

The Search for Light Dark Matter

Tanner Trickle

August 25th, 2026

5th Workshop on
Symmetry and
Structure of the Universe

SSU 2026 BUSAN



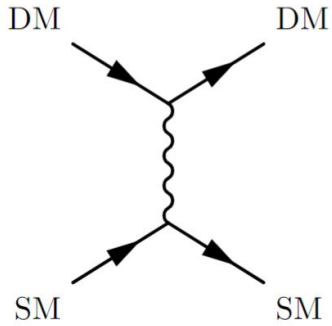
Outline

I. Current Status of Direct Detection

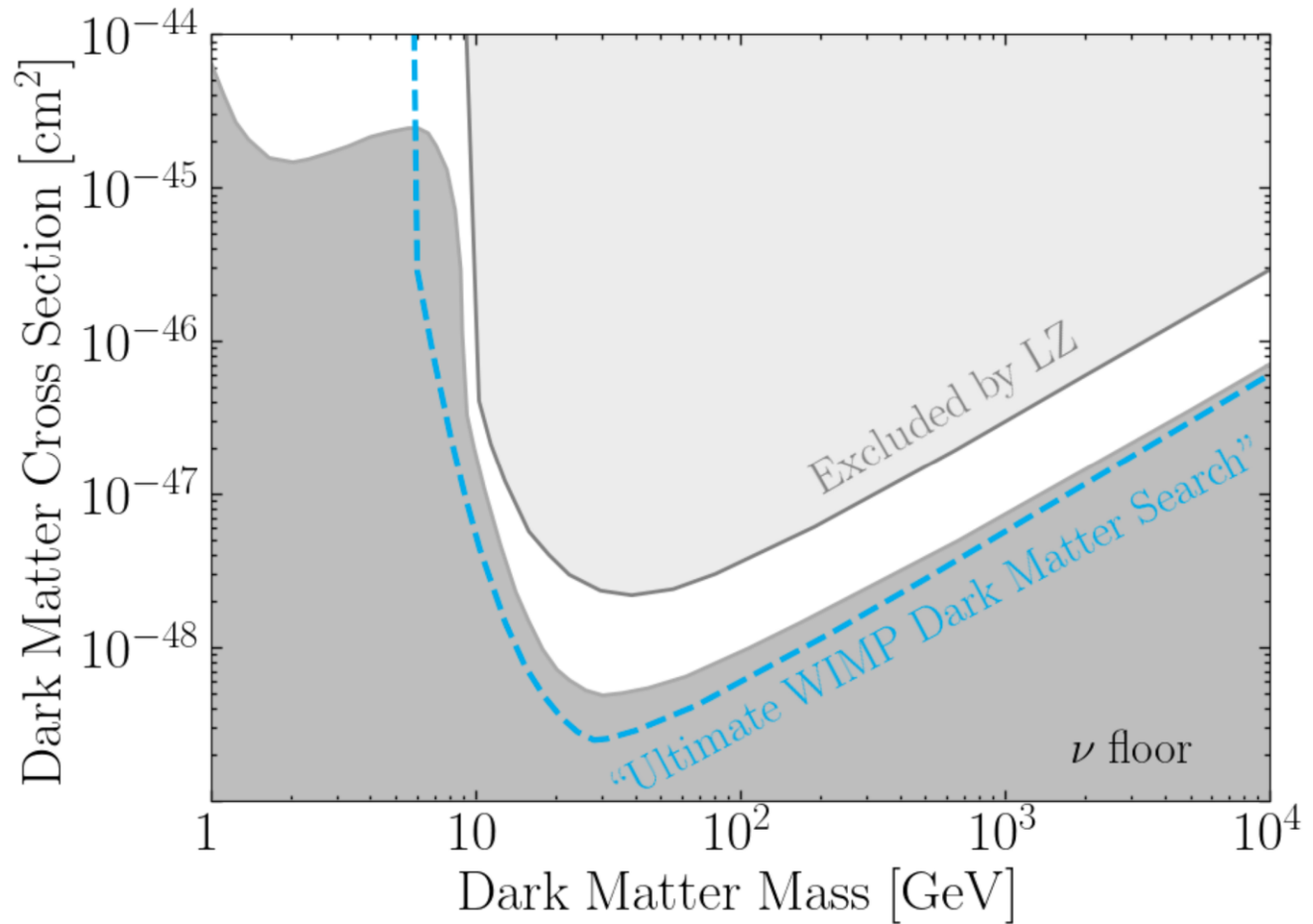
I. Infrared Freeze-In of Magnetic Dipole Dark Matter

II. Magnon-Based Direct Detection

Nuclear Recoil Direct Detection



LUX-ZEPLIN (LZ) detector

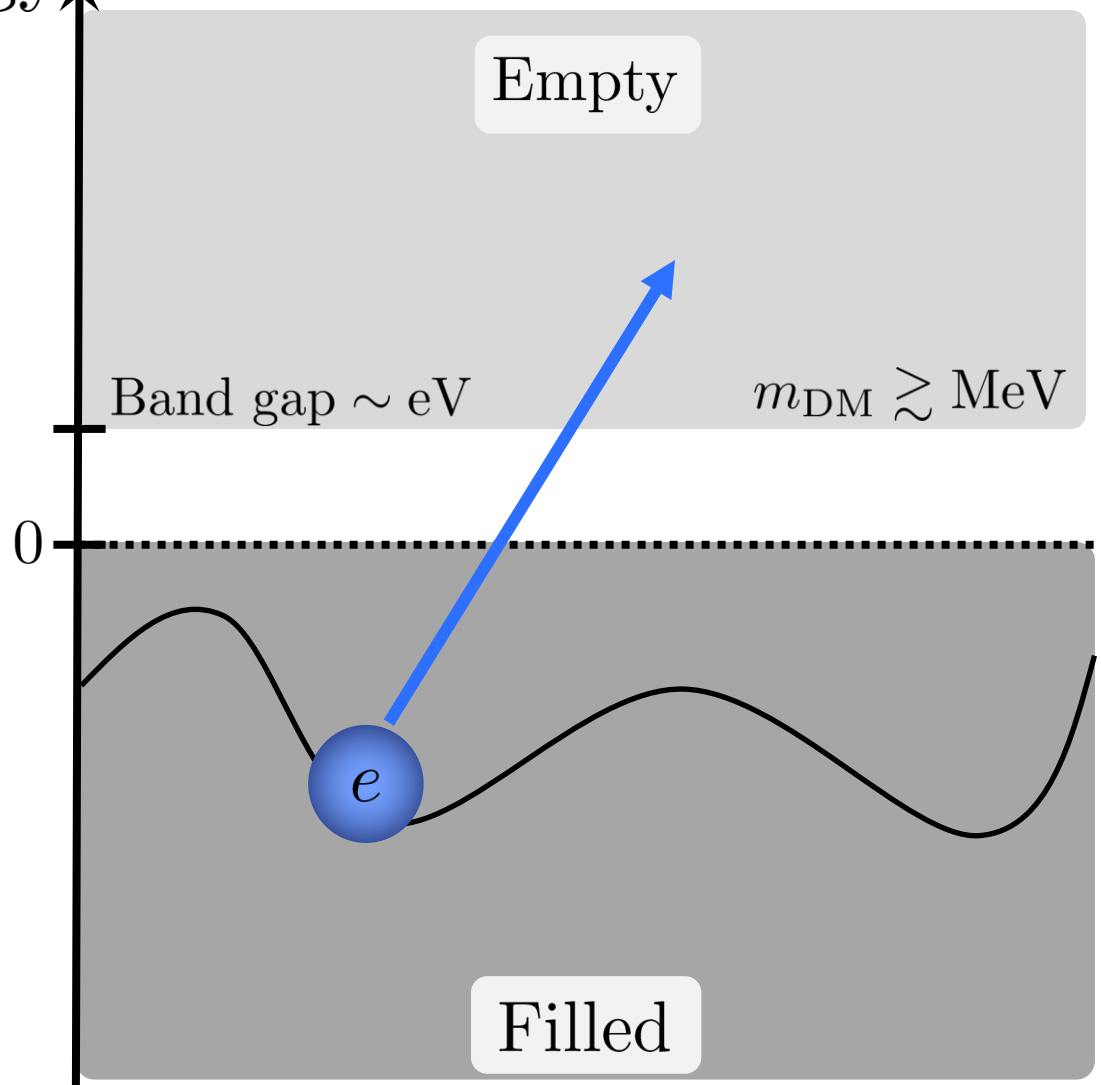
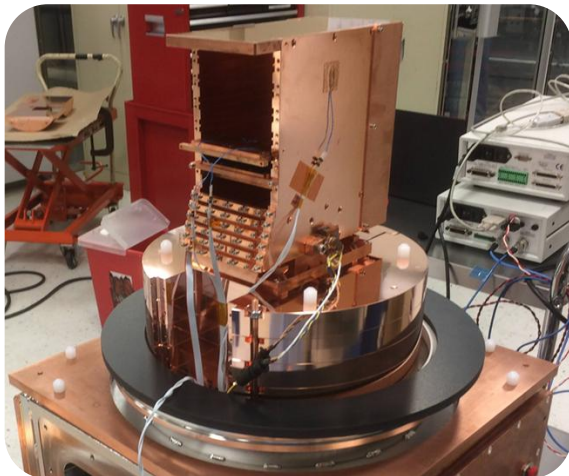
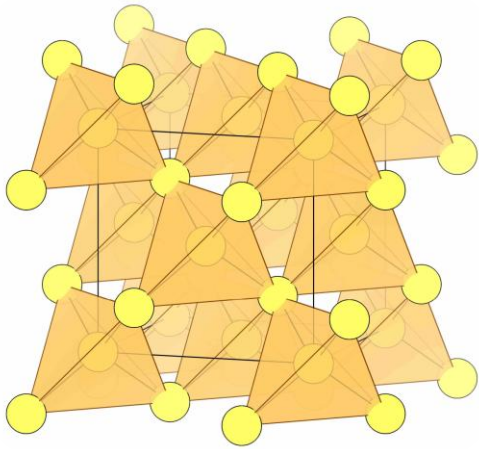


Major Initiative: G3, the Ultimate WIMP Dark Matter Search

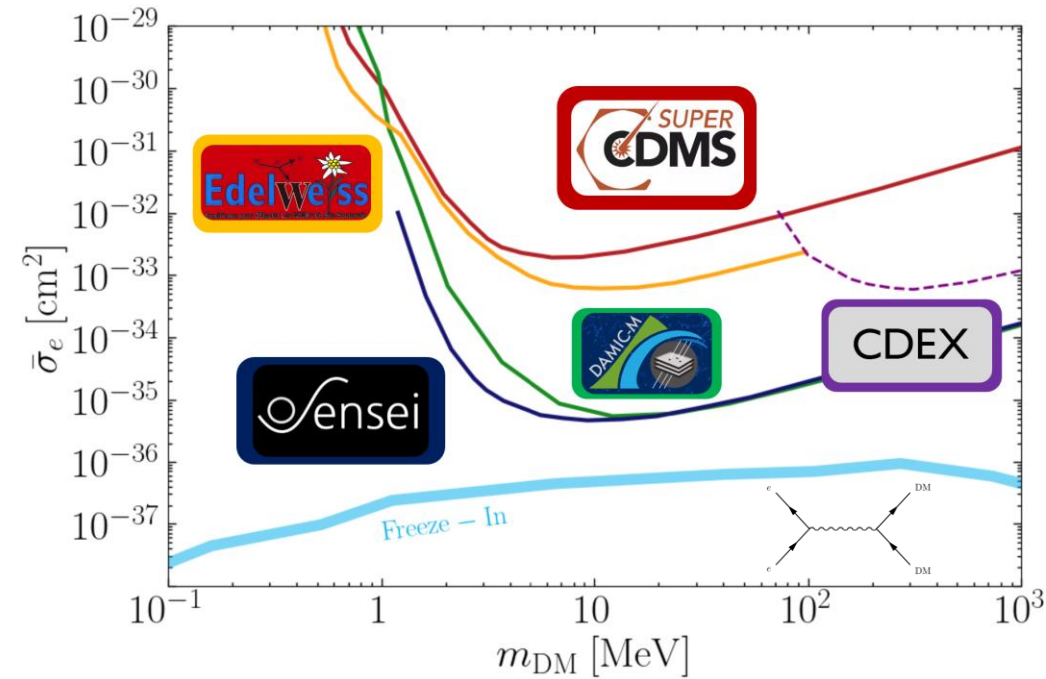
[2023 P5 Report: Exploring the Quantum Universe | Pathways to Innovation and Discovery in Particle Physics.](#)

Electronic Excitations

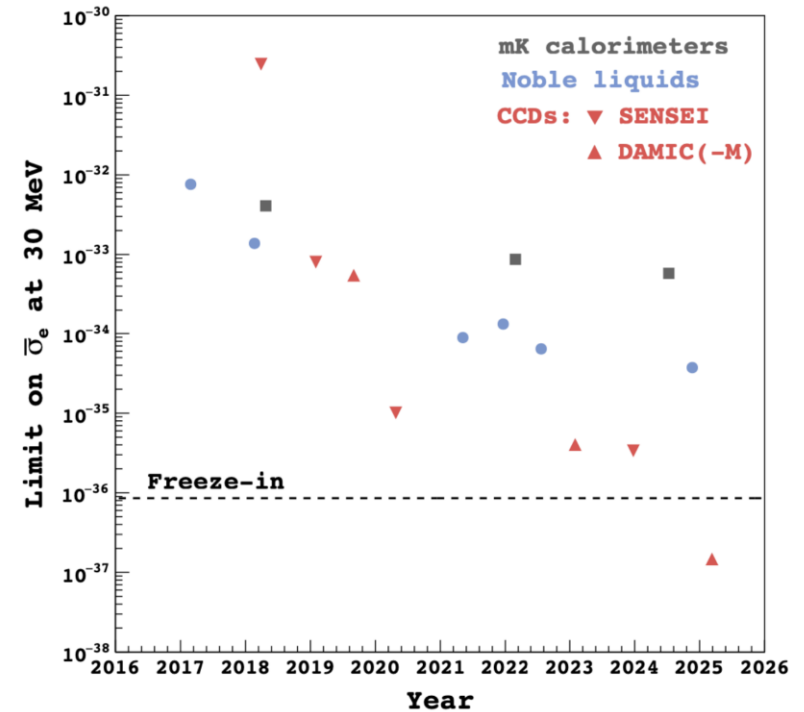
Energy



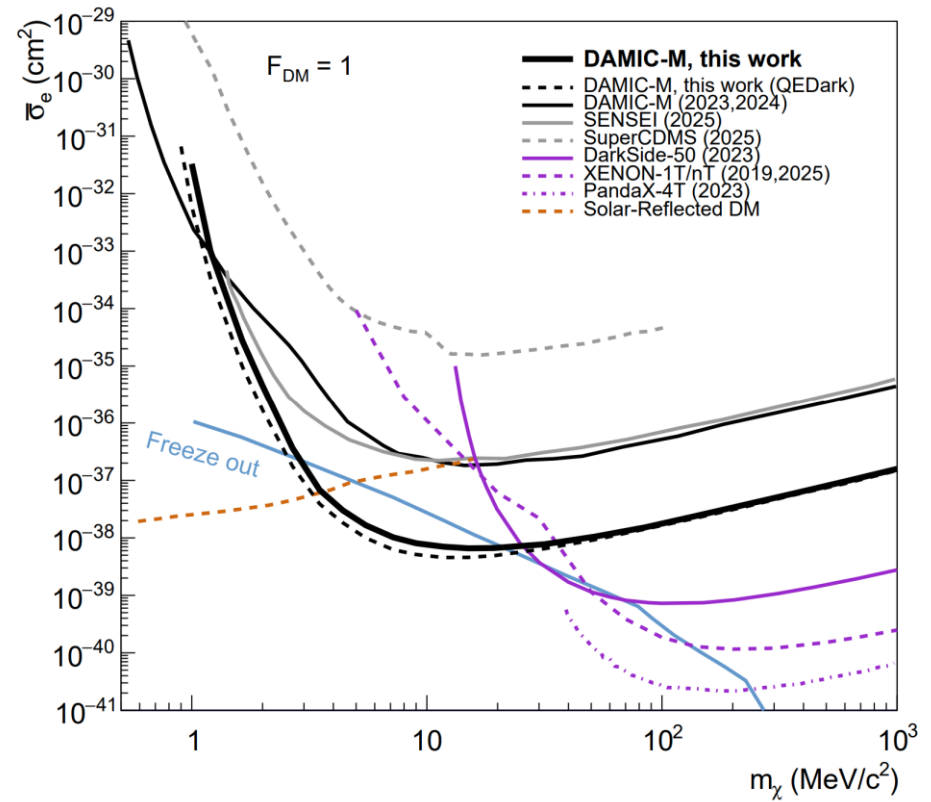
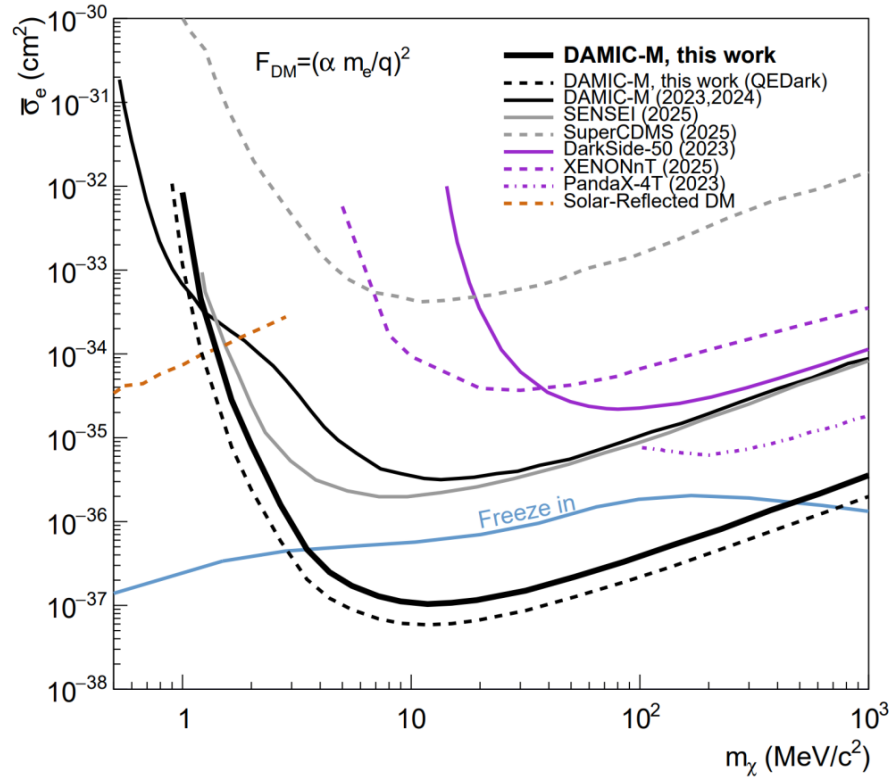
Experimental Sensitivity



History of Light DM Direct Detection

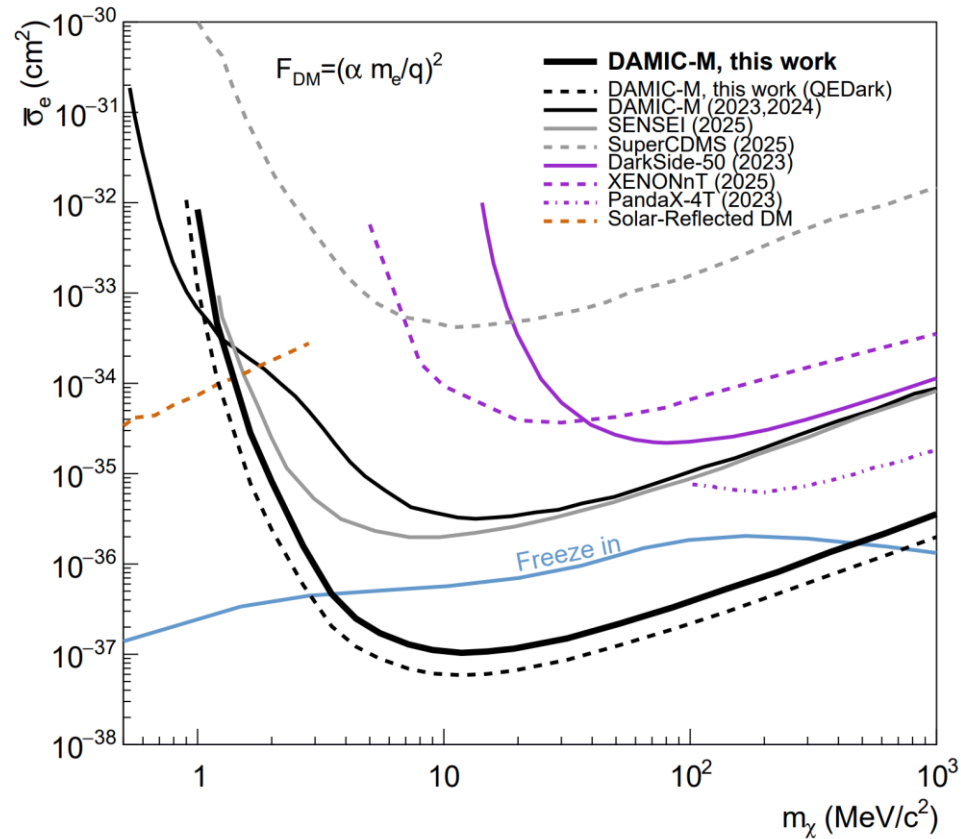


New Results From DAMIC



[\[2503.14617\]](#) Probing Benchmark Models of Hidden-Sector Dark Matter with DAMIC-M

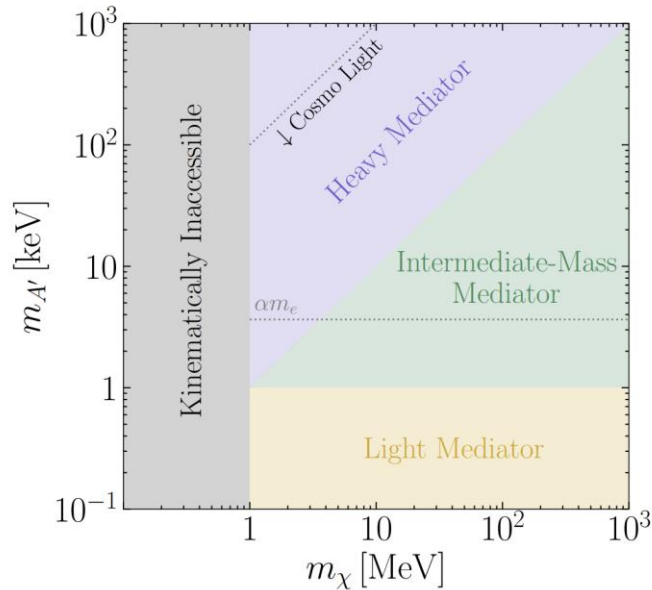
DAMIC Results Motivate New Questions



What new detector technologies must be developed for discovery?

