Cosmology with type la Supernova gravitational lensing

Jacobo Asorey (in collaboration with T. Davis, E. Macaulay)

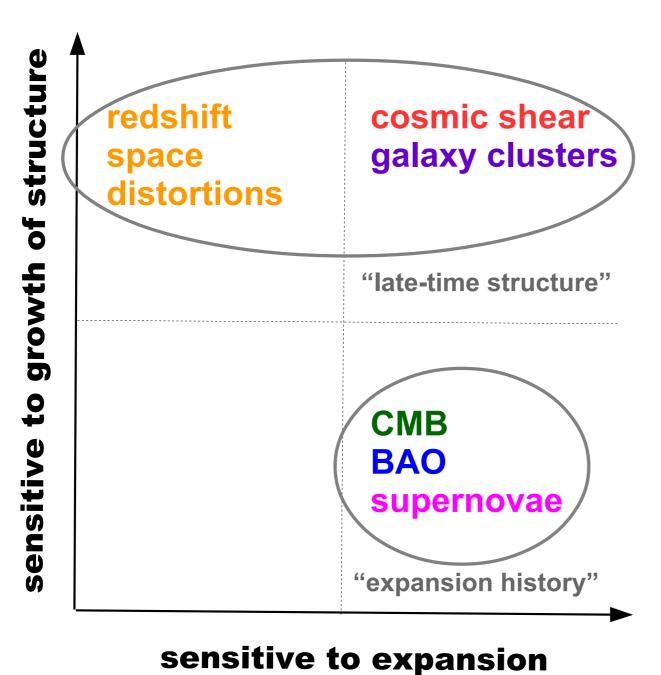
Cosmo-18, IBS, Daejeon, 28 August 2018







How to survey Dark Energy



Q: Do all these measurements agree with predictions in the same, fiducial ΛCDM model?

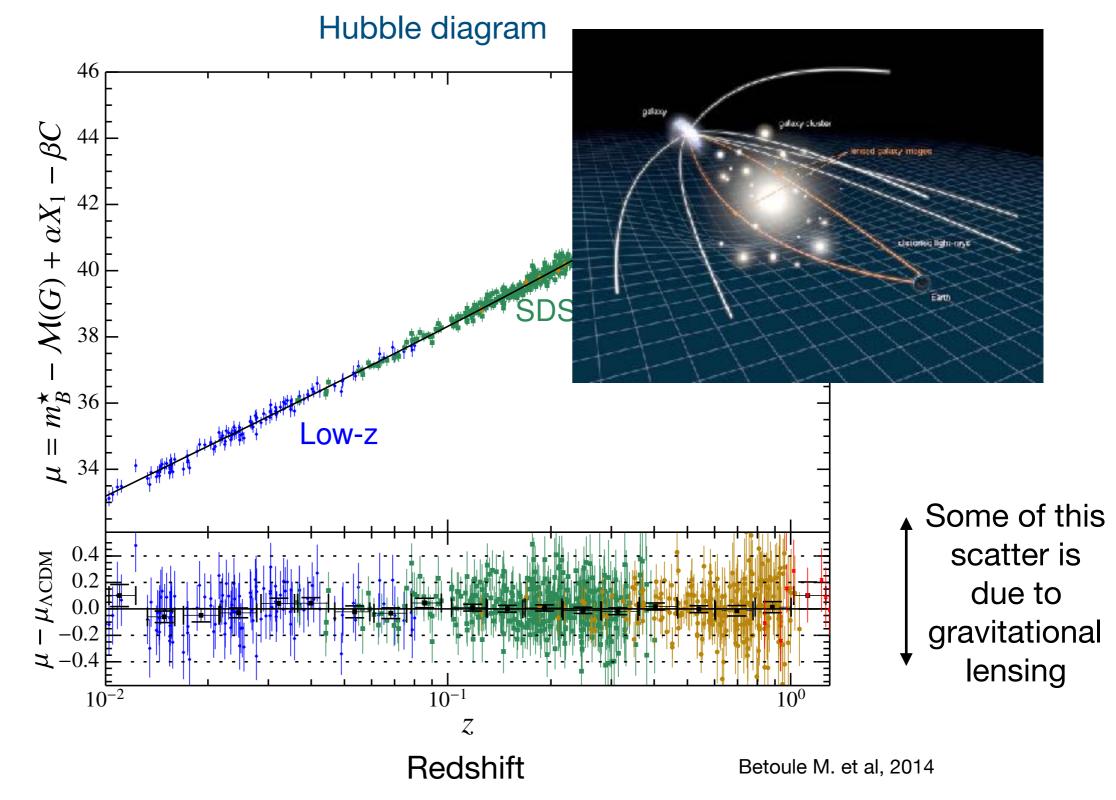
$$-\Omega_{\rm m} \sim 0.3$$

$$-\Omega_{\wedge} \sim 0.7$$

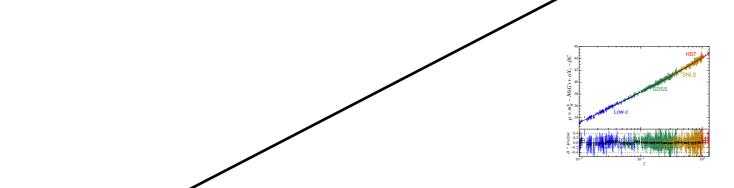
$$-\sigma_8 \sim 0.8$$

$$- h \sim 0.7$$

Influence of growth of structure in SN lensing



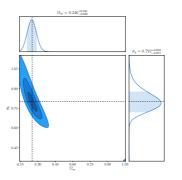
Impact on type Ia SN Cosmology



$$\mu = m_b - (M_b - \alpha x_1 + \beta c) - \frac{5}{\ln 10} \kappa$$

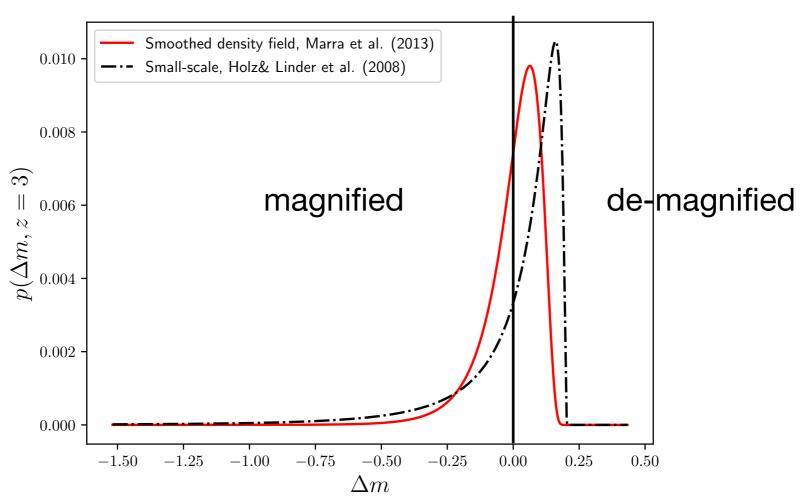
SN lensing

Cosmology with type Ia SN lensing



$$\kappa_{g_i} = \frac{3H_0^2 \Omega_m}{2c^2} \sum_j \delta_{g_{i,j}} \frac{(r_s - r_j)r_j}{r_s a_j} dr_j$$

