Composite dark axions and light dark baryons

Deog Ki Hong

Pusan National University, Busan, Korea

August 28, 2018

COSMO 2018, Daejeon, Korea

Based on arXiv:1808.xxxxx

Introduction Introduction

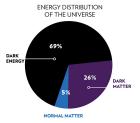
A model for light DM and DR

Dark Matter Paradigms

▶ Most stuffs in the universe are dark. (Planck 2018)



Figure: HST



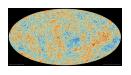


Figure: Planck 2018

- ▶ DM has about 5 times the mass density of baryons.
- ▶ Dark but massive (m = ???)



Figure: Megering galaxy clusters (Abell 520)

- Can't interact too strongly with QED and QCD.
- Doesn't interact too strongly with itself

- ▶ DM has about 5 times the mass density of baryons.
- ▶ Dark but massive (m =???)



Figure: Megering galaxy clusters (Abell 520)

- Can't interact too strongly with QED and QCD.
- Doesn't interact too strongly with itself.

- ▶ DM has about 5 times the mass density of baryons.
- ▶ Dark but massive (m =???)



Figure: Megering galaxy clusters (Abell 520)

- Can't interact too strongly with QED and QCD.
- Doesn't interact too strongly with itself.

- ▶ DM has about 5 times the mass density of baryons.
- ▶ Dark but massive (m =???)

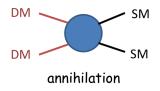


Figure: Megering galaxy clusters (Abell 520)

- Can't interact too strongly with QED and QCD.
- Doesn't interact too strongly with itself.

WIMP miracle

▶ Weakly interacting massive particles (Lee+Weinberg, 1977)



$$\langle \sigma \, \mathbf{v} \rangle = \frac{\alpha^2}{m_{\mathrm{DM}}^2}$$
 $m_{\mathrm{DM}} \sim 100 \; \mathrm{GeV}$

WIMP DM for last 40 years

Searching for WIMPs

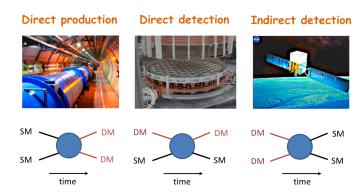
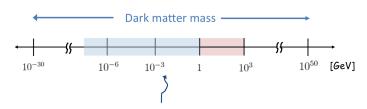


Figure: Hochberg at CERN BSM 2018

Openning windows for DM

Beyond the WIMP



Lots of activity in recent years:

Theory & Experiment

A model for Multi-component DM and DR (DKH 2018)

Consider SU(5) gauge theory with dark quarks in mixed representations.

	SU(5)	$SU(2)^f$	$SU(2)^{as}$	$\mathrm{U}(1)_B$	$\mathrm{U}(1)_{\mathcal{A}}$	$\mathrm{U}(1)_{\mathrm{em}}$
q_i^a			1	1/5	q_f	2/5
Q_{ij}^{α}		1		2/5	q_{as}	-1/5
χ^{a}	$\overline{1}$		1	1	q_f+2q_{as}	0

▶ The model has $G_f \otimes G_{as}$ chiral symmetries

$$G_f = \mathrm{SU}(2)_L^f \otimes \mathrm{SU}(2)_R^f, \quad G_{as} = \mathrm{SU}(2)_L^{as} \otimes \mathrm{SU}(2)_R^{as}$$

A model for Multi-component DM and DR (DKH 2018)

Consider SU(5) gauge theory with dark quarks in mixed representations.

