

Visible and hidden sectors in magnetized D-brane systems

Keigo SUMITA (角田慶吾)

Waseda University (早稲田大学)

Based on

- Phys. Rev. D96 (2017) no.2, 026019
- Recent development (work in progress)

In collaboration with

- Hiroyuki Abe (Waseda University)
- Tatsuo Kobayashi (Hokkaido University)
- Shohei Uemura (Kyoto Sangyo University)

Outline

1. Introduction
2. Review : magnetized toroidal orbifold
3. SYM system and Superfield description
4. Model : MSSM sector
5. Model : MSSM+SUSY breaking
6. Model : MSSM+SUSY breaking + Moduli stabilization
7. Summary

Introduction : Superstring theory

- Incorporate the gravity into the elementary particles
- Quantum gravity without inconsistency
- Gauge theories (the SM?)

The most promising candidate for “the final theory”

- String phenomenology
- 4D effective theory consistent with the SM
- Hidden sector

Introduction : Extra dimensional space

- Superstrings predict 6D extra space
- 4D chiral spectrum vs Higher dimensional SUSY
- Origin of the flavor structure

Toroidal compactification with Magnetic fluxes and orbifolding

- Generations of chiral fermions
- Calculable spectrum : Hierarchical Yukawa couplings

Bachas '95

Cremades, Ibanez, Marchesano '04

Abe, Kobayashi, Ohki '04

Abe, Choi, Kobayashi, Ohki '09

Introduction : D-brane system

- D-branes in type IIB superstrings
- Effective Super-Yang-Mills (SYM) theories
 - $U(N)$ gauge group
 - 4D, 6D, 8D, 10D and their mixtures

Higher-dimensional $U(N)$ SYM theories
compactified on Magnetized Toroidal Orbifolds

- MSSM
- SUSY breaking
- Moduli stabilization

Review : 6D U(2) SYM on magnetized T^2

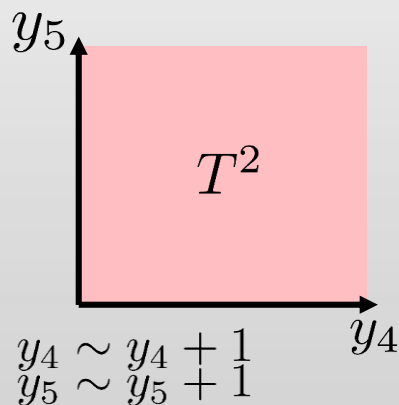
$$\mathcal{L} = \frac{1}{4g^2} \text{Tr} (F^{MN} F_{MN}) + \frac{i}{2g^2} \text{Tr} (\bar{\lambda} \Gamma^M D_M \lambda)$$

$$F_{MN} = \partial_M A_N - \partial_N A_M - i [A_M, A_N]$$

$$D_M \lambda = \partial_M \lambda - i [A_M, \lambda]$$

- Torus periodicity and KK mode expansion

$$X_M = (x_\mu, y_m), \quad \mu : 0, 1, 2, 3, \quad m = 4, 5$$



$$A_M(x^\mu, y^m) = \sum_n \varphi_{n,M}(x^\mu) \times \phi_{n,M}(y^m)$$

$$\lambda(x^\mu, y^m) = \sum_n \chi_n(x^\mu) \times \psi_n(y^m)$$

Review : 6D U(2) SYM on magnetized T^2

- Constant Abelian Flux on T^2

$$F_{45} = 2\pi M \quad \text{Gauge potential } A_4 = 0, \quad A_5 = 2\pi M y_4$$

- Gauge symmetry breaking : $U(2) \rightarrow U(1) \times U(1)$

$$M = \begin{pmatrix} M_a & 0 \\ 0 & M_b \end{pmatrix} \quad (M_a, M_b \in \mathbb{Z})$$

