Dark pion DM: WIMP or SIMP ?

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Overview on WIMP/SIMP scenarios in hidden (dark) QCD models

Contents

- Hidden (Dark) QCD scenario

- WIMP scenario with the S-H portal

- SIMP scenario in dark QCD

- SIMP + dark resonances (vector, scalar, etc.)

Hidden (Dark) QCD Scenario

hQCD (Dark QCD): WIMP & SIMP

- Strassler + Zurek (2006) : hQCD + U(1)' , new collider signatures but no discussion on DM from hQCD. hep-ph/0604261. PLB (2007)

- B. Patt and F. Wilczek, hep-ph/0605188. "Higgs portal"

- Hur, Ko, Jung, Lee (2007): EWSB and CDM from h-QCD, arXiv:0709.1218 [hep-ph], PLB (2011)

- Hur, Ko (2007) : scale inv. extension of SM+hQCD. All the mass scales (including DM mass) from hQCD, written in 2007, arXiv:1103.2571 [hep-ph] PRL(2011)

- Proceedings: Int.J.Mod.Phys. A23 (2008) 3348-3351, AIP Conf.Proc. 1178 (2009) 37-43, arXiv:1012.0103 (ICHEP), etc

- Many works on scale sym. models or dark QCD models during the past years (apology for not citing all of them)

- Hochberg et al. : SIMP in Dark QCD (2014, 2015)

- Hatanaka, Jung, Ko : AdS/QCD approach, arXiv:1606.02969, JHEP (2016)

Hidden Sector

- Any NP @ TeV scale is strongly constrained by EWPT and CKMology

- Hidden sector made of SM singlets, and less constrained, and could make CDM

- Hidden gauge sym can stabilize CDM

- Generic in many BSM's including SUSY models

- Can address "QM generation of all the mass scales from strong dynamics in the hidden sector" (orthogonal to the Coleman-Weinberg) : Hur and Ko, PRL (2011) and earlier paper and proceedings

Nicety of QCD

- Renormalizable

- Asymptotic freedom : no Landau pole

- QM dim transmutation :

- Light hadron masses from QM dynamics

- Flavor & Baryon # conservations : accidental symmetries of QCD (pion is stable if we switch off EW interaction, ignoring dim-5 operators; proton is stable or very long lived) $\dfrac{1}{M_{\text{Planck}}} H^{\dagger} H \overline{q_h} \gamma_5 q_h$

h-pion & h-baryon DMs

- In most WIMP DM models, DM is stable due to some ad hoc Z_2 symmetry

- If the hidden sector gauge symmetry is confining like ordinary QCD, the lightest mesons and the baryons could be stable or long-lived >> Good CDM candidates

- If chiral sym breaking in the hidden sector, light h-pions can be described by chiral Lagrangian in the low energy limit
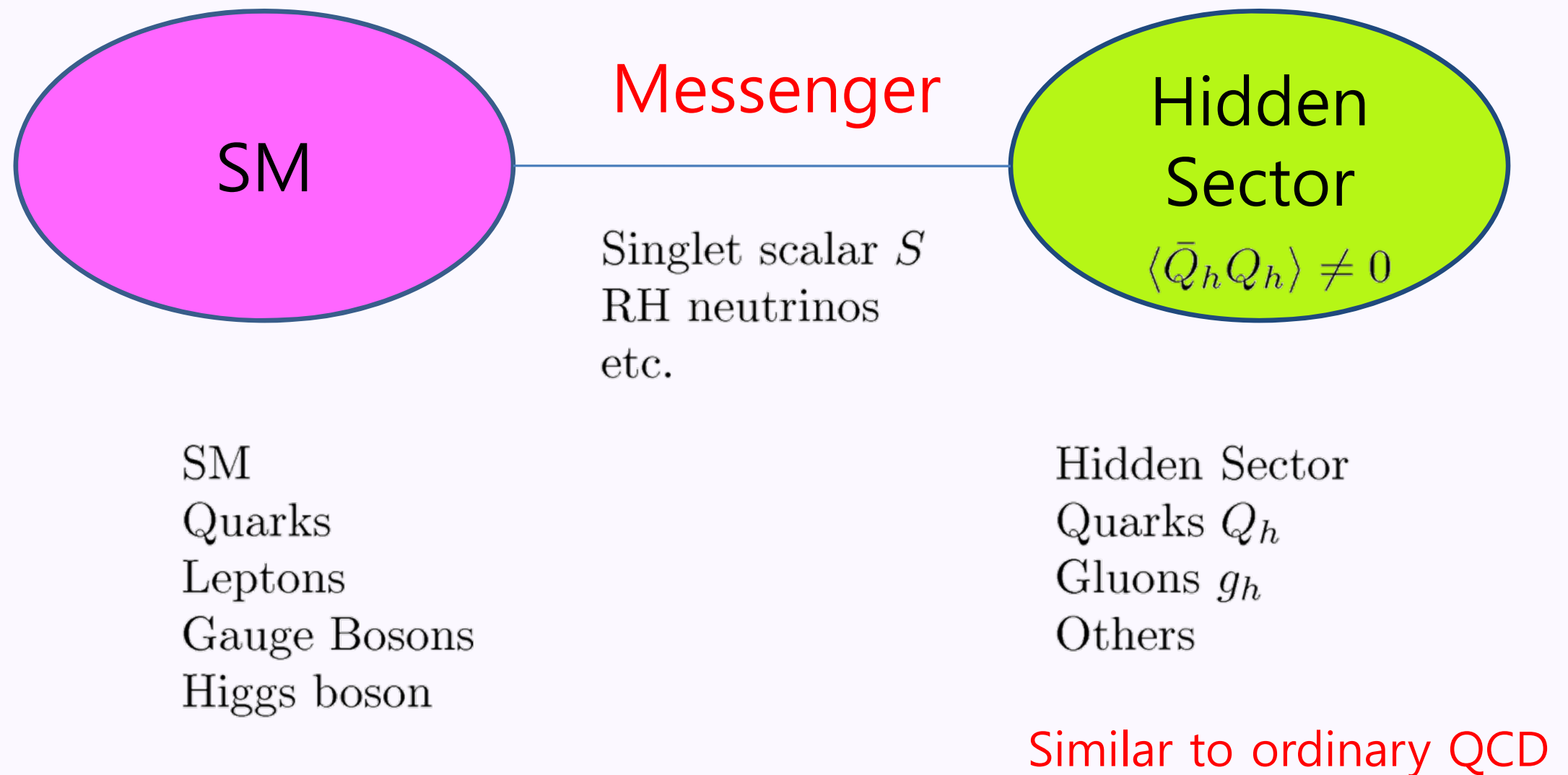
WIMP scenario with the Higgs-Singlet portal

- **Hur, Jung, Ko, Lee, arXiv:0709.1218**
- **Hur, Ko, 1103.2571, PRL (2011)**
- **Hatanaka, Jung, Ko, 1606.02969, JHEP (2016)**

And proceedings:

- **Int. J. Mod. Phys. A23 (2008) 3348-3351**
- **AIP Conf. Proc. 1178 (2009) 37-43**
- **ICHEP 2010 Proceeding, hep-ph/1012.0103**

Basic Picture

SM

Messenger

Hidden Sector
$\langle \bar{Q}_h Q_h \rangle \neq 0$

Singlet scalar S
RH neutrinos
etc.

SM
Quarks
Leptons
Gauge Bosons
Higgs boson

Hidden Sector
Quarks Q_h
Gluons g_h
Others

Similar to ordinary QCD

Key Observation

- If we switch off gauge interactions of the SM, then we find

- Higgs sector ~ Gell-Mann-Levy's linear sigma model which is the EFT for QCD describing dynamics of pion, sigma and nucleons

- One Higgs doublet in 2HDM could be replaced by the GML linear sigma model for hidden sector QCD

- Potential for H_1 and H_2

$$V(H_1, H_2) = -\mu_1^2(H_1^\dagger H_1) + \frac{\lambda_1}{2}(H_1^\dagger H_1)^2 - \mu_2^2(H_2^\dagger H_2)$$

$$+ \frac{\lambda_2}{2}(H_2^\dagger H_2)^2 + \lambda_3(H_1^\dagger H_1)(H_2^\dagger H_2) + \frac{av_2^3}{2}\sigma_h$$

Not present in the two-Higgs Doublet model

- Stability : $\lambda_{1,2} > 0$ and $\lambda_1 + \lambda_2 + 2\lambda_3 > 0$

- Consider the following phase:

$$H_1 = \begin{pmatrix} 0 \\ \frac{v_1 + h_{\mathrm{SM}}}{\sqrt{2}} \end{pmatrix}, \qquad H_2 = \begin{pmatrix} \pi_h^+ \\ \frac{v_2 + \sigma_h + i\pi_h^0}{\sqrt{2}} \end{pmatrix}$$