	SU(5)	$SU(2)^f$	$SU(2)^{as}$	$\mathrm{U}(1)_B$	$\mathrm{U}(1)_A$	$\mathrm{U}(1)_{\mathrm{em}}$
q_i^a			1	1/5	q_f	2/5
Q_{ij}^{lpha}	H	1		2/5	q_{as}	-1/5
χ^{a}	$\overline{1}$		1	1	q_f+2q_{as}	0

▶ The model has $G_f \otimes G_{as}$ chiral symmetries:

$$G_f = \mathrm{SU}(2)_L^f \otimes \mathrm{SU}(2)_R^f, \quad G_{as} = \mathrm{SU}(2)_L^{as} \otimes \mathrm{SU}(2)_R^{as}$$

The chiral symmetry of decuplet Q_{ij}^{α} is spontaneously broken at $\Lambda \sim \text{confinement scale}$:

$$\left\langle Q_{\alpha} \bar{Q}_{\beta} \right\rangle = \Lambda^{3} \delta_{\alpha\beta}$$

 $\mathrm{SU}(2)_{L}^{as} \otimes \mathrm{SU}(2)_{R}^{as} \mapsto \mathrm{SU}(2)_{V}$,

- ▶ $U(1)_A$ is non-anomalous by construction and is spontaneously broken together with G_{as} .
- There are 4 Nambu-Goldstone bosons: π^A (A=1,2,3) and dark-axion a with mass, assuming $m_U \ll m_D$

$$m_a = rac{f_\pi m_\pi}{f_a/6} \cdot rac{\sqrt{m_U m_D}}{m_U + m_D} \ll m_\pi$$

The chiral symmetry of decuplet Q_{ij}^{α} is spontaneously broken at $\Lambda \sim \text{confinement scale}$:

$$\left\langle Q_{\alpha} \bar{Q}_{\beta} \right\rangle = \Lambda^{3} \delta_{\alpha\beta}$$

 $\mathrm{SU}(2)_{L}^{as} \otimes \mathrm{SU}(2)_{R}^{as} \mapsto \mathrm{SU}(2)_{V}$,

- ▶ $U(1)_A$ is non-anomalous by construction and is spontaneously broken together with G_{as} .
- ► There are 4 Nambu-Goldstone bosons: π^A (A = 1, 2, 3) and dark-axion a with mass, assuming $m_U \ll m_D$

$$m_a = rac{f_\pi m_\pi}{f_a/6} \cdot rac{\sqrt{m_U m_D}}{m_U + m_D} \ll m_\pi$$

The chiral symmetry of decuplet Q_{ij}^{α} is spontaneously broken at $\Lambda \sim \text{confinement scale}$:

$$\left\langle Q_{\alpha} \bar{Q}_{\beta} \right\rangle = \Lambda^{3} \delta_{\alpha\beta}$$

 $\mathrm{SU}(2)_{L}^{as} \otimes \mathrm{SU}(2)_{R}^{as} \mapsto \mathrm{SU}(2)_{V}$,

- ▶ $U(1)_A$ is non-anomalous by construction and is spontaneously broken together with G_{as} .
- ► There are 4 Nambu-Goldstone bosons: π^A (A = 1, 2, 3) and dark-axion a with mass, assuming $m_U \ll m_D$

$$m_a = \frac{f_\pi m_\pi}{f_a/6} \cdot \frac{\sqrt{m_U m_D}}{m_U + m_D} \ll m_\pi$$
.

Dark axion decays into two photons:

$$\mathcal{L}_{a\gamma\gamma} = rac{c_{\gamma}}{32\pi^2} \cdot rac{6a}{f_a} \, F_{\mu
u} ilde{F}^{\mu
u} \, ,$$

Life time of dark axions, $g_{a\gamma} = 216\alpha/5\pi f_a$:

$$\Gamma_{a \to \gamma \gamma} = \frac{g_{a \gamma}^2 m_a^3}{64 \pi} \simeq 5 \times 10^{-22} \,\mathrm{s}^{-1} \left(\frac{m_a}{10^{-3} \,\mathrm{eV}}\right)^3 \cdot \left(\frac{1 \,\mathrm{TeV}}{f_a}\right)^2$$