- Zero mode equation

$$i\Gamma_m D^m \psi_0(y) = 0$$

↓

$$[\partial_4 \pm i\partial_5 \pm 2\pi (M_a - M_b) y_4] \psi_{\pm}^{ab} = 0$$

$$[\partial_4 \pm i\partial_5] \psi_{\pm}^{aa} = 0 \quad (\text{Trivial})$$

$$\psi_0 = \begin{pmatrix} \psi_+ \\ \psi_- \end{pmatrix}$$

$$\psi_{\pm} = \begin{pmatrix} \psi_{\pm}^{aa} & \psi_{\pm}^{ab} \\ \psi_{\pm}^{ba} & \psi_{\pm}^{bb} \end{pmatrix}$$

Review : 6D U(2) SYM on magnetized T^2

$$[\partial_4 + i\partial_5 + 2\pi (M_a - M_b) y_4] \psi_+^{ab} = 0$$

$$[\partial_4 - i\partial_5 - 2\pi (M_a - M_b) y_4] \psi_-^{ab} = 0$$

For $M_{ab} \equiv M_a - M_b > 0$

$$\begin{cases} \psi_+^{ab} \text{ has } M_{ab} \text{ degenerate zero-modes} \\ \psi_-^{ab} \text{ has no zero-modes} \end{cases}$$

- Chirality projection
- Degenerate zero-modes :
generations of quarks and leptons

Review : 6D U(2) SYM on magnetized T^2

- Zero-mode wavefunction (Cremades, Ibanez, Marchesano '04)

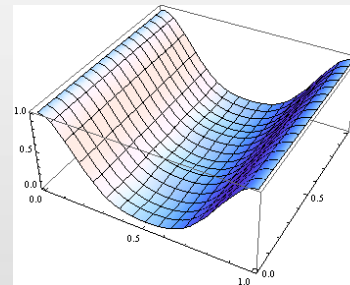
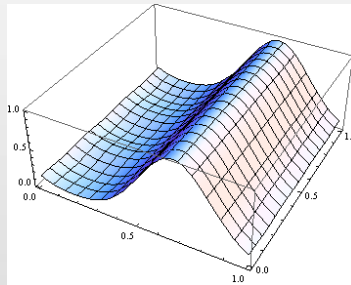
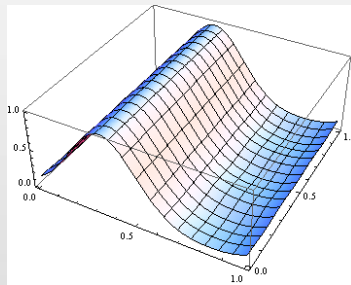
$$\Theta^{j,M_{ab}}(y_4, y_5) = \mathcal{N}_j e^{-M_{ab}\pi y_4^2} \cdot \vartheta \left[\begin{matrix} j/M_{ab} \\ 0 \end{matrix} \right] (-M_{ab}i(y_4 + iy_5), M_{ab}i)$$

$$j = 1, \dots, M_{ab}$$

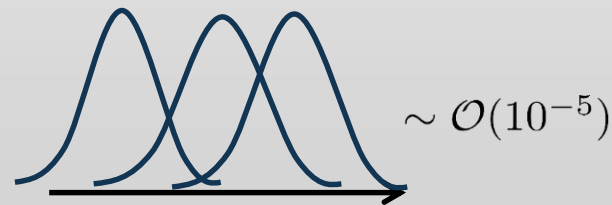
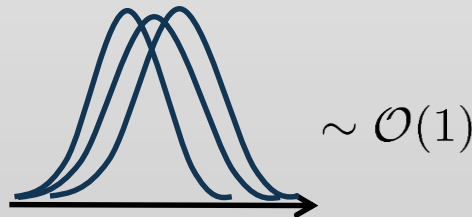
Jacobi theta function

$$\vartheta \left[\begin{matrix} a \\ b \end{matrix} \right] (\nu, \tau) = \sum_{l \in \mathbb{Z}} e^{\pi i(a+l)^2 \tau} e^{2\pi i(a+l)(\nu+b)}$$

