

# GRAVITATIONAL WAVES FROM VACUUM FIRST-ORDER PHASE TRANSITIONS

Cosmo 2018 - Daejeon

28<sup>th</sup> August 2018

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# INTRODUCTION

- First order phase transitions proceed through bubble nucleation and merger.
- Collision of bubble walls can source gravitational waves.
- In a vacuum transition bubble walls accelerate until collision.
  - i.e Fluid effects on wall minimal, behaves as if in a vacuum.
- Previous studies mostly use envelope approximation:
  - Stress-energy concentrated in infinitesimally thin shell at bubble wall.
  - Neglect overlap regions once bubbles have collided.

*[Kosowsky et al, 1992] [Huber and Konstandin, 2008][Weir, 2016] [Konstandin, 2017]*

## MOTIVATION

- LISA will be sensitive to gravitational waves from a first-order transition around the electroweak scale.
- Extensions to the Standard Model can generate a first order phase transition around the electroweak scale.
- Can probe BSM physics if we can characterise the GW signal.

## TOY MODEL

- Single real scalar field  $\phi(x, t)$  with potential as follows:

$$V(\phi) = \frac{1}{2}M^2\phi^2 + \frac{1}{3}\delta\phi^3 + \frac{1}{4}\lambda\phi^4.$$

- Vary parameters  $M^2, \delta, \lambda \rightarrow$  critical bubble radius  $R_c$ , and wall width  $l_0$ .
- The scalar field evolves according to:

$$\square\phi - V'(\phi) = 0.$$

- Then the energy momentum tensor is given by:

$$T_{\mu\nu} = \partial_\mu\phi\partial_\nu\phi - \eta_{\mu\nu} \left( \frac{1}{2}(\partial\phi)^2 + V(\phi) \right).$$



## GRAVITATIONAL WAVES

- Transverse traceless metric perturbation evolves as

$$\square h_{ij}^{TT} = 16\pi G T_{ij}^{TT}.$$

- $P_{\dot{h}}(\mathbf{k}, t)$  is the spectral density of the time derivative of  $h_{ij}^{TT}$ :

$$\langle \dot{h}_{ij}^{TT}(\mathbf{k}, t) \dot{h}_{ij}^{TT}(\mathbf{k}', t) \rangle = P_{\dot{h}}(\mathbf{k}, t) (2\pi)^3 \delta(\mathbf{k} + \mathbf{k}').$$

- Then the gravitational wave density parameter power spectrum is

$$\frac{d\Omega_{GW}}{d\ln(k)} = \frac{d\rho_{GW}}{d\ln(k)} \frac{1}{\rho_c} = \frac{1}{32\pi G \rho_c} \frac{k^3}{2\pi^2} P_{\dot{h}}(\mathbf{k}, t).$$

# INITIAL CONDITIONS

- Different nucleation scenarios:

- simultaneous
- constant nucleation rate

$$p(t) = p_c$$

- exponential nucleation rate

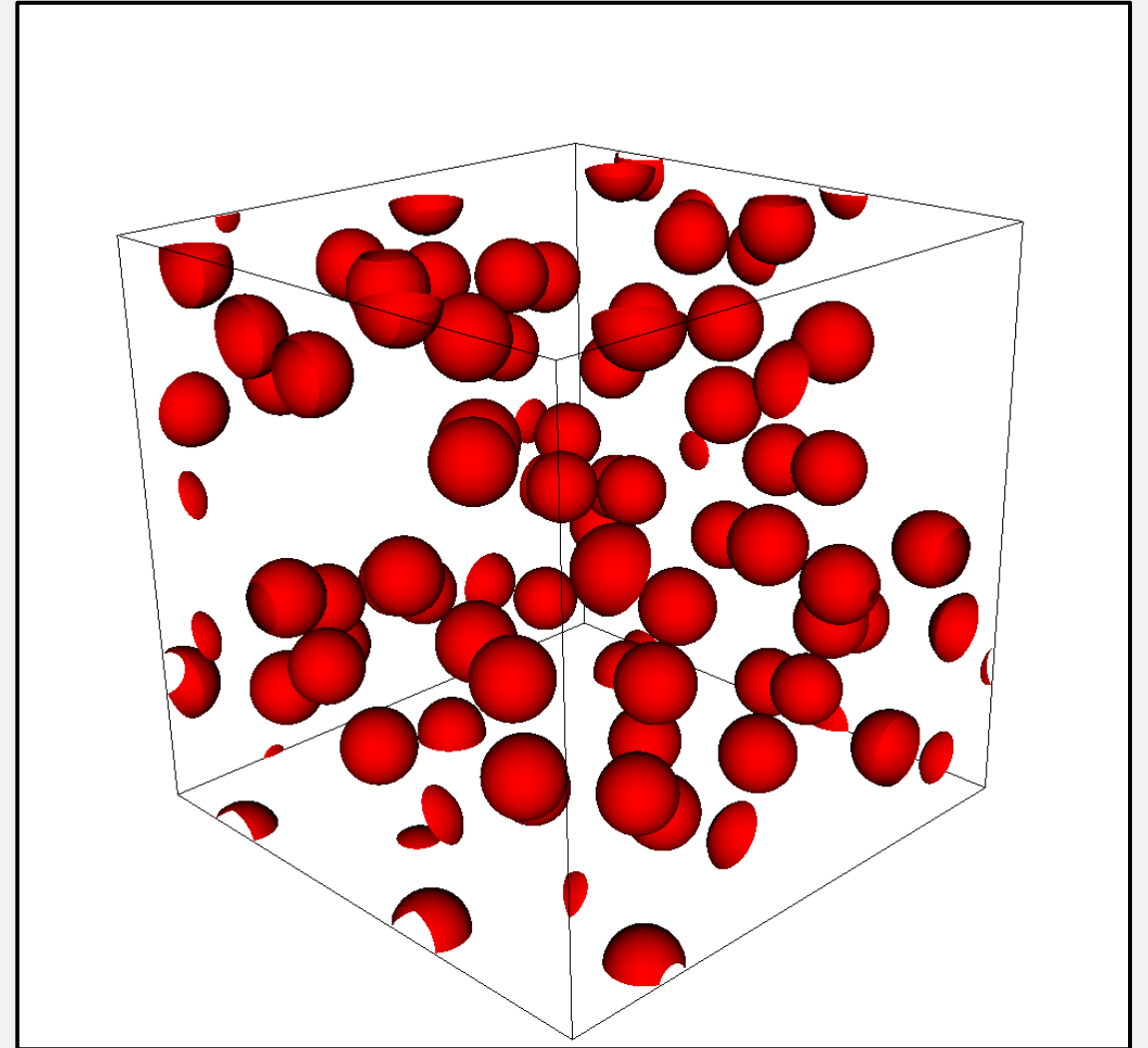
$$p(t) = p_0 \exp(\beta t)$$

- Mean bubble separation:

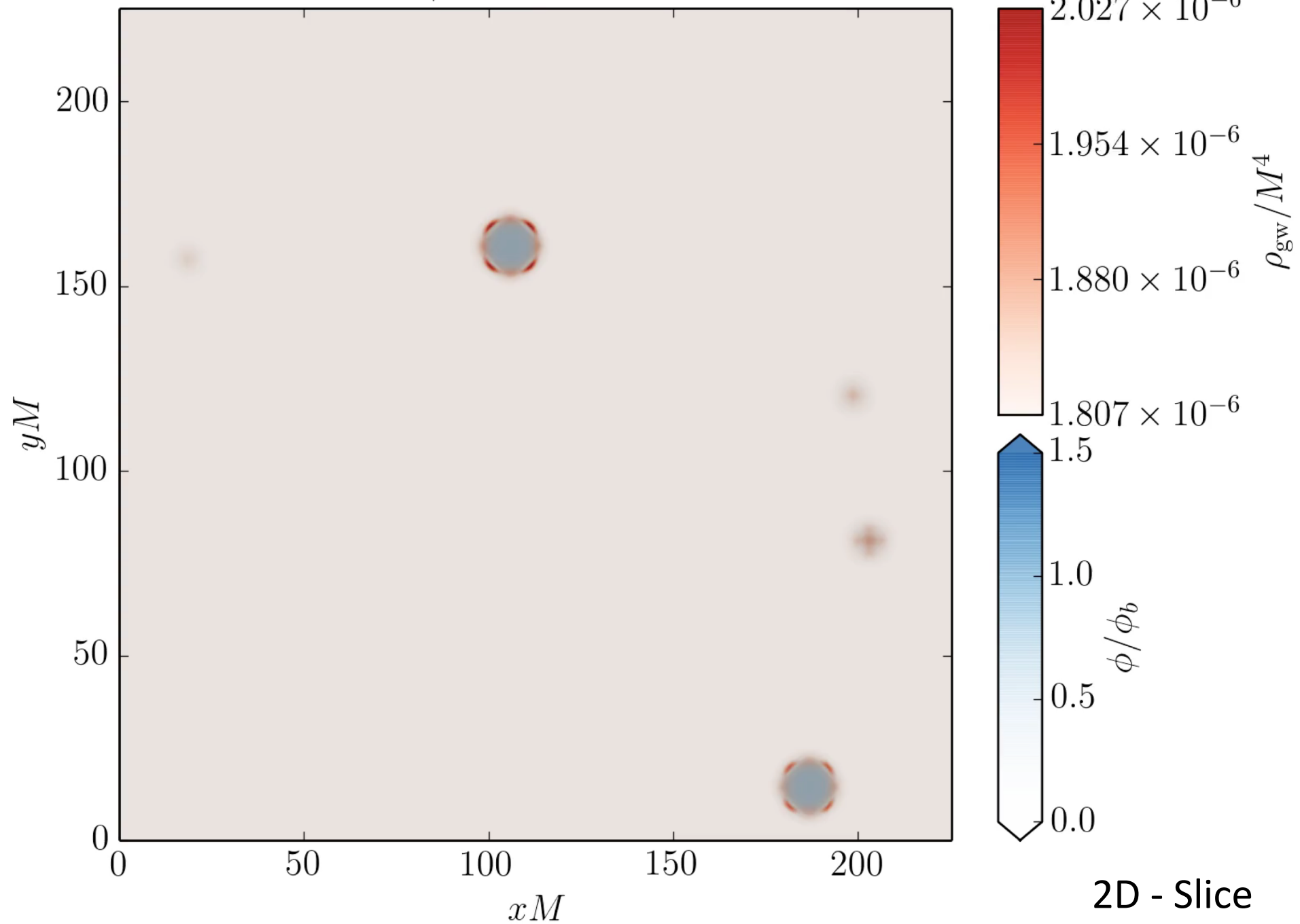
$$R_* = \left( \frac{V}{N_b} \right)^{1/3}$$

