

Self-interacting dark matter, muon $g-2$, and neutrino physics in a gauged Lmu-Ltau model

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Based on

AK, Kunio Kaneta, Keisuke Yanagi, and Hai-bo Yu, JHEP, 2018

June 29, 2018 @ NDM 2018

Talk Plan

Part 1: Gauged $U(1)_{L_\mu-L_\tau}$ extension of the standard model

- new gauge boson Z' and Higgs boson $\Phi \simeq (v_\Phi + \varphi)$
- muon anomalous magnetic moment $(g - 2)_\mu$ and other constraints

Part 2: $U(1)_{L_\mu-L_\tau}$ charged fermions N and $\bar{N}$ as dark matter

- φ mediates strong self-interaction in (dwarf) galaxies, while it diminishes toward galaxy clusters
- solving small-scale issues that are hard to explain in the conventional cold dark matter model

Part 3: Summary and implications for neutrino astrophysics

- IceCube dip
- supernova cooling

Part 1

Gauged $U(1)_{L_\mu - L_\tau}$ extension of the standard model

- new gauge boson Z' and Higgs boson $\Phi \simeq (v_\Phi + \varphi)$
- muon anomalous magnetic moment $(g - 2)_\mu$ and other constraints

Minimal $U(1)_{L_\mu-L_\tau}$ extension

Gauge anomaly free $U(1)_{L_\mu-L_\tau}$

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + g' Z'_\mu \left(L_2^\dagger \bar{\sigma}^\mu L_2 - L_3^\dagger \bar{\sigma}^\mu L_3 - \bar{\mu}^\dagger \bar{\sigma}^\mu \bar{\mu} + \bar{\tau}^\dagger \bar{\sigma}^\mu \bar{\tau} \right) - \frac{1}{4} Z'_{\mu\nu} Z'^{\mu\nu} - \frac{1}{2} \epsilon Z'_{\mu\nu} B^{\mu\nu} + (D_\mu \Phi)^\dagger D^\mu \Phi - V(\Phi, H)$$

only the second (+1) and third (-1) generation leptons
couple to a new gauge boson Z' ($U(1)_{L_\mu-L_\tau}$ charge)

New Higgs boson Φ (-1)

$$V(\Phi, H) = -m_\Phi^2 |\Phi|^2 + \frac{1}{4} \lambda_\Phi |\Phi|^4 + \lambda_{\Phi H} |\Phi|^2 |H|^2$$

develops vacuum expectation value (VEV) $\Phi \simeq (v_\Phi + \varphi)$

$$\rightarrow m_\varphi = \sqrt{\lambda_\Phi/2} v_\Phi, \quad m_{Z'} = g' v_\Phi$$

Turn off **kinetic mixing** $\epsilon = 0$ and **Higgs portal** $\lambda_{\Phi H} = 0$ for simplicity
 Z' - A mixing at the 1-loop level:

$$\epsilon_{AZ'} = -\frac{eg'}{12\pi^2} \ln \left(\frac{m_\tau^2}{m_\mu^2} \right)$$

Muon $g-2$ and other tests

3σ discrepancy between the SM prediction and measurement

$$a_{\mu}^{\text{exp}} - a_{\mu}^{\text{SM}} = (26.1 \pm 8.0) \times 10^{-10} \quad a_{\mu} = (g-2)_{\mu}/2$$

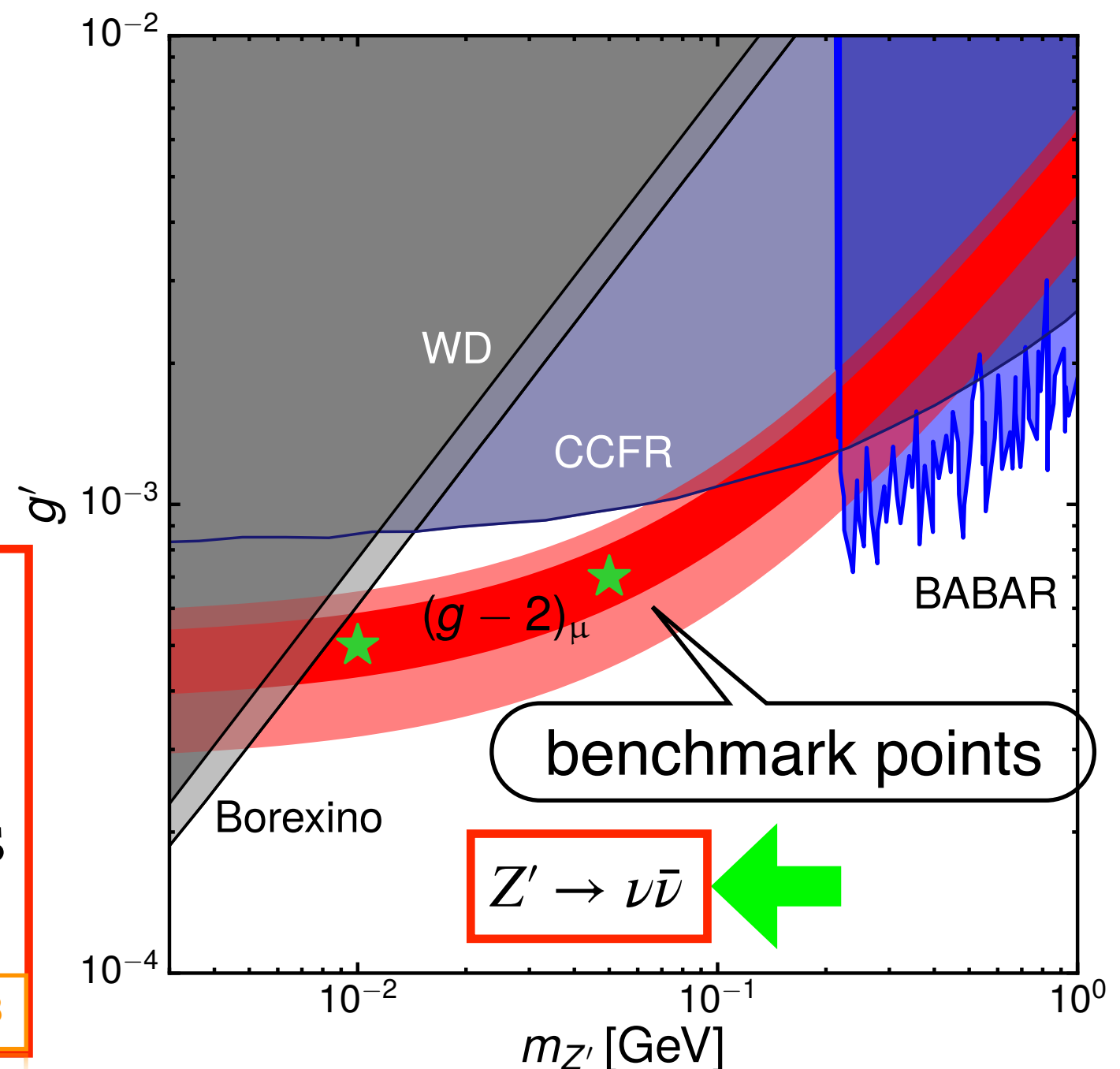
Hagiwara *et al.*, J. Phys. G, 2011

explained by Z' contribution

Baek *et al.*, PRD, 2001

muon beam dump experiment
(NA64 μ) will cover
the whole plane!
 $\mu Z \rightarrow \mu ZZ' \rightarrow \mu Z + \text{invisibles}$
(Z : target nuclei)

Gninenko *et al.*, arXiv:1801.10448



Part 2

$U(1)_{L_\mu - L_\tau}$ charged fermions N and $\bar{N}$ as dark matter

- φ mediates strong self-interaction in (dwarf) galaxies, while it diminishes toward galaxy clusters
- solving small-scale issues that are hard to explain in the conventional cold dark matter model

$U(1)_{L_\mu-L_\tau}$ model with dark matter

Add a vector-like pair of SM singlet fermions $N(+1/2)$ and $\bar{N}(-1/2)$ ($U(1)_{L_\mu-L_\tau}$ charge)

$$\mathcal{L} = \mathcal{L}_{\text{minimal } U(1)_{L_\mu-L_\tau}} + iN^\dagger \bar{\sigma}^\mu D_\mu N + i\bar{N}^\dagger \bar{\sigma}^\mu D_\mu \bar{N} \\ - m_N N \bar{N} - \frac{1}{2} y_N \Phi N N - \frac{1}{2} y_{\bar{N}} \Phi^* \bar{N} \bar{N} + \text{h.c.}$$

VEV of $\Phi(-1): U(1)_{L_\mu-L_\tau} \rightarrow Z_2$

($v_\Phi = 20$ and 70 GeV for benchmark points)

stabilize the lightest mass eigenstate N_1 as dark matter

$$-\mathcal{L}_{\text{mass}} = \frac{1}{2} \begin{pmatrix} N & \bar{N} \end{pmatrix} \begin{pmatrix} y_N \frac{v_\Phi}{\sqrt{2}} & m_N \\ m_N & y_{\bar{N}} \frac{v_\Phi}{\sqrt{2}} \end{pmatrix} \begin{pmatrix} N \\ \bar{N} \end{pmatrix} = \frac{1}{2} \begin{pmatrix} N_1 & N_2 \end{pmatrix} \begin{pmatrix} M_1 & 0 \\ 0 & M_2 \end{pmatrix} \begin{pmatrix} N_1 \\ N_2 \end{pmatrix}$$

$$\text{where } \begin{pmatrix} N_1 \\ N_2 \end{pmatrix} = U \begin{pmatrix} N \\ \bar{N} \end{pmatrix} \text{ and } 0 \leq M_1 \leq M_2$$

Pseudo-Dirac case

Consider a C- and P-conserving pseudo-Dirac case:

$$m_N/v_\Phi \gg y_N = y_{\bar{N}} \equiv y > 0$$

$$N_1 = (N - \bar{N})/(\sqrt{2}i) \quad \text{and} \quad N_2 = (N + \bar{N})/\sqrt{2}$$

$$M_1 \approx m_N - yv_\Phi/\sqrt{2} \quad \text{and} \quad M_2 \approx m_N + yv_\Phi/\sqrt{2}$$

$$\mathcal{L} \supset -\frac{y}{2\sqrt{2}}\varphi (-\bar{N}_1 N_1 + \bar{N}_2 N_2) + ig' Q_N Z'_\mu \bar{N}_2 \gamma^\mu N_1$$

Yukawa interaction

- determine y by the relic abundance
- p-wave self-annihilation and s-wave co-annihilation
(+ $\varphi \rightarrow Z'\nu\bar{\nu}$ and $Z' \rightarrow \nu\bar{\nu}$) $\rightarrow$ indirect detection is not constraining
- **self-interaction!**

Z' coupling (+ Z' - A mixing)

- inelastic scattering $\rightarrow$ direct detection is not constraining!