Cosmology with type IA SN lensing: Probabilistic approach



Lensing magnification (in magnitude)

Assume a universal PDF that describes the probability of a given SN at redshift z to be magnified or demagnified

Moments of the Hubble diagram residuals at different redshift bins

$$\mu_{1} = 0$$

$$\mu_{2} = \sigma_{lens}^{2} + \sigma_{I}^{2}$$

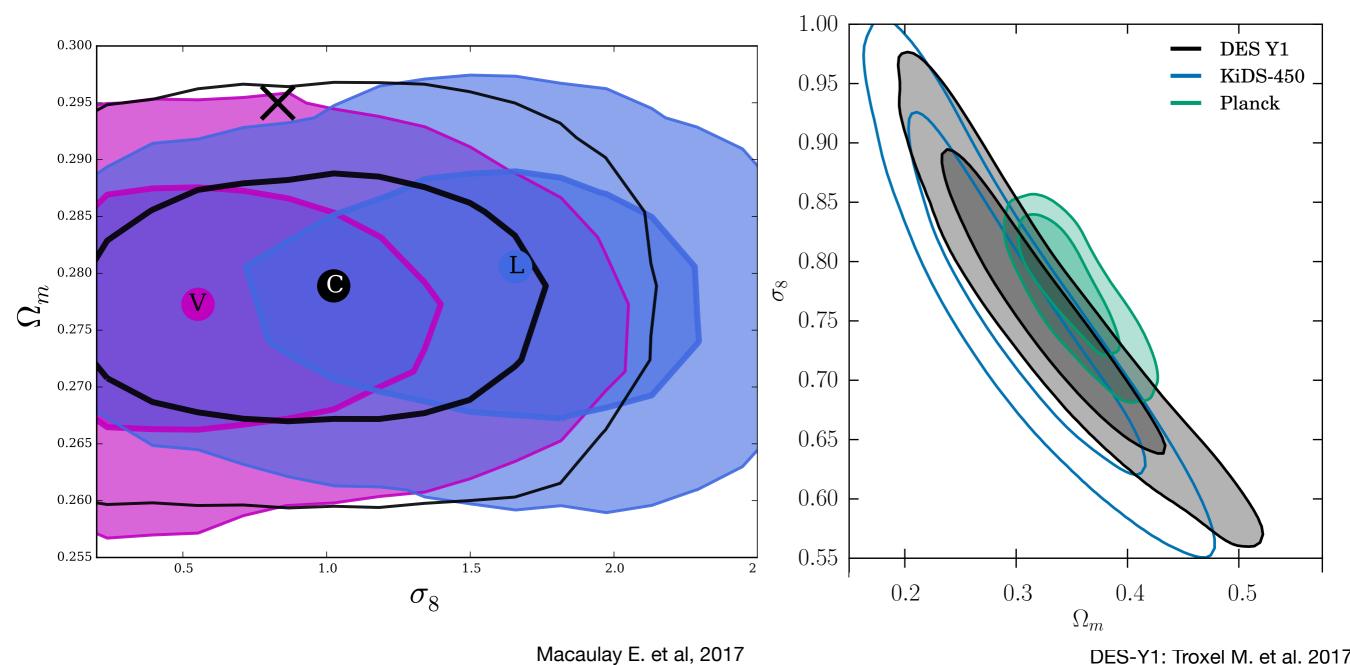
$$\mu_{3} = \mu_{3,lens} + \mu_{3,I}$$

$$\mu_{4} = \mu_{4,lens} + \mu_{4,I} + 3\mu_{2}^{2} - 3\sigma_{lens}^{4}$$

Free parameters of the model:

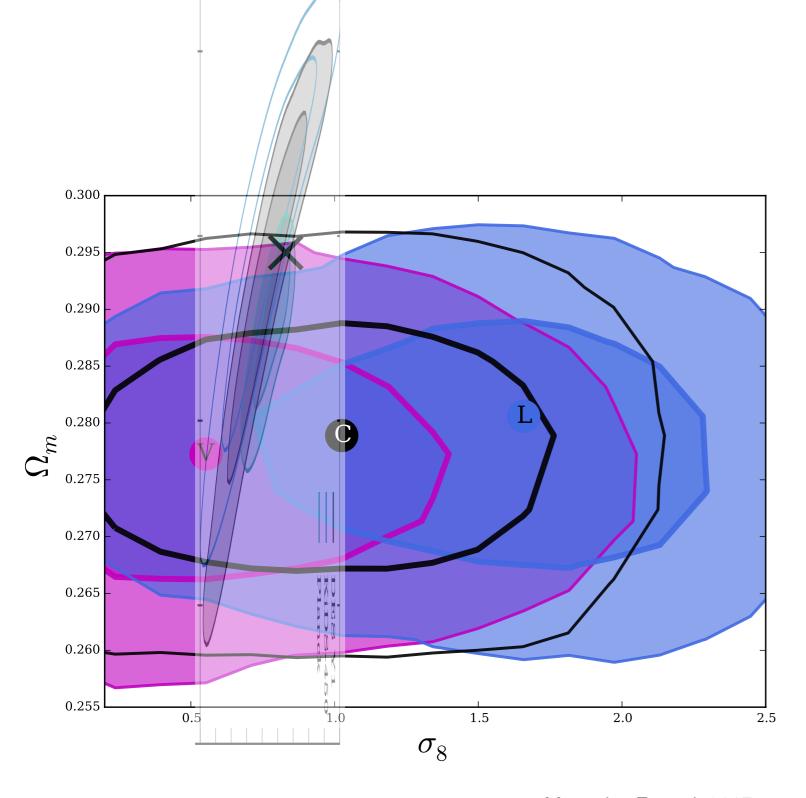
$$\{\Omega_m, \sigma_8, \sigma_I, \mu_{3,I}, \mu_{4,I}\}$$