- Lorentz factor of bubble wall at collision given by

$$\gamma_* = \frac{1}{2} \frac{R_*}{R_c}.$$



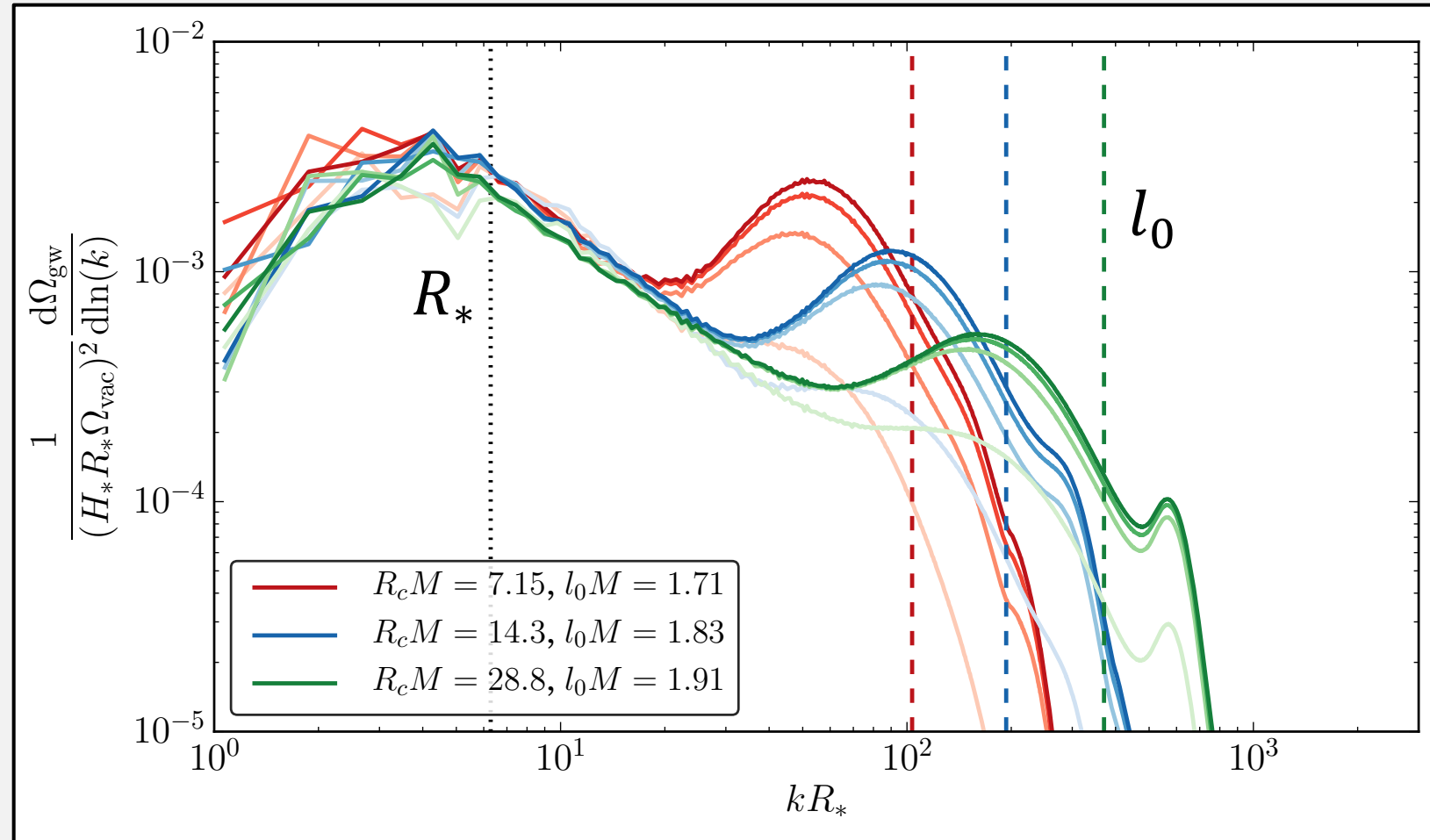
$$t/R_* = 0.00391$$



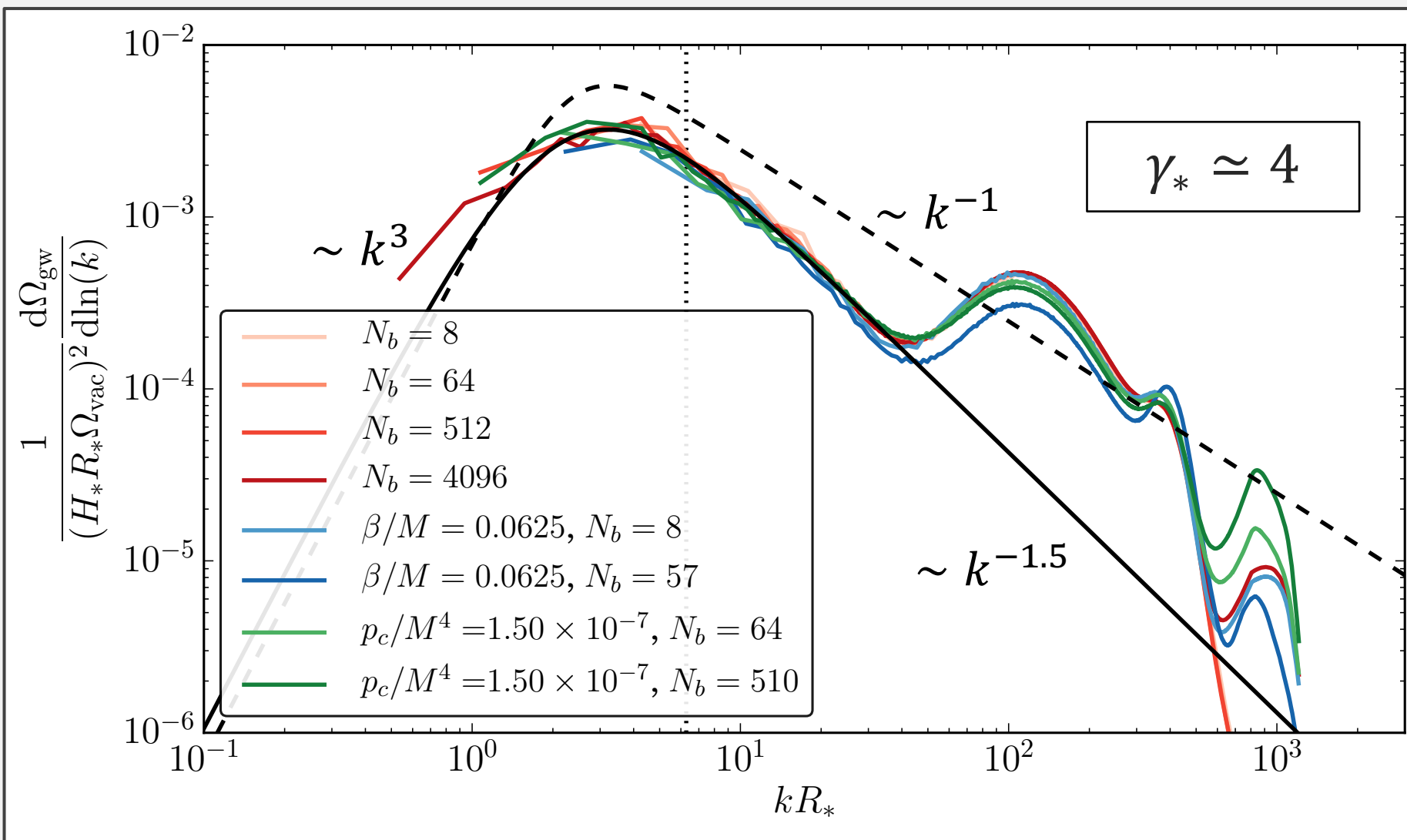
# PEAKS IN THE SPECTRUM

$$\gamma_* \simeq 2, N_b = 512$$

- Dual peak structure.
- IR peak scales with bubble radius (dotted line).
- UV peak scale set by wall width (coloured dashed lines).
- Most models have  $R_* \gg l_0$  and so UV peak suppressed.



