

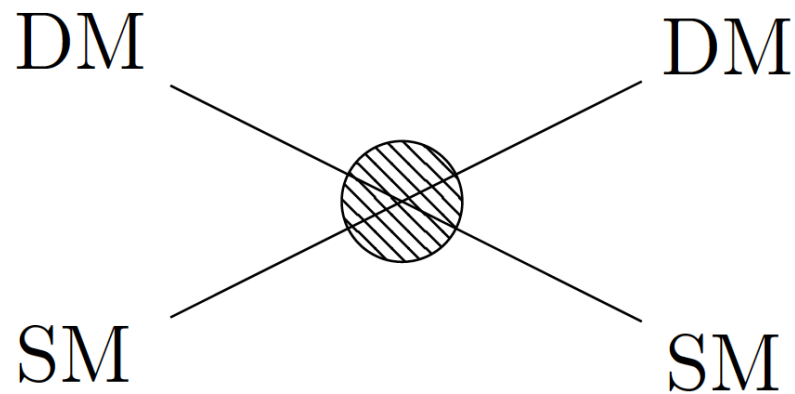
Dark Matter Direct Detection with Spin-2 Mediators

Yoo-Jin Kang

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Alba Carrillo-Monteverde, **YJK**, Hyun Min Lee,
Myeonghun Park and Veronica Sanz,
JHEP 1806 (2018) 037
([arXiv:1803.02144](https://arxiv.org/abs/1803.02144))

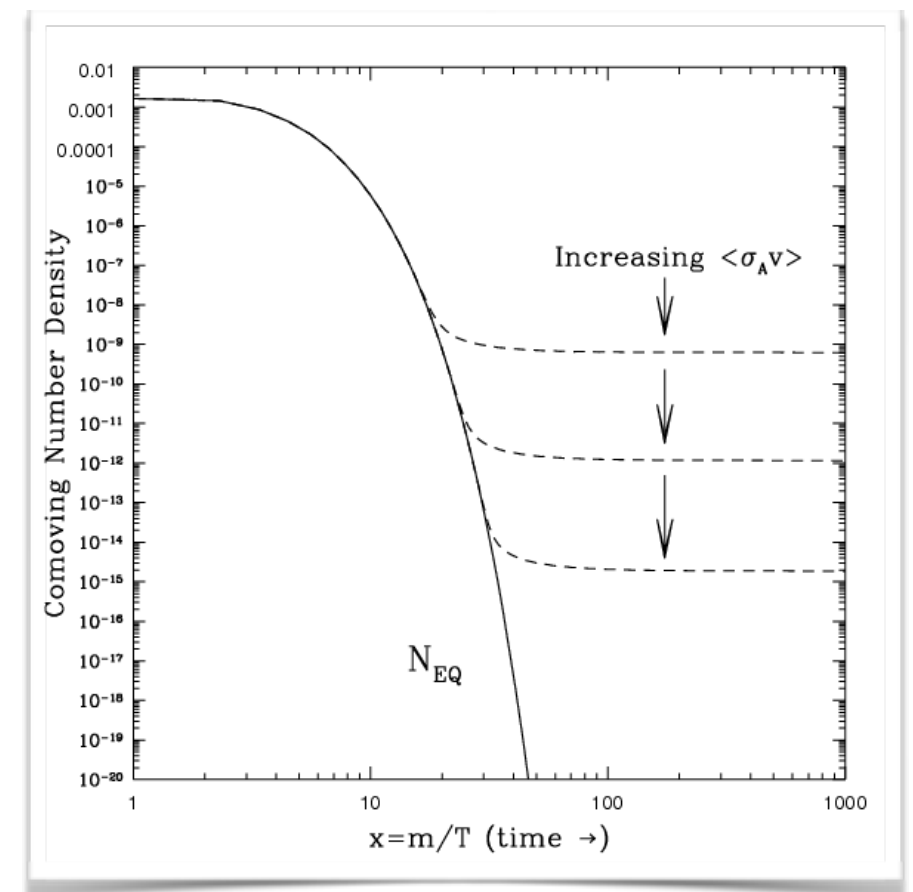
WIMP Dark Matter



- About 25% of the total energy
- Not standard model particles (WIMP, SIMP, Forbidden DM and so on)