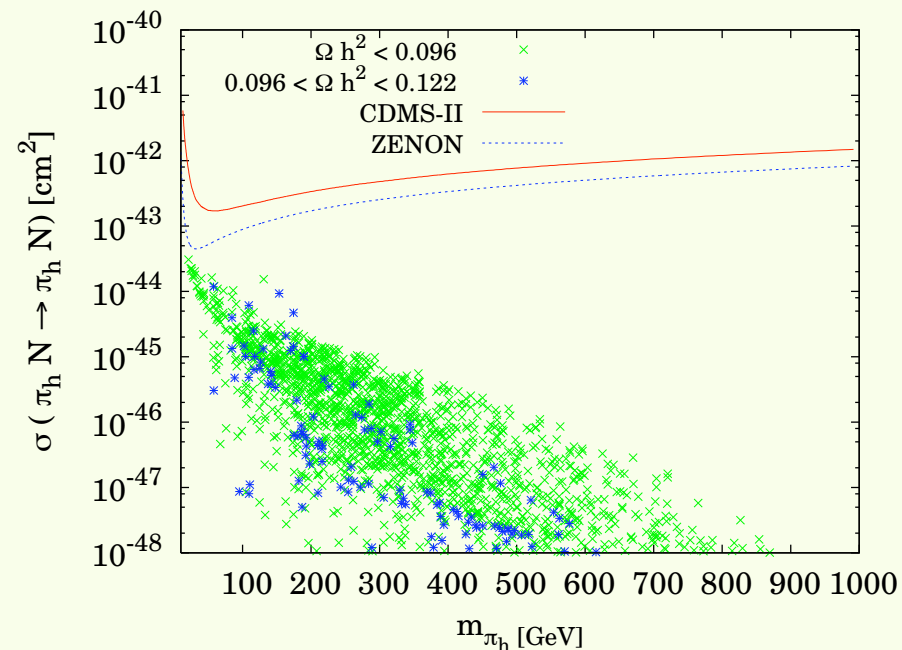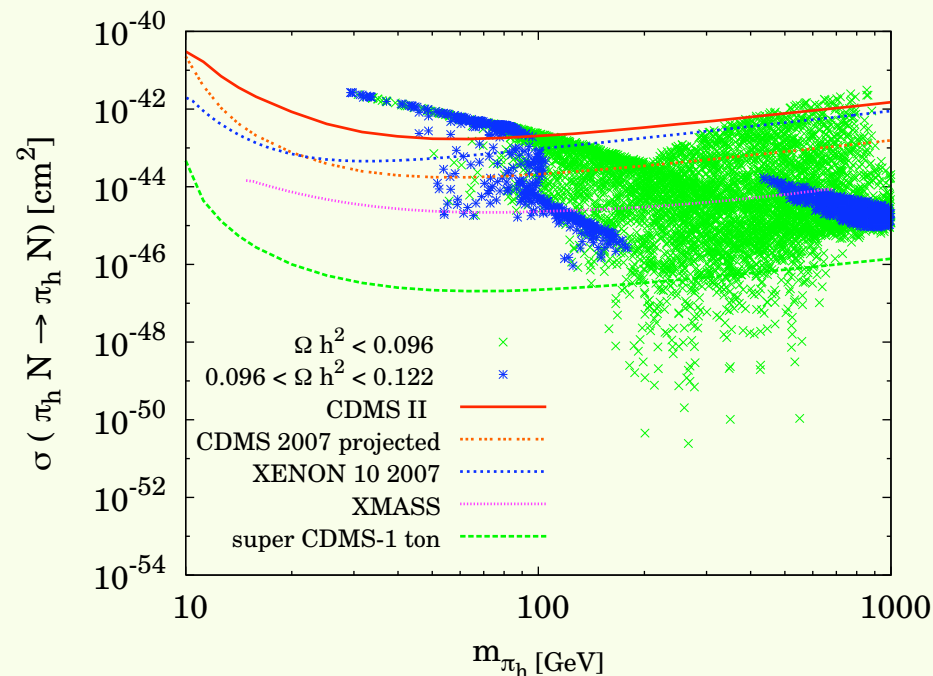- Correct EWSB : $\lambda_1(\lambda_2 + a/2) \equiv \lambda_1 \lambda_2' > \lambda_3^2$

Relic Density
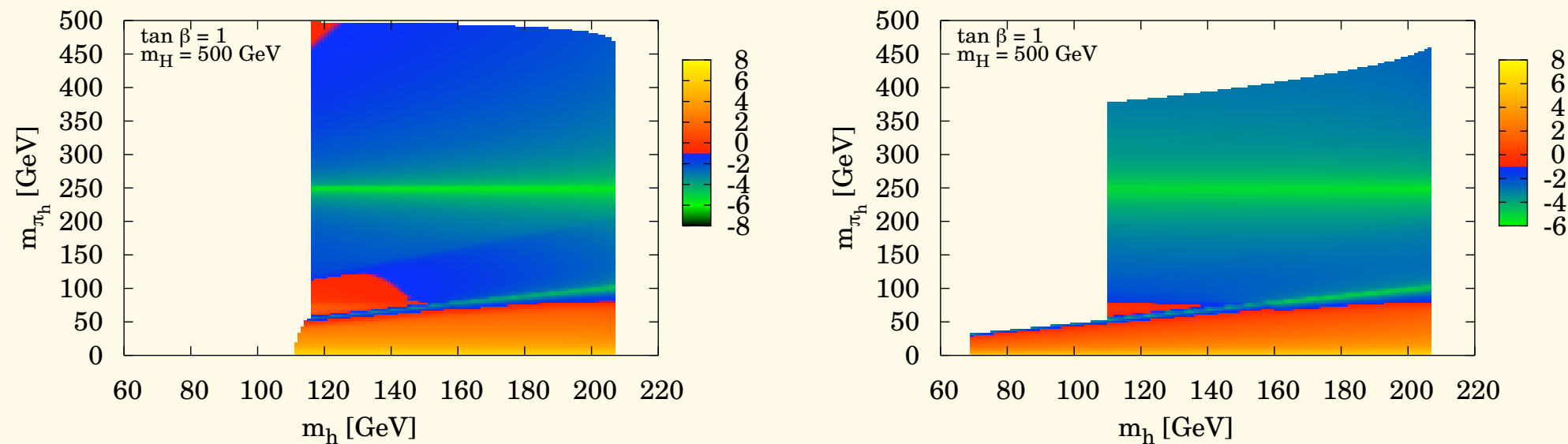
- $\Omega_{\pi_h} h^2$ in the (m_{h_1}, m_{π_h}) plane for $\tan\beta = 1$ and $m_H = 500$ GeV

- Labels are in the $\log_{10}$

- Can easily accommodate the relic density in our model

Direct detection rate

- $\sigma_{SI}(\pi_h p \to \pi_h p)$ as functions of m_{π_h} for $\tan\beta = 1$ and $\tan\beta = 5$.

- σ_{SI} for $\tan\beta = 1$ is very interesting, partly excluded by the CDMS-II and XENON 10, and als can be probed by future experiments, such as XMASS and super CDMS

- $\tan\beta = 5$ case can be probed to some extent at Super CDMS

Classical Scale Sym Model

- Scale invariant extension of the SM + hQCD

- Mass scale is generated by nonperturbative strong dynamics in the hidden sector

- EWSB and CDM from hQCD sector

All the masses (including CDM mass) from hidden sector strong dynamics

Kubo, Lindner et al with dark scalar QCD condensate

Appraisal of Scale Invariance

- May be the only way to understand the origin of mass dynamically (including spontaneous sym breaking)

- Without it, we can always write scalar mass terms for any scalar fields, and Dirac mass terms for Dirac fermions, the origin of which is completely unknown

- Probably only way to control higher dimensional op's suppressed by Planck scale

Model I (Scalar Messenger)
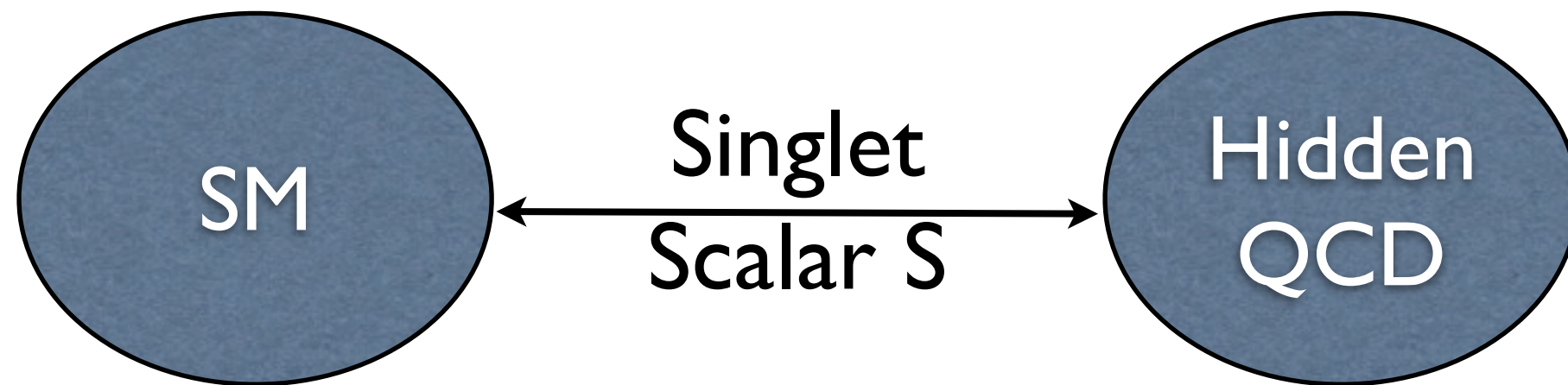
- SM - Messenger - Hidden Sector QCD