- Quasi-localization : $|\Theta_j^M|^2$ for $M = 3$



- Hierarchical Yukawa couplings : $y_{IJK} = \int dy^2 \Theta^{I,M_{ab}}(y) \Theta^{J,M_{bc}}(y) \Theta^{I,M_{ca}}(y)$



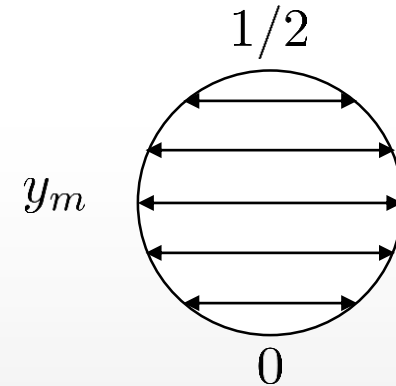
Arkani-Hamed, Schmaltz '00

Review : Magnetized T^2 with Z_2 orbifolding

- Z_2 orbifold : $(y_4, y_5) \sim (-y_4, -y_5)$

$$\psi_{\pm}(x_{\mu}, -y_m) = \pm P \psi_{\pm}(x_{\mu}, y_m) P^{-1}$$

Projection operator : $P^2 = 1$



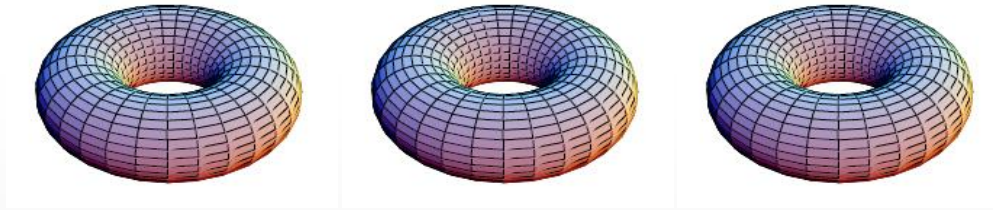
- Z_2 even and odd zero-modes

$$\begin{matrix} j = 1, 2, \dots, M \\ \psi^j(y) \end{matrix} \rightarrow \begin{cases} \psi_{\text{even}}^j(y) = \frac{1}{\sqrt{2}} (\psi^j(y) + \psi^{M-j}(y)) \\ \psi_{\text{odd}}^j(y) = \frac{1}{\sqrt{2}} (\psi^j(y) - \psi^{M-j}(y)) \end{cases}$$

M	0	1	2	3	4	5	2n	2n+1
Pure T^2	1	1	2	3	4	5	2n	2n+1
Even	1	1	2	2	3	3	n+1	n+1
Odd	0	0	0	1	1	2	n-1	n

SYM systems and Superfield description

Toroidal compactification



- Torus parameter : (R_i, τ_i) $i : 1, 2, 3$
- Complex coordinate : $z^i \equiv \frac{1}{2} (y^{2+2i} + \tau_i y^{3+2i})$ $\bar{z}^{\bar{i}} \equiv (z^i)^*$
- Periodicity : $z_i \sim z_i + 1$ $z_i \sim z_i + \tau_i$

$$ds^2 = G_{MN} dX^M dX^N = \eta_{\mu\nu} dx^\mu dx^\nu + 2h_{i\bar{j}} dz^i d\bar{z}^{\bar{j}}$$

$$h_{i\bar{j}} = 2(2\pi R_i)^2 \delta_{i\bar{j}}$$

Superfield description of D-brane systems

- Higher-dimensional SYM theory : $D = 4, 6, 8, 10$
- 10D SYM compactified on $T^2 \times T^2 \times T^2$
- 4D N=1 decomposition of 10D fields

$$A_M = (A_\mu, A_i) \quad i : 1, 2, 3$$

$$\lambda = (\lambda_0, \lambda_i) \quad A_i \equiv -\frac{1}{\text{Im}\tau_i} (\bar{\tau}_i A_{2+2i} - A_{3+2i})$$