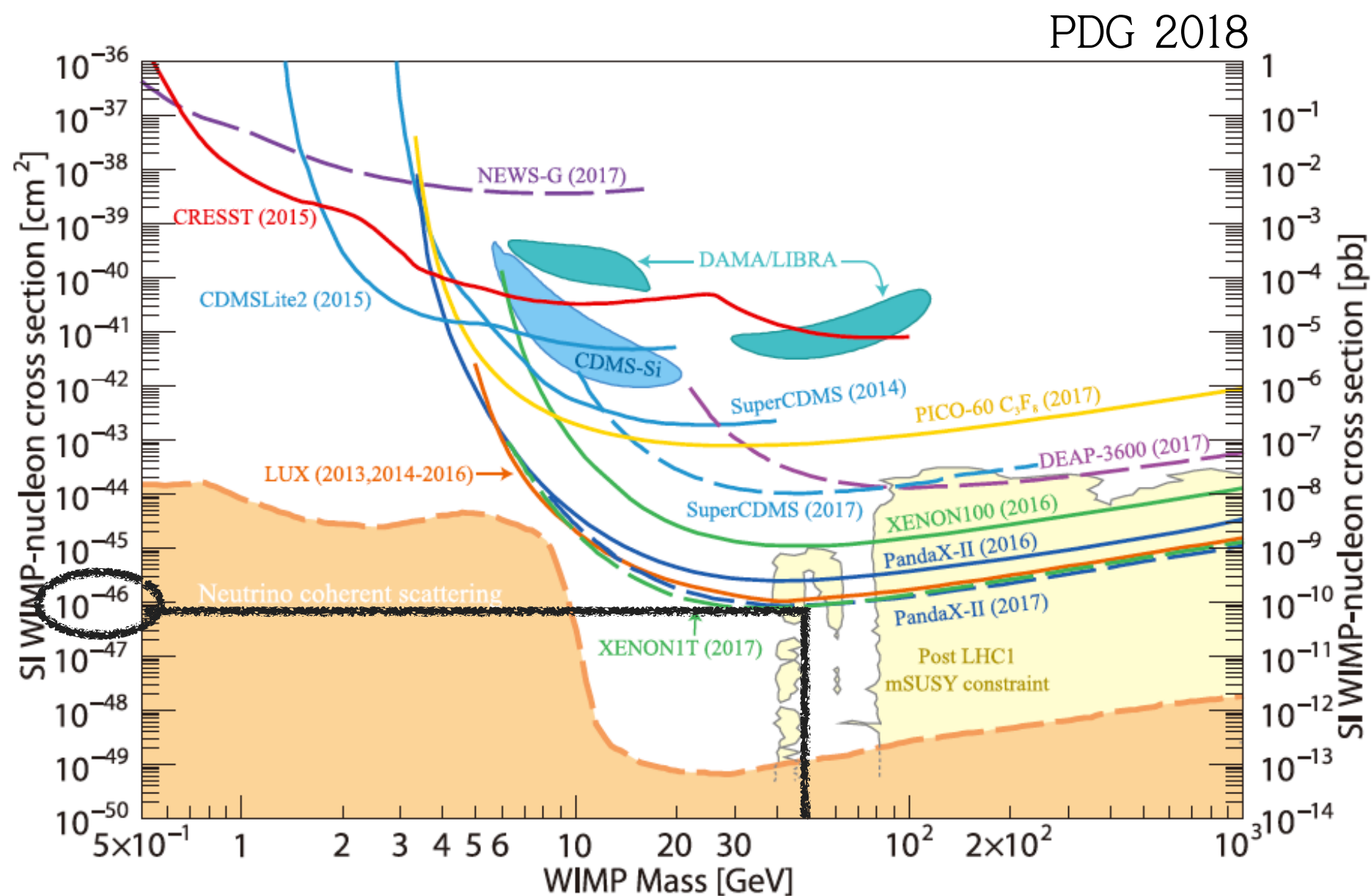
- Thermal WIMP was in the [thermal equilibrium](#) with the SM particles
- WIMP had '[freeze-out](#)' from the thermal equilibrium (freeze-in is possible)

$$\Omega_\chi h^2 \approx \frac{3 \times 10^{-27} \text{cm}^3 \text{s}^{-1}}{\langle \sigma v \rangle_{\chi\bar{\chi} \rightarrow \psi\bar{\psi}}} \approx \underbrace{0.12}_{\text{central value from Planck}} \underbrace{\left(\frac{0.01}{\alpha} \right)^2}_{\text{weak scale}} \left(\frac{m}{100 \text{GeV}} \right)^2$$