- ► The dark-axions with $m_a < 1.6 \times 10^{-2} \text{ eV}$ live longer than the age of the universe for $f_a = 1 \text{ TeV}$.
- Since they couple to SM particles at one-loop, unless $m_a > \mathcal{O}(1)$ keV, from the stellar cooling constraints

$$f_a \sim \Lambda > 3 \times 10^5 \text{ GeV}$$

Dark axion decays into two photons:

$$\mathcal{L}_{a\gamma\gamma} = rac{c_{\gamma}}{32\pi^2} \cdot rac{6a}{f_a} F_{\mu
u} ilde{F}^{\mu
u} \,,$$

• Life time of dark axions, $g_{a\gamma} = 216\alpha/5\pi f_a$:

$$\Gamma_{a\to\gamma\gamma} = \frac{g_{a\gamma}^2 m_a^3}{64\pi} \simeq 5 \times 10^{-22} \,\mathrm{s}^{-1} \left(\frac{m_a}{10^{-3} \,\mathrm{eV}}\right)^3 \cdot \left(\frac{1 \,\mathrm{TeV}}{f_a}\right)^2 \,,$$

- ► The dark-axions with $m_a < 1.6 \times 10^{-2} \text{ eV}$ live longer than the age of the universe for $f_a = 1 \text{ TeV}$.
- Since they couple to SM particles at one-loop, unless $m_a > \mathcal{O}(1)$ keV, from the stellar cooling constraints

$$f_a \sim \Lambda > 3 \times 10^5 \text{ GeV}$$

Dark axion decays into two photons:

$$\mathcal{L}_{a\gamma\gamma} = rac{c_{\gamma}}{32\pi^2} \cdot rac{6a}{f_a} \, F_{\mu
u} ilde{F}^{\mu
u} \, ,$$

Life time of dark axions, $g_{a\gamma}=216\alpha/5\pi f_a$:

$$\Gamma_{a\to\gamma\gamma} = \frac{g_{a\gamma}^2 m_a^3}{64\pi} \simeq 5 \times 10^{-22} \,\mathrm{s}^{-1} \left(\frac{m_a}{10^{-3} \,\mathrm{eV}}\right)^3 \cdot \left(\frac{1 \,\mathrm{TeV}}{f_a}\right)^2 \,,$$

- ► The dark-axions with $m_a < 1.6 \times 10^{-2} \text{ eV}$ live longer than the age of the universe for $f_a = 1 \text{ TeV}$.
- Since they couple to SM particles at one-loop, unless $m_a > \mathcal{O}(1)$ keV, from the stellar cooling constraints

$$f_a \sim \Lambda > 3 \times 10^5 \text{ GeV}$$

Dark axion decays into two photons:

$$\mathcal{L}_{a\gamma\gamma} = rac{c_{\gamma}}{32\pi^2} \cdot rac{6a}{f_a} \, F_{\mu
u} ilde{F}^{\mu
u} \, ,$$

Life time of dark axions, $g_{a\gamma}=216\alpha/5\pi f_a$:

$$\Gamma_{a\to\gamma\gamma} = \frac{g_{a\gamma}^2 m_a^3}{64\pi} \simeq 5 \times 10^{-22} \, \mathrm{s}^{-1} \left(\frac{m_a}{10^{-3} \, \mathrm{eV}}\right)^3 \cdot \left(\frac{1 \, \mathrm{TeV}}{f_a}\right)^2 \,,$$

- ► The dark-axions with $m_a < 1.6 \times 10^{-2} \text{ eV}$ live longer than the age of the universe for $f_a = 1 \text{ TeV}$.
- Since they couple to SM particles at one-loop, unless $m_a > \mathcal{O}(1) \text{ keV}$, from the stellar cooling constraints

$$f_a \sim \Lambda > 3 \times 10^5 \text{ GeV}$$
,

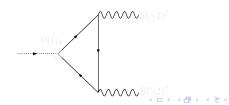
Light dark baryons

- The chiral symmetry of q_i^{α} is NOT spontaneously broken, however, by 't Hooft anomaly matching.
- The flavor anomalies of q_i^{α} is saturated in IR by massless spin 1/2 chimera baryons:

$$\chi^{a}\sim\epsilon_{lphaeta}{f q}_{f i}^{a}{f Q}_{f jk}^{lpha}{f Q}_{f lm}^{eta}\epsilon^{ijklm}$$
 .