$$\text{4D N=1 vector superfield} \quad V \equiv -\theta\sigma^\mu\bar{\theta}A_\mu + i\bar{\theta}\bar{\theta}\theta\lambda_0 - i\theta\theta\bar{\theta}\bar{\lambda}_0 + \frac{1}{2}\theta\theta\bar{\theta}\bar{\theta}D$$

$$\text{4D N=1 chiral superfield} \quad \phi_i \equiv \frac{1}{\sqrt{2}}\varphi_i + \sqrt{2}\theta\lambda_i + \theta\theta F_i$$

$$\mathcal{K} = \frac{2}{g^2} h^{i\bar{j}} \text{Tr} \left[\left(\sqrt{2}\bar{\partial}_{\bar{i}} + \bar{\phi}_{\bar{i}} \right) e^{-V} \left(-\sqrt{2}\partial_j + \phi_j \right) e^V + \bar{\partial}_{\bar{i}} e^{-V} \partial_j e^V \right]$$

$$\mathcal{W} = \frac{1}{g^2} \epsilon^{ijk} e_i^i e_j^j e_k^k \text{tr} \left[\sqrt{2}\phi_i \left(\partial_j \phi_k - \frac{1}{3\sqrt{2}} [\phi_j, \phi_k] \right) \right]$$

Marcus, Sagnotti, Siegel '83
Arkani-Hamed, Gregoire, Wacker '02

Superfield description of D-brane systems

- D=4,6,8 are obtained by dimensional reduction of D=10
- Some of ϕ_i becomes the position modulus
- Overlap of different SYMs requires additional multiplets
- Magnetized toroidal orbifold compactification and 4D effective actions in the superfield description

Model : MSSM sector

MSSM sector : two typical models

- Two typical models : D9 model vs D7 model
- Massless open string moduli
 - D9 contains some harmful massless modes
- Association with hidden sectors
 - D9 inevitably overlaps hidden D-branes

D7 model

8D $U(4)_A$ SYM on $T^2 \times T^2 \times T^2$
and
8D $U(4)_B$ SYM on $T^2 \times T^2 \times T^2$

- Field contents

A sector : $U(4)_A$ adjoint

B sector : $U(4)_B$ adjoint

A-B sector : Bi-fundamental

$\phi_1^A, \tilde{\phi}_2^A, \phi_3^A$

$\phi_1^B, \phi_2^B, \tilde{\phi}_3^B$

ϕ_2^{AB}, ϕ_3^{BA}

\uparrow
 $(\mathbf{4}, \bar{\mathbf{4}})$ of $U(4)_A \times U(4)_B$

Position modulus

D7 model

- Magnetized background

$$M_A^{(1)} = \begin{pmatrix} -5 \times \mathbf{1}_3 & 0 \\ 0 & -4 \end{pmatrix}, \quad M_A^{(3)} = -M_A^{(1)}$$

$$M_B^{(1)} = \begin{pmatrix} 0 \times \mathbf{1}_2 & 0 \\ 0 & -12 \times \mathbf{1}_2 \end{pmatrix}, \quad M_B^{(2)} = \begin{pmatrix} 0 \times \mathbf{1}_2 & 0 \\ 0 & 1 \times \mathbf{1}_2 \end{pmatrix}$$

- Gauge symmetry breaking

$$U(4)_A \rightarrow U(3)_C \times U(1)_\ell$$

$$U(4)_B \rightarrow U(2)_L \times U(2)_R$$

- 4D N=1 Supersymmetry

$$F_i = D_L = 0 \quad D_C = D_\ell = \frac{-5}{\mathcal{A}_1} + \frac{5}{\mathcal{A}_3} \quad D_R = \frac{-12}{\mathcal{A}_1} + \frac{1}{\mathcal{A}_2}$$