Self-scattering cross section

Transfer cross section in the partial wave expansion

$$\sigma_T = 4\pi \int_0^1 d\cos\theta (1 - \cos\theta) \frac{d\sigma}{d\Omega}$$

Tulin *et al.*, PRD, 2013

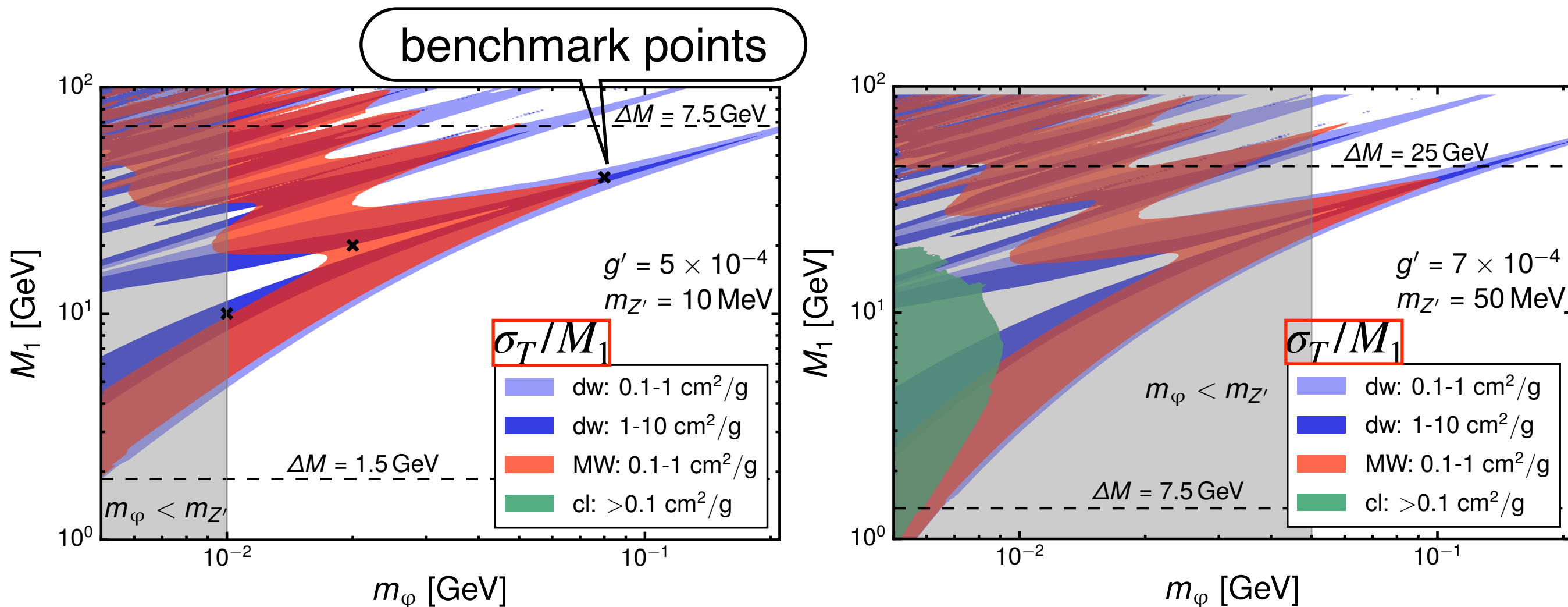
Kahlhoefer *et al.*, MNRAS, 2014

Kahlhoefer *et al.*, JCAP, 2017

as a function of the relative velocity $v_{\text{rel}} = 30 \text{ km/s}$ - dwarf galaxies

$v_{\text{rel}} = 200 \text{ km/s}$ - Milky-Way-size galaxies

$v_{\text{rel}} = 1000 \text{ km/s}$ - galaxy clusters



Solving small-scale issues

$\sigma_T/M_1 \sim 1 \text{ cm}^2/\text{g}$ changes the dark matter density profile in inner halos
 $\rightarrow$ explains a diversity of galactic rotation curves in inner shape
 that is hard to understand in the collisionless cold dark matter model

Tulin *et al.*, Phys. Rept., 2018

AK, Kaplinghat, Pace, Yu, PRL, 2017

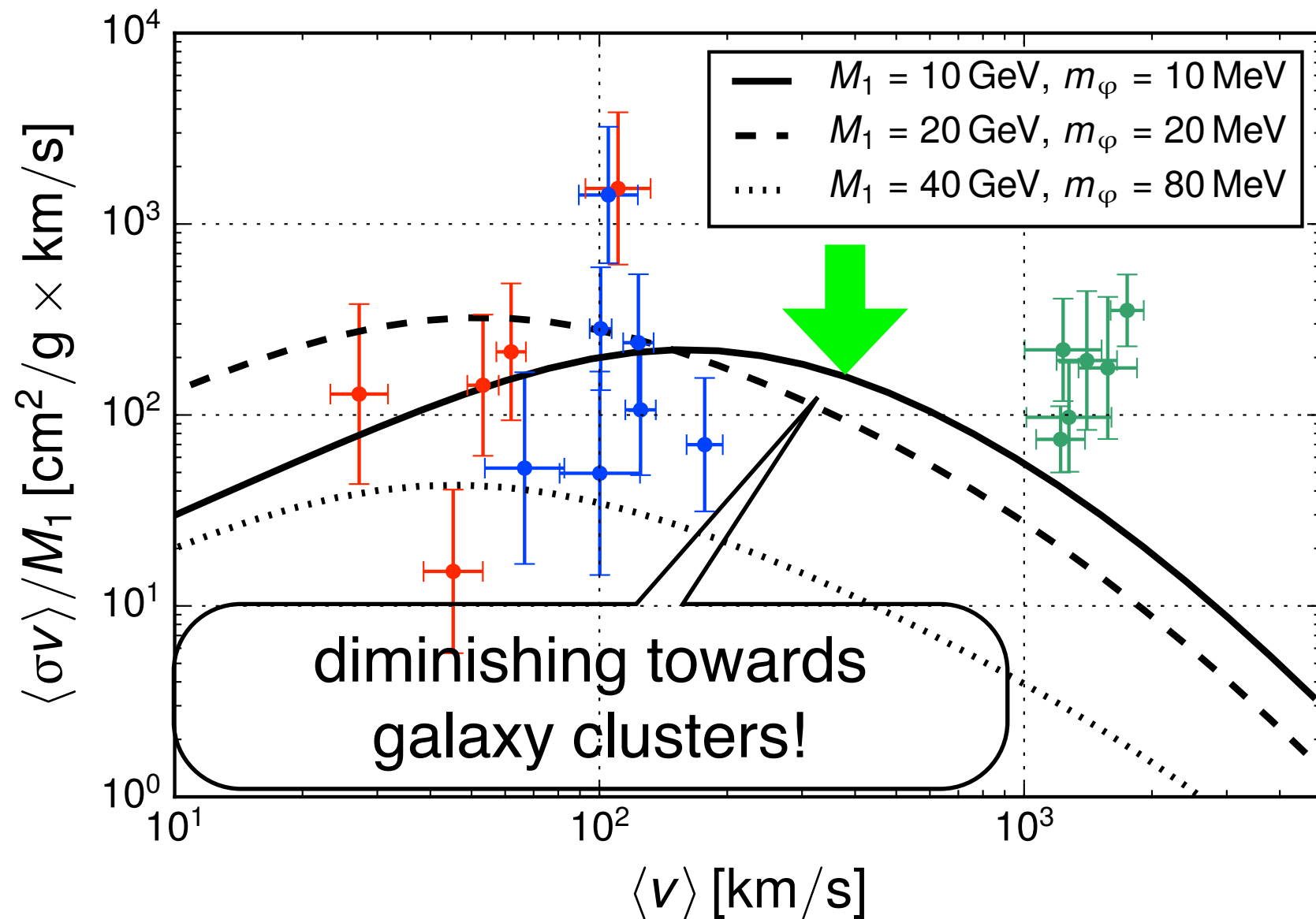
Inferred distribution-
 averaged cross section
 from

dwarf galaxies

low surface brightness
 galaxies

galaxy clusters

Kaplinghat *et al.*, PRL, 2016



Meanwhile it does not spoil the cold dark matter success
 in galaxy clusters

Part 3

Summary and implications for neutrino astrophysics

- IceCube dip
- supernova cooling

Summary

Simple $U(1)_{L_\mu-L_\tau}$ extension of the standard model

- explain the discrepancy in $(g-2)_\mu$ by the Z' contribution
- parameter space will be tested in future facilities
- offer a dark matter candidate N_1 and force mediator φ
- strong self-interaction reconciles the small-scale issues of the cold dark matter model
- self-interaction diminishes towards galaxy clusters
- evade both direct and indirect detection constraints

Resonant self-scattering and IceCube dip

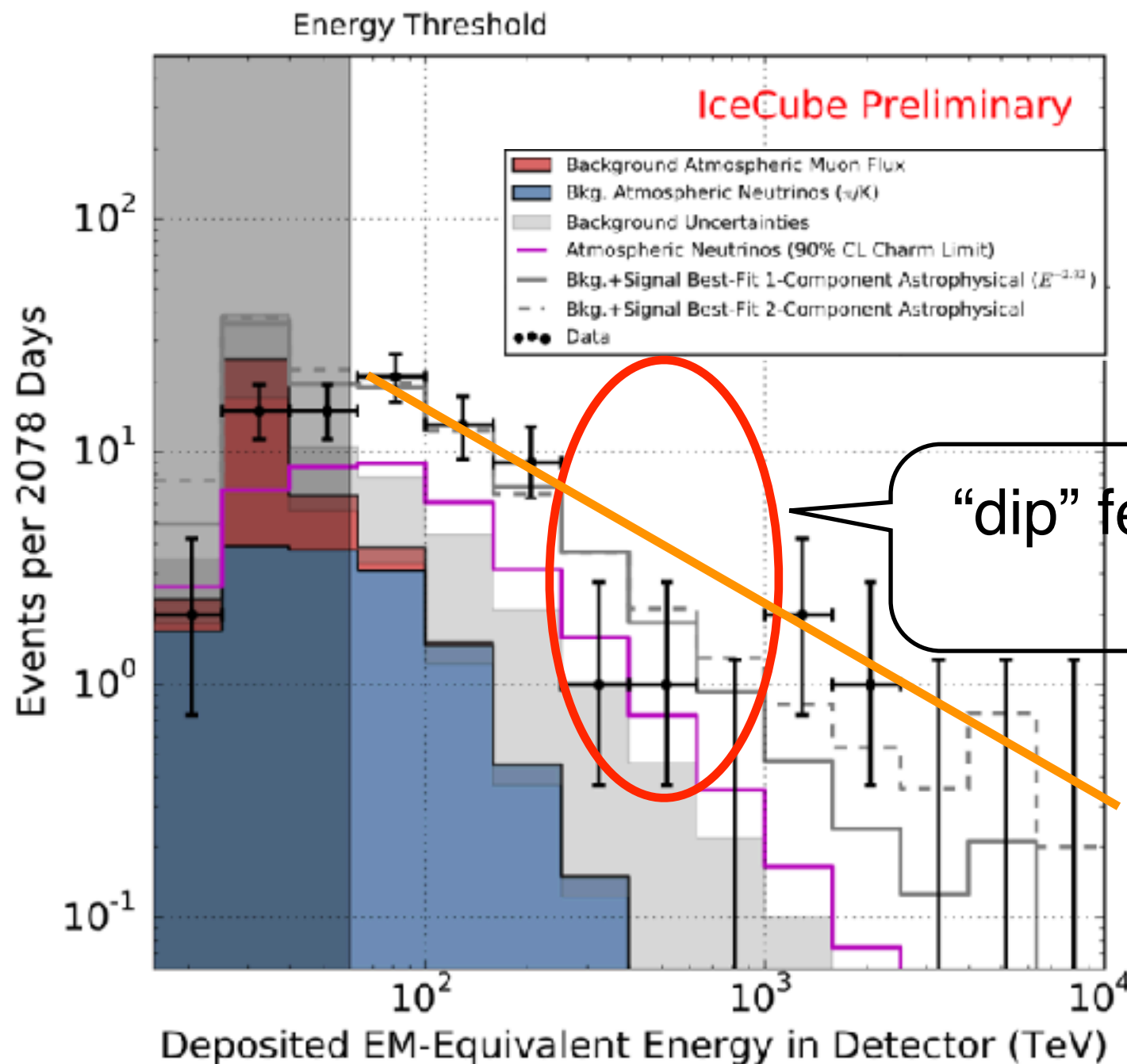
High-energy neutrino scattering with cosmic neutrino background is resonantly enhanced when $E_{\text{cm}} \simeq m_{Z'}$: $\nu\bar{\nu} \rightarrow Z' \rightarrow \nu\bar{\nu}$

$$E_{\text{res}} = 500 \text{ TeV} \left(\frac{m_{Z'}}{10 \text{ MeV}} \right)^2 \left(\frac{0.1 \text{ eV}}{m_{\nu}} \right)$$

