

Reheating the Universe at Criticality

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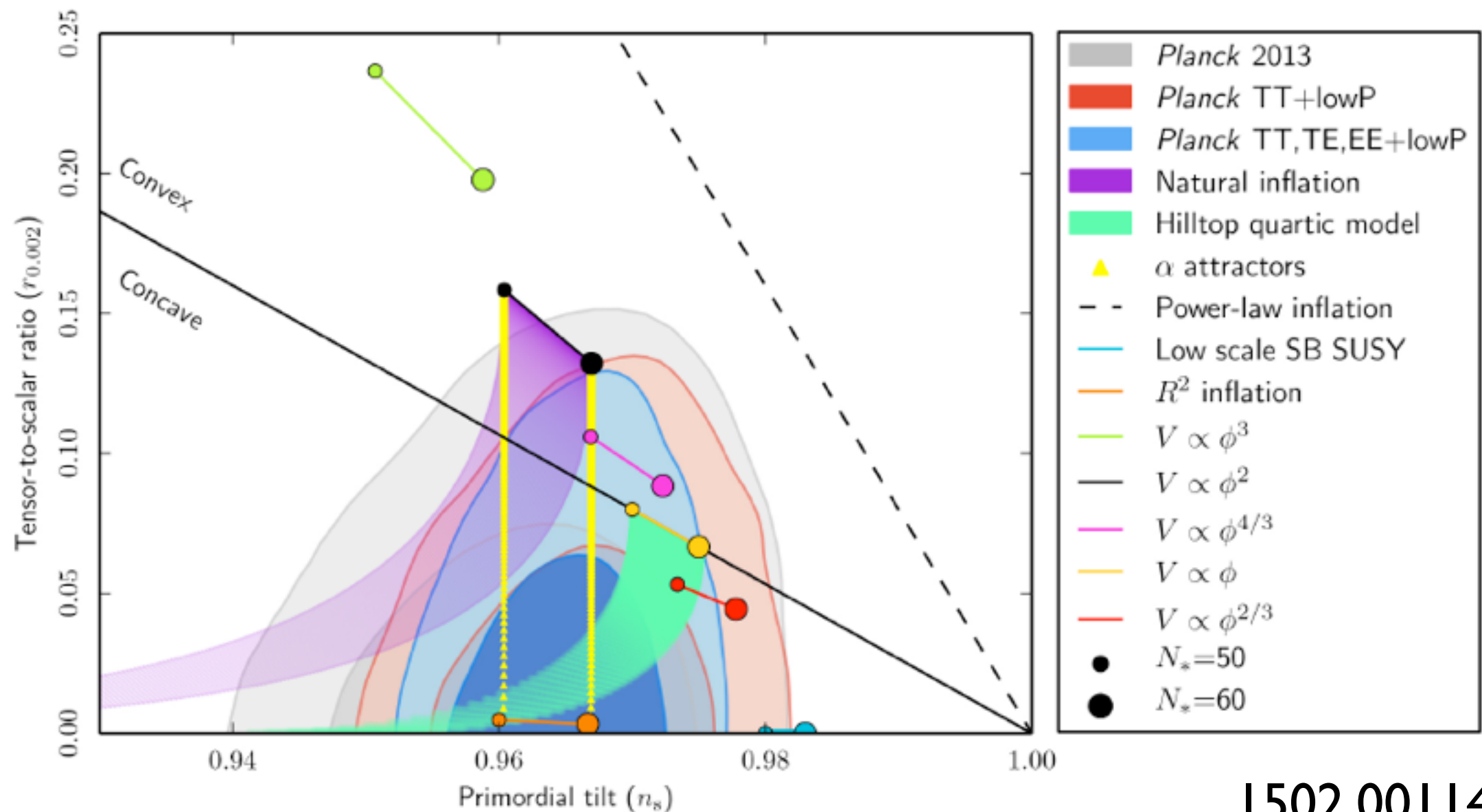
Ref. S.-M Choi, HML, K.-C. Kim, To appear.

CosPA 2015
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Outline

- Introduction
- Inflation and reheating at inflection point
- Higgs inflation at criticality
- Conclusions

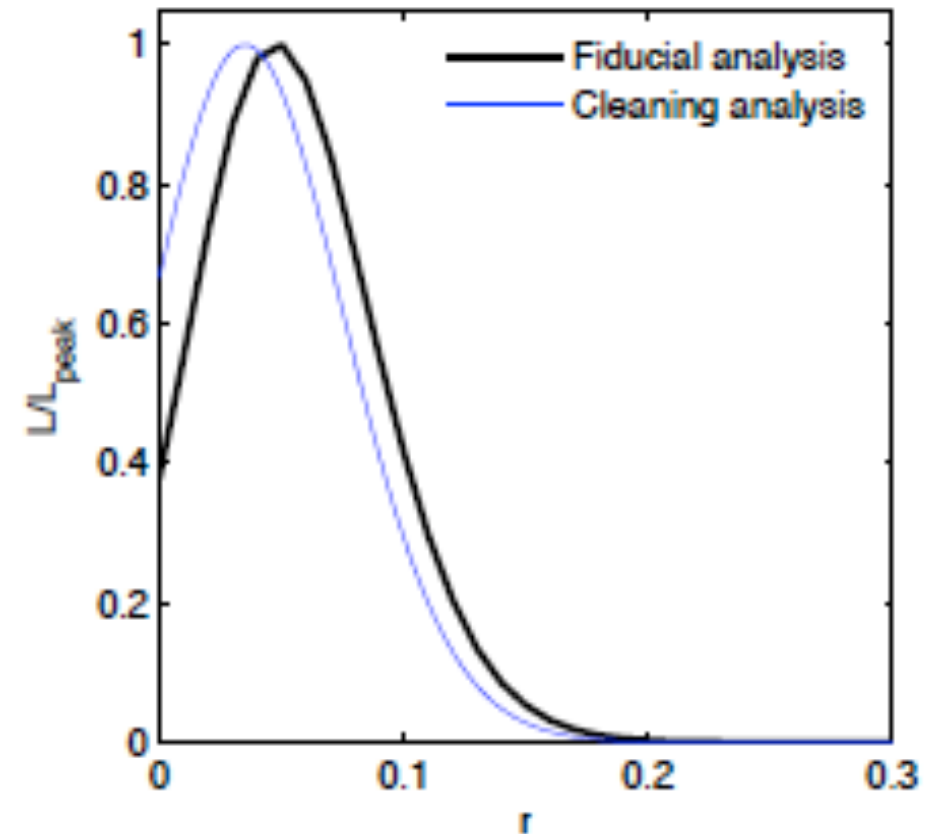
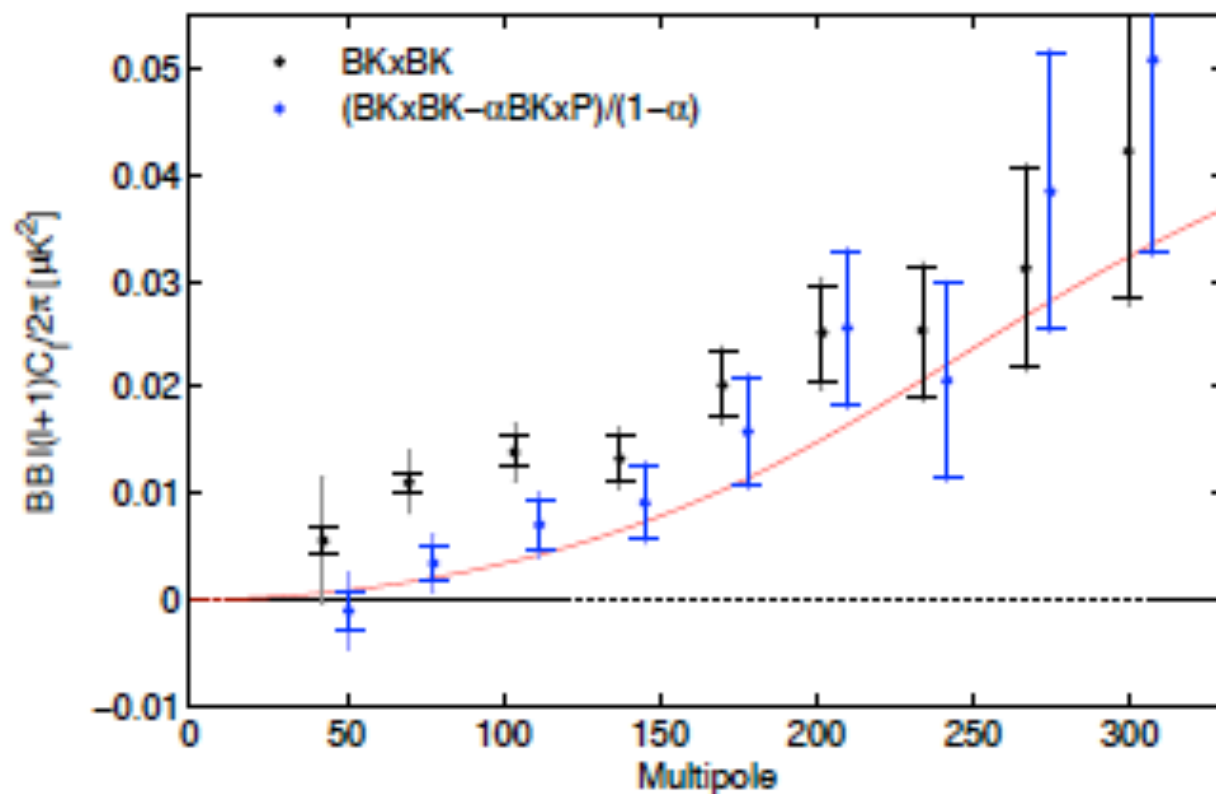
Planck 2015