What are other theoretically-motivated light dark matter models?

Intermediate-Mass Mediators



$$m_{A'} \ll \frac{\omega_{\text{th}}}{v_{\text{max}}}$$

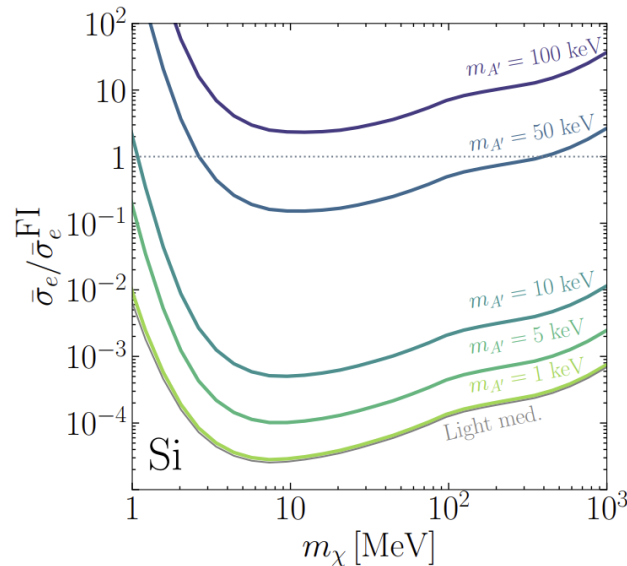
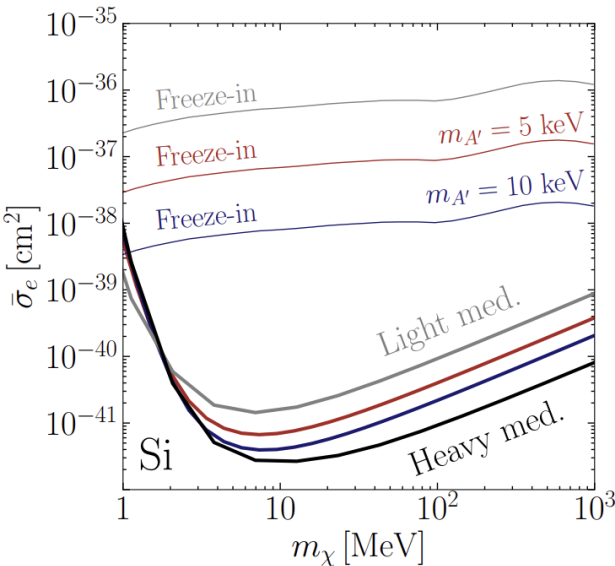
Light Mediator

$$\frac{\omega_{\text{th}}}{v_{\text{max}}} \lesssim m_{A'} \lesssim 2m_{\chi}v_{\text{max}}$$

Intermediate-Mass Mediator

$$2m_{\chi}v_{\text{max}} \ll m_{A'}$$

Heavy Mediator



[\[2605.11063\] Electronic Direct Detection of Light Dark Matter with Intermediate-Mass Mediators](#)

• C. Stratman, T. Trickle



Outline

I. Current Status of Direct Detection

I. Infrared Freeze-In of Magnetic Dipole Dark Matter

II. Magnon-Based Direct Detection

A Minimal Model of Light Dark Matter

$$\mathcal{L} \supset \underbrace{\bar{\chi}(\not{\partial} - m_{\chi})\chi + g_{\chi} A'_{\mu} \bar{\chi} \gamma^{\mu} \chi}_{\text{Dark sector}} + \underbrace{\frac{\varepsilon}{2} F'_{\mu\nu} F^{\mu\nu}}_{\text{Interaction (Kinetic mixing)}}$$

Dark sector

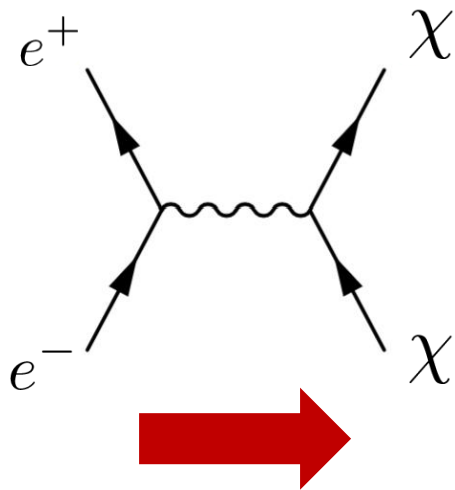
Interaction
(Kinetic mixing)

$$\mathcal{L} \supset A'_{\mu} \left[g_{\chi} (\bar{\chi} \gamma^{\mu} \chi) + \varepsilon e (\bar{e} \gamma^{\mu} e) \right]$$

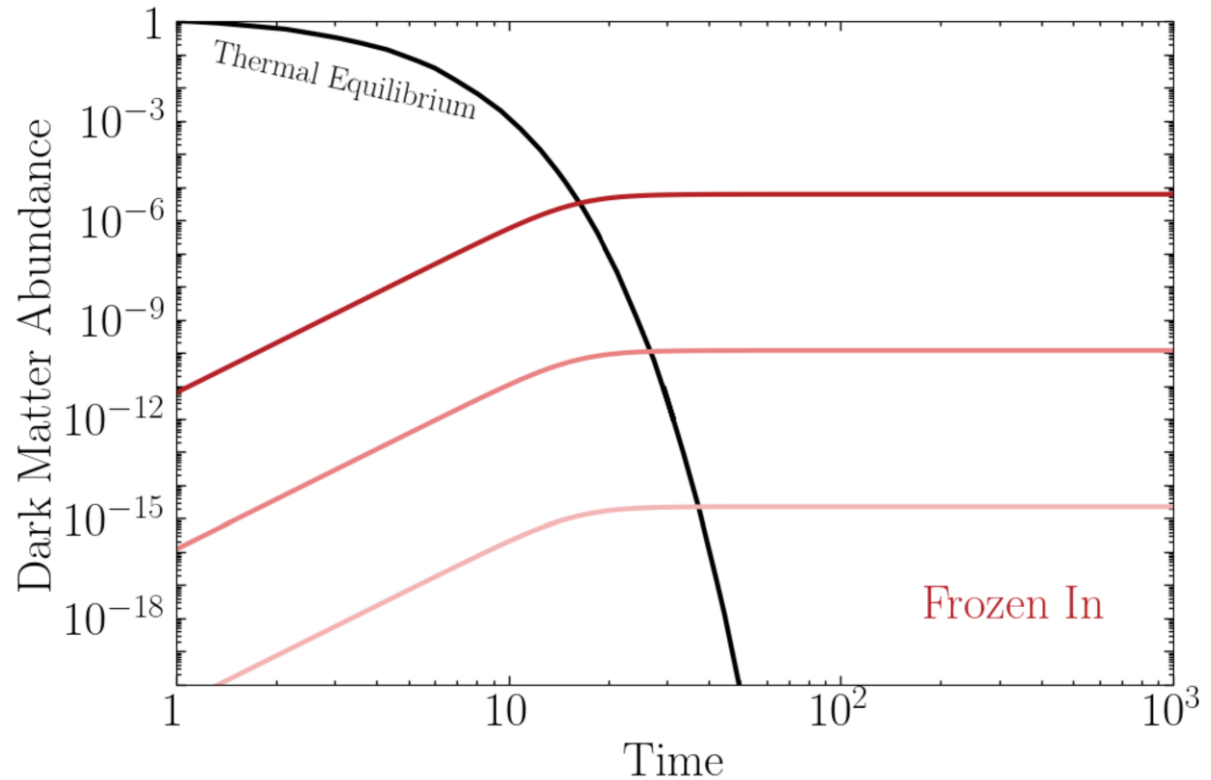
Interaction Lagrangian

Freeze-In

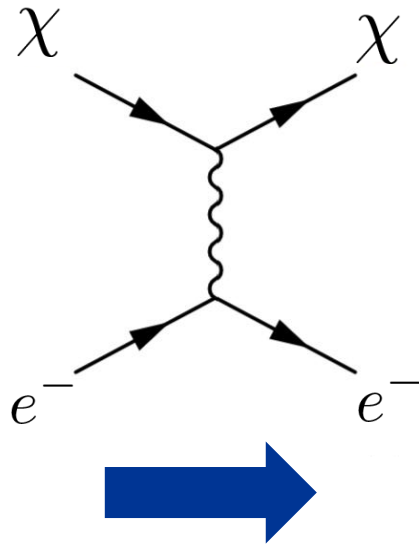
$$\mathcal{L} \supset A'_\mu \left[g_\chi (\bar{\chi} \gamma^\mu \chi) + \varepsilon e (\bar{e} \gamma^\mu e) \right]$$



Freeze-in Production

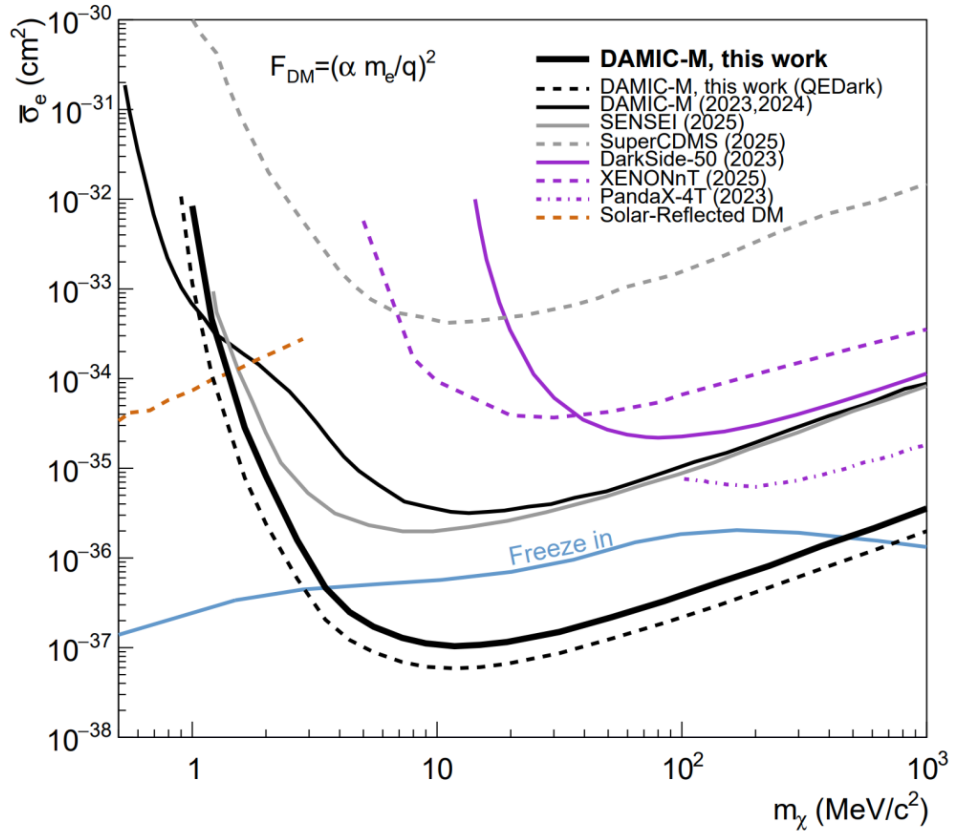


Freeze-In

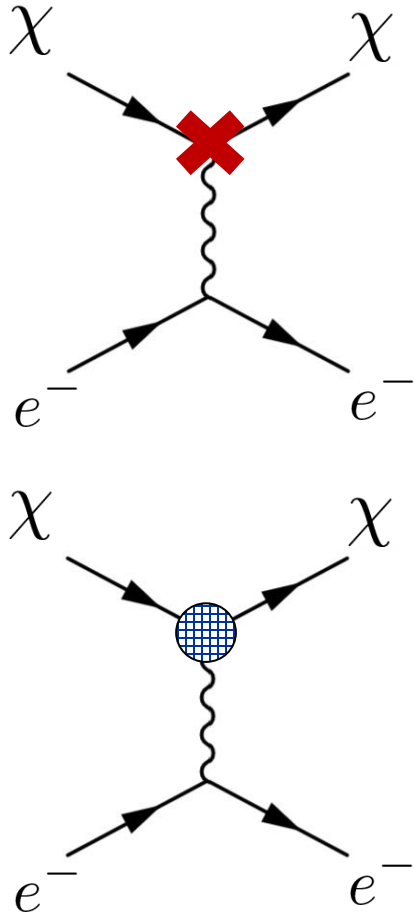


$$\mathcal{L} \supset A'_\mu [g_\lambda$$

Dark Matter Abundance



Magnetic Dipole-Coupled Dark Matter



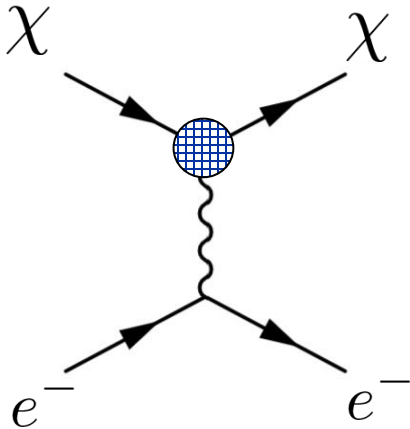
$$\mathcal{L} \supset A'_\mu \left[g_\chi \cancel{\bar{\chi} \gamma^\mu \chi} + \varepsilon e (\bar{e} \gamma^\mu e) \right]$$

“Dark electron”

“Dark neutron”

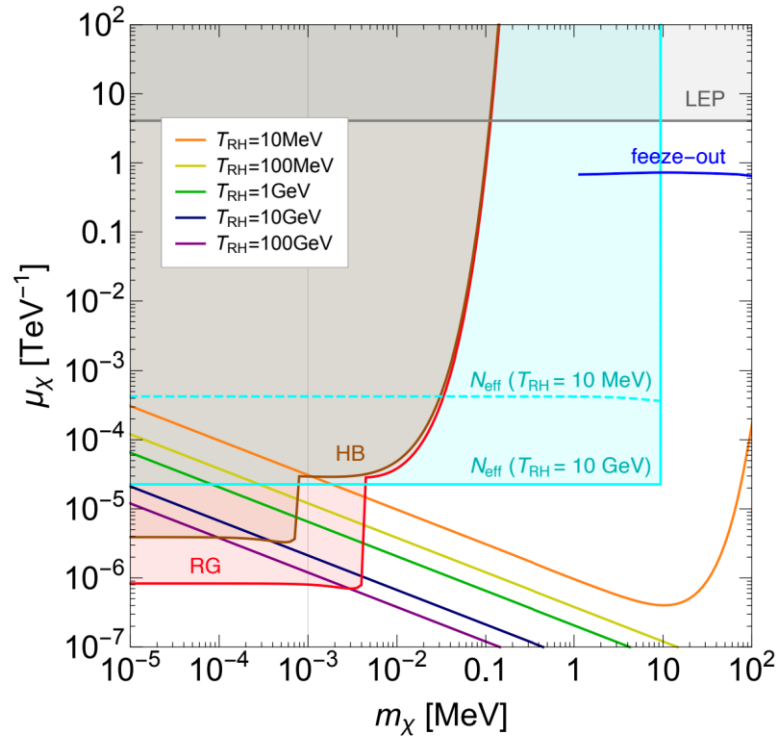
$$\mathcal{L} \supset \frac{\mu'_\chi}{2} F'_{\mu\nu} (\bar{\chi} \sigma^{\mu\nu} \chi) + \varepsilon e A'_\mu (\bar{e} \gamma^\mu e)$$

Freeze-In of Magnetic Dipole Dark Matter



$$\mathcal{L} \supset \frac{\mu'_\chi}{2} F'_{\mu\nu} (\bar{\chi} \sigma^{\mu\nu} \chi) + \varepsilon e A'_\mu (\bar{e} \gamma^\mu e)$$

dark matter with a magnetic dipole moment



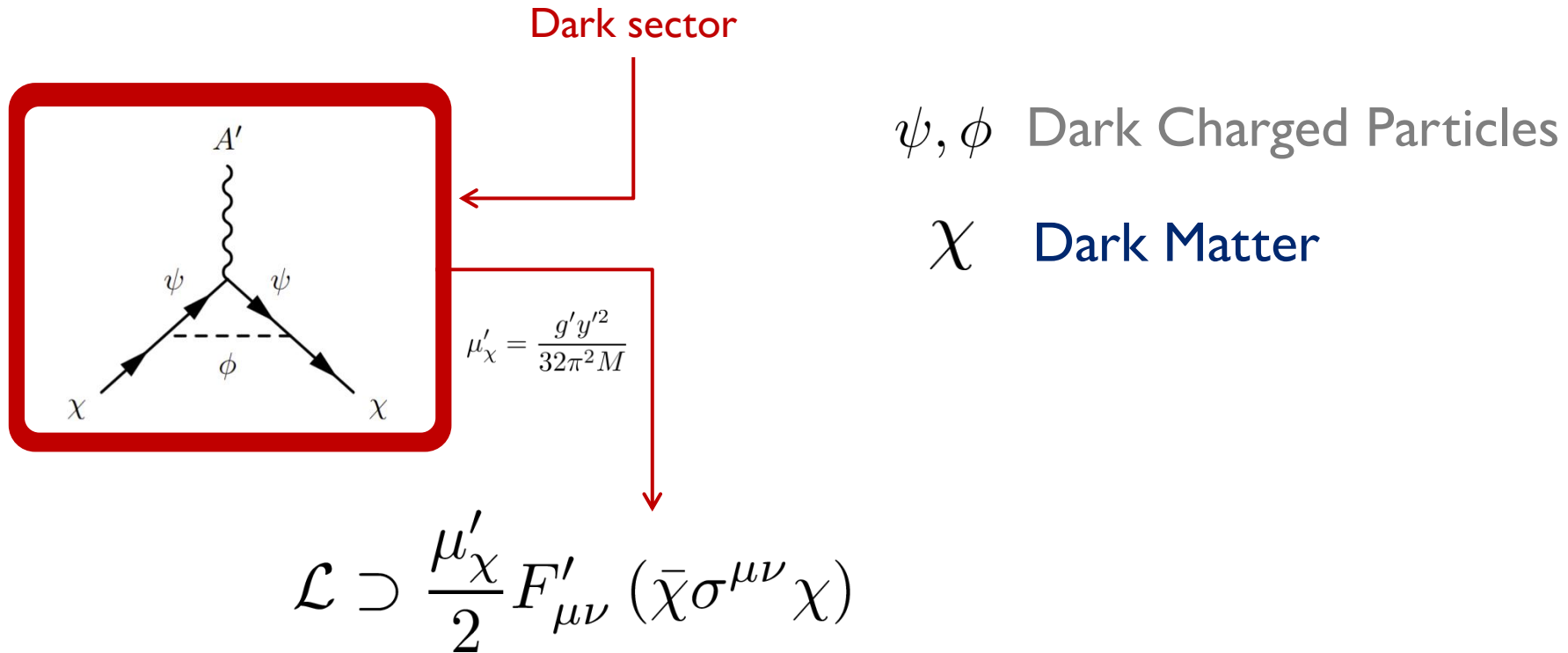
[\[1911.03389\] Light\(ly\)-coupled Dark Matter in the keV Range: Freeze-In and Constraints](#)

[\[1410.6157\] UltraViolet Freeze-in](#)