- Assume classically scale invariant lagrangian --> No mass scale in the beginning

- Chiral Symmetry Breaking in the hQCD generates a mass scale, which is injected to the SM by "S"

Scale invariant extension of the SM with strongly interacting hidden sector

Modified SM with classical scale symmetry

$$\mathcal{L}_{\text{SM}} = \mathcal{L}_{\text{kin}} - \frac{\lambda_H}{4}(H^\dagger H)^2 - \frac{\lambda_{SH}}{2}S^2 H^\dagger H - \frac{\lambda_S}{4}S^4$$

$$+ \left(\overline{Q}^i H Y_{ij}^D D^j + \overline{Q}^i \tilde{H} Y_{ij}^U U^j + \overline{L}^i H Y_{ij}^E E^j \right.$$

$$+ \left.\overline{L}^i \tilde{H} Y_{ij}^N N^j + S N^{iT} C Y_{ij}^M N^j + h.c. \right)$$

Model considered by Meissner and Nicolai, hep-th/0612165
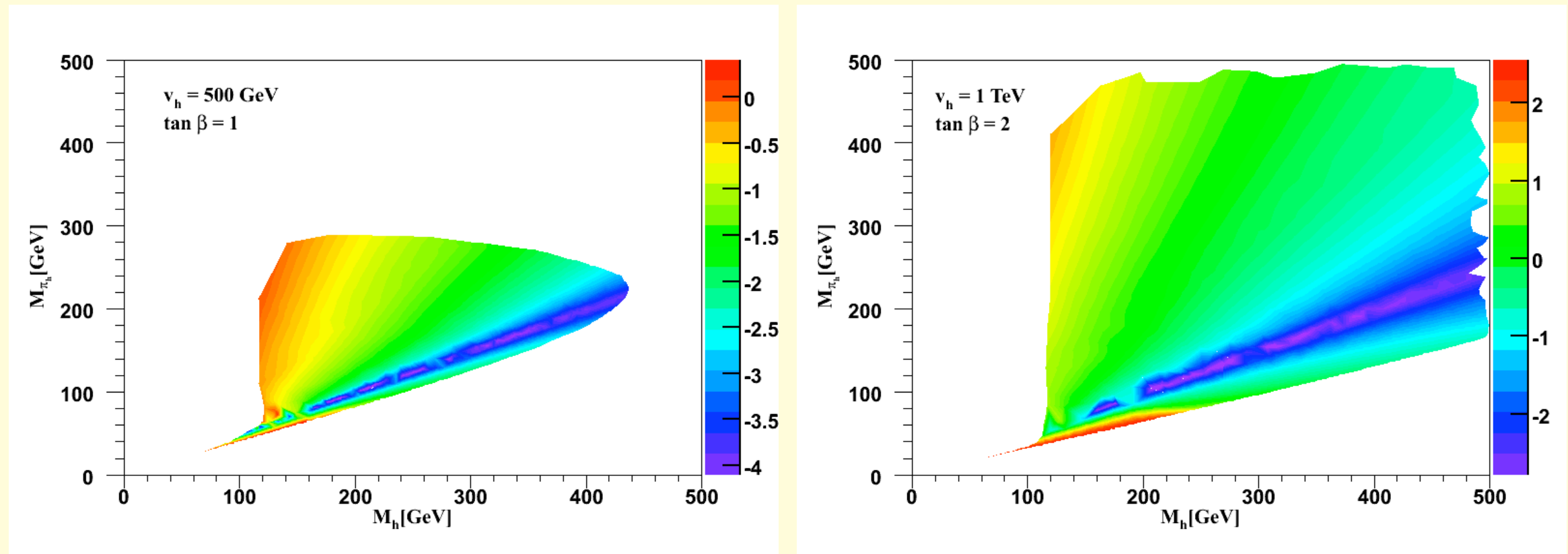
Hidden sector lagrangian with new strong interaction

$$\mathcal{L}_{\text{hidden}} = -\frac{1}{4}\mathcal{G}_{\mu\nu}\mathcal{G}^{\mu\nu} + \sum_{k=1}^{N_{HF}} \overline{\mathcal{Q}}_k(i\mathcal{D}\cdot\gamma - \lambda_k S)\mathcal{Q}_k$$

Effective lagrangian far below $\Lambda_{h,\chi} \approx 4\pi\Lambda_h$

$$
\begin{aligned}
\mathcal{L}_{\text{full}} &= \mathcal{L}_{\text{hidden}}^{\text{eff}} + \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{mixing}} \\
\mathcal{L}_{\text{hidden}}^{\text{eff}} &= \frac{v_h^2}{4}\text{Tr}[\partial_\mu \Sigma_h \partial^\mu \Sigma_h^\dagger] + \frac{v_h^2}{2}\text{Tr}[\lambda S \mu_h (\Sigma_h + \Sigma_h^\dagger)] \\
\mathcal{L}_{\text{SM}} &= -\frac{\lambda_1}{2}(H_1^\dagger H_1)^2 - \frac{\lambda_{1S}}{2}H_1^\dagger H_1 S^2 - \frac{\lambda_S}{8}S^4 \\
\mathcal{L}_{\text{mixing}} &= -v_h^2 \Lambda_h^2 \left[\kappa_H \frac{H_1^\dagger H_1}{\Lambda_h^2} + \kappa_S \frac{S^2}{\Lambda_h^2} + \kappa_S' \frac{S}{\Lambda_h} \right. \\
&\quad + \left. O(\frac{SH_1^\dagger H_1}{\Lambda_h^3}, \frac{S^3}{\Lambda_h^3}) \right] \\
&\approx -v_h^2 \left[\kappa_H H_1^\dagger H_1 + \kappa_S S^2 + \Lambda_h \kappa_S' S \right]
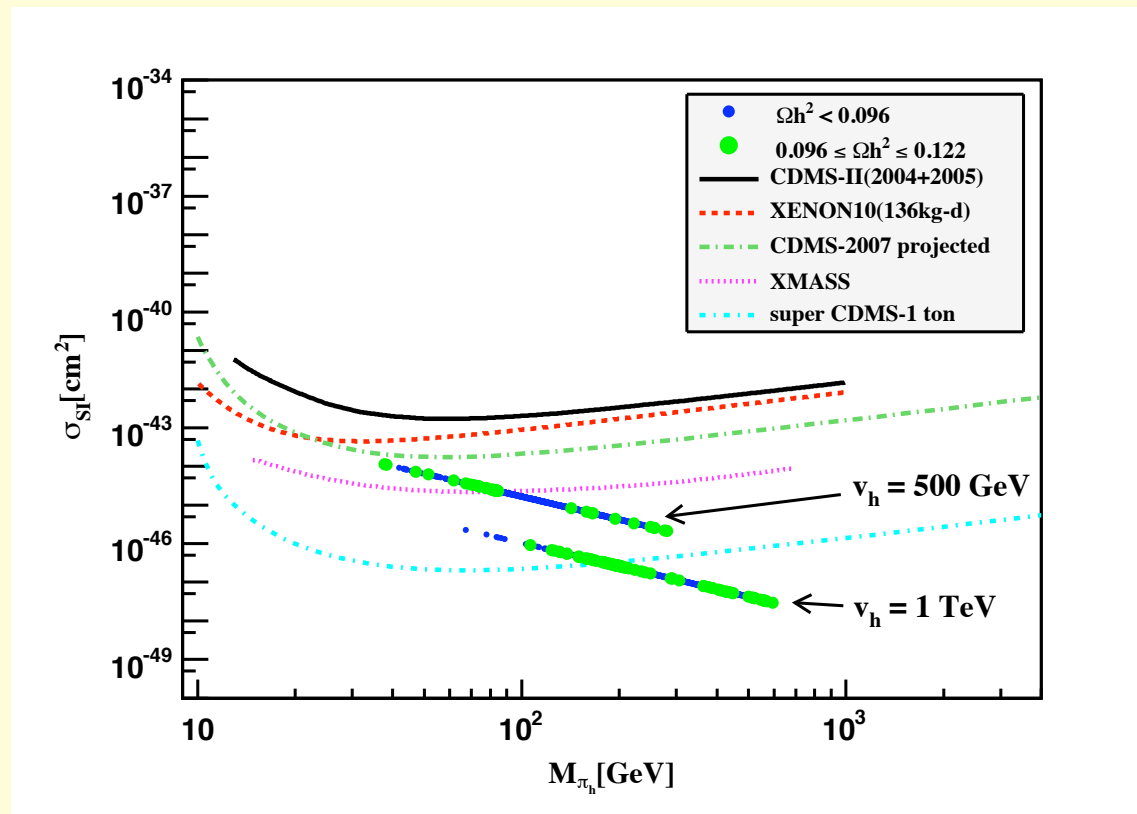\end{aligned}
$$

Relic density

$\Omega_{\pi_h} h^2$ in the (m_{h_1}, m_{π_h}) plane for
(a) $v_h = 500$ GeV and $\tan\beta = 1$,

(b) $v_h = 1$ TeV and $\tan\beta = 2$.