# IR PEAK



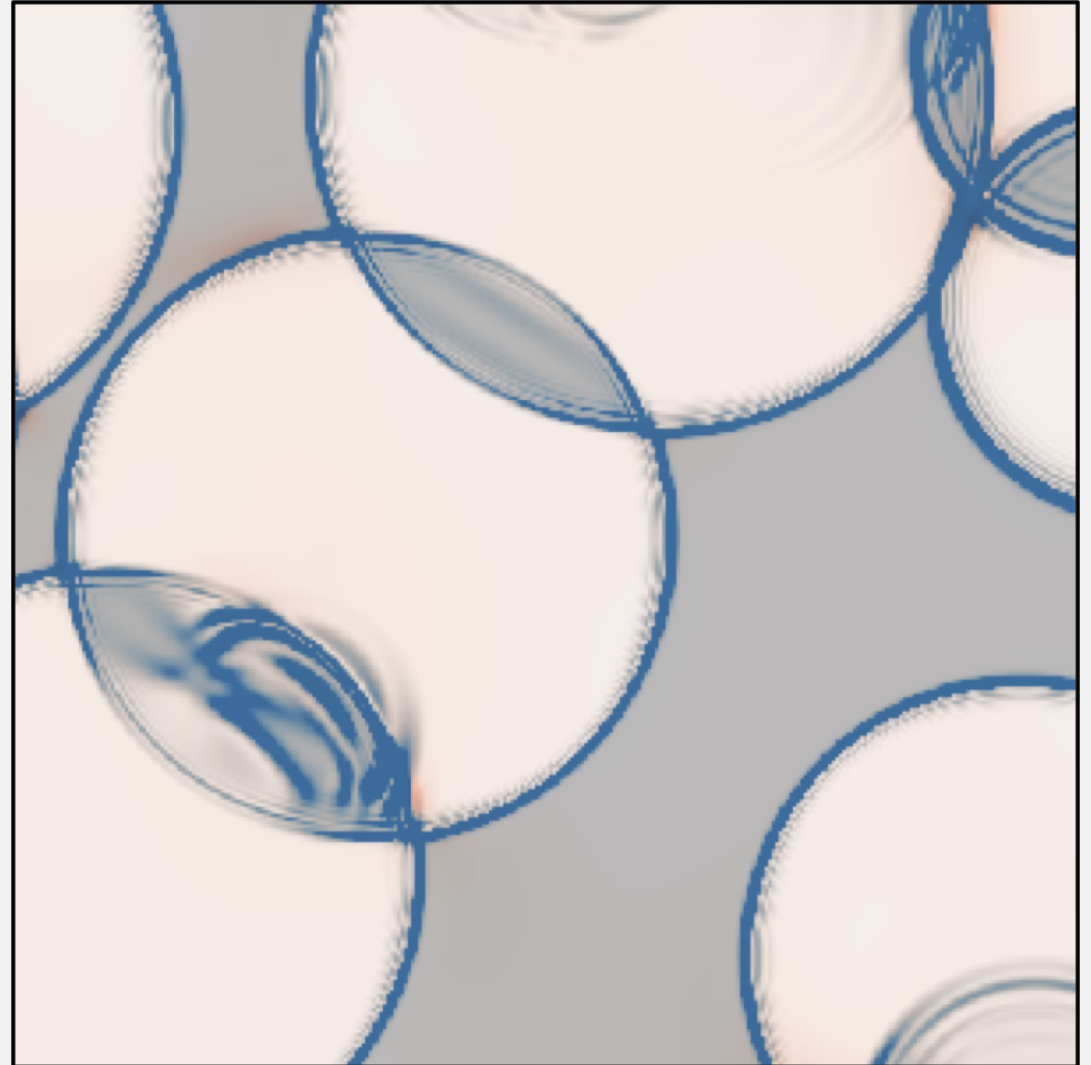
## CONCLUSIONS

- Peak gravitational wave power has approximate agreement with envelope approximation fit.
- Peak frequency agrees well with the envelope approximation.
- Power law steeper than envelope for large  $\gamma_*$ , with  $k^{-1.5}$  instead of  $k^{-1}$ .
- Second peak from scalar field oscillations found in UV.
- UV peak will have negligible contribution for most models.

# ENVELOPE APPROXIMATION

- Assumptions:
  - Stress-energy concentrated in infinitesimal thin shell.
  - Neglect any region where bubbles overlap.
- Broken power law:
  - Rises as  $k^3$  in IR.
  - Falls like  $k^{-1}$  towards UV.
  - Peak location and amplitude given by  $R_*$ .

*[Huber and Konstandin, 2008] [Konstandin, 2017]*



# UV PEAK GROWTH

- Linear growth of UV peak contribution to spectrum  $\Omega_{gw}^{osc}$ ,

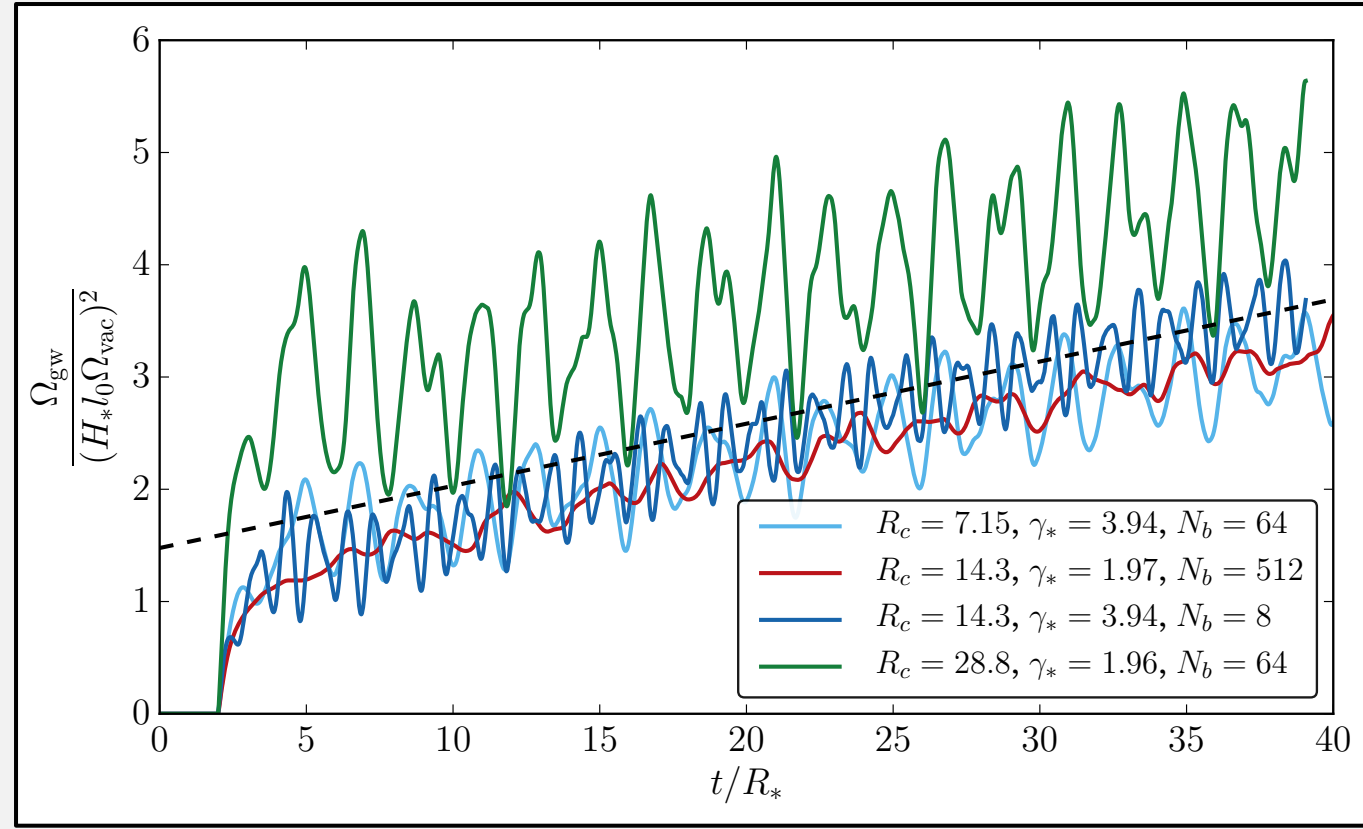
$$\frac{d\Omega_{gw}^{osc}}{dt} \sim 10^{-1} \frac{(H_* l_0 \Omega_{vac})^2}{R_*}.$$