1502.00114

- Bound on tensor mode: Planck TT+lowP: $r_{0.002} < 0.10$ (95% CL)
 $\Rightarrow$ + running: $r_{0.002} < 0.18$ (95% CL)
- No non-Gaussianity observed: canonical single field inflation favored. e.g. $f_{NL}^{\text{local}} = 0.8 \pm 5.0$ (T & E 68% CL)

Dust and tensor mode

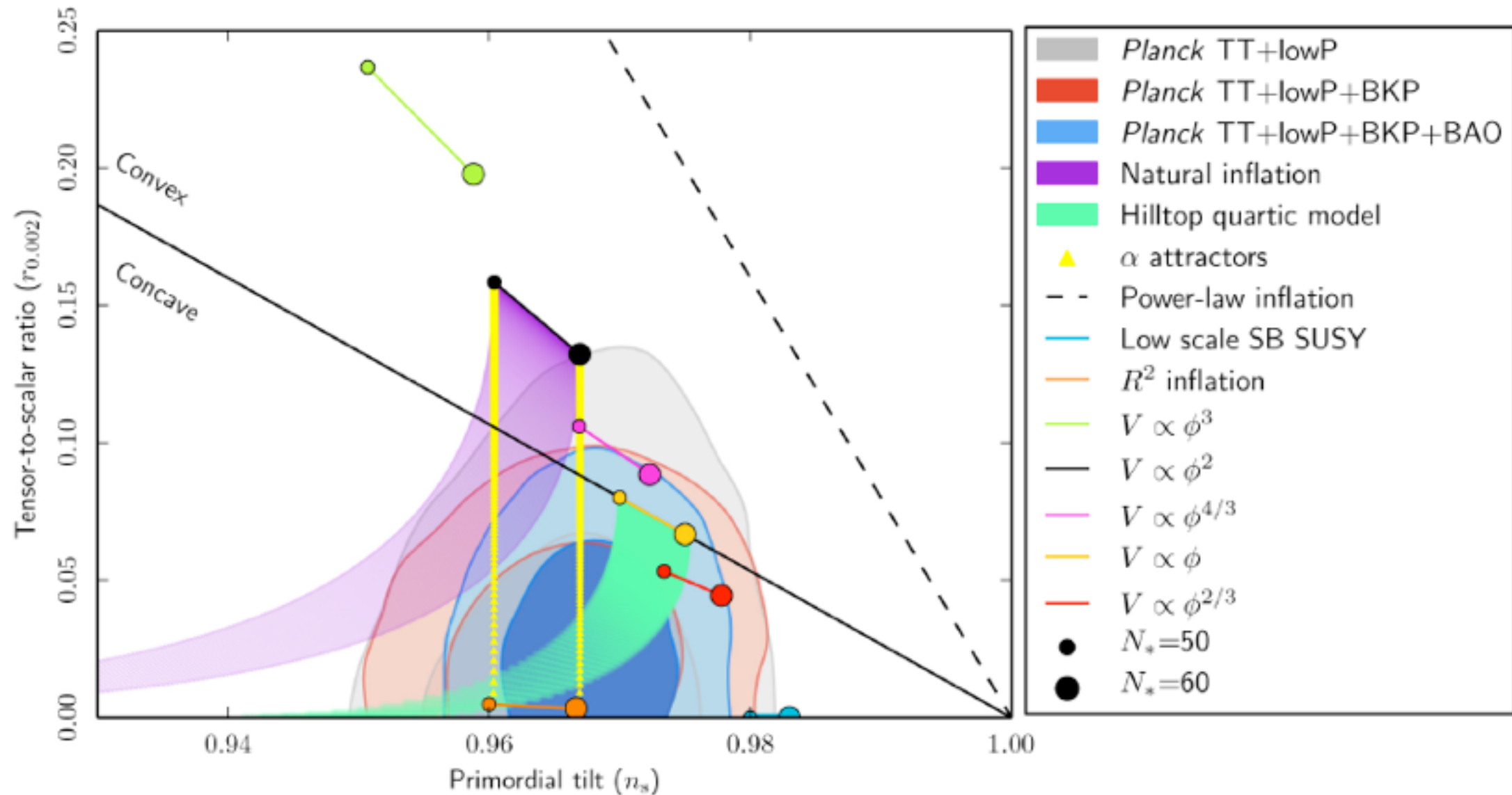


Blue: after subtraction of dust,
estimated from Planck 353GHz.

1502.00612

- Posterior probability peaks at $r=0.05$, but $r=0$ is allowed with large probability.

Planck+BICEP2+Keck



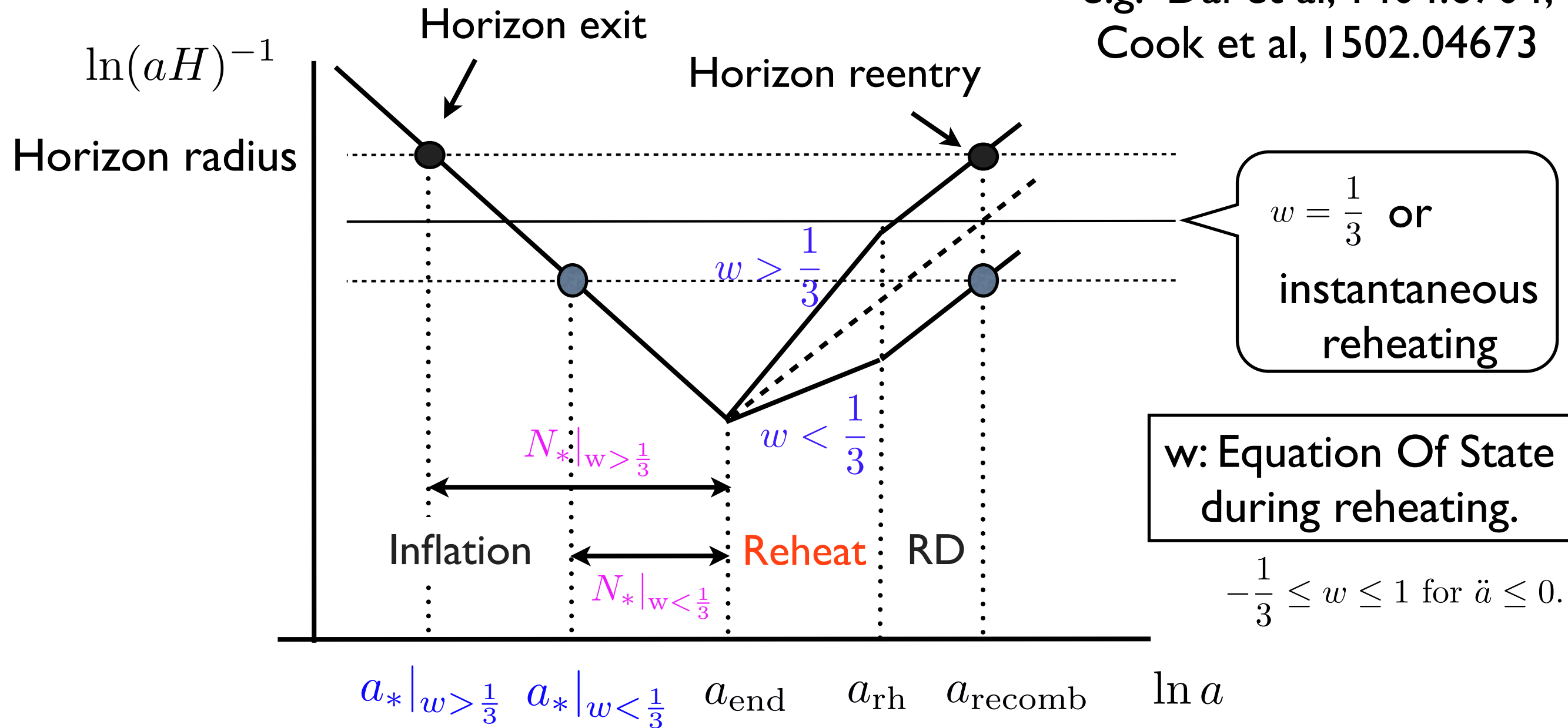
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- BICEP2+Keck array data at 150GHz are consistent with Planck maps at higher frequencies.

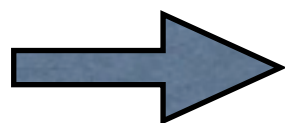
Tensor-to-scalar ratio: $r_{0.05} < 0.12$ (95% CL)

Reheating & EOS

e.g. Dai et al, I404.6704;
Cook et al, I502.04673



$$\ln(aH)_I^{-1} \sim -\ln a, \quad \ln(aH)_{rh}^{-1} \sim \frac{1}{2}(1 + 3w) \ln a, \quad \ln(aH)_{RD}^{-1} \sim \ln a,$$



$$N_*|_{w > \frac{1}{3}} > N_*|_{w = \frac{1}{3}} > N_*|_{w < \frac{1}{3}}$$

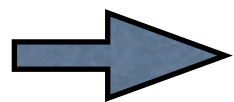
w from preheating

- A small coupling to another scalar can change the equation of state w during preheating.