- Dark matter search : **Direct**, Indirect, Collider

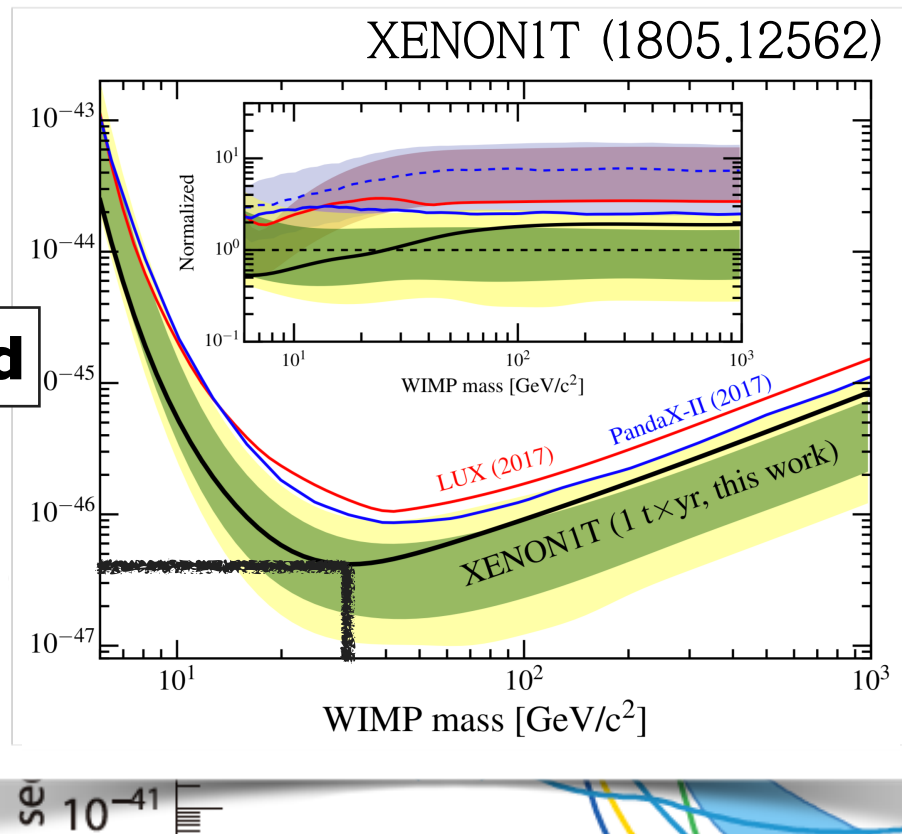
Direct Detection - experiments



- 10^{-46} cm^2 constraint at 50 GeV

Direct

Updated

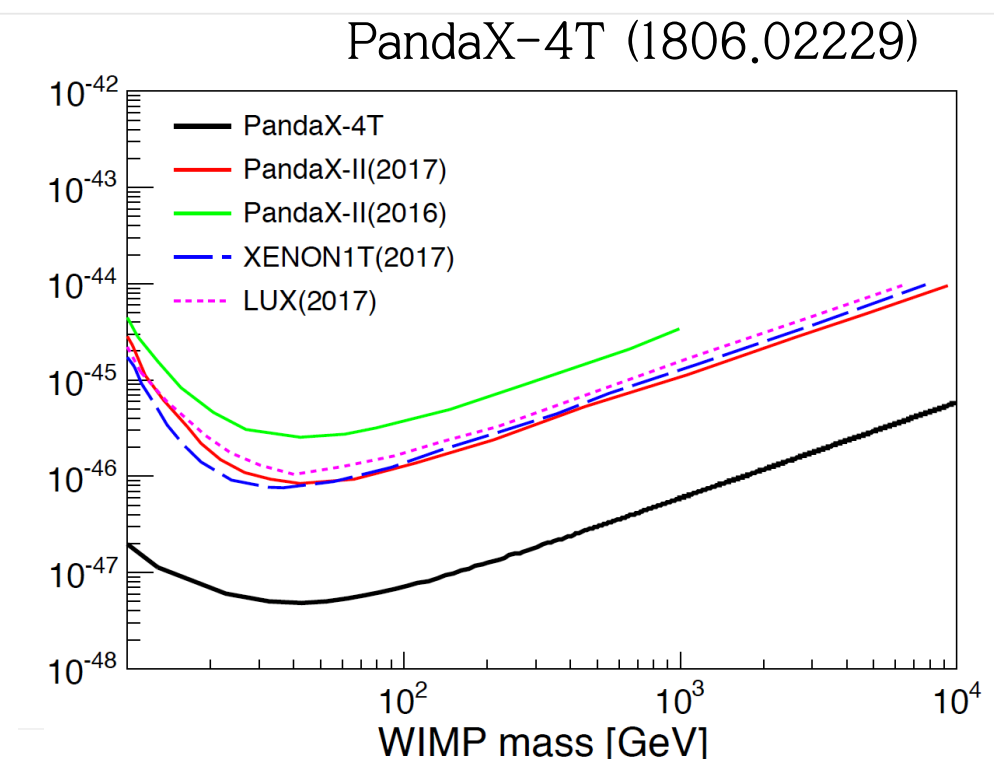
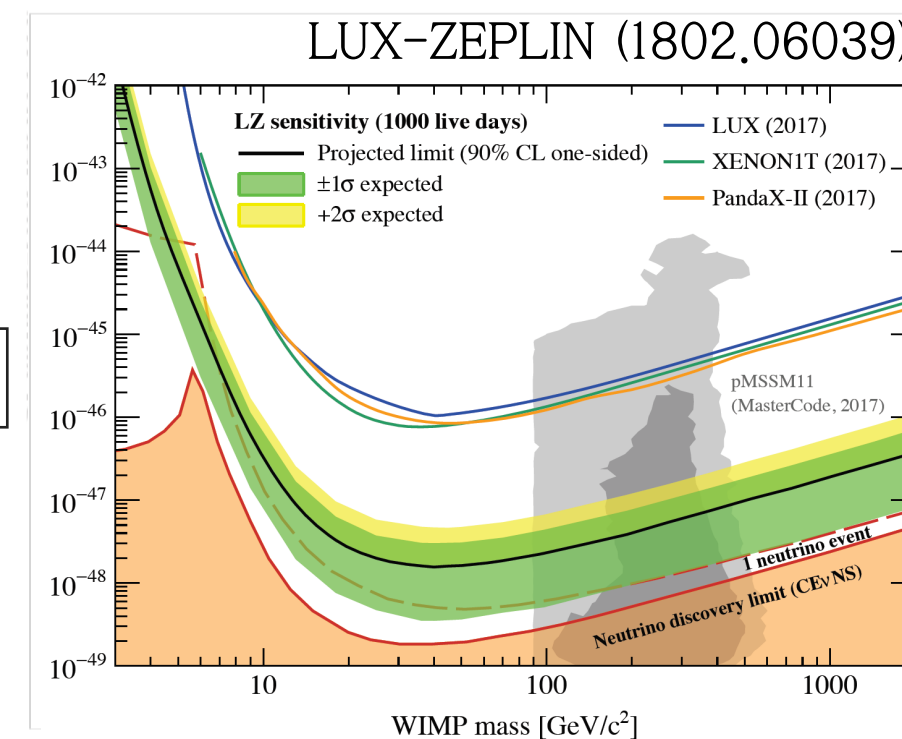


experiments

XENONnT (2019)



Future



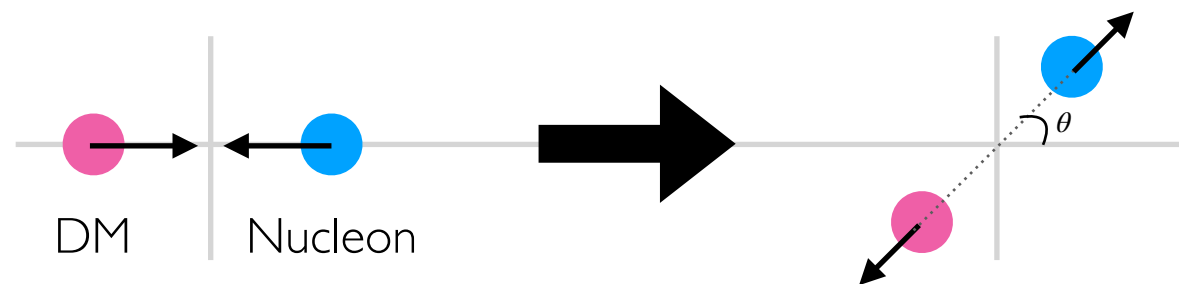
- 10^{-46} cm^2 constraint at 50 GeV
- Heavy DM bounds are **getting strong**. $4 \times 10^{-47} \text{ cm}^2$ constraint at 30 GeV

Direct Detection - differential event rate

Fitzpatrick et al (1203.3542, 1308.6288)

In the CM frame, the relative velocity is v .

$$E_R = \frac{\vec{q}^2}{2m_T} = \frac{\mu_T^2 v^2}{m_T} (1 - \cos \theta) : \text{recoil energy for nucleon coherent scattering, } m_T : \text{target mass}$$