- Contribution from the bubble collisions is

$$\Omega_{gw}^{coll} \sim 10^{-3} (H_* R_* \Omega_{vac})^2.$$

- Ratio of contributions:

$$\frac{\Omega_{gw}^{osc}}{\Omega_{gw}^{coll}} \lesssim 10 \frac{n_b}{H_*^3} \left( \frac{M_b}{m_{Pl}} \right)^2.$$

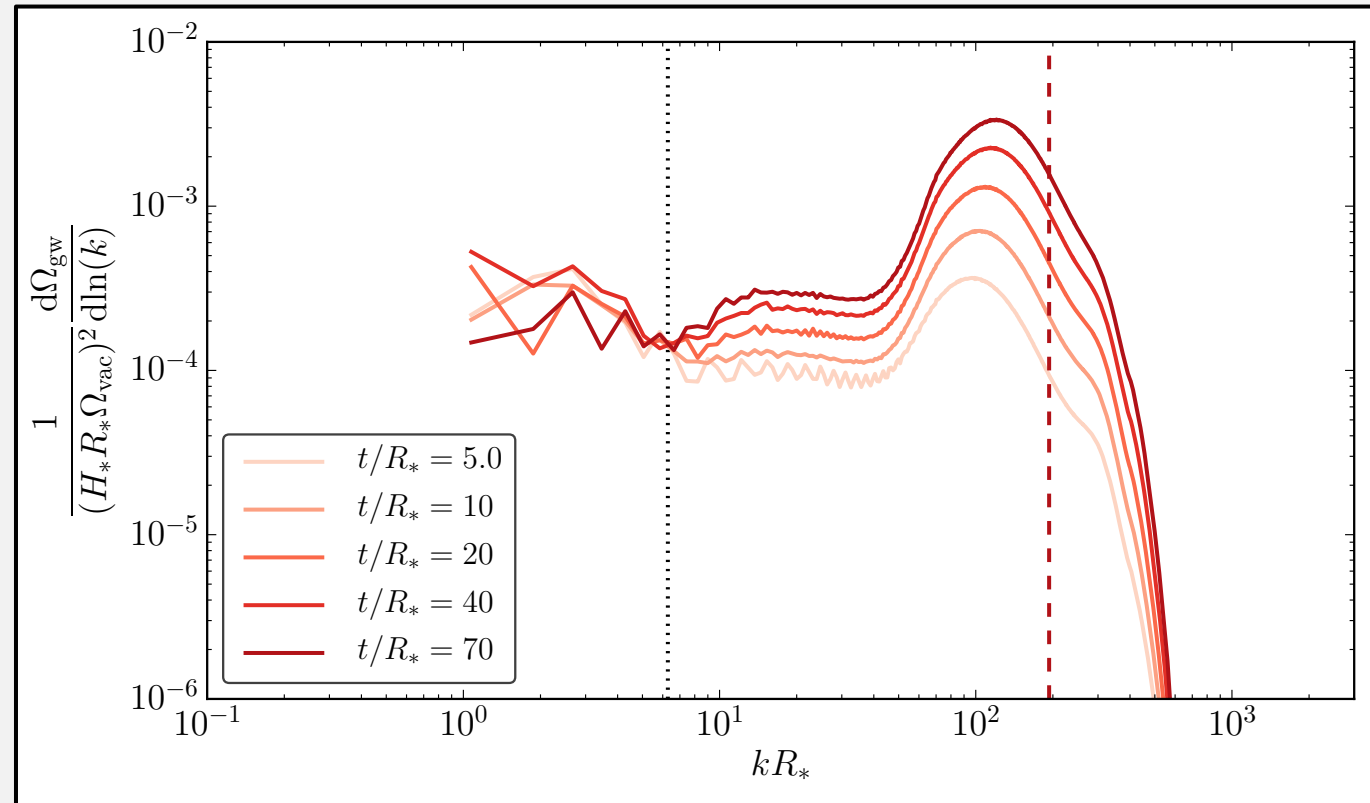




## UV PEAK

$$\gamma_* \simeq 4, N_b = 512$$

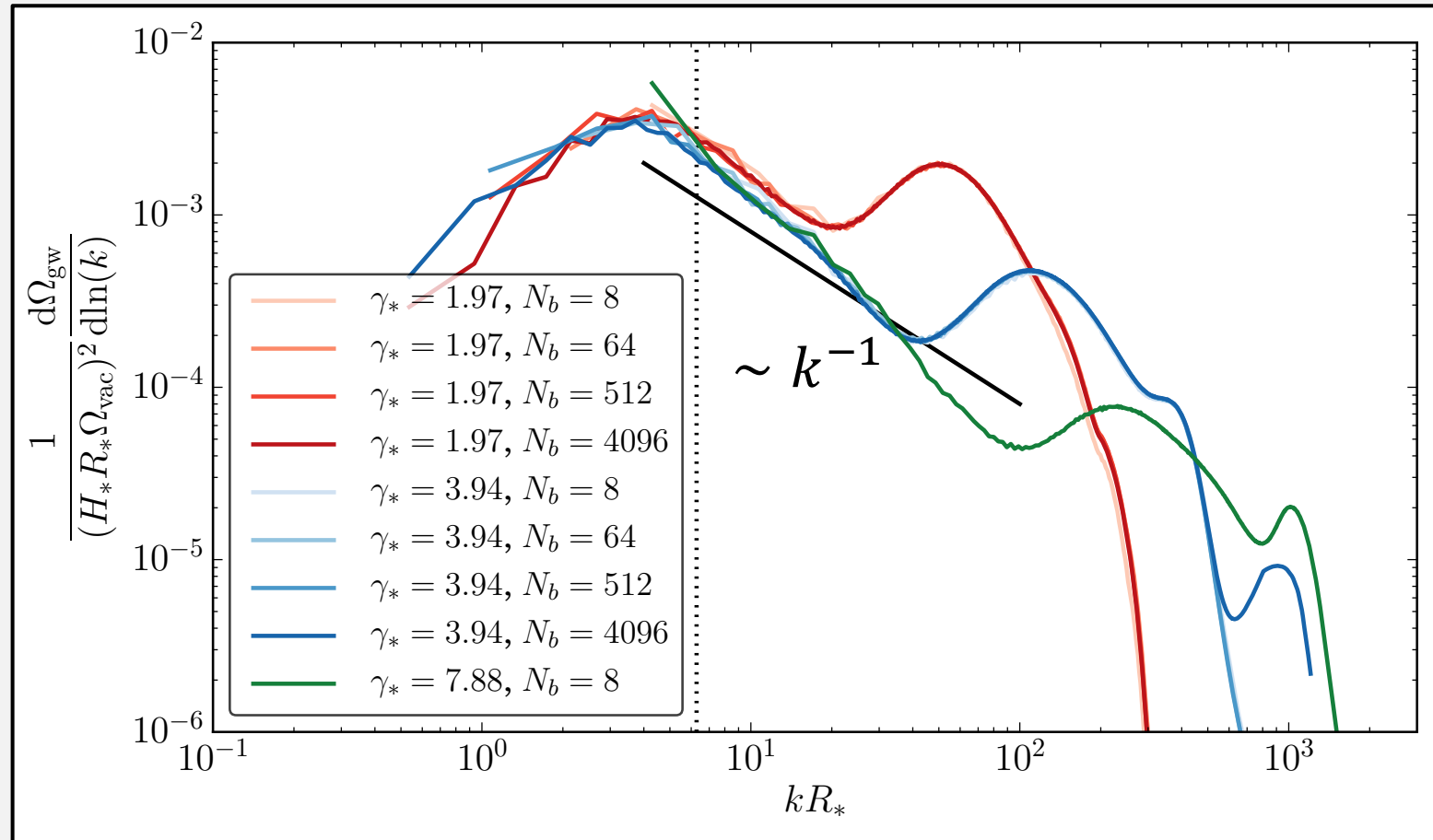
- Can turn off evolution of metric perturbations until bubbles finish colliding.
- Ringing in the IR for scales above  $R_*$ .
- UV peak continues to grow until late times.
- Growing plateau extending from  $R_*$  up until the UV peak.