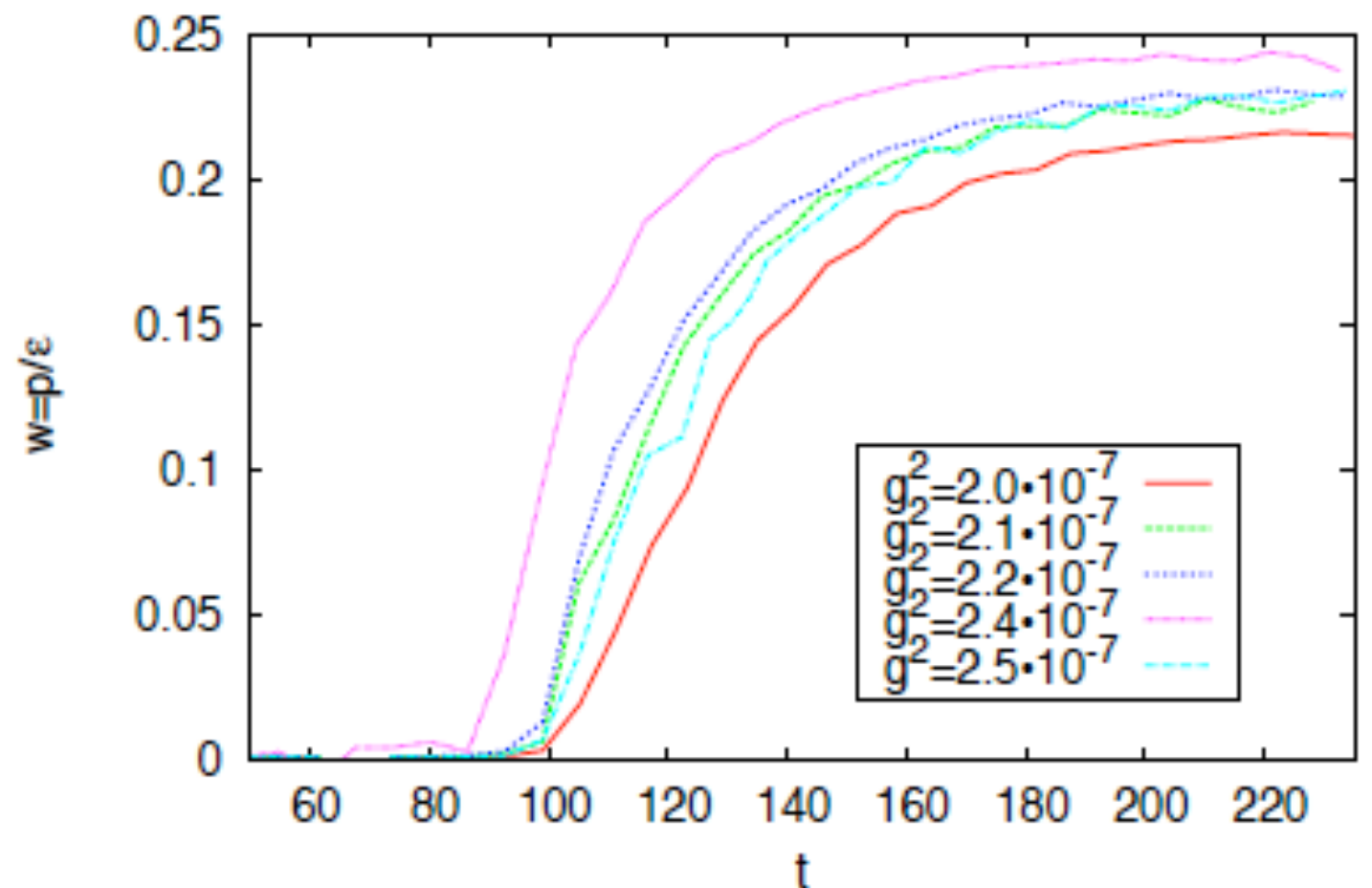
e.g. quadratic inflation

Immediately after
inflation, $\langle w \rangle = 0$

$$\mathcal{L}_{int} = -\frac{g^2}{2}\phi^2\chi^2$$



w changes sharply from w=0
at the end of preheating.



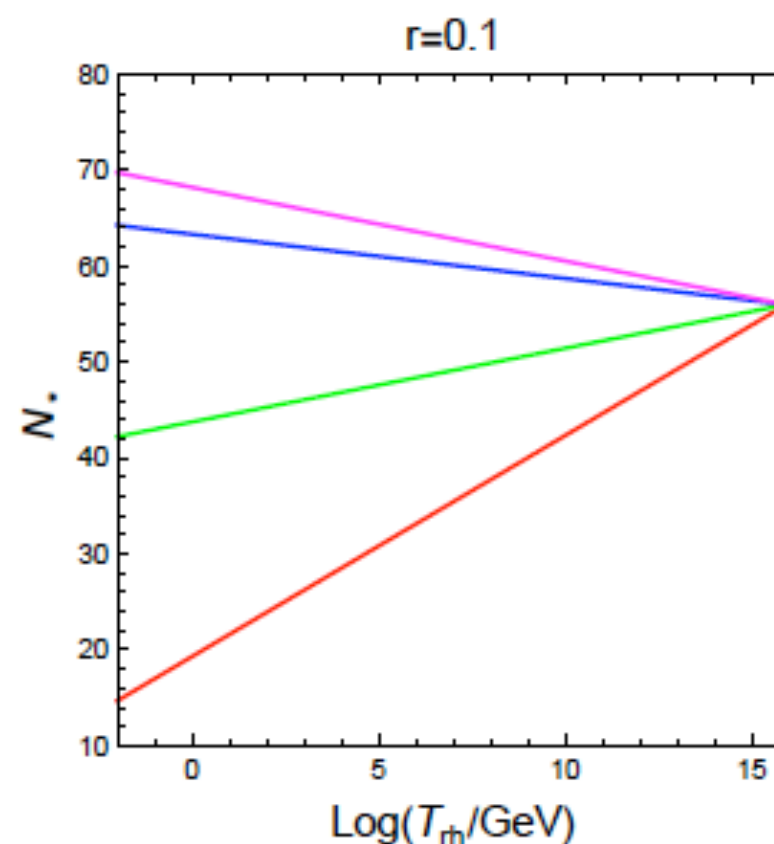
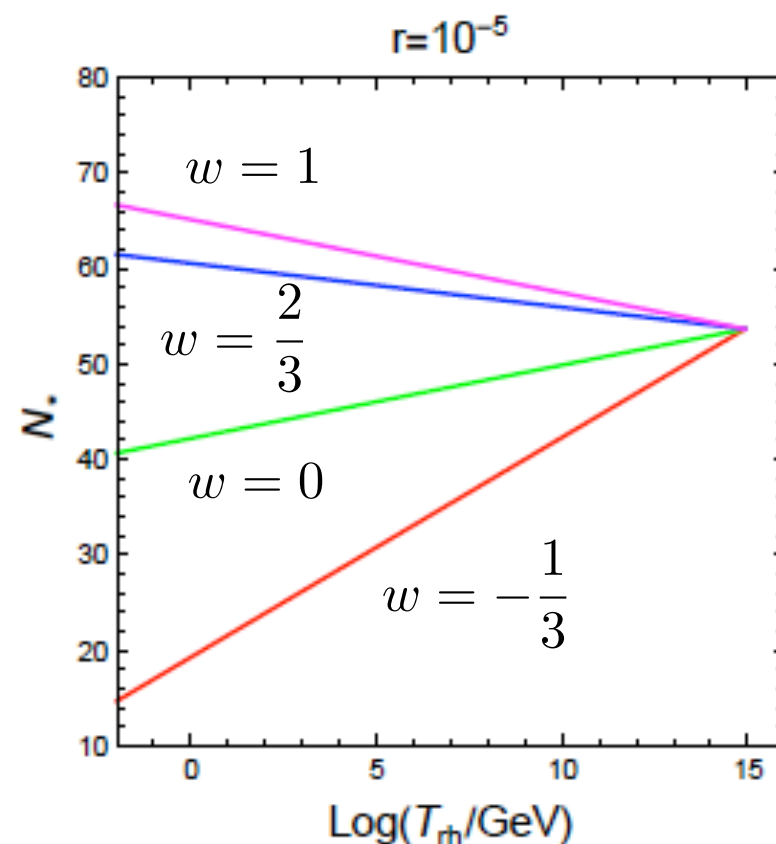
Podolsky et al,
hep-ph/0507096

Number of efoldings

$$N_* = 67.2 + \frac{1}{4}(3w - 1)N_{\text{rh}} - \ln\left(\frac{k}{a_0 H_0}\right) - \ln\left(\frac{V_{\text{end}}^{1/4}}{H_*}\right) - \frac{1}{12}\ln(g_*(T_{\text{rh}}))$$

➔
$$N_* = 61.4 + \frac{3w - 1}{12(1 + w)} \ln\left(\frac{45}{\pi^2} \frac{V_*}{g_*(T_{\text{rh}}) T_{\text{rh}}^4}\right) - \ln\left(\frac{V_*^{1/4}}{H_*}\right).$$

Planck, l 303.5082; Cook et al, l 502.04673



cf. $\Delta N_* = 0$:

$$N_* = 53.7 + \frac{1}{4} \ln(r/10^{-5}).$$

- Reheating temperature and equation of state w could change N_* and the inflation predictions.