Direct Detection Rate

$\sigma_{SI}(\pi_h p \to \pi_h p)$ as functions of m_{π_h}.

the upper one: $v_h = 500$ GeV and $\tan\beta = 1$,

the lower one: $v_h = 1$ TeV and $\tan\beta = 2$.

Comparison with the previous models

- Dark gauge symmetry is unbroken (DM could be absolutely stable if they appeared in the asymptotic states), but confining like QCD (No long range dark force, DM becomes composite)

- DM : composite hidden hadrons (mesons and baryons)

- All masses including CDM masses from dynamical sym breaking in the hidden sector

- Singlet scalar is necessary to connect the hidden sector and the visible sector

- Higgs Signal strengths : universally reduced from one

- Additional singlet scalar improves the vacuum stability up to Planck scale

- Can modify Higgs inflation scenario (Higgs-portal assisted Higgs inflation [arXiv:1405.1635, JCAP (2017) with Jinsu Kim, WIPark]

- The 2nd scalar could be very very elusive

- Can we find the 2nd scalar at LHC ?

- We will see if this class of DM can survive the LHC Higgs data in the coming years

SIMP scenario + dark resonances

**Work in progress with
Soo-Min Choi, Hyunmin Lee (CAU)
and Alexander Natale (KIAS)**
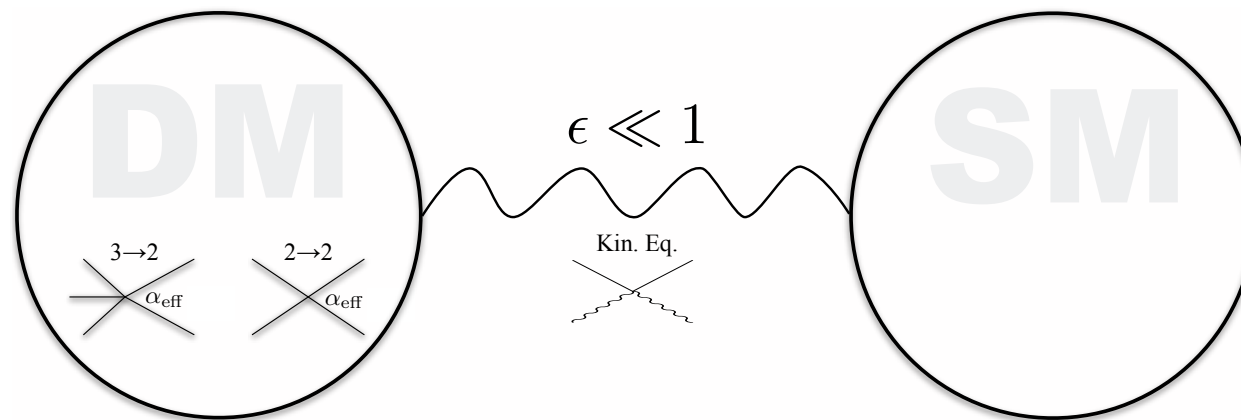
SIMP Scenario in Dark QCD

SIMP paradigm

FIG. 1: A schematic description of the SIMP paradigm. The dark sector consists of DM which annihilates via a $3 \to 2$ process. Small couplings to the visible sector allow for thermalization of the two sectors, thereby allowing heat to flow from the dark sector to the visible one. DM self interactions are naturally predicted to explain small scale structure anomalies while the couplings to the visible sector predict measurable consequences.

Hochberg, Kuflik, Tolansky, Wacker, arXiv:1402.5143
Phys. Rev. Lett. 113, 171301 (2014)

SIMP Conditions

Freeze-out :

$$\Gamma_{3\to 2} = n_{DM}^2 \langle \sigma v^2 \rangle_{3\to 2} \sim H(T_F)$$

$$\langle \sigma v^2 \rangle_{3\to 2} = \frac{\alpha_{\text{eff}}^3}{m_{\text{DM}}^5}$$

$$\alpha_{\text{eff}} = 1 - 30 \to m_{\text{DM}} \sim 10\text{MeV} - 1\text{GeV}$$

2->2 Self scattering :

$$\frac{\sigma_{\text{scatter}}}{m_{\text{DM}}} = \frac{a^2 \alpha_{\text{eff}}^2}{m_{\text{DM}}^3}$$

with a~O(1)

$$\frac{\sigma_{\text{scatter}}}{m_{\text{DM}}} \lesssim 1 \text{ cm}^2/\text{g}$$

Dark QCD + WZW

- Dark flavor symmetry G=SU(Nf)L x SU(Nf)R is SSB into diagonal H=SU(Nf)V by dark QCD condensation

- Effective Lagrangian for NG bosons (dark pions) contain 5-point self interaction : WZW term for Π_5 (G/H) = Z (Nf > 2)

$$\Gamma_{\mathrm{WZ}} = C \int_{M^5} d^5x \, \mathrm{Tr}(\alpha^5) \qquad \text{with} \quad \alpha = dUU^\dagger.$$
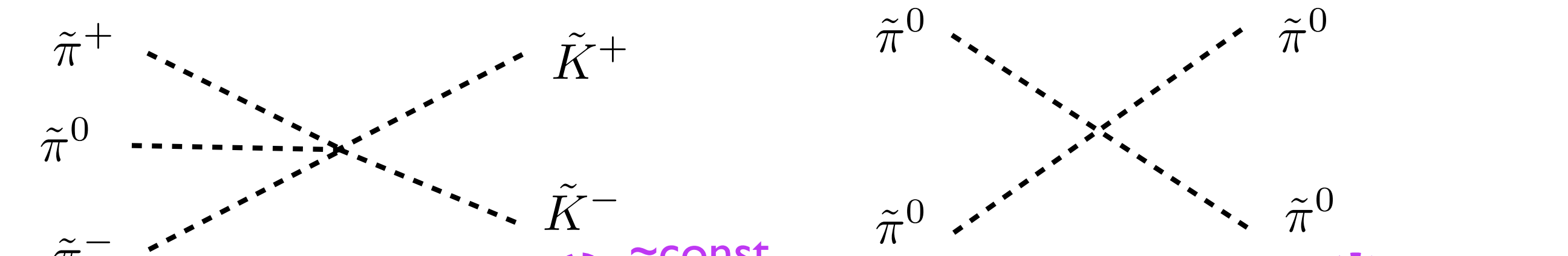
$$U = e^{2i\pi/F} \qquad\qquad C = -i\frac{N_c}{240\pi^2}$$

$$\mathcal{L}_{WZW} = \frac{2N_c}{15\pi^2} \epsilon^{\mu\nu\rho\sigma} \mathrm{Tr}[\partial_\mu\pi\partial_\nu\pi\partial_\rho\pi\partial_\sigma\pi]$$

