

Exotic structures in the nuclear dipole spectrum

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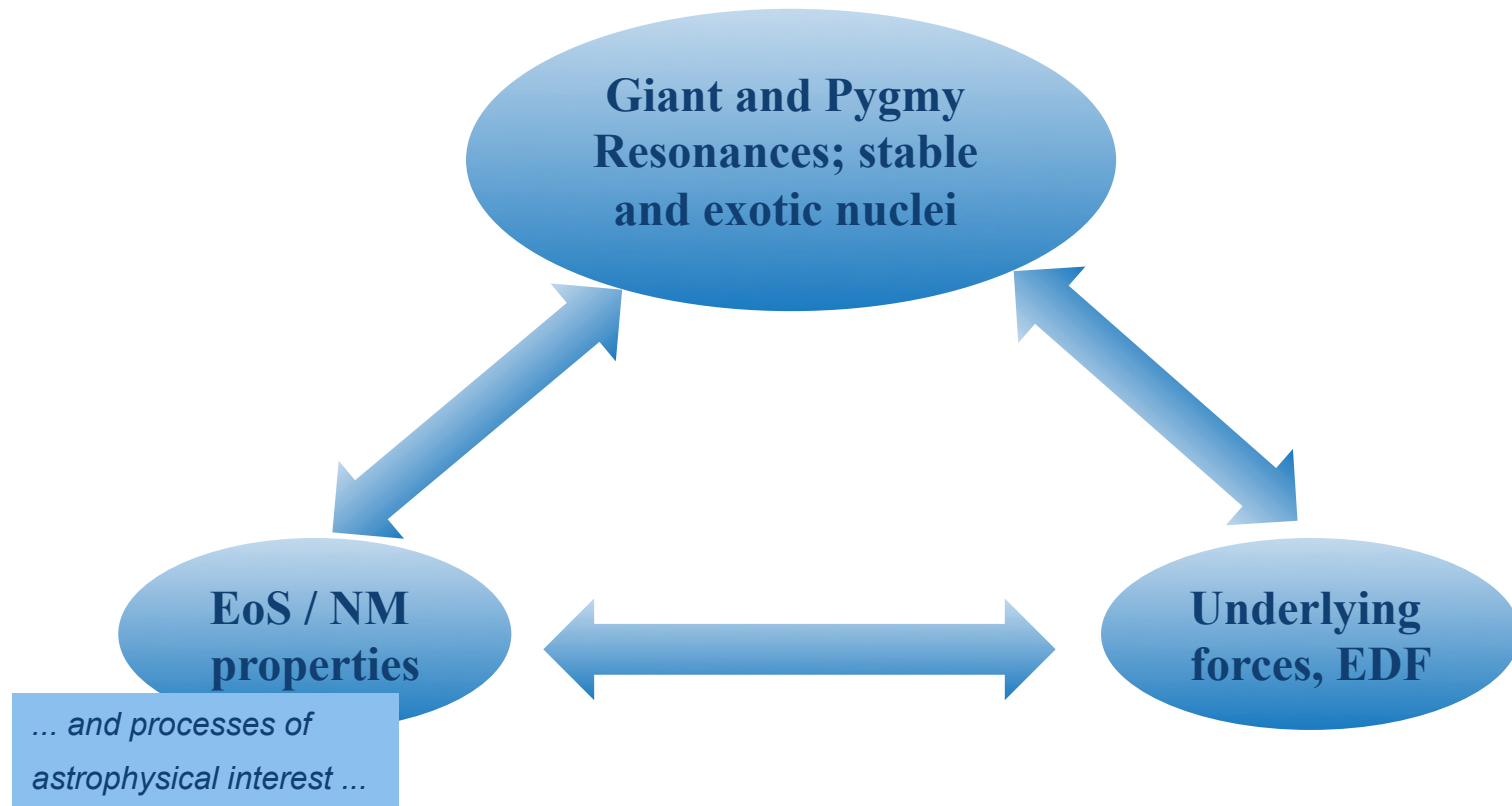
RAON at Science Day



VENI VIDI MANSI



A triangle of interests



Nuclear photoresponse / dipole response

- ❖ Ordinary and exotic features
- ❖ Focusing on:
 - Pygmy “resonance”
 - Isoscalar dipole response

Theory prospects

Summary

Nuclear photoresponse / dipole response

- ❖ Ordinary and exotic features
- ❖ Focusing on:
 - Pygmy “resonance”
 - Isoscalar dipole response

mainly medium-mass, heavy nuclei

Theory prospects

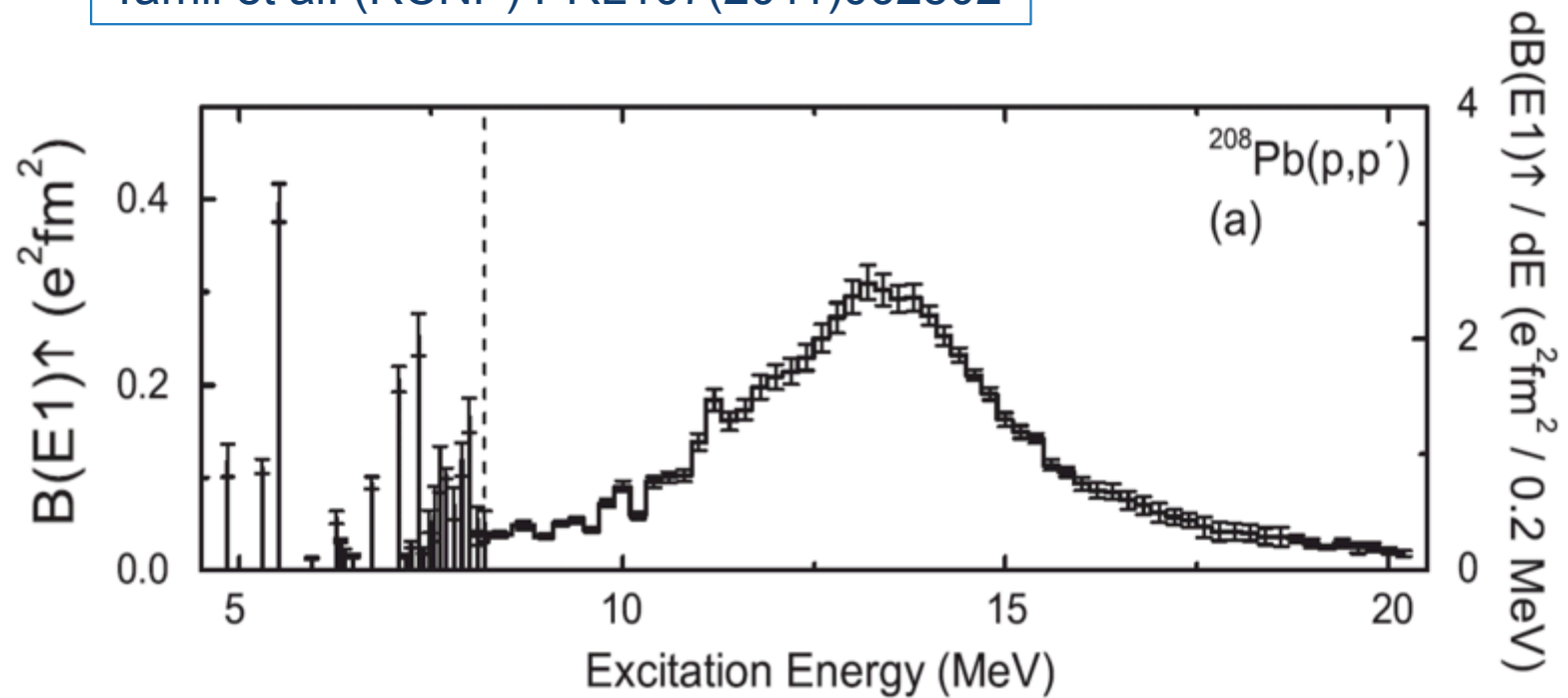
Summary

- ❖ "*Proton pygmy resonances: predictions for **N=20 isotones***" Y. Kim, P. P., Eur. Phys. J. A 52 (2011) 176
- ❖ "*Isoscalar and neutron modes in the E1 spectra of **Ni isotopes** and the relevance of shell effects and the continuum*" P. P., H. Hergert, R. Roth, Phys. Rev. C 92 (2015) 034311
- ❖ "*Low-energy electric dipole response of **Sn isotopes***" P.P., H.Hergert, V.Yu.Ponomarev, R.Roth, Phys. Rev. C 89 (2014) 034306
- ❖ "*Isospin properties of electric dipole excitations in **48Ca***" V.Derya et al., Phys. Lett. B 730 (2014) 288
- ❖ "*Low-energy dipole strength and the critical case of **48Ca***" P.P., H.Hergert, V.Yu.Ponomarev, R.Roth, Phys. Lett. B 709 (2012) 270
- ❖ "*Isoscalar dipole coherence at low energies and forbidden E1 strength*" P.P., V.Yu.Ponomarev, R.Roth, J.Wambach, Eur. Phys. J. A 47 (2011) 14