Cosmology with type IA SN lensing: Probabilistic approach



Best fit to JLA Supernova Sample

DES-Y1: Troxel M. et al. 2017
DES-Y1 galaxy shear-shear



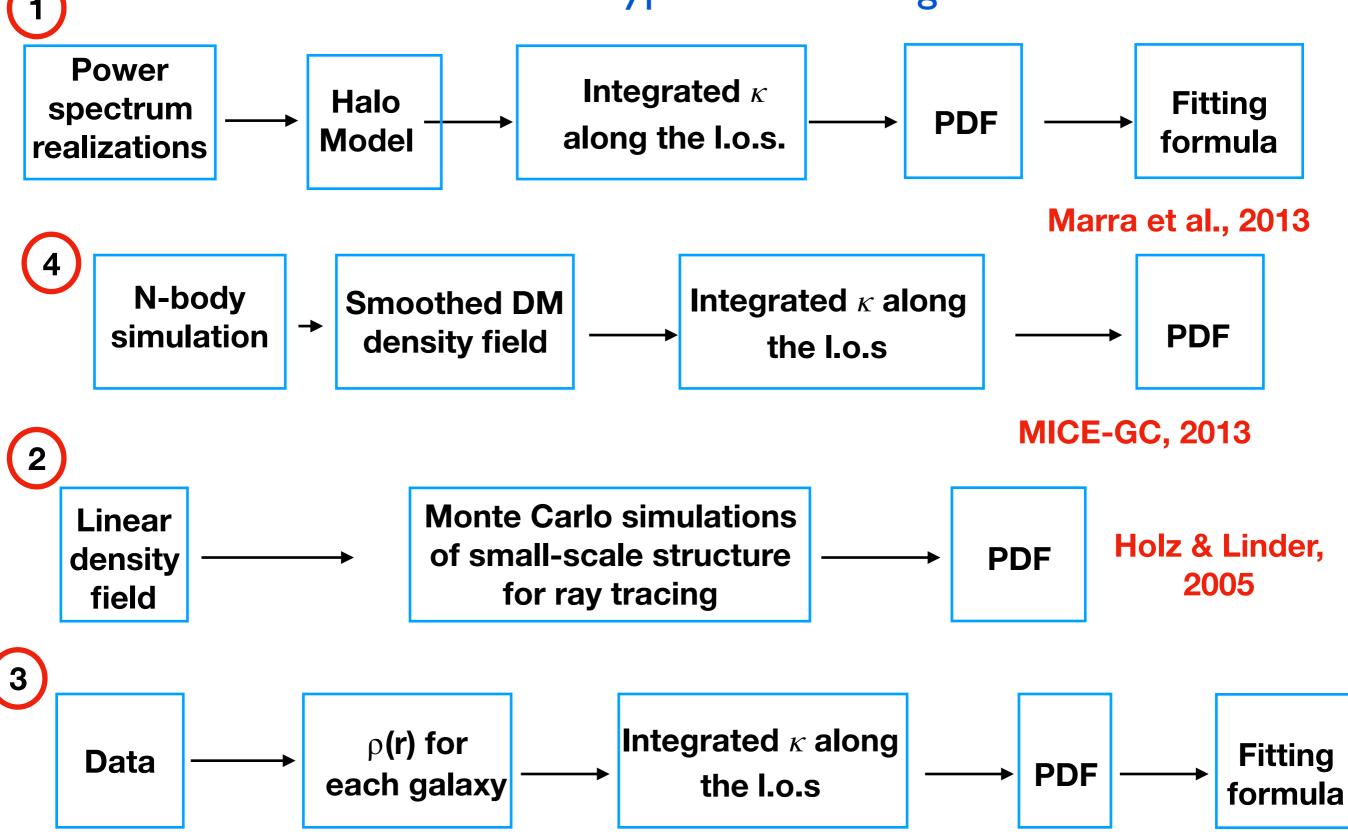
Macaulay E. et al, 2017

Best fit to JLA Supernova Sample

DES-Y1: Troxel M. et al. 2017

DES-Y1 galaxy shear-shear

Models for type la SN lensing



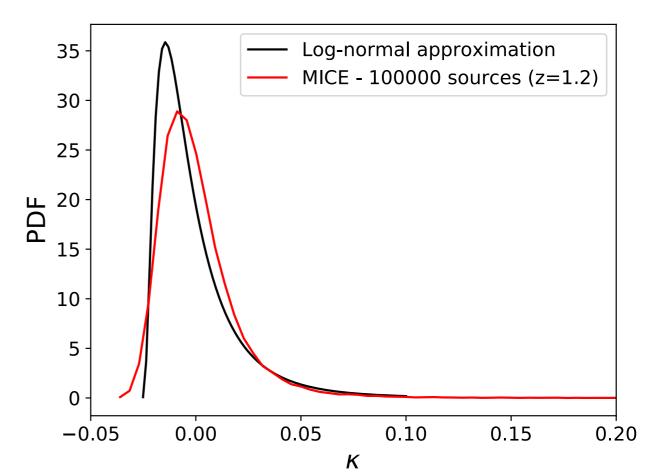
Jonsson, 2010

1) Log-normal approach

$$p(\kappa) = \frac{exp\left[-\frac{\log(\kappa + \mu_{logn}) - \bar{\kappa} - \mu_{gauss}}{2\sigma_{gauss}}\right]}{\sqrt{2\pi}\sigma_{gauss}(\kappa + \mu_{logn} - \bar{\kappa})}$$

$$\mu_{gauss} = \frac{1}{2} \log \left[\frac{\mu_{logn}^2}{1 + \sigma_{gauss}^2 / \mu_{logn}^2} \right] \quad = \frac{1}{15}$$

$$\sigma_{gauss}^2 = \log\left[1 + \sigma_{logn}^2/\mu_{logn}^2\right]$$



$$\sigma_{\text{lens}}(z, \sigma_8, \Omega_{m0}) = \frac{0.0004 - 0.00176\sigma_8 + (-0.035 + \sigma_8 \Omega_{m0} + 0.0453\sigma_8)z}{(2.19 + \sigma_8^2)\Omega_{m0}z + 3.19 \exp\left[0.365/(0.193 + z)\right]};$$

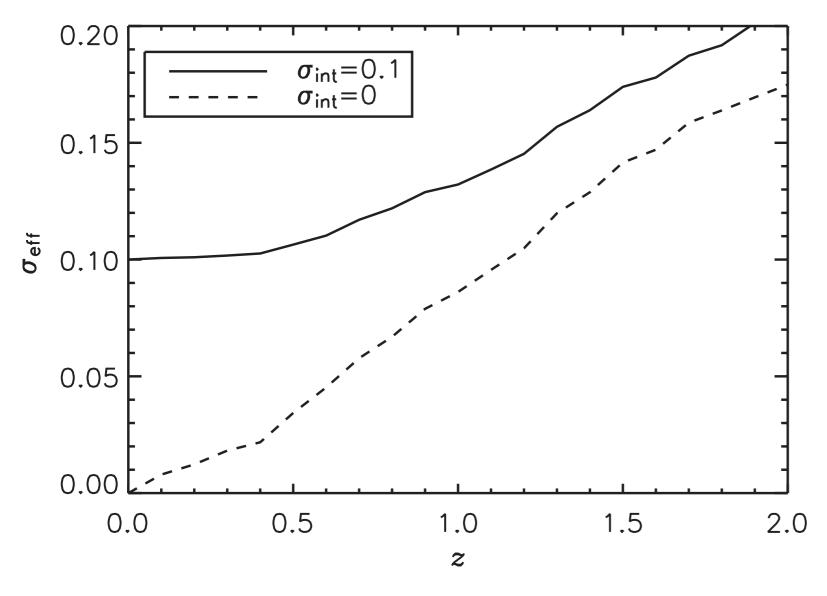
$$\mu_{3,\text{lens}}^{1/3}(z, \sigma_8, \Omega_{m0}) = \frac{\sigma_8^2 \Omega_{m0} z^2}{\sigma_8 \sqrt{z} + 1.1z + (4.24\sigma_8^2 - \Omega_{m0}^2)\Omega_{m0} z^2 + 0.118(1 - \sigma_8)z^3};$$

$$\mu_{4,\text{lens}}^{1/4}(z, \sigma_8, \Omega_{m0}) = \frac{(-0.029 + 0.1\sigma_8 + 0.47\Omega_{m0}\sigma_8)z}{\exp\left[(-0.029 + 0.1\sigma_8 + 0.47\Omega_{m0}\sigma_8)z + \frac{0.021}{0.018 + \Omega_{m0}\sigma_8z}\right] + 0.3z}.$$

Marra, Quartin & Amendola, 2013

Create realizations for different parameter values and estimate fitting formulas.