in the absence of external gauge fields

SIMP Dark Mesons
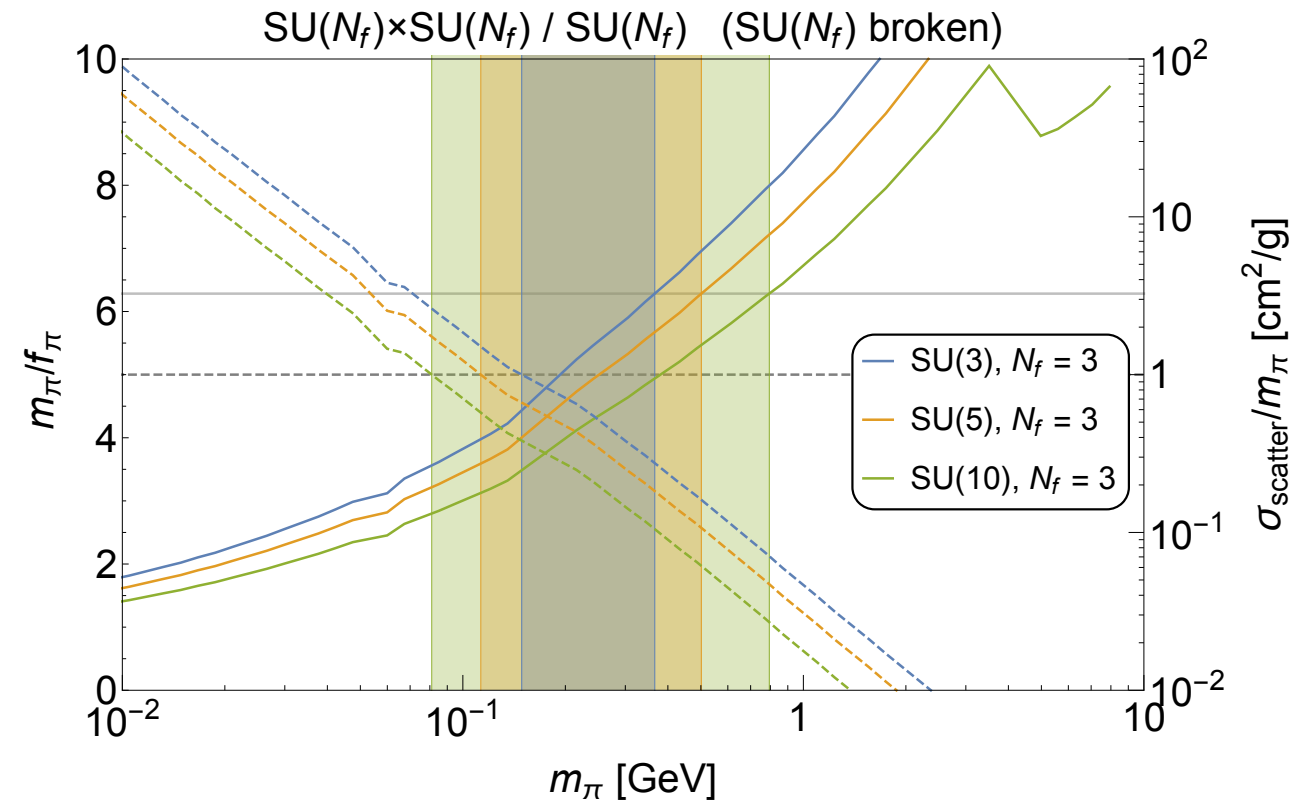

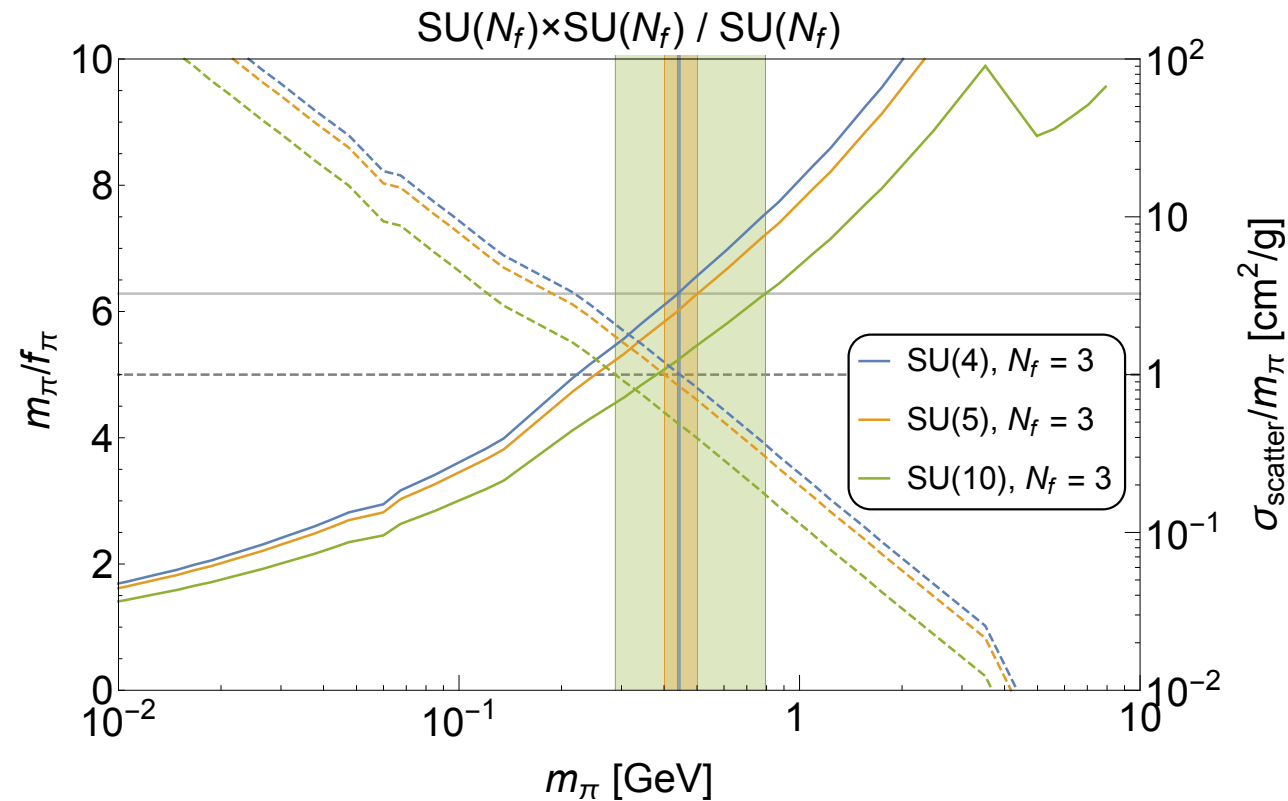
$$\langle \sigma v^2 \rangle_{3\to 2} = \frac{5\sqrt{5}N_c^2 m_\pi^5}{2\pi^5 F^{10}} \frac{t^2}{N_\pi^3} \left(\frac{T_F}{m_\pi}\right)^2,$$

~const

$$\sigma_{\text{self}} = \frac{m_\pi^2}{32\pi F^4} \frac{a^2}{N_\pi^2}$$

~const

G_c	G_f/H	N_π	t^2	$N_f^2 a^2$
SU(N_c)	$\frac{\text{SU}(N_f)\times\text{SU}(N_f)}{\text{SU}(N_f)}$ $(N_f \geq 3)$	$N_f^2 - 1$	$\frac{4}{3}N_f(N_f^2-1)(N_f^2-4)$	$8(N_f-1)(N_f+1)(3N_f^4-2N_f^2+6)$
SO(N_c)	SU(N_f)/SO(N_f) $(N_f \geq 3)$	$\frac{1}{2}(N_f+2)(N_f-1)$	$\frac{1}{12}N_f(N_f^2-1)(N_f^2-4)$	$(N_f-1)(N_f+2)(3N_f^4+7N_f^3-2N_f^2-12N_f+24)$
Sp(N_c)	SU($2N_f$)/Sp($2N_f$) $(N_f \geq 2)$	$(2N_f+1)(N_f-1)$	$\frac{2}{3}N_f(N_f^2-1)(4N_f^2-1)$	$4(N_f-1)(2N_f+1)(6N_f^4-7N_f^3-N_f^2+3N_f+3)$

[Hochberg, Kuflik, Murayama, Volansky, Wacker, 1411.3727, PRL (2015)]

Hochberg, Kuflik, Murayama, Volansky, Wacker, 1411.3727, PRL

- DM self scattering : $\sigma_{\text{self}}/m_{\text{DM}} < 1\,\text{cm}^2/\text{g}$ **Large Nc > 3**

- Validity of ChPT : $m_\pi/f_\pi < 2\pi$ **More serious in NNLO ChPT**
Sannino et al, 1507.01590

Issues in the SIMP w/ hQCD

- Dark flavor sym is not good enough to stabilize dark pion (We have to assume dim-5 operator is highly suppressed)

- Dark baryons can make additional contribution to DM of the universe (It could produce additional diagrams for SIMP)

- Validity region of ChPT : need to include resonances (dark rho meson, dark sigma meson, etc. ➡️ this talk)

- How to achieve Kinetic equilibrium with the SM ? (Dark sigma meson or adding singlet scalar S may help. Or lifting the mass degeneracy of dark pionscan help. Work in progress.)