► The coefficients of the UV and IR anomalies match

$$A_{\mathrm{UV}}^{ab} = \frac{1}{5} \cdot 5 \operatorname{Tr} \left(\tau^a \tau^b \right), \quad A_{\mathrm{IR}}^{ab} = 1 \cdot \operatorname{Tr} \left(\tau^a \tau^b \right)$$



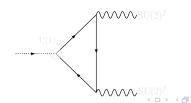
Light dark baryons

- The chiral symmetry of q_i^{α} is NOT spontaneously broken, however, by 't Hooft anomaly matching.
- The flavor anomalies of q_i^{α} is saturated in IR by massless spin 1/2 chimera baryons:

$$\chi^{a} \sim \epsilon_{\alpha\beta} q_{i}^{a} Q_{jk}^{\alpha} Q_{lm}^{\beta} \epsilon^{ijklm}$$
,

The coefficients of the UV and IR anomalies match

$$A_{\mathrm{UV}}^{ab} = \frac{1}{5} \cdot 5 \operatorname{Tr} \left(\tau^a \tau^b \right), \quad A_{\mathrm{IR}}^{ab} = 1 \cdot \operatorname{Tr} \left(\tau^a \tau^b \right)$$



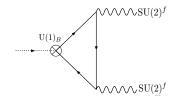
Light dark baryons

- The chiral symmetry of q_i^{α} is NOT spontaneously broken, however, by 't Hooft anomaly matching.
- The flavor anomalies of q_i^{α} is saturated in IR by massless spin 1/2 chimera baryons:

$$\chi^a \sim \epsilon_{\alpha\beta} q_i^a Q_{jk}^{\alpha} Q_{lm}^{\beta} \epsilon^{ijklm}$$
,

The coefficients of the UV and IR anomalies match,

$$A_{\mathrm{UV}}^{ab} = rac{1}{5} \cdot 5 \operatorname{Tr} \left(au^a au^b
ight), \quad A_{\mathrm{IR}}^{ab} = 1 \cdot \operatorname{Tr} \left(au^a au^b
ight),$$



Mass and magnetic moment of chimera baryons

Dark (chimera) baryons are massless in the chiral limit:

$$m_{\chi} \sim m_q \ll \Lambda$$

The dark-baryons are neutral but have magnetic dipole moment, μ_{χ} , when chiral symmetry is broken, $m_q \neq 0$:

$$\mu_{\chi} = g \frac{e}{2m_{\chi}}, \quad g = \kappa \frac{m_{\chi}^2}{\Lambda^2},$$

where $\kappa = \mathcal{O}(1)$.

Dark-baryons in our model belongs to dipolar DM but with naturally small magnetic moments.

Mass and magnetic moment of chimera baryons

Dark (chimera) baryons are massless in the chiral limit:

$$m_{\chi} \sim m_q \ll \Lambda$$

The dark-baryons are neutral but have magnetic dipole moment, μ_{χ} , when chiral symmetry is broken, $m_q \neq 0$:

$$\mu_{\chi} = g \frac{e}{2m_{\chi}}, \quad g = \kappa \frac{m_{\chi}^2}{\Lambda^2},$$

where
$$\kappa = \mathcal{O}(1)$$
 .

Dark-baryons in our model belongs to dipolar DM but with naturally small magnetic moments.