Problem: production is UV dominated

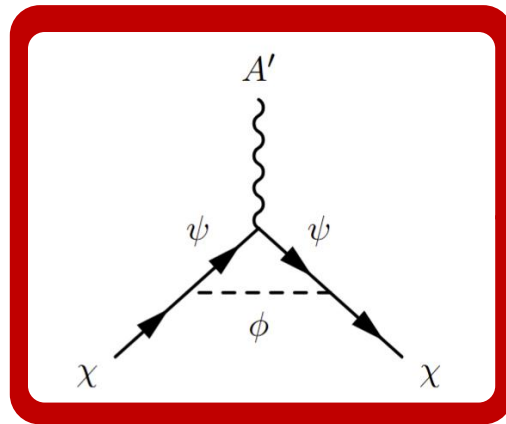
Magnetic Dipole-Coupled Dark Matter

$$\mathcal{L} \supset A'_\mu \left[g' (\bar{\psi} \gamma^\mu \psi) + g' (\phi^* \partial^\mu \phi) \right] + y' \phi \bar{\psi} \chi$$



Magnetic Dipole-Coupled Dark Matter

$$\mathcal{L} \supset \underbrace{A'_\mu \left[g'(\bar{\psi}\gamma^\mu\psi) + g'(\phi^*\partial^\mu\phi) \right] + y'\phi\bar{\psi}\chi}_{\text{Dark sector}} + \underbrace{\frac{\varepsilon}{2}F'_{\mu\nu}F^{\mu\nu}}_{\text{Interaction (Kinetic mixing)}}$$

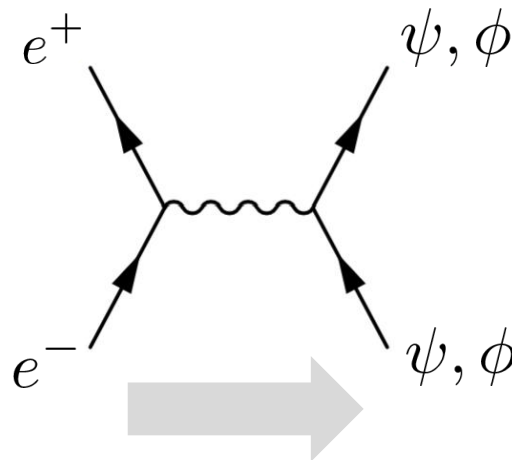
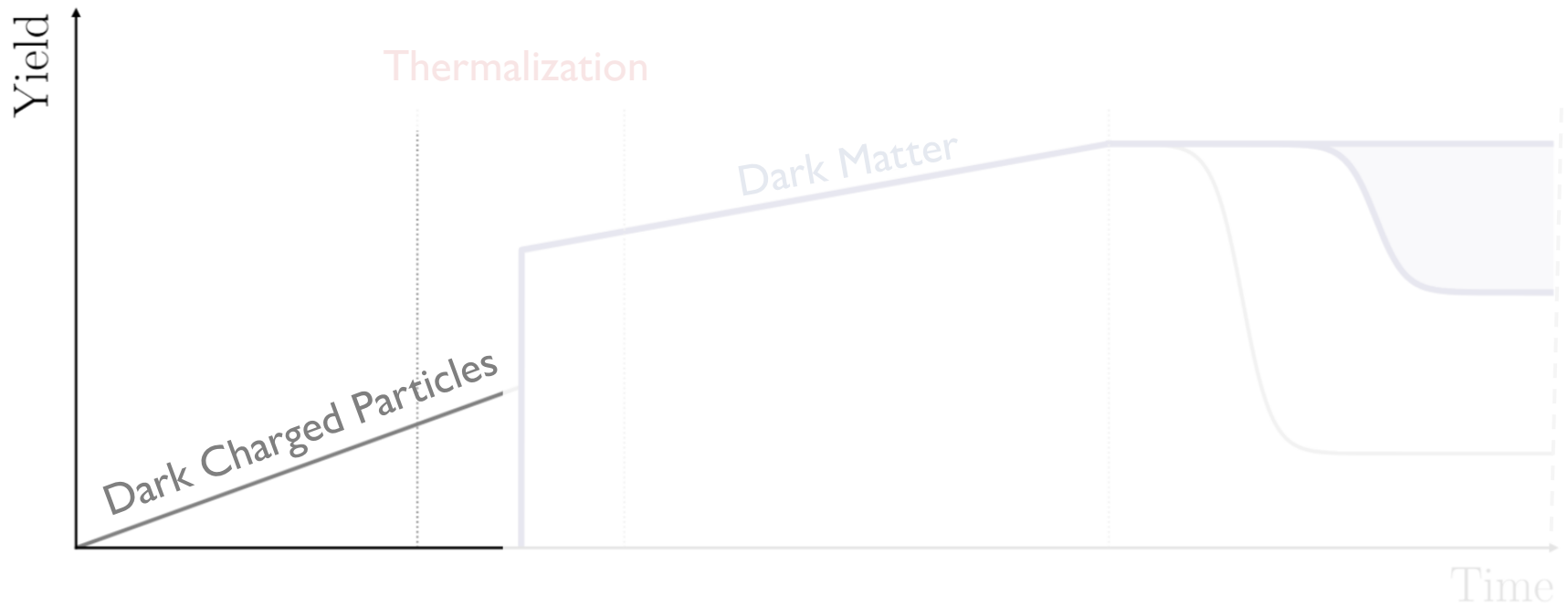


$$\mu'_\chi = \frac{g'y'^2}{32\pi^2 M}$$

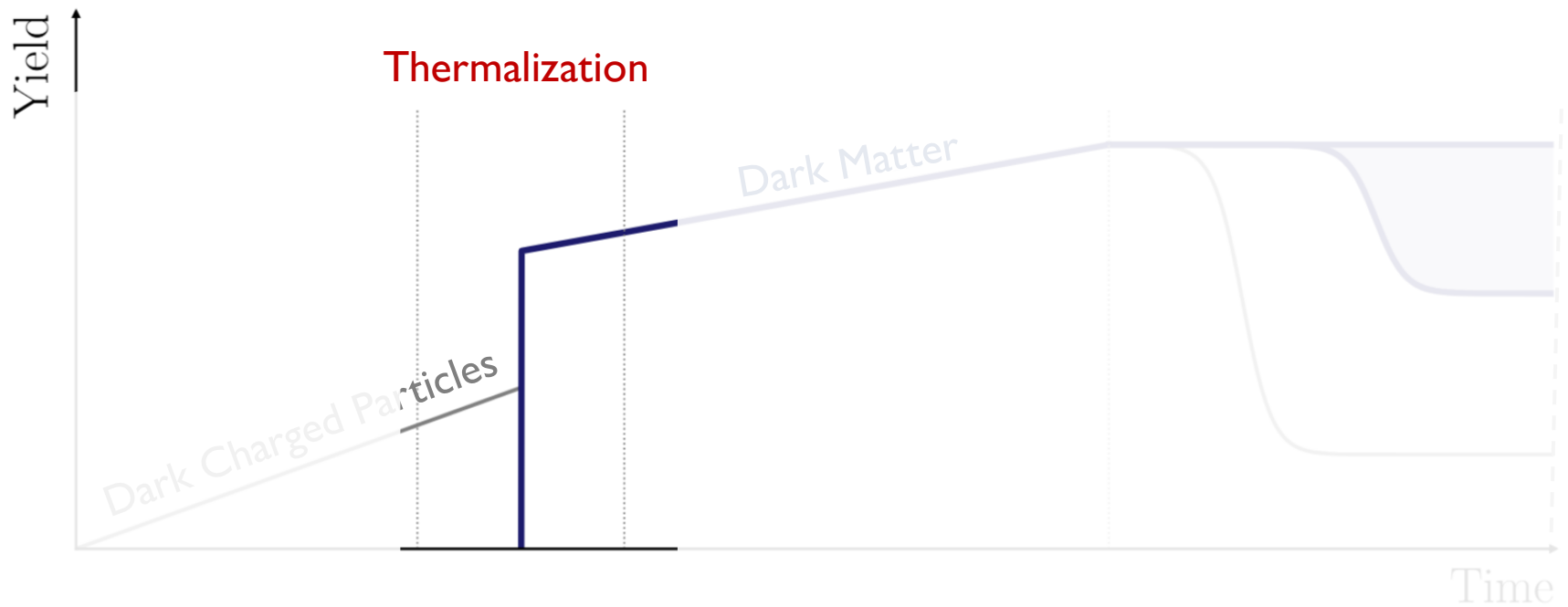
$$\mathcal{L} \supset \frac{\mu'_\chi}{2} F'_{\mu\nu} (\bar{\chi}\sigma^{\mu\nu}\chi) + \varepsilon e A'_\mu (\bar{e}\gamma^\mu e)$$

Magnetic Dipole-Coupled Interaction Lagrangian

Pre-Thermalization



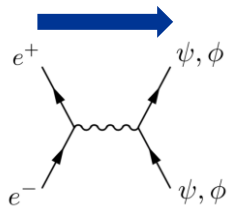
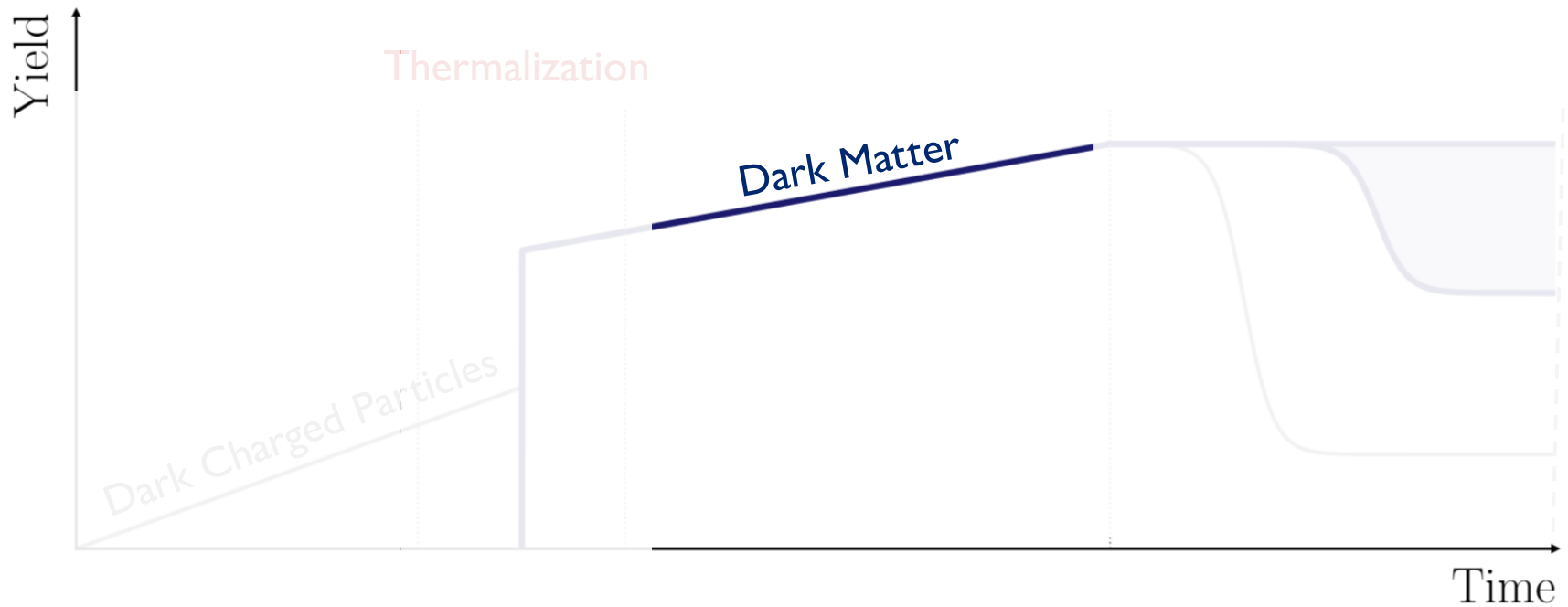
Thermalization



$$\phi \leftrightarrow \psi\chi \quad , \quad \phi\phi \leftrightarrow A'A' \quad , \quad \psi\psi \leftrightarrow A'A' \quad , \quad \phi\phi \leftrightarrow \chi\chi$$

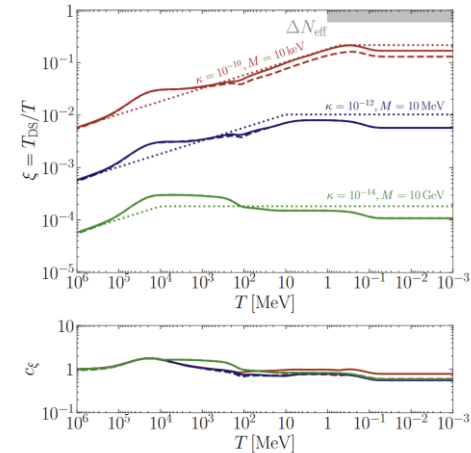
All processes must be faster than Hubble.

Post-Thermalization

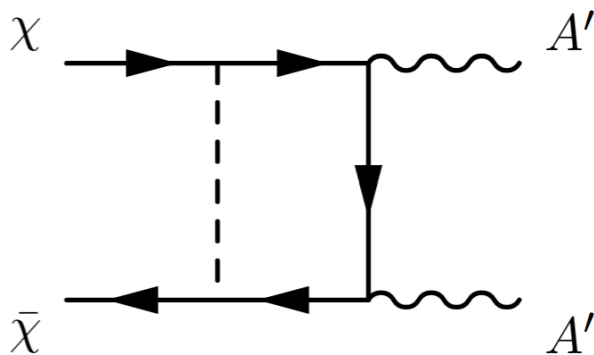
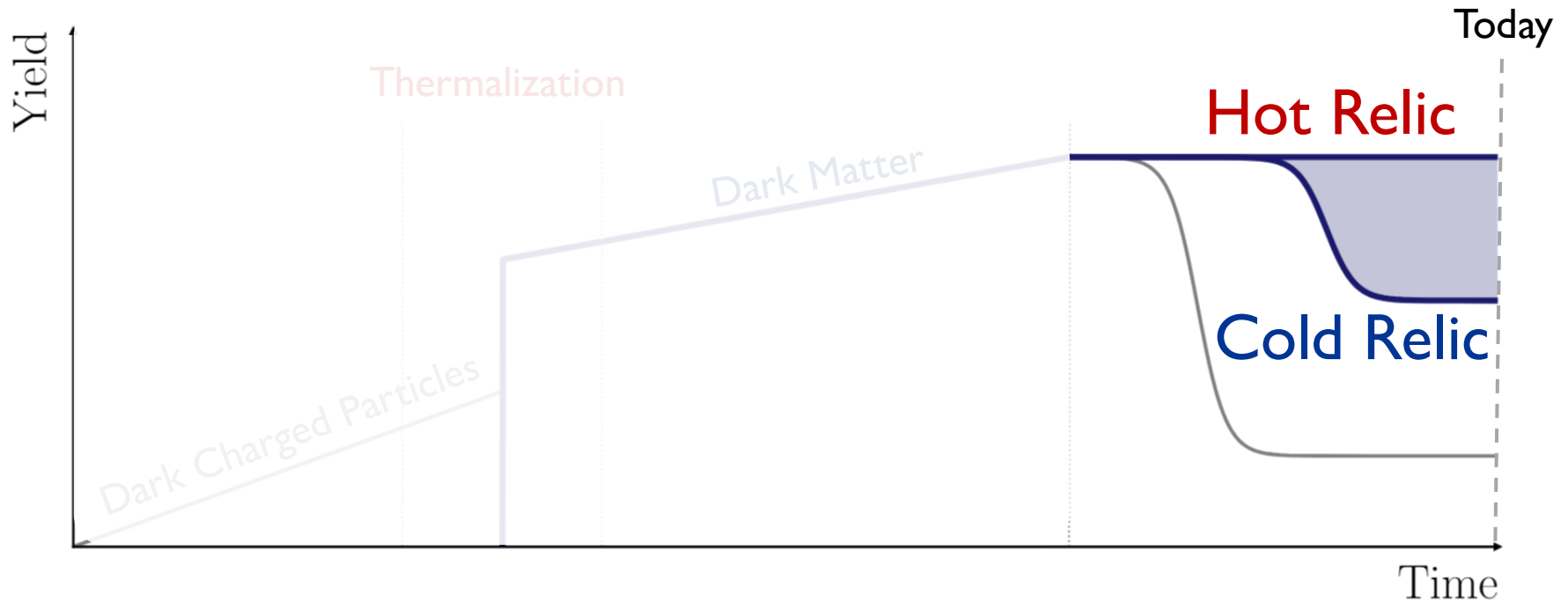


$$\frac{d(\rho_{\text{DS}}/s^{4/3})}{dT} \propto -(e^2 \kappa)^2 \frac{M_{\text{Pl}}}{T^2} \quad \Rightarrow \quad \frac{T_{\text{DS}}}{T} \sim \sqrt{e^2 \kappa} \left(\frac{M_{\text{Pl}}}{T} \right)^{1/4}$$

Energy density
Boltzmann equation



Dark Matter Decoupling

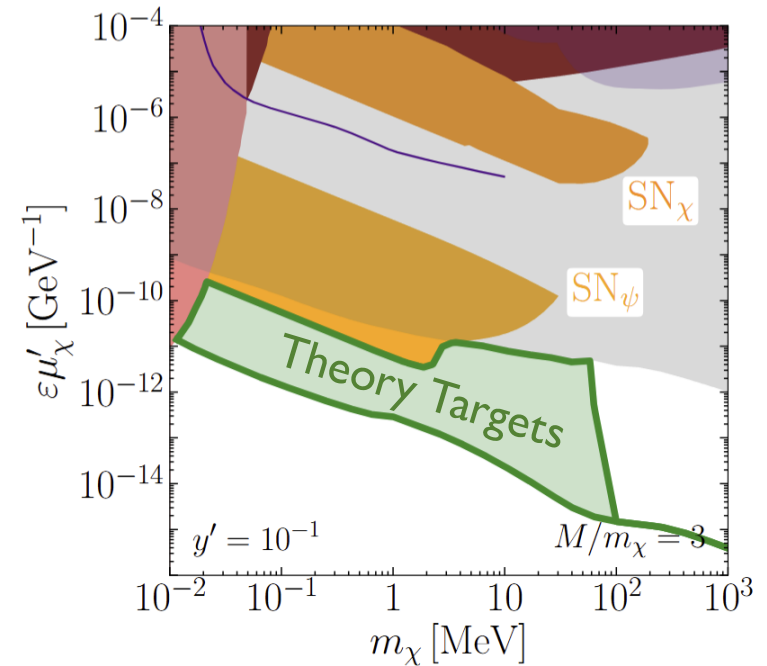
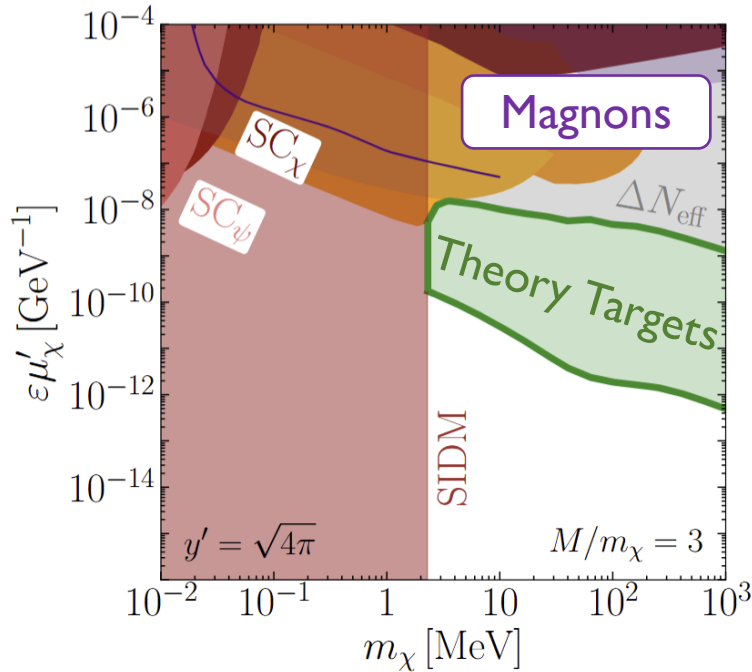


$$n_{\chi} \langle \sigma v \rangle_{\chi\chi \rightarrow A' A'} \lesssim H \quad @ \quad T_{\text{DS}} \sim m_{\chi}$$

$$\langle \sigma v \rangle_{\chi\chi \rightarrow A' A'} \sim \frac{y'^4 g'^4}{768 \pi^5} \frac{m_{\chi}^4}{M^6}$$

Hot Relic : **smaller** dark sector couplings
Cold Relic: **larger** dark sector couplings

Direct Detection Theory Targets



$$\mathcal{L} \supset \frac{\mu'_\chi}{2} F'_{\mu\nu} (\bar{\chi} \sigma^{\mu\nu} \chi) + \varepsilon e A'_\mu (\bar{e} \gamma^\mu e)$$

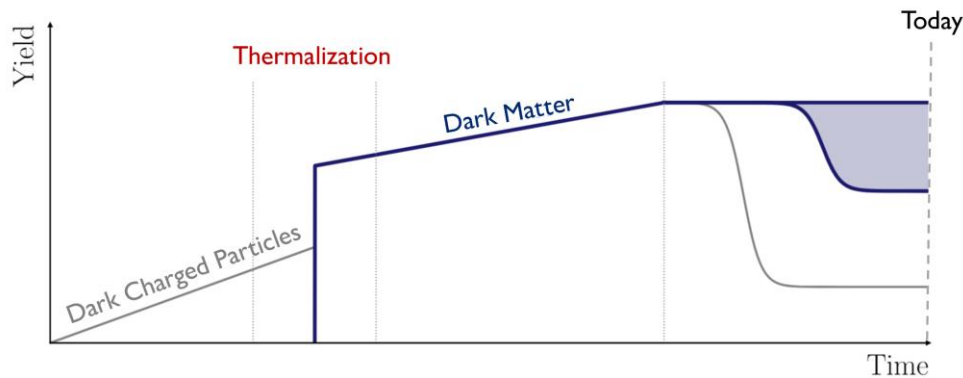
Example model parameter space ranges from optimistically detectable to un-detectable.