Digression on ChPT + VM

- We consider G$_{global}$ SSB into H$_{global}$: non Linear sigma model on G$_{global}$/H$_{global}$ is equivalent to linear sigma model on G$_{global}$ X H$_{local}$

- Vector meson ~ gauge field for H$_{local}$

  - **CCWZ (1969)**
  - **Bando, Kugo, Yamawaki, Phys. Rept. 164, 217 (1988)**

The Lagrangian $\mathcal{L}_A$ can be cast into the following form in terms of a new exponential field $U(x)$ defined as $\Sigma(x) \equiv \xi_L^\dagger(x)\xi_R(x) = \exp[2i\pi(x)/f_\pi]$ with $\xi_L^\dagger(x) = \xi_R(x) = \exp[i\pi(x)/f_\pi]$:

$$\Sigma(x) \to L\Sigma(x)R^\dagger$$

Note that the π field is normalzied in such a way that

$$\pi(x) = \frac{1}{\sqrt{2}} \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta_8 + \frac{1}{\sqrt{3}}\eta_0 & \pi^+ K^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta_8 + \frac{1}{\sqrt{3}}\eta_0 & K^0 \\ K^- & \overline{K^0} & -\frac{2}{\sqrt{6}}\eta_8 + \frac{1}{\sqrt{3}}\eta_0 \end{pmatrix} \tag{6}$$

Vector meson as hidden local gauge boson

$$
\begin{aligned}
\xi_L(x) &\rightarrow U(x)\xi_L(x)L^\dagger \\
\xi_R(x) &\rightarrow U(x)\xi_R(x)R^\dagger \\
gV_\mu(x) &\rightarrow U(x)\left[\partial_\mu - igV_\mu(x)\right]U^\dagger(x) \\
D_\mu\xi_L &= (\partial_\mu - igV_\mu)\xi_L(x) + i\xi_L(x)l_\mu \\
D_\mu\xi_R &= (\partial_\mu - igV_\mu)\xi_R(x) + i\xi_R(x)l_\mu
\end{aligned}
$$

$$
V_\mu = \frac{1}{\sqrt{2}}
\begin{pmatrix}
\frac{1}{\sqrt{2}}\rho^0_\mu + \frac{1}{\sqrt{6}}\omega_{8\mu} + \frac{1}{\sqrt{3}}\omega_{0\mu} & \rho^+_\mu K^{*+}_\mu & \\
\rho^-_\mu & -\frac{1}{\sqrt{2}}\rho^0_\mu + \frac{1}{\sqrt{6}}\omega_{8\mu} + \frac{1}{\sqrt{3}}\omega_{0\mu} & K^{*0}_\mu \\
K^{*-}_\mu & \overline{K^{*0}_\mu} & -\frac{2}{\sqrt{6}}\omega_{8\mu} + \frac{1}{\sqrt{3}}\omega_{0\mu}
\end{pmatrix}
\tag{7}
$$

Ch Lagrangian (pi,V)

The chiral Lagrangian for pions and vector mesons is given by

$$
\begin{aligned}
\mathcal{L} &= \mathcal{L}_A + \mathcal{L}_m + \mathcal{L}_B + \mathcal{L}_{\mathrm{kin}}(V) + \Gamma^{\mathrm{anom}}(\xi_L, \xi_R, V, l, r) \\
\mathcal{L}_A &= -\frac{f_\pi^2}{4} \mathrm{Tr} \left[(D_\mu \xi_L)\xi_L^\dagger - (D_\mu \xi_R)\xi_R^\dagger \right]^2 \\
\mathcal{L}_m &= -\frac{f_\pi^2}{2} \mathrm{Tr} \left[\mu(\Sigma + \Sigma^\dagger) \right] \\
\mathcal{L}_B &= -a\frac{f_\pi^2}{4} \mathrm{Tr} \left[(D_\mu \xi_L)\xi_L^\dagger +_\mu \xi_R)\xi_R^\dagger \right]^2 \\
\mathcal{L}_{\mathrm{kin}} &= -\frac{1}{2} \mathrm{Tr} \left[F_{\mu\nu} F^{\mu\nu} \right] \\
F_{\mu\nu} &= \partial_\mu V_\nu - \partial_\nu V_\mu - ig[V_\mu, V_\nu]
\end{aligned}
$$

$$
\begin{aligned}
\mathcal{L}_B &= m_V^2 \mathrm{Tr} V_\mu V^\mu - 2ig_{V\pi\pi} \mathrm{Tr}\left(V_\mu [\partial^\mu \pi, \pi]\right) + ... \\
m_V^2 &= ag^2 f_\pi^2 \\
g_{V\pi\pi} &= \frac{1}{2}ag
\end{aligned}
$$

a~2 and g~6 in real QCD. In Dark QCD, we consider they are free

Another useful quantities

$$\xi(x) \rightarrow L\xi(x)U^\dagger(x) = U(x)\xi(x)R^\dagger$$

$$\mathcal{A}_\mu(x) \equiv \frac{i}{2}\left[\xi^\dagger\partial_\mu\xi - \xi\partial_\mu\xi^\dagger\right]$$

$$\rightarrow U(x)\mathcal{A}_\mu(x)U^\dagger(x)$$

$$\mathcal{V}_\mu(x) \equiv \frac{i}{2}\left[\xi^\dagger\partial_\mu\xi + \xi\partial_\mu\xi^\dagger\right]$$

$$\rightarrow U(x)\mathcal{V}_\mu(x)U^\dagger(x) + U(x)\partial U^\dagger(x)$$

$$V_\mu(x) \rightarrow U(x)V_\mu(x)U^\dagger(x) + U(x)\partial_\mu U^\dagger(x)$$

**Here `V' is the vector meson associated with
hidden local gauge symmetry**

WZW (gauged)

$$\Gamma_{LR} = C \int_{M^5} d^5x \, \mathrm{Tr}\,\alpha^5 + (\text{covariantization}) \,,$$

where we define

$$\alpha = dU\,U^{-1}, \quad \beta = U^{-1}\,dU, \quad C = -i\frac{N_c}{240\pi^2} \,.$$

Anomaly Conditions

$$\delta\Gamma_{LR}(U,l,r)$$
$$= -\frac{N_c}{24\pi^2}\int_{M^4} d^4x \left[\epsilon_L \left[(dl)^2 - \frac{i}{2}dl^3 \right] - (L\rightarrow R) \right]$$

$$\Gamma_{LR}(U,l_\mu,r_\mu) = C\int_{M^5} d^5x \, \mathrm{Tr}(\alpha^5)$$
$$+ 5C\int_{M^4} d^4x \, \mathrm{Tr}\{i(l\alpha^3 + r\beta^3) - [(dl\,l + l\,dl)\alpha + (dr\,r + r\,dr)\beta] + (dl\,dU\,rU^{-1} - dr\,dU^{-1}\,lU)$$
$$+ (rU^{-1}lU\beta^2 - lUrU^{-1}\alpha^2) + \tfrac{1}{2}[(l\alpha)^2 - (r\beta)^2] + i[l^3\alpha + r^3\beta]$$
$$+ i[(dr\,r + r\,dr)U^{-1}lU - (dl\,l + l\,dl)UrU^{-1}] + i[lUrU^{-1}l\alpha + rU^{-1}lUr\beta] \,.$$
$$+ [r^3U^{-1}lU - l^3UrU^{-1} + \tfrac{1}{2}(UrU^{-1}l)^2]\} \,,$$

$$\Gamma_{WZ}(U,l,r) = \Gamma_{LR}(U,l,r) - \Gamma_{LR}(U=1,l,r)$$

WZW with vector mesons

$$\hat{\alpha}_L = D\xi_L \cdot \xi_L^\dagger = \alpha_L - igV + i\hat{l}$$

$$\hat{\alpha}_R = D\xi_R \cdot \xi_R^\dagger = \alpha_L - igV + i\hat{r}$$

$$\alpha_L = d\xi_L \cdot \xi_L^\dagger,$$

$$\alpha_R = d\xi_R \cdot \xi_R^\dagger$$

$$\hat{l} = \xi_L \cdot \xi_L^\dagger,$$

$$\hat{r} = \xi_R \cdot \xi_R^\dagger$$

$$F_V = dV - igV^2$$

$$\hat{F}_L = \xi_L \cdot F_L \cdot \xi_L^\dagger = \xi_L(dl - il^2)\xi_L^\dagger$$

$$\hat{F}_L = \xi_R \cdot F_R \cdot \xi_R^\dagger = \xi_R(dr - ir^2)\xi_R^\dagger$$

$$\Gamma^{\mathrm{anom}} = \Gamma_{\mathrm{WZW}} + \sum_{i=1}^{4} c_i \mathcal{L}_i$$

$$\mathcal{L}_1 = \mathrm{TR}\left[\hat{\alpha}_L^3 \hat{\alpha}_R - \hat{\alpha}_R^3 \hat{\alpha}_L\right] - (\xi_L = \xi_R = 1, V = 0, l, r)$$

$$\mathcal{L}_2 = \mathrm{TR}\left[\hat{\alpha}_L \hat{\alpha}_R \hat{\alpha}_L \hat{\alpha}_R\right] - (\xi_L = \xi_R = 1, V = 0, l, r)$$

$$\mathcal{L}_3 = i\mathrm{Tr}\left[F_V(\hat{\alpha}_L \hat{\alpha}_R - \hat{\alpha}_R \hat{\alpha}_L\right] - (\xi_L = \xi_R = 1, V = 0, l, r)$$

$$\mathcal{L}_4 = i\mathrm{Tr}\left[\hat{F}_L \hat{\alpha}_L \hat{\alpha}_R - \hat{F}_R \hat{\alpha}_R \hat{\alpha}_L\right] - (\xi_L = \xi_R = 1, V = 0, l, r)$$