2) Ray tracing including compact objects

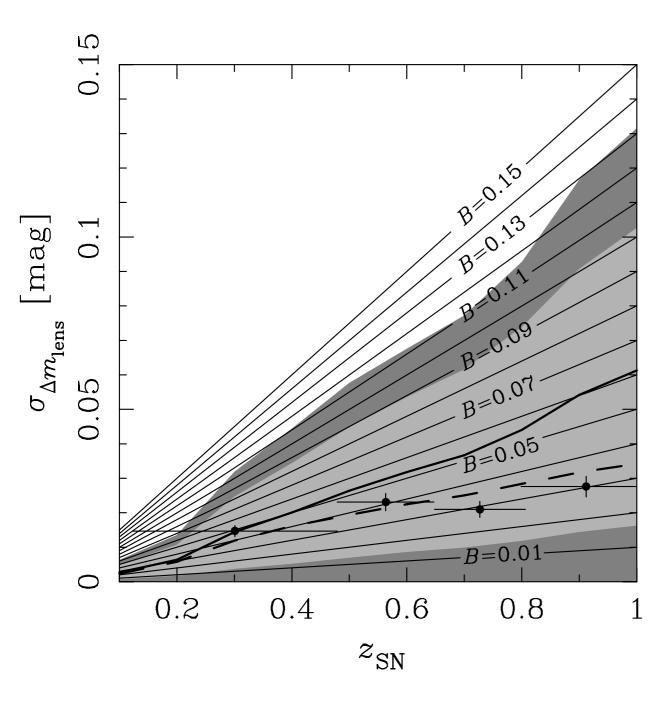


Ray tracing including small scales clustering

$$\sigma_{\delta m} = 0.088z$$

Holz & Linder 2005

3) Use data to reconstruct halo model

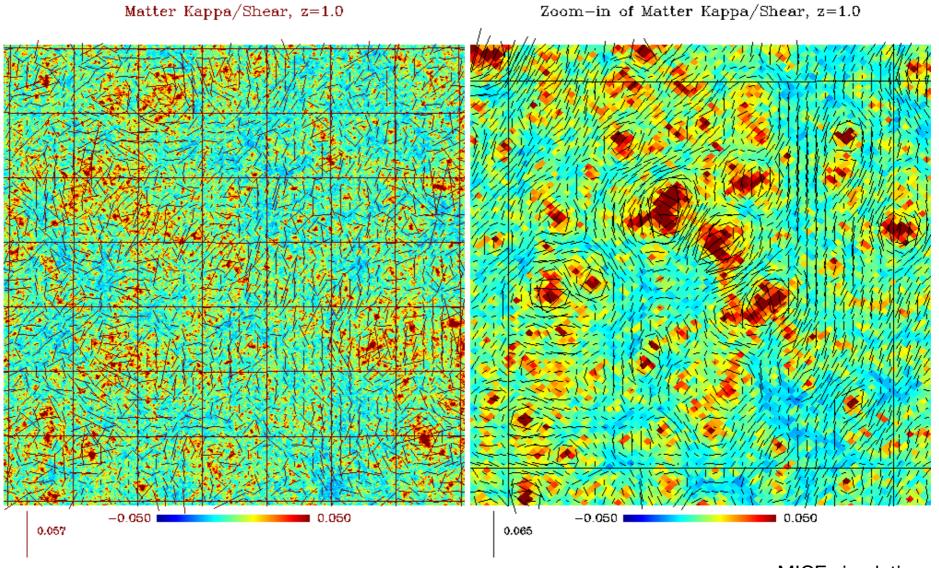


Measure the dispersion obtained by fitting halo model to observed dispersion in the Hubble diagram