Mass and magnetic moment of chimera baryons

Dark (chimera) baryons are massless in the chiral limit:

$$m_\chi \sim m_q \ll \Lambda$$

The dark-baryons are neutral but have magnetic dipole moment, μ_{χ} , when chiral symmetry is broken, $m_q \neq 0$:

$$\mu_{\chi} = g \frac{e}{2m_{\chi}}, \quad g = \kappa \frac{m_{\chi}^2}{\Lambda^2},$$

where $\kappa = \mathcal{O}(1)$.

Dark-baryons in our model belongs to dipolar DM but with naturally small magnetic moments.

Dark baryons as Dark radiation

- ▶ Up dark-baryon can be made very light or massless by taking $m_q = (m_u \approx 0, m_d)$.
- In the chiral limit the Pauli form factor $F_2(q^2) = 0$ and thus the magnetic dipole moment $\mu_{\chi} = F_2(0)$ vanishes:

$$\bar{u}_{\chi}(p')\left[\gamma^{\mu}F_{1}(q^{2})+\frac{i\sigma^{\mu\nu}q_{\nu}}{2m_{\chi}}F_{2}(q^{2})\right]u_{\chi}(p)$$

Very light dark-baryons still couple to SM particles, since the Dirac form factors $F_1(q^2) \neq 0$ though $F_1(0) = 0$:

$$\frac{e \, c_d}{\Lambda^2} \bar{\chi} \gamma_\mu \chi \partial_\nu F^{\mu\nu} \, ; \quad \frac{e^2 c_d}{\Lambda^2} \bar{\chi} \gamma^\mu \chi \, \bar{\psi}_e \gamma_\mu \psi_e$$



Dark baryons as Dark radiation

- ▶ Up dark-baryon can be made very light or massless by taking $m_q = (m_u \approx 0, m_d)$.
- In the chiral limit the Pauli form factor $F_2(q^2) = 0$ and thus the magnetic dipole moment $\mu_{\chi} = F_2(0)$ vanishes:

$$\bar{u}_{\chi}(p')\left[\gamma^{\mu}F_1(q^2)+\frac{i\sigma^{\mu\nu}q_{\nu}}{2m_{\chi}}F_2(q^2)\right]u_{\chi}(p).$$

Very light dark-baryons still couple to SM particles, since the Dirac form factors $F_1(q^2) \neq 0$ though $F_1(0) = 0$:

$$\frac{e\,c_d}{\Lambda^2}\bar{\chi}\gamma_\mu\chi\partial_\nu F^{\mu\nu}\,;\quad \frac{e^2c_d}{\Lambda^2}\bar{\chi}\gamma^\mu\chi\,\bar{\psi}_e\gamma_\mu\psi_e$$

Dark baryons as Dark radiation

- ▶ Up dark-baryon can be made very light or massless by taking $m_q = (m_u \approx 0, m_d)$.
- In the chiral limit the Pauli form factor $F_2(q^2) = 0$ and thus the magnetic dipole moment $\mu_{\chi} = F_2(0)$ vanishes:

$$\bar{u}_{\chi}(p')\left[\gamma^{\mu}F_1(q^2)+\frac{i\sigma^{\mu\nu}q_{\nu}}{2m_{\chi}}F_2(q^2)\right]u_{\chi}(p).$$

Very light dark-baryons still couple to SM particles, since the Dirac form factors $F_1(q^2) \neq 0$ though $F_1(0) = 0$:

$$\frac{e c_d}{\Lambda^2} \bar{\chi} \gamma_\mu \chi \partial_\nu F^{\mu\nu}; \quad \frac{e^2 c_d}{\Lambda^2} \bar{\chi} \gamma^\mu \chi \, \bar{\psi}_e \gamma_\mu \psi_e$$

Dark radiation

▶ The ratio of the interaction rate to the expansion rate

$$\frac{\Gamma_{int}}{H} \sim \frac{e^4 c_d^2 T^5 / \Lambda^2}{T^2 / m_{pl}} = \left(\frac{T}{T_\chi}\right)^3 ,$$

where the decoupling temperature of massless dark-baryons

$$T_{\chi} \simeq 0.06 \,\, \mathrm{GeV} \, \left(\frac{\sqrt{c_d} \, \Lambda}{1 \,\, \mathrm{GeV}} \right)^{4/3} \,.$$