- **Fujiwara, Kugo, Yamawaki et al., Prog. Theo. Phys. 73, 926 (1985)**
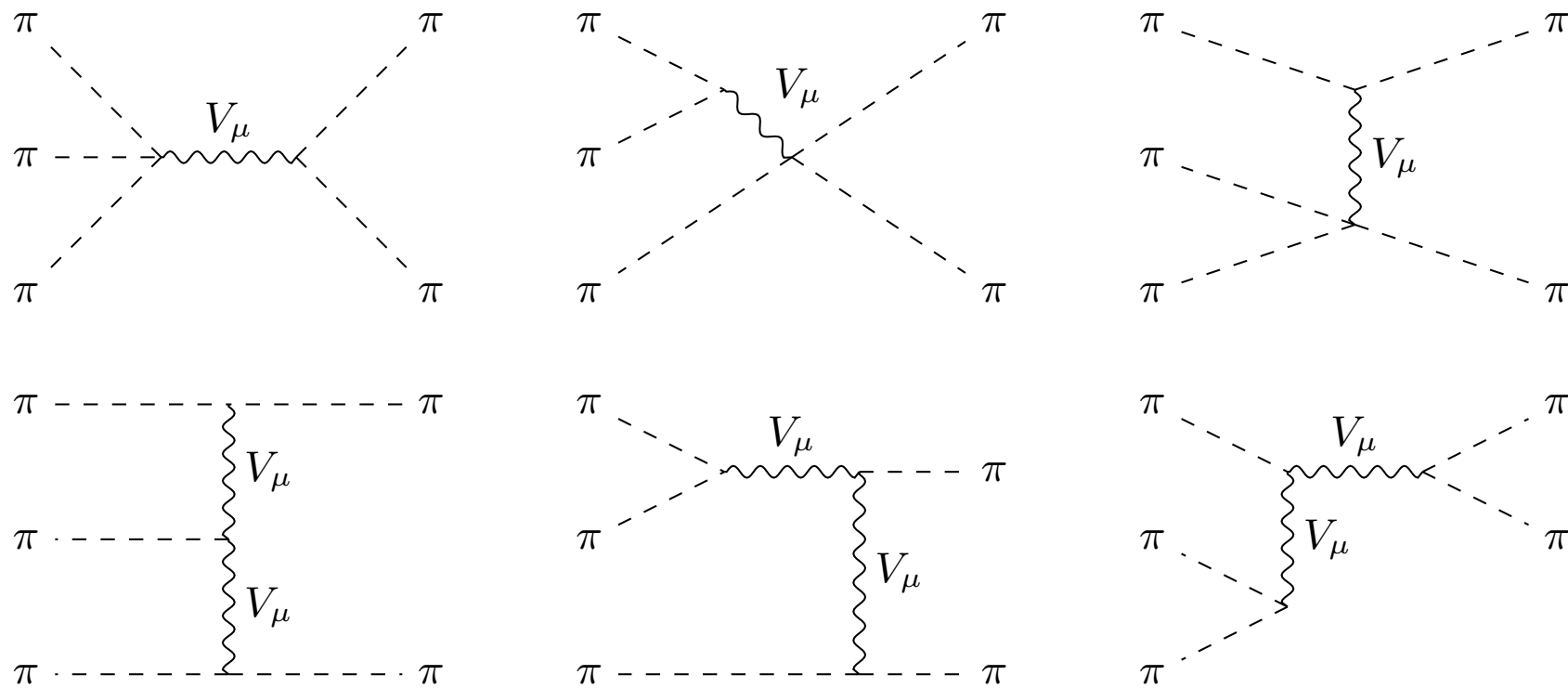- **P.Ko, PRD44, 139 (1991) 139 for a useful compact summary**

SIMP + VDM

FIG. 1: Feynman diagrams contributing to $3 \to 2$ processes for the dark pions with the vector meson interactions.

SIMP + VM

New diagrams involveng dark vector mesons

$$\pi^+ \pi^- \pi^0 \to \omega \to K^+ K^- (K^0 \overline{K^0})$$

$$\gamma = \frac{m_V \Gamma}{9 m_\pi^2}, \text{ and } \epsilon = \frac{m_V^2 - 9 m_\pi^2}{9 m_\pi^2}$$ **(for 3 pi resonance case)**

We choose a small epsilon [say, 0.1 (near resonance)]
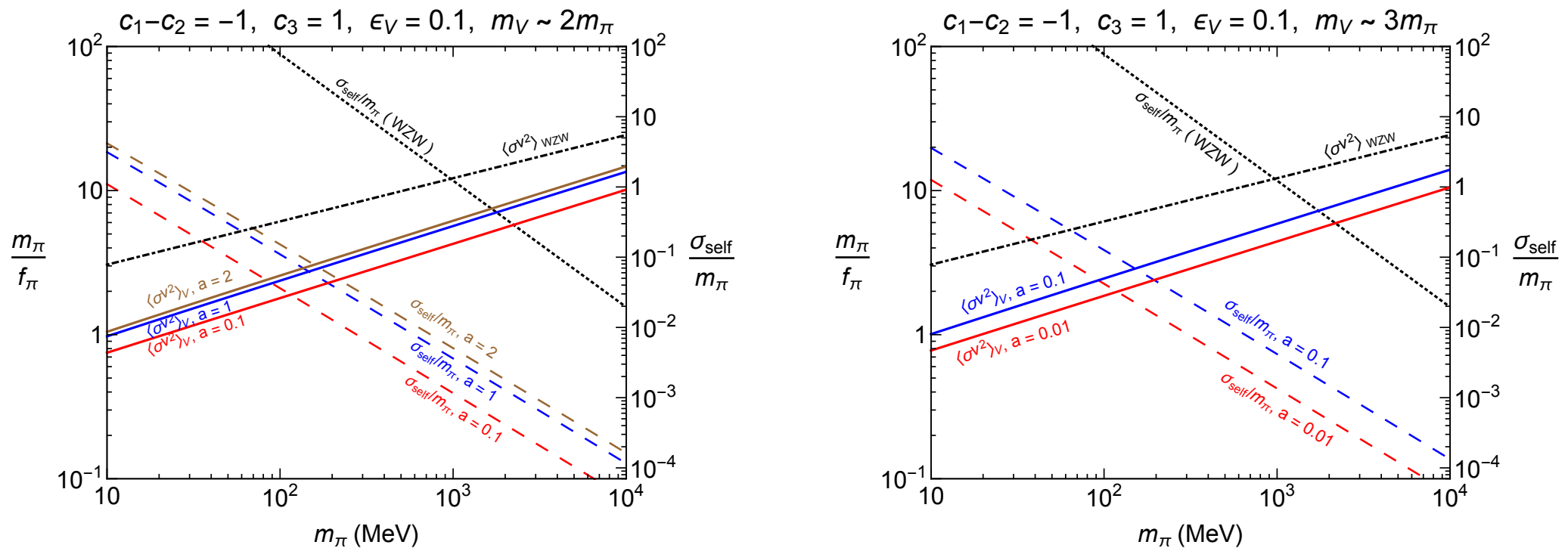**and a small gamma (NWA)**

Results

FIG. 2: Contours of relic density ($\Omega h^2 \approx 0.119$) for m_π and m_π/f_π and self-scattering cross section per DM mass in cm^2/g as a function of m_π. The case without and with vector mesons are shown in black lines and colored lines respectively. We have imposed the relic density condition for obtaining the contours of self-scattering cross section. Vector meson masses are taken near the resonances with $m_V = 2(3)m_\pi\sqrt{1+\epsilon_V}$ on left(right) plots. In both plots, $c_1 - c_2 = -1$ and $\epsilon_V = 0.1$ are taken.