The differential scattering event rate per recoil energy : Counts/keV/kg/day

$$\frac{dR_D}{dE_R} = N_T \left\langle \frac{\rho_\chi m_T}{m_\chi \mu_T^2 v} \frac{d\sigma}{d\cos\theta} \right\rangle$$

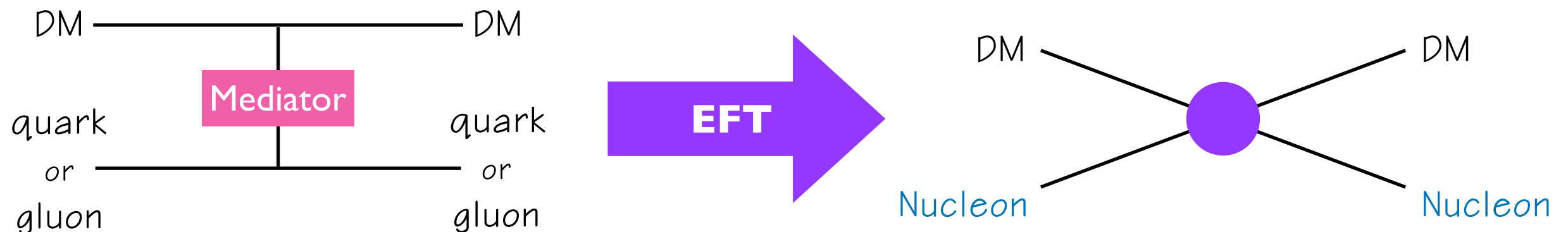
with scattering cross section depending on the detector material.

$$\frac{d\sigma}{d\cos\theta} = \frac{1}{2j_\chi + 1} \frac{1}{2j_N + 1} \sum_{\text{spins}} \frac{1}{32\pi} \frac{|\mathcal{M}|^2}{(m_\chi + m_T)^2} \equiv \frac{m_T^2}{m_N^2} \sum_{i,j} \sum_{N,N'=n,p} c_i^{(N)} c_i^{(N')} \underline{F_{ij}^{(N,N')}(v^2, q^2)}$$

form factors are related to nucleon responses

Mediator and EFT

- EFT approaches are suitable with scattering processes b/w DM and **nucleons**.



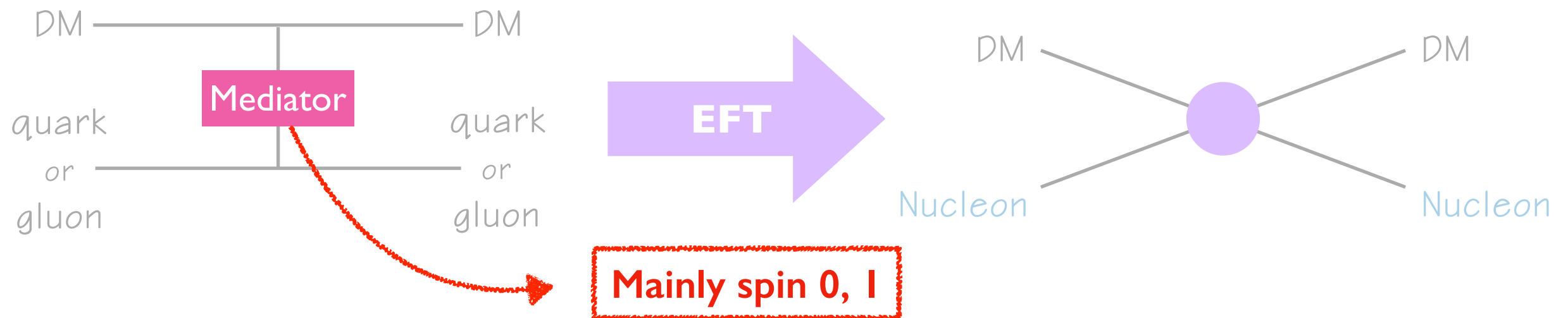
- Mediators** can be directly produced in the early Universe or at the LHC.



∴ "EFT is valid from freeze-out/LHC to DD"

Mediator and EFT

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∴ "EFT is valid from freeze-out/LHC to DD"

We consider **Scattering of dark matter and nucleon**
in the **spin-2** mediator model with the **effective operators**
and compute differential event rates **for direct detection**.

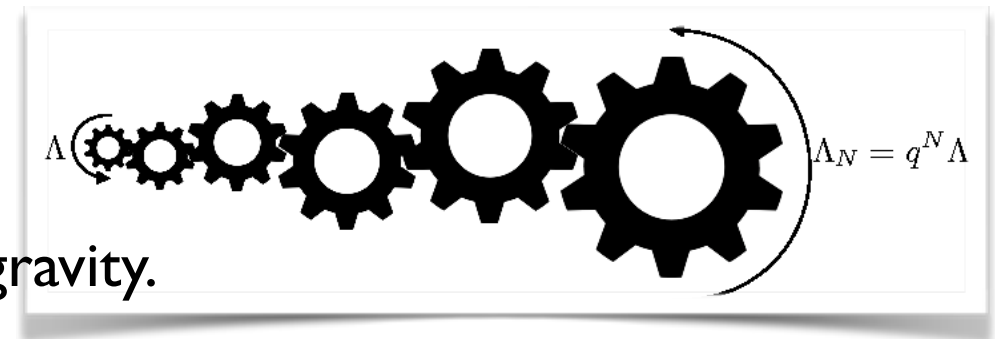
Spin-2 Graviton and Mediator model

- Spin-2 graviton has been studied to explain weak gravity with the **Extra dimension** model, **Kaluza-Klein** tower, **Clockwork theory** and so on.

