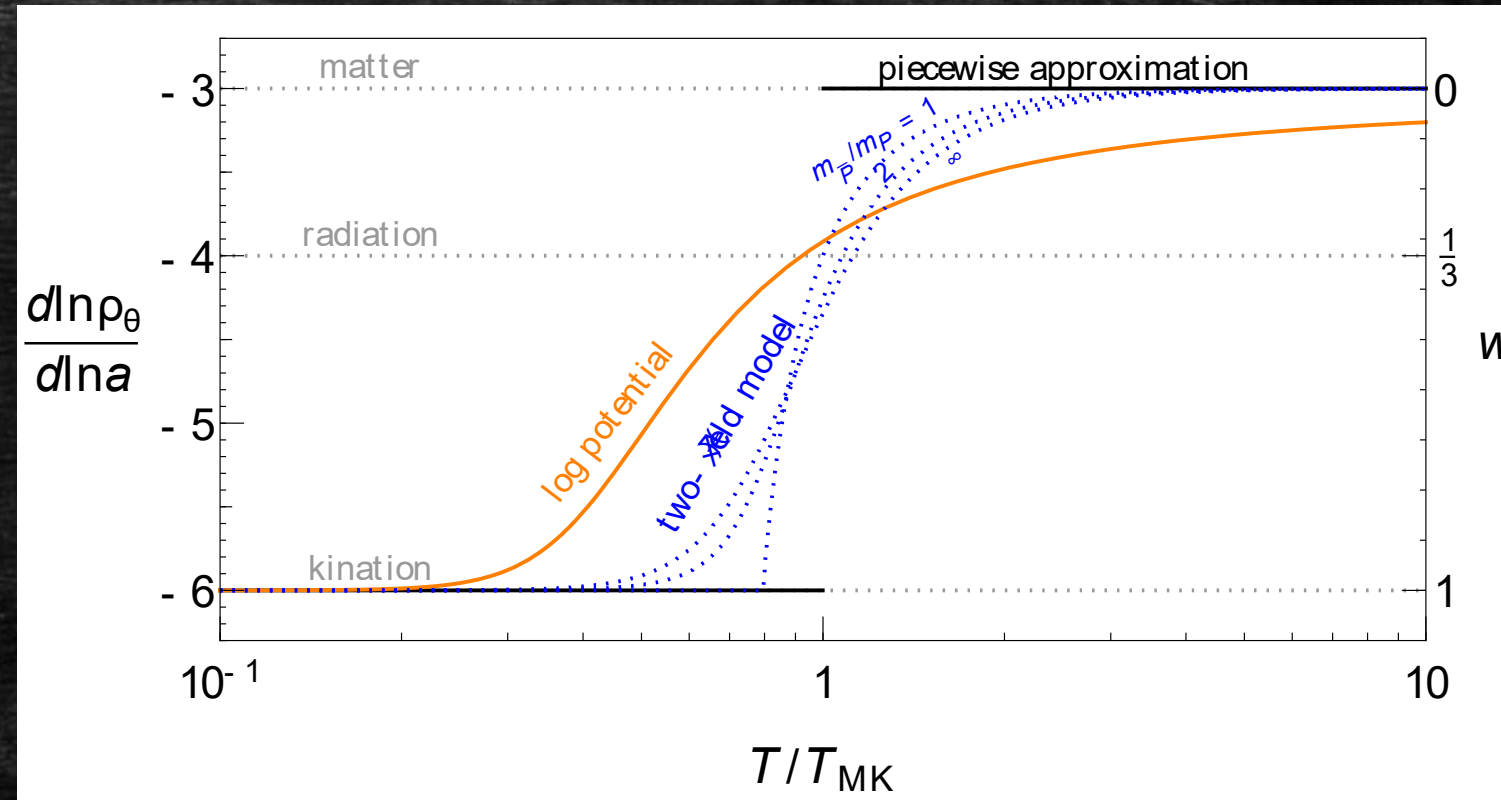
log potential

$$V(P) = m_S^2 |P|^2 \left(\ln \frac{2|P|^2}{f_a^2} - 1 \right)$$

Two-field model

$$W = X(P\bar{P} - v_P^2)$$

$$V_{\text{soft}} = m_P^2 |P|^2 + m_{\bar{P}}^2 |\bar{P}|^2$$



PQ-breaking Potential

Piecewise approximation

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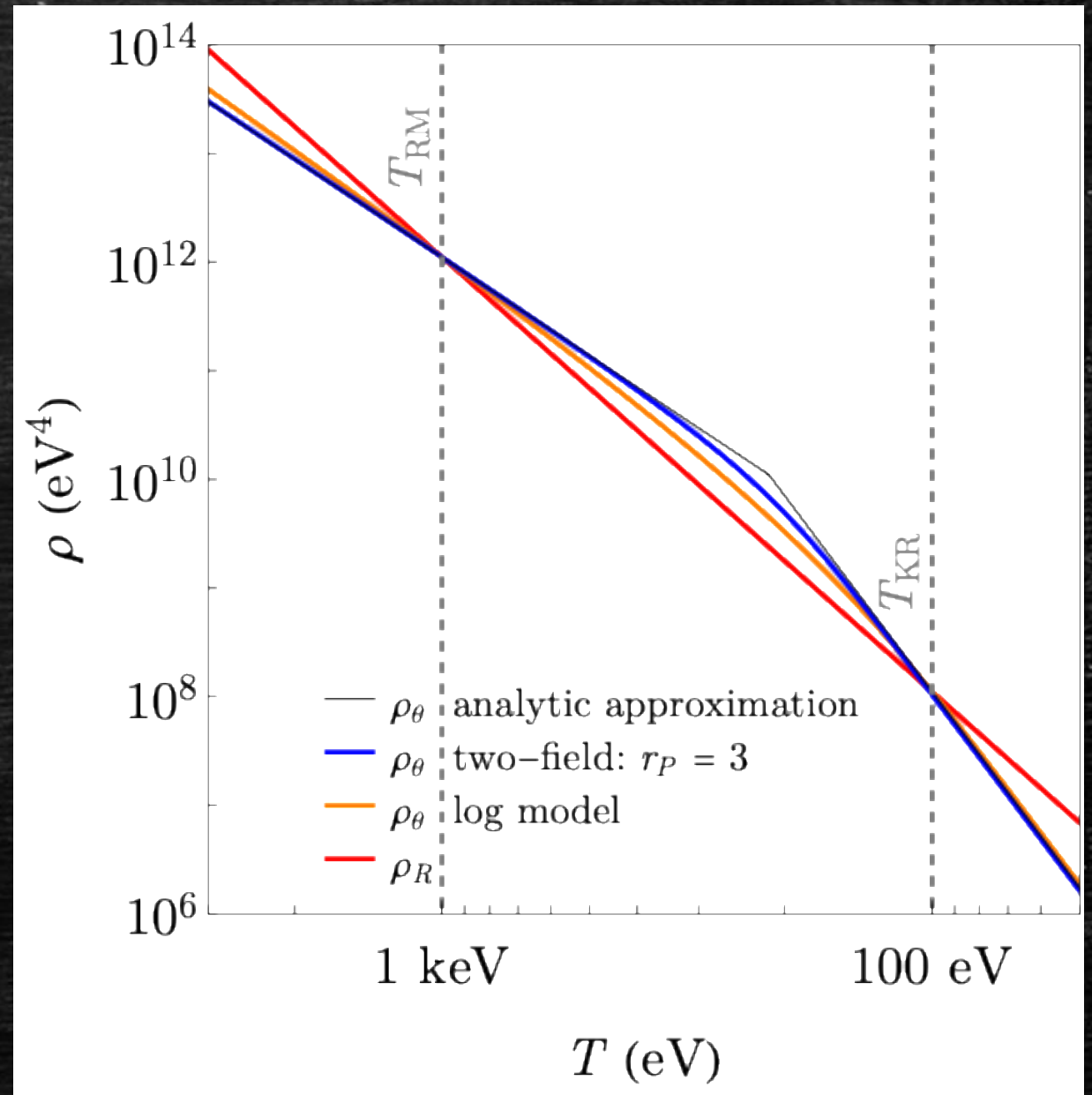
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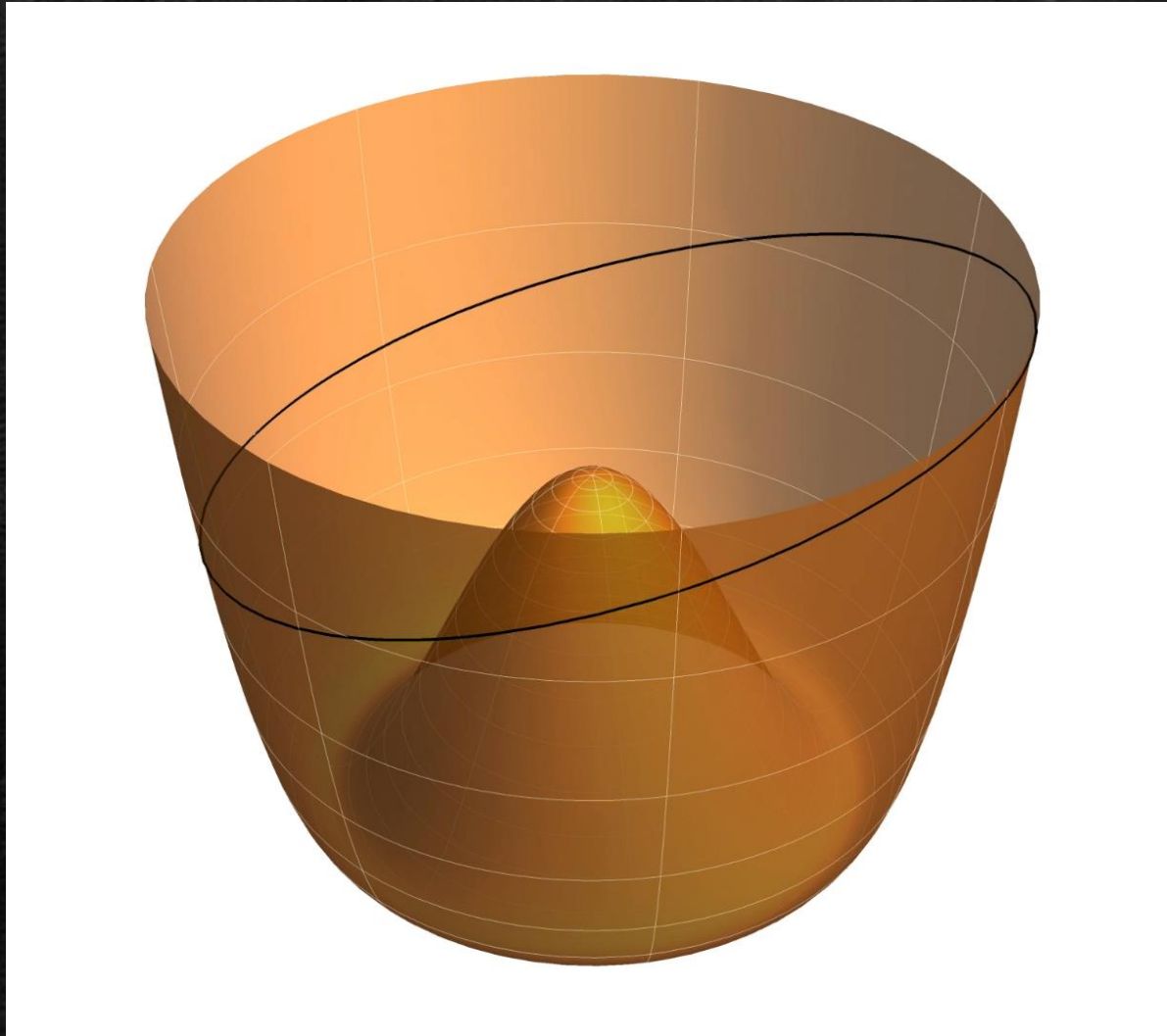
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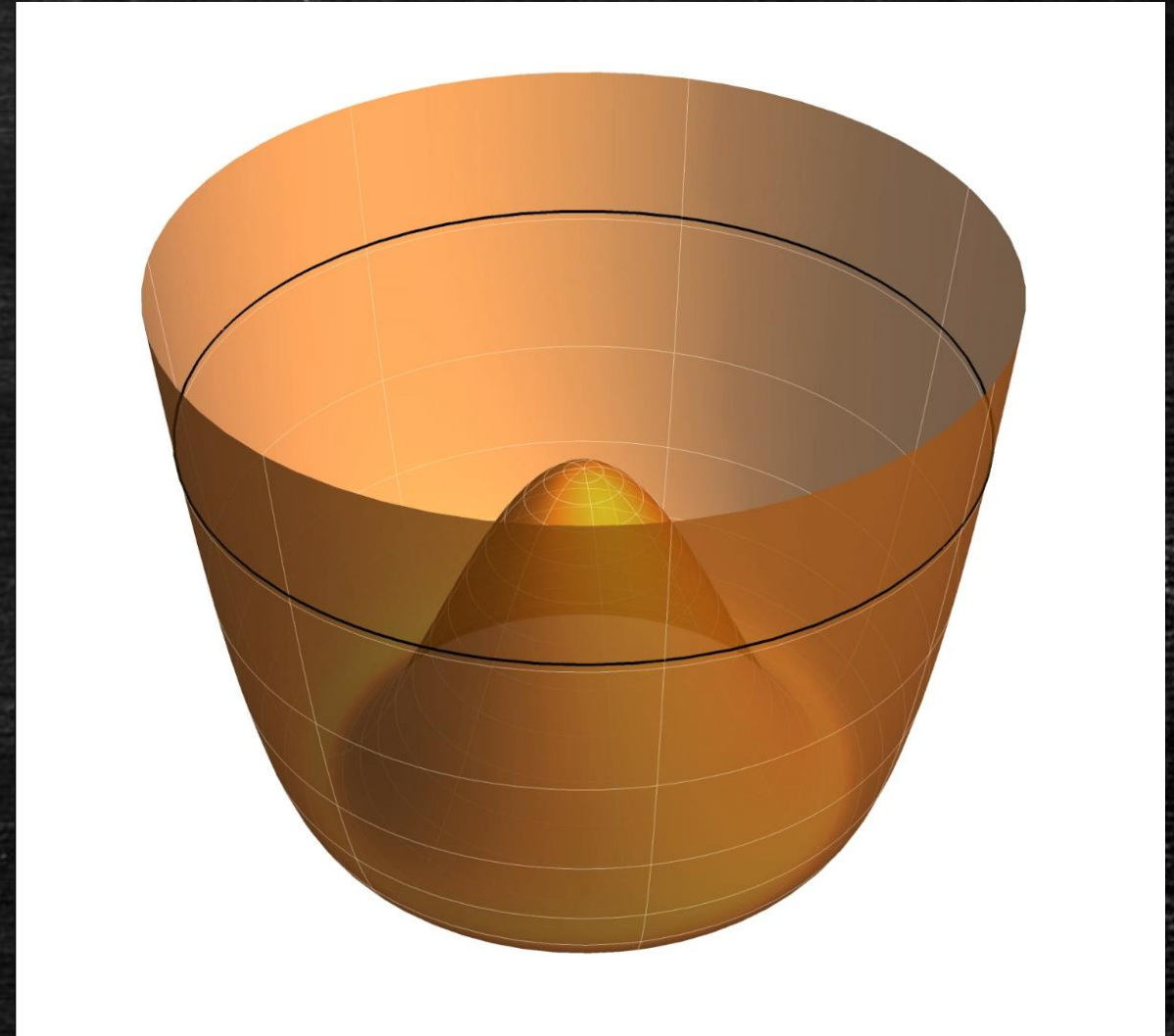
$$V_{\text{soft}} = m_P^2 |P|^2 + m_{\bar{P}}^2 |\bar{P}|^2$$