Thermalizing Freeze-In Summary

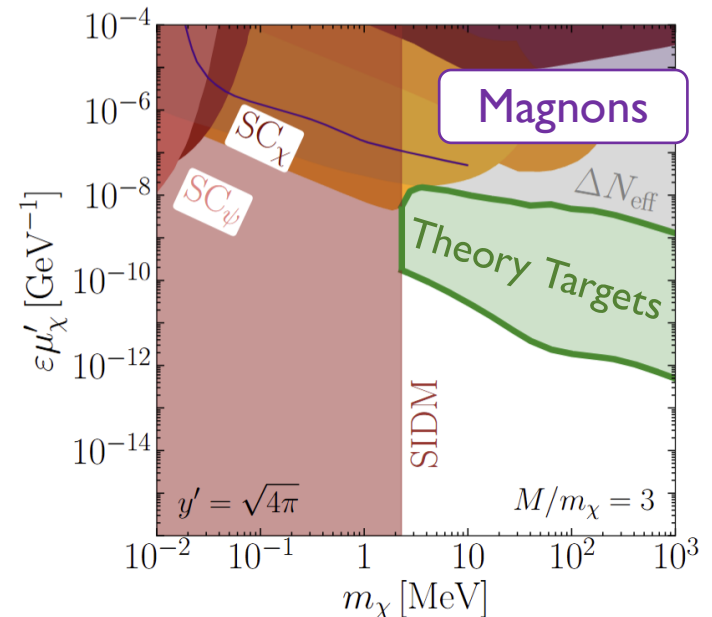
A simple dark sector...

$$\mathcal{L} \supset \underbrace{A'_\mu \left[g'(\bar{\psi}\gamma^\mu\psi) + g'(\phi^*\partial^\mu\phi) \right]}_{\text{Dark sector}} + \underbrace{y'\phi\bar{\psi}\chi + \frac{\varepsilon}{2}F'_{\mu\nu}F^{\mu\nu}}_{\text{Kinetic mixing}}$$

**thermalizing in the
early universe...**



**realizes detectable
magnetic dipole-couplings.**



Outline

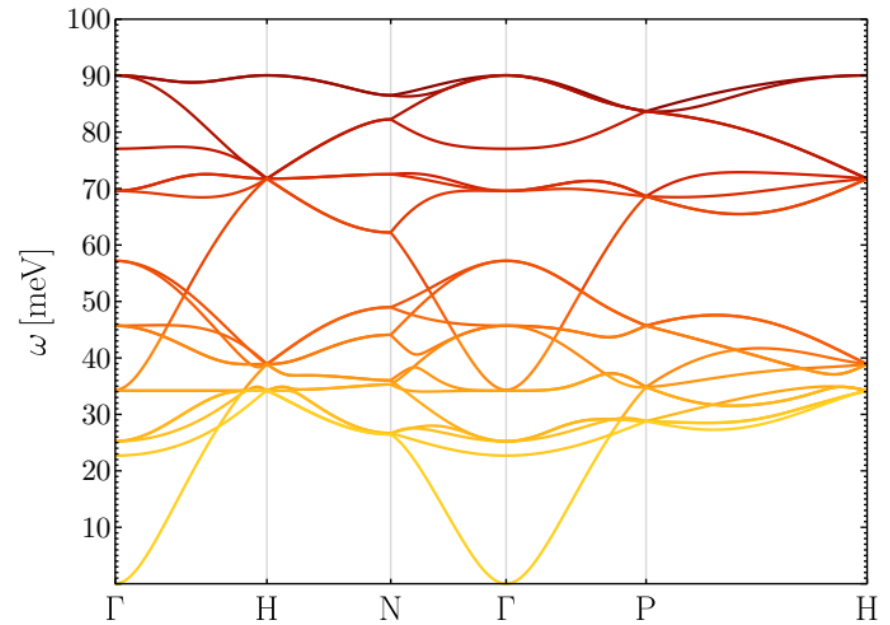
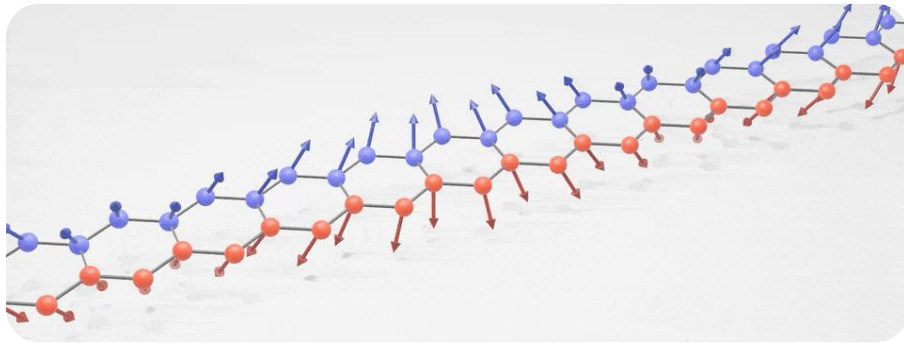
I. Current Status of Direct Detection

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Magnons

Collective spin excitations

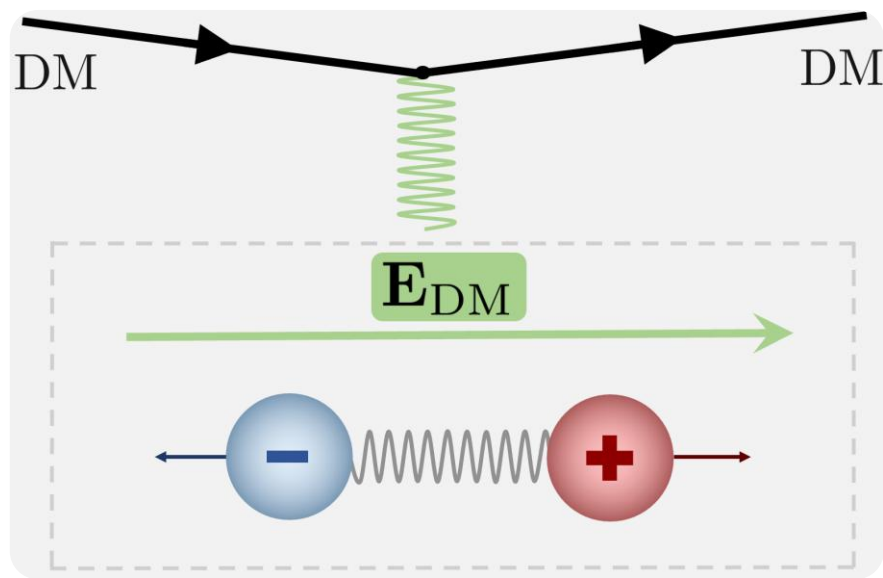


[\[1905.13744\] Detecting Light Dark Matter with Magnons](#)

- **T. Trickle**, Zhang, Zurek

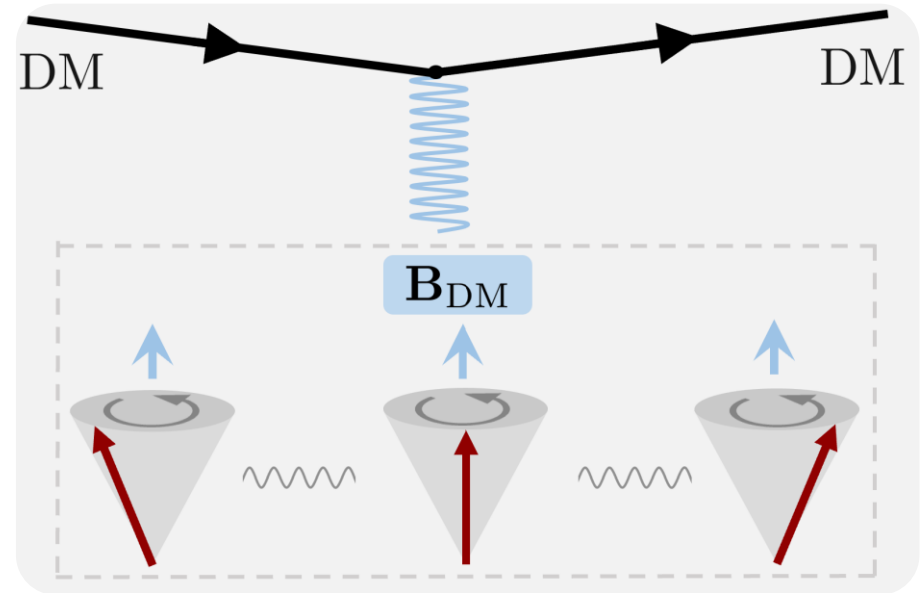
Phonon vs. Magnon Scattering

Phonons



“Spin-**independent** coupling”

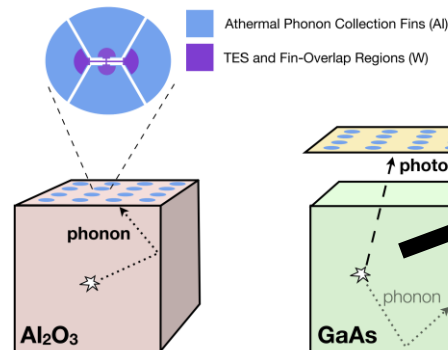
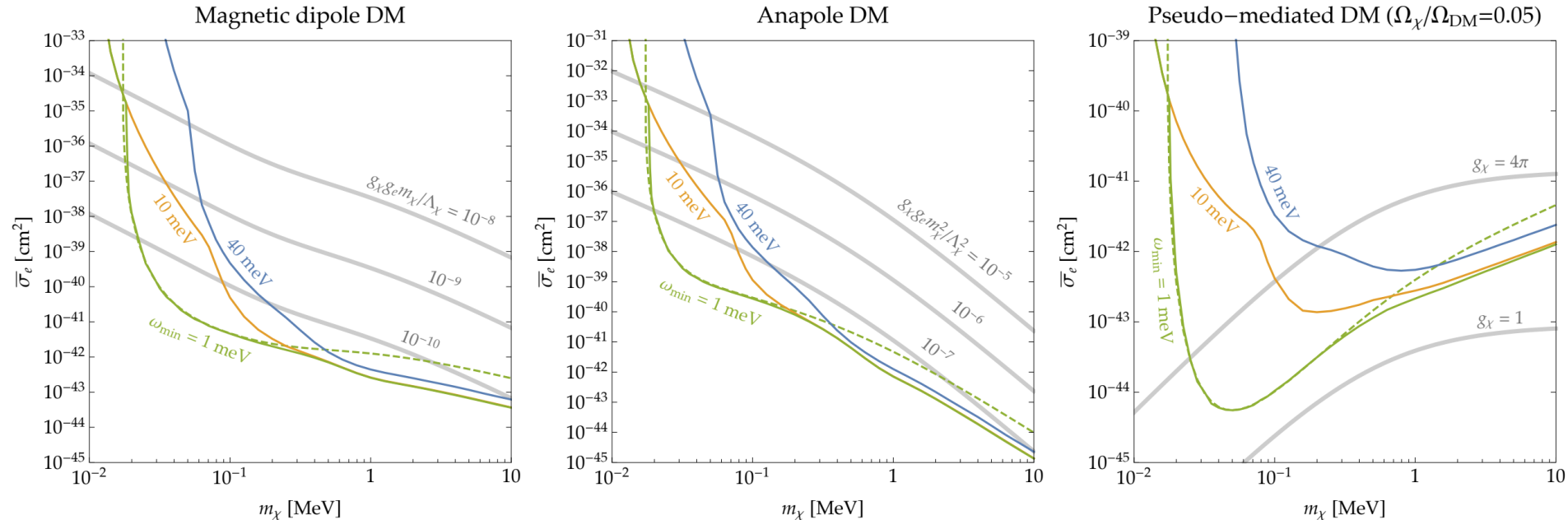
Magnons



“Spin-**dependent** coupling”

Sensitivity To Dark Matter Scattering

First-Principles



[\[1905.13744\] Detecting Light Dark Matter with Magnons](#)

- **T. Trickle**, Zhang, Zurek

The saga of YIG: Spectra, thermodynamics, interaction and relaxation of magnons in a complex magnet

Vladimir Cherepanov^{*1,3}, Igor Kolokolov³, Victor L'vov^{*1,c}

The Dark Matter Scattering Rate

Data-Driven Approach

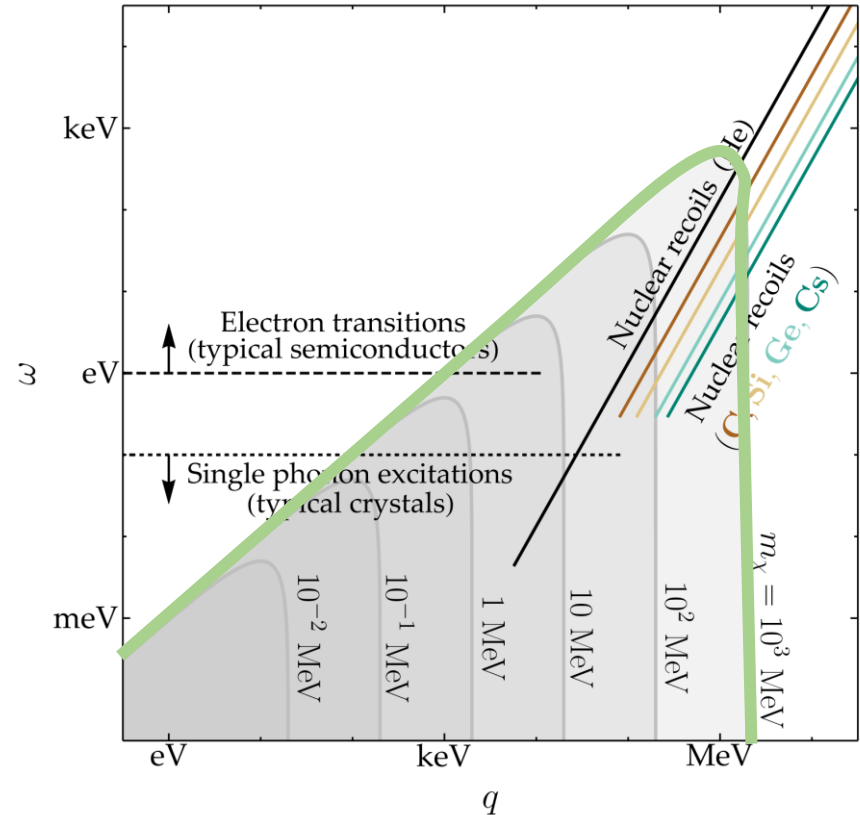
Similarities With Neutron Scattering

Effective neutron-electron interaction

$$\mathcal{L} \supset \frac{\gamma_n e}{4m_n} \bar{n} \sigma^{\mu\nu} n F_{\mu\nu} - e A_\mu \bar{e} \gamma^\mu e$$

Dark magnetic dipole dark matter

$$\mathcal{L} \supset \frac{\mu'_\chi}{2} F'_{\mu\nu} (\bar{\chi} \sigma^{\mu\nu} \chi) + \varepsilon e A'_\mu (\bar{e} \gamma^\mu e)$$

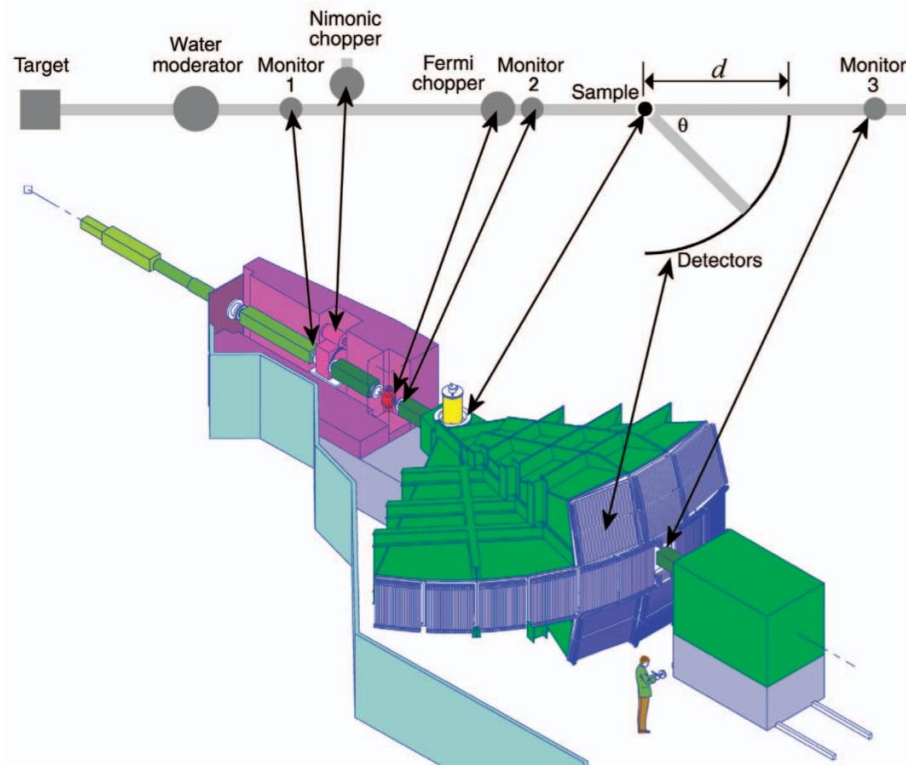


Interaction structure



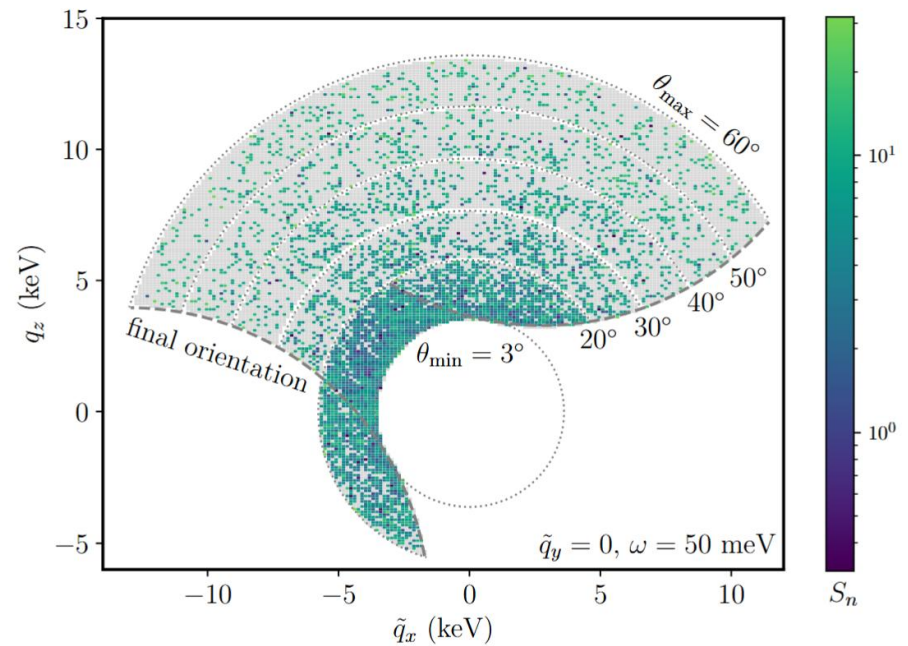
Kinematics

A Neutron Scattering Dataset



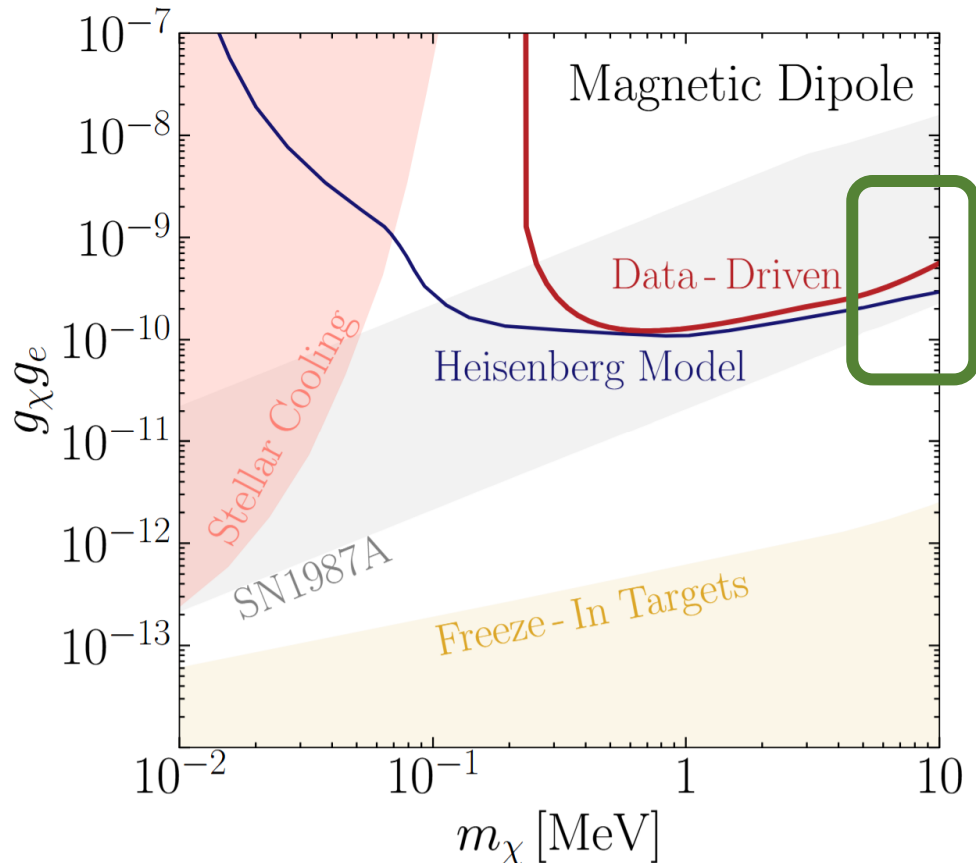
The MAPS Spectrometer

ISIS Neutron and
Muon Source



A 2D slice of the data

Comparison of First-Principles and Data-Driven Sensitivity



- Data-driven enhanced by *phonon* contribution
- First-principles enhanced by neglecting *magnetic form factors*