K. Choi and S. H. Im (1511.00132), D. E. Kaplan and R. Rattazzi (1511.01827),

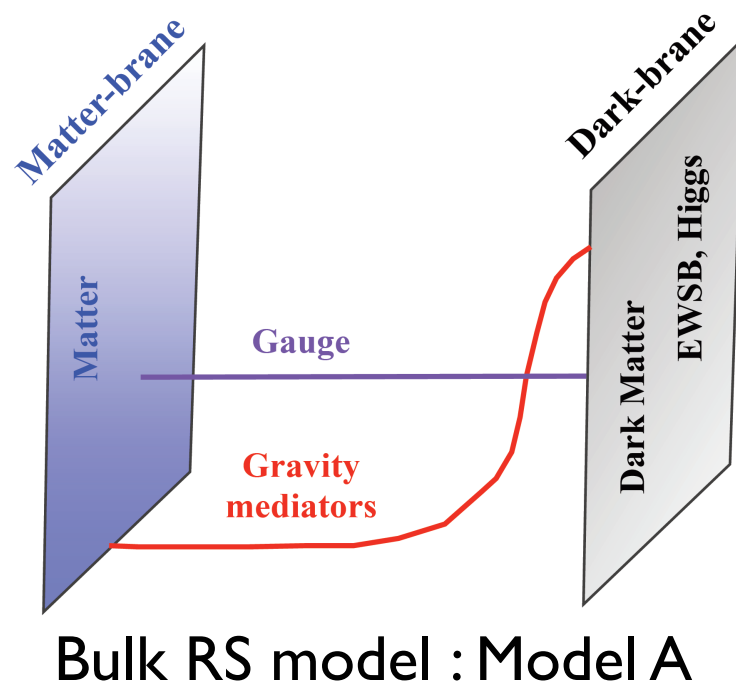
For example) clockwork theory G. F. Giudice and M. McCulough (1610.07962), H. M. Lee (1708.03564)

$\phi_N = \frac{1}{q} \phi_{N-1} = \dots \frac{1}{q^N} \phi_0$ ground state of clock gear
can be graviton to explain weak gravity.

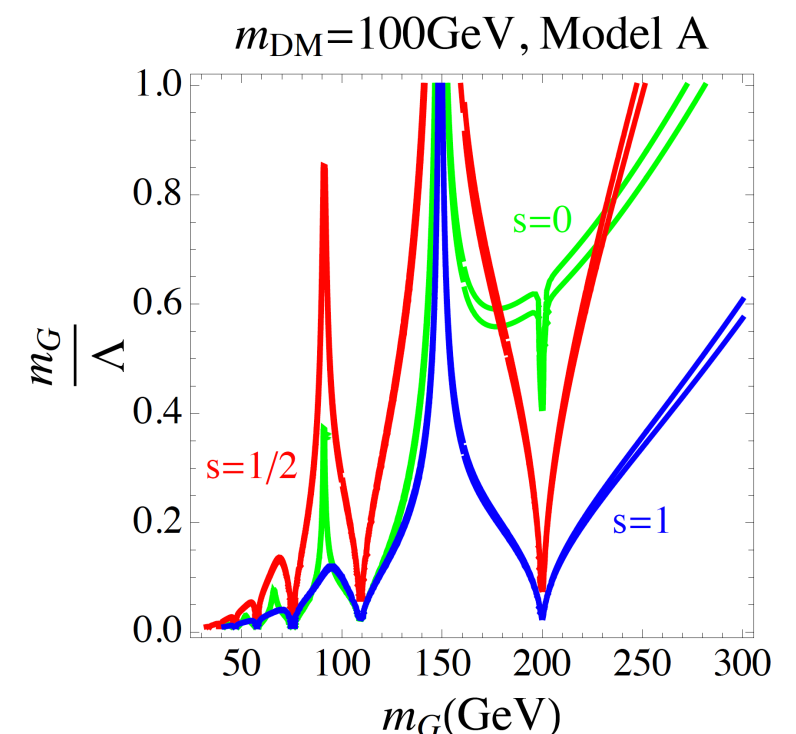


- There are gravity-mediated models

H. M. Lee, M. Park and V. Sanz (1306.4107, 1401.5301)



IR brane : Higgs, DM, top
UV brane : SM matter
Bulk : Gauge field



Spin-2 Mediator Model

H. M. Lee, M. Park and V. Sanz
(1306.4107, 1401.5301)

- We consider the spin-2 mediator for dark matter in **model-independent way**.
- The tensor structure is dictated by Lorentz invariance only.

$$\mathcal{L}_{\text{int}} = -\frac{c_{\text{SM}}}{\Lambda} \mathcal{G}^{\mu\nu} T_{\mu\nu}^{\text{SM}} - \frac{c_{\text{DM}}}{\Lambda} \mathcal{G}^{\mu\nu} T_{\mu\nu}^{\text{DM}} \quad \left\{ \begin{array}{l} \mathcal{G}^{\mu\nu} : \text{massive spin-2 mediator} \\ T_{\mu\nu} : \text{energy-momentum tensor} \end{array} \right.$$

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$\mathcal{G}^{\mu\nu}$: massive spin-2 mediator
 $T_{\mu\nu}$: energy-momentum tensor

- We consider the tree-level scattering amplitude b/w DM and quark through **a massive spin-2 propagator**.

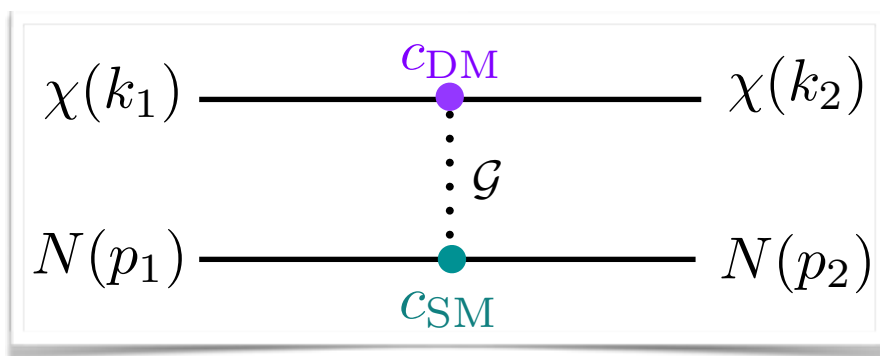
$$\mathcal{M} = -\frac{c_{\text{DM}} c_{\text{SM}}}{\Lambda^2} \frac{i}{q^2 - m_G^2} T_{\mu\nu}^{\text{DM}}(q) \mathcal{P}^{\mu\nu, \alpha\beta}(q) T_{\alpha\beta}^{\text{SM}}(-q) \quad q = k_2 - k_1 = p_1 - p_2$$