# GAMMA DEPENDENCE

- IR peak dependence on  $\gamma_*$  only via  $R_*$
- Power law towards UV becomes steeper than  $k^{-1}$  for

$$\gamma_* \gtrsim 2.$$

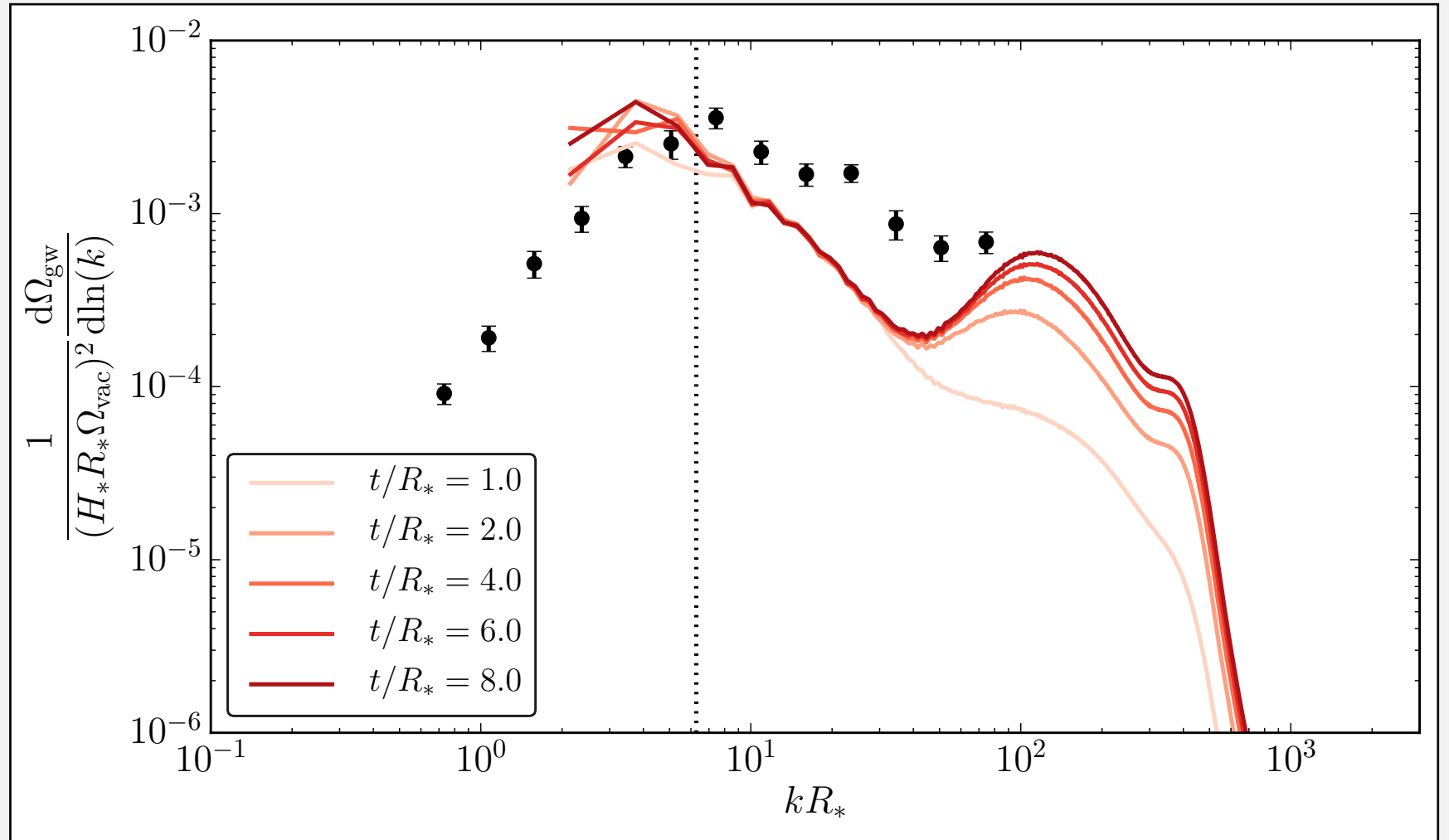


# EVOLUTION OF GW SPECTRUM

$$\gamma_* \simeq 4, N_b = 64$$

Simultaneous nucleation

- Black dots gives spectrum from envelope simulation.
- Coloured lines show spectrum from lattice simulation.



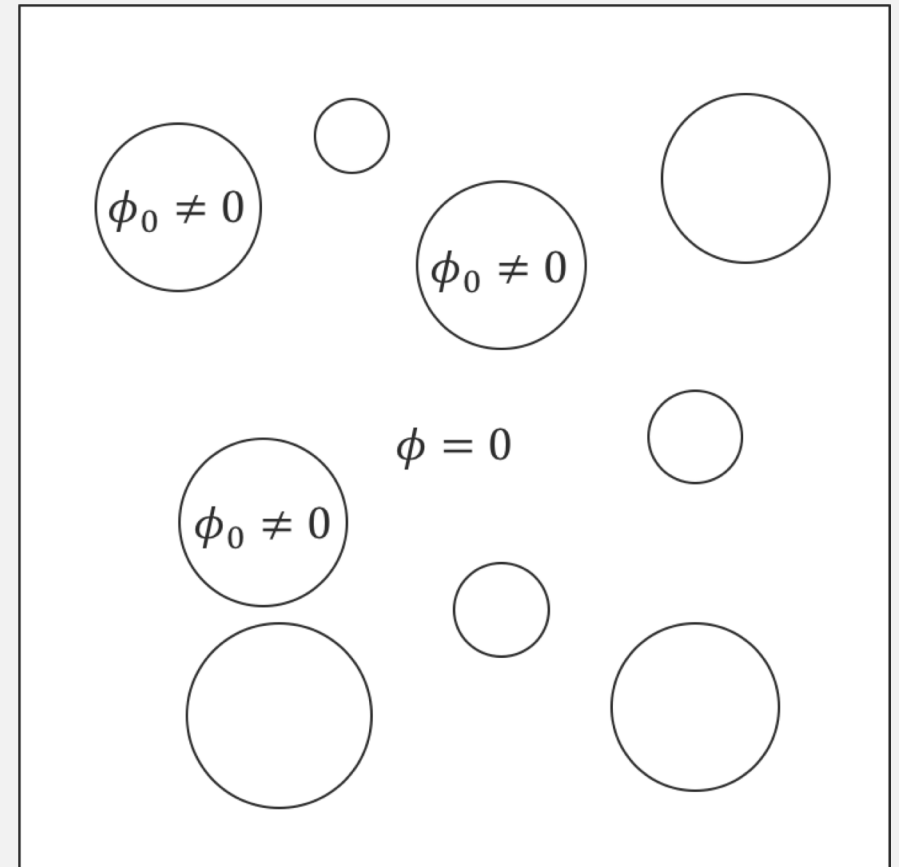
## SIMULATION DETAILS

- 3+1 dimensional classical lattice simulation.
- Built using LATfield2, an open source massively parallel lattice code. *[Daverio, Hindmarsh and Bevis, 2015]*
- Periodic boundary conditions.
- The leapfrog algorithm to evolve fields.
- Resolve the bubble wall:

$$dx \ll l_* = l_0/\gamma_*$$

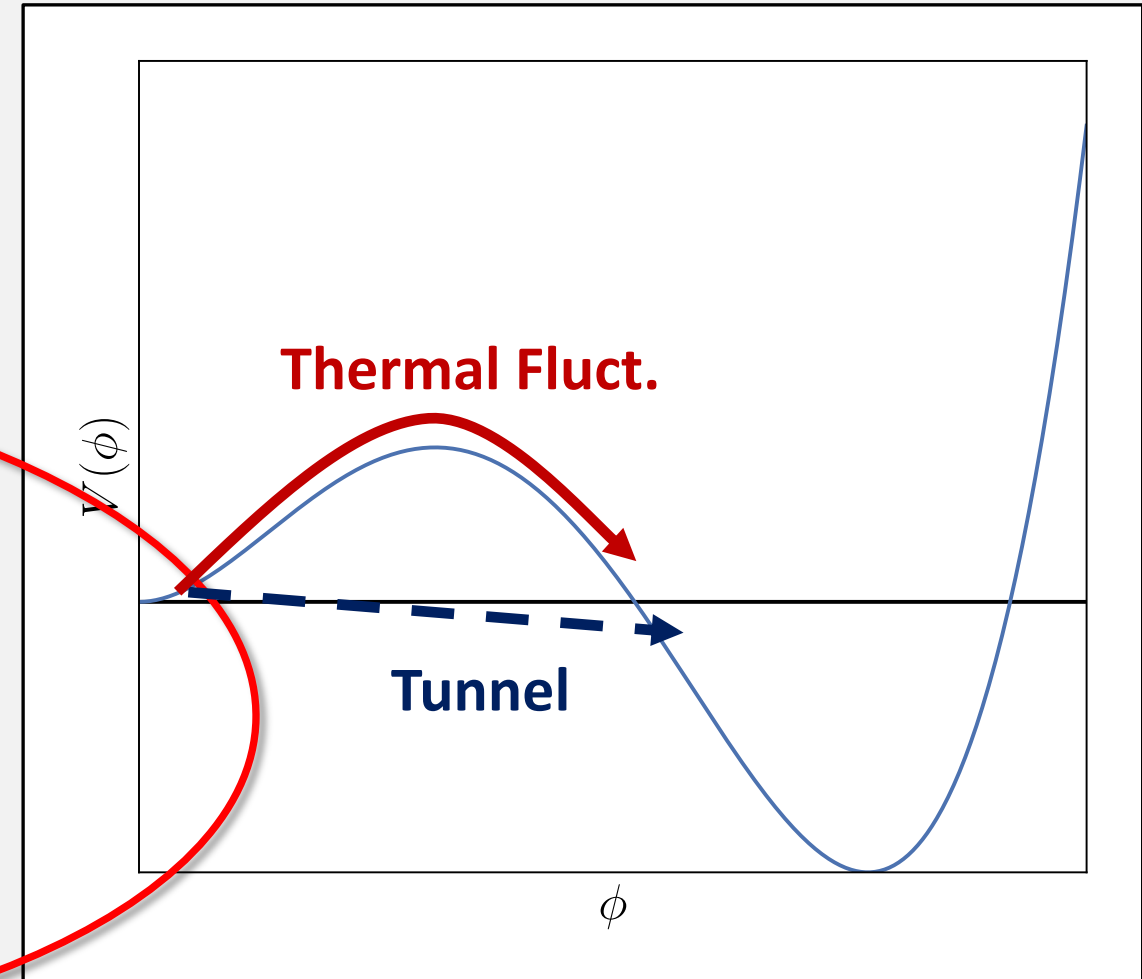
# COSMOLOGICAL FIRST-ORDER PHASE TRANSITIONS