- HF(B)+(Q)RPA non-relativistic (Gogny, Skyrme)**

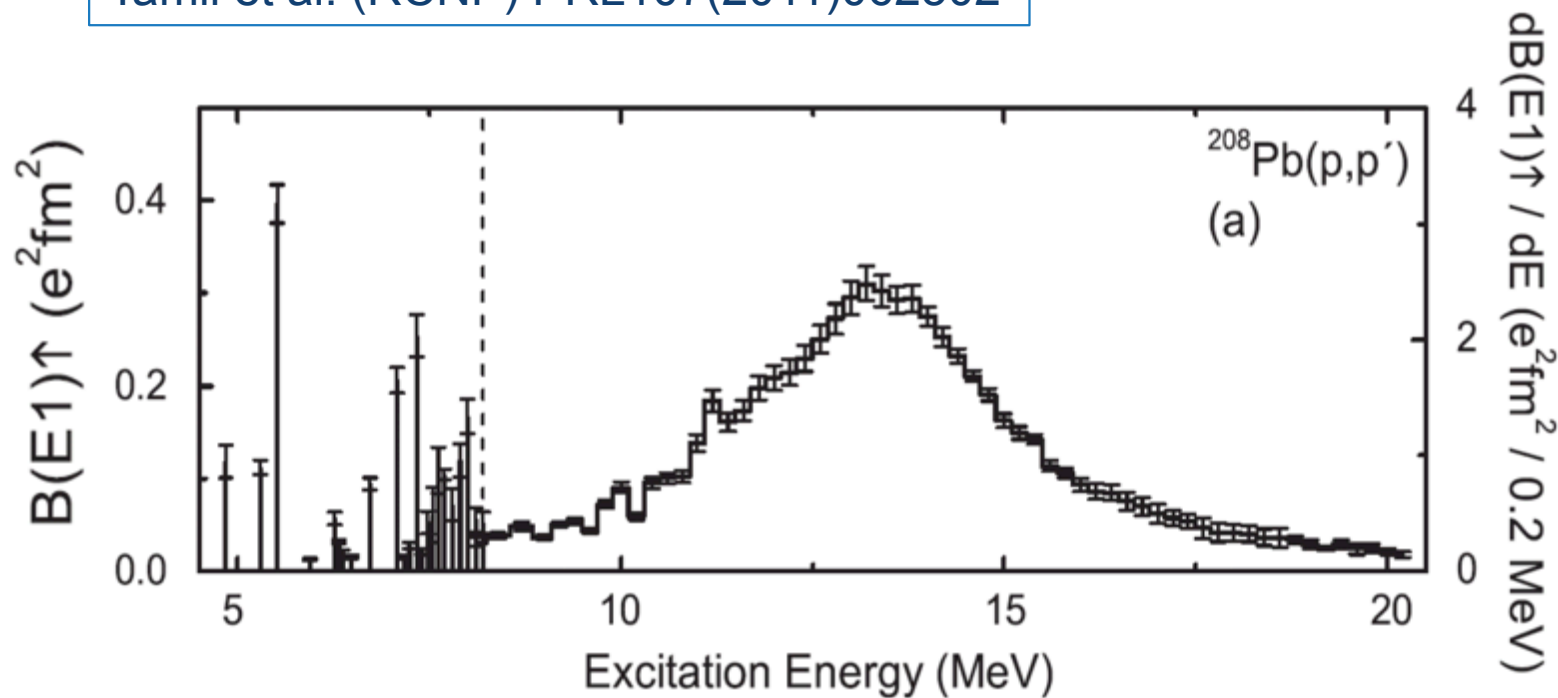
Electric dipole spectrum of ^{208}Pb

Tamii et al. (RCNP) PRL107(2011)062502



Electric dipole spectrum of ^{208}Pb

Tamii et al. (RCNP) PRL107(2011)062502



$$\int \sigma_{\gamma}(E) dE \quad \text{nucleon forces}$$

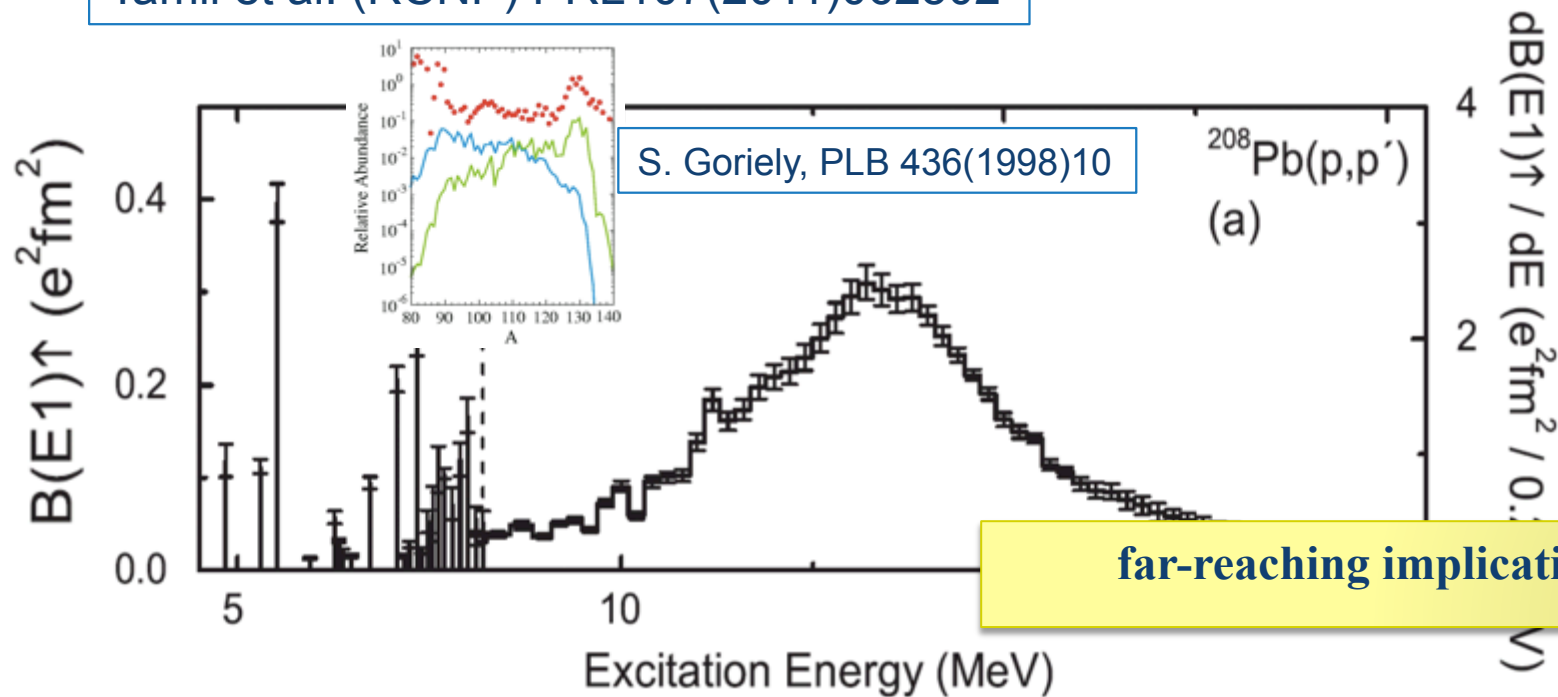
TRK sum

$$\int \frac{\sigma_{\gamma}(E)}{E^2} dE \quad \text{polarizability}$$

cf P.G.Reinhard, W.Nazarewicz, PRC87,014324
(but also: X. Roca-Maza et al., PRC92, 064304)

Electric dipole spectrum of ^{208}Pb

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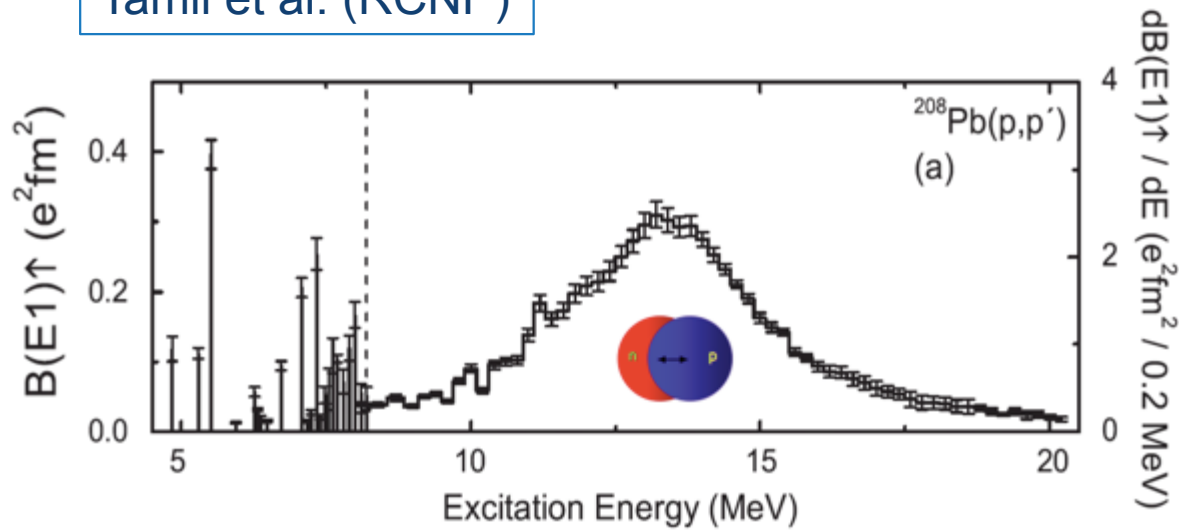
$$\int \sigma_{\gamma}(E) dE \quad \text{nucleon forces}$$

TRK sum

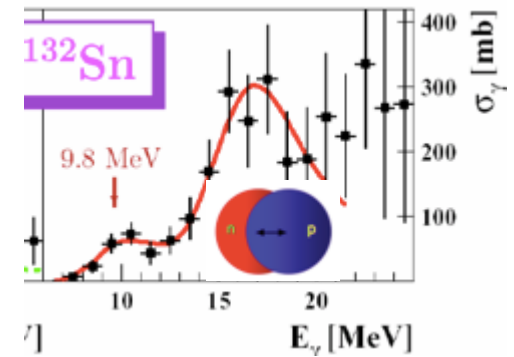
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Tamii et al. (RCNP)

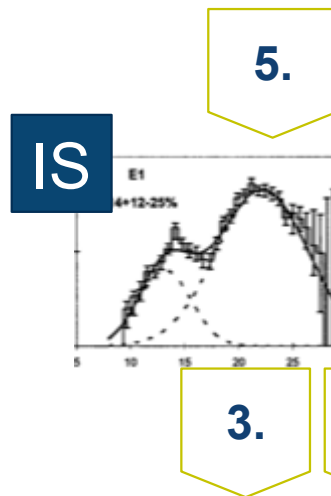
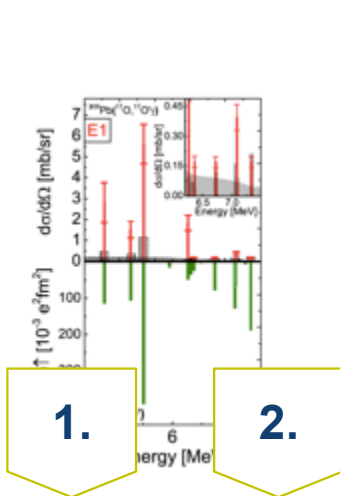


Adrich et al. (GSI)

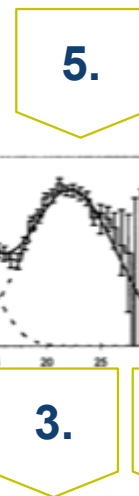


- ❖ Nuclear resonance fluorescence
- ❖ Coulomb excitation incl. inverse kinematics
- ❖ Alpha scattering
- ❖ Proton scattering
- ❖ Gamma-ray spectroscopy following beta decay
- ❖ ...