The contribution from the massless dark-baryons to the radiation energy (g = 4)

$$\Delta N_{\mathrm{eff}} = \frac{13.56}{g_*^{s}(T_{\chi})^{4/3}} \cdot g \lesssim 0.12 \quad \text{for} \quad \Lambda \gtrsim 3 \text{ GeV}$$

Dark radiation

▶ The ratio of the interaction rate to the expansion rate

$$\frac{\Gamma_{int}}{H} \sim \frac{e^4 c_d^2 T^5 / \Lambda^2}{T^2 / m_{pl}} = \left(\frac{T}{T_\chi}\right)^3 \,,$$

where the decoupling temperature of massless dark-baryons

$$T_{\chi} \simeq 0.06 \,\, \mathrm{GeV} \, \left(\frac{\sqrt{c_d} \, \Lambda}{1 \,\, \mathrm{GeV}} \right)^{4/3} \,.$$

The contribution from the massless dark-baryons to the radiation energy (g = 4)

$$\Delta N_{\mathrm{eff}} = \frac{13.56}{g_*^s (T_{\chi})^{4/3}} \cdot g \lesssim 0.12 \quad \text{for} \quad \Lambda \gtrsim 3 \text{ GeV}.$$

Results of light Dark-baryon model

Our model accommodates dark radiation, light dark-baryons or very light dark-axions, which contribute significantly to relic density, depending on the confinement scale, Λ:

$$\Omega_m h^2 \sim 0.12, \quad \Delta N_{\rm eff} \sim 0.1$$

	$\Lambda = 1 - 10^{-2} \text{ TeV}$	$\Lambda = 200~{\rm MeV}$	$\Lambda \gtrsim 10^7~{ m GeV}$
χ_u	≈ 0	pprox 0	≈ 0
χ_{d}	$\sim 1-10^3~{ m MeV}$	10 eV	×
а	$\times (> \text{keV})$	$\times (> \text{keV})$	$\lesssim 10~{ m eV}$

Dark axion ad QCD axion

▶ If we identify $U(1)_A$ as the $U(1)_{PQ}$ Peccei-Quinn symmetry, the electroweak single PQ field of DFSZ model is then a composite field of decuplet dark-quarks:

$$\phi_{\rm PQ} \sim \bar{Q} Q$$
,.

The confining scale is then

$$\Lambda \sim f_{\rm PQ} \sim 10^9 - 10^{12} \; {
m GeV} \, .$$

lacktriangle The dark baryons are too weakly interacting, $g\sim m_\chi^2/\Lambda^2\ll 1$

Dark axion ad QCD axion

▶ If we identify $U(1)_A$ as the $U(1)_{PQ}$ Peccei-Quinn symmetry, the electroweak single PQ field of DFSZ model is then a composite field of decuplet dark-quarks:

$$\phi_{\rm PQ} \sim \bar{Q}Q$$
,.

► The confining scale is then

$$\Lambda \sim f_{\rm PQ} \sim 10^9 - 10^{12} \ {
m GeV} \, .$$

lacktriangle The dark baryons are too weakly interacting, $g\sim m_\chi^2/\Lambda^2\ll 1$

Dark axion ad QCD axion

If we identify $U(1)_A$ as the $U(1)_{PQ}$ Peccei-Quinn symmetry, the electroweak single PQ field of DFSZ model is then a composite field of decuplet dark-quarks:

$$\phi_{\rm PQ} \sim \bar{Q}Q$$
,.

► The confining scale is then

$$\Lambda \sim f_{\rm PQ} \sim 10^9 - 10^{12} \ {
m GeV} \, .$$

► The dark baryons are too weakly interacting, $g \sim m_{\chi}^2/\Lambda^2 \ll 1$.