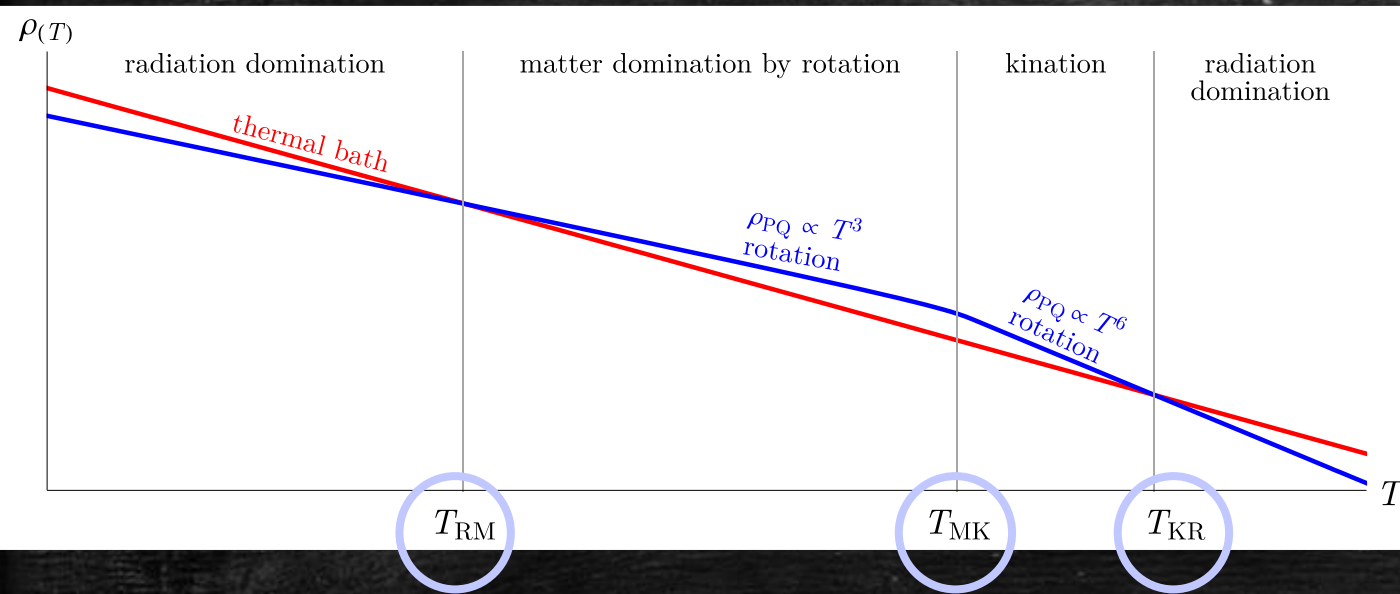
Thermalization



Redshift



Relevant Temperatures



$$T_{\text{RM}} = \frac{4}{3} m_S Y_\theta$$

$$\simeq 10^7 \text{ GeV} \left(\frac{m_S}{100 \text{ TeV}} \right) \left(\frac{Y_\theta}{100} \right)$$

$$T_{\text{MK}} = \left(\frac{45}{2\pi^2 g_*} \frac{m_S f_a^2}{Y_\theta} \right)^{\frac{1}{3}}$$

$$\simeq 3 \times 10^6 \text{ GeV} \left(\frac{m_S}{100 \text{ TeV}} \right)^{\frac{1}{3}} \left(\frac{f_a}{10^9 \text{ GeV}} \right)^{\frac{2}{3}}$$

$$T_{\text{KR}} = \frac{3\sqrt{15}}{2\sqrt{g_*}\pi} \frac{f_a}{Y_\theta}$$

$$\simeq 2 \times 10^6 \text{ GeV} \left(\frac{f_a}{10^9 \text{ GeV}} \right) \left(\frac{100}{Y_\theta} \right)$$

$$T_{\text{MK}}^3 = T_{\text{KR}}^2 T_{\text{RM}}$$

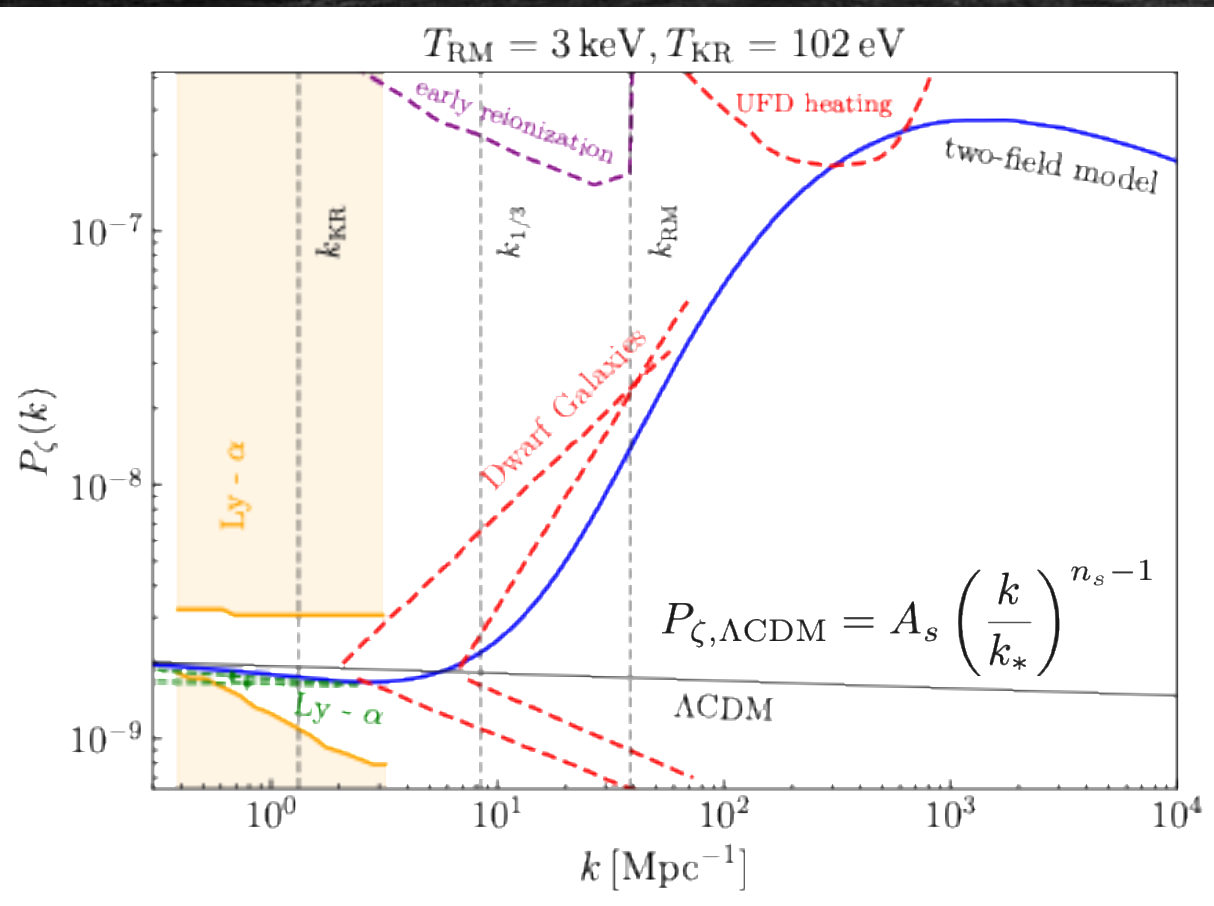
Axion Kination

Matter Power Spectrum

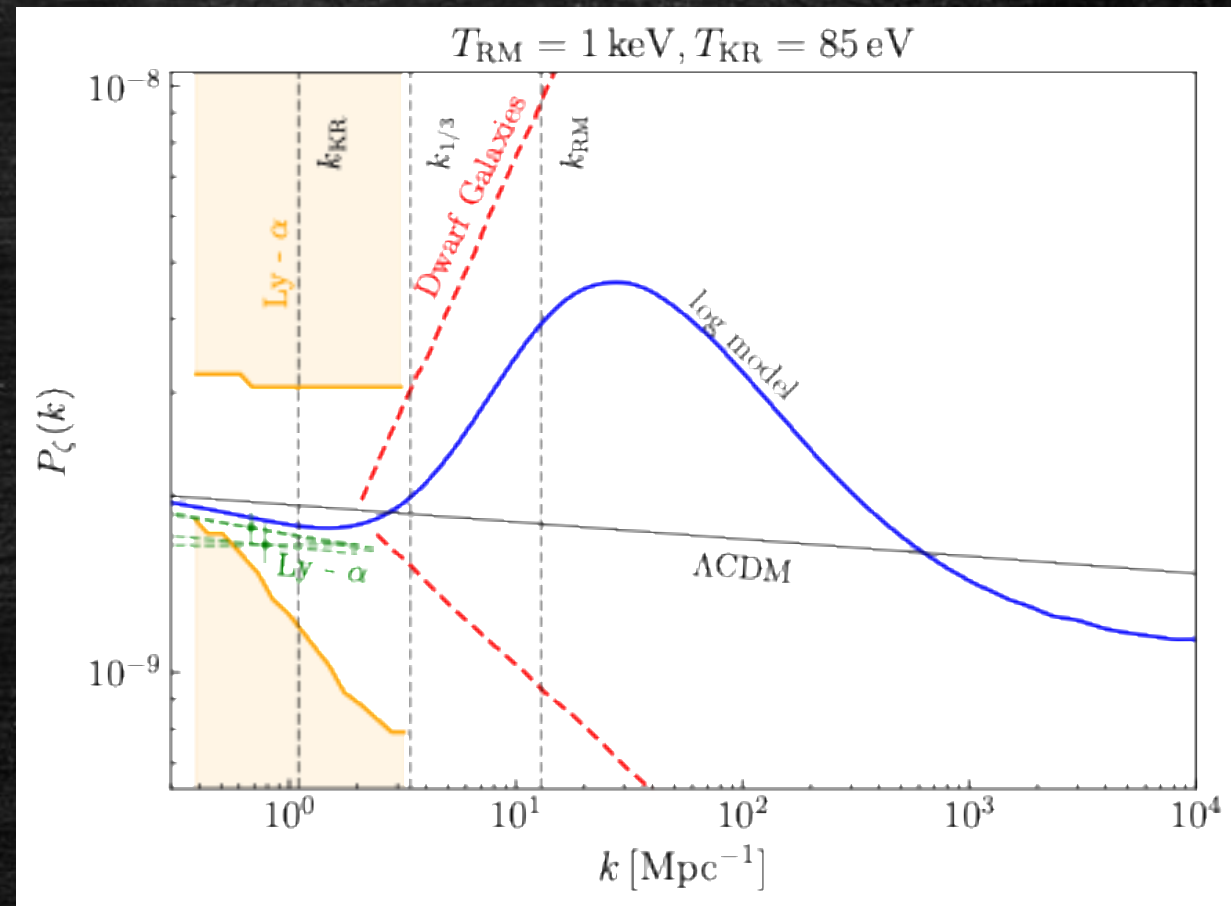
Perturbations

$$P_{\zeta,\text{eff,kin}} = \frac{P_{\text{kin}}(k)}{P_{\Lambda\text{CDM}}(k)} P_{\zeta,\Lambda\text{CDM}}$$