Electric dipole spectrum of ^{208}Pb



IS



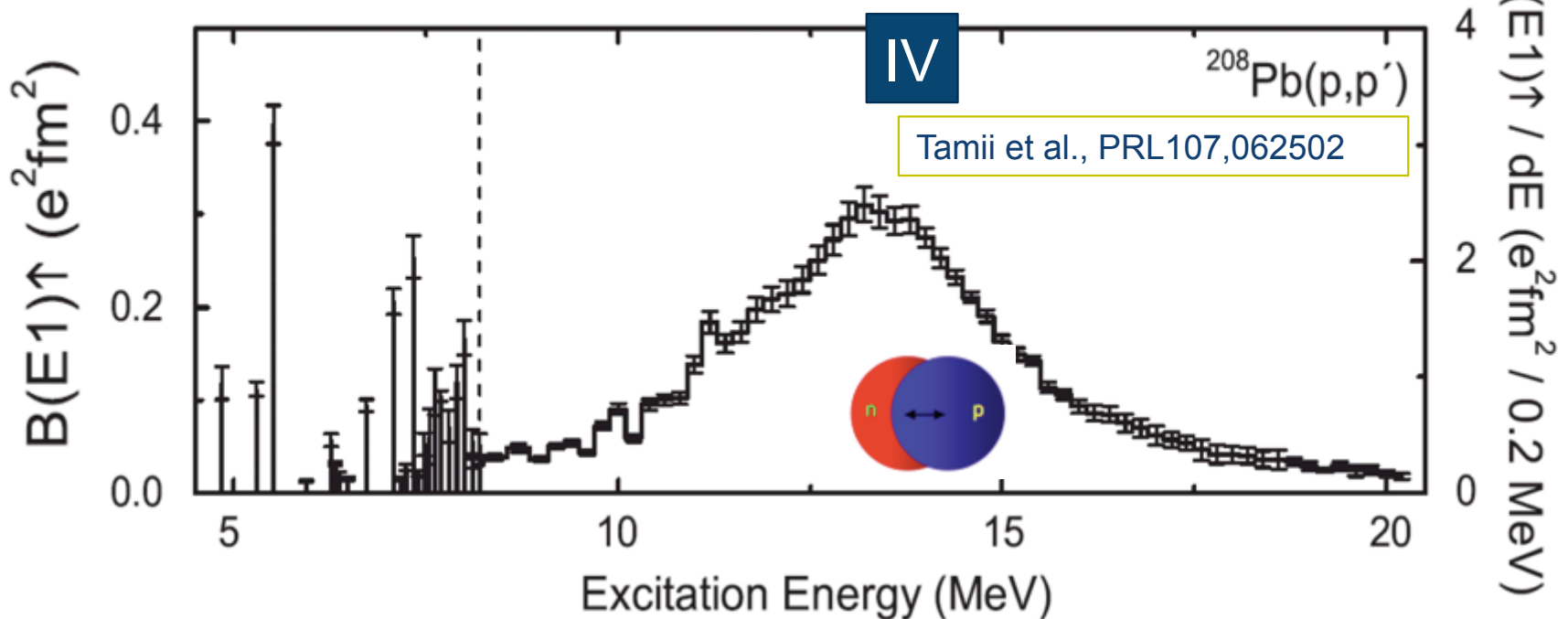
GDR

1,2: Tamii et al., PRL 107(2011)062502
Crespi et al., PRL 113(2014)012501
Poelhakken et al., PLB 278(1992)423

3: Youngblood et al., PRC 69(2004)034315

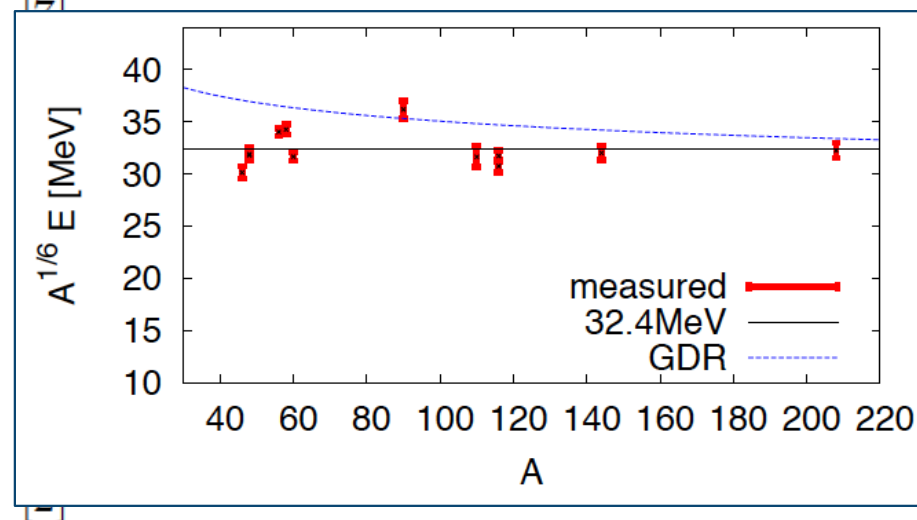
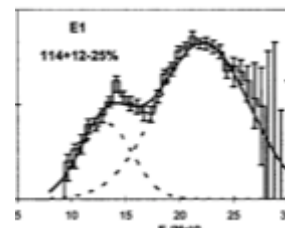
4: GDR (here: Tamii et al.)

5: IS GDR, see 3.



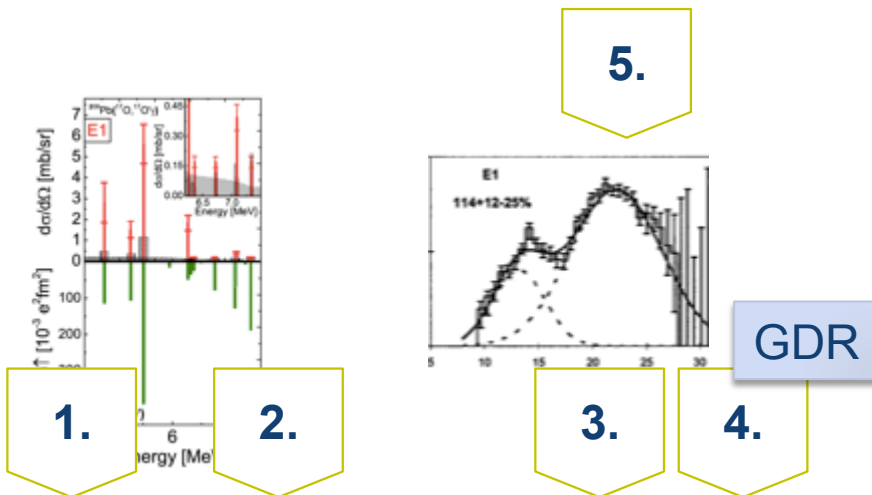
Isoscalar resonance near the GDR

Nucleus	$\frac{N-Z}{A}$	Energy [MeV]	% EWSR	Reference
^{24}Mg	0	$[12.5]$		[6]
^{46}Ti	0.043	15.94 ± 0.31		[5]
^{48}Ti	0.083	$16.75^{+0.31}_{-0.28}$		[5]
^{48}Ca	0.167	$16.69^{+0.19}_{-0.13}$	20^{+12}_{-8}	[7]
^{56}Fe	0.071	17.41 ± 0.20		
^{58}Ni	0.034	17.42 ± 0.25		
^{60}Ni	0.067	16.01 ± 0.20		
^{90}Zr	0.111	17.1 ± 0.4	13 ± 3	
^{110}Cd	0.127	$14.47^{+0.47}_{-0.44}$		
^{116}Cd	0.172	$13.94^{+0.30}_{-0.26}$		
^{116}Sn	0.138	14.38 ± 0.25	25 ± 15	
^{144}Sm	0.138	14.00 ± 0.30	32 ± 15	
^{208}Pb	0.211	13.26 ± 0.30	24 ± 15	



Experiments are quite ahead of theory...

Electric dipole spectrum of ^{208}Pb



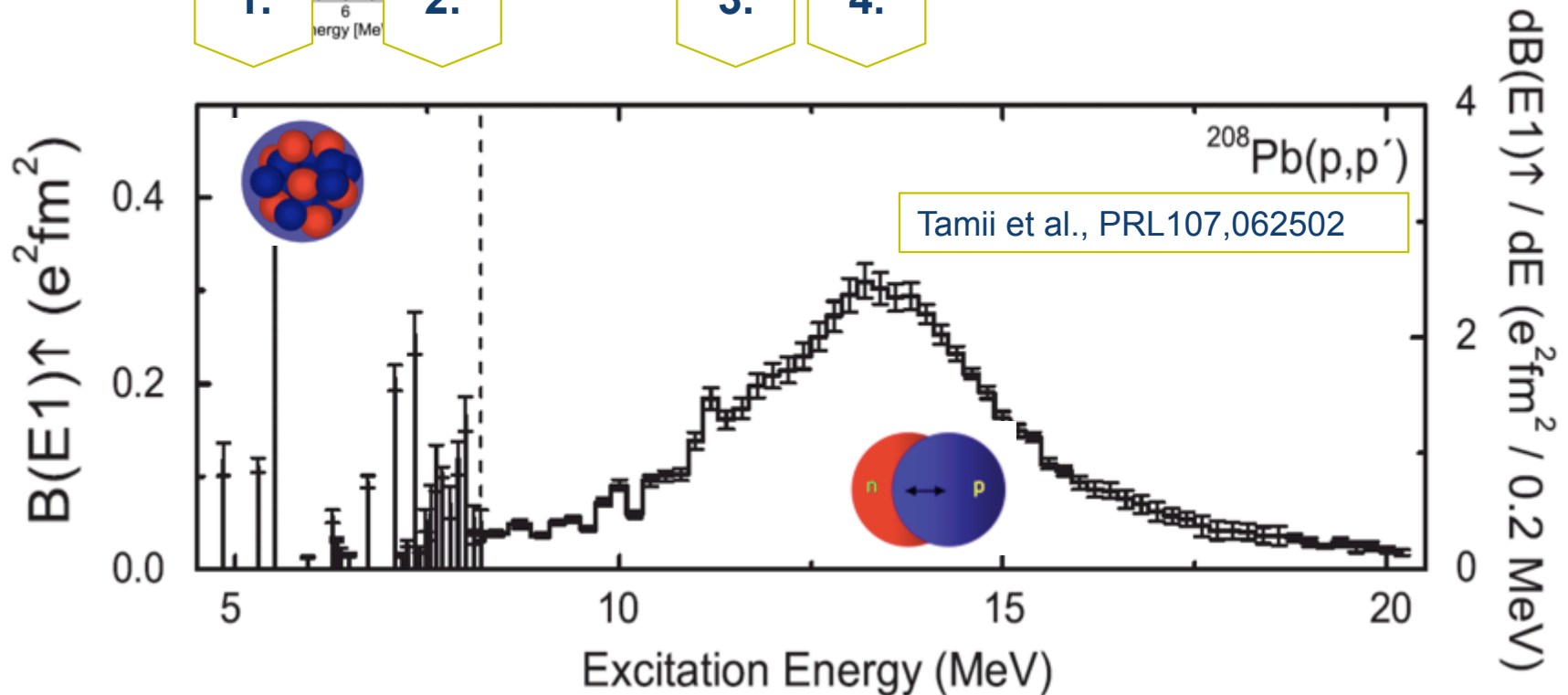
1,2: Tamii et al., PRL 107(2011)062502
Crespi et al., PRL 113(2014)012501
Poelhakken et al., PLB 278(1992)423