[\[2501.18120\]](#) Spin-dependent dark matter scattering in quasi-two-dimensional magnets

$$\mathcal{L} \supset \frac{g_\chi}{4m_\chi} \bar{\chi} \sigma^{\mu\nu} \chi F'_{\mu\nu} + g_e A'_\mu \bar{\Psi} \gamma^\mu \Psi$$

[\[2504.02927\]](#) Determining Spin-Dependent Light Dark Matter Rates from Neutron Scattering

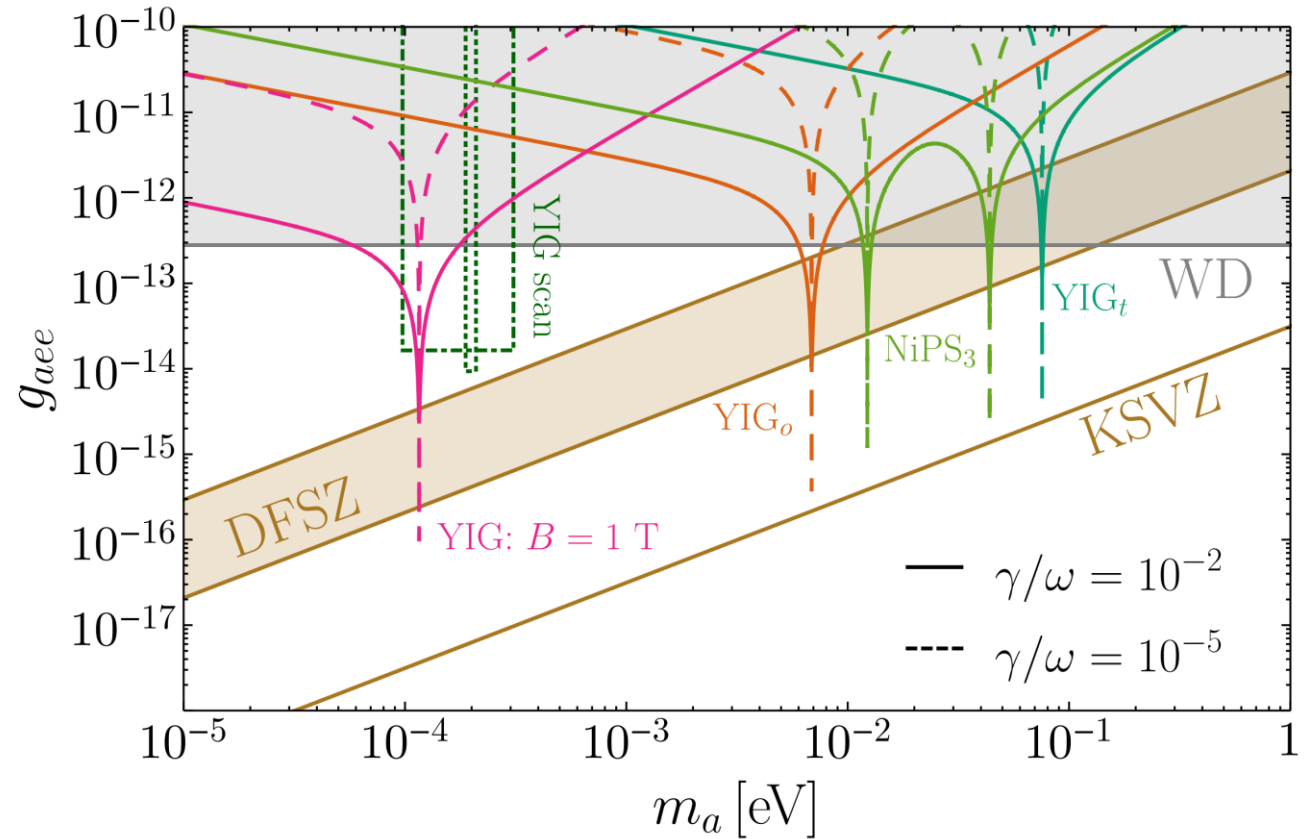
- Berlin, Millar, **T. Trickle**, Zhou

Axion Absorption Into Magnons



The saga of YIG: Spectra, thermodynamics, interaction and relaxation of magnons in a complex magnet

Vladimir Cherepanov^{*1,3}, Igor Kolokolov^b, Victor L'vov^{*1,c}

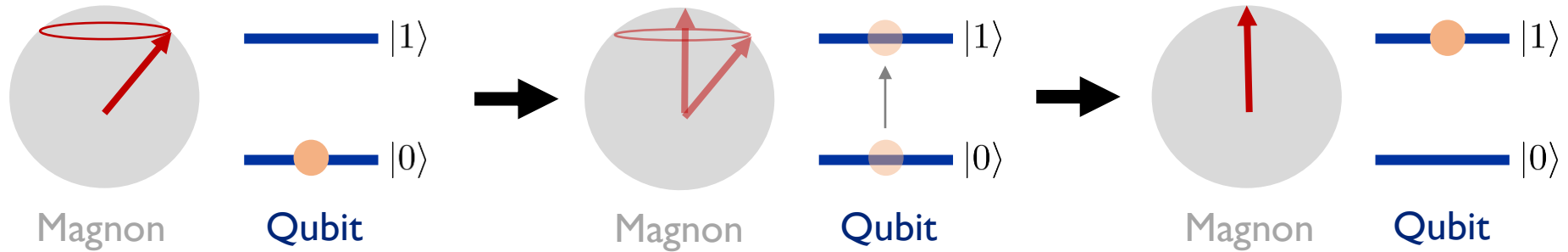


[\[2005.10256\] Detectability of Axion Dark Matter with Phonon Polaritons and Magnons](#)

- Mitridate, **T. Trickle**, Zhang, Zurek

How To Detect Single Magnons?

Single Magnon Counting With Qubits



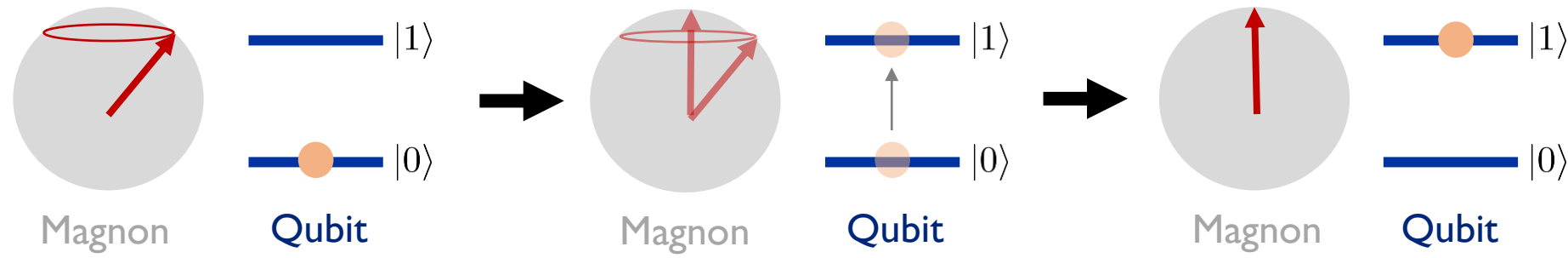
$$\frac{\omega_{|1\rangle} - \omega_{|0\rangle}}{2\pi} \sim 6 \text{ GHz}$$

If $\omega_m \sim (\omega_{|1\rangle} - \omega_{|0\rangle})$ then resonant conversion between magnon-qubit states.

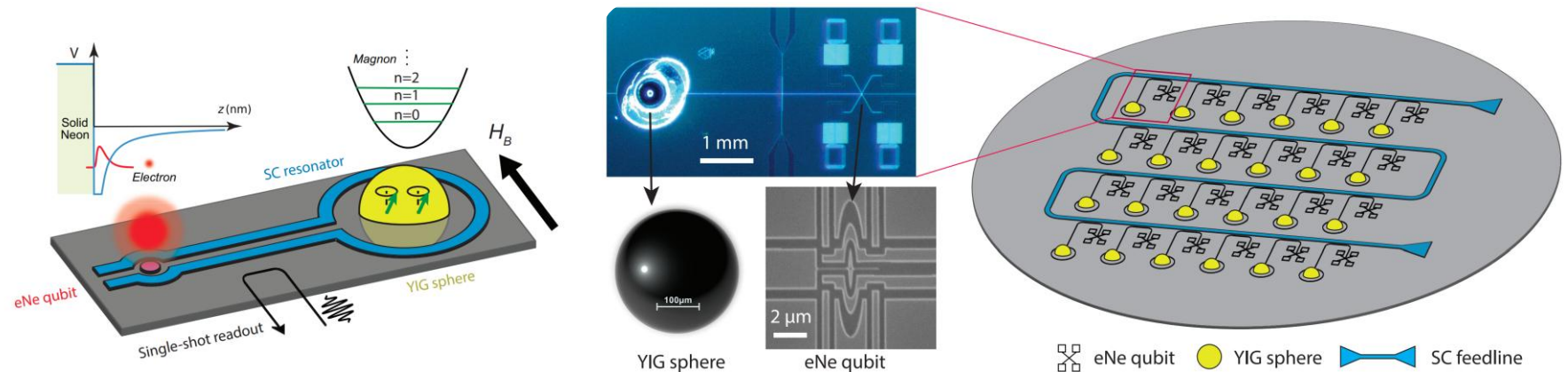
Similar idea with phonons:

- [\[2410.17308\] Listening For New Physics With Quantum Acoustics](#)
Linehan, **T. Trickle**, Conner, Ghosh, Lin, Sholapurkar, Cleland

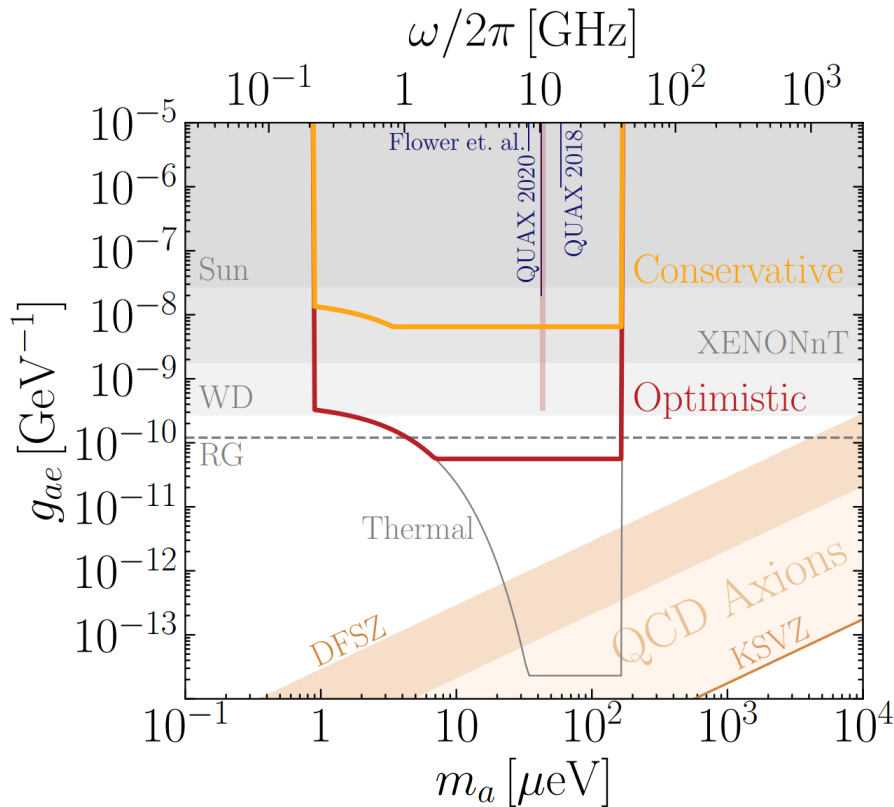
Single Magnon Detection With Quantum Magnonics



Quantum Information Science Enabled Discovery (QuantISED) 2.0
Quantum Magnonics For Spin-Dependent BSM Physics
 Argonne National Laboratory – Notre Dame – **T. Trickle** (Co-PI)



Projected MOSAIC Sensitivity



$$g_{ae} \sim \frac{10^{-8}}{\text{GeV}} N_s^{-\frac{1}{4}} \left(\frac{2.7 \text{ mg}}{m_{\text{YIG}}} \right)^{\frac{1}{2}} \left(\frac{p_{\text{dc}}}{3 \times 10^{-4}} \right)^{\frac{1}{4}}$$

Number of spheres Mass of sphere Dark count probability

Conservative – achievable today

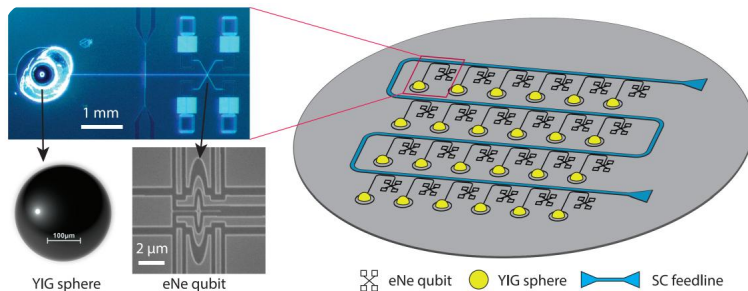
$$N_s \sim 10^3, m_{\text{YIG}} \sim 2.7 \text{ mg}$$

Optimistic – improvements to $N_s, m_{\text{YIG}}, p_{\text{dc}}$

$$N_s \sim 10^4, m_{\text{YIG}} \sim 2.7 \text{ g}$$

Each tile can achieve sensitivity beyond SQL

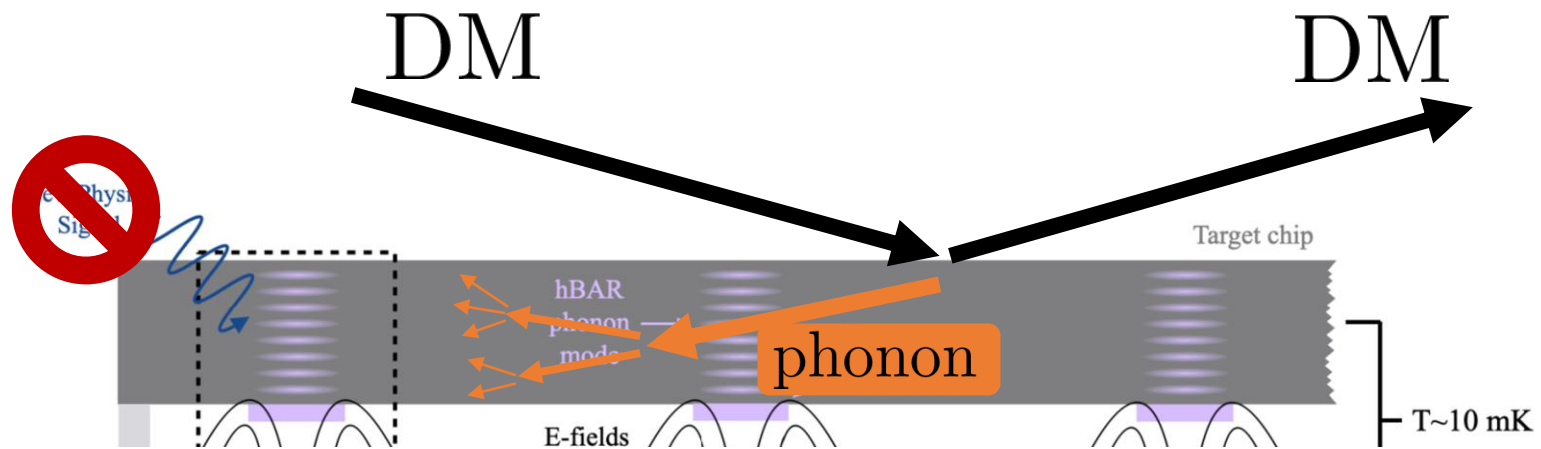
$$\frac{\text{SNR}}{\text{SNR}_{\text{SQL}}} \sim \left(\frac{10^{-4}}{p_{\text{dc}}} \right)^{\frac{1}{2}} \left(\frac{m_a}{10 \mu\text{eV}} \right)^{\frac{1}{2}}$$



Many open questions...

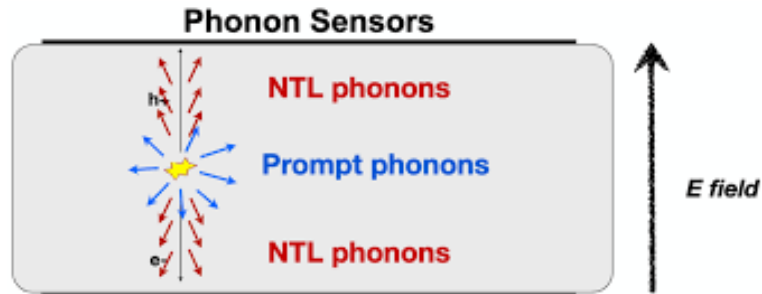
- Improvements to dark count probability?
- Use axion coherence?
- Magnon down-conversion?