two-field model



log model

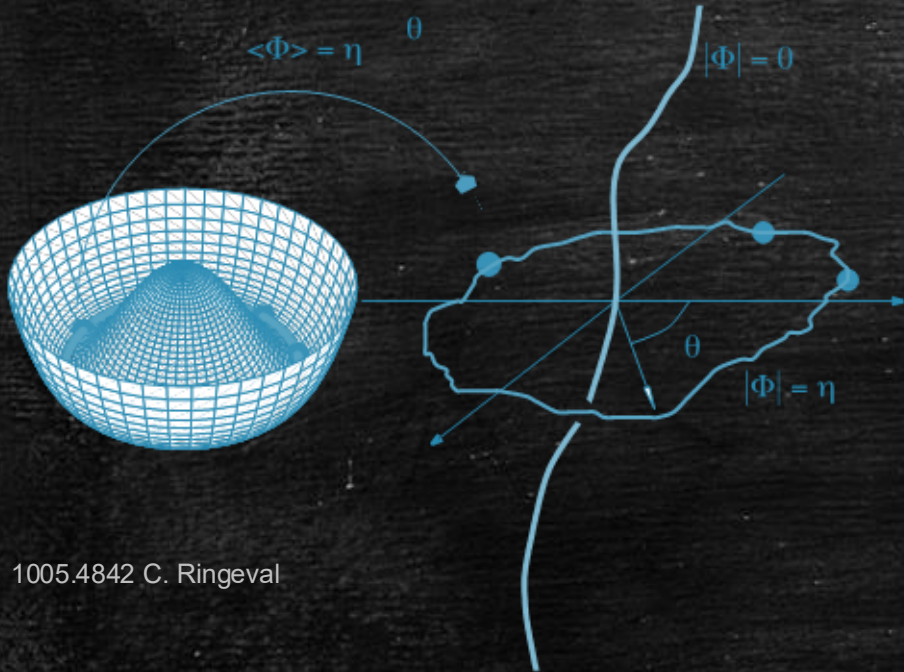


Axion Kination

Gravitational Waves

Gravitational Waves from Cosmic Strings

Gauge symmetry breaking



1005.4842 C. Ringeval

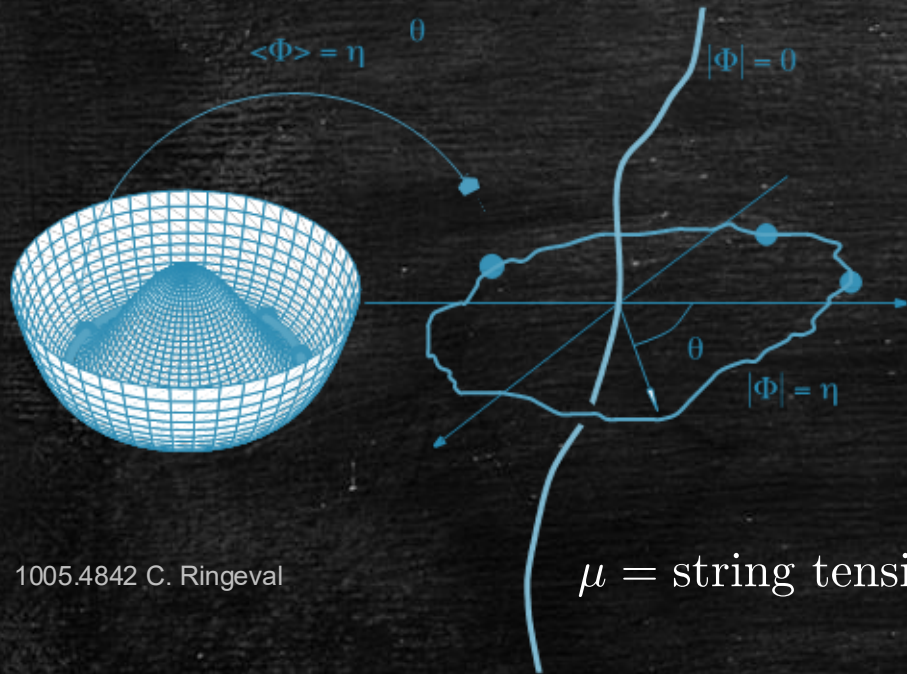


Daniel Dominguez/CERN

Energy emitted via GWs

Gravitational Waves from Cosmic Strings

Gauge symmetry breaking



1005.4842 C. Ringeval

μ = string tension

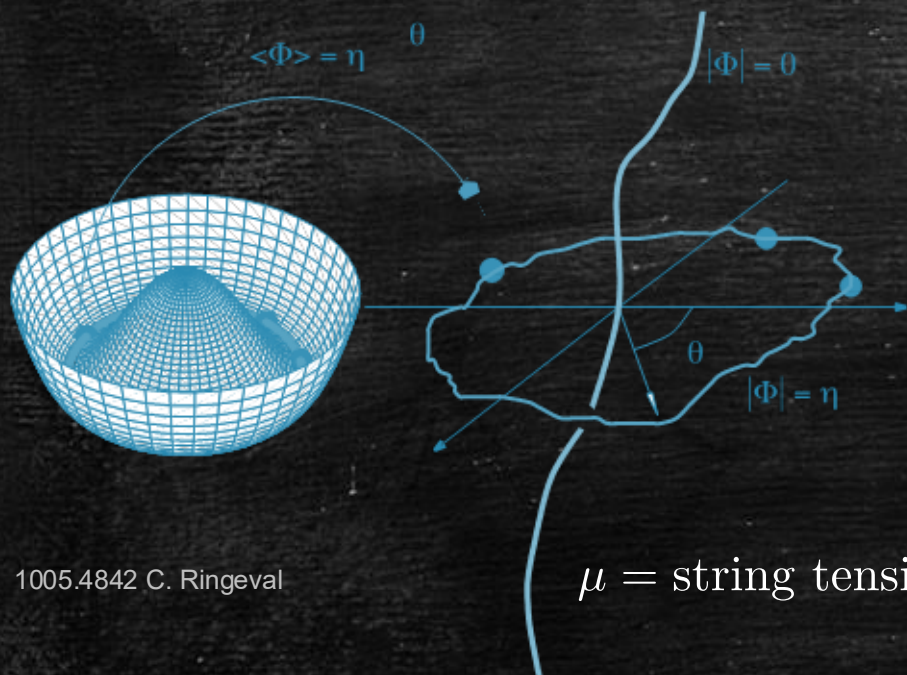
PRD (1985) T. Vachaspati and A. Vilenkin

$$\rho_{\text{loop}} = \left(\frac{\mu \times \text{length}}{\text{volume}} \right) = \mu \frac{t_{\text{form}}}{t_{\text{form}}^3} = \mu H_{\text{form}}^2.$$

$$t_{\text{decay}} \sim \frac{\overset{\text{energy/loop}}{\mu \alpha t_{\text{form}}}}{\underset{\text{power emitted}}{\Gamma G \mu^2}}$$

Gravitational Waves from Cosmic Strings

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$$\rho_{\text{loop}} = \left(\frac{\mu \times \text{length}}{\text{volume}} \right) = \mu \frac{t_{\text{form}}}{t_{\text{form}}^3} = \mu H_{\text{form}}^2.$$

$$\Omega_{\text{GW}} h^2 \sim \Omega_{r,0} \frac{\rho_{\text{loop}}(T_{\text{decay}})}{\rho_r(T_{\text{decay}})}$$

$$\sim \Omega_{r,0} \frac{\rho_{\text{loop}}(T_{\text{form}}) \left(\frac{T_{\text{decay}}}{T_{\text{form}}} \right)^3}{T_{\text{decay}}^4} \quad \text{for RD}$$

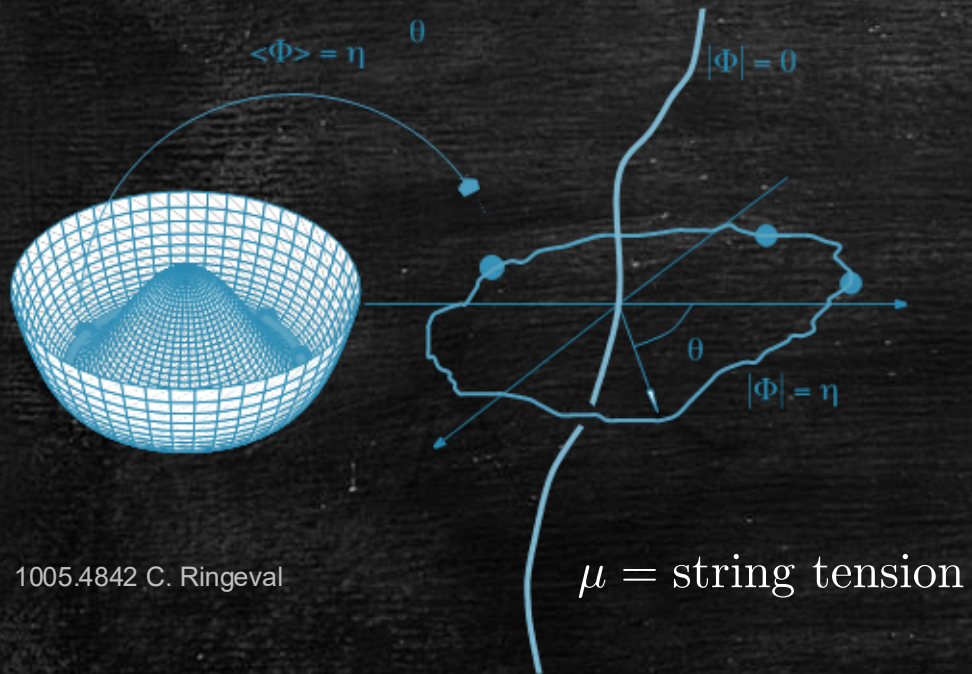
$$t_{\text{decay}} \sim \frac{\overset{\text{energy/loop}}{\mu \alpha t_{\text{form}}}}{\underset{\text{power emitted}}{\Gamma G \mu^2}}$$

$$\sim \Omega_{r,0} \frac{\mu H_{\text{form}}^2}{T_{\text{decay}} T_{\text{form}}^3} \sim \Omega_{r,0} \frac{\mu}{M_{\text{Pl}}^2} \frac{T_{\text{form}}}{T_{\text{decay}}}$$

1. Flat spectrum for radiation domination
2. An enhanced Hubble increases loop energy density.

Gravitational Waves from Cosmic Strings

Gauge symmetry breaking



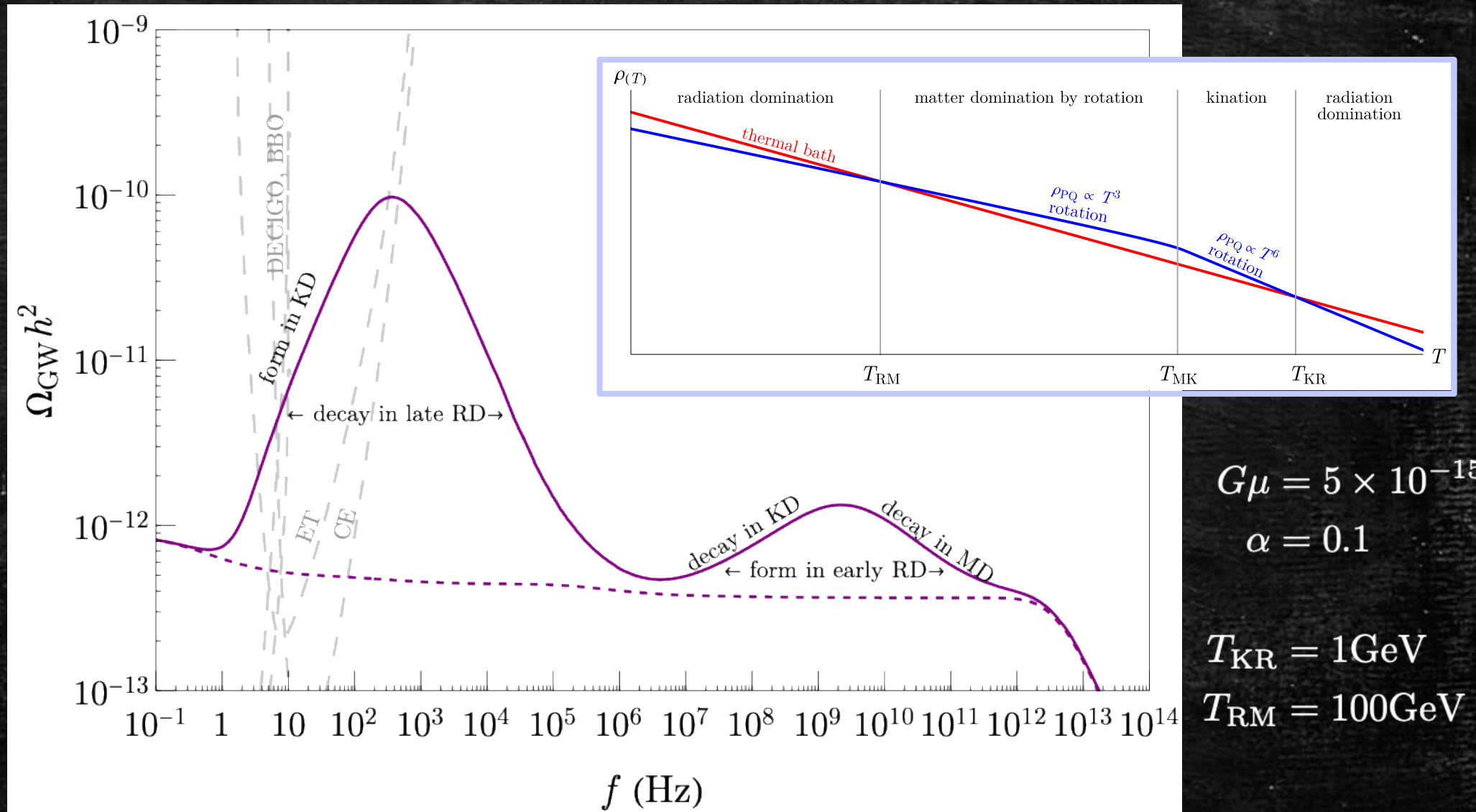
1005.4842 C. Ringeval

Loop decay era

Loop formation era

	Radiation	Matter	Kination
Radiation	f^0	f^{-1}	f^1
Matter	$f^{-1/2}$	f^{-1}	f^1
Kination	$f^{1/4}$	$f^{-1/2}$	f^1

