

Lecture plan: IBS summer school

Lecturer: Indrakshi Raychowdhury

IR Lecture 1: Why quantum computation for quantum field theory? Hamiltonian lattice gauge theory from first principles

Motivation: what quantum computers are meant to solve here. Continuum Yang–Mills theory: conventions, Canonical derivation of the Yang–Mills Hamiltonian, Spatial lattice variables. The Kogut–Susskind Hamiltonian, Plaquette term from the continuum magnetic field, Staggered fermions in Hamiltonian lattice gauge theory, Lattice Gauss law, Introduce Schwinger model as an example of each.

Lecture 2: by Jesse (Schwinger model, details, algorithm)

Lecture 3: by IR

IR Lecture 2: From $U(1)$ Schwinger model to $SU(2)$ prepotentials, and the first appearance of loop–string–hadron variables.

Why $SU(2)$ is different, Schwinger bosons for $SU(2)$, Prepotentials on a link, Local singlets from prepotentials, The one-dimensional $SU(2)$ LSH basis, Derivation of the Abelian link constraint, First form of the $SU(2)$ LSH Hamiltonian.

Lecture 4: by Jesse (algorithm for $SU(2)$ LSH)

Lecture 5: by IR

IR Lecture 3: $SU(2)$ LSH

$SU(2)$ LSH operator algebra, 1+1 D to 2+1 dimension, generalize in higher dimensions, introduction to $SU(3)$ LSH.

IR Lecture 4: $SU(2)$ LSH implementation

LSH dynamics, ED results, motivation for tensor network calculations, TN scope and results, limitation of TN, Quantum simulation: first results with approximation; validation of approximations, hardware results, benchmarking (students will reproduce these in one tutorial).

Tutorial Day 1: JW mapping, Derivation of purely fermionic version of Schwinger model, generalizing that for $SU(2)$

Tutorial day 4: <https://quantum.cloud.ibm.com/docs/en/tutorials/loop-string-hadron-dynamics>