[Araki et al., PRD, 2015](#)

[Araki et al., PRD, 2016](#)

[AK and Yu, PRD, 2015](#)



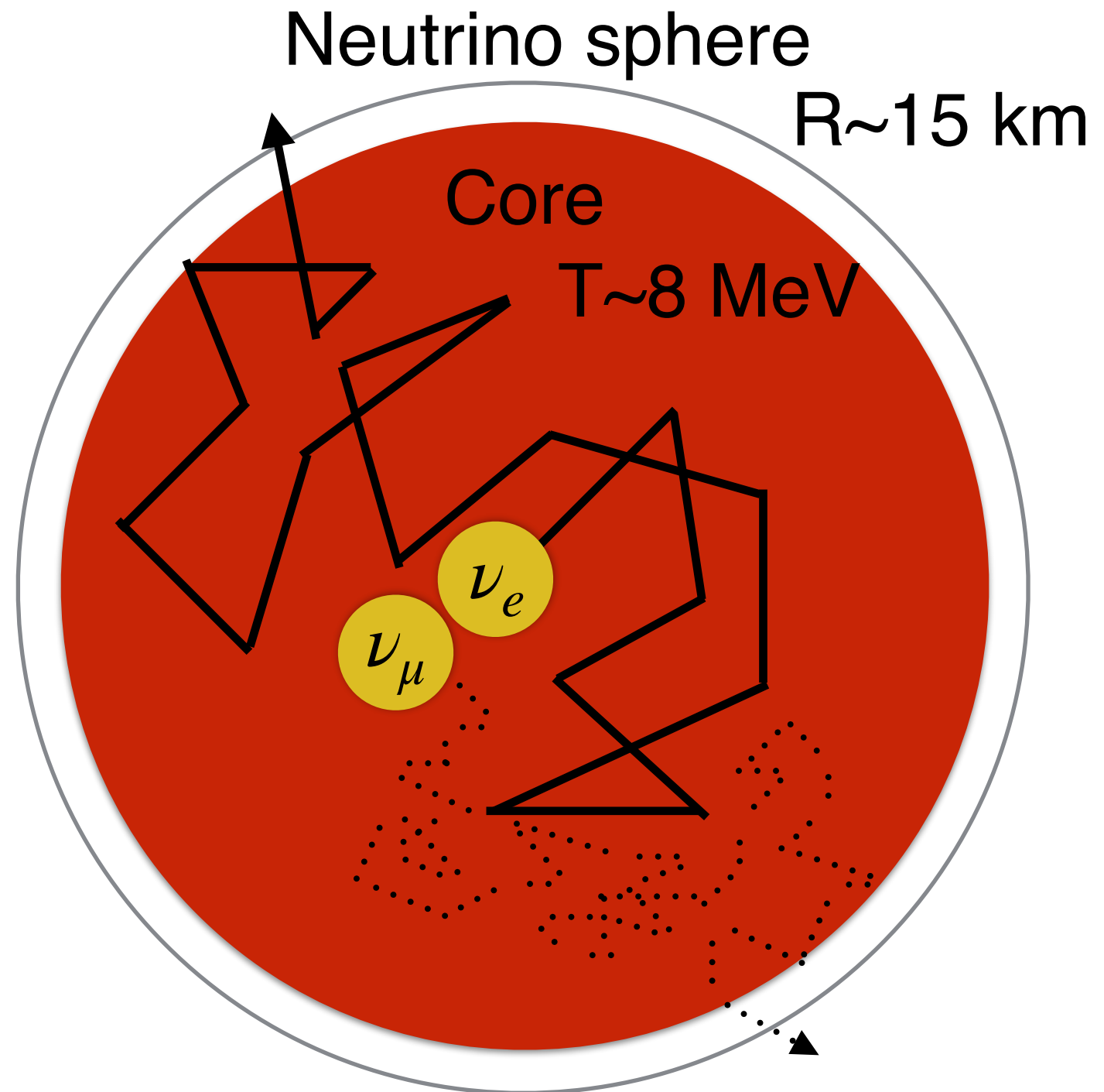
“dip” feature in the neutrino spectrum possible indication?

[IceCube collaboration, arXiv:1710.01191](#)

Supernova cooling

$\nu\bar{\nu} \rightarrow Z' \rightarrow \nu\bar{\nu}$ shortens the mean-free path of ν_μ and ν_τ
 $\lambda \sim 0.01 \text{ cm}$, while that of ν_e is unchanged $\lambda \sim 4 \text{ m}$

AK and Yu, PRD, 2015



lengthen diffusion time of
 ν_μ and $\nu_\tau : \tau \sim 10^5 \text{ s}$
 while that of ν_e is unchanged:
 $\tau \sim 10 \text{ s}$ (SN1987A)

Thank you for your attention

Experimental constraints

$$Z' \text{ contribution to } (g-2)_\mu : \Delta a_\mu^{Z'} \simeq 32 \times 10^{-10} \left(\frac{g'}{5 \times 10^{-4}} \right)^2 \text{ for } m_{Z'} \ll m_\mu$$

Evade existing constraints from

- neutrino trident production (CHARM-II, CCFR): $\nu N \rightarrow \nu N \mu \bar{\mu}$

Altmannshofer *et al.*, PRL, 2014

- Υ decay (BABAR): $e\bar{e} \rightarrow \Upsilon \rightarrow \mu\bar{\mu}Z' \rightarrow \mu\bar{\mu}\mu\bar{\mu}$

BaBar Collaboration, PRD, 2016

- ^7Be solar neutrino event rate: ν - e (Borexino)

Bellini *et al.*, PRL, 2011

- white dwarf cooling: $\gamma \rightarrow \nu\bar{\nu}$ (γ : plasmon)

Dreiner *et al.*, PRD, 2013

Caveat on Borexino and WD bounds:

although $\epsilon = 0$, Z' - A and Z' - Z mixings arise at one-loop level

→ Z' couples to the SM electromagnetic current $-\epsilon_{AZ'} e Z'_\mu J_{\text{em}}^\mu$

$$\epsilon_{AZ'} = -\frac{eg'}{12\pi^2} \ln \left(\frac{m_\tau^2}{m_\mu^2} \right) \simeq 7.2 \times 10^{-6} \times \left(\frac{g'}{5 \times 10^{-4}} \right)$$

Cosmological constraint

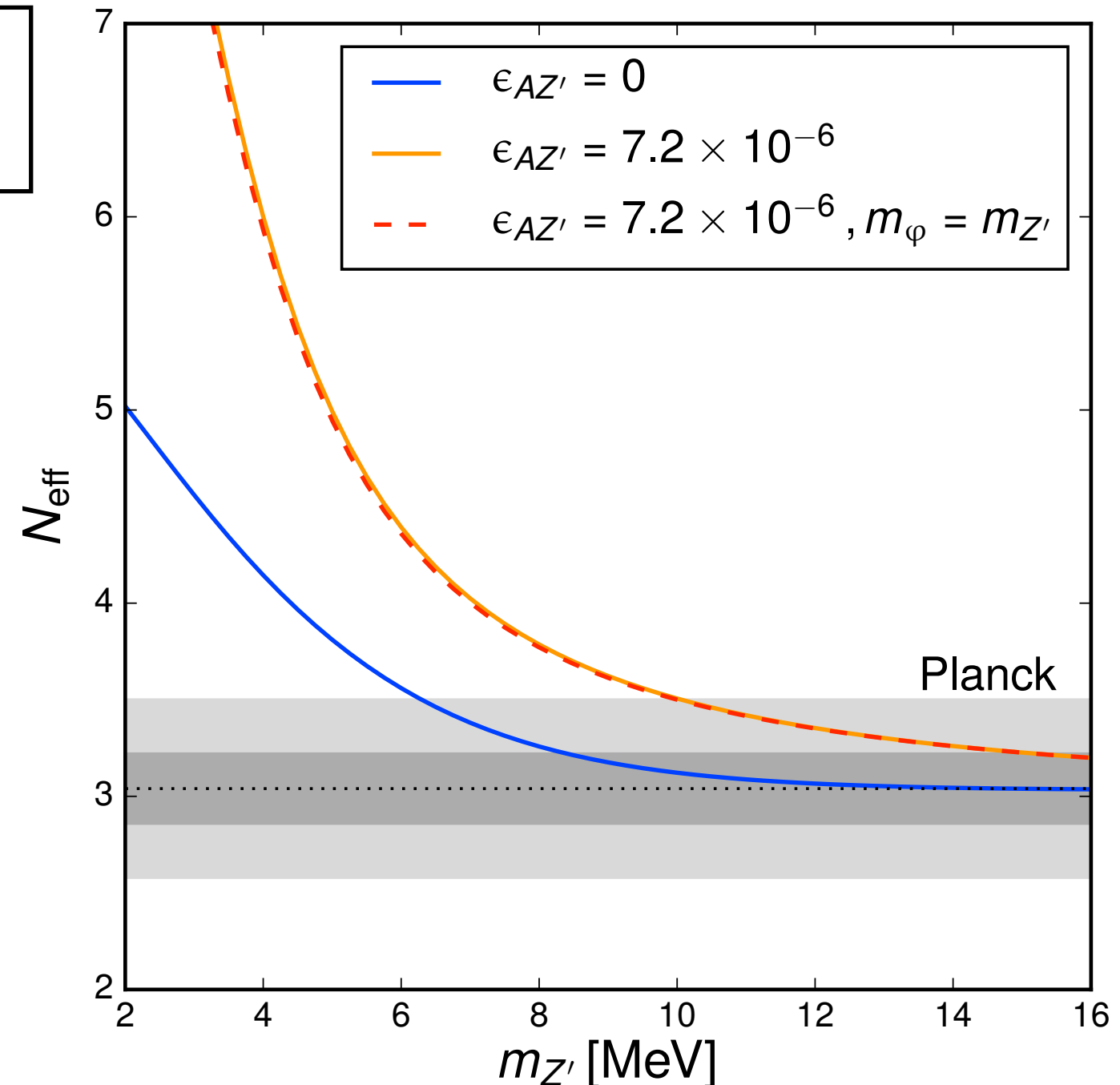
$Z' \rightarrow \nu\bar{\nu}$ heats only ν_μ and ν_τ after neutrino decoupling
 $Z' \rightarrow e\bar{e}$ through Z' - A mixing transfer heats
 between (e, γ) and (ν_μ, ν_τ, Z')

change the effective number
of neutrino degrees of freedom

$\varphi \rightarrow Z'\nu\bar{\nu}$ is sufficiently rapid
for $m_\varphi \geq m_{Z'}$