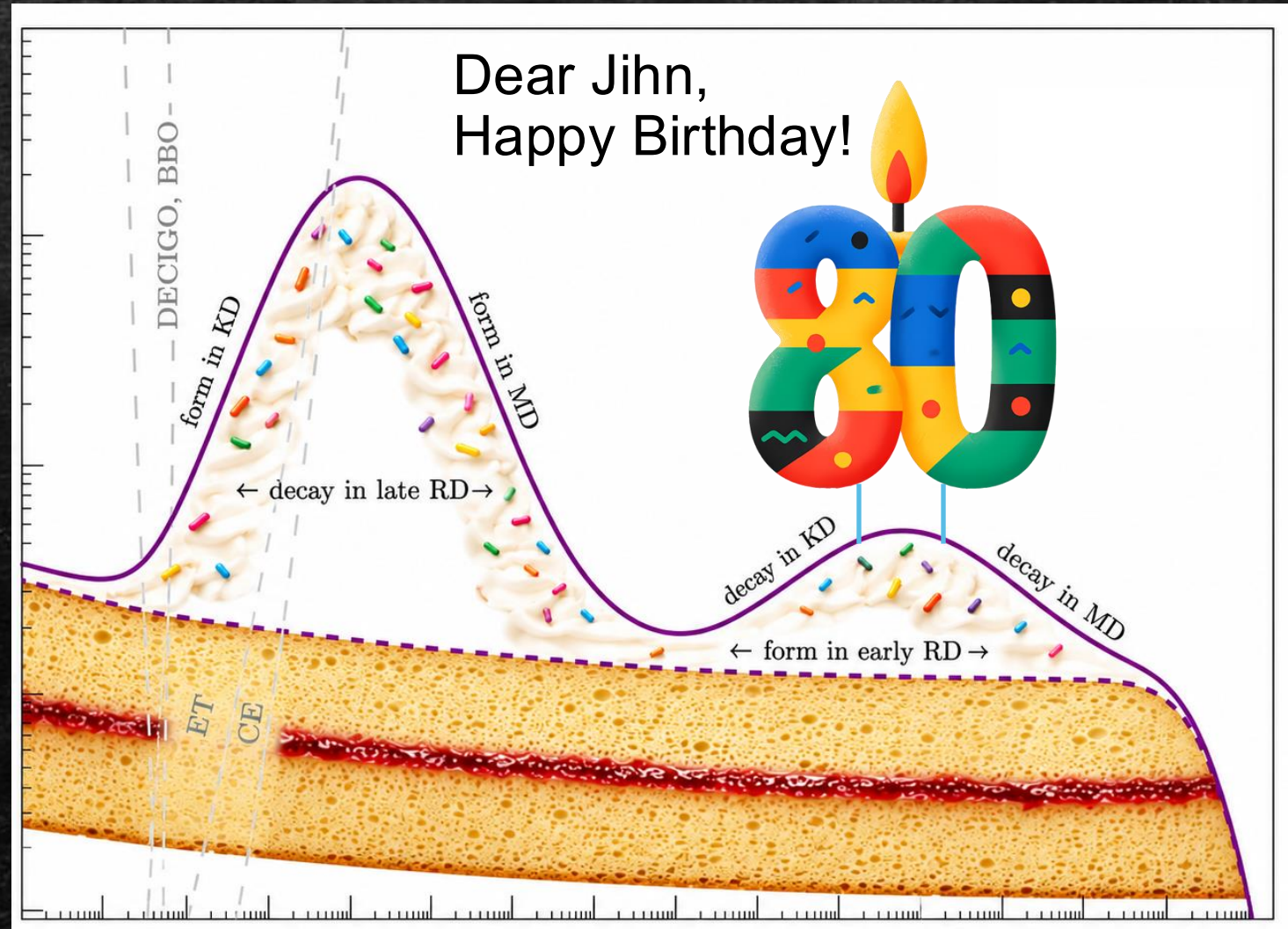
Gravitational Waves from Cosmic Strings



2108.09299 [JHEP 09 \(2022\) 116](#) [RC](#), D. Dunsy, N. Fernandez, A. Ghalsasi, L. Hall, K. Harigaya, J. Shelton

2111.01150 Y. Gouttenoire, G. Servant, P. Simakachorn

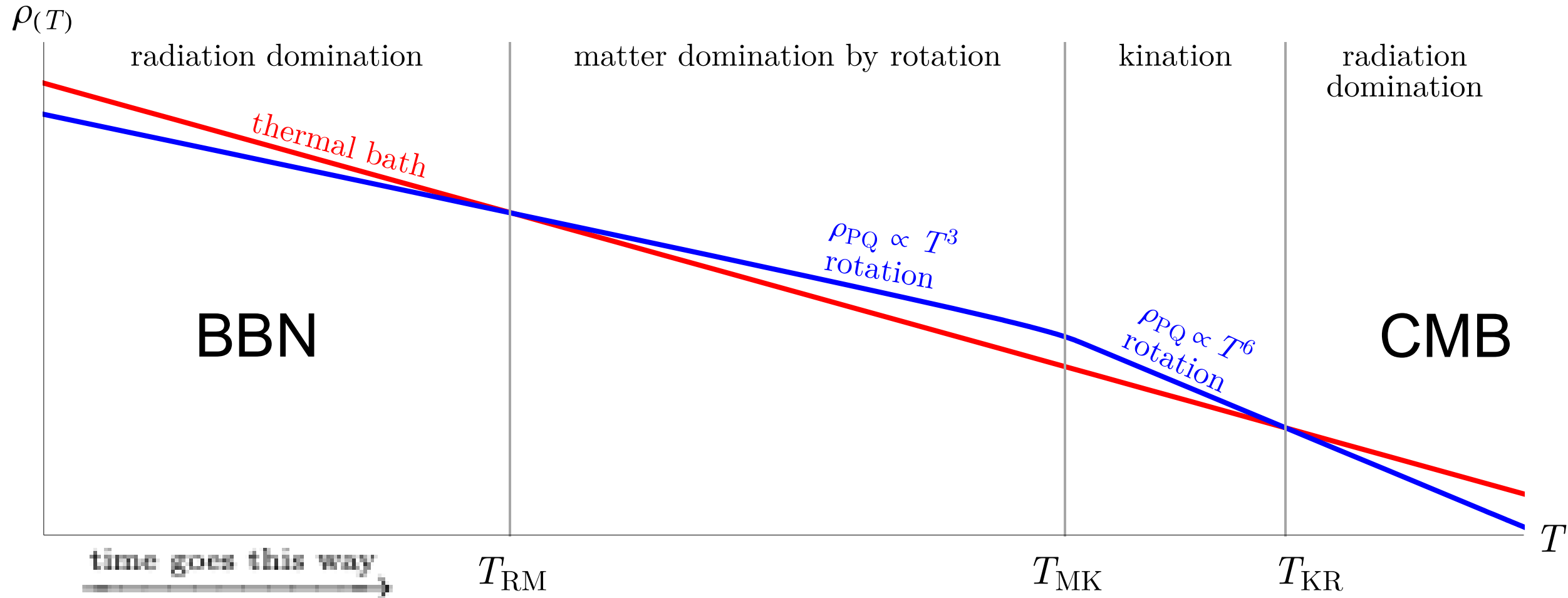
“Axion Rotation as the Icing on the Cosmic Cake”