3: Youngblood et al., PRC 69(2004)034315

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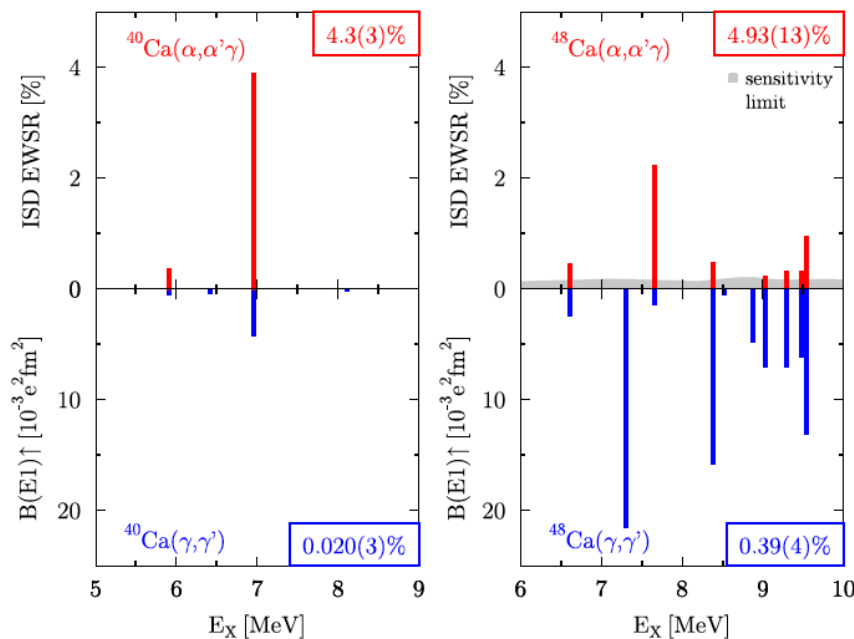
GDR



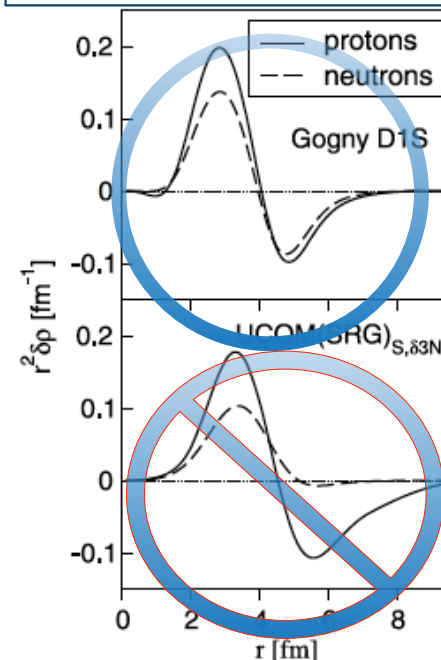
Low-energy dipole response of ^{40}Ca , ^{48}Ca

- ❖ Strong IS transitions (4-5% EWSR) below 9MeV
- ❖ **Weak E1 channel** despite large asymmetry of ^{48}Ca
- ❖ Reproduced, e.g., by the Gogny D1S interaction

V.Derya et al., PLB730,288



PP et al., PLB709,270



Some kind of toroidal/diffuseness oscillation

- $E \sim 6-7$ MeV
- $B(E1) \ll 1 \text{ W.u.}$

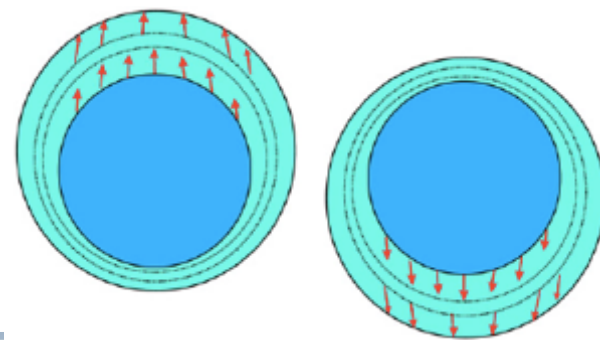
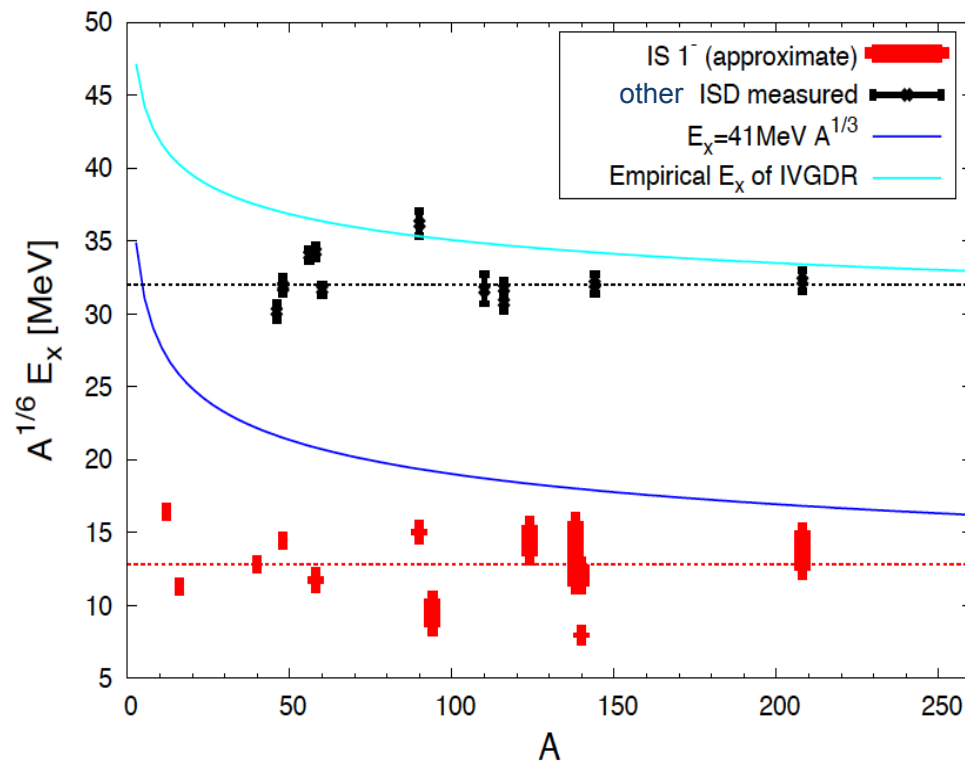
Data for IS dipole transitions from:

- Savran et al., Derya et al., Crespi et al., Poelheken et al., Harakeh et al.

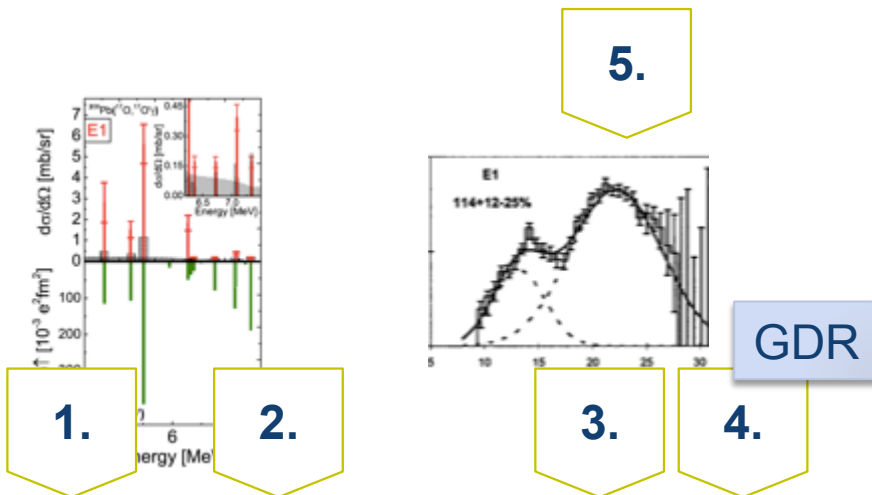
Theoretical investigations:

- [PP, H.Hergert, V.Yu.Ponomarev, R.Roth, J.Wambach + exp]:

N=Z
Ca
Sn
Ni
N=20



Electric dipole spectrum of ^{208}Pb



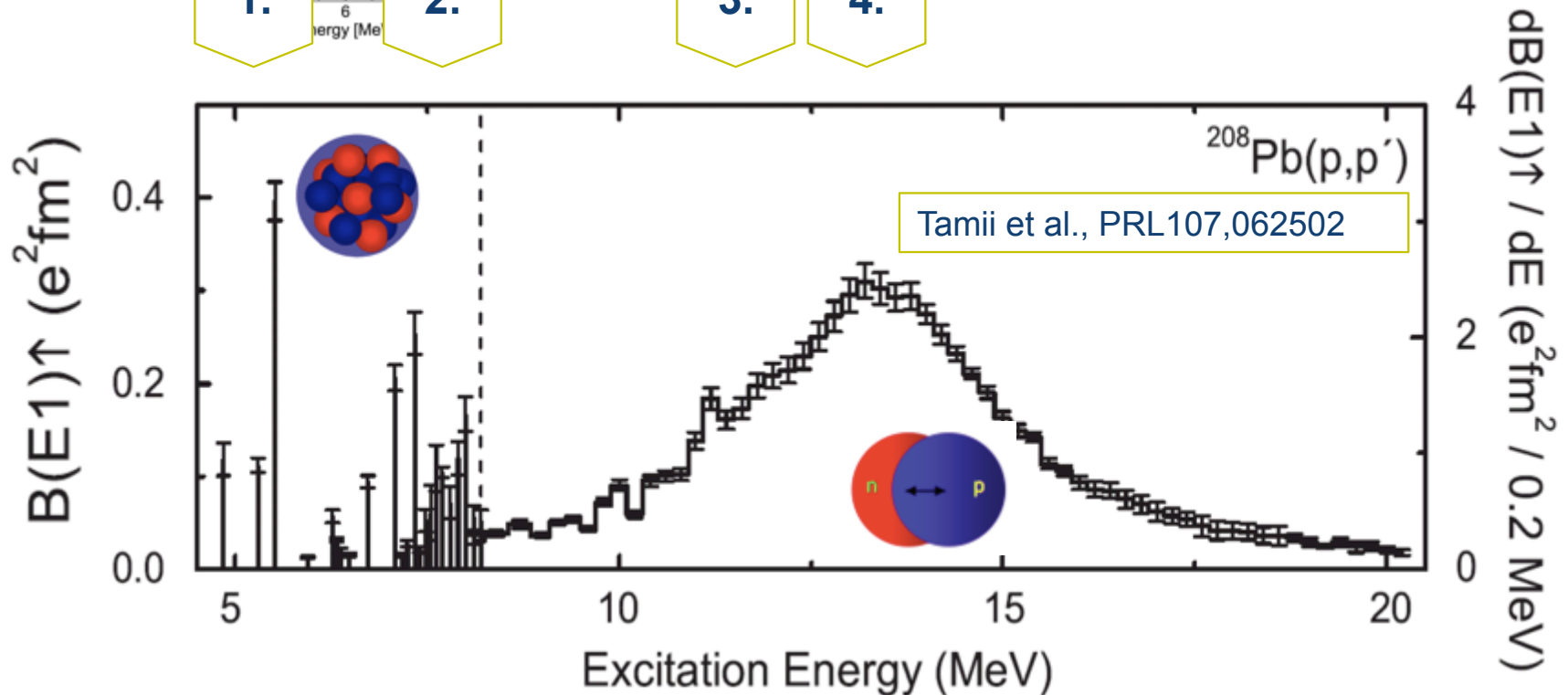
1,2: Tamii et al., PRL 107(2011)062502
Crespi et al., PRL 113(2014)012501
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GDR