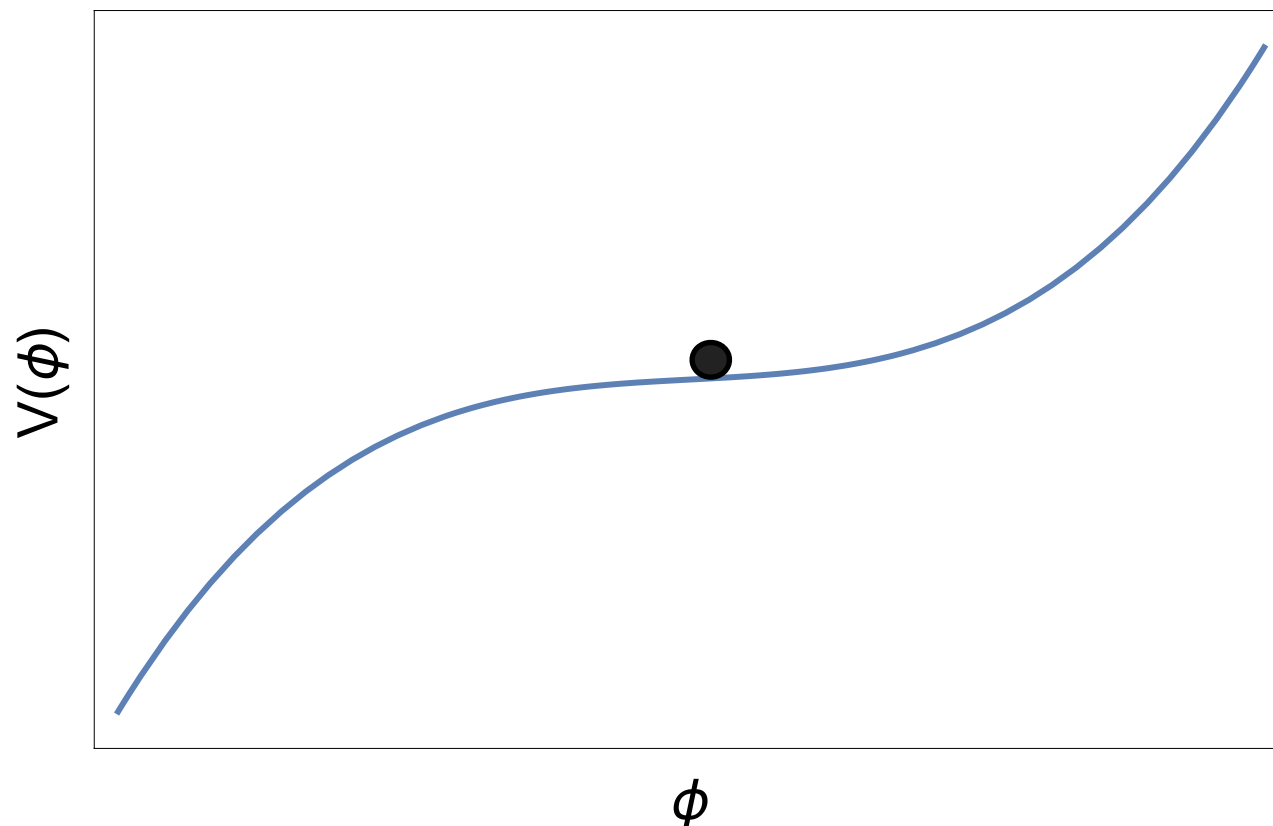
Inflation at criticality

- Small or large field values have been considered in usual inflation models.

Small fields - graceful exit?

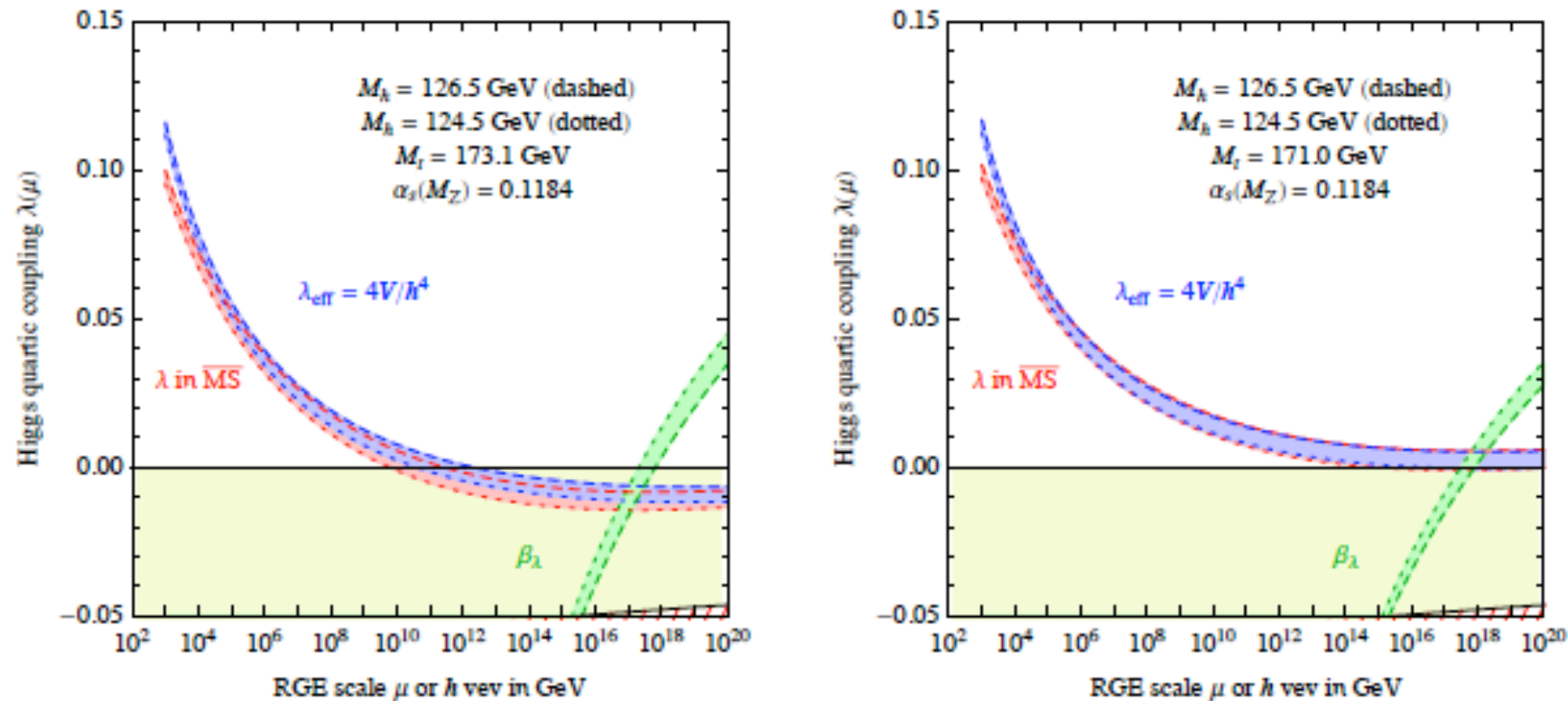
Large fields - quantum gravity?

- Symmetry could be enhanced at a certain field space and protect large (quantum) corrections to inflation.



Inflection point inflation?
+ reheating dynamics

Higgs at criticality?



Degrassi et al, 1205.6497

- SM Higgs quartic coupling as well as its beta function might vanish at a similar scale: criticality.
 ➡ Inflation at criticality (inflection point)?

cf. Similar models> D-brane inflation: Baumann et al, 0705.3837,
 MSSM flat-direction: Allahverdi et al, hep-ph/0605035

Inflation and reheating at inflection point

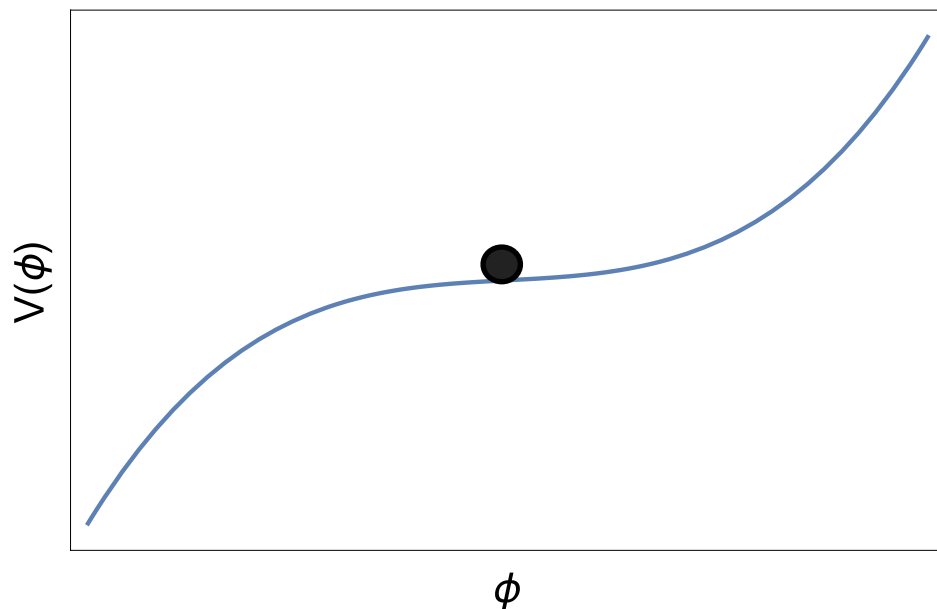
Inflection point inflation

- Expand the inflaton potential near inflection point(IP):

$$V = V_0 + \lambda_1(\phi - \phi_0) + \frac{1}{3!} \lambda_3(\phi - \phi_0)^3 \quad (V_0, \lambda_1, \lambda_3 : \text{positive const.})$$

(Suppressed higher order terms for small field excursion or small coefficients.)