- We propose a model for light DM and dark radiation, which has a light dark-baryons, very light dark-axions, and almost massless dark-baryon.
- ► The model supports massless spin 1/2 chimera baryons that saturate the flavor anomaly:

$$\chi^{a} \sim \epsilon_{lphaeta} q_{i}^{a} Q_{jk}^{lpha} Q_{lm}^{eta} \epsilon^{ijklm}$$

- Dark baryons are light or almost massless because of unbroken chiral symmetry.
- Dark baryons are neutral but carry a magnetic moment

$$u_{\chi} = g \frac{e}{2m_{\chi}}, \quad g \approx \left(\frac{m_{\chi}}{\Lambda}\right)^2.$$

- We propose a model for light DM and dark radiation, which has a light dark-baryons, very light dark-axions, and almost massless dark-baryon.
- ► The model supports massless spin 1/2 chimera baryons that saturate the flavor anomaly:

$$\chi^{a} \sim \epsilon_{\alpha\beta} q_{i}^{a} Q_{jk}^{\alpha} Q_{lm}^{\beta} \epsilon^{ijklm}$$
,

- Dark baryons are light or almost massless because of unbroken chiral symmetry.
- ▶ Dark baryons are neutral but carry a magnetic moment

$$\mu_{\chi} = g \frac{e}{2m_{\chi}}, \quad g \approx \left(\frac{m_{\chi}}{\Lambda}\right)^2.$$

- We propose a model for light DM and dark radiation, which has a light dark-baryons, very light dark-axions, and almost massless dark-baryon.
- ► The model supports massless spin 1/2 chimera baryons that saturate the flavor anomaly:

$$\chi^{\mathsf{a}} \sim \epsilon_{\alpha\beta} q_{\mathsf{i}}^{\mathsf{a}} Q_{\mathsf{j}k}^{\alpha} Q_{\mathsf{lm}}^{\beta} \epsilon^{\mathsf{i}\mathsf{j}\mathsf{k}\mathsf{lm}} \,,$$

- Dark baryons are light or almost massless because of unbroken chiral symmetry.
- Dark baryons are neutral but carry a magnetic moment,

$$\mu_{\chi} = g \frac{e}{2m_{\chi}}, \quad g \approx \left(\frac{m_{\chi}}{\Lambda}\right)^2.$$

- We propose a model for light DM and dark radiation, which has a light dark-baryons, very light dark-axions, and almost massless dark-baryon.
- ► The model supports massless spin 1/2 chimera baryons that saturate the flavor anomaly:

$$\chi^{a} \sim \epsilon_{\alpha\beta} q_{i}^{a} Q_{jk}^{\alpha} Q_{lm}^{\beta} \epsilon^{ijklm}$$
,

- Dark baryons are light or almost massless because of unbroken chiral symmetry.
- Dark baryons are neutral but carry a magnetic moment,

$$\mu_{\chi} = g \frac{e}{2m_{\chi}}, \quad g pprox \left(\frac{m_{\chi}}{\Lambda}\right)^2.$$

The model has a very light dark-axion,

$$m_a \lesssim 10 \ {\rm eV} \quad {\rm for} \quad \Lambda \gtrsim 10^7 \ {\rm GeV} \, .$$

The dark-axion becomes the QCD axion, solving the strong CP problem as in the DFSZ model, if we identify the electroweak singlet $\phi_{\rm PQ} \sim \bar{Q} Q$, which requires $\Lambda \sim f_{\rm PQ}$.

The model has a very light dark-axion,

$$m_a \lesssim 10 \text{ eV}$$
 for $\Lambda \gtrsim 10^7 \text{ GeV}$.

► The dark-axion becomes the QCD axion, solving the strong CP problem as in the DFSZ model, if we identify the electroweak singlet $\phi_{\rm PQ} \sim \bar{Q} Q$, which requires $\Lambda \sim f_{\rm PQ}$.