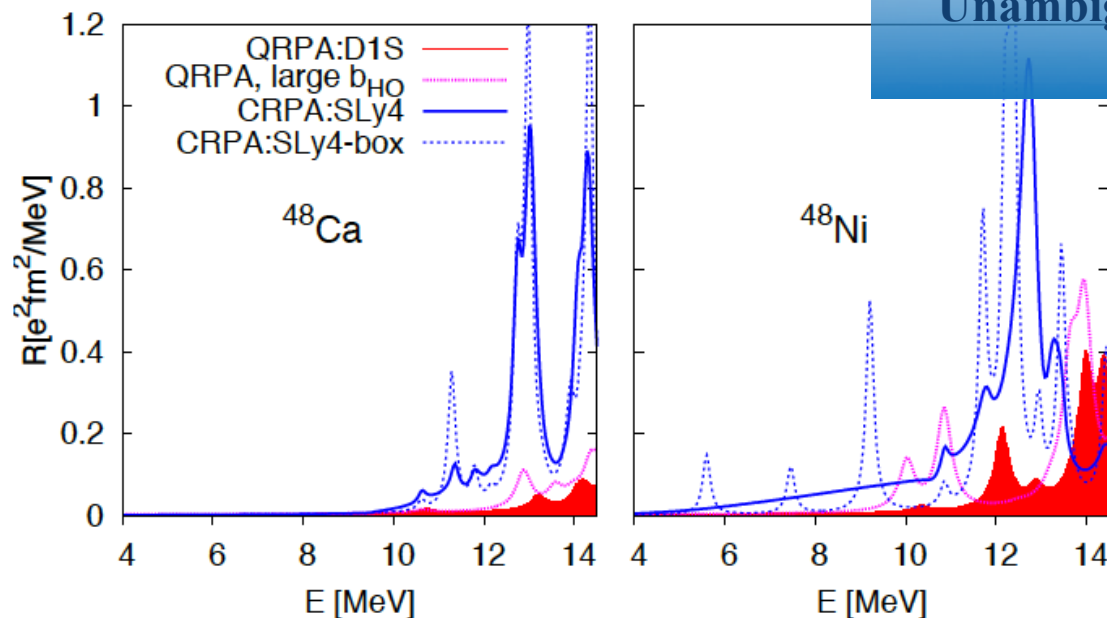


- ❖ Neutrons or protons near the Fermi surface
- ❖ Examples:
 - $N=20$ isotones and their mirror Ca isotopes
 - Shell closures in Ni, Ca, Sn isotopes

Proton-rich nuclei and their stable mirrors

Y.Kim,P.P, EPJA52(2016)176

Pygmies in the mirror:
Unambiguous role of loose
binding



	$B_{s.p}$	$B(E_1)$	$\sum_{E_i < 13} B(E_i)$	$\sum_{E_i < 15} B(E_i)$	$\sum_{E_i < 17} B(E_i)$	$ R_p - R_n $
^{40}Ca	0.188	0.004	0.008	0.117	0.179	0.042
^{42}Ti	0.177	0.008	0.116	0.249	0.361	0.106
^{44}Cr	0.166	0.009	0.189	0.320	0.576	0.159
^{46}Fe	0.156	0.008	0.251	0.421	0.835	0.207
^{48}Ni	0.148	0.009	0.161	0.553	1.211	0.249
^{46}Ca	0.156	0.003	0.050	0.149	0.443	0.108
^{48}Ca	0.148	0.006	0.006	0.089	0.763	0.145

candidate for
proton-skin
oscillation

Polarizability and shell structure in Ni

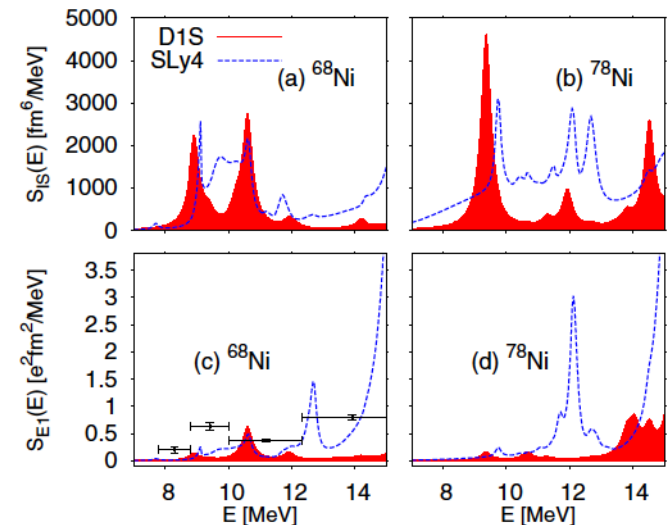
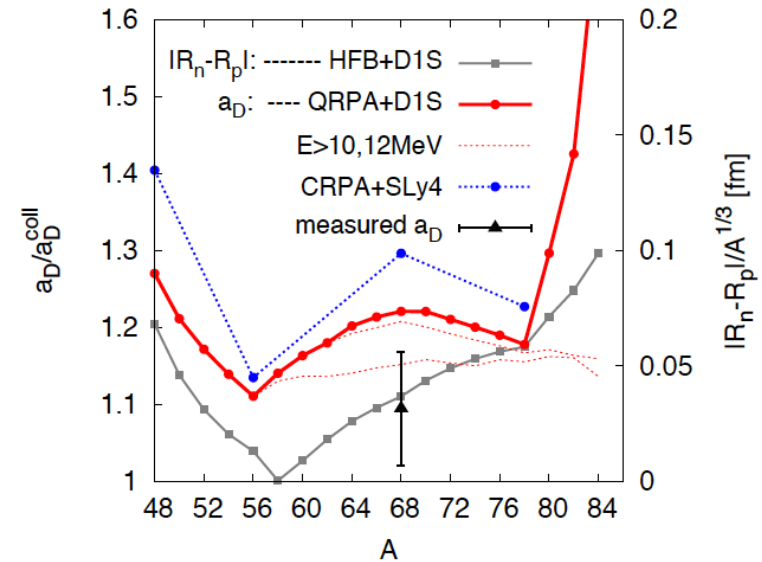
PP,H.Hergert, R.Roth, PRC92(2015)034311

$$a_D = \frac{\hbar c}{2\pi^2} \int \frac{\sigma_{\text{abs}}}{\omega^2} d\omega$$

Reference value: assuming 100% GDR

$$a_D^{\text{coll}} = \frac{\hbar c}{2\pi^2} \frac{60NZ\text{MeVmb}}{AE_{\text{GDR}}^2}$$

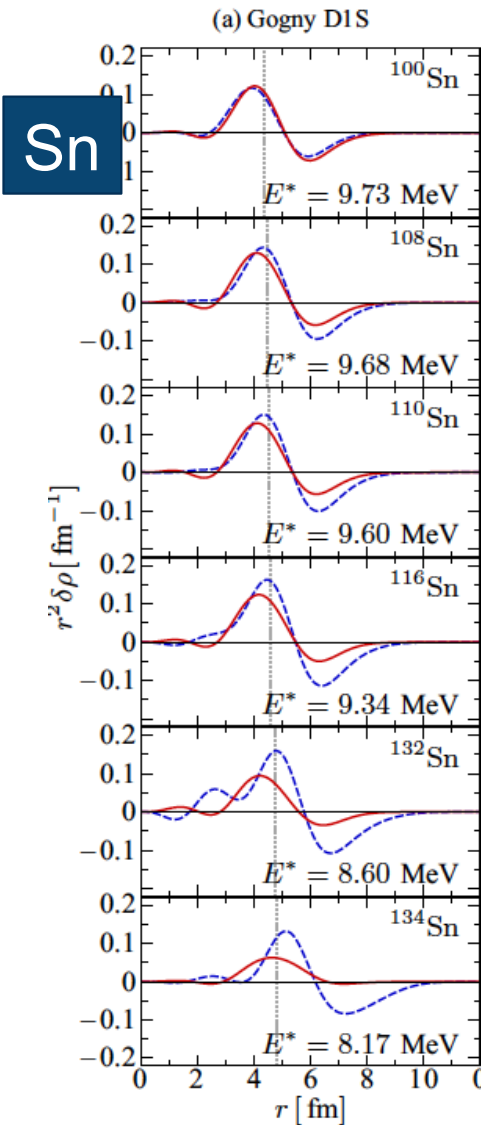
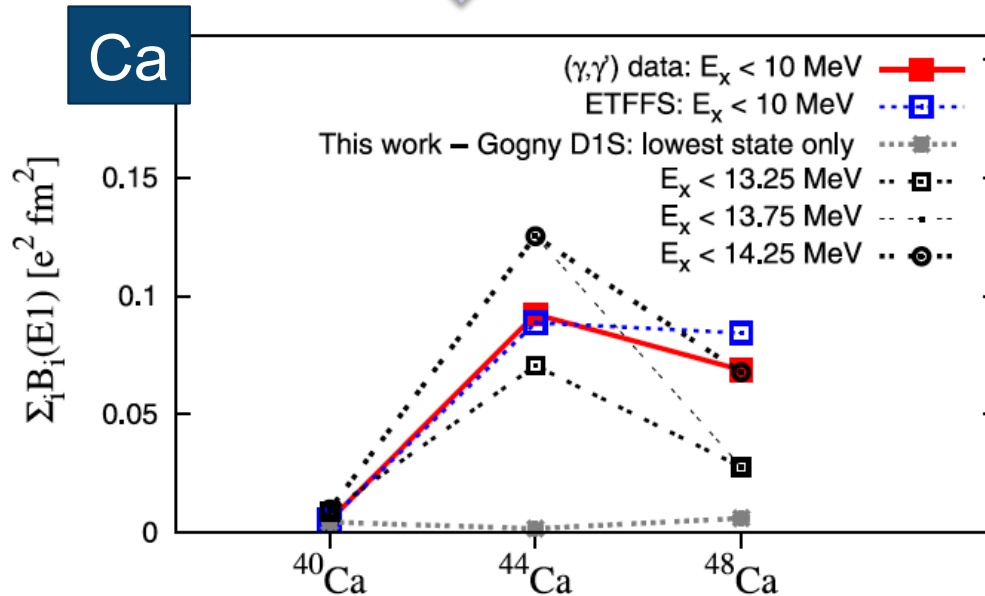
$$E_{\text{GDR}} = (31.2A^{-1/3} + 20.6A^{-1/6}) \text{ MeV}$$