$\lambda_1 > 0$
ensures graceful exit.



e.g. Baumann et al, 0705.3837
(warped D-brane inflation)

Slow-roll
parameters:

$$\epsilon \simeq \frac{1}{2} \left(\frac{\lambda_1 + \frac{1}{2} \lambda_3 (\phi - \phi_0)^2}{V_0} \right)^2,$$

$$\eta \simeq \frac{\lambda_3}{V_0} (\phi - \phi_0).$$

Number of efoldings:

$$N_* = \frac{N_{\max}}{\pi} \left(\arctan \left(\frac{N_{\max}}{2\pi} \eta_* \right) - \arctan \left(\frac{N_{\max}}{2\pi} \eta_{\text{end}} \right) \right)$$

$$N_{\max} \equiv \int_{-\infty}^{+\infty} \frac{d\phi}{\sqrt{2\epsilon}} = \pi V_0 \sqrt{\frac{2}{\lambda_1 \lambda_3}}.$$

$$N_{\max} \gtrsim 2N_* \quad \frac{V_0}{\sqrt{\lambda_1 \lambda_3}} \ll 1 : \text{ necessary condition for large N.}$$

Inflation conditions

- Sufficient number of efoldings

$$\frac{V_0}{\sqrt{\lambda_1 \lambda_3}} \ll 1$$

- Slow-roll or small tensor mode

$$\lambda_1 \ll V_0$$

- Small vs large field excursions + above two

$$V_0 \lesssim \lambda_3 : \text{sub-Planckian} \quad \longrightarrow \quad \lambda_1 \ll V_0 \lesssim \lambda_3$$

$$V_0 \gtrsim \lambda_3 : \text{trans-Planckian} \quad \longrightarrow \quad \lambda_3 \ll \lambda_1 \ll V_0$$

IP inflation vs Planck

- Spectral index and tensor-to-scalar ratio are given by

$$n_s = 1 - 3 \left(\frac{\lambda_1}{V_0} \right)^2 + \frac{4\pi}{N_{\max}} \tan \left(\pi \frac{N_*}{N_{\max}} + \arctan \left(\frac{N_{\max}}{2\pi} \eta_{\text{end}} \right) \right),$$

$$r = 8 \left(\frac{\lambda_1}{V_0} \right)^2.$$

Planck TT, TE, EE + low P

$$n_s = 0.9652 \pm 0.0047$$

$$r < 0.10 \text{ at } 95 \% \text{ C.L.}$$

- CMB normalization fixes one parameter while the other two are to be determined by n_s (or $N_{\max}$) and r .

$$A_s = \frac{1}{24\pi^2} \frac{V_*}{\epsilon_*} \simeq 2.196 \times 10^{-9} \quad \text{at } k = 0.05 \text{ Mpc}^{-1}$$

$$\Rightarrow V_0 = 3.25 \times 10^{-9} \left(\frac{r}{0.10} \right), \quad \lambda_3 = 3.98 \times 10^{-11} \left(\frac{120}{N_{\max}} \right)^2 \left(\frac{r}{0.10} \right)^{1/2}$$

$$r = 0.10 \left(\frac{\lambda_1}{3.63 \times 10^{-10}} \right)^{2/3}$$

Small-field case

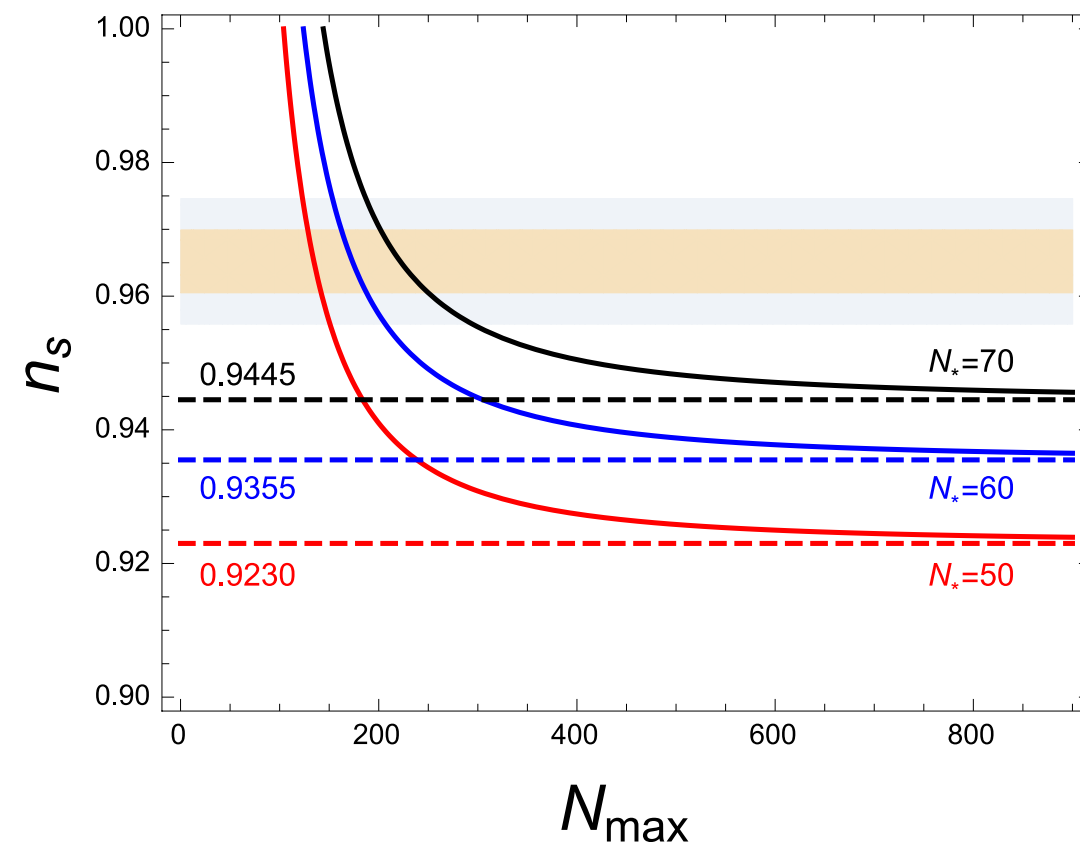
Baumann et al, 0706.0360

- Perturbative regime:

$$\lambda_1 \ll V_0 \lesssim \lambda_3$$

$$\eta_{\text{end}} = -1$$

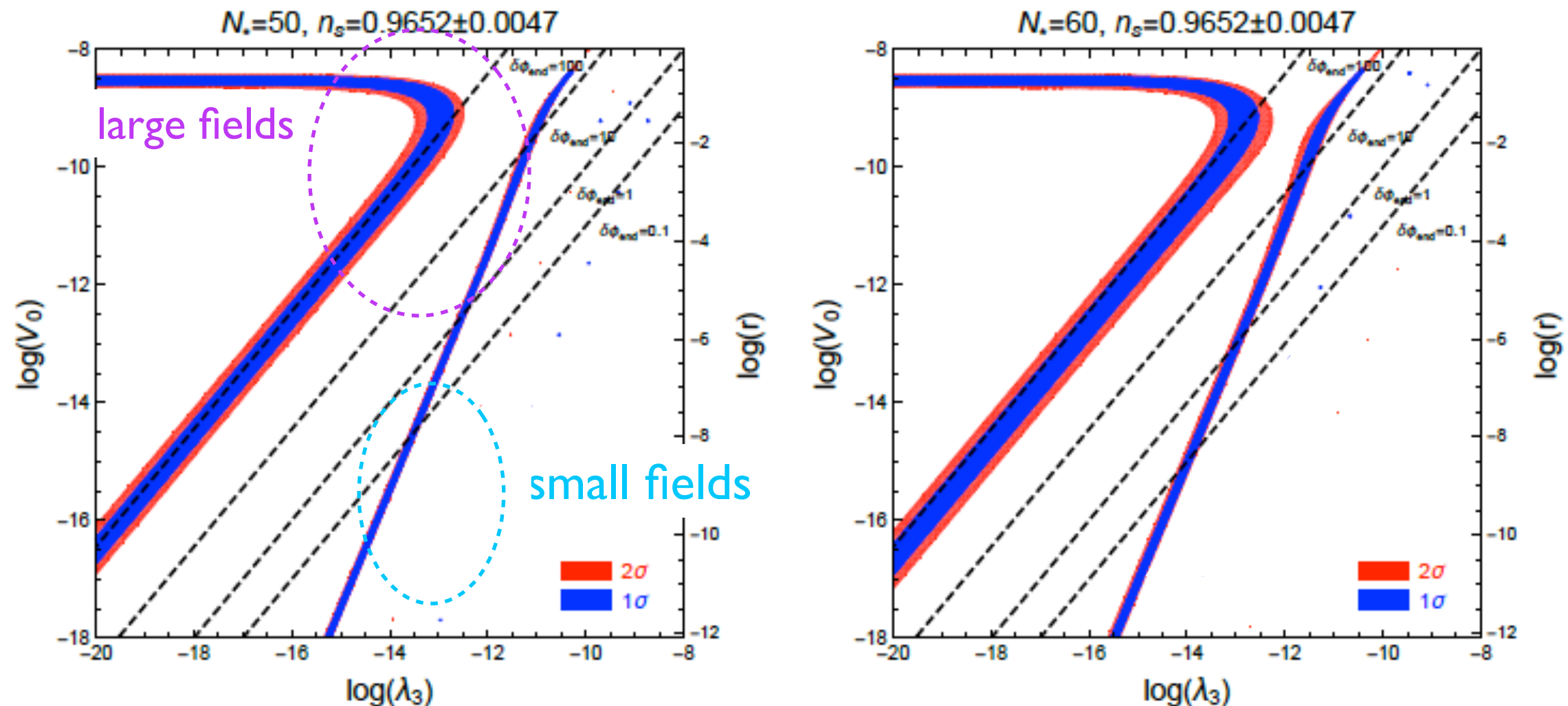
$$N_{\text{max}} = \pi V_0 \sqrt{\frac{2}{\lambda_1 \lambda_3}} \sim 200$$