Down-Conversion Detection



[\[2410.17308\] Listening For New Physics With Quantum Acoustics](#)

- Linehan, **T. Trickle**, Conner, Ghosh, Lin, Sholapurkar, Cleland



Analogous idea with magnons

Summary

I. Current Status of Direct Detection

- ***DAMIC results motivate thinking about new models and new detection technologies.***

I. Infrared Freeze-In of Magnetic Dipole Dark Matter

- ***Dark sector thermalization allows for IR dominated freeze-in of light, magnetic dipole-coupled dark matter.***

II. Magnon-Based Direct Detection

- ***Magnons are exceptionally sensitive to light, spin-dependent dark matter, including axions. Quantum magnonics is a promising approach for single magnon readout.***

Axion-like Particles

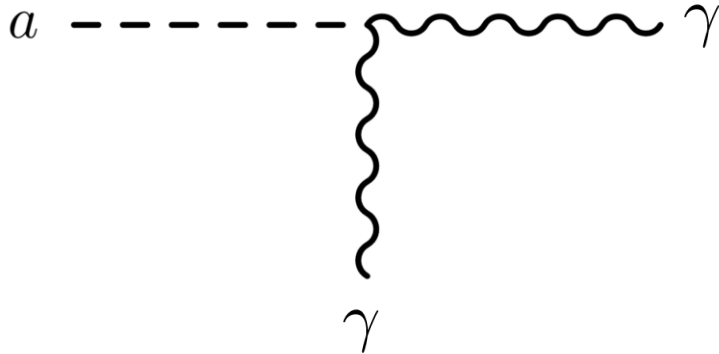


QCD Axion: gluon coupling mandatory, solves strong CP problem

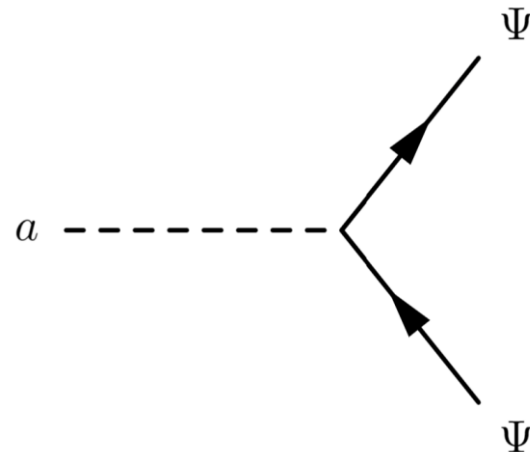
$$\mathcal{L} \supset \frac{a}{f_a} \frac{g^2}{32\pi^2} G_{\mu\nu}^a \tilde{G}_a^{\mu\nu} \quad m_a = \sqrt{\frac{m_u m_d}{(m_u + m_d)^2}} \frac{m_\pi f_\pi}{f_a} \sim 6 \mu\text{eV} \left(\frac{10^{12} \text{ GeV}}{f_a} \right)$$

Axion-like particles: pNG bosons of broken PQ, more diverse phenomenology

$$\mathcal{L} \supset g_{a\gamma\gamma} a F^{\mu\nu} \tilde{F}_{\mu\nu}$$



$$\mathcal{L} \supset g_{a\Psi} \partial_\mu a \bar{\Psi} \gamma^\mu \gamma^5 \Psi \quad (\Psi \in \{e, p, n\})$$

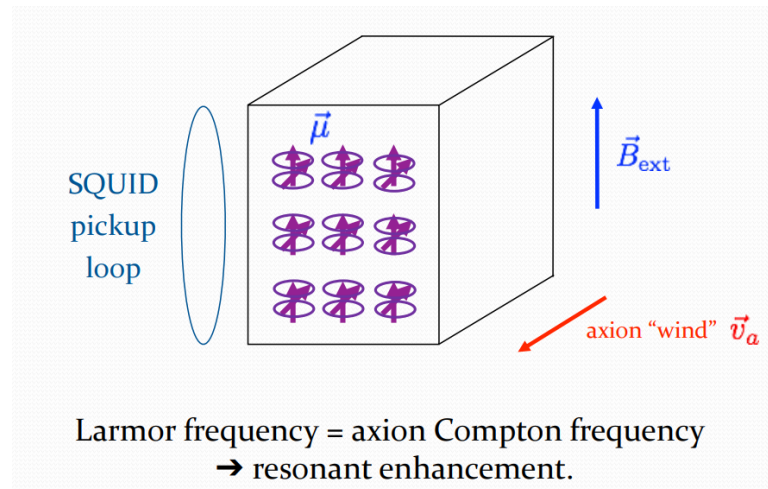


Axion Absorption Into Magnons

$$\mathcal{L} \supset g_{ae} \partial_\mu a \bar{e} \gamma^\mu \gamma^5 e \longrightarrow \delta H \supset g_{ae} \vec{\nabla} a \cdot \vec{S}_e$$

$$a \text{ ----- } \times \text{ ===== magnon}$$

CASPEr Wind – but with electrons



Axion Absorption Into Magnons

First-Principles

Setup

$$H = \sum_{\ell\ell'jj'} \mathbf{S}_{\ell'j'} \cdot \mathbf{J}_{\ell\ell'jj'} \cdot \mathbf{S}_{\ell j}$$

Fit to neutron scattering data

$$\delta H = g_{ae} \vec{\nabla} a \cdot \sum_{\ell j} \vec{S}_{\ell j}^e$$

Fermi's Golden Rule

$$\Gamma = 2\pi \sum_{\nu \mathbf{k}} |\langle \text{magnon} | \delta H | a \rangle|^2 \delta(m_a - \omega_{\nu \mathbf{k}})$$

Selection rules $[H, \delta H] = 0$

No absorption in simplest magnets!

1. External magnetic field
2. Anisotropic exchange interactions
3. Non-degenerate Lande g-factors

[\[2005.10256\] Detectability of Axion Dark Matter with Phonon Polaritons and Magnons](#)

• A. Mitridate, **T. Trickle**, Z. Zhang, K. Zurek

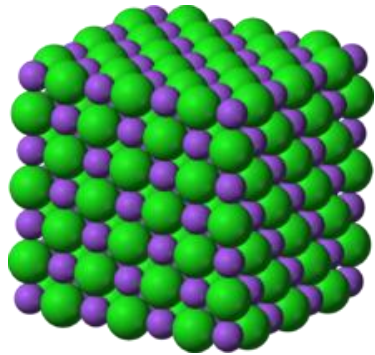
Data-Driven

$$R \simeq \left(\frac{g_{ae} v_{\text{DM}}}{\mu_B} \right)^2 \frac{\rho_{\text{DM}}}{\rho_{\text{T}}} \hat{\mathbf{q}} \cdot \text{Im} \left(-\mu^{-1} \right) \cdot \hat{\mathbf{q}}$$

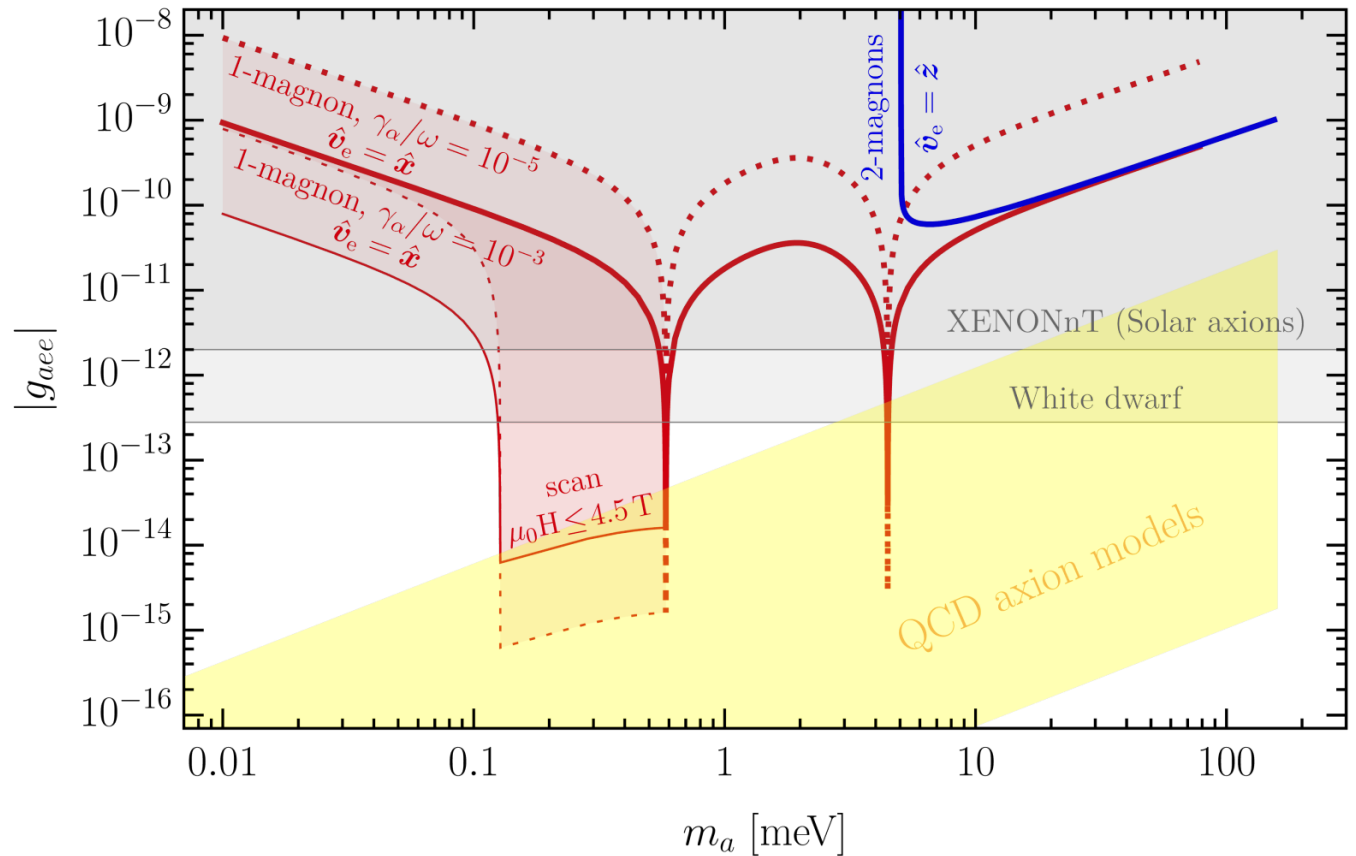
[\[2312.11601\] Physical Signatures of Fermion-Coupled Axion Dark Matter](#)

• A. Berlin, A. Millar, **T. Trickle**, K. Zhou

Axion Absorption Into Magnons

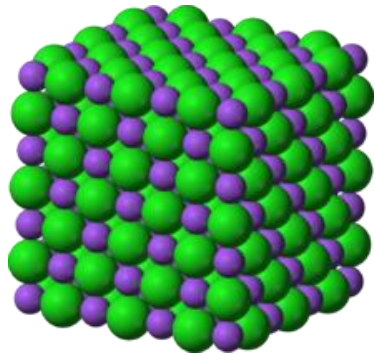


NiO

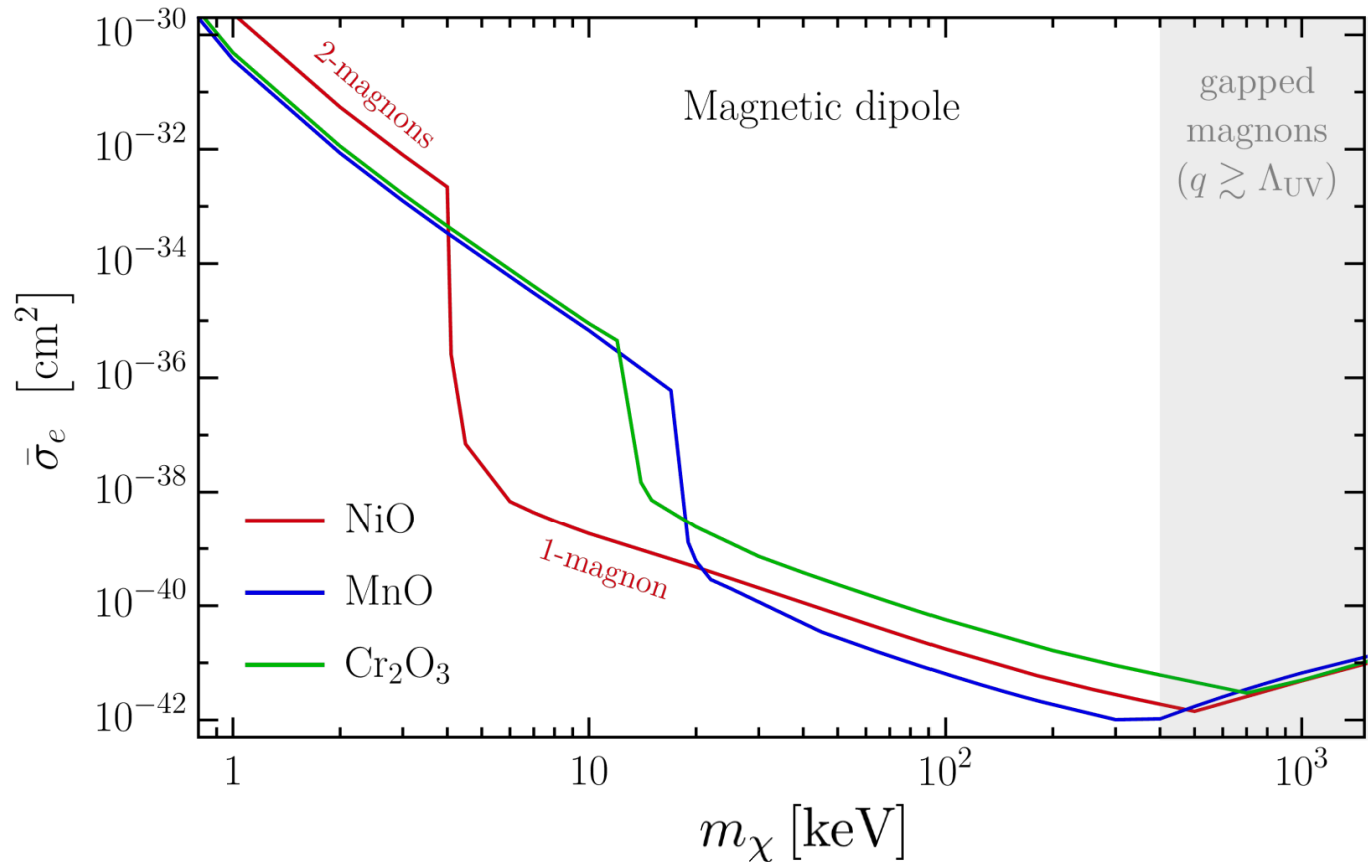


[\[2411.11971\] Hunting axion dark matter with anti-ferromagnets: a case study with nickel oxide](#)

Sensitivity To Dark Matter Scattering

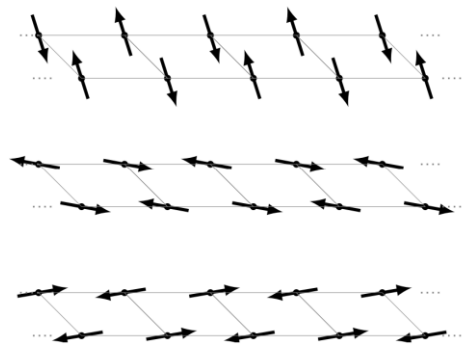


NiO

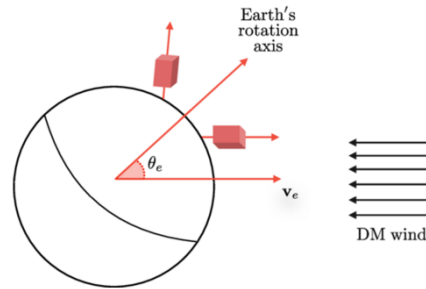


[\[2210.13516\]](#) Optimal anti-ferromagnets for light dark matter detection

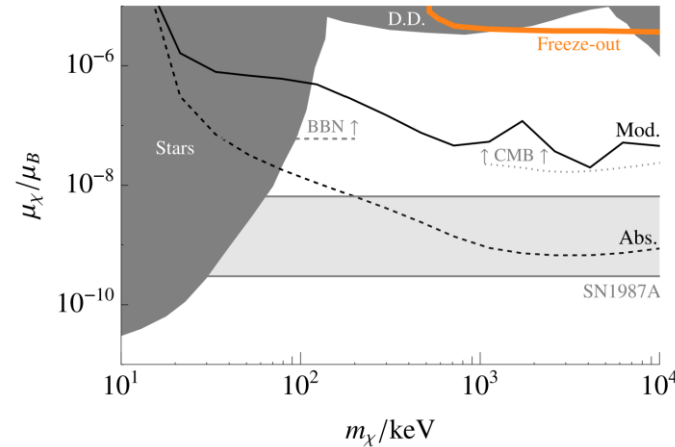
Sensitivity To Dark Matter Scattering



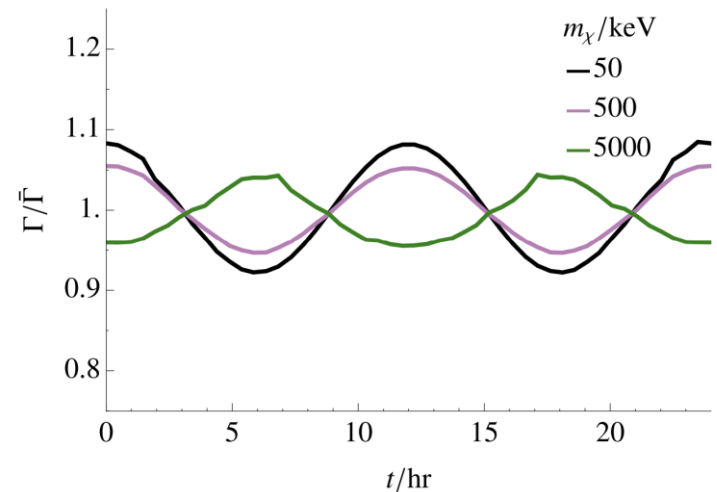
Quasi-2D material



Sensitivity



Daily modulation effects



[\[2501.18120\] Spin-dependent dark matter scattering in quasi-two-dimensional magnets](#)

The Dark Matter Scattering Rate

First-Principles

$$\Gamma = 2\pi \sum_{\nu \mathbf{k}} |\langle \nu \mathbf{k} | H_{\text{int}} | 0 \rangle|^2 \delta(\omega_{\nu \mathbf{k}} - \omega_{\mathbf{q}}) \quad + \quad H_{\text{int}} \sim \sum_{\ell j} \mathcal{O}_{\ell j}^{\chi} \cdot \mathbf{S}_{\ell j}^e$$

Derived from high-energy theory

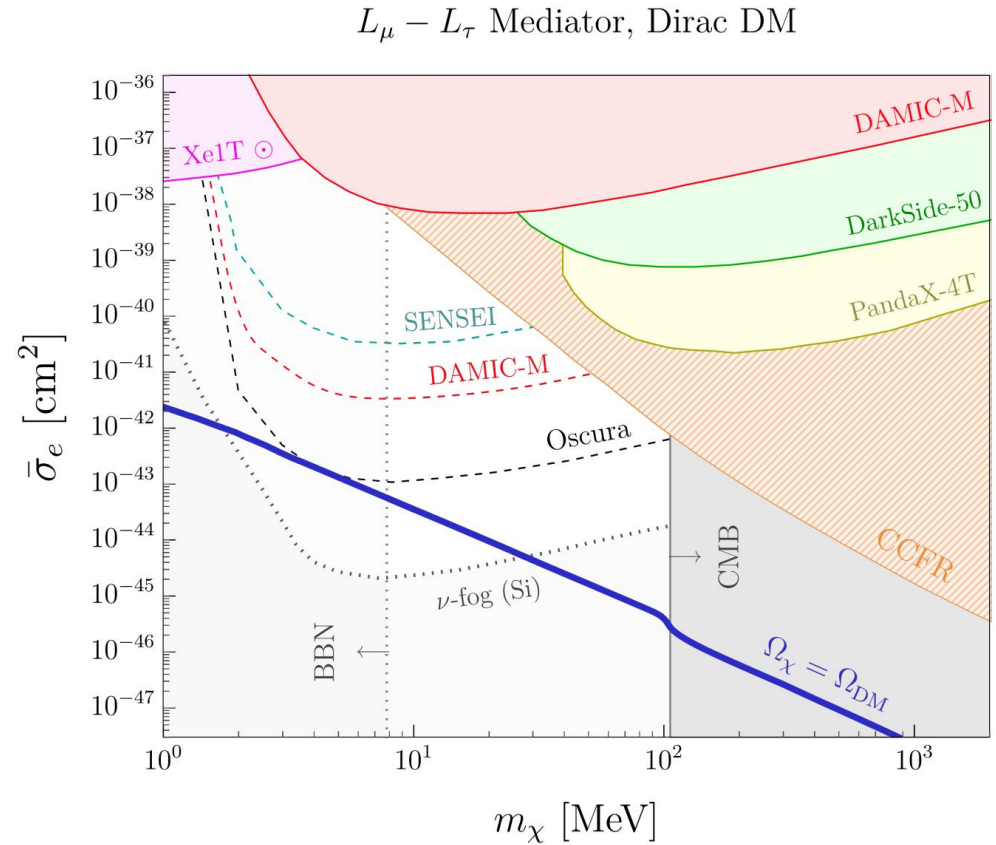
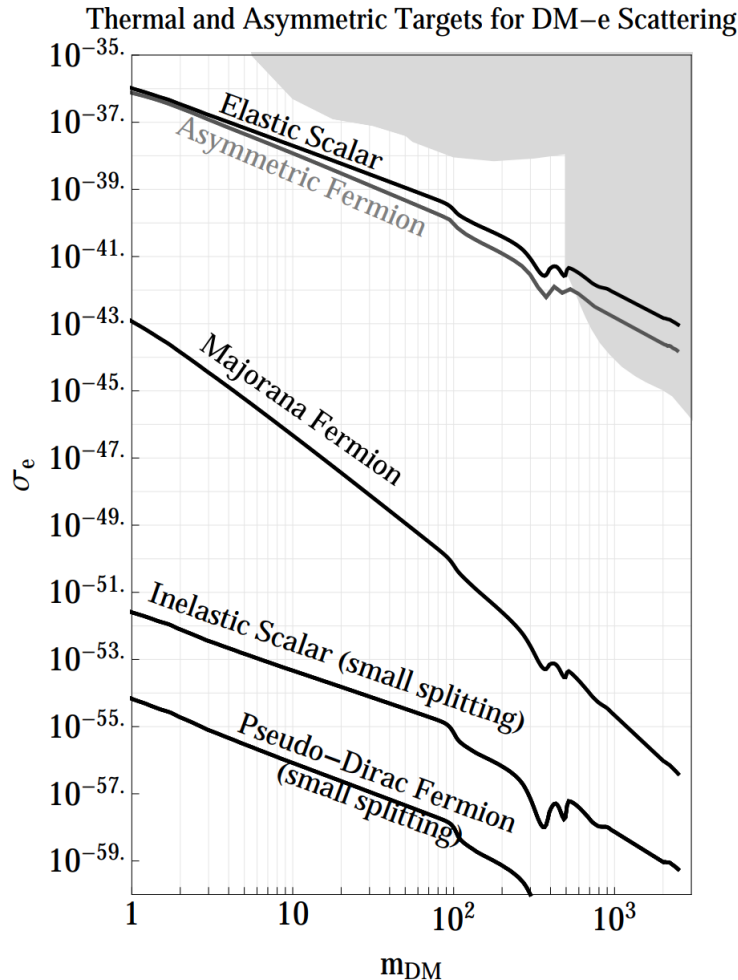
Magnon modes derived from diagonalizing Heisenberg Hamiltonian

$$H = \sum_{\ell \ell' j j'} \mathbf{S}_{\ell' j'} \cdot \mathbf{J}_{\ell \ell' j j'} \cdot \mathbf{S}_{\ell j} \quad S_{lj} = \mathbf{R}'(\mathbf{x}_{lj}) \left[\sqrt{\frac{S_j}{2}} \left(\mathbf{r}_j^* \hat{a}_{lj} + \mathbf{r}_j \hat{a}_{lj}^\dagger \right) + \mathbf{t}_j \left(S_j - \hat{a}_{lj}^\dagger \hat{a}_{lj} \right) \right]$$