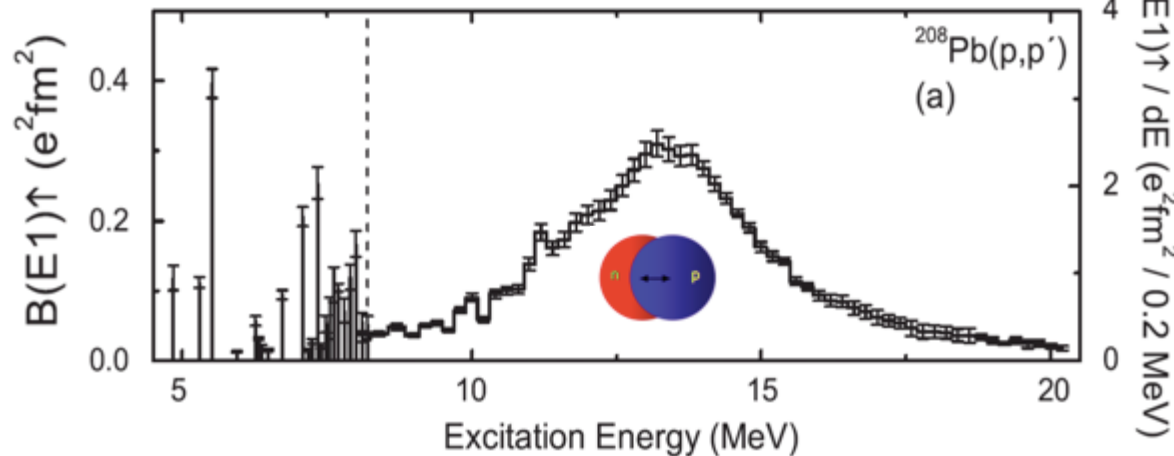
Measurement: D.Rossi et al., PLR 111,242503

Shell structure in Ca, Sn

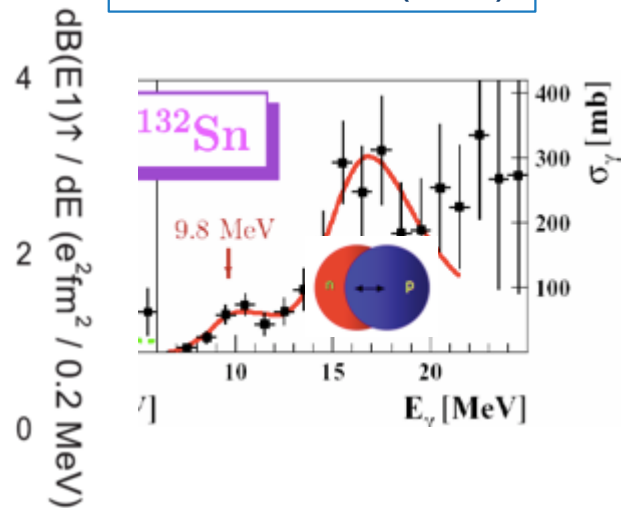
Weak transitions and apparent shell effect; strong neutron transitions predicted only beyond the N=28 closure



Tamii et al. (RCNP)



Adrich et al. (GSI)



The dipole spectrum contains **a wealth of structure information** with several implications

- GDR, lowest isoscalar state: universal features
- *Neutron/proton skin modes: in very exotic nuclei or above 8-9 MeV (or both)*
- Other isoscalar resonance?
- Data on stable nuclei so far favor asysoft models
- Finite-system peculiarities must be taken into account – separation energy
- Dramatic effects at shell closure

Measurements on either side of a shell closure?

Proton pygmy resonance?

Nuclear photoresponse / dipole response

- ❖ Ordinary and exotic features
- ❖ Focusing on:
 - Pygmy “resonance”
 - Isoscalar dipole response

Theory prospects

Summary

Roughly two approaches

❖ Given interaction + many-body method

- Variational reference state + Equations of Motion
- To lowest order, HF+RPA
- Systematic inclusion of correlations / mp-mh until convergence

- *“Wave-function approach”*
- *Known Hamiltonian*

❖ Energy-density functionals + linear-response theory

- *Kohn-Sham EDFT*
- *$E[\rho, \dots]$ known; Hamiltonian not necessarily known*
- *“black box”*

- The order of truncation depends on the application

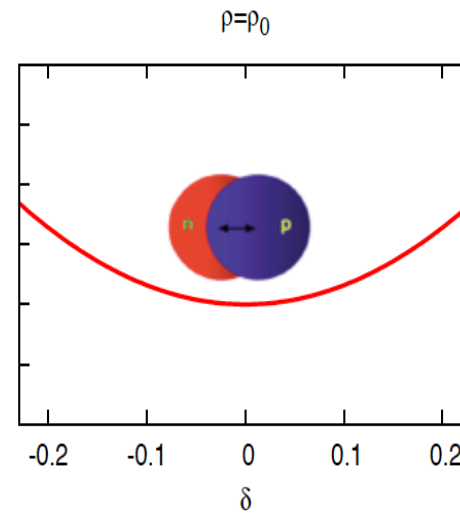
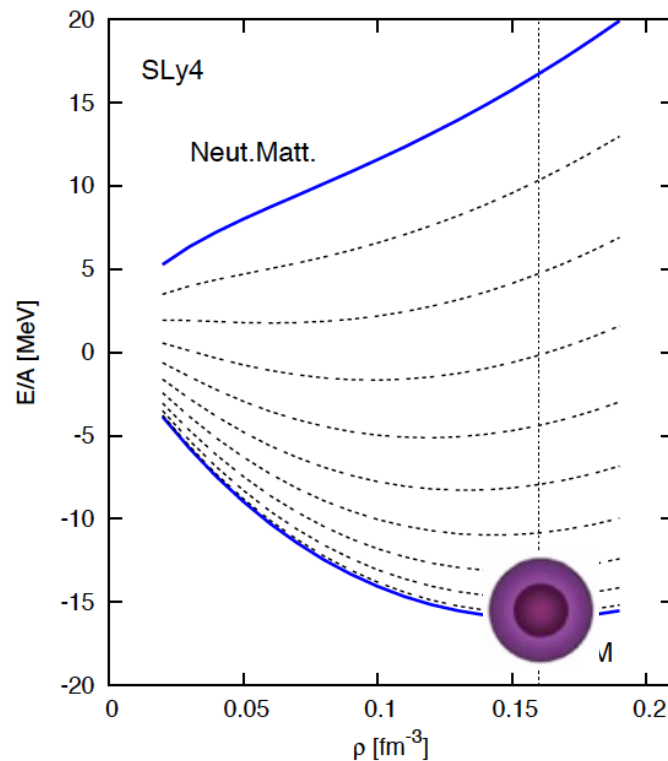
ground state vs excited states

$$\frac{E}{A}(\rho, \delta^2) = \left(\frac{E}{A} \right)_{\rho=\rho_0} + \frac{(\rho - \rho_0)^2}{18} \left(\frac{\partial^2(E/A)}{\partial \rho^2} \right)_{\rho=\rho_0} + \frac{\delta^2}{2} \left(\frac{\partial^2(E/A)}{\partial \delta^2} \right)_{\delta=0}$$

K

J

absolute values vs. derivatives



❖ KIDS = Korea: IBS - Daegu – Sungkyunkwan



EFT/QMBT: powers of Fermi momentum

$$\mathcal{E}(\rho, \delta) = \frac{E(\rho, \delta)}{A} = \mathcal{T}(\rho, \delta) + \sum_{i=0}^3 c_i(\delta) \rho^{1+i/3} + c_{\ln}(\delta) \rho^2 \ln[\rho/(1\text{fm}^3)]$$

kinetic energy: $\mathcal{T} = \mathcal{T}_p + \mathcal{T}_n$; $\mathcal{T}_{p,n} = \frac{3}{5} \frac{\hbar^2}{2m_{p,n}} x_{p,n}^{5/3} (3\pi^2 \rho)^{2/3}$; $x_{p,n} \equiv \rho_{p,n}/\rho$

asymmetry: $c_k(\delta) = \alpha_k + \delta^2 \beta_k$
 $\delta = (\rho_n - \rho_p)/\rho$

correspondence
with Skyrme

Nuclear potential	Order	KIDS parameter	Skyrme parameter
$\mathcal{E}_0$	k_F^3	$c_0(\delta)$	(t_0, x_0)
$\mathcal{E}_1$	k_F^4	$c_1(\delta)$	$(t_3, x_3), \alpha = 1/3$
$\mathcal{E}_2$	k_F^5	$c_2(\delta)$	$(t_1, x_1), (t_2, x_2), (t'_3, x'_3), \alpha' = 2/3$
$\mathcal{E}_3$	k_F^6	$c_3(\delta)$	$(t''_3, x''_3), \alpha'' = 1$



EFT/QMBT: powers of Fermi momentum

$$\mathcal{E}(\rho, \delta) = \frac{E(\rho, \delta)}{A} = \mathcal{T}(\rho, \delta) + \sum_{i=0}^3 c_i(\delta) \rho^{1+i/3} + c_{\ln}(\delta) \rho^2 \ln[\rho/(1\text{fm}^3)]$$

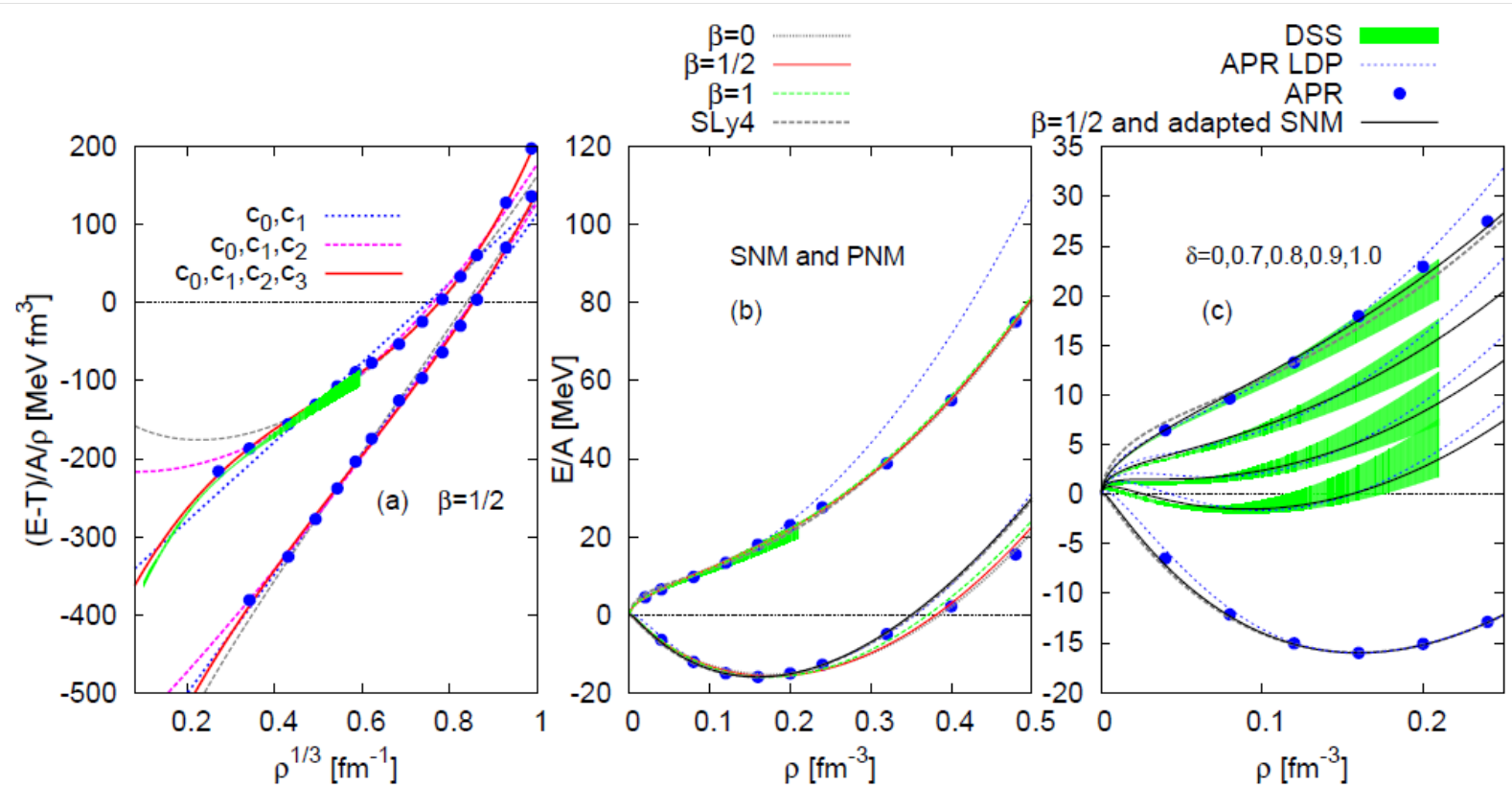
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asymmetry: $c_k(\delta) = \alpha_k + \delta^2 \beta_k$
 $\delta = (\rho_n - \rho_p)/\rho$