- In cosmological phase transitions (PTs) an (effective) scalar field transitions from false vacuum to true vacuum.
- In a first-order PT phases separated by potential barrier.
- Proceed through the nucleation and merger of bubbles.
- Extensions to the Standard Model can generate a first-order PT at the electroweak scale.



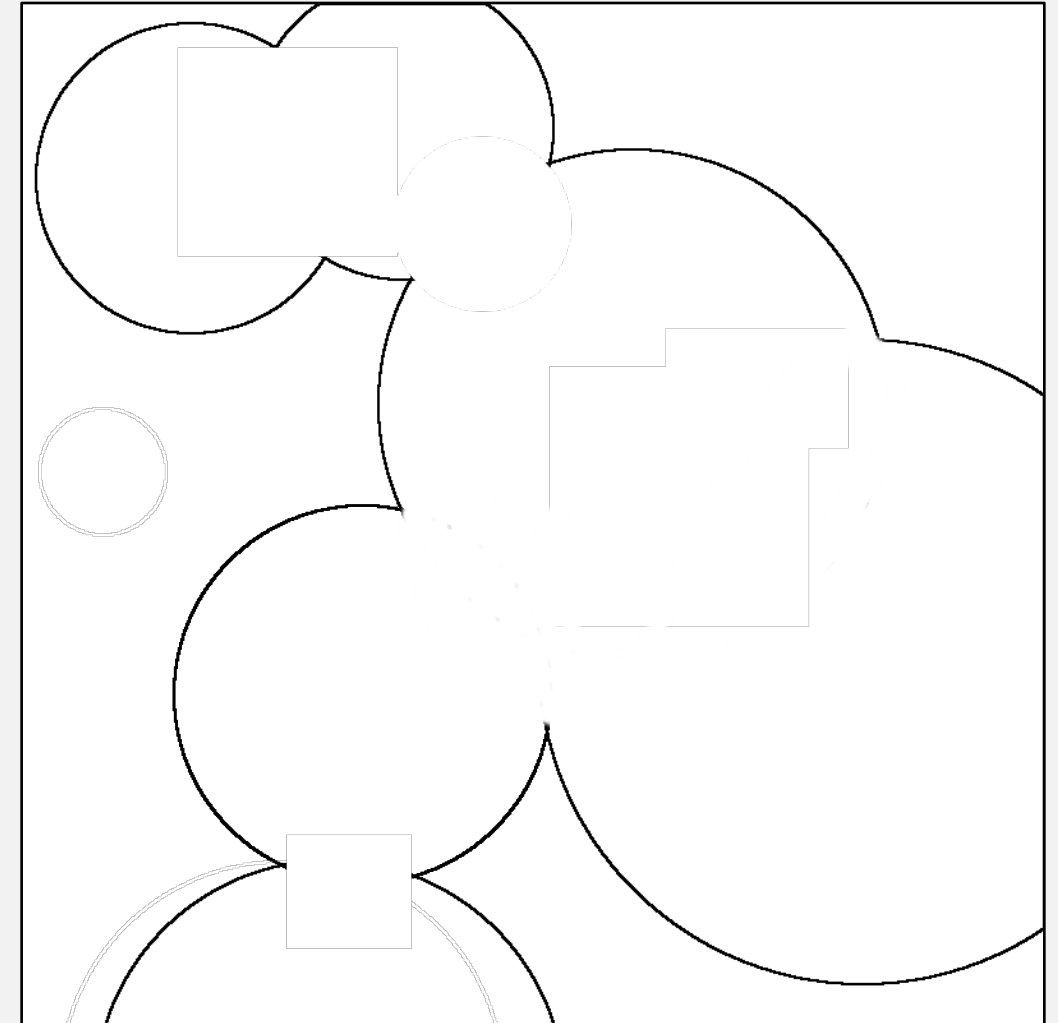
# THERMAL VS VACUUM PHASE TRANSITIONS

- Thermal PTs:
  - Thermally fluctuate over barrier.
  - Fluid shell around bubble wall, exerts friction.
  - Terminal wall velocity.
  - Free energy difference mostly shared between bulk motion of fluid and thermal radiation.
- Vacuum PTs:
  - Quantum tunnel through barrier.
  - Fluid effects negligible.
  - Bubble wall accelerates until collision.
  - Free energy difference deposited into motion of the bubble wall.
  - Limit of highly super cooled PTs or a PT in a hidden sector.



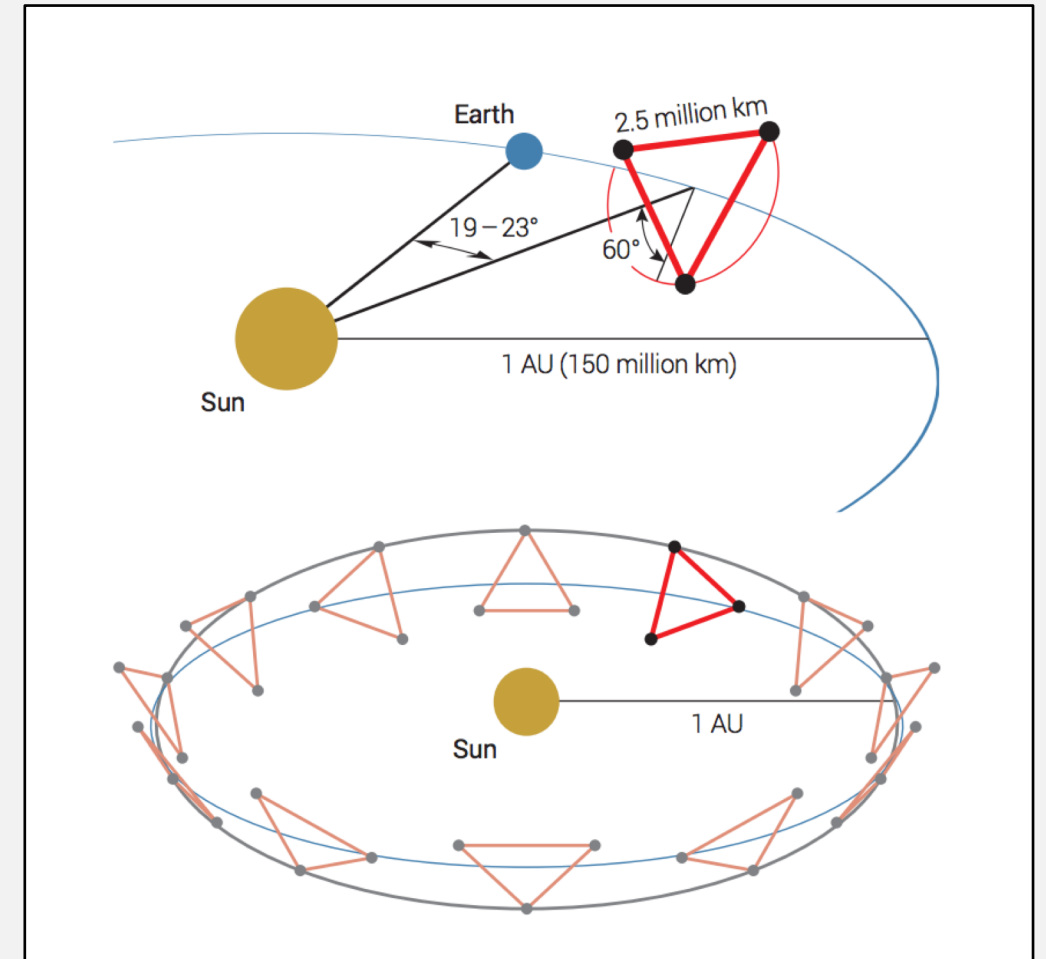
# GRAVITATIONAL WAVES FROM COSMOLOGICAL PHASE TRANSITIONS

- Colliding bubbles break spherical symmetry  
→ radiate gravitational waves (GWs).
- In thermal PTs the dominant GW signal is from acoustic oscillations in fluid.  
*[Hindmarsh et al, 2014] [Hindmarsh, et al, 2015]*  
*[Hindmarsh et al, 2017]*
- In vacuum PTs the GW signal expected to be from shear stress in scalar field at bubble wall.
- Scalar field contribution to GW signal previously studied using envelope approximation.  
E.g *[Kosowsky et al, 1992] [Huber and Konstandin, 2008] [Weir, 2016] [Konstandin, 2017]*