[\[1905.13744\] Detecting Light Dark Matter with Magnons](#)

- **T. Trickle**, Zhang, Zurek

Some (Heavy Mediator) Motivated Models



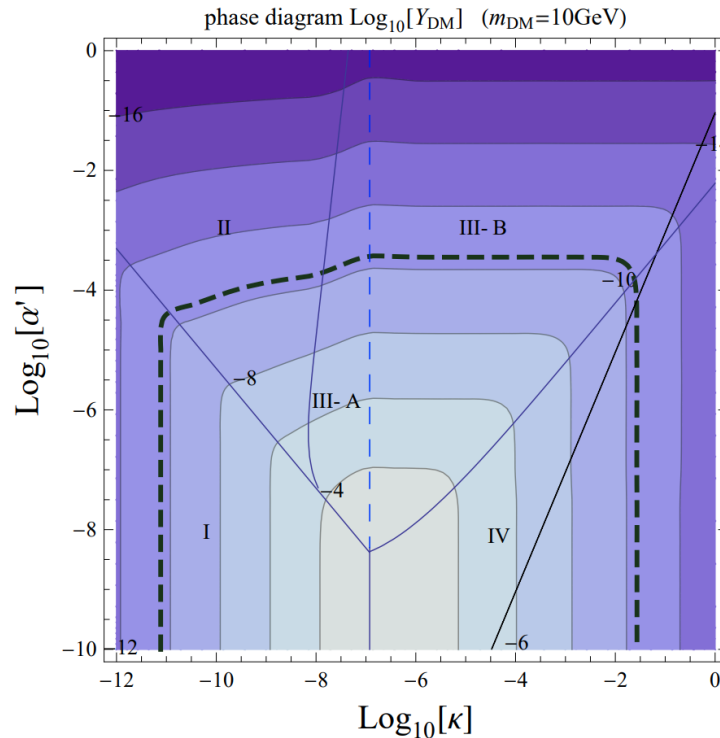
[\[2603.03444\] New Thermal-Relic Targets for sub-GeV Dark Matter Direct Detection](#)

[\[1707.04591\] US Cosmic Visions: New Ideas in Dark Matter 2017: Community Report](#)

[\[2505.04626\] Testing Thermal-Relic Dark Matter with a Dark Photon Mediator](#)

The Mesa Diagram: Why Freeze-In Is Special

$$\mathcal{L} \supset A'_\mu \left[g_\chi (\bar{\chi} \gamma^\mu \chi) + \varepsilon e (\bar{e} \gamma^\mu e) \right]$$



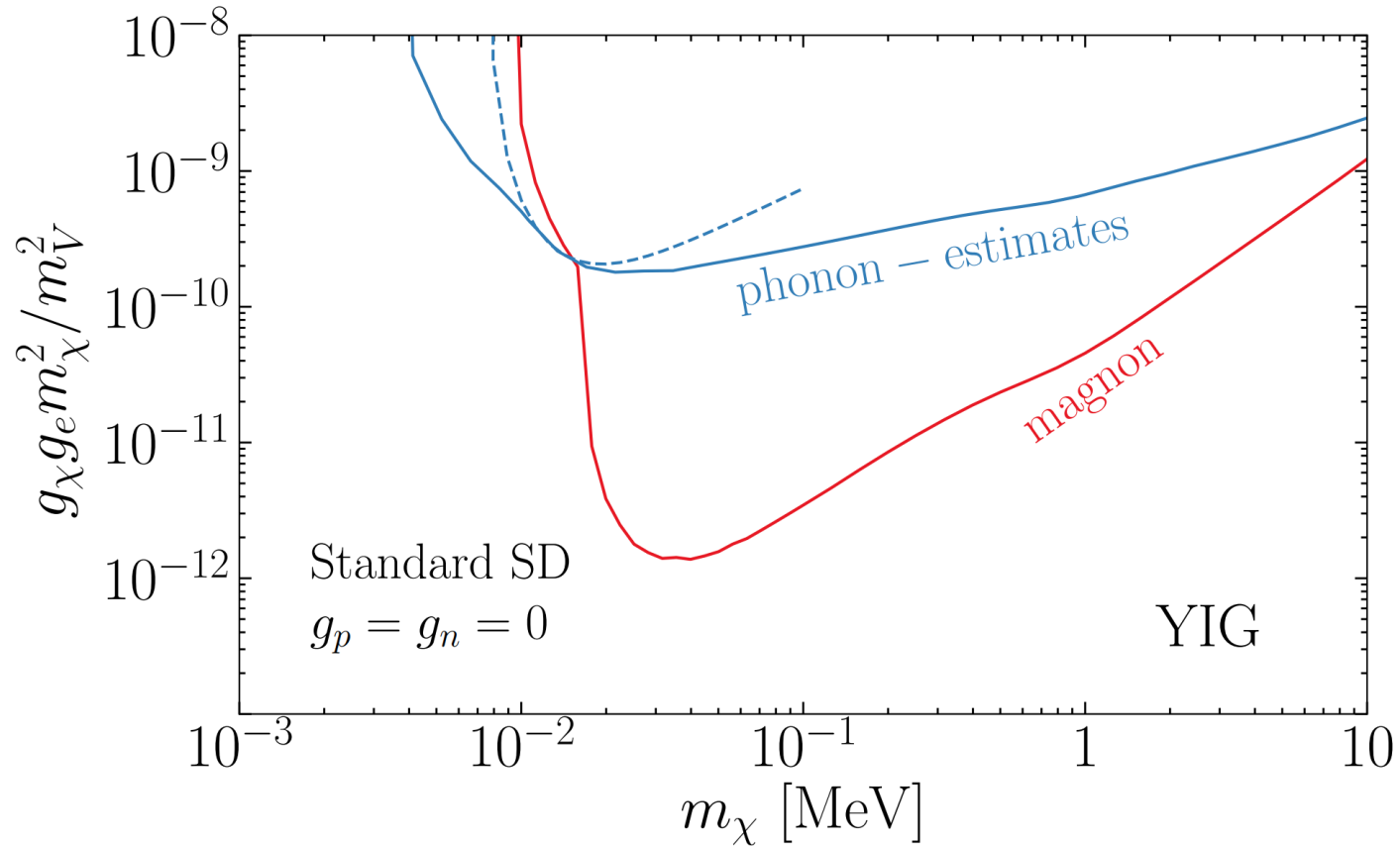
$$\kappa \propto \sqrt{\bar{\sigma}_e}$$

$$\alpha' = \frac{g_\chi^2}{4\pi}$$

[\[1112.0493\] The Four Basic Ways of Creating Dark Matter Through a Portal](#)

SD Dominance of Magnon Scattering

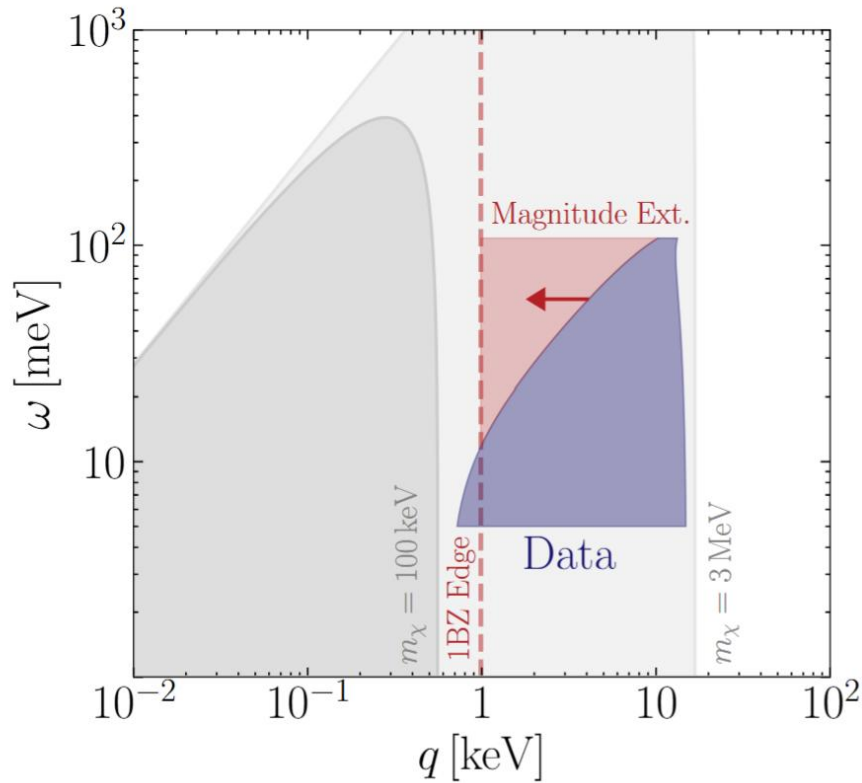
$$\mathcal{L} \supset g_\chi V_\mu \bar{\chi} \gamma^\mu \gamma^5 \chi + g_e V_\mu \bar{e} \gamma^\mu \gamma^5 e$$



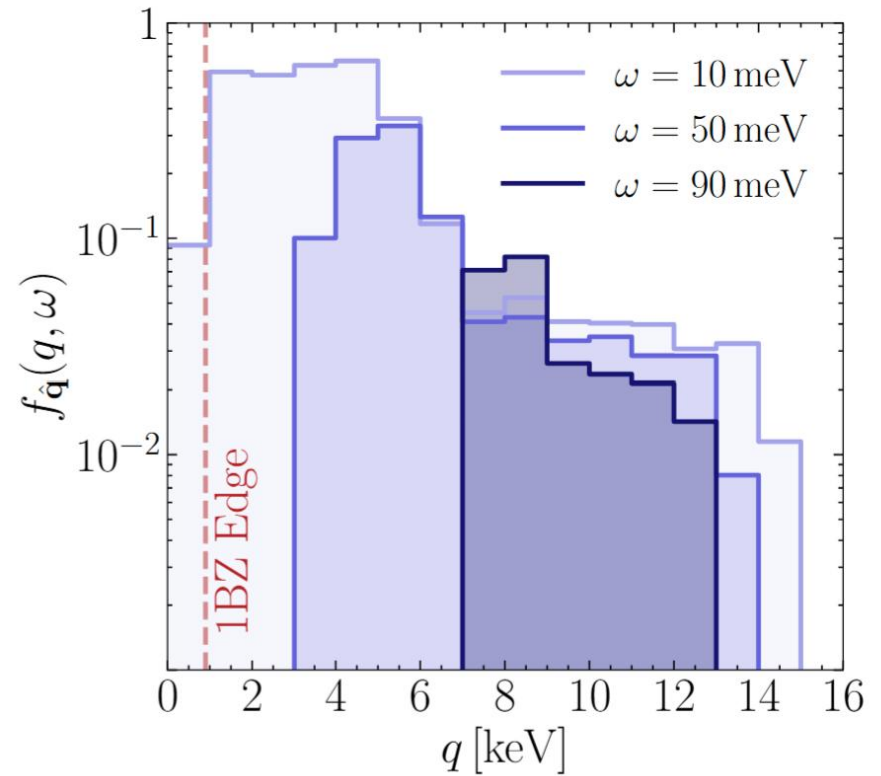
[2009.13534] Effective Field Theory of Dark Matter Direct Detection With Collective Excitations

• T. Trickle, Zhang, Zurek

A Neutron Scattering Dataset



Kinematic coverage



Angular coverage

Additional Interesting Directions

Calibrating results to data

[\[2101.08275\] Dark matter-electron scattering in dielectrics](#)

[\[2101.08263\] Determining Dark Matter-Electron Scattering Rates from the Dielectric Function](#)

Dark photon scattering rate

$$\Gamma(\mathbf{v}_\chi) = \int \frac{d^3\mathbf{q}}{(2\pi)^3} |V(\mathbf{q})|^2 \left[2 \frac{q^2}{e^2} \operatorname{Im} \left(-\frac{1}{\epsilon(\mathbf{q}, \omega_{\mathbf{q}})} \right) \right]$$

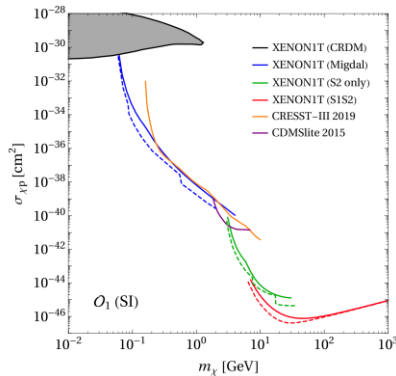
measurable

Other physical effects

Migdal Effect

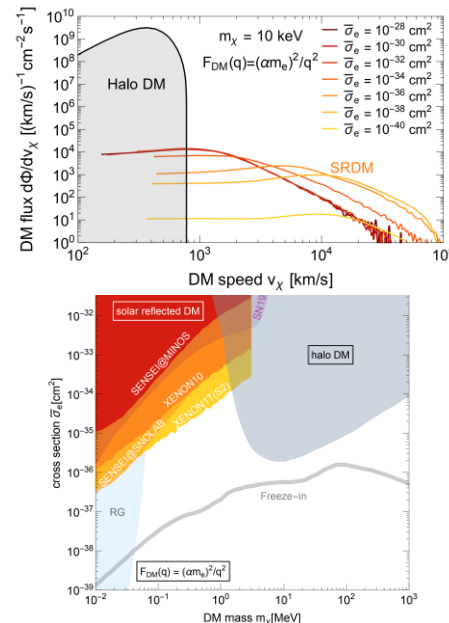
[\[1908.10881\] On the relation between Migdal effect and dark matter-electron scattering in isolated atoms and semiconductors](#)

[\[2210.06490\] The Migdal Effect in Semiconductors for Dark Matter with Masses below \$\sim 100\$ MeV](#)



Boosted Dark Matter

[\[2404.10066\] Solar reflection of dark matter with dark-photon mediators](#)

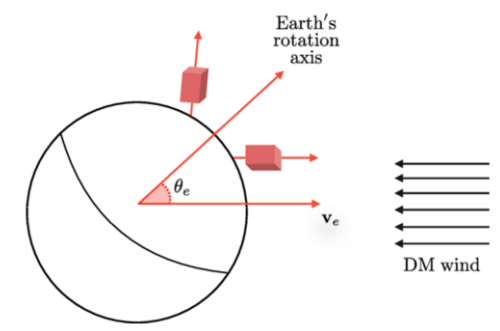
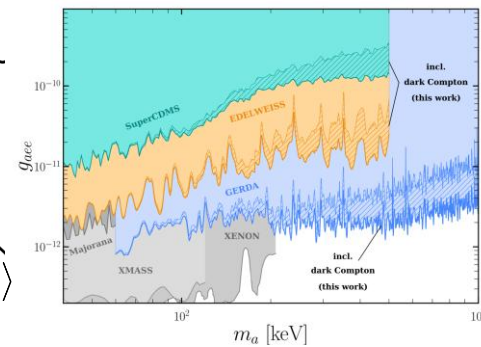
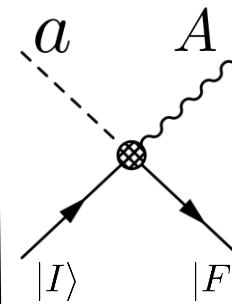


Dark Thomson

[\[2109.08168\] Impact of Dark Compton Scattering on Direct Dark Matter Absorption Searches](#)

[\[2407.14598\] The Non-Relativistic Effective Field Theory Of Dark Matter-Electron Interactions](#)

• G. Krnjaic, D. Rocha, **T. Trickle**



Daily Modulation

[\[2102.09567\] Directional Detectability of Dark Matter With Single Phonon Excitations: Target Comparison](#)

• A. Coskuner, **T. Trickle**, Z. Zhang, K. Zurek

[\[2212.04505\] Directional detection of dark matter with anisotropic response functions](#)

High-Frequency GWs

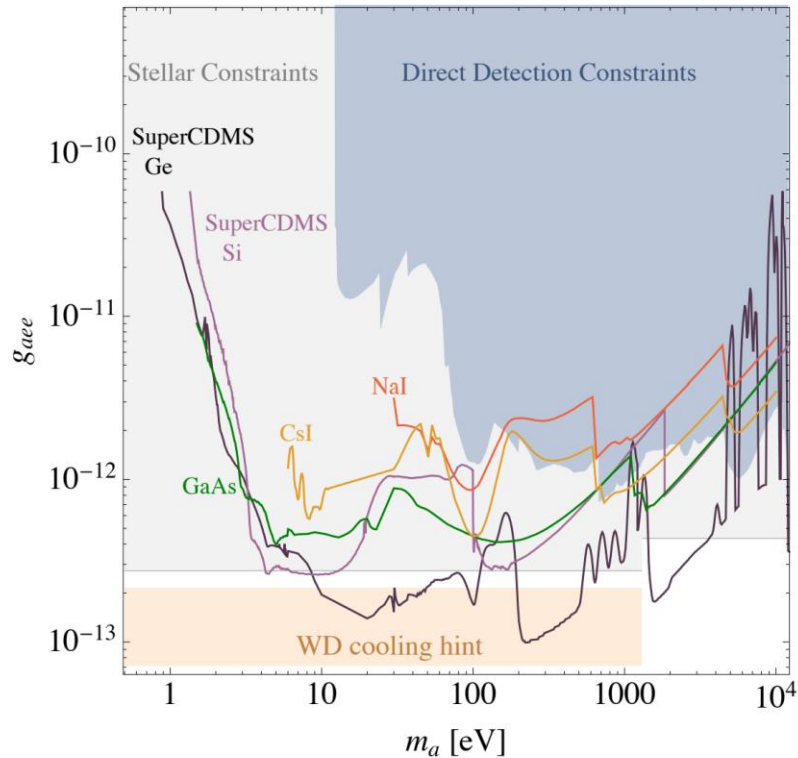
[\[2311.17147\] Searching for High Frequency Gravitational Waves with Phonons](#)