Massive spin-2 propagator

satisfies transverse, traceless condition.

$$\mathcal{P}^{\mu\nu, \alpha\beta}(q) = \frac{1}{2} (G^{\mu\alpha} G^{\nu\beta} + G^{\nu\alpha} G^{\mu\beta} - \frac{2}{3} G^{\mu\nu} G^{\alpha\beta})$$

$$G^{\mu\nu} \equiv \eta^{\mu\nu} - \frac{q^\mu q^\nu}{m_G^2}$$



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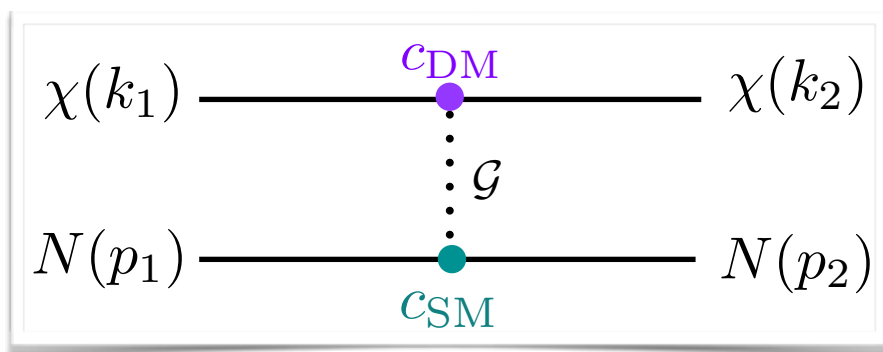
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Integrated Out

$$\mathcal{M} = \frac{i c_{\text{DM}} c_{\text{SM}}}{2 m_G^2 \Lambda^2} \left(\underbrace{2 \tilde{T}_{\mu\nu}^{\text{DM}} \tilde{T}^{\text{SM}, \mu\nu}}_{\text{traceless part}} - \frac{1}{6} \underbrace{T^{\text{DM}} T^{\text{SM}}}_{\text{trace}} \right)$$

Matching with Form Factors

- Form factor for the scalar current

ψ : SM quarks

$$q = p_1 - p_2$$

Trace of the energy-momentum tensor : $T^\psi = -m_\psi \bar{u}_\psi(p_2)u_\psi(p_1)$

Matching from quark to nucleon : $\langle N(p_2) | m_\psi \psi \bar{\psi} | N(p_1) \rangle = F_S(q^2) m_N \bar{u}_N(p_2)u_N(p_1)$

J. Zupan et al (1708.02678, 1710.10218)

If $q=0$, $\langle N(p) | m_\psi \psi \bar{\psi} | N(p) \rangle = f_{T\psi}^N m_N \bar{u}_N(p)u_N(p)$

mass fraction of light quarks in
a nucleon

f_{Tu}^p	0.023	f_{Tu}^n	0.017
f_{Td}^p	0.032	f_{Td}^n	0.017
f_{Ts}^p	0.020	f_{Ts}^n	0.020

K. Ishiwata et al (1012.5455)

A. Corsetti et al (hep-ph/0003186)

H. Ohki et al (0806.4744)

H. Y. Cheng '1989

Gravitational Form Factors

- Gravitational form factor $\longrightarrow$ Matrix elements of the energy-momentum tensor

$$p' = (p_1 + p_2)/2$$

$$\begin{aligned} \langle N(p_2) | T_{\mu\nu}^\psi | N(p_1) \rangle &= \bar{u}_N(p_2) \left[A(q^2) \gamma_{(\mu} p'_{\nu)} + B(q^2) \frac{i}{2m_N} p'_{(\mu} \sigma_{\nu)\lambda} q^\lambda + C(q^2) \frac{1}{m_N} (q_\mu q_\nu - \eta_{\mu\nu} q^2) \right] u_N(p_1) \\ &= -2A(q^2) T_{\mu\nu}^N + \frac{1}{m_N} \bar{u}_N(p_2) \left[B(q^2) \frac{i}{2} p_{(\mu} \sigma_{\nu)\lambda} q^\lambda + C(q^2) (q_\mu q_\nu - \eta_{\mu\nu} q^2) \right] u_N(p_1) \end{aligned}$$

All defined inside nucleon.

mass fraction

related to spin information

pressure distribution

In the case of 5-dimensional AdS spacetime and the transverse-traceless gauge,
the remaining term is only A term in the 5D action.

$\therefore$ we can set $A(q^2) \neq 0, B(q^2) = C(q^2) = 0$

Z. Abidin and C. E. Carlson
(0903.4818)

Therefore, the traceless part is $\langle N(p_2) | \tilde{T}_{\mu\nu}^\psi | N(p_1) \rangle = F_T(q^2) \tilde{T}_{\mu\nu}^N$ with $F_T(q^2) \equiv -2A(q^2)$

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$$\text{If } q=0, \quad \langle N(p) | \tilde{T}_{\mu\nu}^\psi | N(p) \rangle = -\frac{F_T(0)}{m_N} \left(p_\mu p_\nu - \frac{1}{4} m_N^2 g_{\mu\nu} \right) \bar{u}_N(p) u_N(p)$$

$$\text{and } F_T(0) = \psi(2) + \bar{\psi}(2) = \int_0^1 dx [\psi(x) + \bar{\psi}(x)]$$

second moments of PDF

$\mu \approx m_Z$, CTEQ

$u(2) + \bar{u}(2)$	0.22+0.034
$d(2) + \bar{d}(2)$	0.11+0.036
$s(2) + \bar{s}(2)$	0.026+0.026
$c(2) + \bar{c}(2)$	0.019+0.019
$b(2) + \bar{b}(2)$	0.012+0.012