Axion Kination

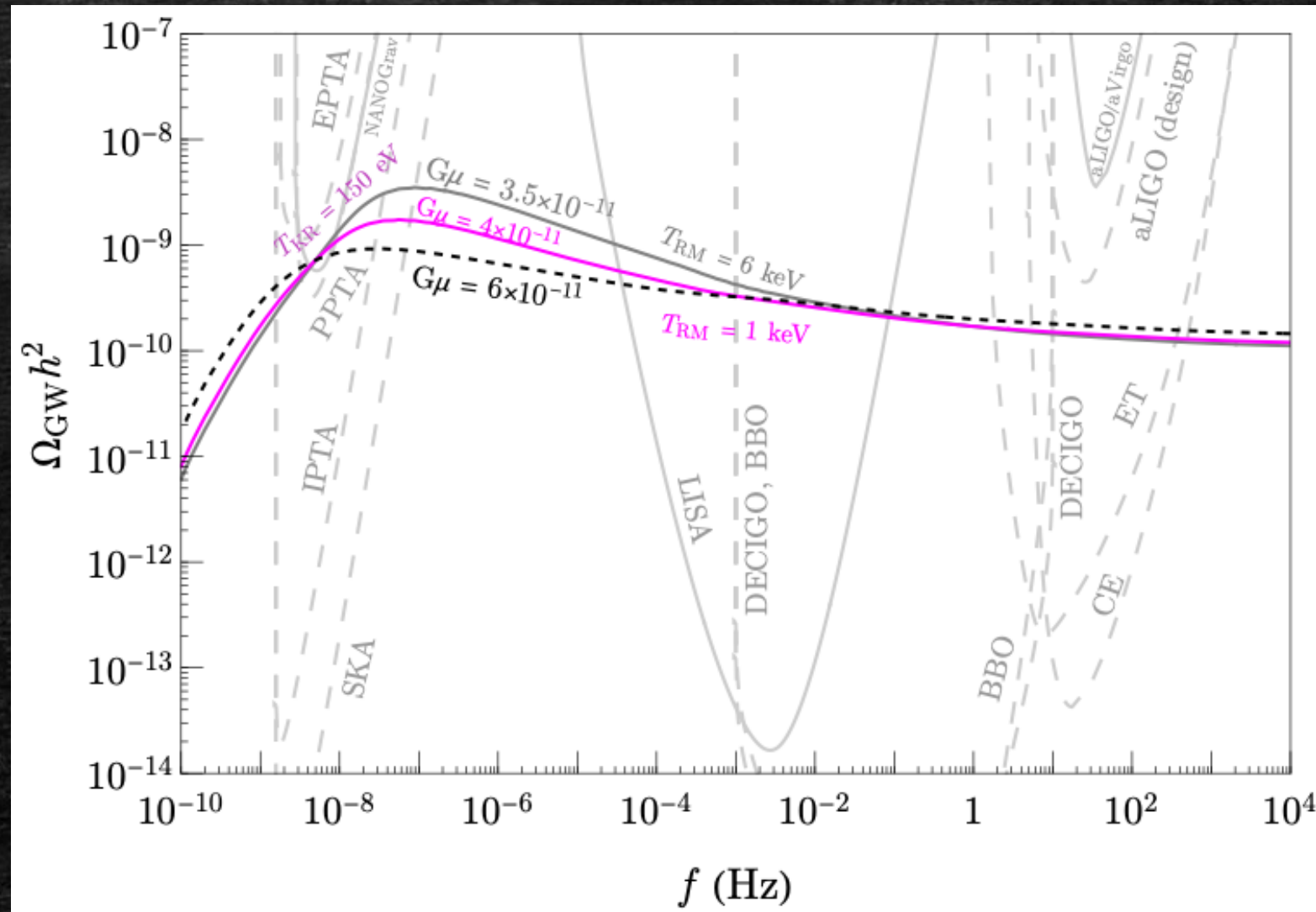
NanoHertz Gravitational Waves

Relevant Temperatures



Gravitational Waves from Cosmic Strings

Matter and kination domination between BBN and recombination



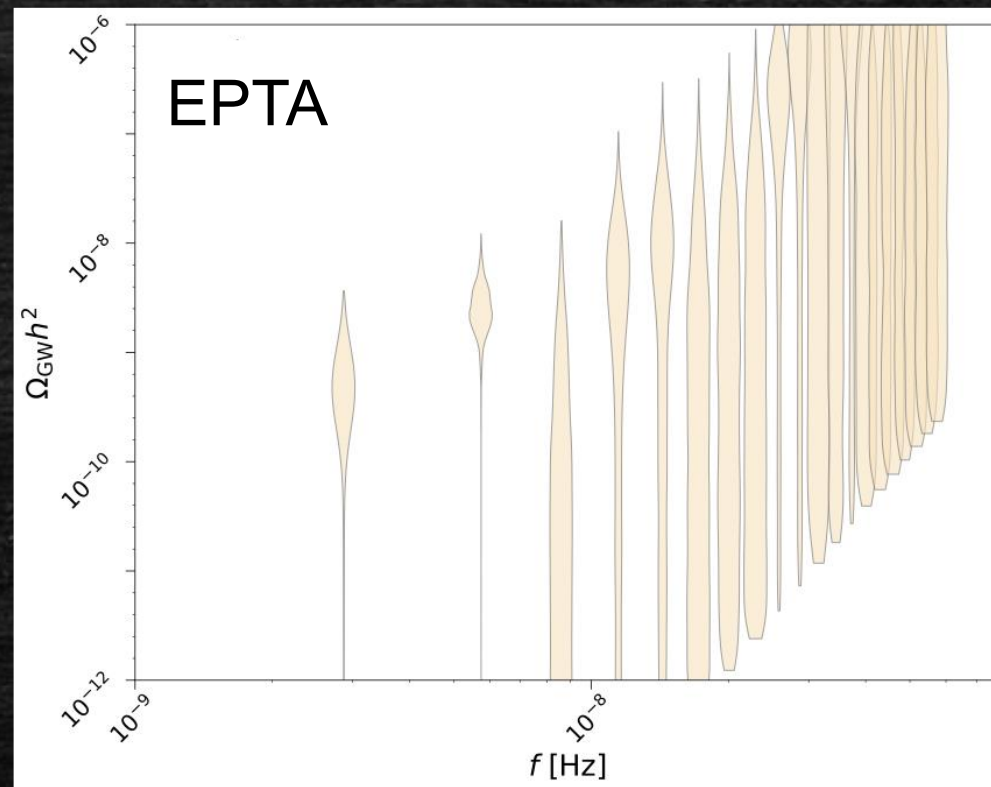
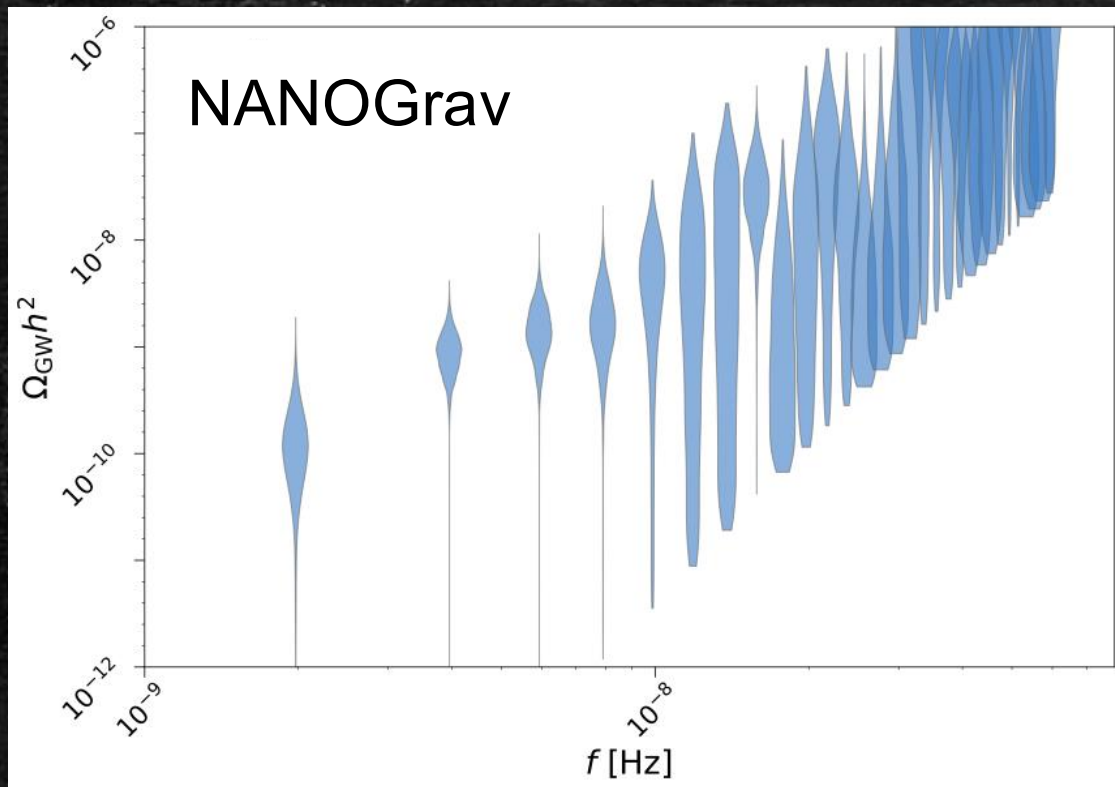
2108.09299 [JHEP 09 \(2022\) 116](#) [RC](#), D. Dunskey, N. Fernandez, A. Ghalsasi, L. Hall, K. Harigaya, J. Shelton

2111.01150 Y. Gouttenoire, G. Servant, P. Simakachorn

Pulsar Timing Arrays

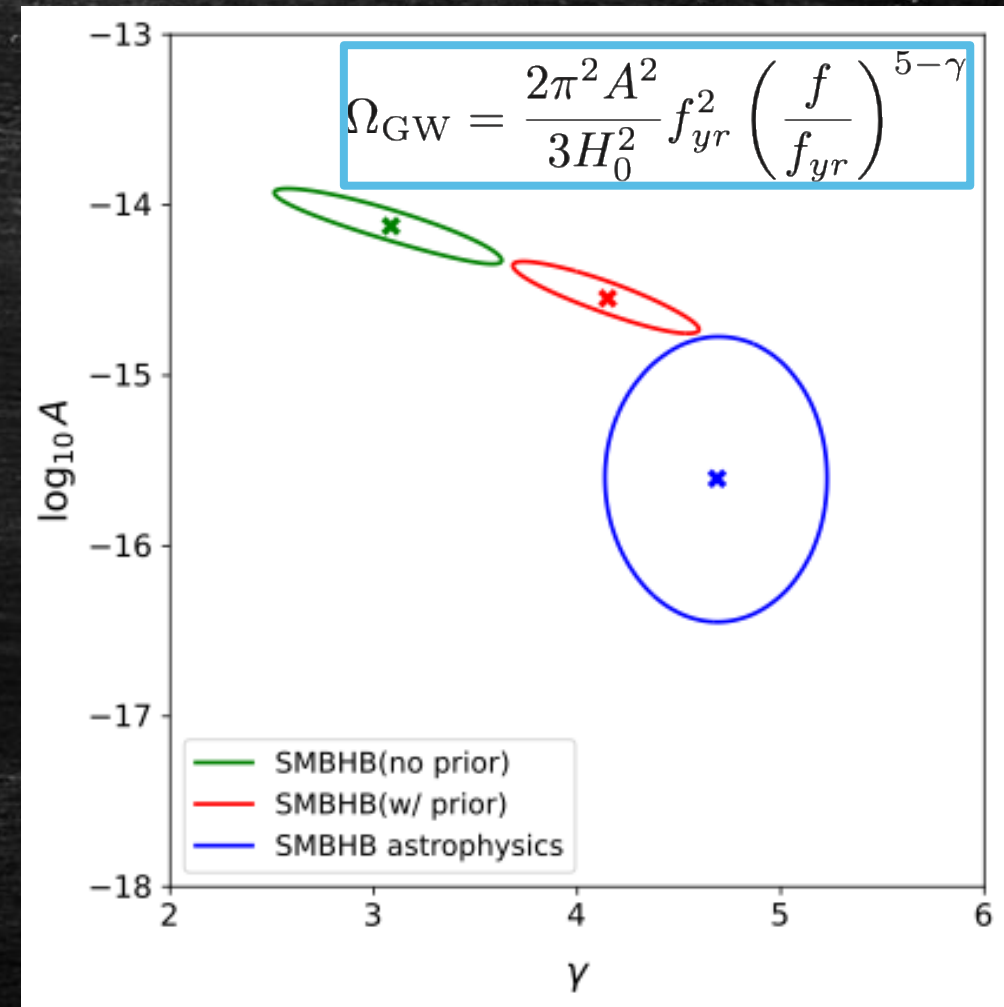
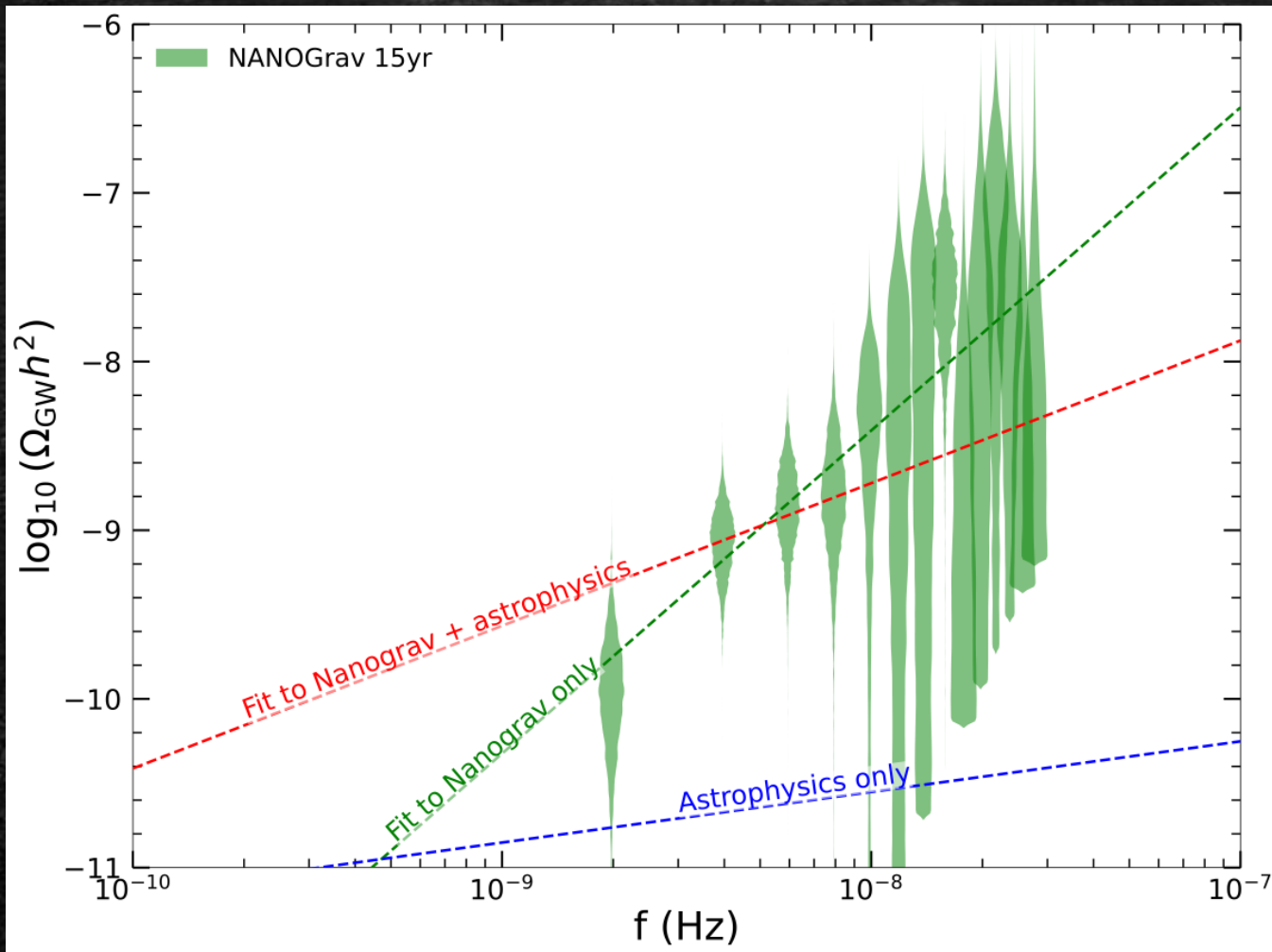
Potential detection of nHz gravitational waves by Pulsar Timing Arrays (PTA)

- NANOGrav 15-year data: evidence for Hellings–Downs correlations at the 3.2σ level 2407.20510
- EPTA 10-year DR2 New+ data: $\sim 3\sigma$ significance 2306.16214



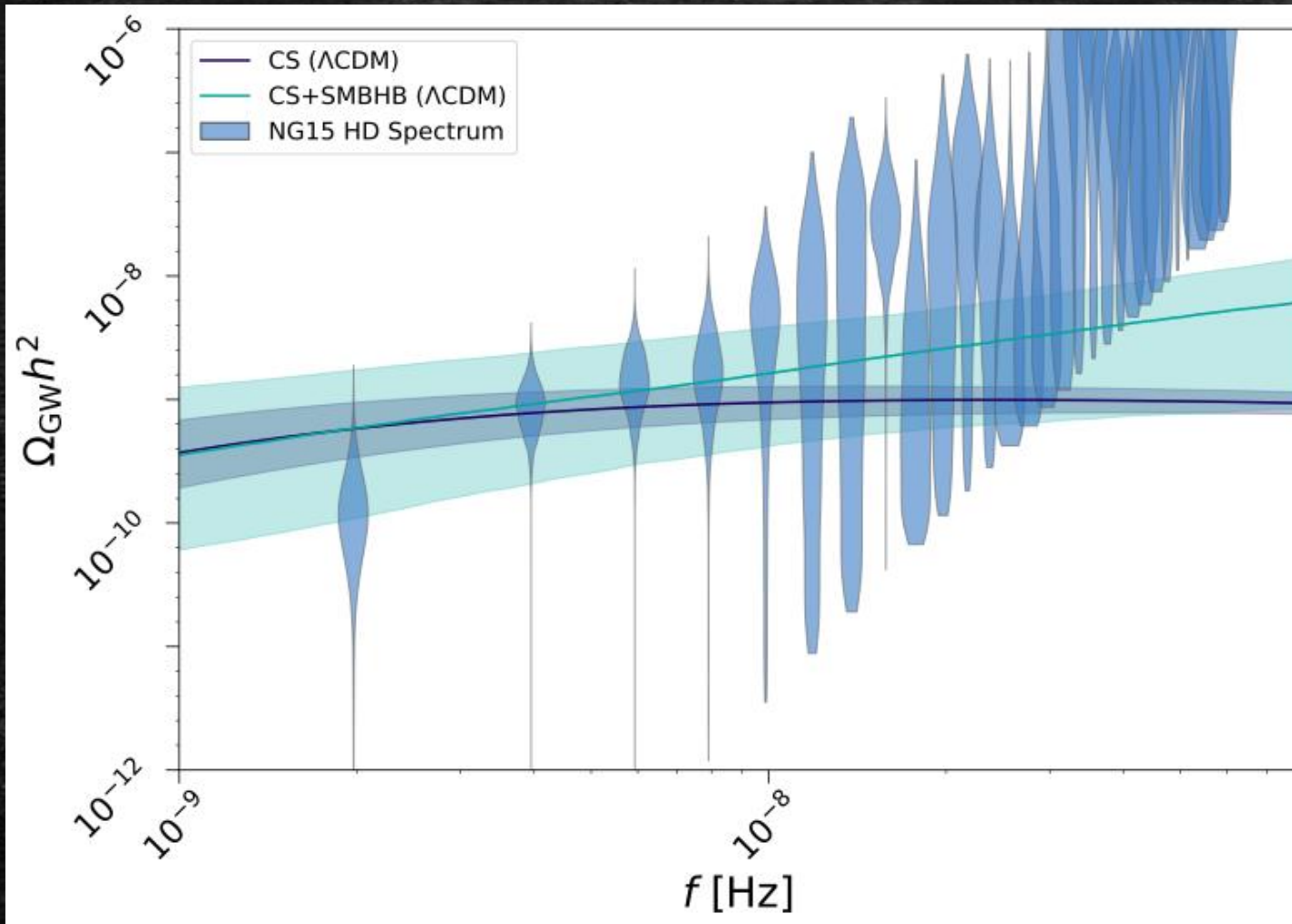
NanoHertz Gravitational Waves

Supermassive Black Hole Binaries (SMBHB)