$$\sigma_{\delta m} = 0.055z$$

Jonsson et al. 2010

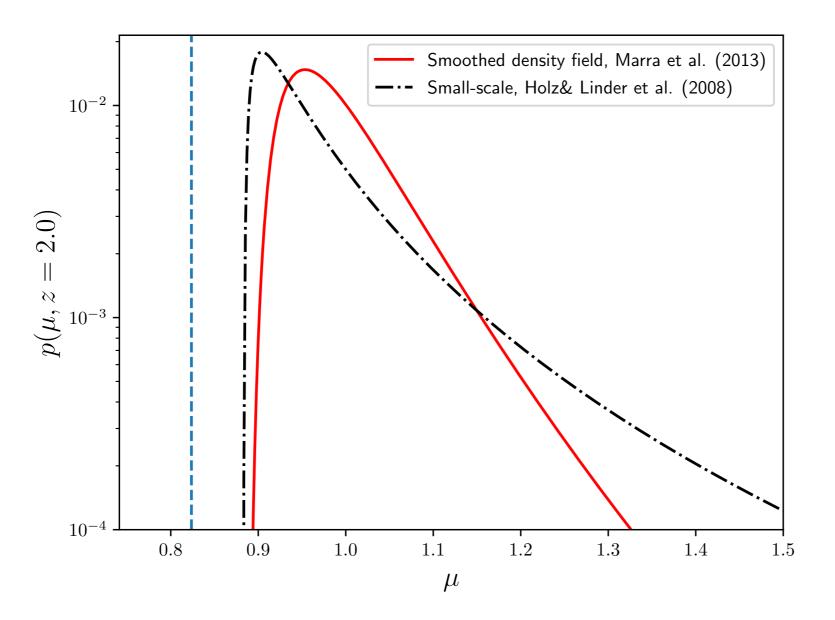
4) From N-body simulation light-cone



MICE simulations, Fosalba et al, 2014

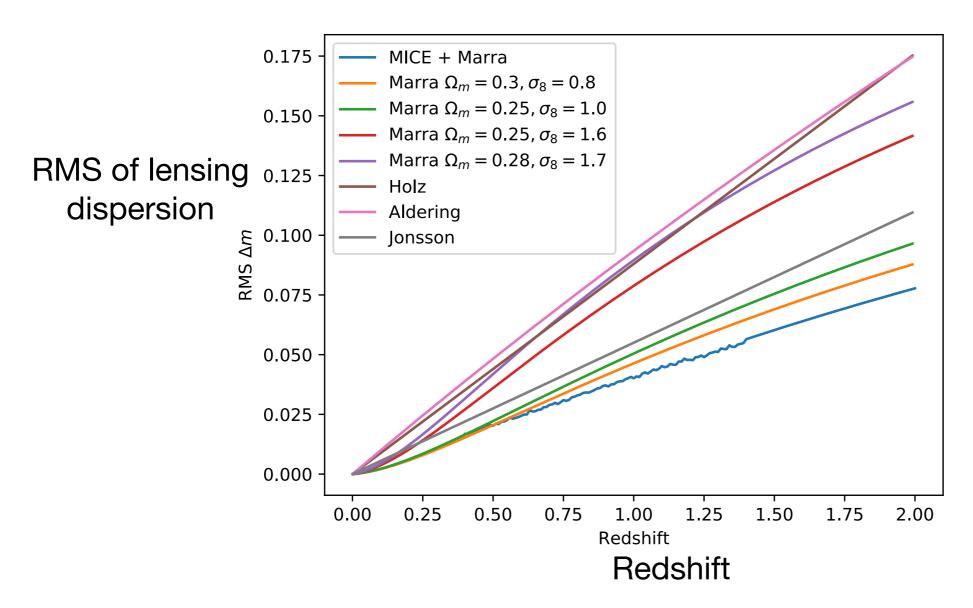
$$\kappa_i = \frac{3H_0^2\Omega_m}{2c^2} \sum_j \delta_{i,j} \frac{(r_{source} - r_j)r_j}{r_s a_j} dr_j$$

Different predictions for LSS effect on lensing probabilities

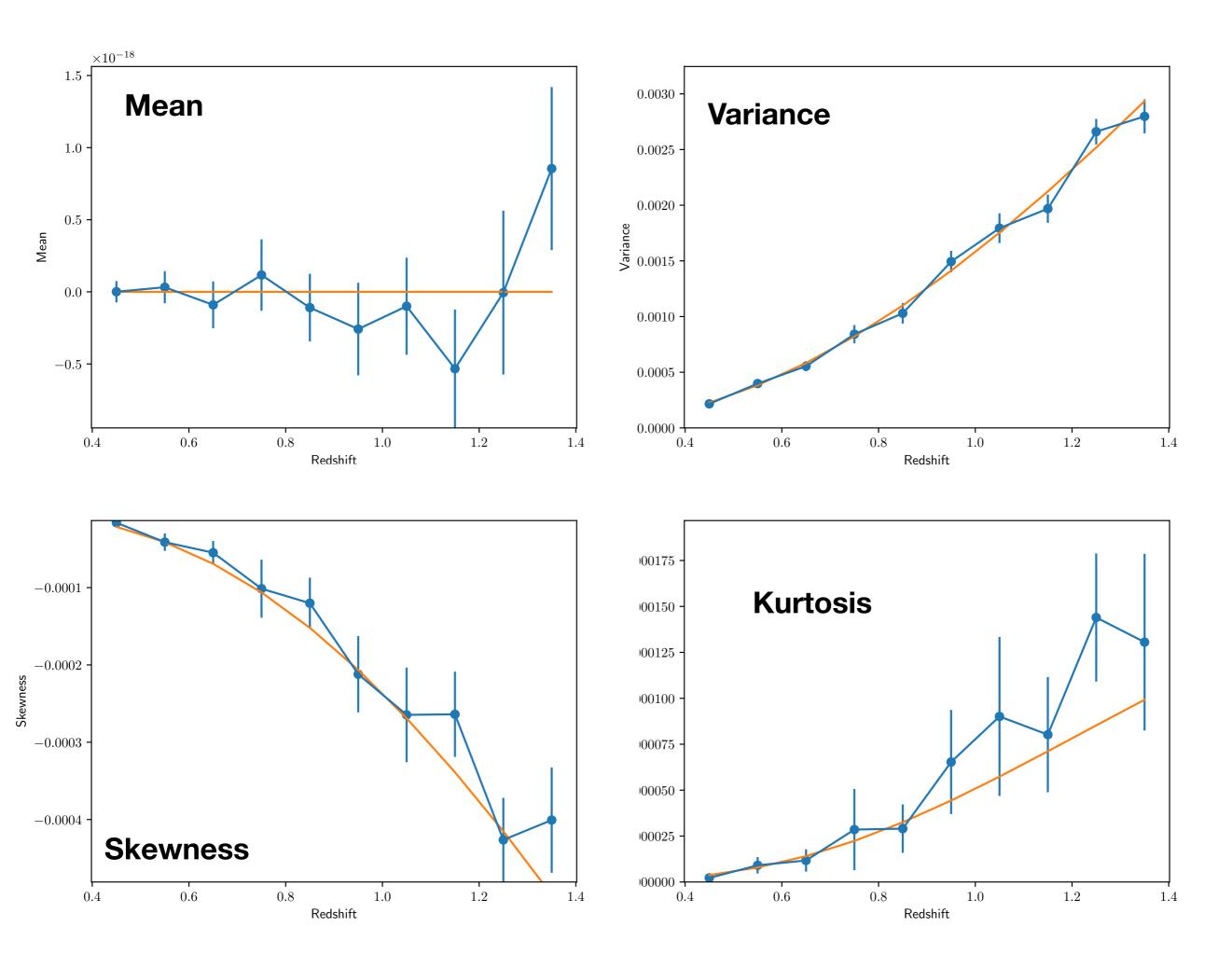


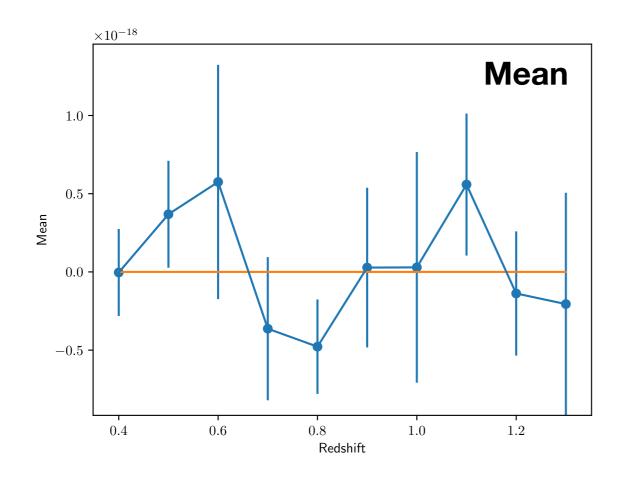
Lensing magnification

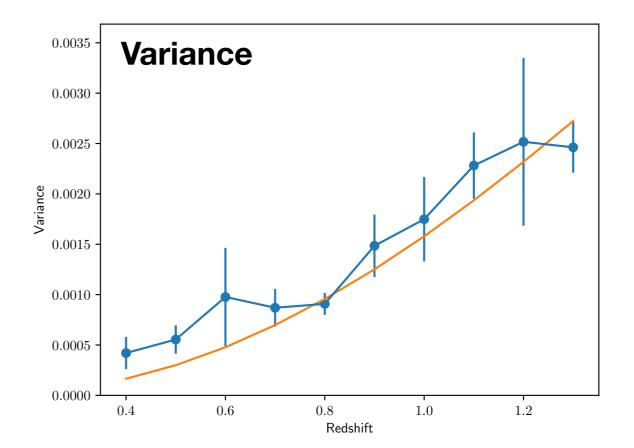
Different predictions for LSS effect on lensing probabilities