Benchmark points
($m_{Z'} > 10 \text{ MeV}$) satisfy
 $N_{\text{eff}} < 3.5$

Planck Collaboration, A&A, 2015



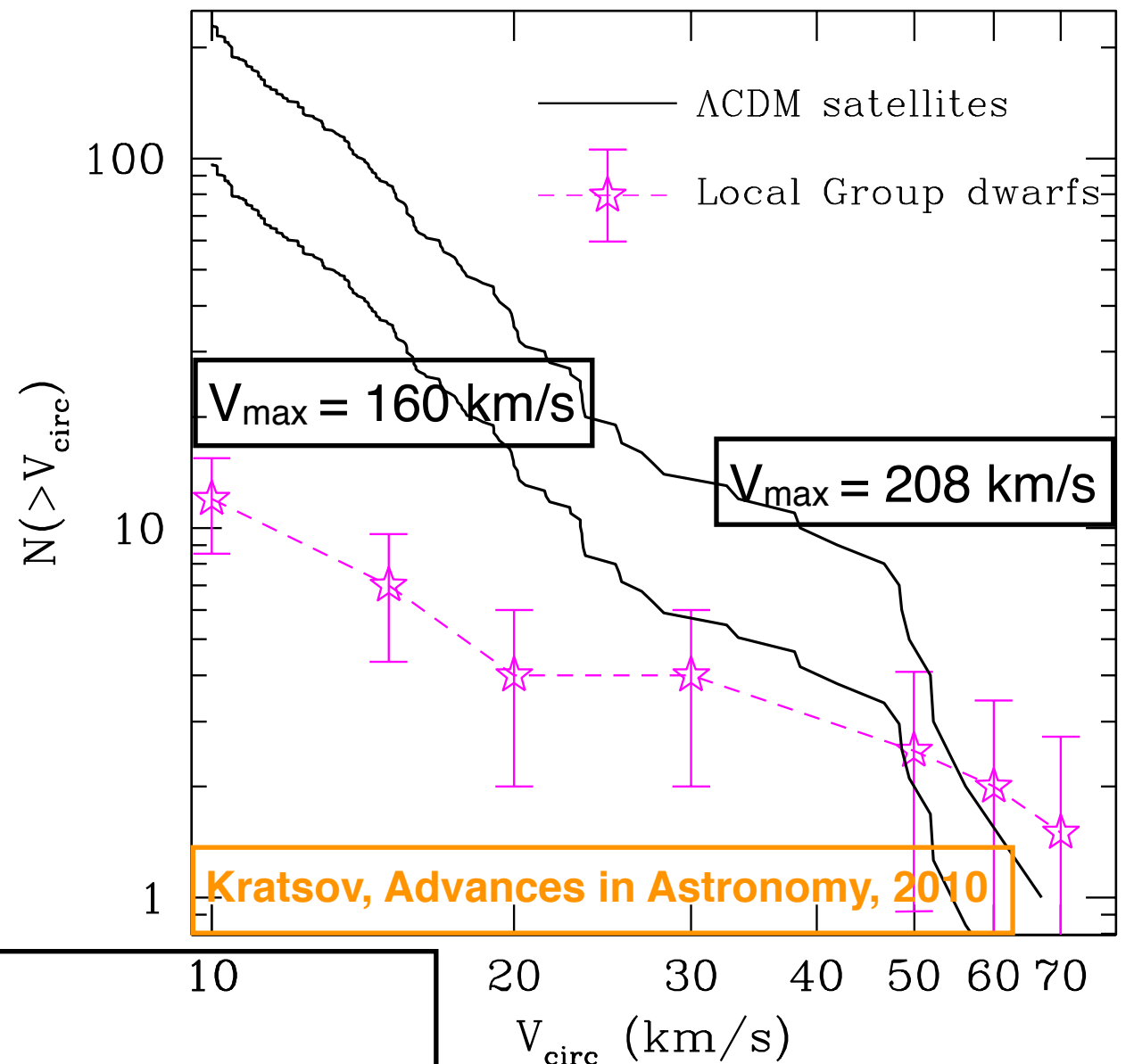
Small scale crisis I

When N -body simulations in the Λ CDM model and observations are compared, problems appear at (sub-)galactic scales: **small scale crisis**

missing satellite problem

N -body (DM-only) simulations in the Λ CDM model $\rightarrow$ Milky Way-size halos host $\mathcal{O}(10)$ times larger number of subhalos than that of observed dwarf spheroidal galaxies

cumulative number of subhalos



(maximum) circular velocity

$$V_{\text{circ}}^2(r) = \frac{GM(<r)}{r} \quad V_{\max} = \max_r \{V_{\text{circ}}(r)\}$$