- Tensor-to-scalar ratio is very small.

$$\frac{V_0}{\lambda_3} = \left(\frac{N_{\text{max}}}{120} \right)^2 \left(\frac{r}{1.50 \times 10^{-5}} \right)^{1/2} \Rightarrow \boxed{r \lesssim 10^{-6}}$$

Large field case



- Trans-Planckian field could lead to a large $r \sim 0.1$.
- Higher order terms?

$$V = V_0 + \lambda_1 \delta\phi + \frac{\lambda_3}{3!} (\delta\phi)^3 + \boxed{\frac{\lambda_4}{4!} (\delta\phi)^4} + \dots$$

$\delta\phi \sim 100$

$\Rightarrow \lambda_4 < 0.04\lambda_3?$

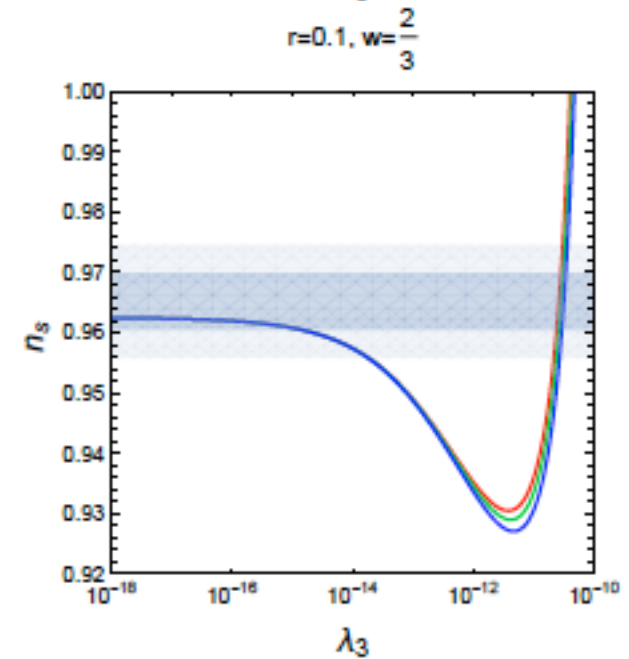
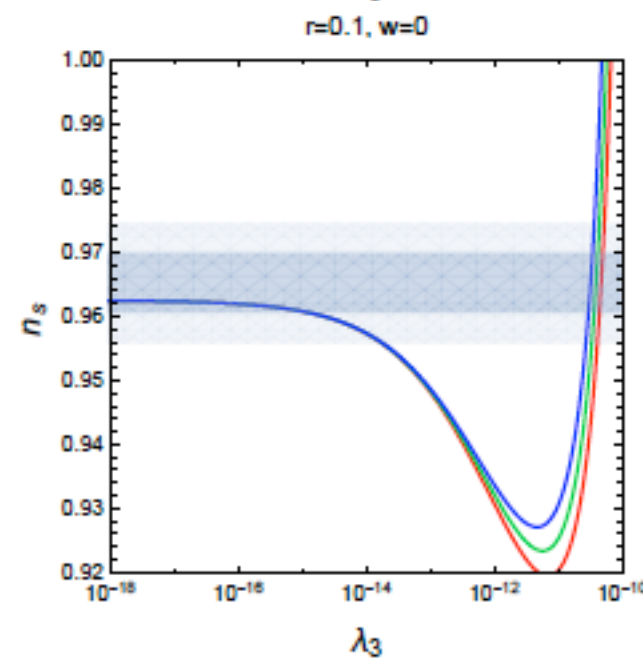
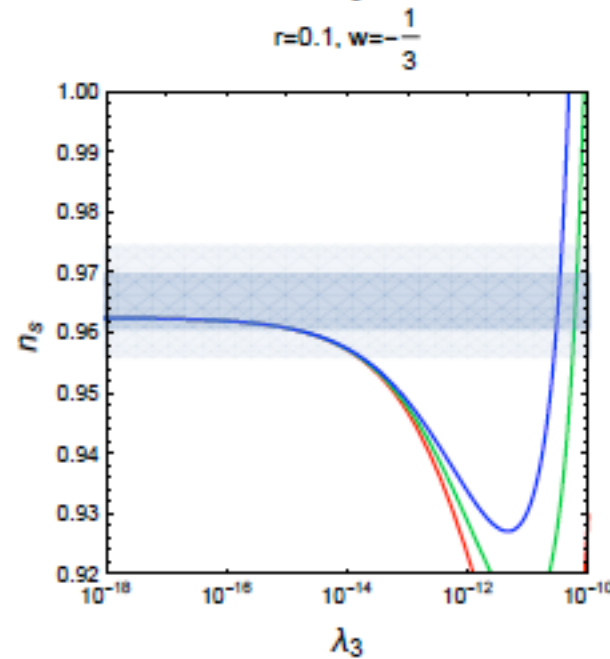
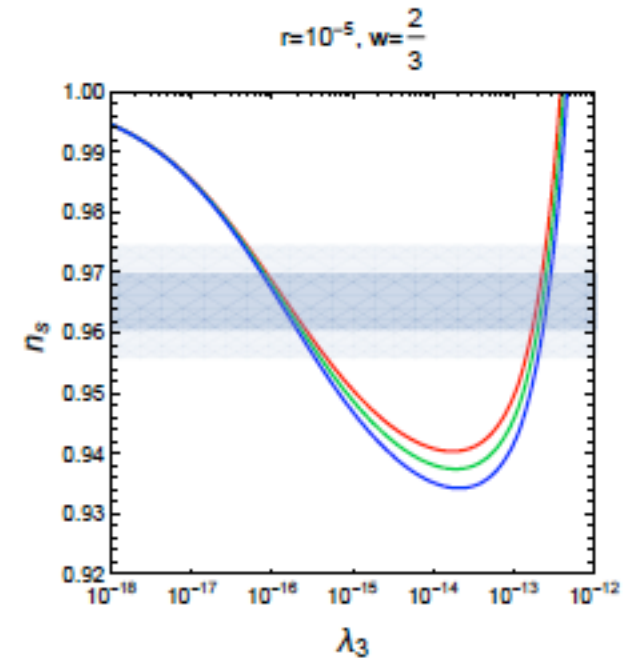
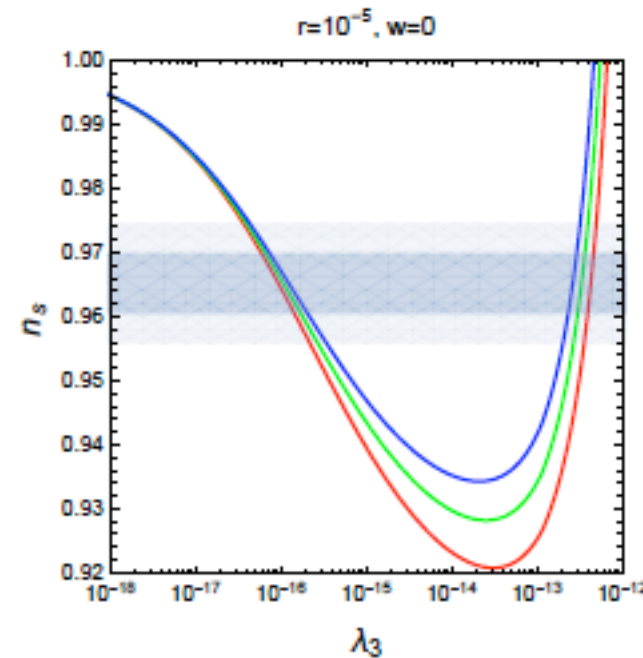
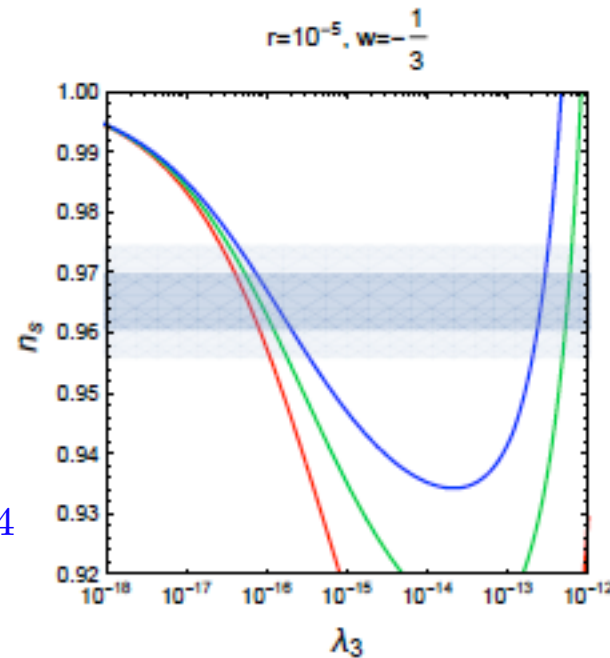
Reheating & effective coupling