$$\mathcal{A}_1/\mathcal{A}_2 = 12, \quad \mathcal{A}_1/\mathcal{A}_3 = 1$$

D7 model

$$Z_2 : (z_1, z_2, z_3) \rightarrow (-z_1, -z_2, z_3)$$

$$Z'_2 : (z_1, z_2, z_3) \rightarrow (z_1, -z_2, -z_3)$$

- Orbifold transformation : $P_A, P'_A, P_B, P'_B,$

$$\begin{aligned} Z_2 : \phi_{1,2}^A &\rightarrow -P_A \phi_{1,2}^A P_A^{-1}, & \phi_3^A &\rightarrow +P_A \phi_3^A P_A^{-1} \\ \phi_{1,2}^B &\rightarrow -P_B \phi_{1,2}^B P_B^{-1}, & \phi_3^B &\rightarrow +P_B \phi_3^B P_B^{-1} \\ \phi_2^{AB} &\rightarrow -P_A \phi_2^{AB} P_B^{-1}, & \phi_3^{BA} &\rightarrow +P_B \phi_3^{BA} P_A^{-1} \end{aligned}$$

$$\begin{aligned} Z'_2 : \phi_{2,3}^A &\rightarrow -P'_A \phi_{2,3}^A P'^{-1}_A, & \phi_1^A &\rightarrow +P'_A \phi_1^A P'^{-1}_A \\ \phi_{2,3}^B &\rightarrow -P'_B \phi_{2,3}^B P'^{-1}_B, & \phi_1^B &\rightarrow +P'_B \phi_1^B P'^{-1}_B \\ \phi_2^{AB} &\rightarrow -P'_A \phi_2^{AB} P'^{-1}_B, & \phi_3^{BA} &\rightarrow -P'_B \phi_3^{BA} P'^{-1}_A \end{aligned}$$

$$P_A = P'_A = P_B = -P'_B = \mathbf{1}_4$$

D7 model : zero-mode contents

$$\phi_1^B = \begin{pmatrix} 0 & H \\ 0 & 0 \end{pmatrix}, \quad \phi_2^{AB} = \begin{pmatrix} Q_L & 0 \\ L_L & 0 \end{pmatrix}, \quad \phi_3^{BA} = \begin{pmatrix} 0 & 0 \\ Q_R & L_R \end{pmatrix}$$

$$\phi_1^A, \tilde{\phi}_2^A, \phi_3^A, \phi_2^B, \tilde{\phi}_3^B = 0$$

- Three generations of Q_L, L_L, Q_R, L_R
- Five generations of $H = (H_u, H_d)$
- Hopeful spectrum : $\text{Im } \tau_1 = 1.5 \quad \frac{\langle H_{u4} \rangle}{\langle H_{u5} \rangle} = 0.29 \quad \frac{\langle H_{d4} \rangle}{\langle H_{d5} \rangle} = 0.38 \quad \frac{\langle H_{d3} \rangle}{\langle H_{d5} \rangle} = 0.10$

	Sample values	Observed
$(m_u, m_c, m_t)/m_t$	$(1.7 \times 10^{-5}, 5.7 \times 10^{-3}, 1)$	$(1.5 \times 10^{-5}, 7.5 \times 10^{-3}, 1)$
$(m_d, m_s, m_b)/m_b$	$(2.0 \times 10^{-3}, 6.8 \times 10^{-2}, 1)$	$(1.2 \times 10^{-3}, 2.3 \times 10^{-2}, 1)$
$(m_e, m_\mu, m_\tau)/m_\tau$	$(2.7 \times 10^{-4}, 5.9 \times 10^{-2}, 1)$	$(2.9 \times 10^{-4}, 6.0 \times 10^{-2}, 1)$
$ V_{\text{CKM}} $	$\begin{pmatrix} 0.96 & 0.29 & 0.01 \\ 0.29 & 0.96 & 0.07 \\ 0.01 & 0.07 & 1.0 \end{pmatrix}$	$\begin{pmatrix} 0.97 & 0.23 & 0.0035 \\ 0.23 & 0.97 & 0.041 \\ 0.0087 & 0.040 & 1.0 \end{pmatrix}$