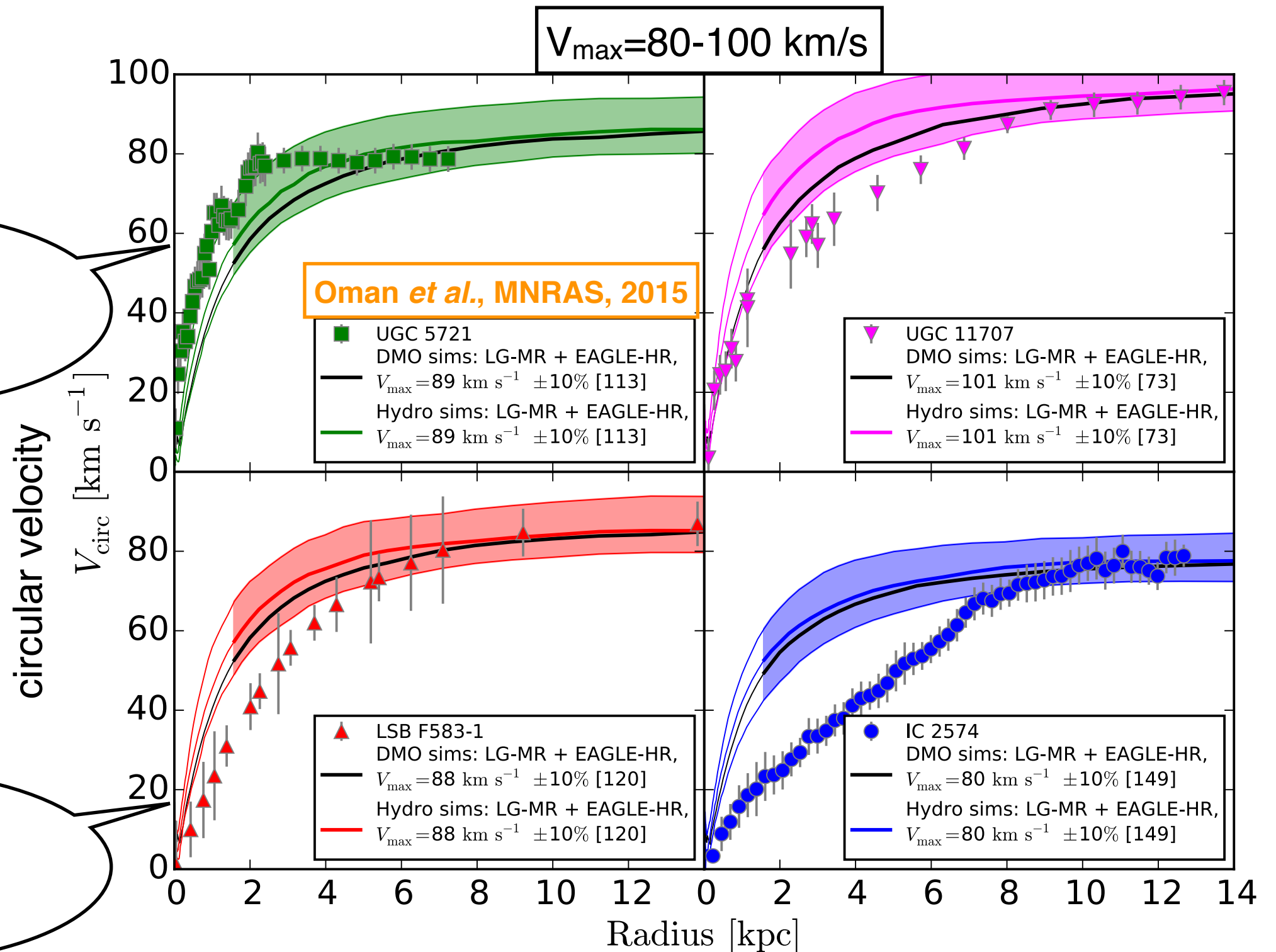
maximal circular velocity of subhalo

Small scale crisis II

Unexpected diversity of rotation curves

well-reproduced

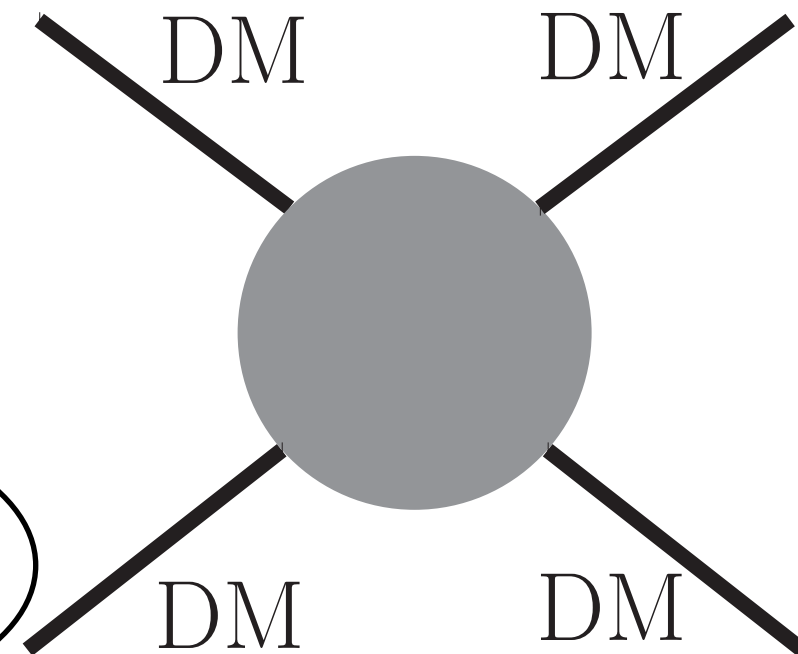
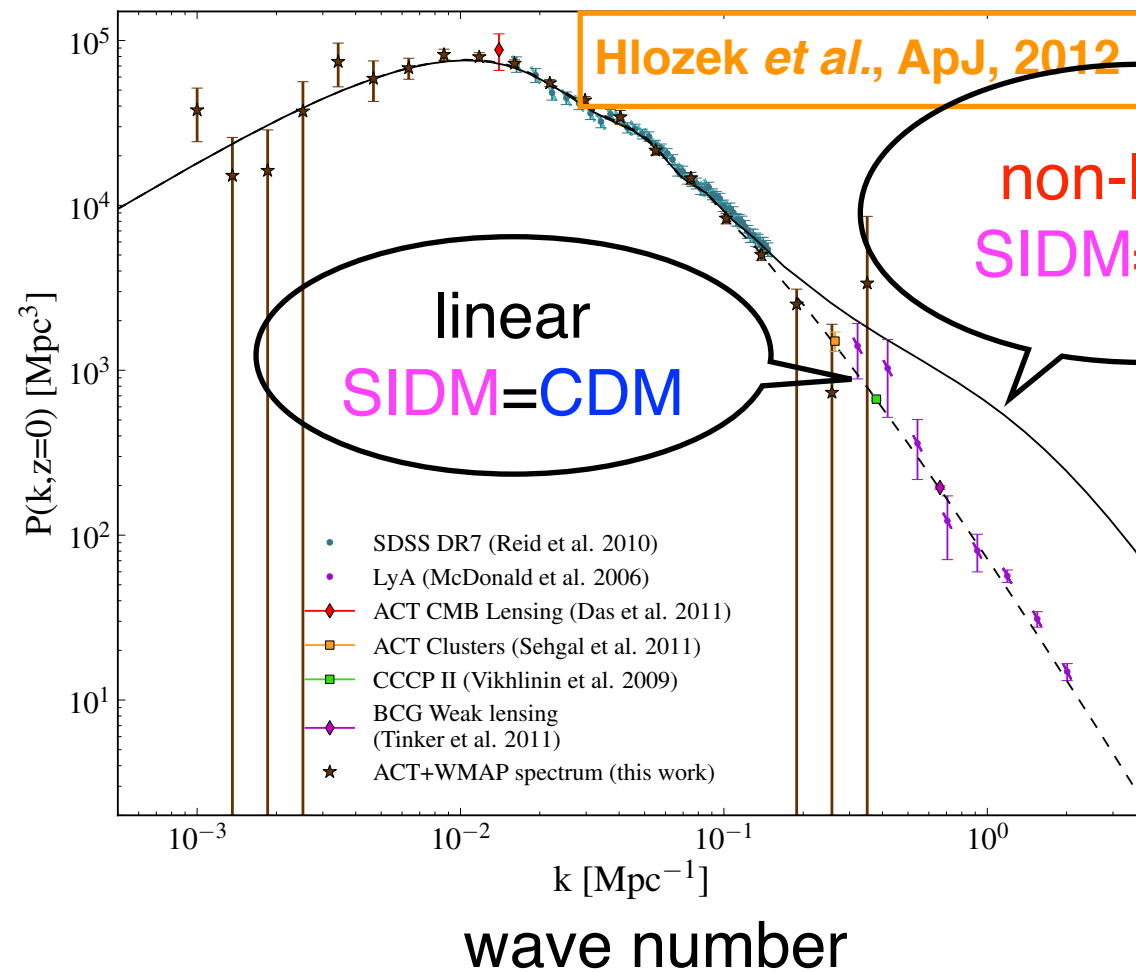
badly-reproduced



Dark matter self-interaction

Self-Interacting Dark Matter: **SIDM**

power spectrum of density perturbations



Reaction rate $\Gamma = \sigma v \rho / m$

σ : cross section

v : relative velocity

ρ : dark matter mass density

m : dark matter mass

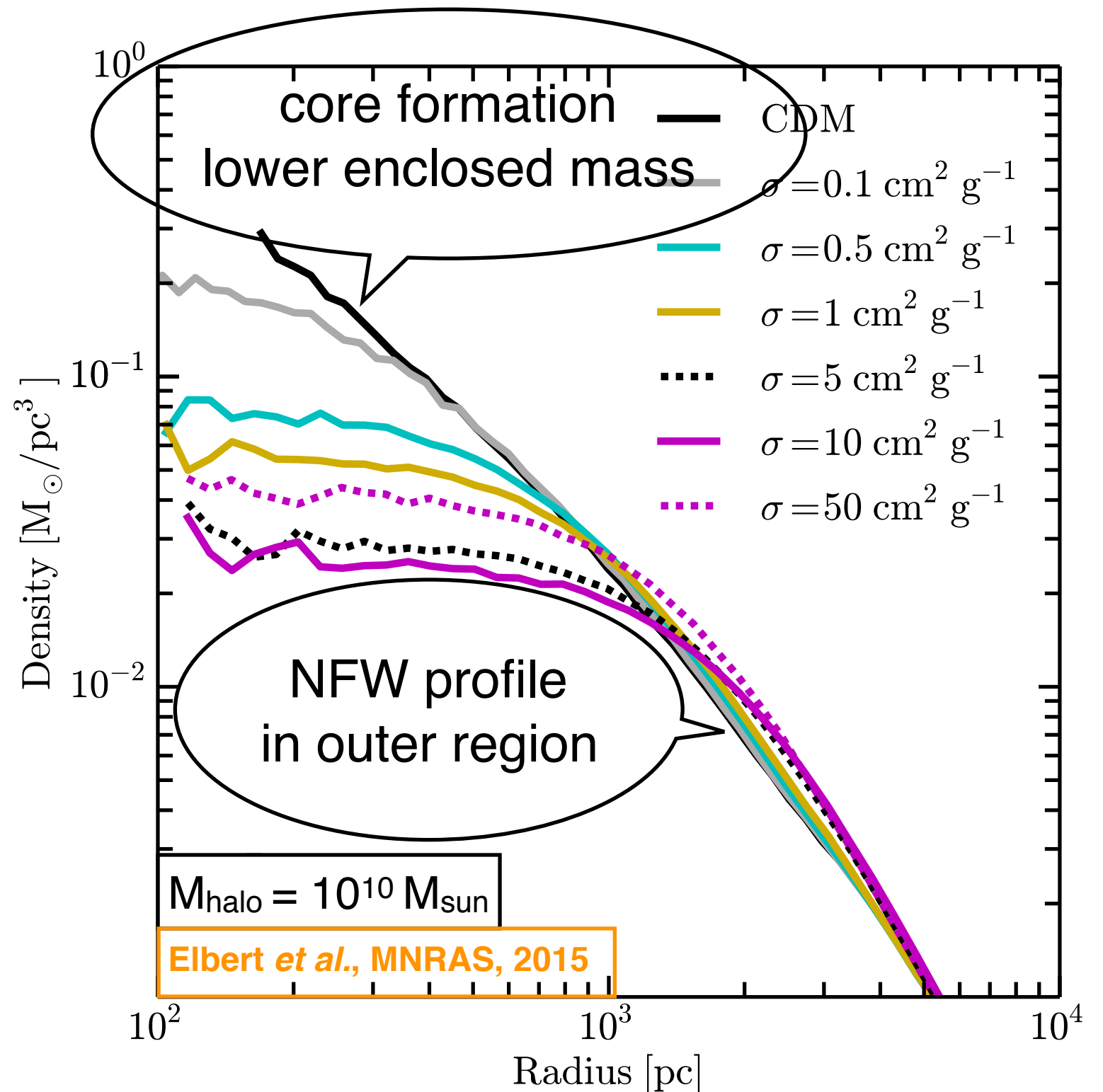
SIDM structure formation starts with the same linear (initial) matter power spectra as **CDM**, but self-interactions become **important** as structure formation proceeds $\leftrightarrow \rho$ increases

SIDM halo - mass density

SIDM-only simulation

As σ/m increases,
central density decreases

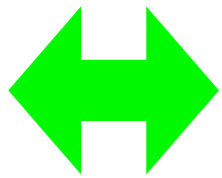
Inverted at some point
← gravo-thermo instability
↔ core-collapse



$\sigma/m = 0.5\text{-}5 \text{ cm}^2/\text{g}$ may solve the inner mass deficit problem

Origin of the diversity

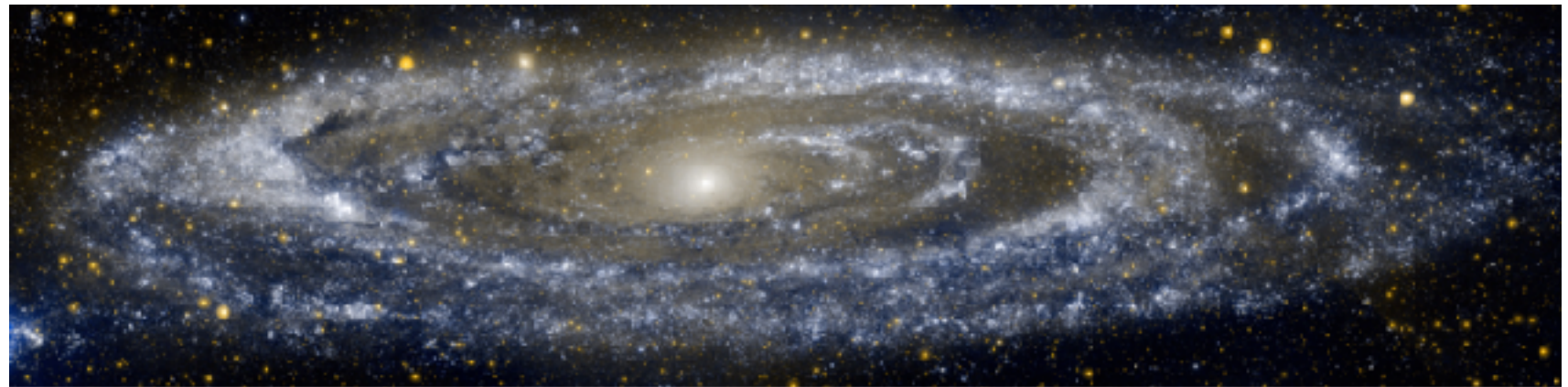
How does SIDM solve the unexpected diversity problem?



For a given cross section ($\sigma/m = 3 \text{ cm}^2/\text{g}$ in the following),
SIDM halo profile is still **definite** and characterized
by only one parameter V_{max}

Scatter in distributions of the baryons
even among similar-size halos!