$$T_{\text{rh}} = 10^3 \text{ GeV}$$

$$T_{\text{rh}} = 10^9 \text{ GeV}$$

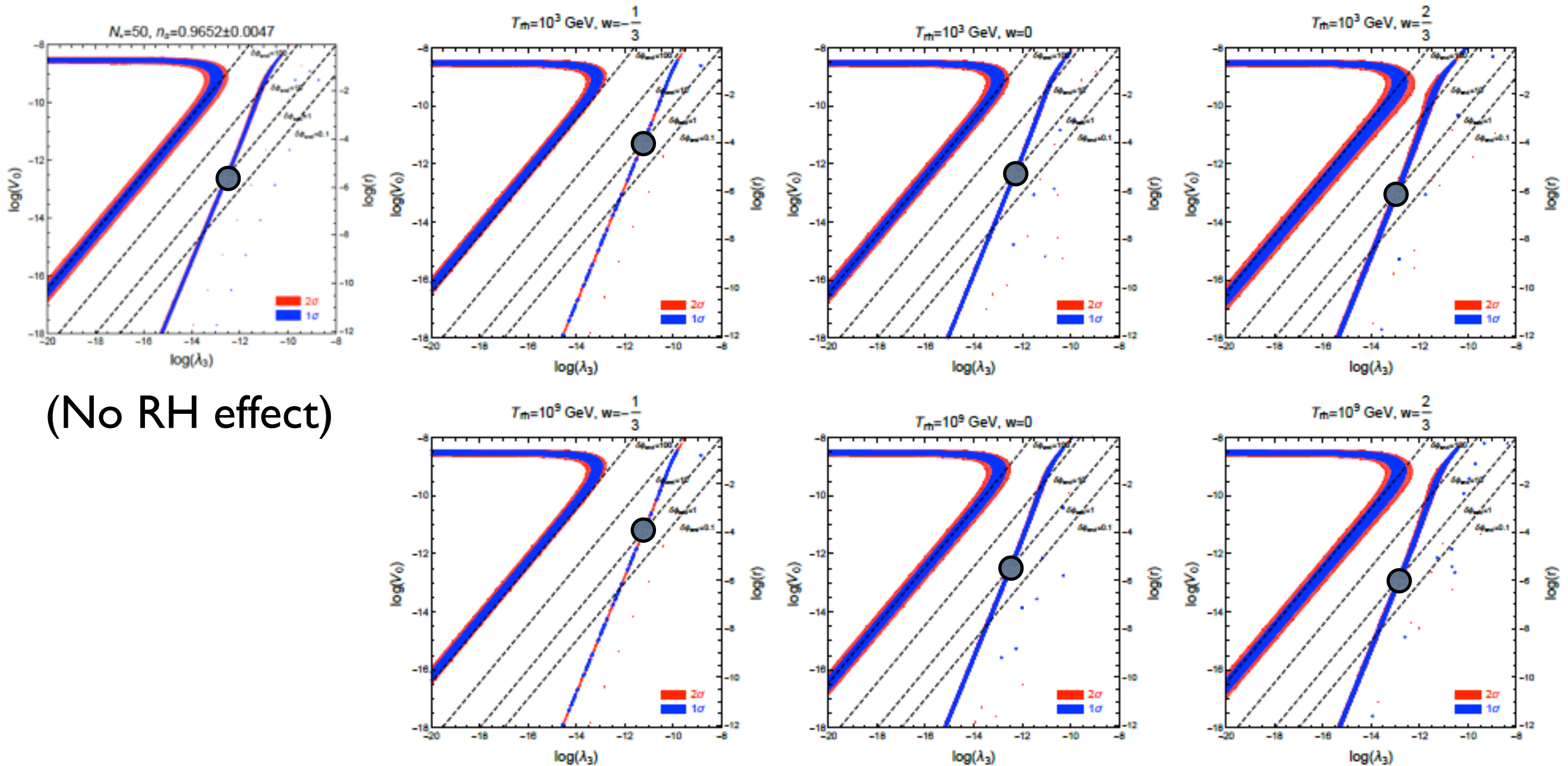
$$T_{\text{rh}} = T_{\text{max}}$$

$$= 8.5 \times 10^{14} (r/10^{-5})^{1/4}$$



- $w < 1/3$ (smaller N_*): the lower T_{rh} , the smaller λ_3 .
- $w > 1/3$ (larger N_*): the lower T_{rh} , the larger λ_3 .

Reheating & tensor mode



- In perturbative regime, tensor-to-scalar ratio is $10^{-6} - 10^{-4}$, getting larger for $w < 1/3$.

Higgs inflation at criticality

SM Higgs inflation

- Near criticality, the effective Higgs quartic and its beta function is vanishingly small.

$$V(h) = \frac{1}{4}\lambda(h)h^4, \quad \lambda(h) = \lambda_{\text{cr}} + b \left(\ln \frac{h}{h_{\text{cr}}} \right)^2, \quad b = 10^{-5}, \quad h_{\text{cr}} \sim 1.$$

➡ Effective parameters near IP:

$$V_0 = \frac{1}{24}b \left(\frac{37}{12} - 7\sqrt{\frac{25}{144} - \frac{\lambda_{\text{cr}}}{b}} \right) h_0^4,$$

$$\lambda_1 = \frac{2}{3}b \left(\frac{1}{3} - \sqrt{\frac{25}{144} - \frac{\lambda_{\text{cr}}}{b}} \right) h_0^3,$$

$$\lambda_3 = 6b\sqrt{\frac{25}{144} - \frac{\lambda_{\text{cr}}}{b}} h_0$$

Here, IP condition:

$$\ln \frac{h_0}{h_{\text{cr}}} = -\frac{7}{12} + \sqrt{\frac{25}{144} - \frac{\lambda_{\text{cr}}}{b}}$$

- Small slope: $\lambda_1 \ll V_0 \Rightarrow \lambda_{\text{cr}} \approx \frac{b}{16}, \quad h_0 \approx e^{-\frac{1}{4}} h_{\text{cr}}.$

$$V_0 \approx \frac{1}{24}bh_0^4, \quad \lambda_3 \approx 2bh_0 \Rightarrow N_{\text{max}} \sim 0.5 h_0^{1/2} : \text{too small.}$$

Higgs with non-minimal coupling

- Non-minimal coupling makes Higgs potential flat, even near inflection point located at $\gtrsim 1/\sqrt{\xi}$.
- Effective Higgs potential with non-minimal coupling:

$$S = \int d^4x \sqrt{-g} \left(\frac{1}{2}(1 + \xi h^2)R - \frac{1}{2}(\partial_\mu h)^2 - \frac{1}{4}\lambda(h^2 - v^2)^2 \right)$$

$$\Rightarrow S = \int d^4x \sqrt{-g_E} \left(\frac{1}{2}R - \frac{1}{2}(\partial_\mu \chi)^2 - V_E \right), \quad \frac{d\chi}{dh} = \frac{\sqrt{1 + \xi(1 + 6\xi)h^2}}{1 + \xi h^2},$$

$$V_E = \frac{1}{4}\lambda\varphi^4, \quad \varphi \equiv \frac{h}{\sqrt{1 + \xi h^2}}, \quad \lambda(\varphi) = \lambda_{\text{cr}} + b \left(\ln \frac{\varphi}{\varphi_{\text{cr}}} \right)^2.$$