MSSM+SUSY breaking

Dynamical Supersymmetry Breaking (DSB)

- SYM system : restricted field contents and their couplings
- Supersymmetric $SU(N_C)$ gauge theory with N_F fundamental flavors (Q, \tilde{Q})
- For $N_C > N_F$, the Affleck-Dine-Seiberg potential is obtained

$$W_{\text{ADS}} = c \times \left(\frac{\Lambda^{3N_C - N_F}}{\det Q\tilde{Q}} \right)^{1/(N_C - N_F)}$$

- The simplest DSB model with a singlet X [I. Affleck, M. Dine & N. Seiberg '85]

$$W = gXQ\tilde{Q} + c \times \left(\frac{\Lambda^{3N_C - N_F}}{\det Q\tilde{Q}} \right)^{1/(N_C - N_F)}$$

$$\langle Q\tilde{Q} \rangle = \Lambda^2 \quad W_{\text{effective}} = gX\Lambda^2$$

DSB models in Magnetized D-brane systems

- Gauge Symmetry Breaking : $G \rightarrow U(N_C) \times U(1) \times U(1)$
- Field contents ; $Q(N_C, -1, 0), \quad \tilde{Q}(\bar{N}_C, 0, +1), \quad X(0, +1, -1)$
- Degeneracy $(Q, \tilde{Q}, X) = (N_F, N_F, 1)$
- Global symmetries allowing the coupling of $XQ\tilde{Q}$
- $N_C > N_F$ in order to get W_{ADS}

Many successful models (without the visible sector) !

DSB with the MSSM sector

- Consistency with the visible D7-branes

$$Z_2 : (z_1, z_2, z_3) \rightarrow (-z_1, -z_2, z_3)$$

$$Z'_2 : (z_1, z_2, z_3) \rightarrow (z_1, -z_2, -z_3)$$

$$\mathcal{A}_1/\mathcal{A}_2 = 12, \quad \mathcal{A}_1/\mathcal{A}_3 = 1$$

- Harmful zero-modes connecting the two sectors

Additional D7 models

8D $U(1)_C$ SUSY gauge theory on $T^2 \times T^2 \times T^2$

and

8D $U(N_C + 1)_D$ SYM on $T^2 \times T^2 \times T^2$

- Additional field contents

C sector : Singlet

$$\phi_1^C, \tilde{\phi}_2^C, \phi_3^C$$

D sector : $U(N_C + 1)_D$ adjoint

$$\phi_1^D, \phi_2^D, \tilde{\phi}_3^D$$

C-D sector : Fundamental charged under $U(1)_C$ ϕ_2^{CD}, ϕ_3^{CD}

A-C, A-D, B-C, B-D sector : Bi-fundamentals and others

Configuration of a Magnetized orbifold

- Magnetized background

$$M_C^{(1)} = M_C^{(3)} = 0$$

$$M_D^{(1)} = \begin{pmatrix} 12 \times \mathbf{1}_{N_C} & 0 \\ 0 & 0 \end{pmatrix}, \quad M_D^{(2)} = \begin{pmatrix} -1 \times \mathbf{1}_{N_C} & 0 \\ 0 & 0 \end{pmatrix}$$

- SUSY is preserved by $\mathcal{A}_1/\mathcal{A}_2 = 12$, $\mathcal{A}_1/\mathcal{A}_3 = 1$

- Gauge symmetry breaking

$$U(1)_C \times U(N_C + 1)_D \rightarrow U(N_C) \times U(1)_C \times U(1)_D$$

- Orbifold parity : $P_C = -P'_C = 1$ $P_D = P'_D = \mathbf{1}_{N_C+1}$

Configuration of a Magnetized orbifold

- The essential structure of DSB is realized
- One singlet X and five generations of (Q, \tilde{Q}) ; $N_F = 5$
- Extra zero-modes are completely eliminated
 - MSSM and DSB are decoupled to each other
- For $N_C > N_F = 5$, we get

$$W_{\text{effective}} = g\Lambda^2 X$$

↑
Dynamical scale of the SUSY $SU(N_C)$

MSSM + SUSY breaking + Moduli stabilization

Moduli stabilization in IIB superstrings

Dilaton	S
Complex structure	U_1, U_2, U_3
Kähler moduli	T_1, T_2, T_3

- 3-form fluxes to stabilize S and U
- D-term potential for T_i
- Ratios of T_i are stabilized at a SUSY vacuum
- One flat direction of Kähler moduli