NanoHertz Gravitational Waves

Cosmic Strings (CS) (+ SMBGB)



Baseline Model: **SMBHB**

Model	Bayes Factor
CS (Λ CDM)	0.16
CS+SMBHB (Λ CDM)	0.64

Jeffreys' scale of Bayes factor:

< 1 : Model disfavored

$1 - \sqrt{10}$: Negligibly small

$\sqrt{10} - 10$: Substantially strong

...

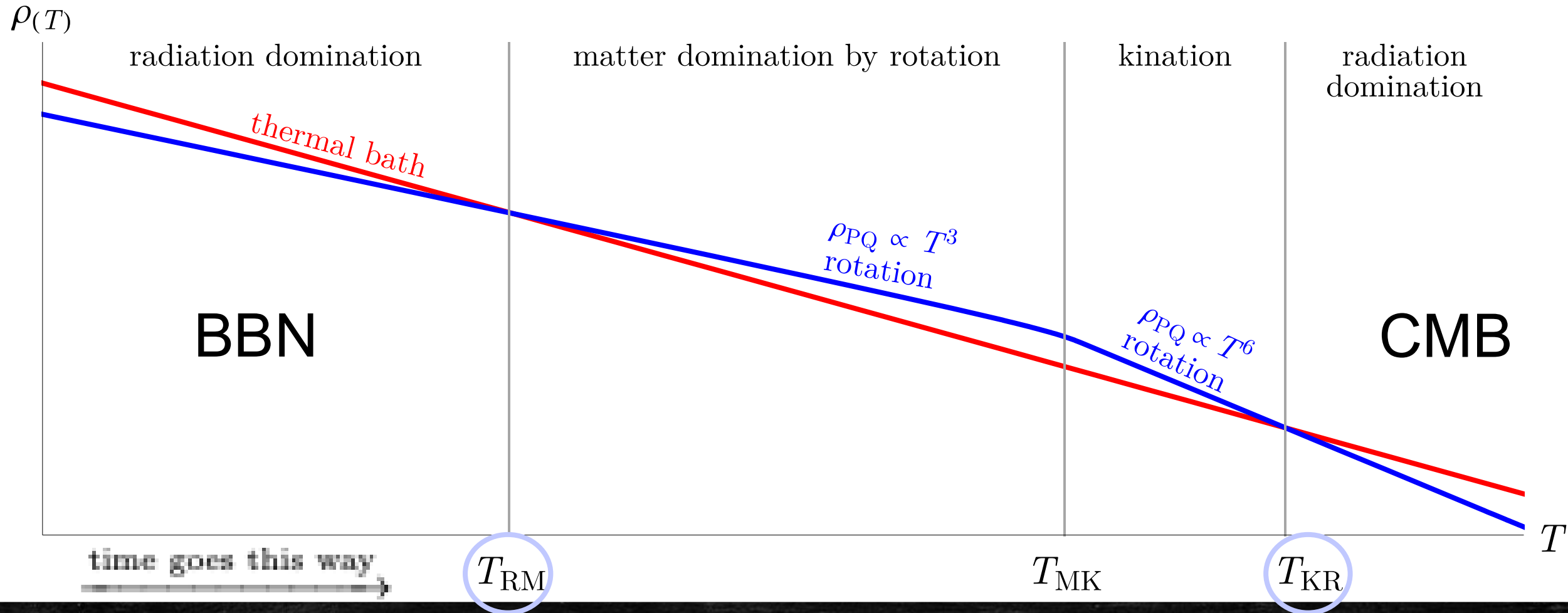


Grad student: **Taegyu Lee**



Grad student: **Nicolas Lam**

Relevant Temperatures

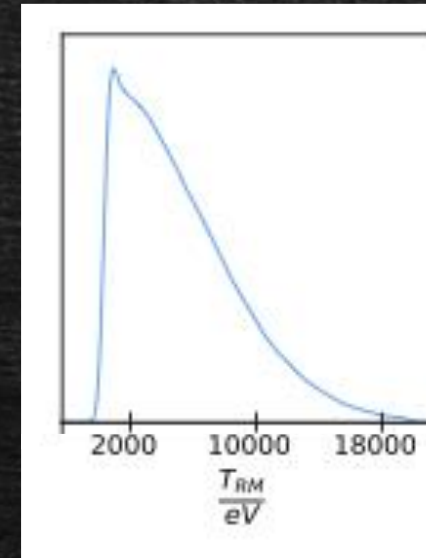
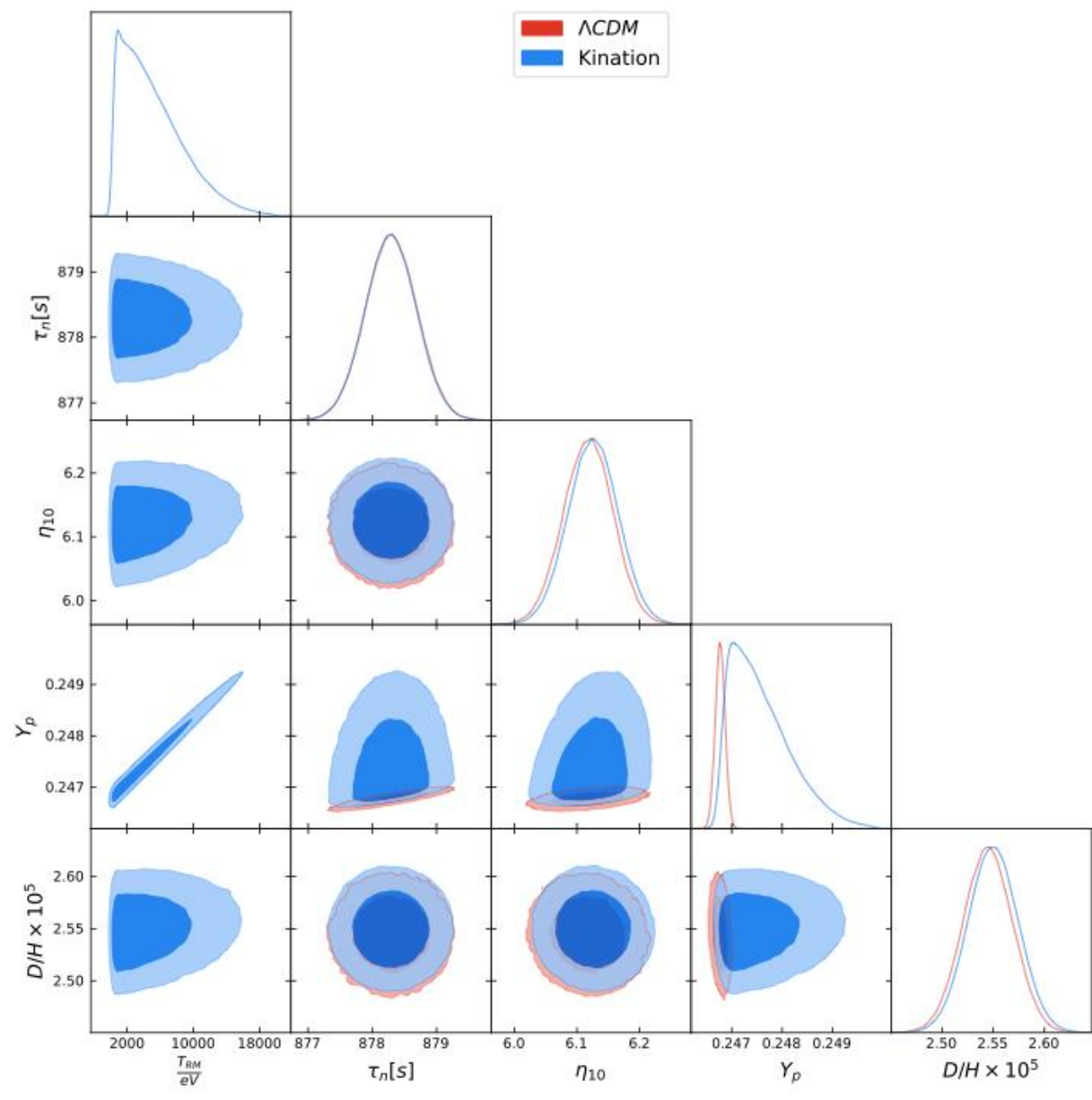


BBN

PRyMordial

2307.07061 A. Burns, T. Tait, and M. Valli

At 2σ , $T_{\text{RM}} < 12.6$ keV



Grad student: Taegyu Lee



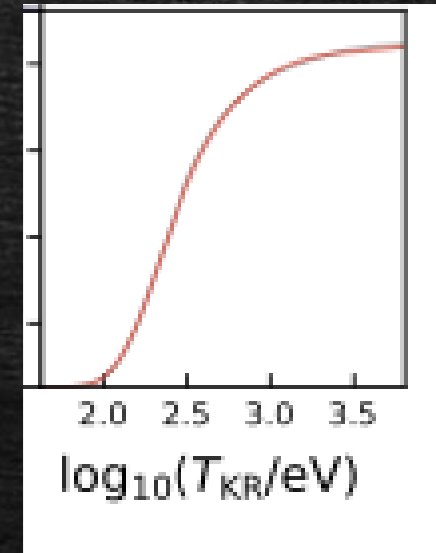
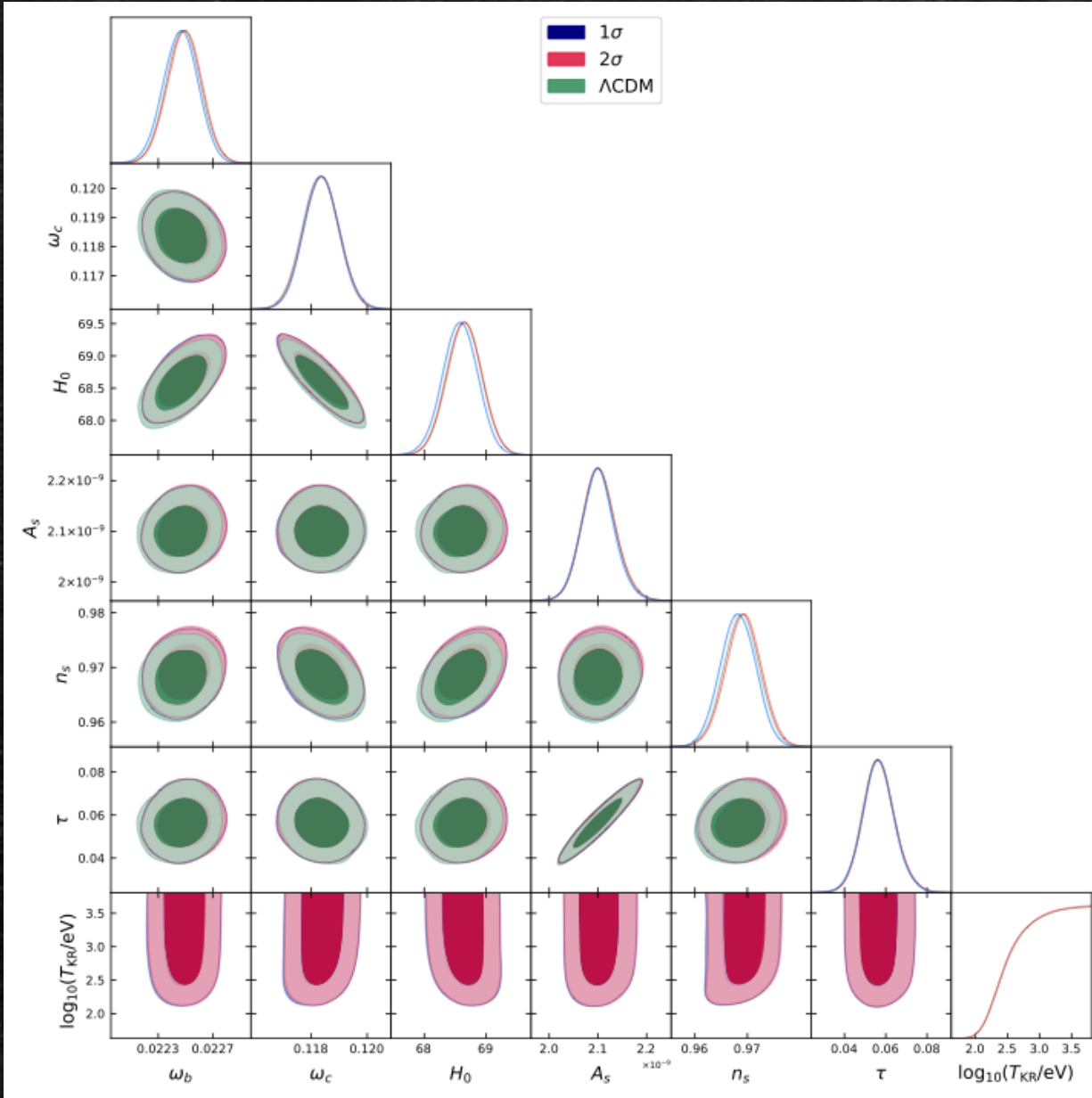
Grad student: Nicolas Lam