parameters: from fits to (pseudo-)data on homogeneous matter

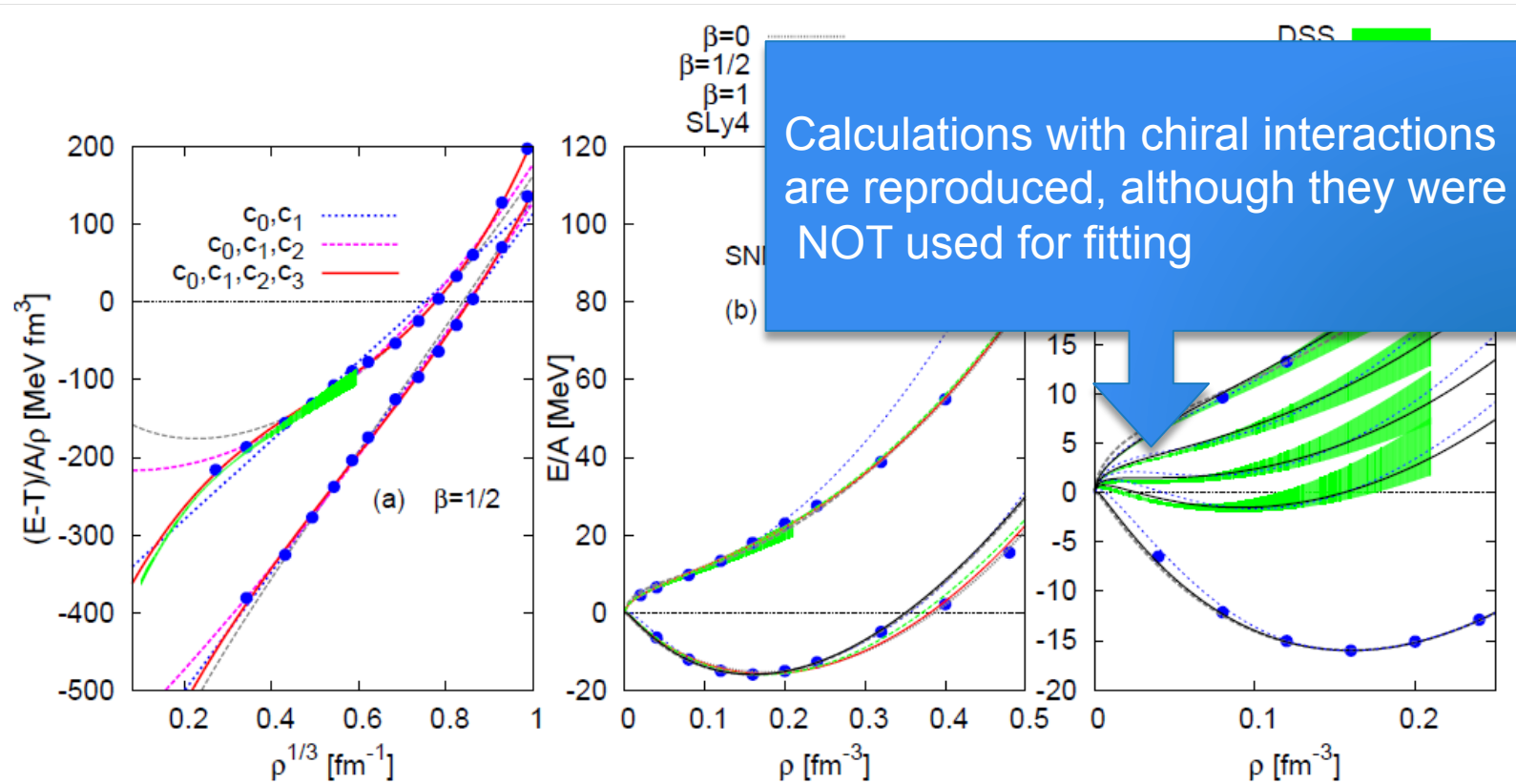
microscopic calculations of symmetric and neutron matter

PP, Park, Lim, Hyun, arXiv:1606.04219



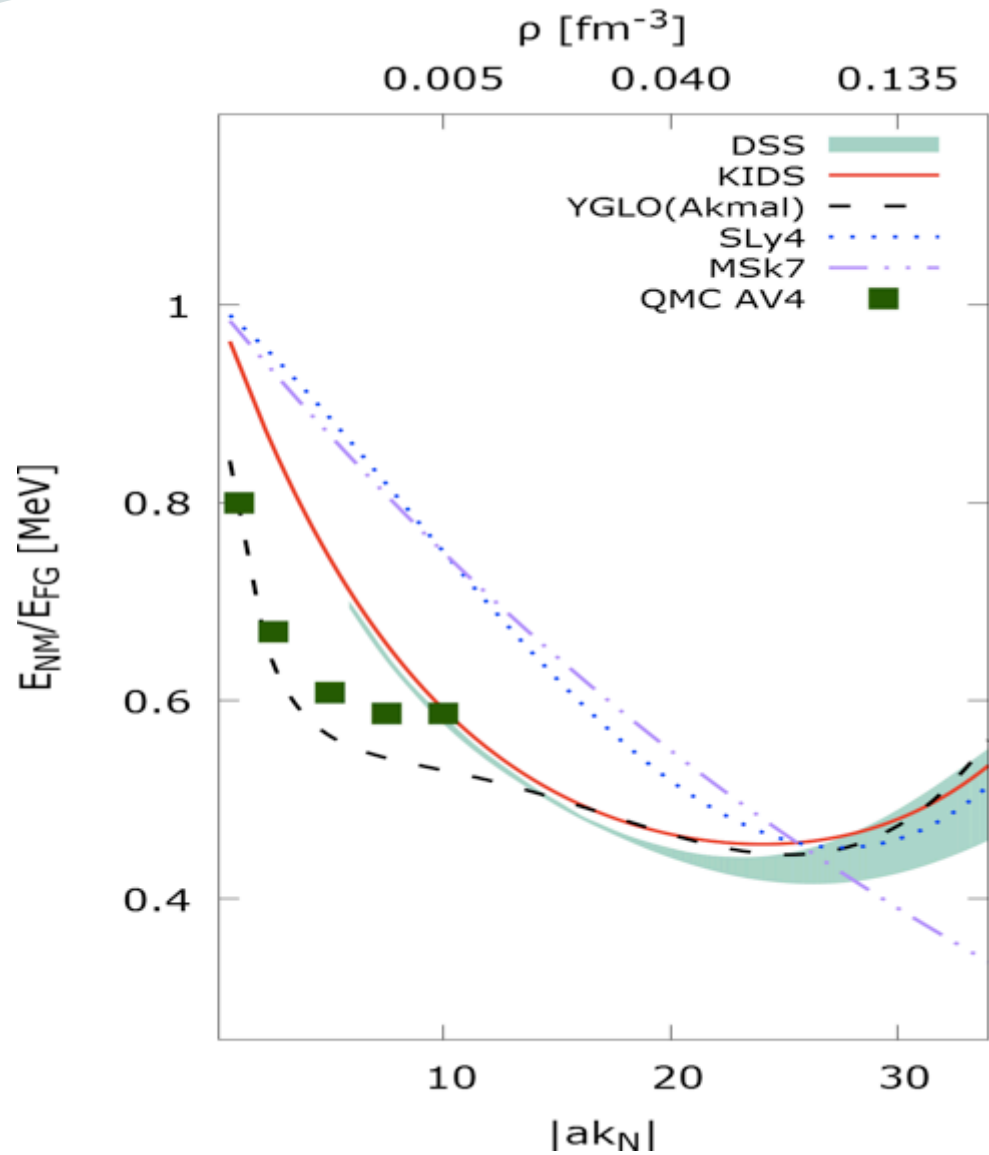
β : controls the weight we put on the lower-density data