E-brane (D-brane instanton)

- Localized at a point in the 4D spacetime
- Finite volume in the extra dimensional space

Sequestered : $A_i e^{-a_i T_i}$ \rightarrow Moduli stabilization

Not sequestered : $A_i e^{-a_i T_i} \Psi_1 \Psi_2 \dots$

E-branes in D7 brane systems

- E3-brane (wrapping a 4-cycle)

- If there is no charged zero-mode, we get

$$W = W_0 + A_i e^{-4\pi T_i}$$

$$K = -\log(T_i + \bar{T}_i)$$

the modulus is stabilized at a SUSY vacuum

- Origin of the constant term, W_0

- E(-1)-brane (completely localized at a point)

$$W = A_S e^{-4\pi S} \rightarrow A_S e^{-4\pi \langle S \rangle} \quad (\text{stabilized by 3-form fluxes})$$

- The stringy fluxes can directly produce W_0

Specific model in the D7-brane system

- E3-brane sequestered from $D7_A, D7_B, D7_C, D7_D$
- A successful configuration ;

One E3-brane on $T^2 \times T^2 \times T^2$ with $P_E = P'_E = 1$

$$W_{\text{Non-perturbative}} = Ae^{-a_1 T_1}$$

- Interplay of the DSB and the moduli stabilization dynamics

$$W_{\text{total}} = W_0 + Ae^{-aT_1} + B\Lambda^2 X$$

F-term uplifting

- Solving the RGE for the hidden gauge coupling, we get

$$\Lambda \sim M_{\text{compact}} e^{\frac{2\pi}{N_F - 3N_C} 4T_3 + 24S}$$

- Massless direction of the D-terms :
$$\begin{aligned} T_1 &= \frac{12}{17} \mathcal{T} + \dots \\ T_3 &= \frac{12}{17} \mathcal{T} + \dots \end{aligned}$$

$$\begin{aligned} W_{\text{total}} &= W_0 - Ae^{-a\mathcal{T}} + Be^{-b\mathcal{T} - c\langle S \rangle} X \\ K &= -3 \log(\mathcal{T} + \bar{\mathcal{T}}) \end{aligned}$$

resembles a model shown in [Abe, Higaki, Kobayashi '07]

- W_0 tunned to realize the Polonyi vacuum

$$W_0 = Ae^{-a\mathcal{T}_0} + B(1 - X_0)e^{-b\mathcal{T}_0 - c\langle S \rangle}$$

$$a = 4\pi \frac{12}{17}$$

$$b = 4\pi \frac{12}{17} \frac{2}{3N_C - N_F}$$

$$c = 4\pi \frac{24}{3N_C - N_F}$$

Polonyi-KKLT vacuum

- Consistent DSB and KKLT dynamics
- At the vacuum, we find

$$m_{3/2} \sim B \exp\left[-4\pi \frac{24}{3N_C - N_F} \langle S \rangle\right] \sim \mathcal{O}(10^{-15}) M_{\text{Planck}}$$
$$m_{\text{soft}} \sim \frac{m_{3/2}}{4\pi} \sim \mathcal{O}(\text{TeV})$$

Summary

- Magnetized toroidal orbifold compactification
- Superfield description of effective D-brane systems
- The MSSM-like model without massless open strings
- Dynamical SUSY breaking
- Kähler moduli stabilization due to E-branes
- Interplay of DSB and moduli stabilization

Future prospects

- Phenomenology in detail : SUSY spectrum ...
- String theoretical consistency
- Cosmology

Thank you very much !!