CMB

CLASS

1104.2933 B. Blas, J. Lesgourgues, and T. Tram

At 2σ , $T_{\text{KR}} > 237$ eV



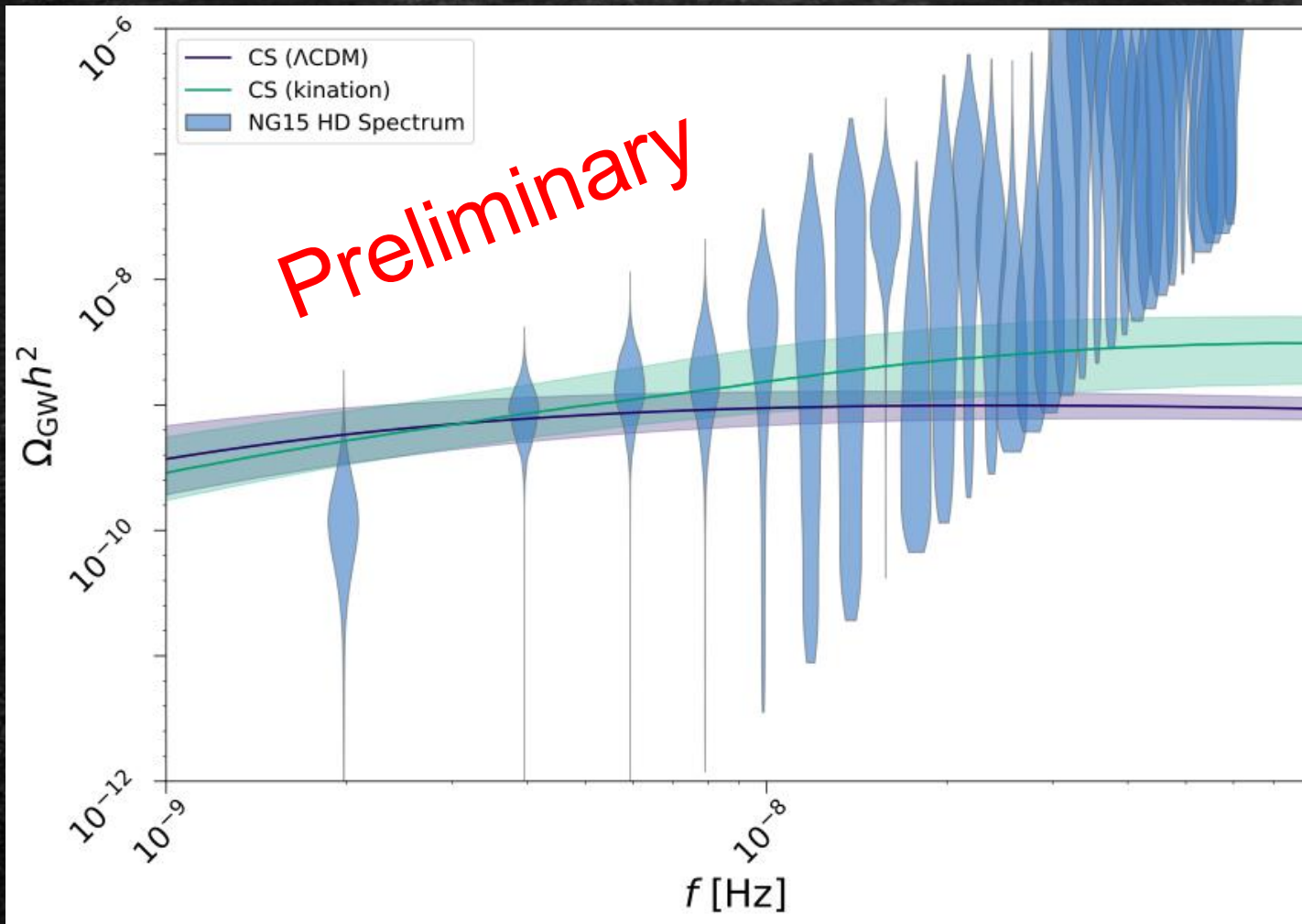
Grad student: Taegyu Lee



Grad student: Nicolas Lam

NanoHertz Gravitational Waves

Cosmic Strings (CS)



Baseline Model: SMBHB

Model	Bayes Factor
CS (Λ CDM)	0.16
CS+SMBHB (Λ CDM)	0.64
CS (kination)	0.60

Jeffreys' scale of Bayes factor:

< 1 : Model disfavored

$1 - \sqrt{10}$: Negligibly small

$\sqrt{10} - 10$: Substantially strong

...



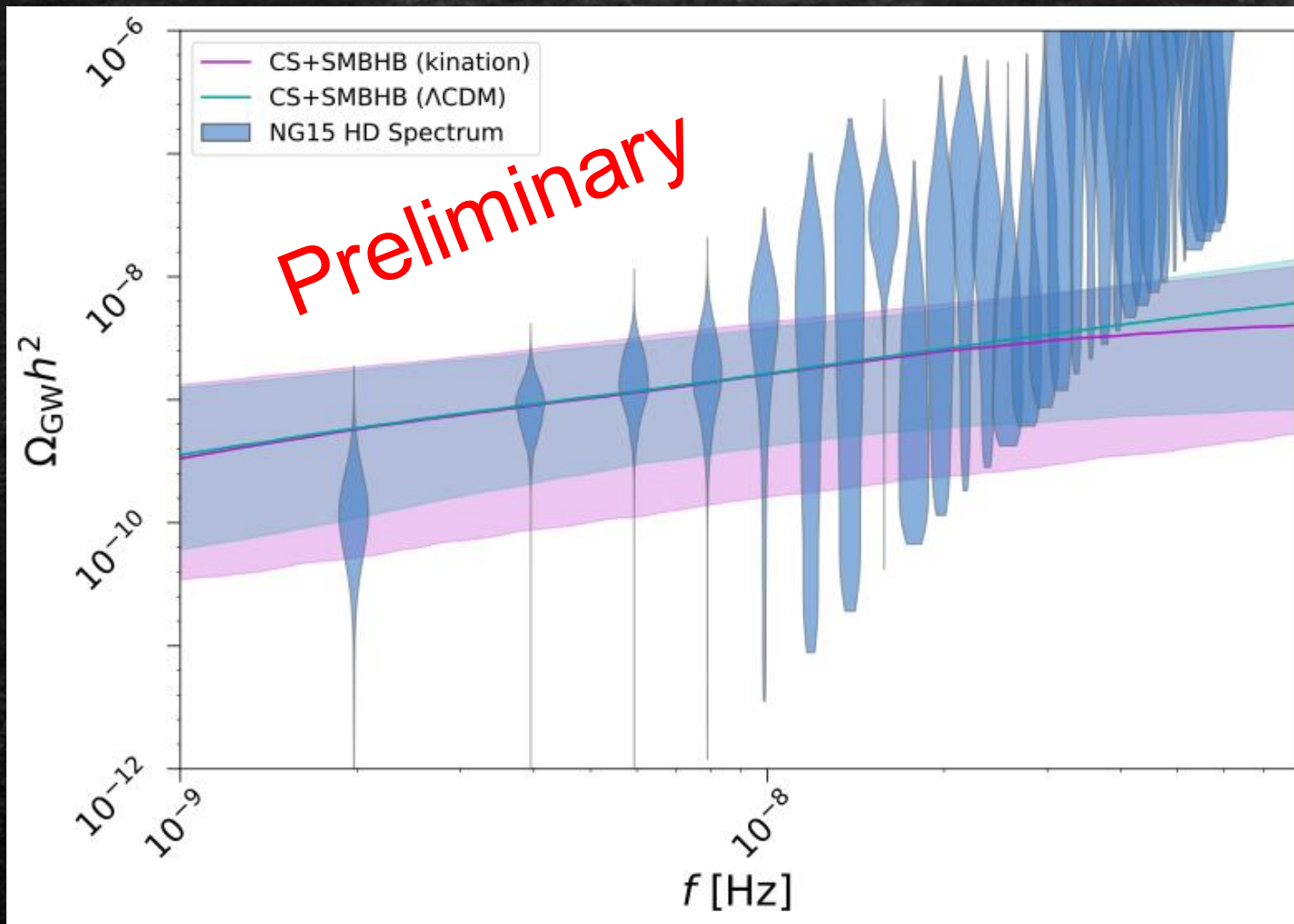
Grad student: Taegyu Lee



Grad student: Nicolas Lam

NanoHertz Gravitational Waves

CS + SMBHB



Baseline Model: SMBHB

Model	Bayes Factor
CS (Λ CDM)	0.16
CS+SMBHB (Λ CDM)	0.64
CS (kination)	0.60
CS+SMBHB (kination)	1.28

Jeffreys' scale of Bayes factor:

< 1 : Model disfavored

$1 - \sqrt{10}$: Negligibly small

$\sqrt{10} - 10$: Substantially strong

...



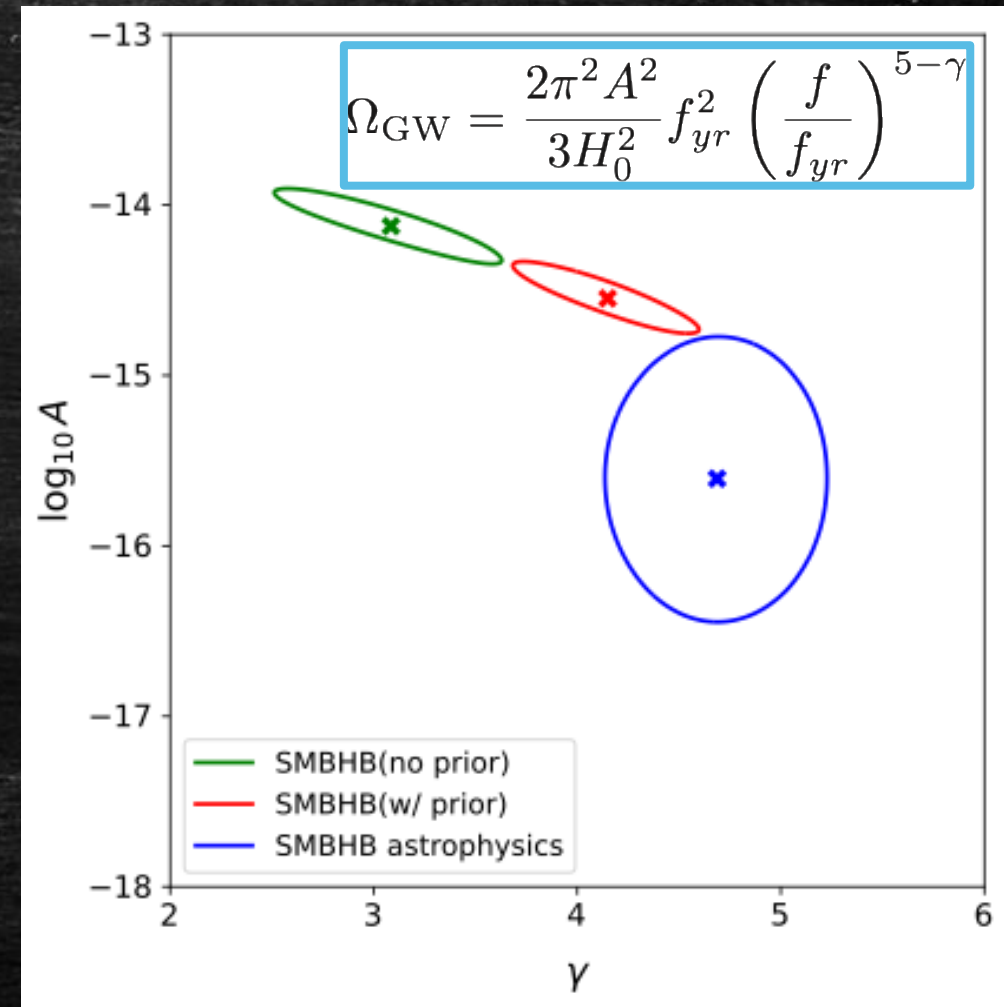
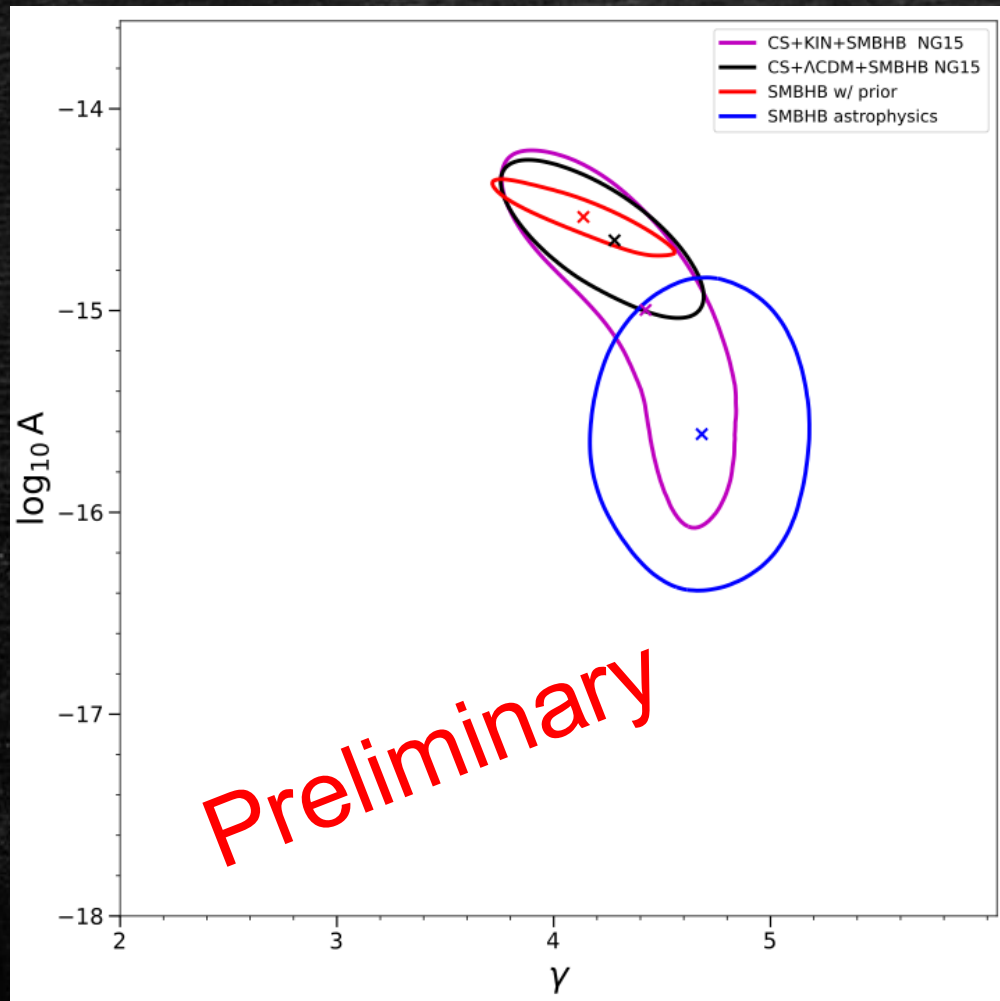
Grad student: Taegyu Lee