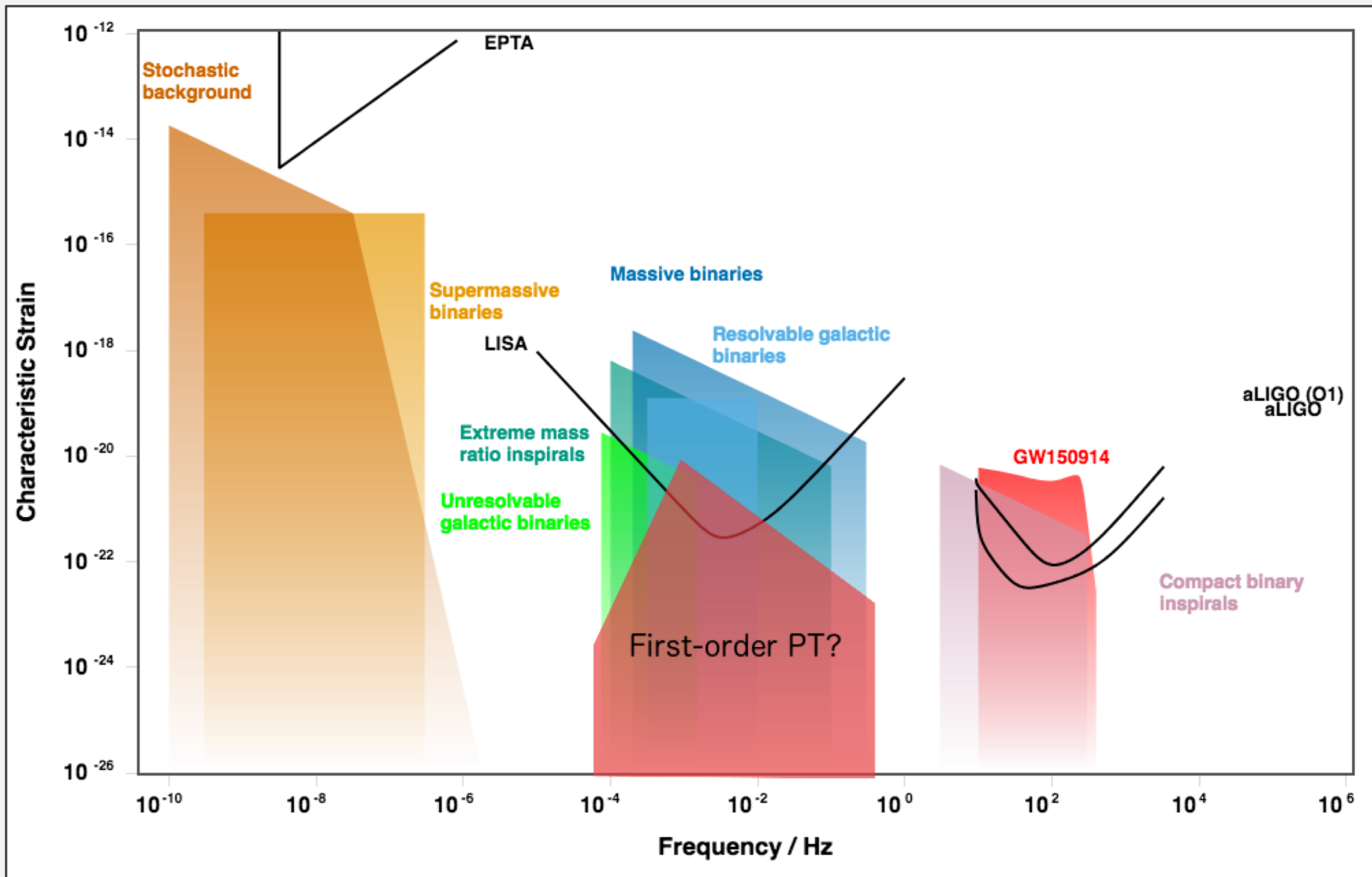
# LASER INTERFEROMETER SPACE ANTENNA (LISA)

- Space based gravitational wave observatory using laser interferometry.
- Planned launch date of 2034.
- Three arms with length of 2.5 million km.
- Among goals is direct detection of a stochastic GW background of cosmological origin. [[arXiv:1702.00786](#)]
- Sensitive to GWs with frequencies of  $10^{-4} \text{ Hz}$  to  $10^{-1} \text{ Hz}$ . [[arXiv:1702.00786](#)] (Electroweak scale)

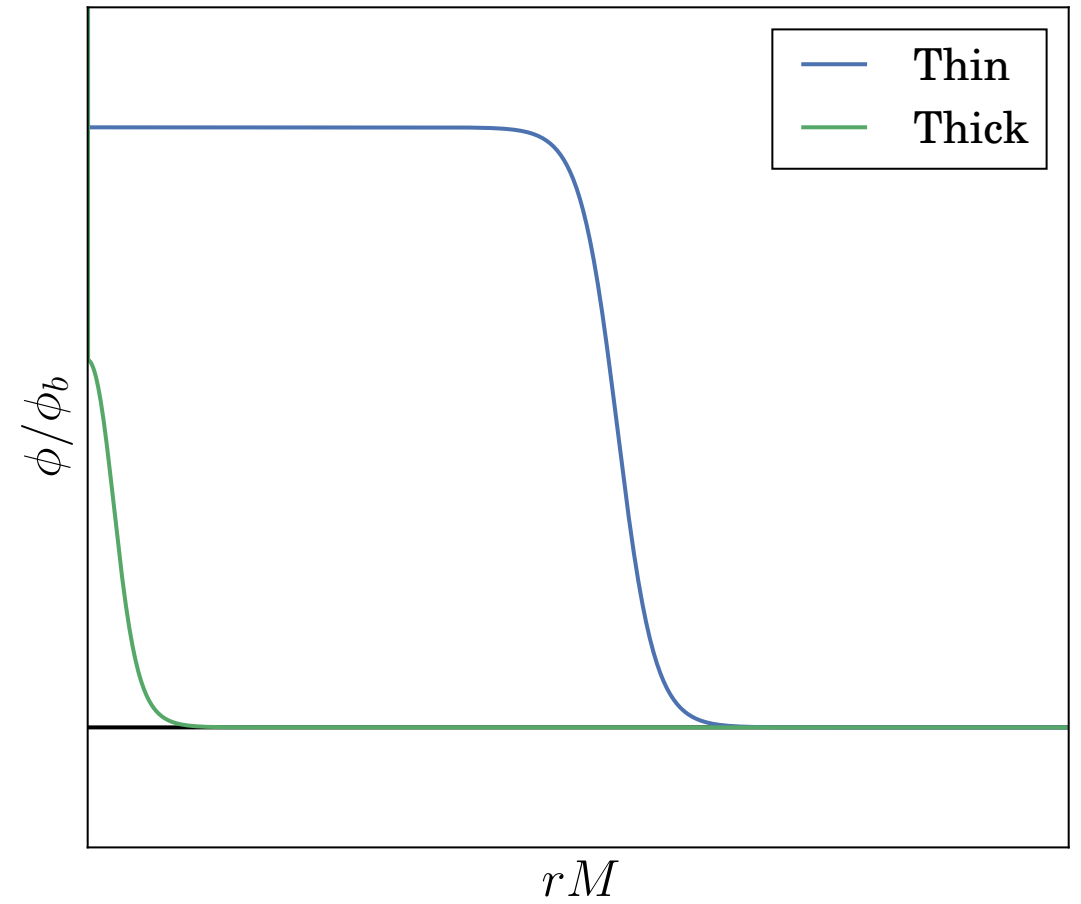
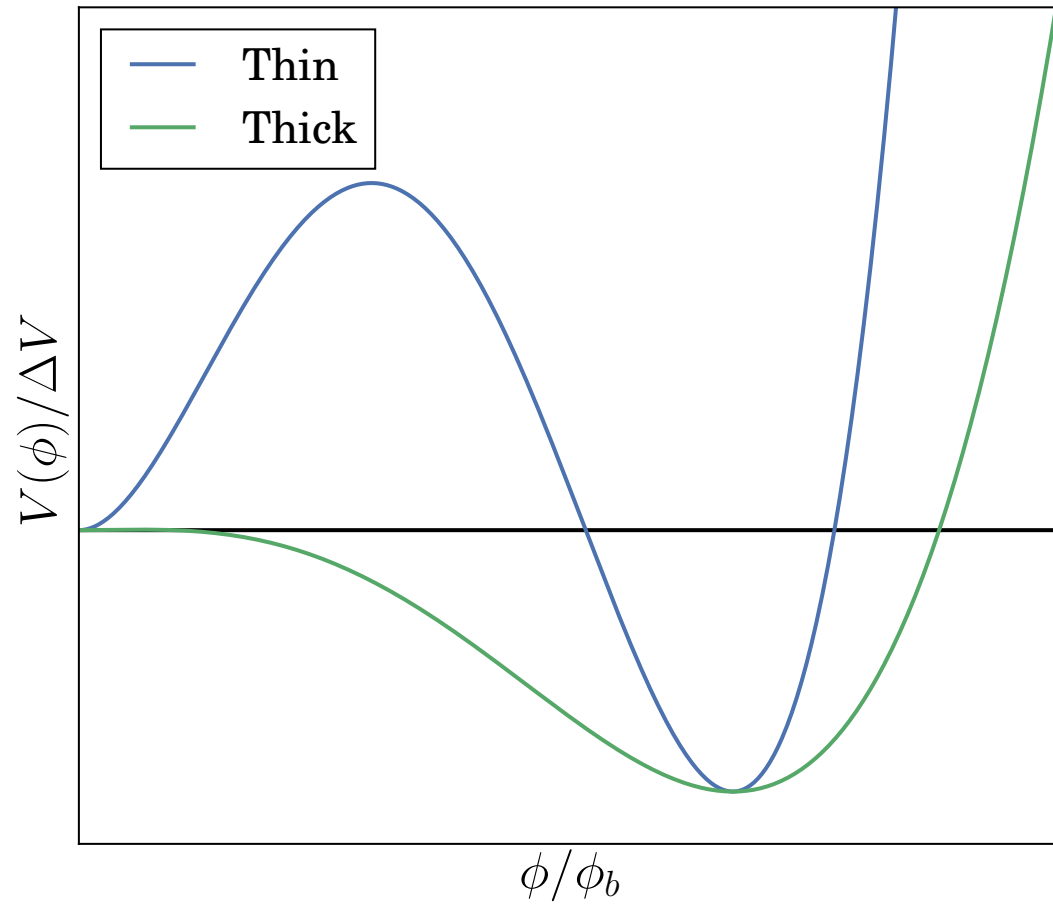