K. Ishiwata et al (1012.5455)

J. Huston et al (hep-ph/0201195)

Effective Operators

- Elastic scattering of **WIMP** & **Nucleon** Fitzpatrick et al (1203.3542, 1308.6288)

$$\mathcal{L}_{\text{int}}(\vec{x}) = \underbrace{c\Psi_{\chi}^*(\vec{x})\mathcal{O}_{\chi}\Psi_{\chi}(\vec{x})}_{\text{WIMP}} \underbrace{\Psi_N^*(\vec{x})\mathcal{O}_N\Psi_N(\vec{x})}_{\text{Nucleon}}$$

- Amplitude : $\sum_{i=1}^{\mathcal{N}} \left(c_i^{(n)} \mathcal{O}_i^{(n)} + c_i^{(p)} \mathcal{O}_i^{(p)} \right)$ $\mathcal{O}_i$ is formed from the $\mathcal{O}_{\chi}$ and $\mathcal{O}_N$

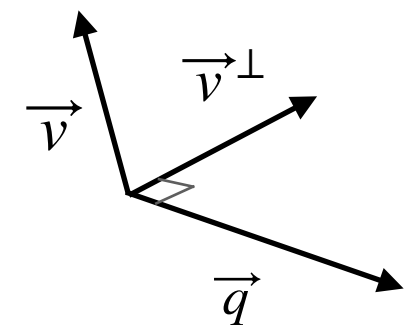
- 4 basic Hermitian quantities

1. Momentum transfer $\vec{q}$

2. Relative perpendicular velocity $\vec{v}^{\perp} \equiv \vec{v} + \frac{\vec{q}}{2\mu_N}$

3. Spin of WIMP $\vec{S}_{\chi}$

4. Spin of nucleon $\vec{S}_N$



where μ_N : reduced mass of DM and nucleon and $\vec{v}^{\perp} \cdot \vec{q} = 0$

Effective Operators

S_{DM}	$\mathcal{O}_i$	$\Sigma_k \mathcal{O}_k^{\text{NR}}$
1/2	$(\bar{\chi}\chi)(\bar{N}N)$	$4m_\chi m_N \mathcal{O}_1^{\text{NR}}$
1/2	$(\bar{\chi}\chi)(K_\nu \bar{N} i \sigma^{\nu\lambda} \frac{q_\lambda}{m_N} N)$	$4 \frac{m_\chi^2}{m_N} \vec{q}^2 \mathcal{O}_1^{\text{NR}} - 16 m_\chi^2 m_N \mathcal{O}_3^{\text{NR}}$
1/2	$(P_\mu \bar{\chi} i \sigma^{\mu\rho} \frac{q_\rho}{m_N} \chi)(\bar{N}N)$	$-4m_N \vec{q}^2 \mathcal{O}_1^{\text{NR}} + 16m_\chi m_N^2 \mathcal{O}_5^{\text{NR}}$
1/2	$(\bar{\chi} i \sigma^{\mu\rho} \frac{q_\rho}{m_N} \chi)(\bar{N} i \sigma_{\mu\lambda} \frac{q^\lambda}{m_N} N)$	$16 \frac{m_\chi}{m_N} (\vec{q}^2 \mathcal{O}_4^{\text{NR}} - m_N^2 \mathcal{O}_6^{\text{NR}})$
1/2	$(P_\mu \bar{\chi} i \sigma^{\mu\rho} \frac{q_\rho}{m_N} \chi)(K_\nu \bar{N} i \sigma^{\nu\lambda} \frac{q_\lambda}{m_N} N)$	$-4 \frac{m_\chi}{m_N} (\vec{q}^2 \mathcal{O}_1^{\text{NR}} - 4m_N^2 \mathcal{O}_3^{\text{NR}})$ $\times (\vec{q}^2 \mathcal{O}_1^{\text{NR}} - 4m_\chi m_N \mathcal{O}_5^{\text{NR}})$
0	$(S^* S)(\bar{N}N)$	$2m_N \mathcal{O}_1^{\text{NR}}$
0	$i(S^* \partial_\mu S - S \partial_\mu S^*)(\bar{N} \gamma^\mu N)$	$4m_S m_N \mathcal{O}_1^{\text{NR}}$
1	$\bar{N}N$	$2m_N f(\epsilon_1, \epsilon_2^*) \mathcal{O}_1^{\text{NR}}$
1	$\epsilon_{1,2}^\alpha \bar{N} i \sigma_{\alpha\lambda} \frac{q^\lambda}{m_N} N$	$4im_N^2 \left(\vec{S}_N \cdot \left(\vec{\epsilon}_{1,2} \times \frac{\vec{q}}{m_N} \right) \right)$
1	$k_{1,2\nu} \bar{N} i \sigma^{\nu\lambda} \frac{q_\lambda}{m_N} N$	$m_\chi (\vec{q}^2 \mathcal{O}_1^{\text{NR}} - 4m_N^2 \mathcal{O}_3^{\text{NR}})$

$$\begin{aligned}
\mathcal{O}_1 &= 1_\chi 1_N \\
\mathcal{O}_2 &= (v^\perp)^2 \\
\mathcal{O}_3 &= i \vec{S}_N \cdot \left(\frac{\vec{q}}{m_N} \times \vec{v}^\perp \right) \\
\mathcal{O}_4 &= \vec{S}_\chi \cdot \vec{S}_N \\
\mathcal{O}_5 &= i \vec{S}_\chi \cdot \left(\frac{\vec{q}}{m_N} \times \vec{v}^\perp \right) \\
\mathcal{O}_6 &= \left(\vec{S}_\chi \cdot \frac{\vec{q}}{m_N} \right) \left(\vec{S}_N \cdot \frac{\vec{q}}{m_N} \right) \\
\mathcal{O}_7 &= \vec{S}_N \cdot \vec{v}^\perp \\
\mathcal{O}_8 &= \vec{S}_\chi \cdot \vec{v}^\perp
\end{aligned}$$