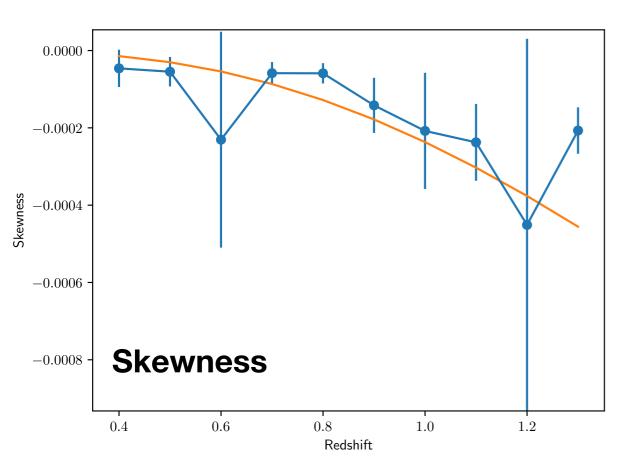


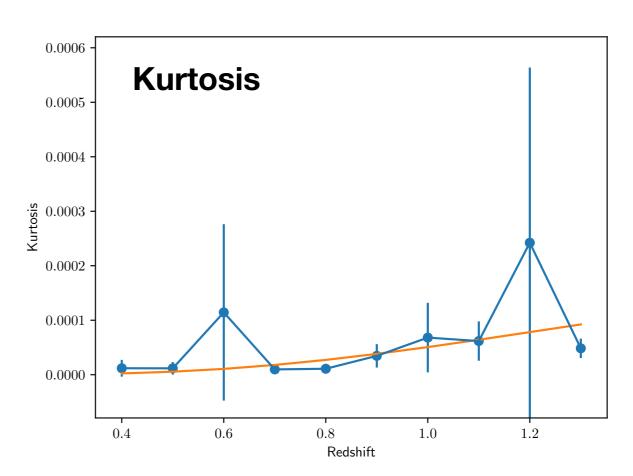
Differences between models up to a factor of 2.