Extended
stellar disk



Compact
stellar disk



Influence of the baryons

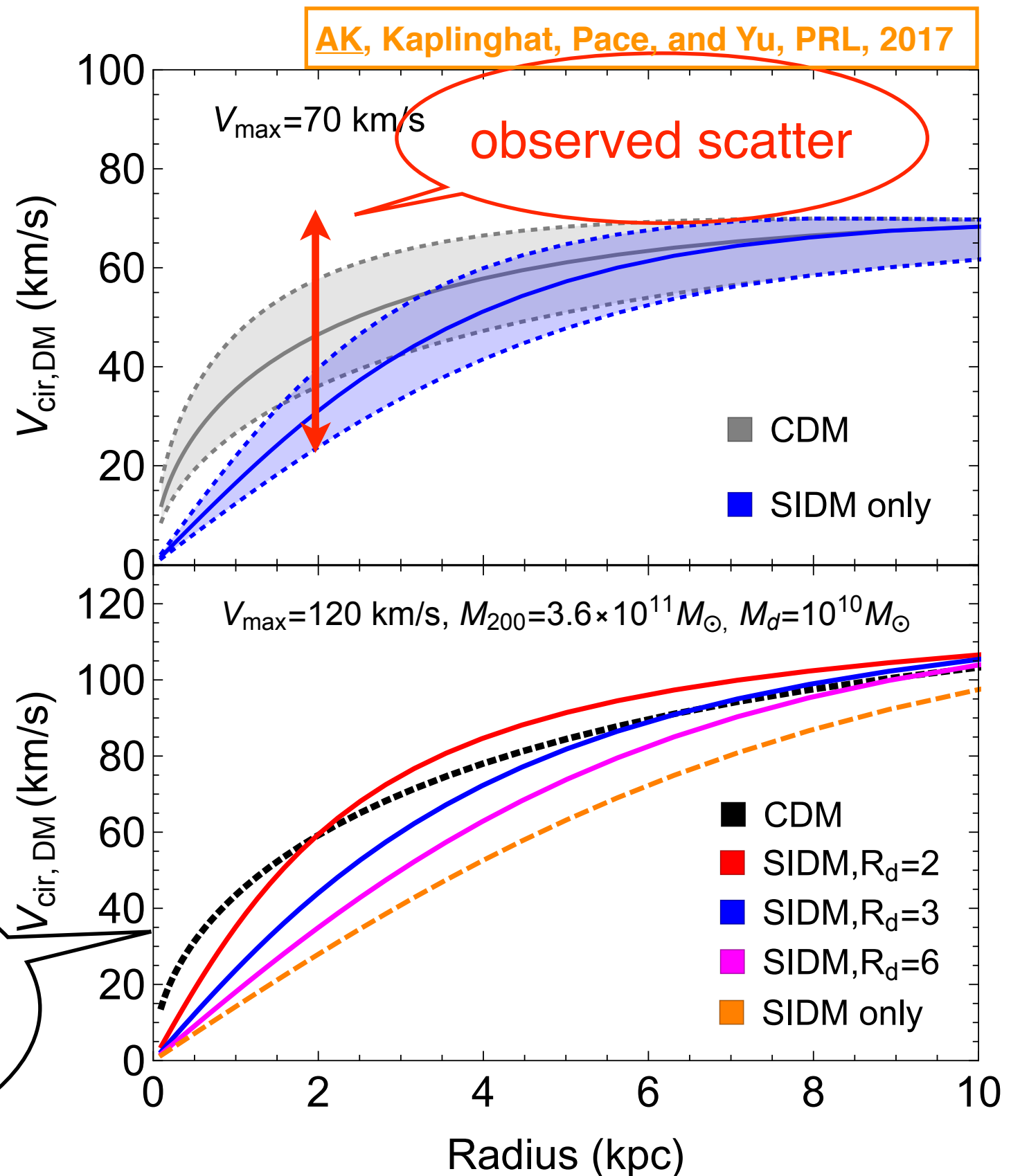
Iso-thermal distribution from the Poisson equation:

$$\rho_{\text{DM}}(\vec{x}) = \rho_{\text{DM}}^0 \exp(-\phi(\vec{x})/\sigma^2)$$

$$\Delta\phi = 4\pi G(\rho_{\text{DM}} + \rho_{\text{baryon}})$$

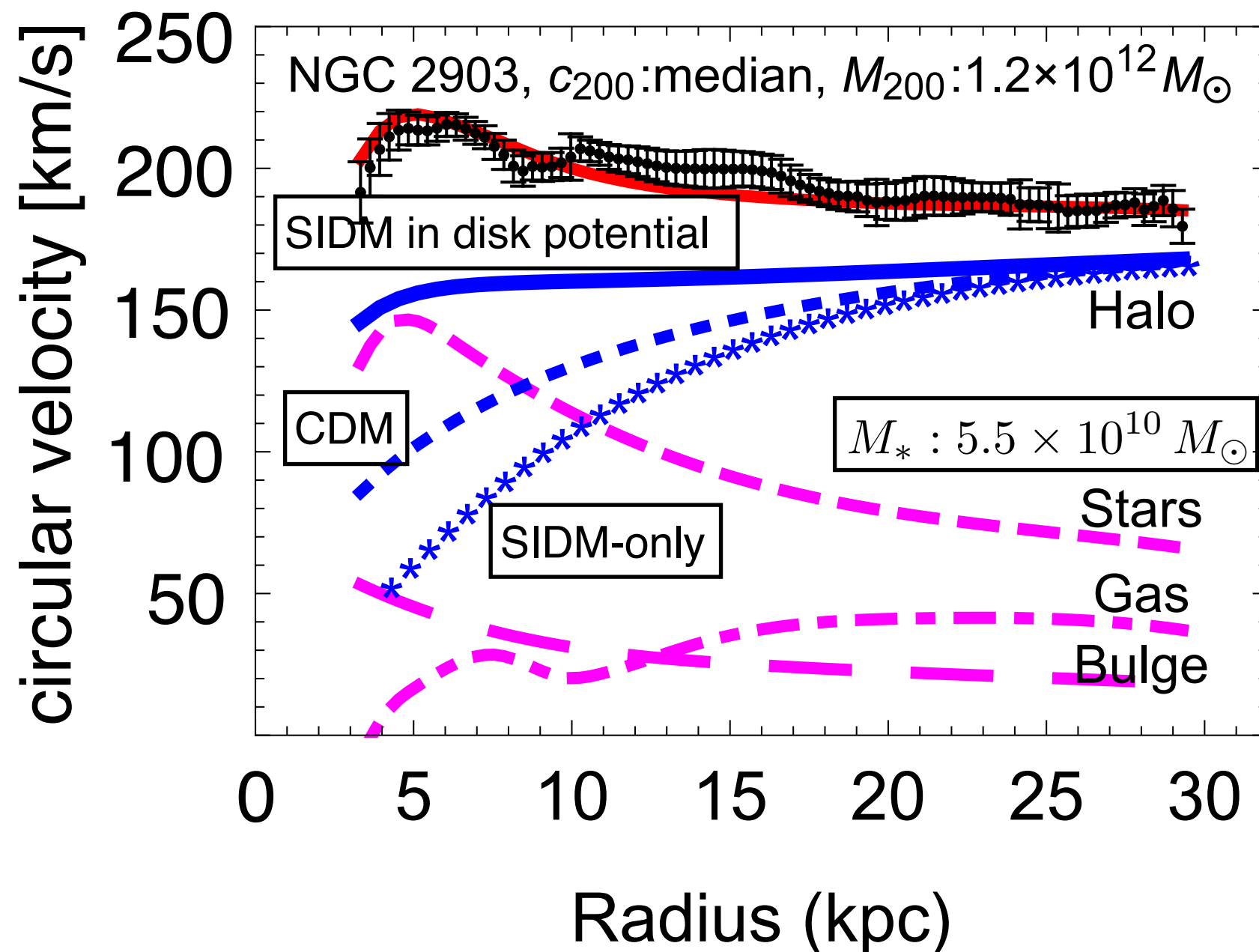
matched to the NFW profile
at r_1 ($\sigma v \rho(r_1) t_{\text{age}}/m = 1$)

SIDM profile **contracts**
under the presence of **compact**
stellar disk



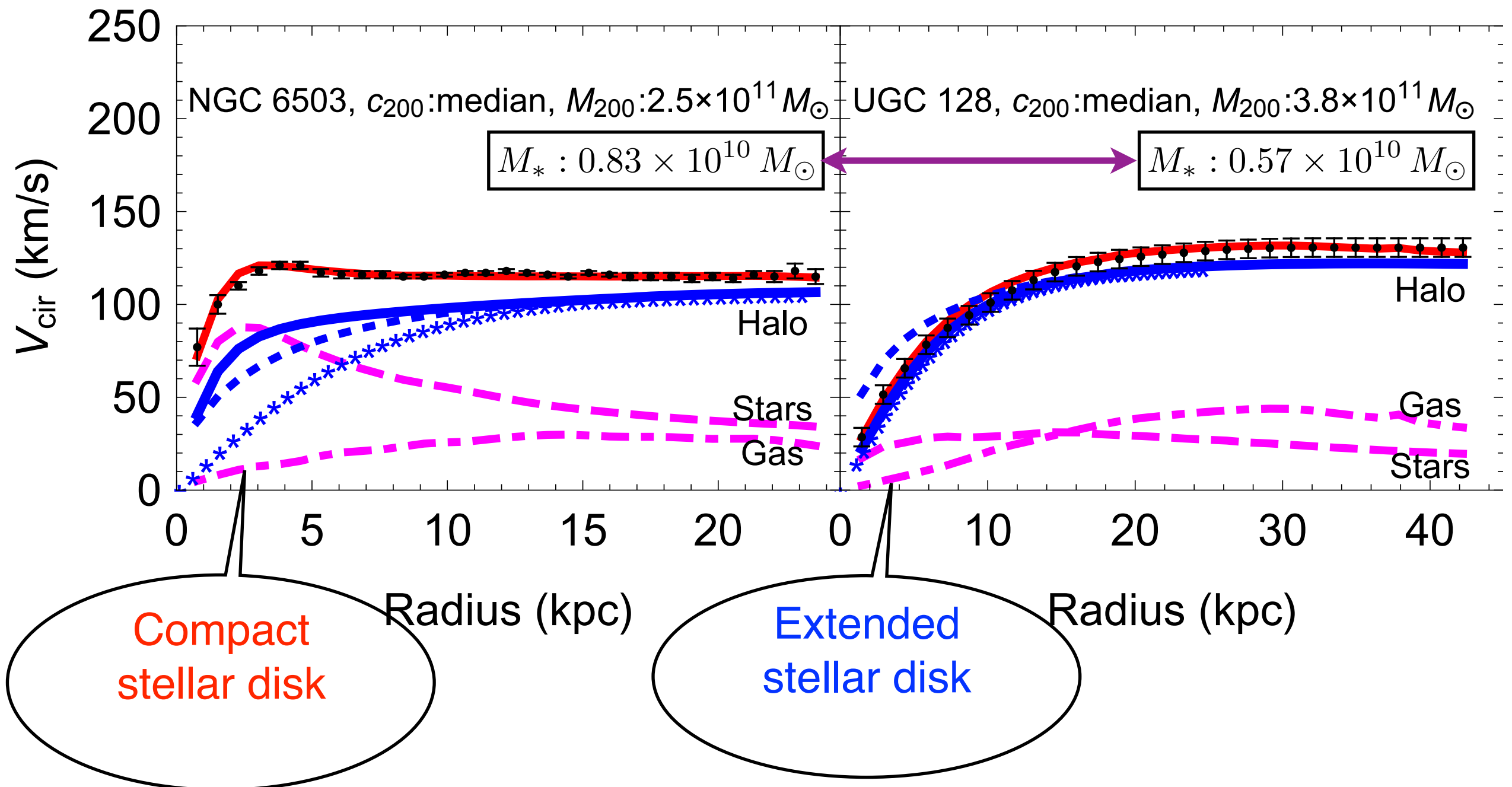
Case study I

In a **massive** spiral galaxy, the observed **compact disk** can change **the whole SIDM distribution**