PP, Park, Lim, Hyun, arXiv:1606.04219



β : controls the weight we put on the lower-density data

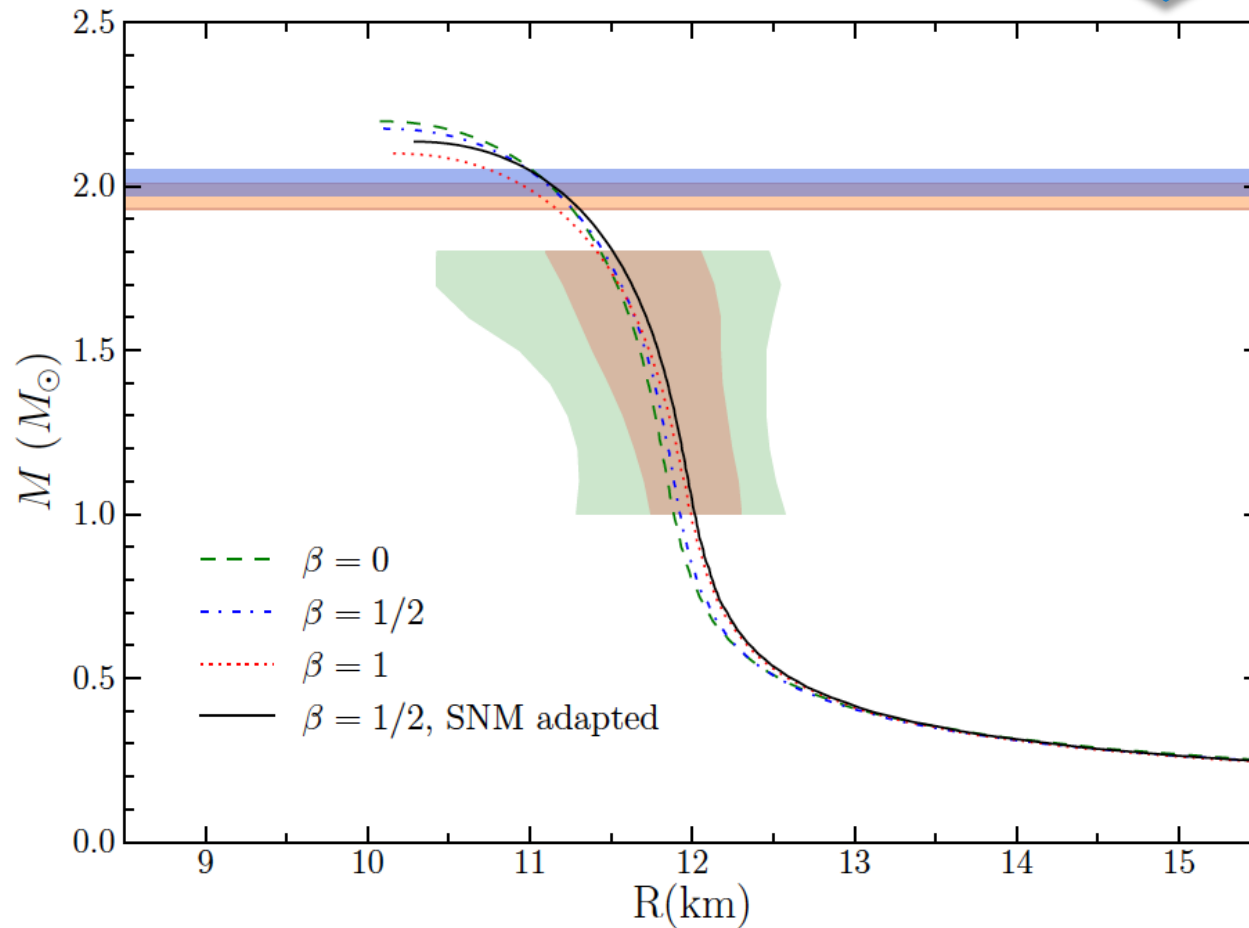
Dilute neutron matter



Dense matter: neutron stars

Agreement with
observational data

PP, Park, Lim, Hyun, arXiv:1606.04219



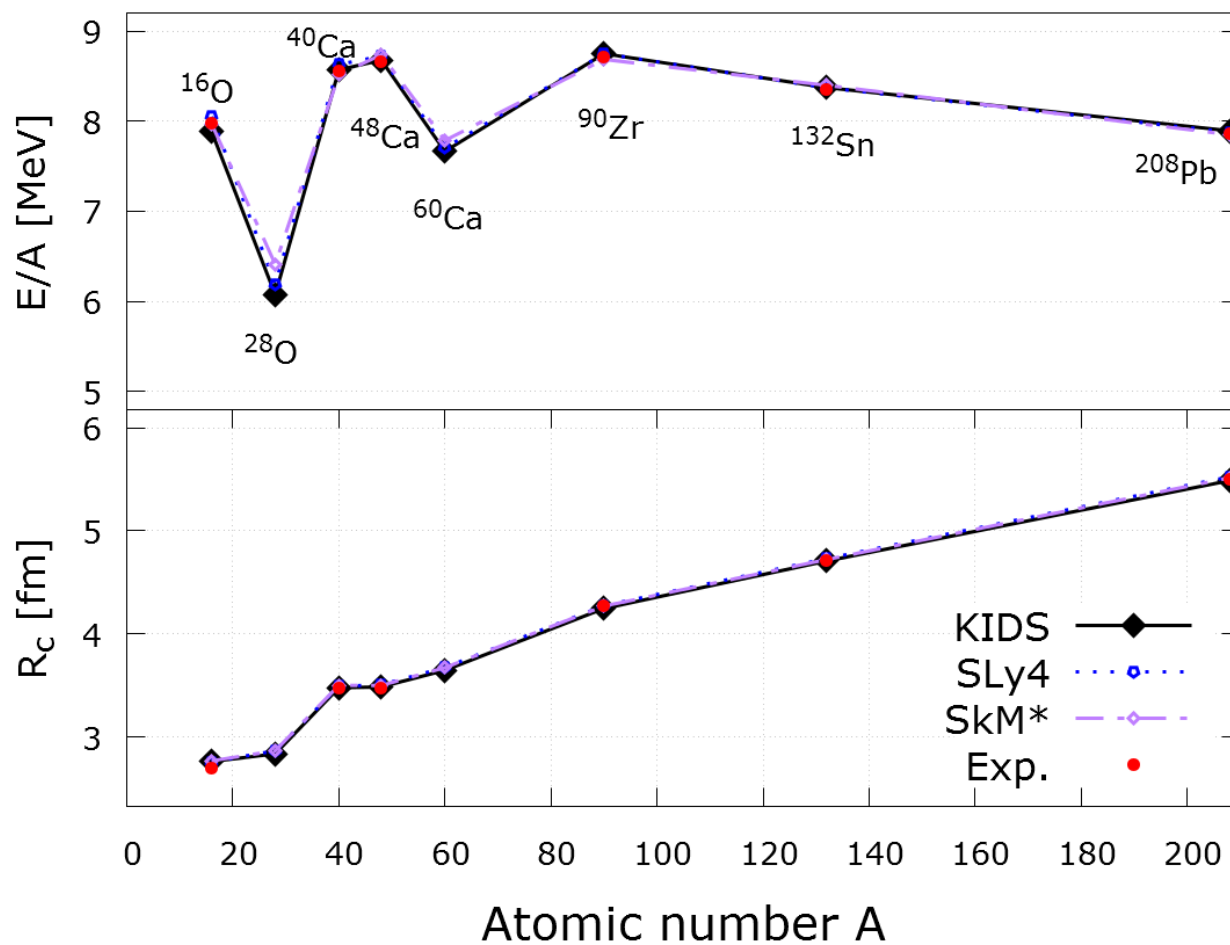
- ❖ Skyrme-type density-dependent “interaction”
- ❖ Skyrme-Hartree-Fock equations
- ❖ Parameters already known from homogeneous matter
- ❖ ... except those which do not contribute to the energy of homogeneous matter:
 - Contribution of momentum-dependent terms t_1 - t_2 to $c_2(\delta)$; effective mass

$$c_2(\delta) = k \cdot c_2(\delta) + (1 - k) \cdot c_2(\delta) \equiv c_2^{t'_3=0}(\delta) + c_2^{t_1=t_2=0}(\delta)$$

$k \sim 0.11$ reproduces the energy and radius of ^{16}O , ^{40}Ca

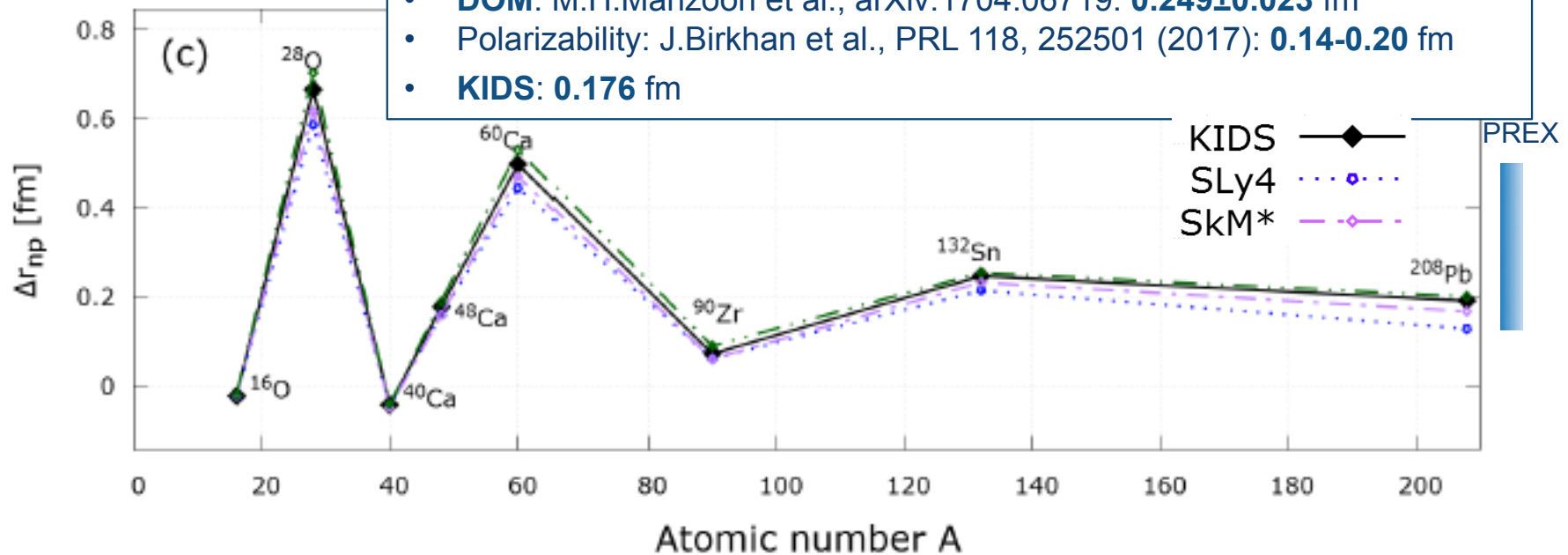
- spin-orbit strength W_0 :
 $W_0 \sim 110$ from ^{48}Ca , ^{208}Pb

Results – proof of principle



neutron skin of ^{48}Ca :

- **CCM**: G.Hagen et al., Nature Phys. 12,186(2016) **0.12-0.15 fm**
- **DOM**: M.H.Mahzoon et al., arXiv:1704.06719: **0.249 ± 0.023 fm**
- Polarizability: J.Birkhan et al., PRL 118, 252501 (2017): **0.14-0.20 fm**
- **KIDS**: **0.176 fm**



■ Prediction of ^{28}O and ^{60}Ca

	^{28}O			^{60}Ca		
Model	E/A [MeV]	R_c [fm]	Δr_{np} [fm]	E/A [MeV]	R_c [fm]	Δr_{np} [fm]
SLy4	6.1925	2.8656	0.58476	7.703	3.6734	0.4435
SkM*	6.4114	2.8646	0.61631	7.7857	3.6713	0.4685
KIDS	6.0757	2.8353	0.66398	7.6652	3.6452	0.4960

AME2016: 5.988

- ❖ The dipole spectrum contains **a wealth of structure information** with several implications
 - Lowest isoscalar state: universal feature
 - Other isoscalar resonance?
 - Photoresponse: Importance of separation energy
 - Dramatic effects at shell closure
- ❖ **Measurements on either side of a shell closure?**
- ❖ **Proton pygmy resonance?**

Theory: New functionals by reverse engineering

>> *Future plans: M1, GT*

Thank you!

감사합니다~

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Thanks to my collaborators and contributors

- ❖ A. Günther, V.Yu.Ponomarev, R.Roth, R.Trippel, J. Wambach...
 - ... and the experimental groups in Darmstadt, S.Africa and Cologne...
- ❖ Youngman Kim *et al*
- ❖ Chang Ho Hyun *et al*
- ❖ Hana Gil, Yongseok Oh
- ❖ H. Hergert
- ❖ J.W.Clark



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