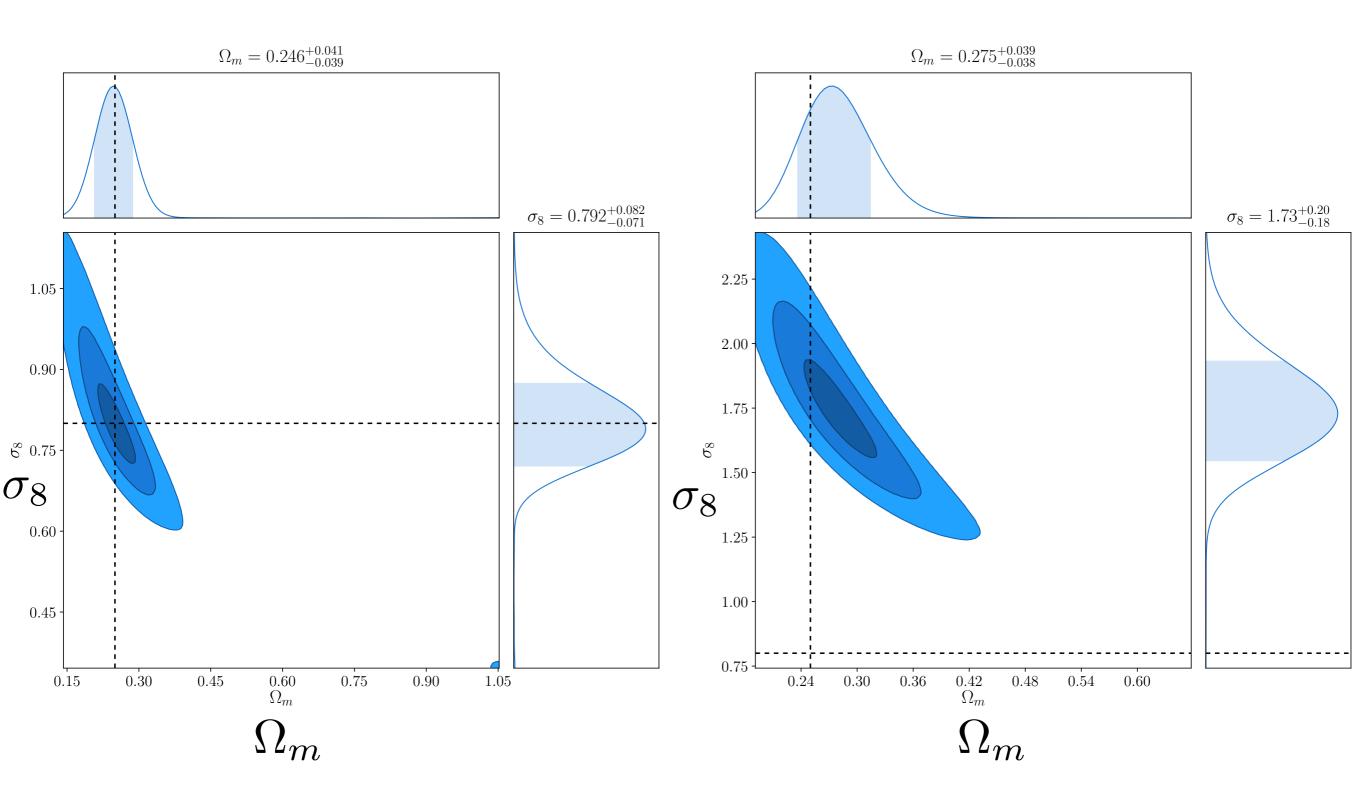




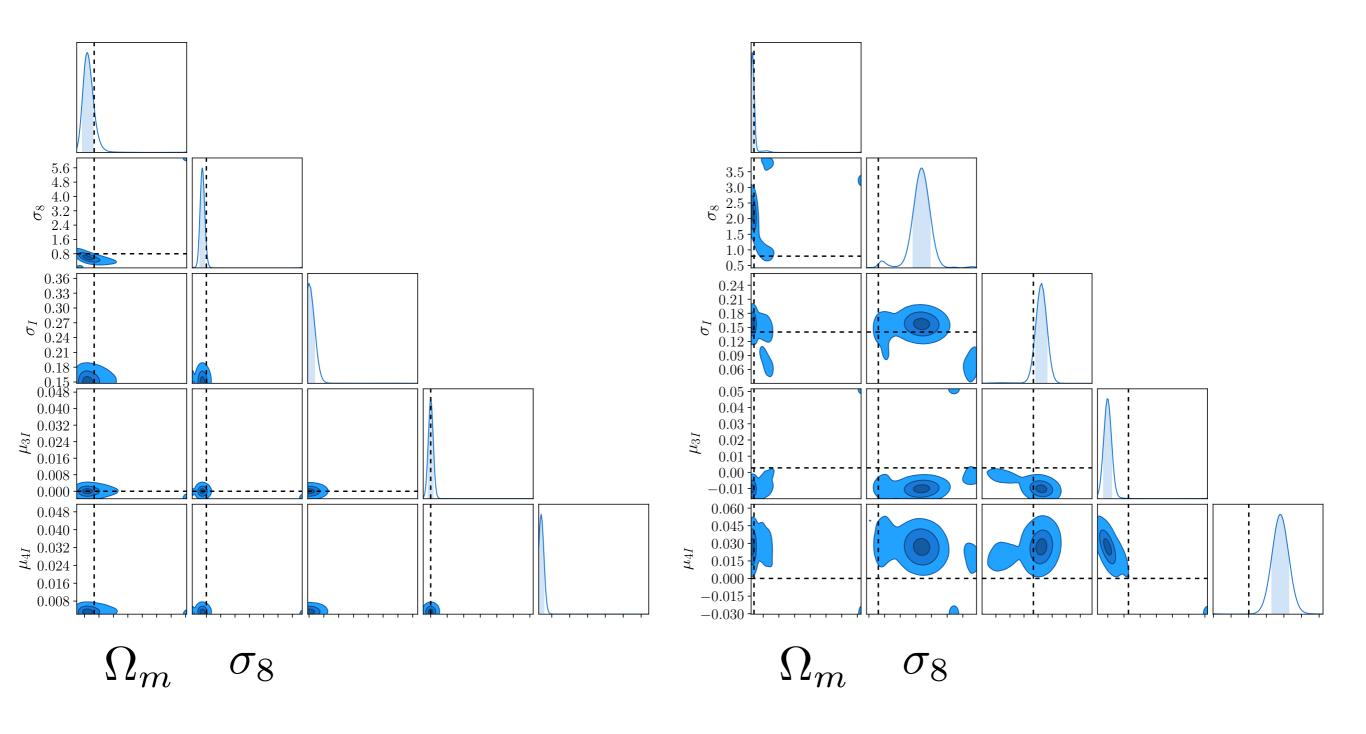




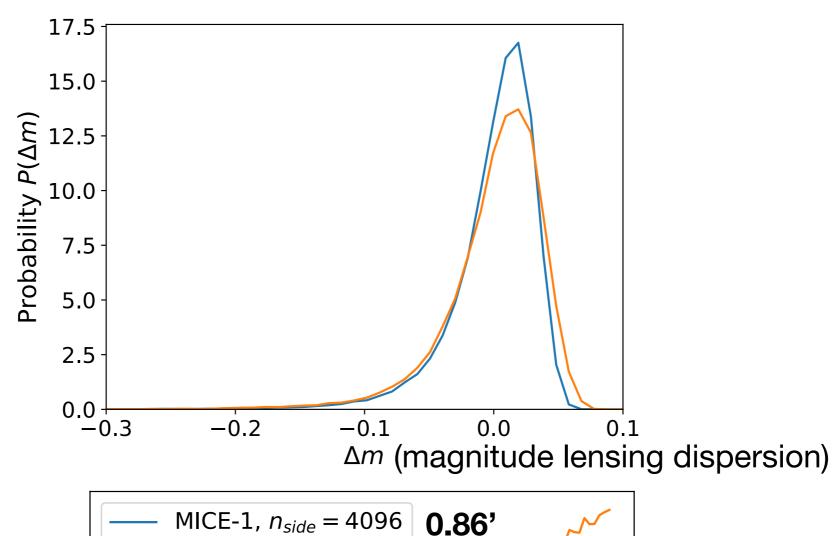
Effect on cosmological parameters

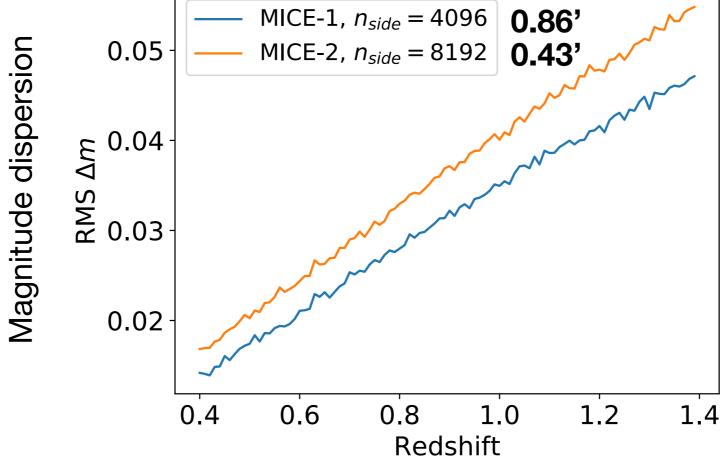


Effect on cosmological parameters



Effect of smoothing scale





Skewness in the magnitude error distribution

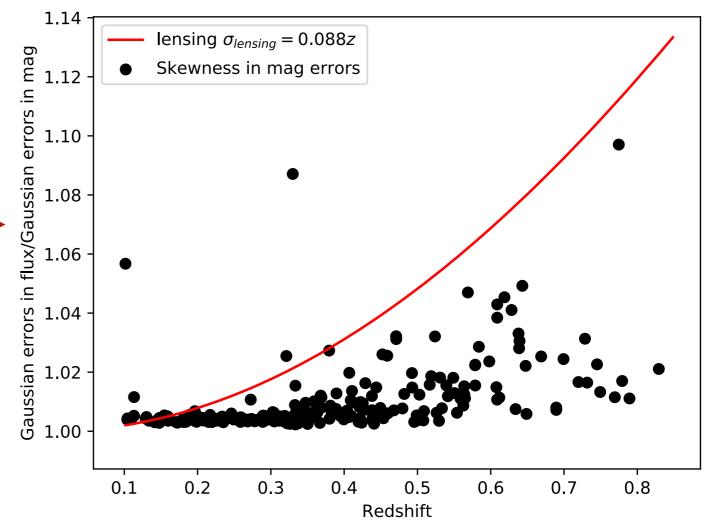
We transform the JLA mag error, assuming is Symmetric (gaussian) to asymmetric values in flux for the 1-sigma confidence interval.