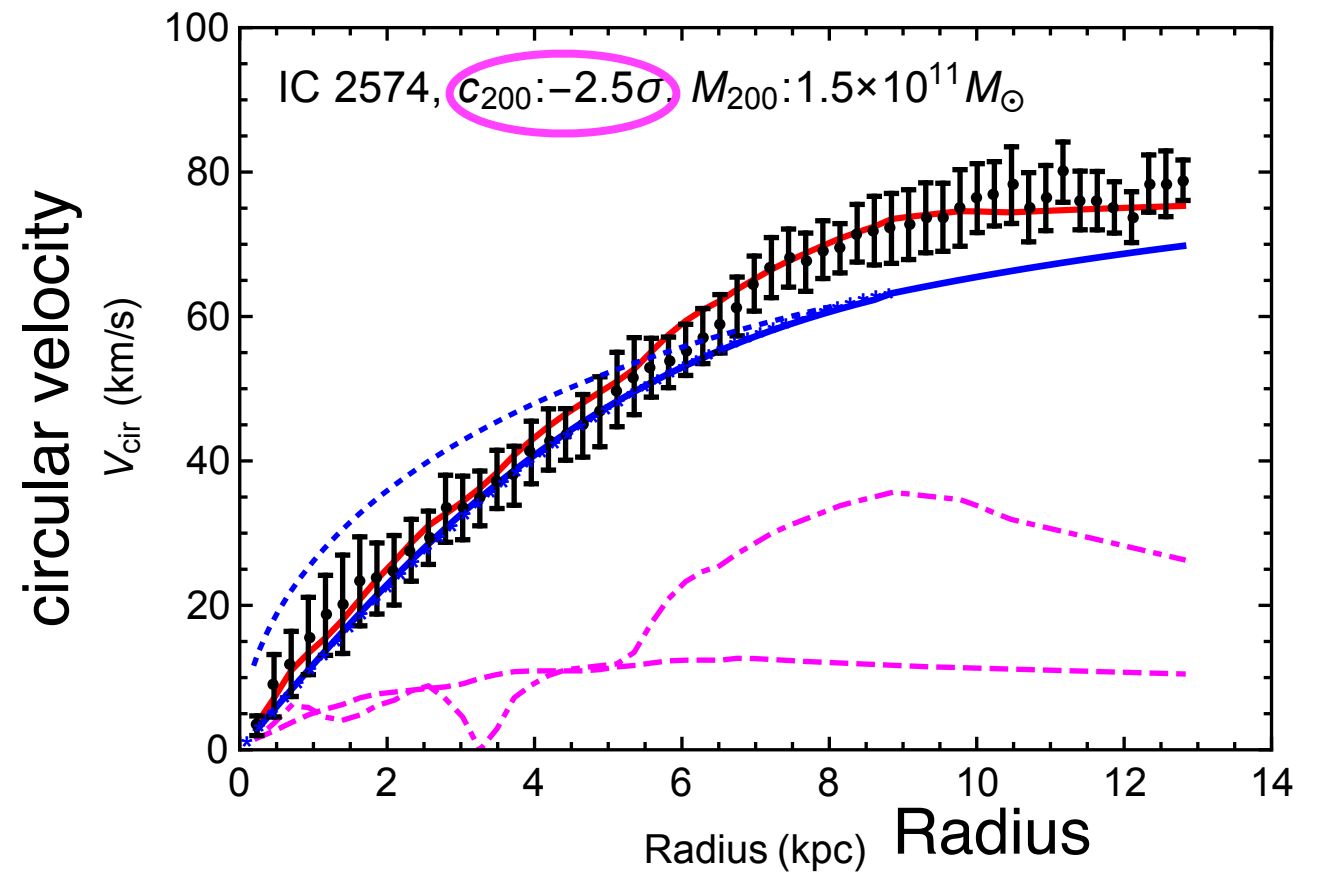
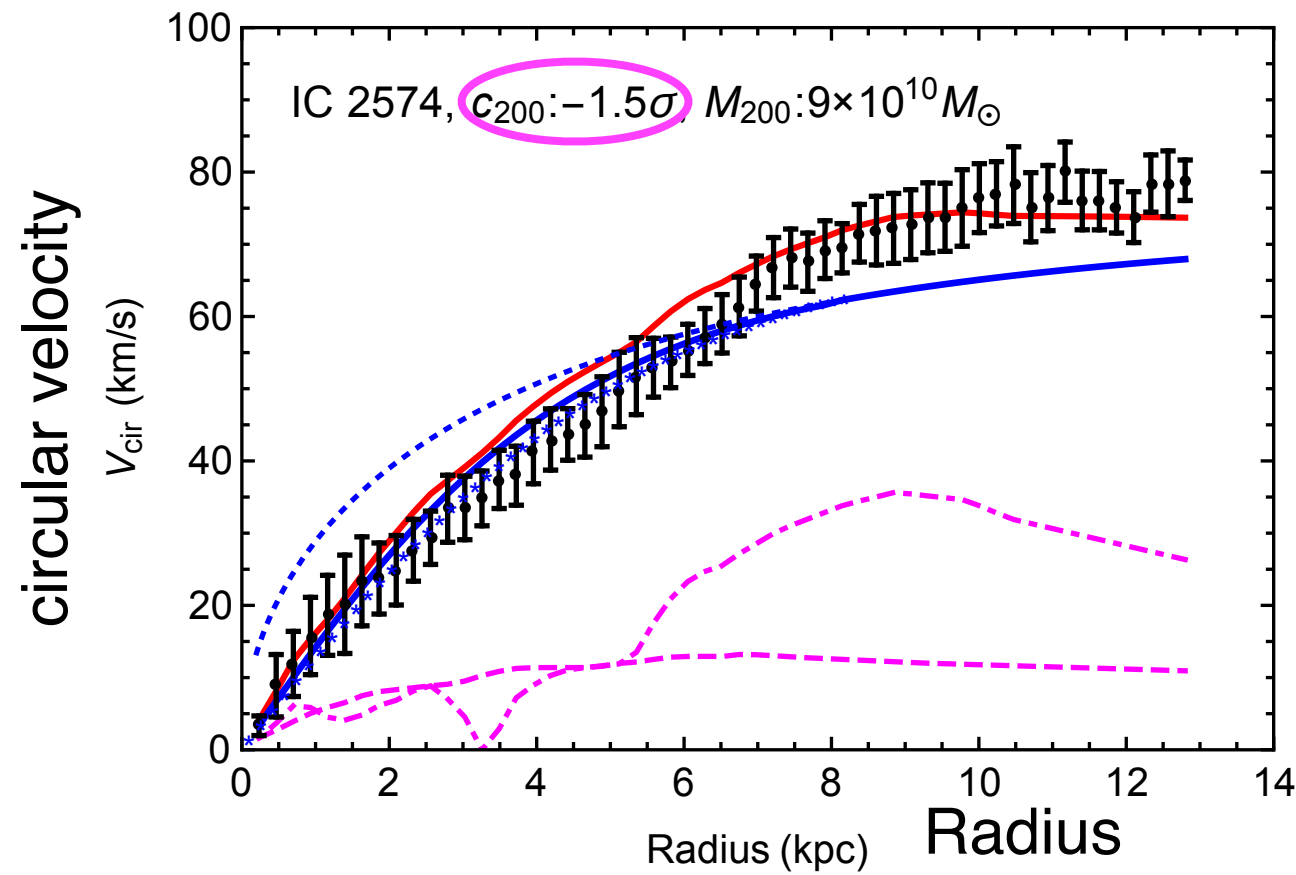
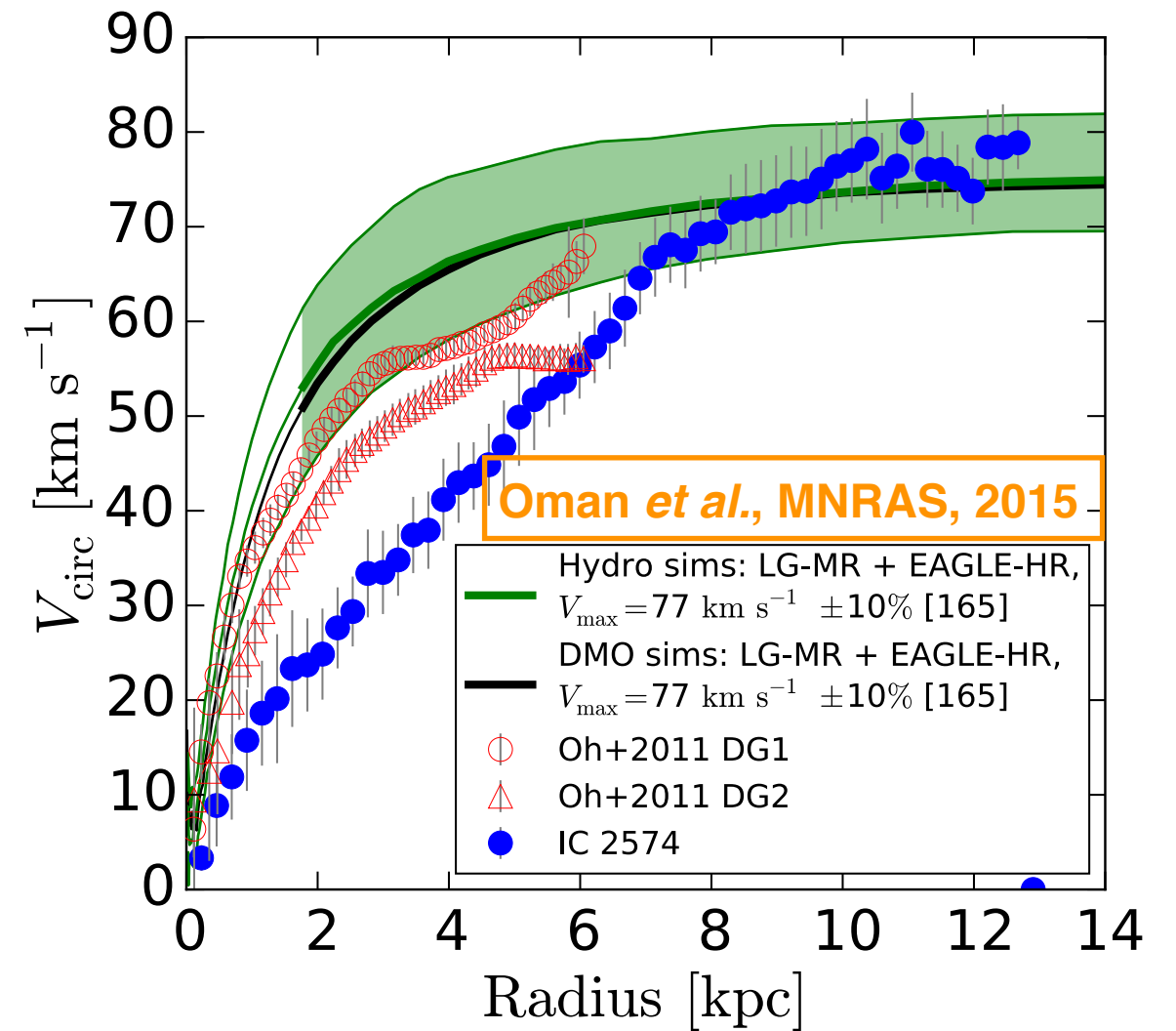
Case study II

SIDM halo profile reflects **how compact** the hosted stellar disk is even with similar $V_{\max}$ and M_*