• Y. Kahn, J. Schutte-Engel, **T. Trickle**

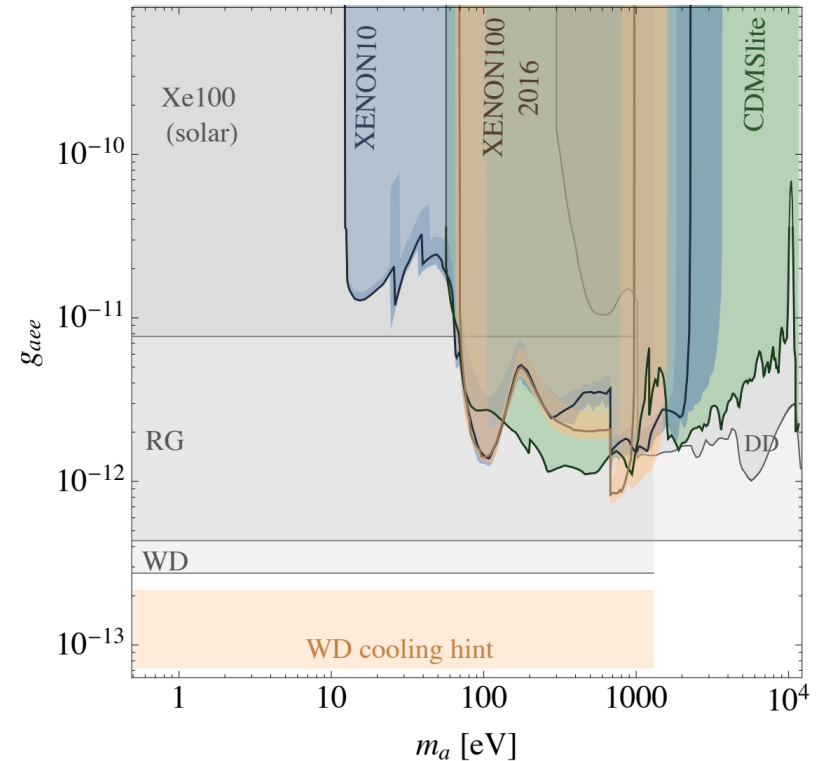
The Search For Light Dark Matter

ttrickle@illinois.edu

Searches For The Axion-Electron Coupling



Semiconductors



Noble Liquid

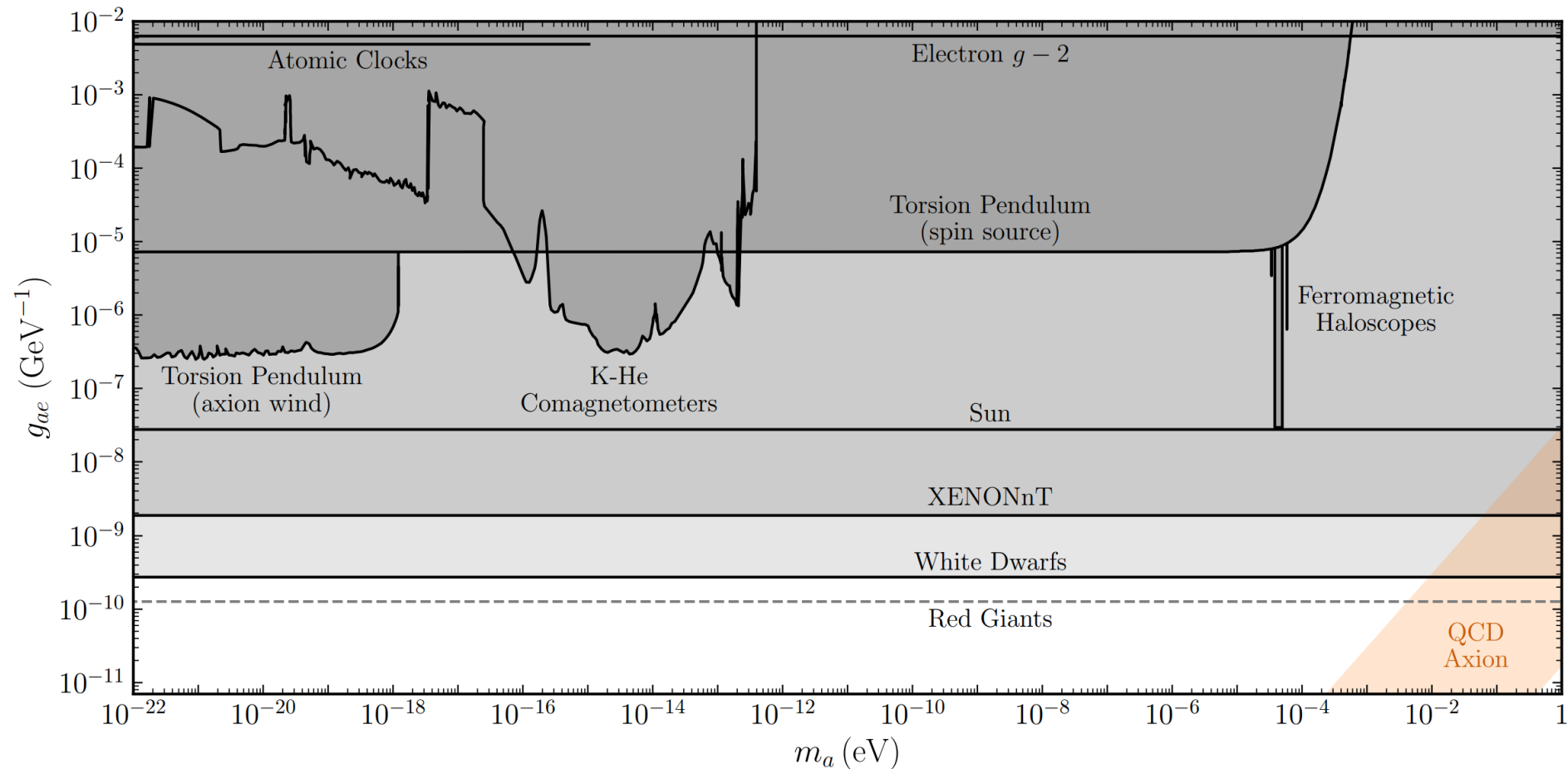
[\[1608.02123\] Searching for Dark Absorption with Direct Detection Experiments](#)

$$R \simeq \left(\frac{g_{ae} m_a}{e} \right)^2 \frac{\rho_{\text{DM}}}{\rho_{\text{T}}} \times \begin{cases} 3 \operatorname{Im} [\varepsilon(m_a)] & (\text{unpolarized target}) \\ \operatorname{Im} \left[\frac{-1}{\varepsilon(m_a)} \right] & (\text{polarized target, spin splitting} \gg m_a) \end{cases}$$

[\[2312.11601\] Physical Signatures of Fermion-Coupled Axion Dark Matter](#)

- A. Berlin, A. Millar, **T. Trickle**, K. Zhou

Existing Limits on Axion-Electron Coupling

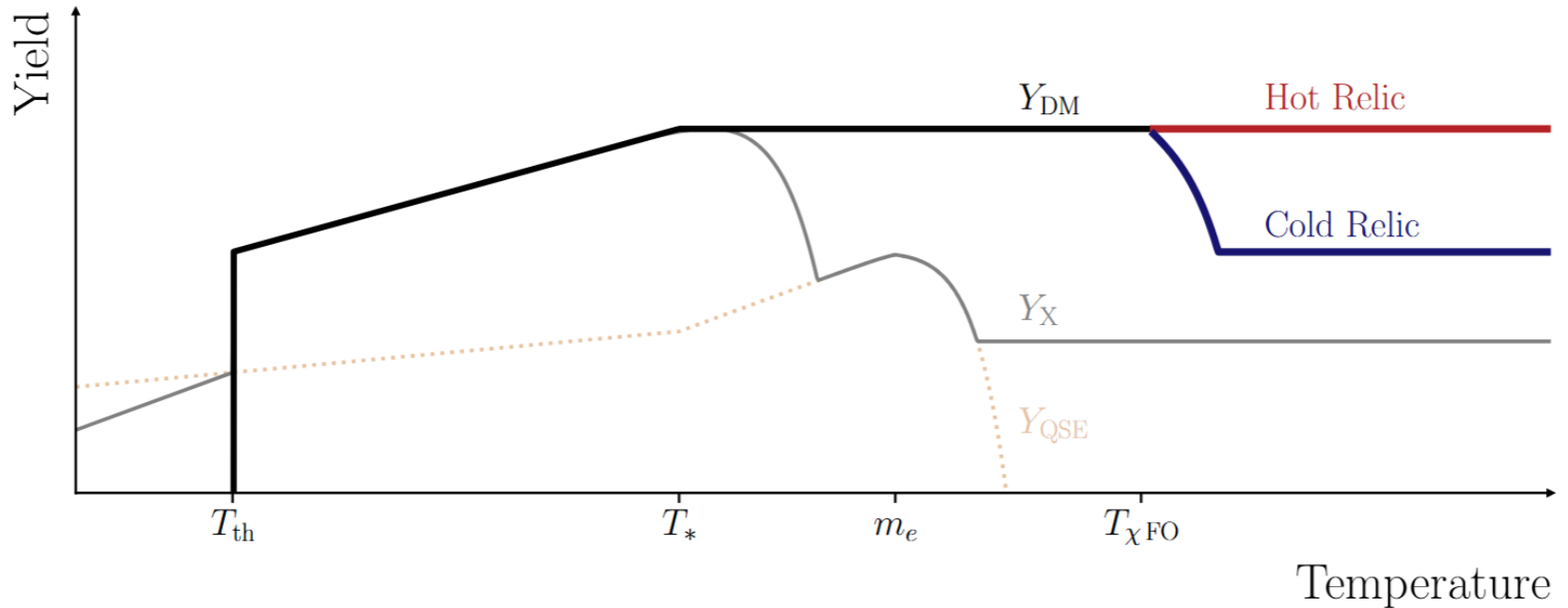


Currently no experiments sensitive enough to search for light axions below stellar cooling limits.

[\[2312.11601\] Physical Signatures of Fermion-Coupled Axion Dark Matter](#)

- Berlin, Millar, **T. Trickle**, Zhou

Quasi-static Equilibrium



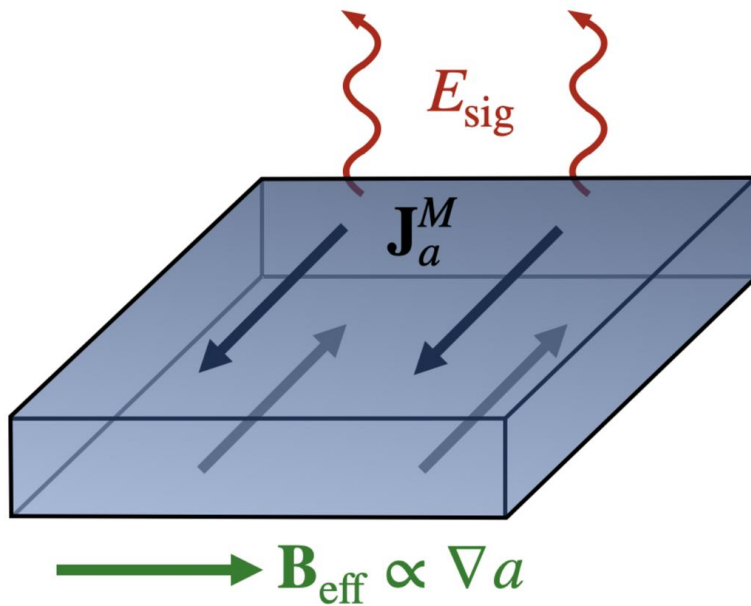
$$\frac{dY_X}{dT} \approx -\frac{c}{sHT} \left[\langle \sigma v \rangle_{XX \rightarrow \text{SM}} (n_X^{\text{eq}})^2 + \langle \sigma v \rangle'_{XX \rightarrow \text{DS}} \left((n_X^{\text{eq}})^2 - n_X^2 \right) \right]$$

$$\frac{dY_X}{dT} \approx -\frac{cs}{HT} \langle \sigma v \rangle'_{XX \rightarrow \text{DS}} [Y_{\text{QSE}}^2 - Y_X^2]$$

Axion Induced Currents

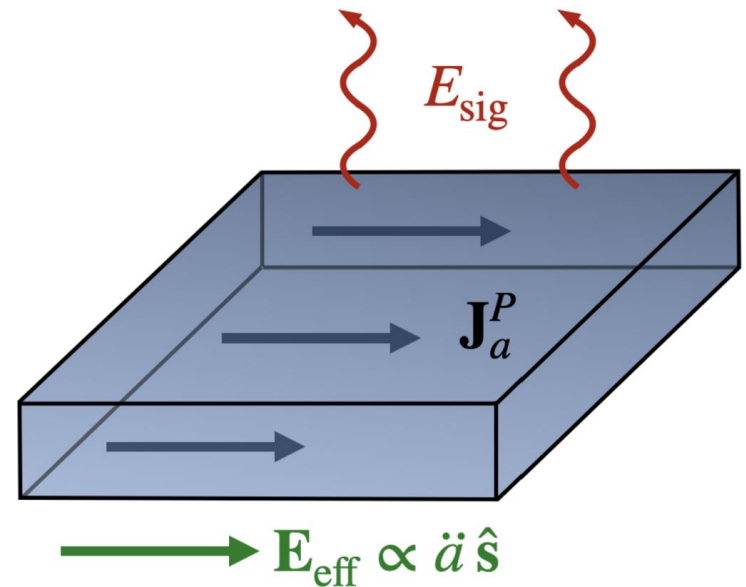
Axion wind term

$$\mathbf{J}_a^M = \nabla \times \left((1 - \mu^{-1}) \mathbf{B}_{\text{eff}} \right)$$



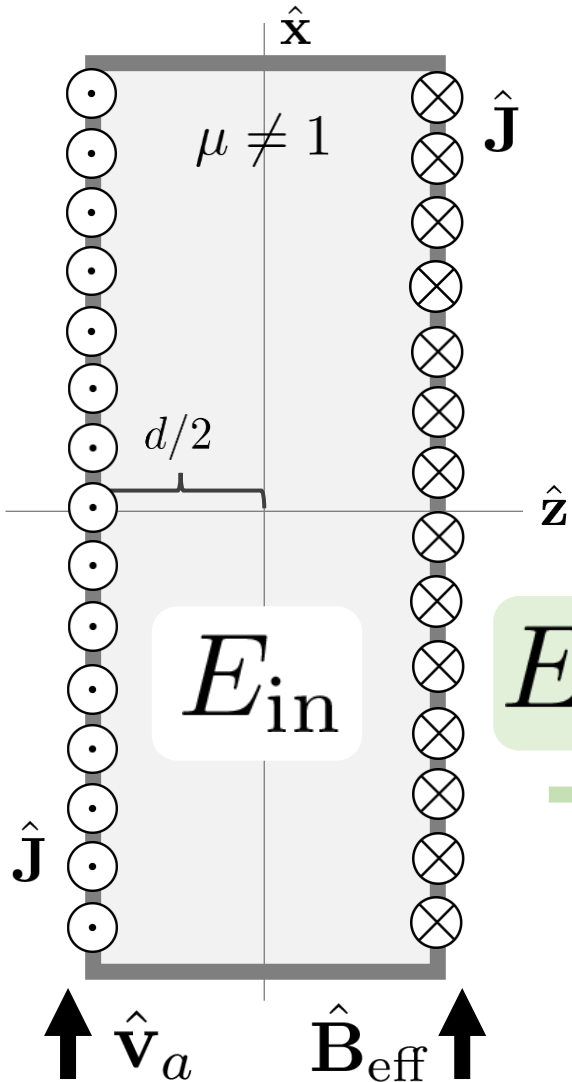
Axio-electric term

$$\mathbf{J}_a^P = (\varepsilon - 1) \partial_t \mathbf{E}_{\text{eff}}$$



Axion Wind Induced Signal

Focus on *Axion wind* induced currents.



Magnetization

$$M_x = \Theta(d/2 - z) \Theta(z + d/2) M_a$$

Surface Current

$$J_y = (\delta(z + d/2) - \delta(z - d/2)) M_a$$

Boundary Conditions

Electric field continuity

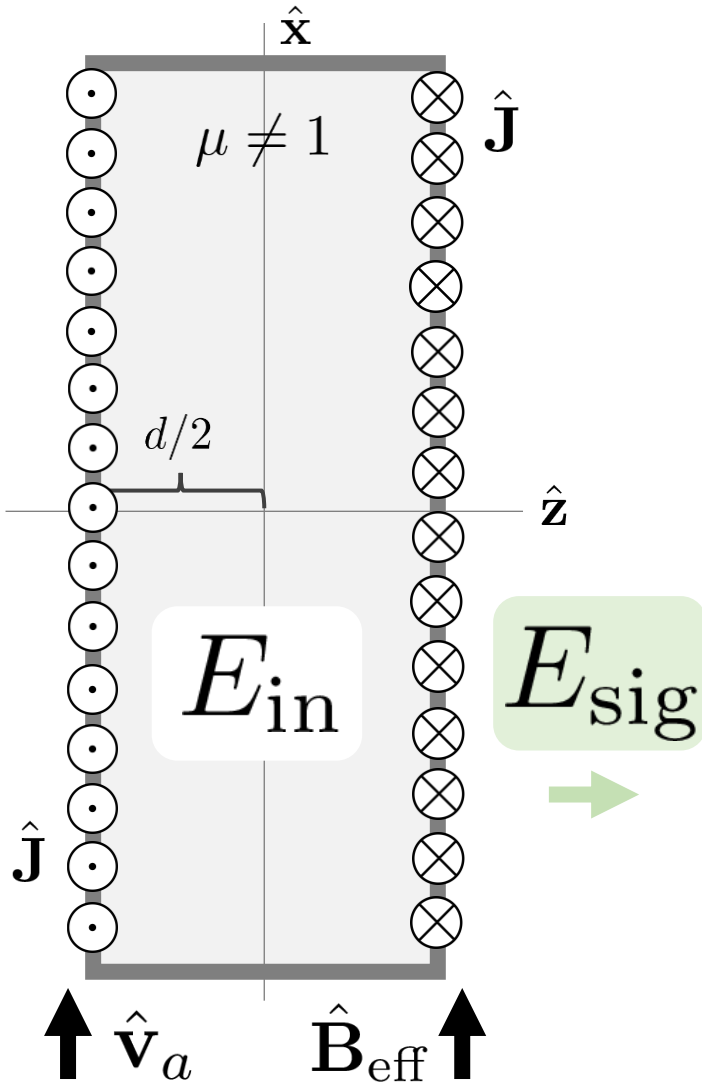
$$E_{\text{in}}^x \sin(n m_a d/2) = E_{\text{sig}}^x e^{i m_a d/2}$$

Magnetic field discontinuity (Amperian loop)

$$-\frac{in}{\mu} E_{\text{in}}^x \cos(n m_a d/2) = E_{\text{sig}}^x e^{i m_a d/2} + M_a$$

Axion Wind Induced Signal

Focus on *Axion wind* induced currents.



$$E_{\text{sig}} = \mathcal{F} \times B_{\text{eff}}$$

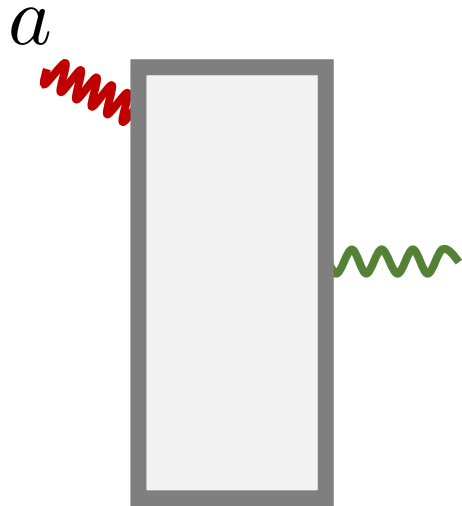
$$\mathcal{F} = \left| \frac{\mu - 1}{\mu + i n \cot(n m_a d/2)} \right|$$

$$n^2 = \epsilon \mu$$

Tunable with external magnetic field.

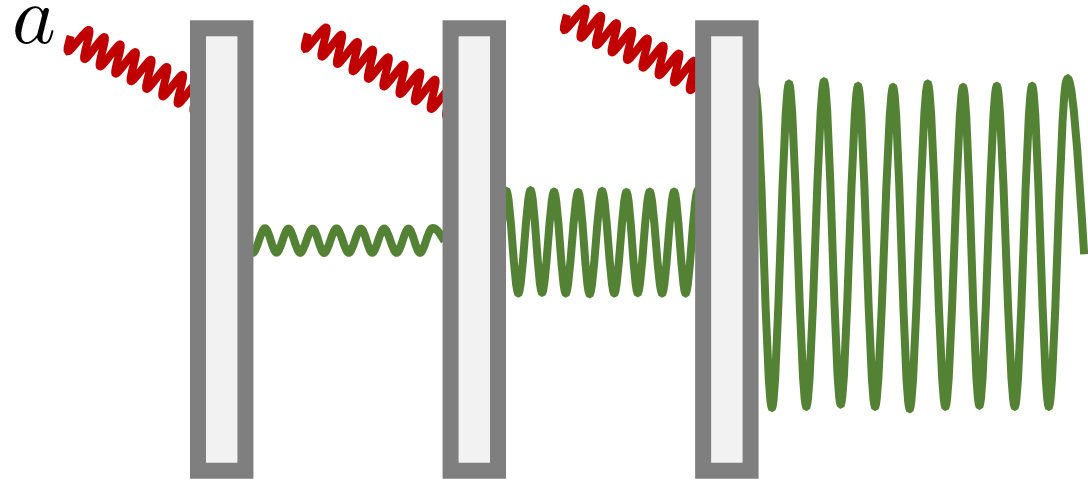
Multi-Layer Coherently Enhances Signal

Single Slab

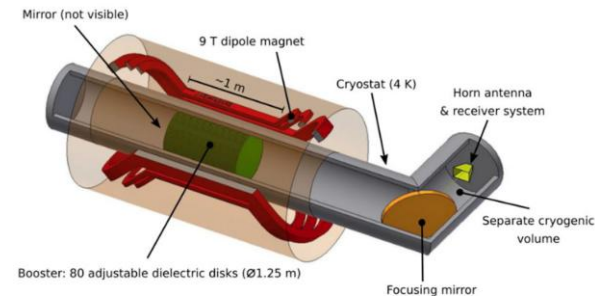


$$P_{\text{sig}} \sim |E_{\text{sig}}|^2 A$$

Many Slabs



$$P_{\text{sig}} \sim N^2 |E_{\text{sig}}|^2 A \quad (\Delta\omega \sim 1/N)$$



Idea behind DALI, LAMPOST, MADMAX, and MuDHI experiments.

Relationship With The Dynamic Structure Factor

$$\frac{d\sigma_n(\mathbf{v})}{d\Omega dE'} = \frac{|\mathbf{p}'|}{|\mathbf{p}|} S_n(\mathbf{q}, \omega_{\mathbf{q}}) \text{ Measurable}$$

Magnetic dipole dark matter model

$$R = \frac{\rho_\chi}{2\pi\rho_T} \frac{g_\chi^2 g_e^2}{m_\chi^3 \gamma_n^2 e^4} \frac{N_f}{\Omega_c} \int d\omega d^3\mathbf{q} \underbrace{g(\mathbf{q}, \omega)}_{\text{Kinematics}} S_n(\mathbf{q}, \omega)$$

Sensitivity and Extrapolation Schemes