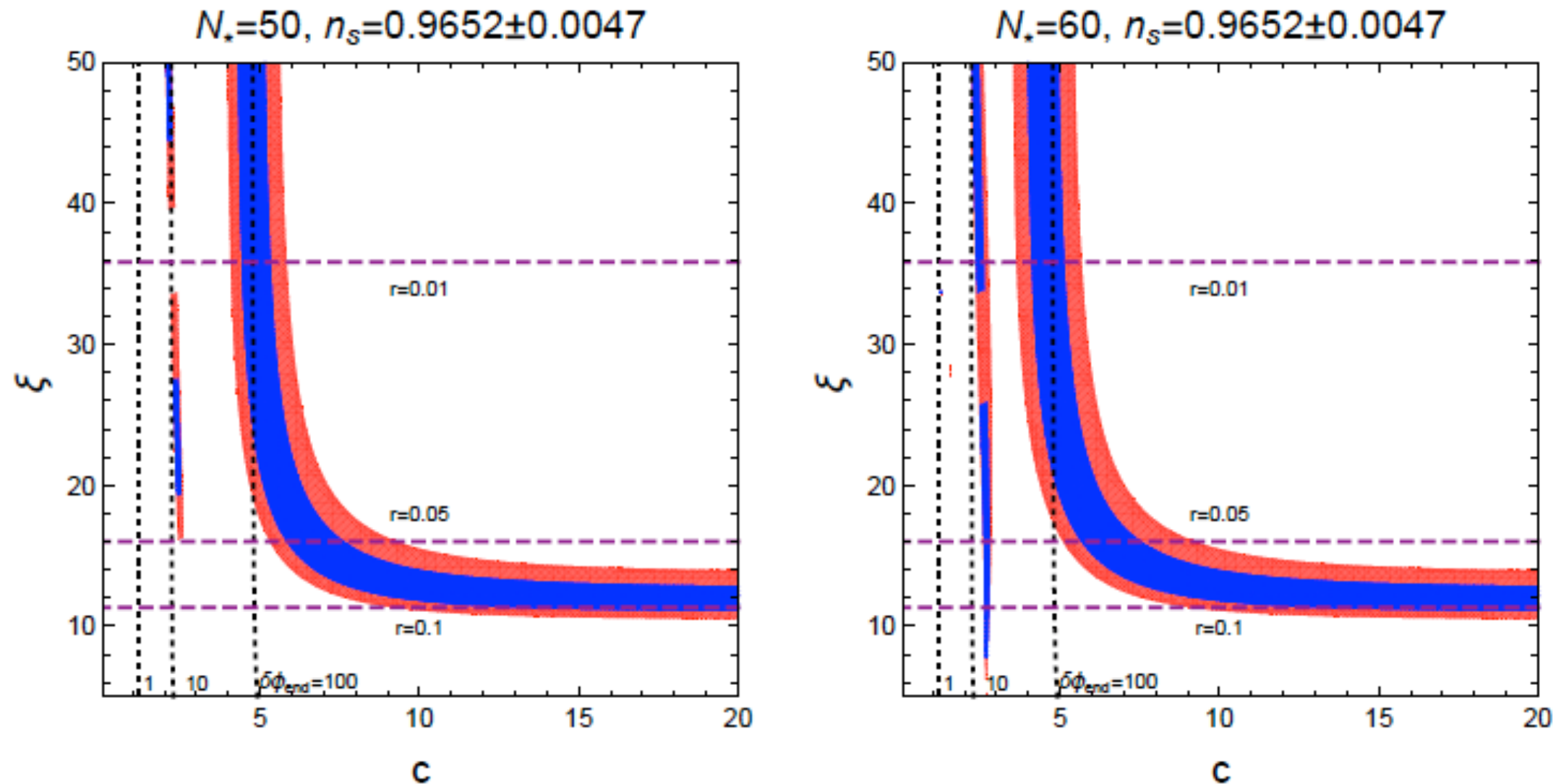
- Derivative wrt canonical Higgs is suppressed:

$$\frac{d}{d\chi} = \frac{dh}{d\chi} \frac{d\varphi}{dh} \frac{d}{d\varphi} \sim \frac{h}{\sqrt{6}} \cdot \frac{1}{\xi^{3/2} h^3} \cdot \frac{d}{d\varphi} \sim \frac{1}{\sqrt{6}\xi^{3/2} h^2} \frac{d}{d\varphi}$$

$\Rightarrow$ higher derivatives are naturally small.

Results

$$h_0 \equiv \frac{c}{\sqrt{\xi}}$$



- Tensor-to-scalar ratio is in a testable range.
- Canonical Higgs field is trans-Planckian, but higher order terms are suppressed by $(\xi^{3n/2} c^{2n})^{-1}$.

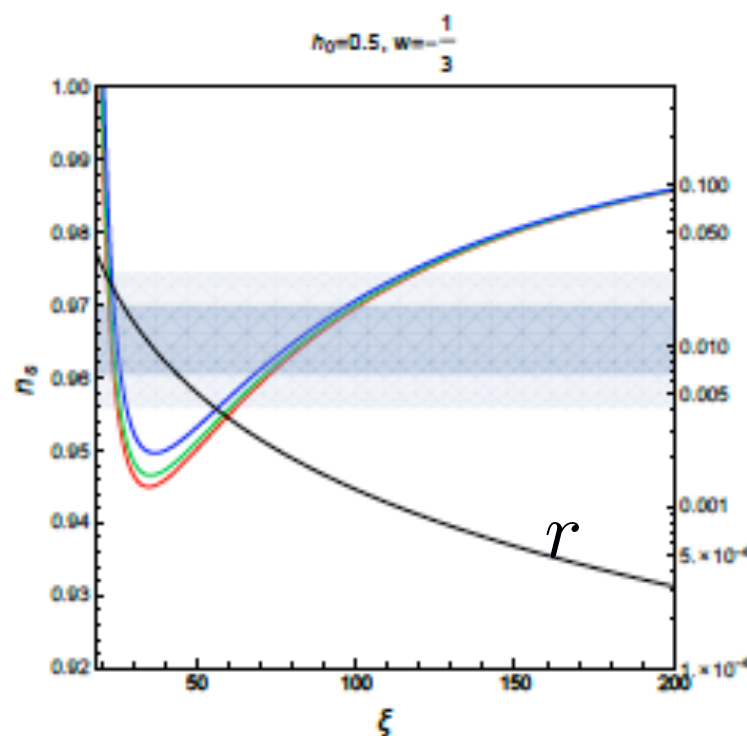
Reheating by Higgs

- Higgs couples to the SM particles with sizable interactions.

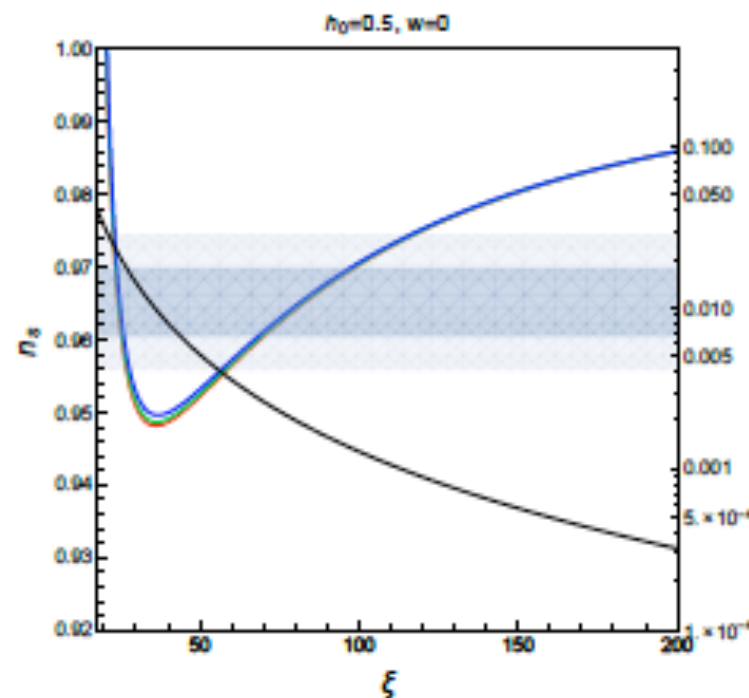
➔ Reheating temperature is typically high.

e.g. classical Higgs inflation: $T_{\text{rh}} = 3 \times 10^{13} - 1.5 \times 10^{14} \text{ GeV}$

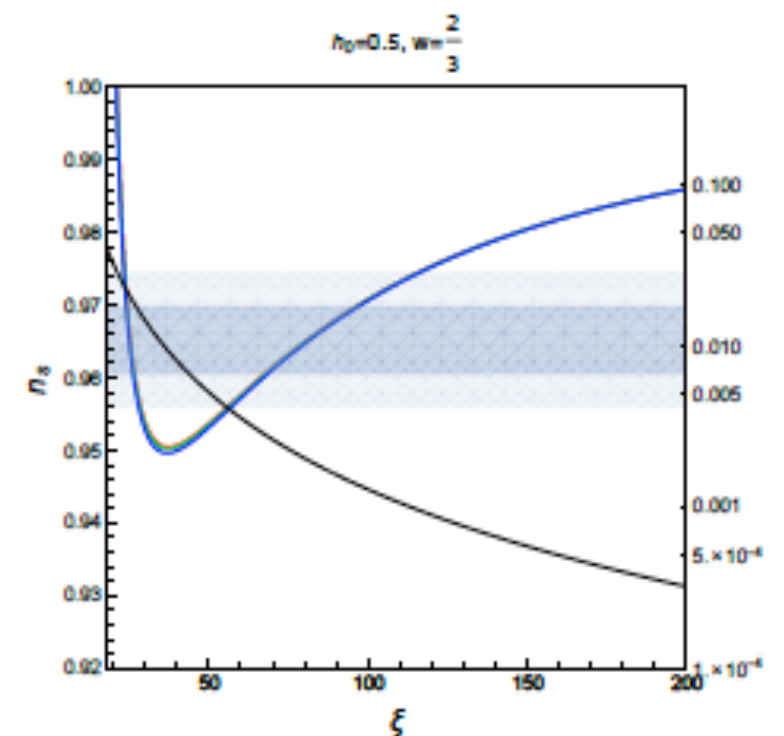
- Taking reheating temperature of similar order, the reheating effects on N^* are mild.



$$T_{\text{rh}} = T_{\text{max}}$$



$$T_{\text{rh}} = 3 \times 10^{13} \text{ GeV}$$



$$T_{\text{rh}} = 1.5 \times 10^{14} \text{ GeV}$$

Conclusions

- We have got the general results for the effective inflation near inflection point and the reheating dynamics in both small and large field regimes.
- New large field regimes could be consistent, if there is a suppression mechanism for higher order terms, such as enhanced symmetry.
- Determination of effective parameters or tensor-to-scalar ratio depends on reheating dynamics.
- Higgs inflation at criticality belongs to a trans-Planckian inflection-point inflation but higher order terms are suppressed due to a sizable non-minimal coupling.