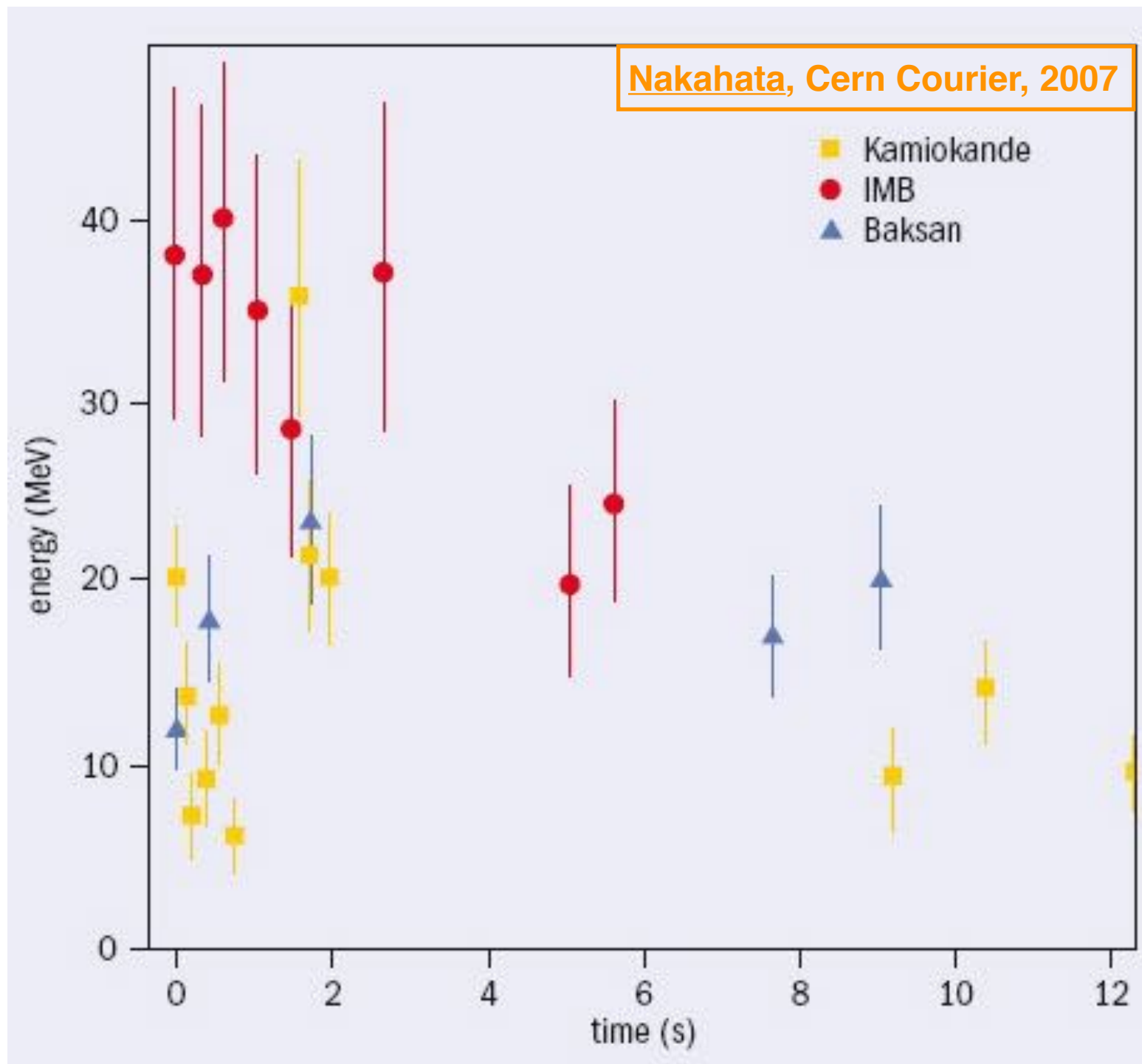
Case study III

The **intrinsic scatter of SIDM halos** is also needed to reproduce the observed diversity

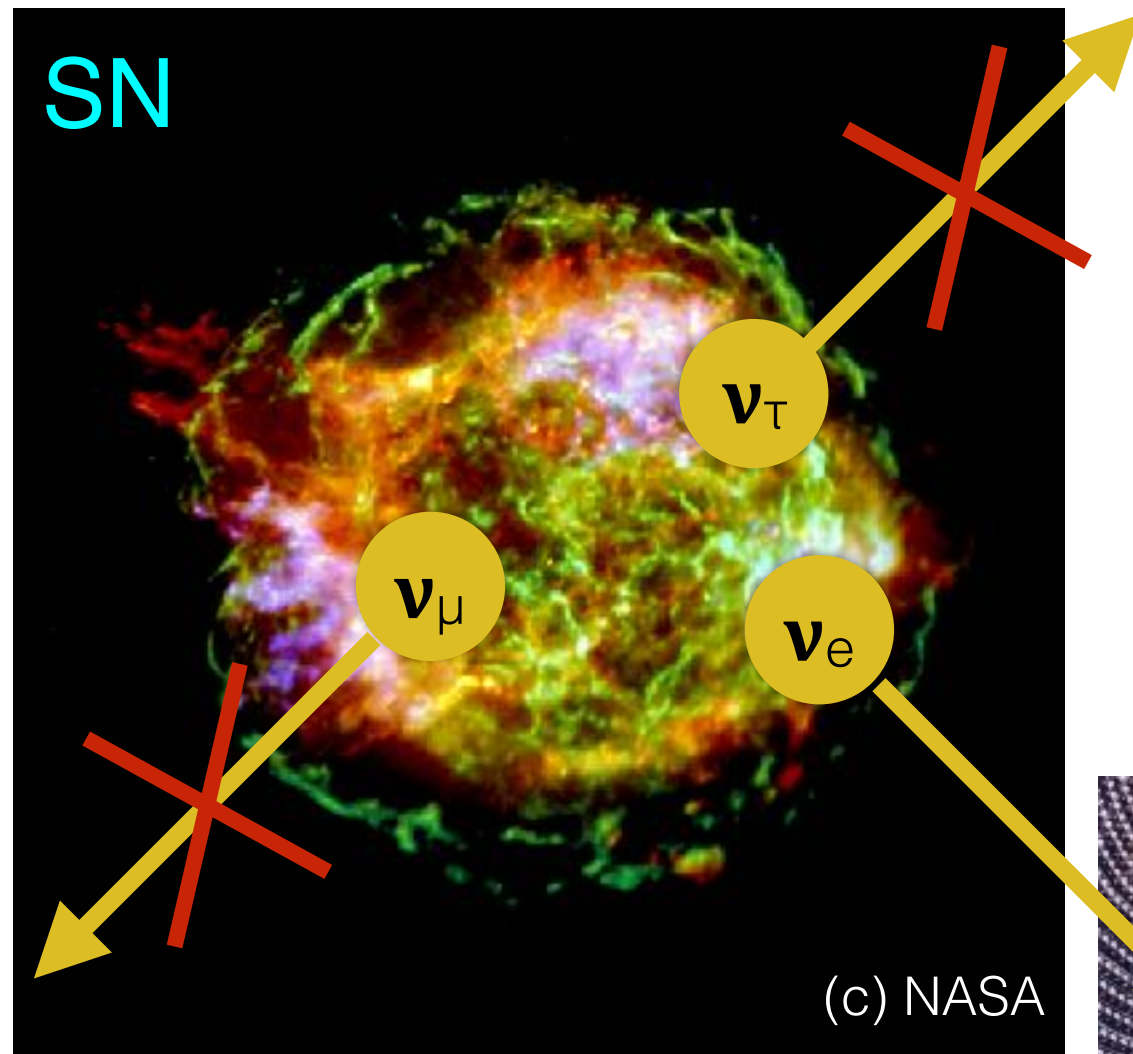


SN 1987A

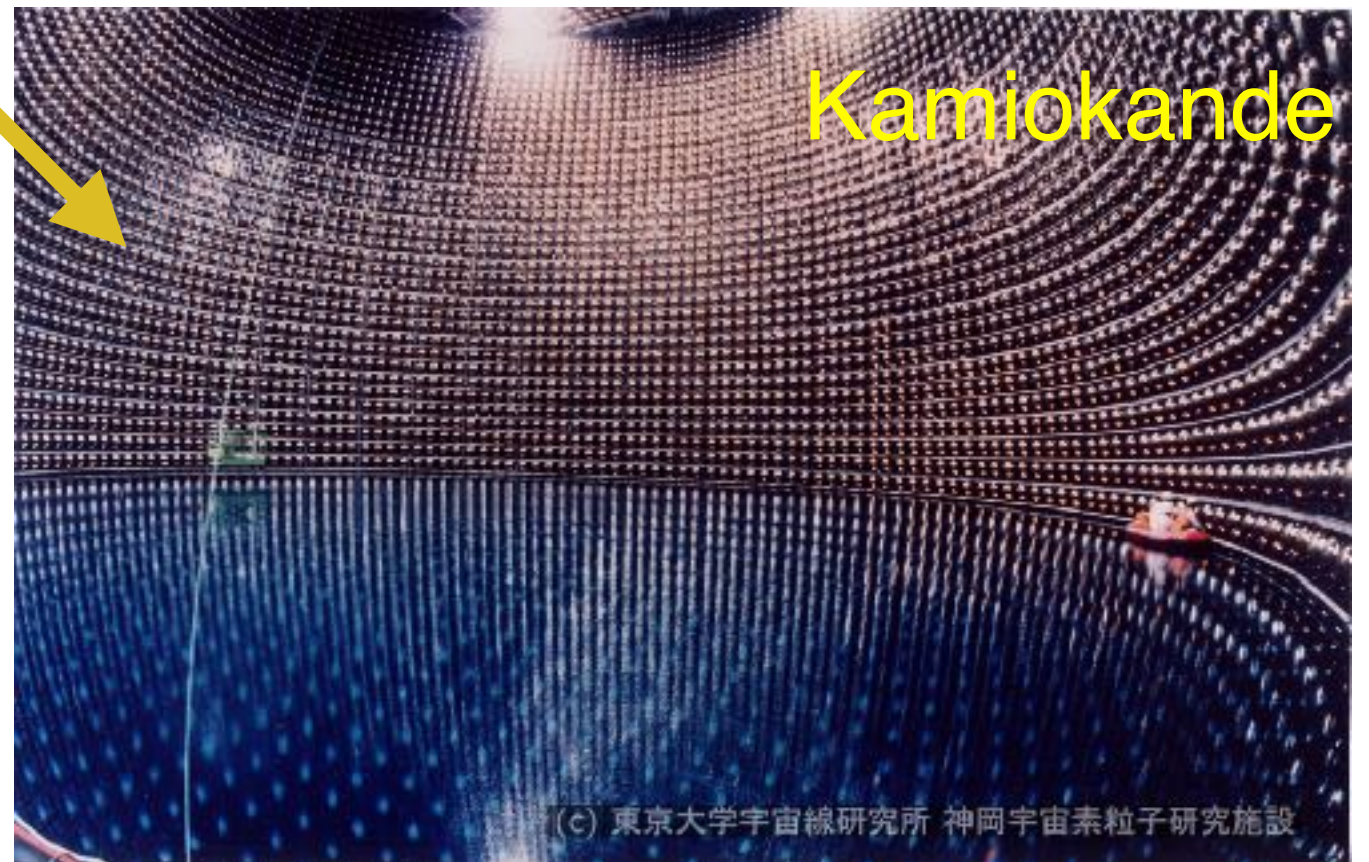
10s determines the duration of neutrino cooling



Summary of astrophysical implications



Only ν_e is emitted from SN



Summary of astrophysical implications