$$m - m_{ref} = -2.5 \log_{10} \left(\frac{f}{f_{ref}} \right)$$

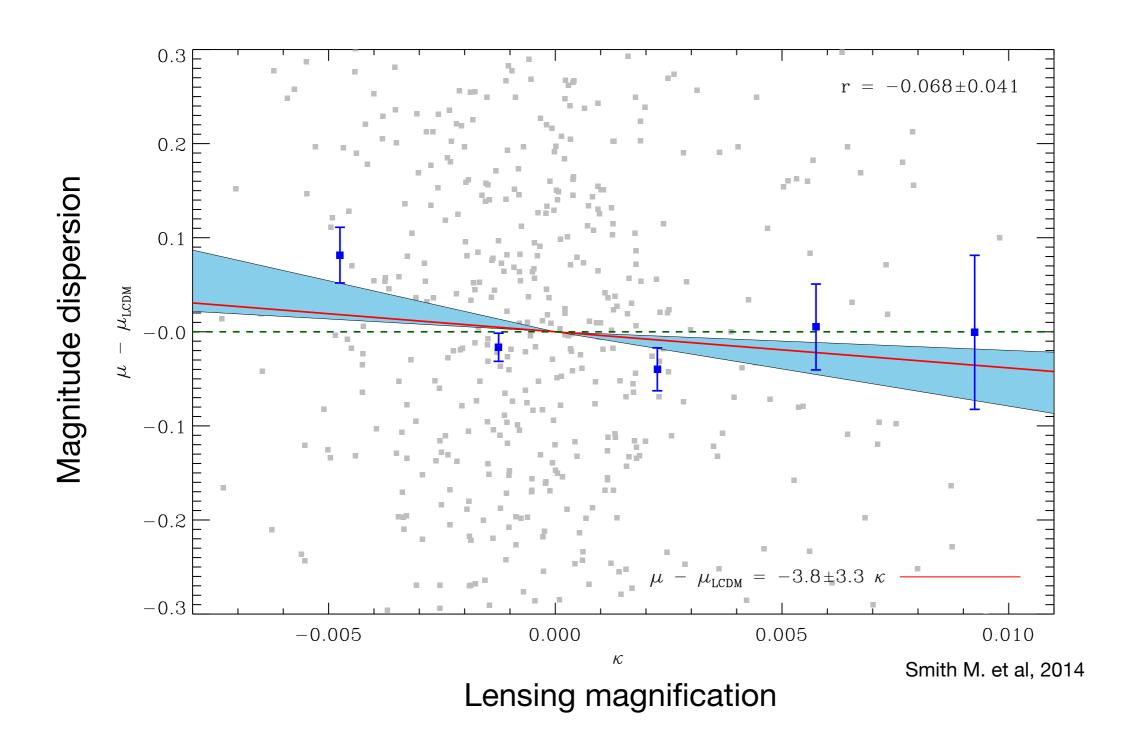
We assume the flux values should be symmetrical and then we transform back to asymmetric values in magnitude. We estimate the width of the confidence interval

Compare with original estimation for the error and the expected lensing error from Holz & Linder

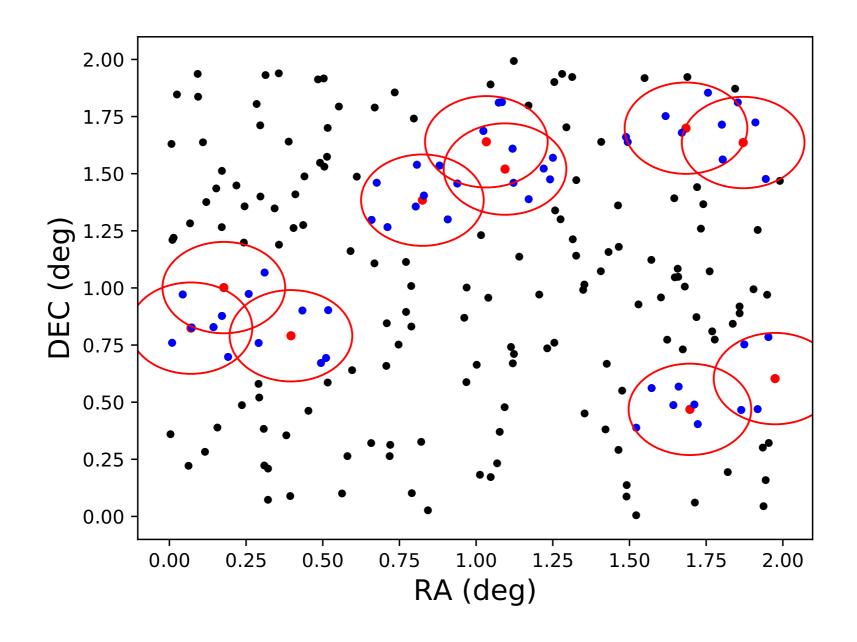
If the mag errors PDF is skewed then the errors increase, but below the lensing effect.



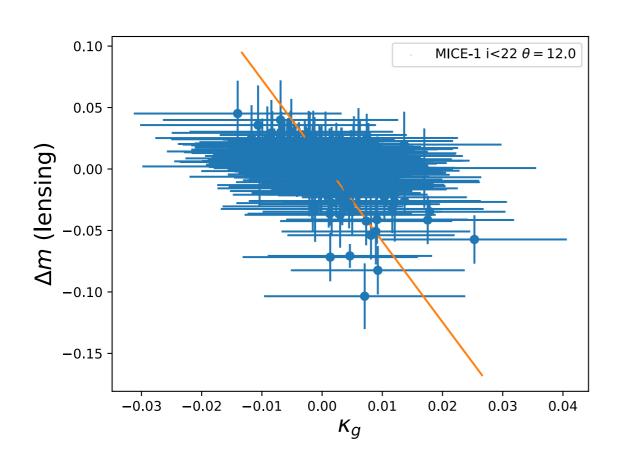
Cross-correlation magnitude-lensing

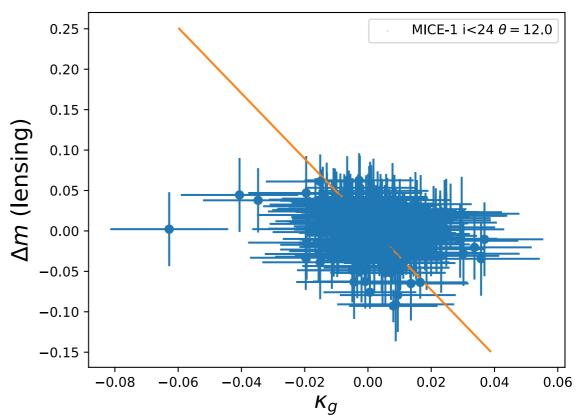


Magnification measurements



Mock catalogues correlation





$$\kappa_{g_i} = \frac{3H_0^2 \Omega_m}{2c^2} \sum_j \delta_{g_{i,j}} \frac{(r_s - r_j)r_j}{r_s a_j} dr_j$$

$$\mu = m_b - (M_b - \alpha x_1 + \beta c) - \frac{5}{\ln 10b_g} \kappa_g$$

Galaxy bias not well recovered

$$b_{g,BF}(i < 22) = 0.33 \pm 0.54,$$

$$b_{g,BF}(i < 24) = 0.54 \pm 0.80$$

Conclusions & Outlook

- Supernova brightness is affected by gravitational lensing. The relevance of this effect increases with redshift. The effect of small-scale clustering on the type Ia SN lensing is important and cannot be neglected. Include different set of 4-moments and smoothing scales in the analysis.
- We need to develop ray-tracing simulations that include the properties
 of compact structures along the line of sight to define the theoretical
 model for the lensing PDFs.
- Alternative is to measure direct correlation between the dispersion in the Hubble diagram and lensing maps. If using density fields to reconstruct magnification we must find a better estimator for magnification.
- Other systematics adding intrinsic skewness may affect the lensing detection.

Thank you! 감사합니다