Taken from: [arXiv:1702.00786](#)

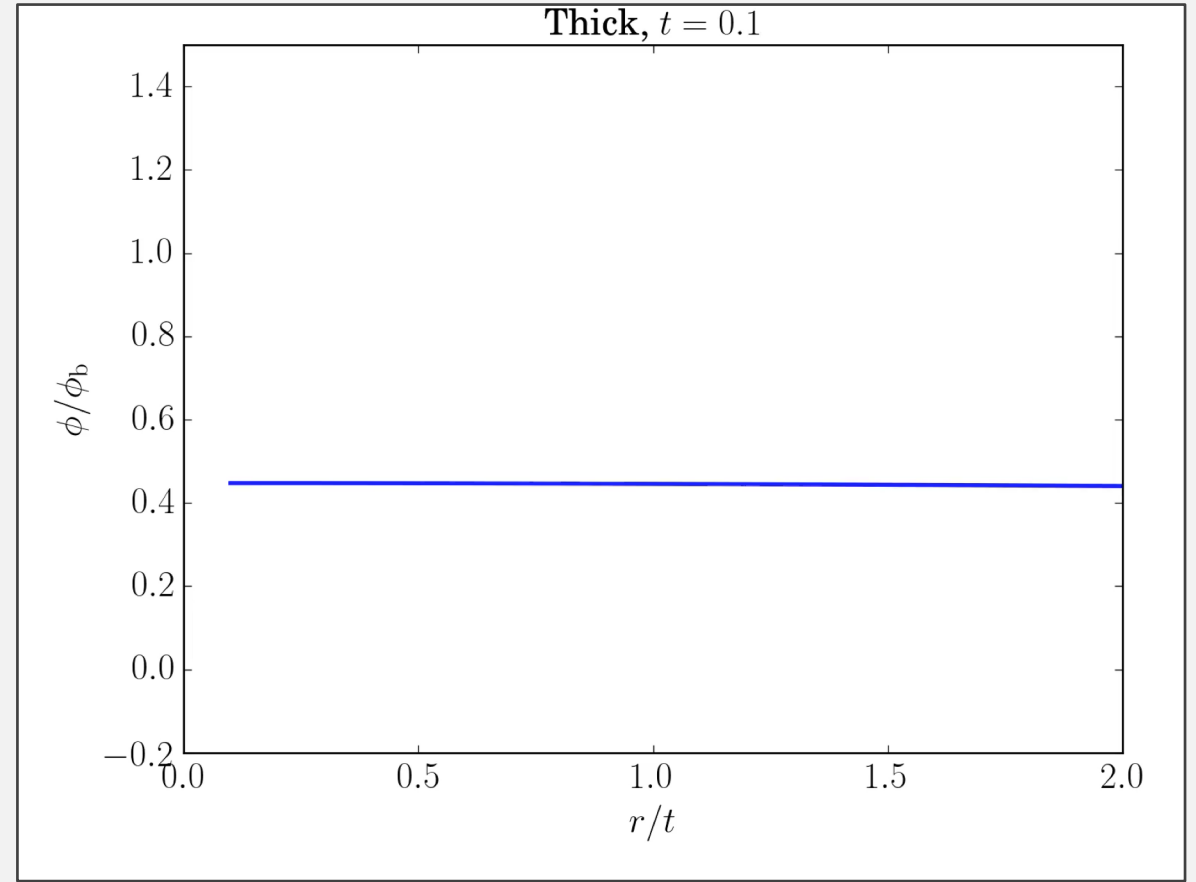
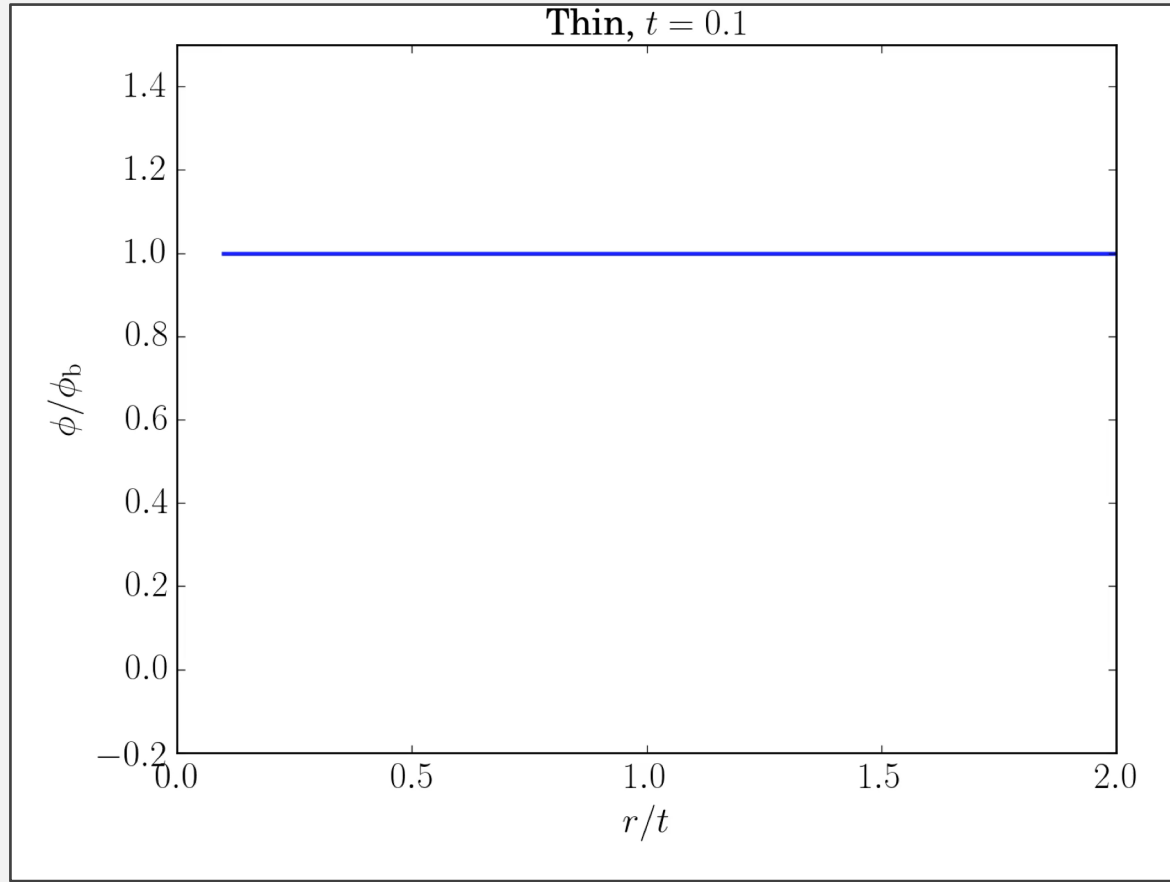




# CRITICAL BUBBLE PROFILE



# BUBBLE EXPANSION



Movie credit: Elva Granados Escartin