- The allowed parameter space is in a better shape now, especially for 2 pi resonance case
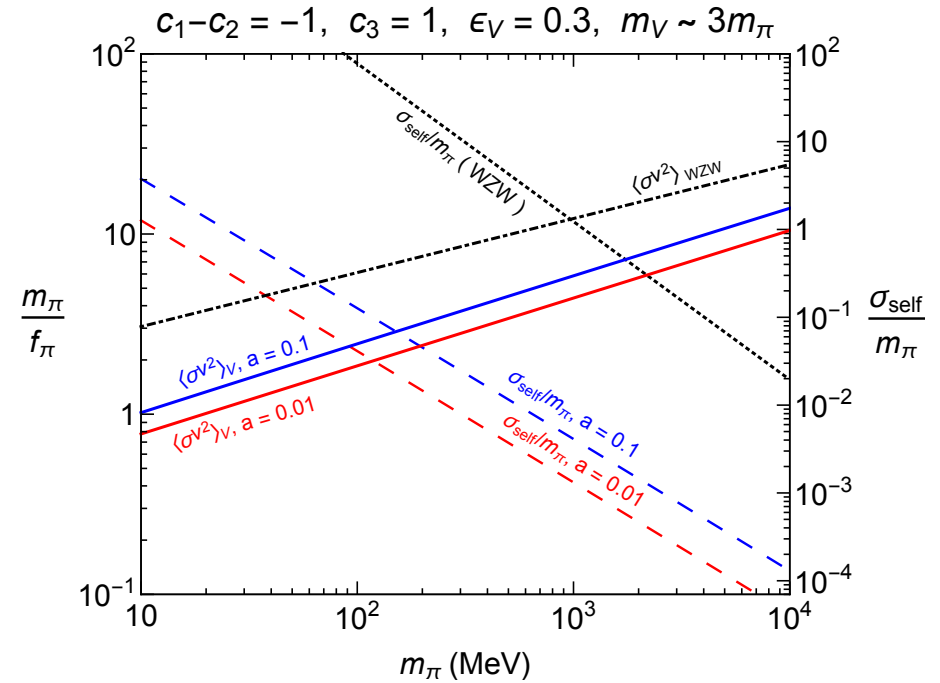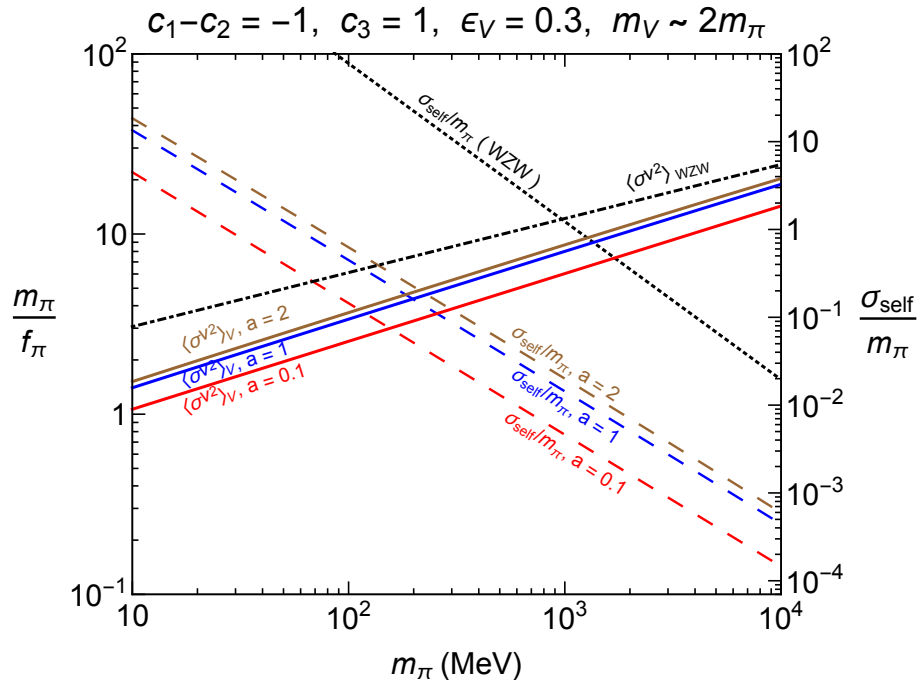
FIG. 3: Similar contours of relic density for m_π and m_π/f_π and self-scattering cross section per DM mass as in Fig. 2. Vector meson masses are taken off the resonance with $\epsilon_V = 0.3$, and $c_1 - c_2 = -1$ and $c_3 = 1$ are chosen.
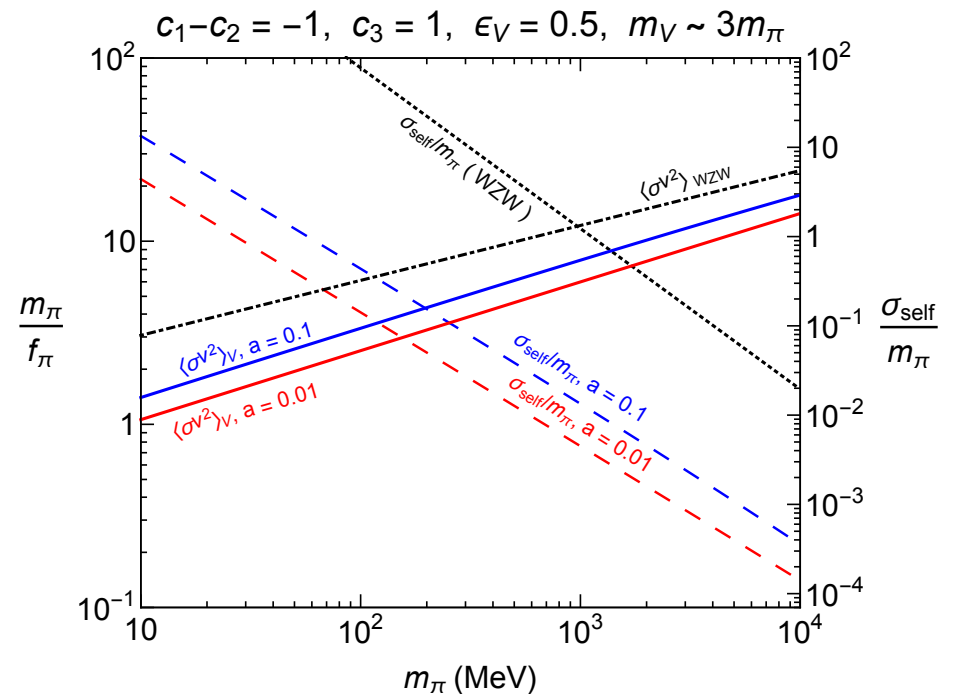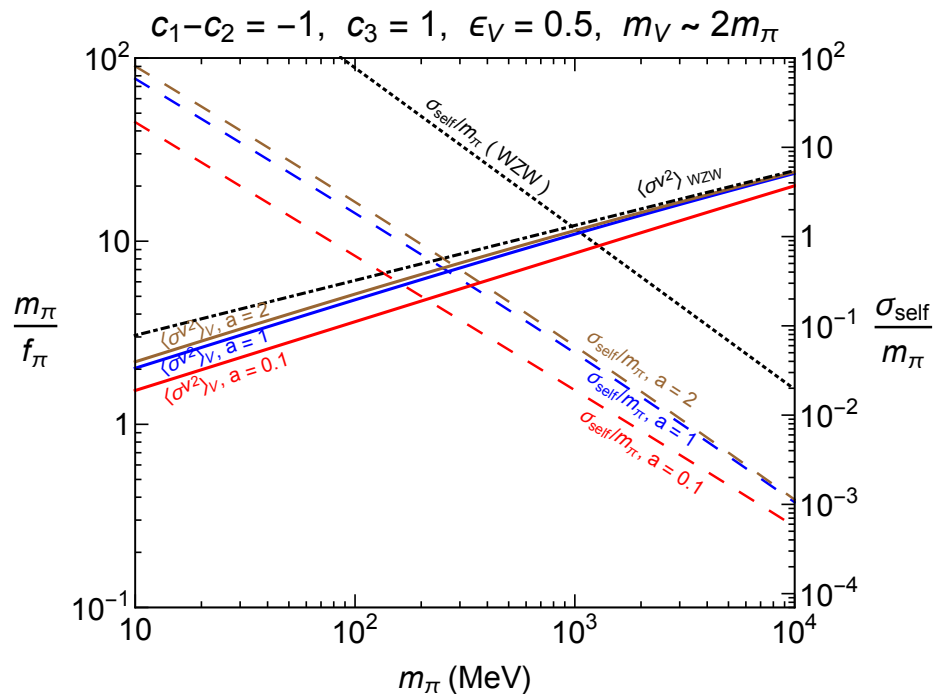

FIG. 4: Similar contours of relic density for m_π and m_π/f_π and self-scattering cross section per DM mass as in Fig. 2. Vector meson masses are taken off the resonance with $\epsilon_V = 0.5$, and $c_1 - c_2 = -1$ and $c_3 = 1$ are chosen.

Conclusion

- Hidden (dark) QCD models make an interesting possibility to study the origin of EWSB, (C)DM

- WIMP scenario is still viable, and will be tested to some extent by precise measurements of the Higgs signal strength and by discovery of the singlet scalar, which is however a formidable task unless we are very lucky

- SIMP scenario using 3->2 scattering via WZW term is interesting, but there are a few issues which ask for further study (dark resonance could play an important role for thermal relic and kinetic contact with the SM sector)