Grad student: Nicolas Lam

NanoHertz Gravitational Waves

Consistency with astrophysical simulations



NanoHertz Gravitational Waves

Thus far, the nHz gravitational wave signal is not yet statistically strong enough to distinguish between Λ CDM and kination cosmology.

We will need more data from

- **IPTA**: Continued data integration across NANOGrav, EPTA, PPTA, CPTA, and InPTA to form a unified, ultra-sensitive global.
- **SKAO** (Square Kilometre Array): Will dramatically increase the number of precisely timed millisecond pulsars, lowering the noise floor and allowing the detection of tens of individual supermassive black hole binaries.
- **DSA-2000**: A large radio radio-survey instrument in the United States that will contribute high-cadence timing and help refine gravitational wave sky-mapping and diffractive lensing measurements

Gravitational Waves from Inflation

The origin is the quantum fluctuations during inflation.

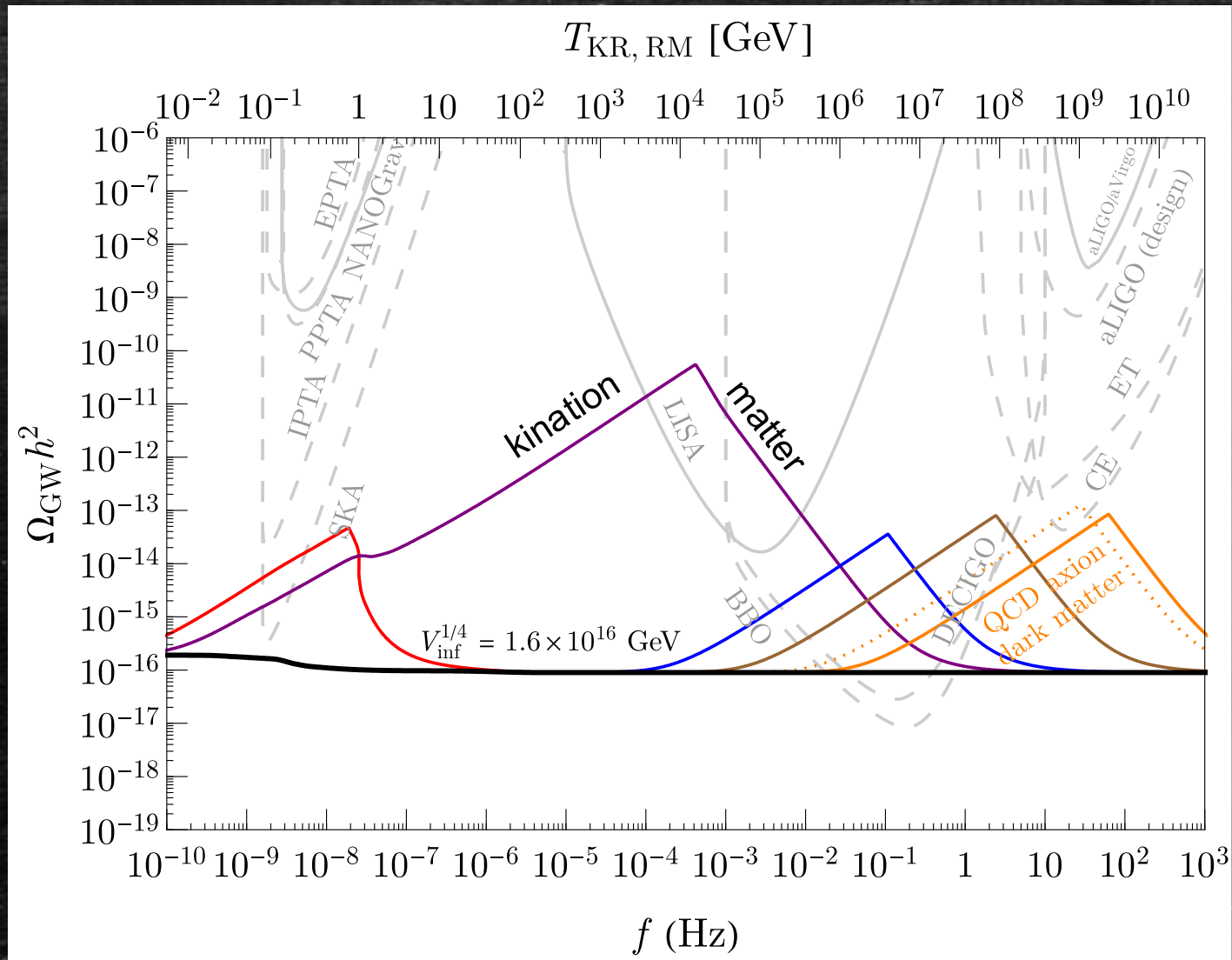
The horizon crossing, $k = H$, determines the onset of mode evolutions.

$$\Omega_{\text{GW}} h^2 = \Omega_{r,0} h^2 \frac{1}{\rho_R(T_{\text{hc}})} \frac{k^2}{64\pi G} \mathcal{P}_T(k) \quad \mathcal{P}_T(k) = \frac{2H_I^2}{\pi^2 M_{\text{Pl}}^2}$$

$$k = H(T_{\text{hc}})$$

$$\Omega_{\text{GW}} h^2 \simeq 1.4 \times 10^{-17} \left(\frac{V_{\text{inf}}^{1/4}}{10^{16} \text{ GeV}} \right)^4 \left(\frac{g_{*,\text{SM}}}{g_*(T_{\text{hc}})} \right)^{\frac{1}{3}} \begin{cases} 1 & \text{RD : } f_{\text{RM}} < f \\ \left(\frac{f_{\text{RM}}}{f} \right)^2 & \text{MD : } f_{\text{MK}} < f < f_{\text{RM}} \\ \frac{f}{f_{\text{KR}}} & \text{KD : } f_{\text{KR}} < f < f_{\text{MK}} \\ 1 & \text{RD : } f < f_{\text{KR}} \end{cases}$$

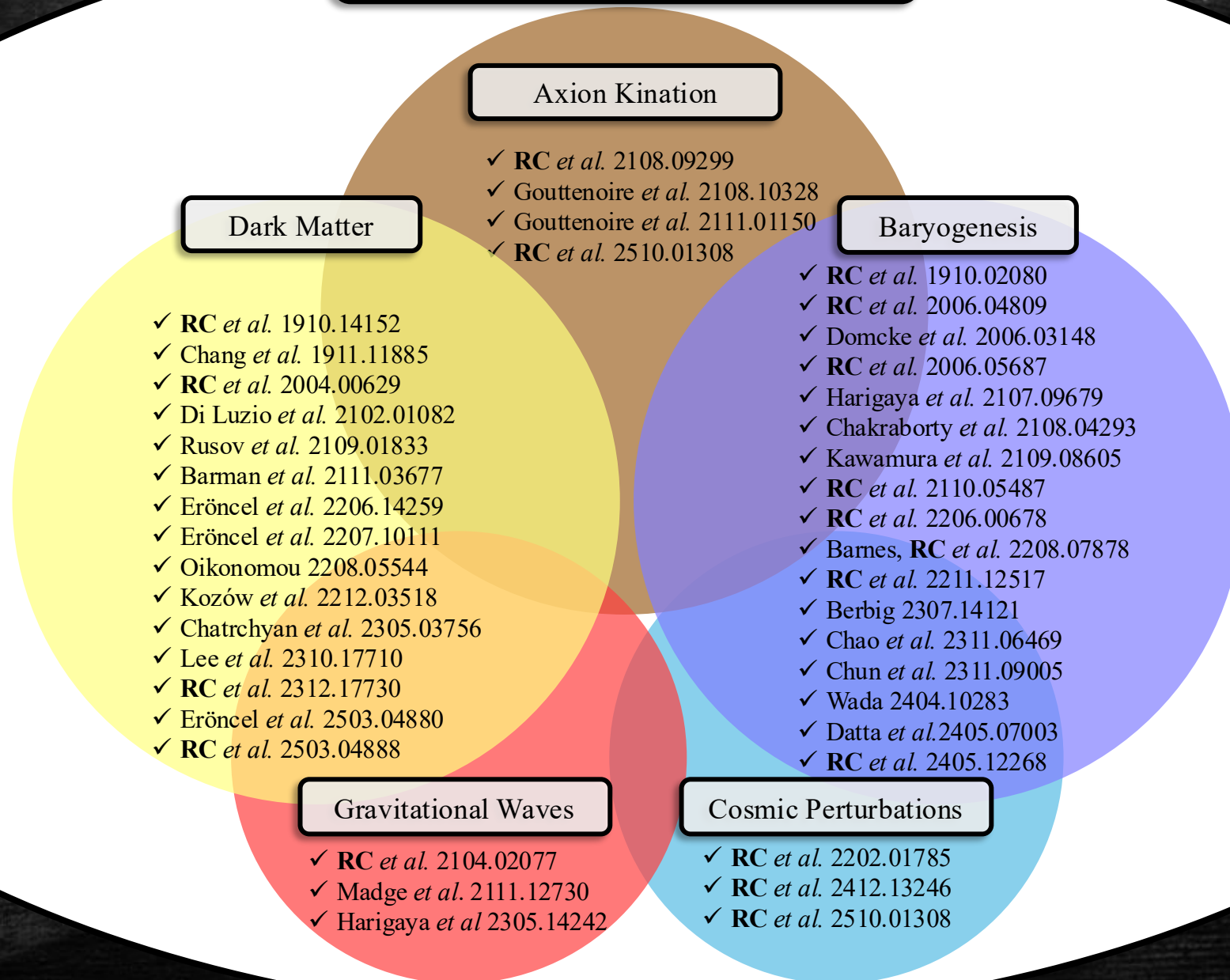
Smoking Gun: Triangular Peak in Gravitational Wave Spectra



2108.09299 [JHEP 09 \(2022\) 116](#) [RC](#), D. Dunsky, N. Fernandez, A. Ghalsasi, L. Hall, K. Harigaya, J. Shelton

2108.10328, 2111.01150 Y. Gouttenoire, G. Servant, P. Simakachorn

Axion Rotations



Conclusions

- ✓ **New axion dynamics** gives rise to interesting cosmological evolution involving matter and kination domination.
- ✓ This enhances Hubble expansion rate and predicts
 - ✓ **enhanced matter power spectrum**
 - ✓ **enhanced gravitational wave spectra**
- ✓ The same dynamics allows the QCD axion to simultaneously
 - ✓ Strong CP problem
 - ✓ dark matter abundance
 - ✓ baryon asymmetry
- ✓ Other possible signatures include
 - ✓ gravitational lensing of axion mini-clusters
 - ✓ warm axion dark matter
- ✓ New model building opportunities
 - ✓ **other open questions** across disciplines