Effective Lagrangians

Fermion DM

Unsuppressed operator for
DM-nucleon scattering

$$\mathcal{L}_{\chi,\text{eff}} \approx \frac{c_\chi c_\psi m_\chi^2 m_N^2}{2m_G^2 \Lambda^2} \left[\left\{ \underline{6F_T \left(1 + \frac{\vec{q}^2}{3m_N^2} + \frac{\vec{q}^2}{3m_\chi^2} \right) - \frac{2}{3}F_S} \right\} \underline{\mathcal{O}_1^{\text{NR}}} - 8F_T \mathcal{O}_3^{\text{NR}} - \frac{4\vec{q}^2}{m_\chi m_N} F_T \underline{\mathcal{O}_4^{\text{NR}}} \right. \\ \left. - \frac{8m_N}{m_\chi} F_T \left(1 + \frac{\vec{q}^2}{8m_N^2} \right) \mathcal{O}_5^{\text{NR}} + \frac{4m_N}{m_\chi} F_T \mathcal{O}_6^{\text{NR}} + \frac{4m_N}{m_\chi} F_T \mathcal{O}_3^{\text{NR}} \mathcal{O}_5^{\text{NR}} \right]$$

Scalar DM

$$\mathcal{L}_{S,\text{eff}} = \frac{c_S c_\psi m_S^2 m_N^2}{2m_G^2 \Lambda^2} \left[\underline{F_T \left(6 - \frac{\vec{q}^2}{m_S^2} \right) - \frac{2}{3}F_S \left(1 - \frac{\vec{q}^2}{2m_S^2} \right)} \right] \underline{\mathcal{O}_1^{\text{NR}}}$$

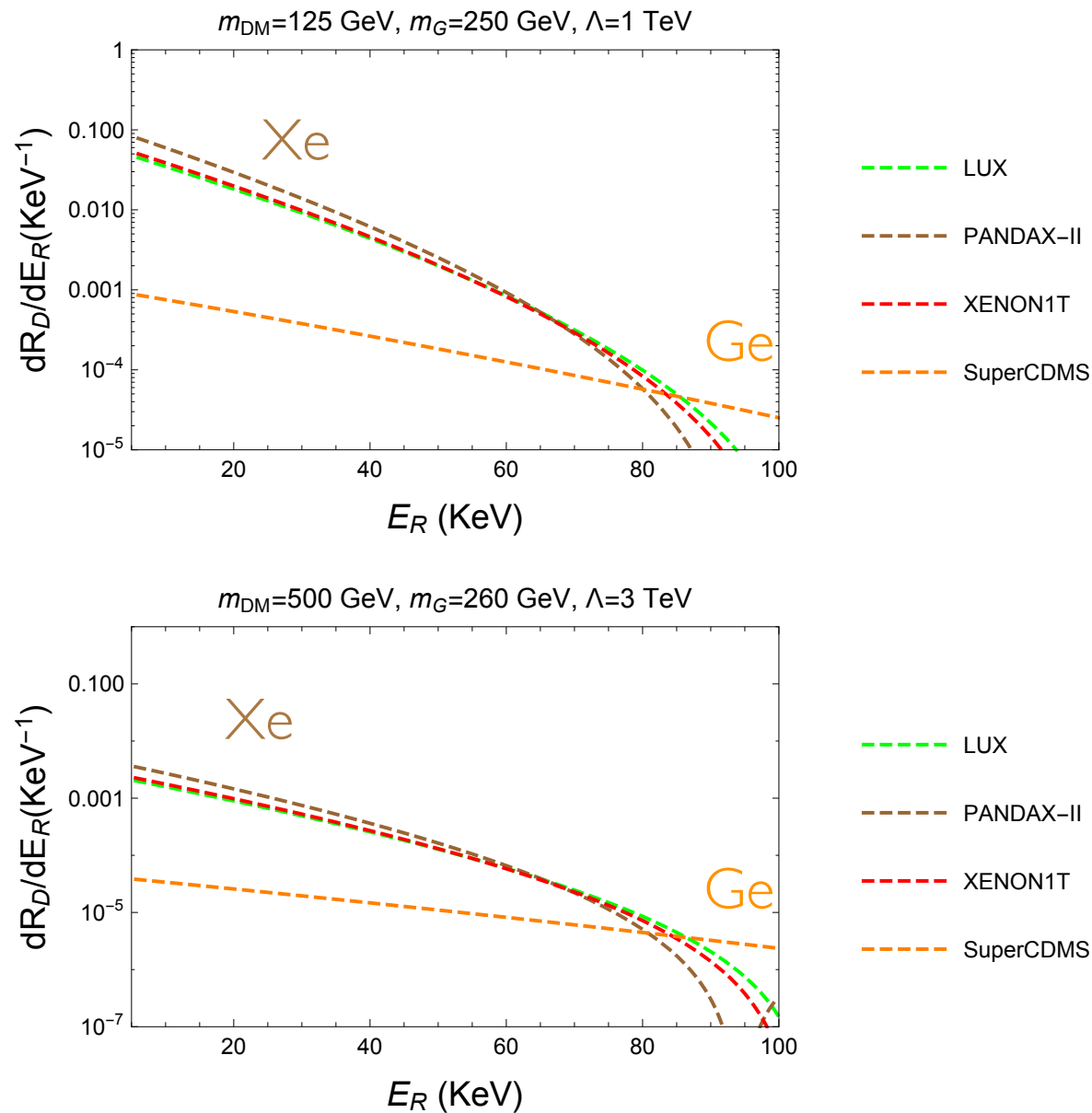
As a result, leading terms are independent of DM spins.

Dimension : $\int \frac{d^3p}{(2\pi)^3 \sqrt{2E}} a_N^{(\dagger)}$ and $\int \frac{d^3p}{(2\pi)^3 \sqrt{2E}} a_\chi^{(\dagger)}$ per each nucleon & DM state are to be multiplied.

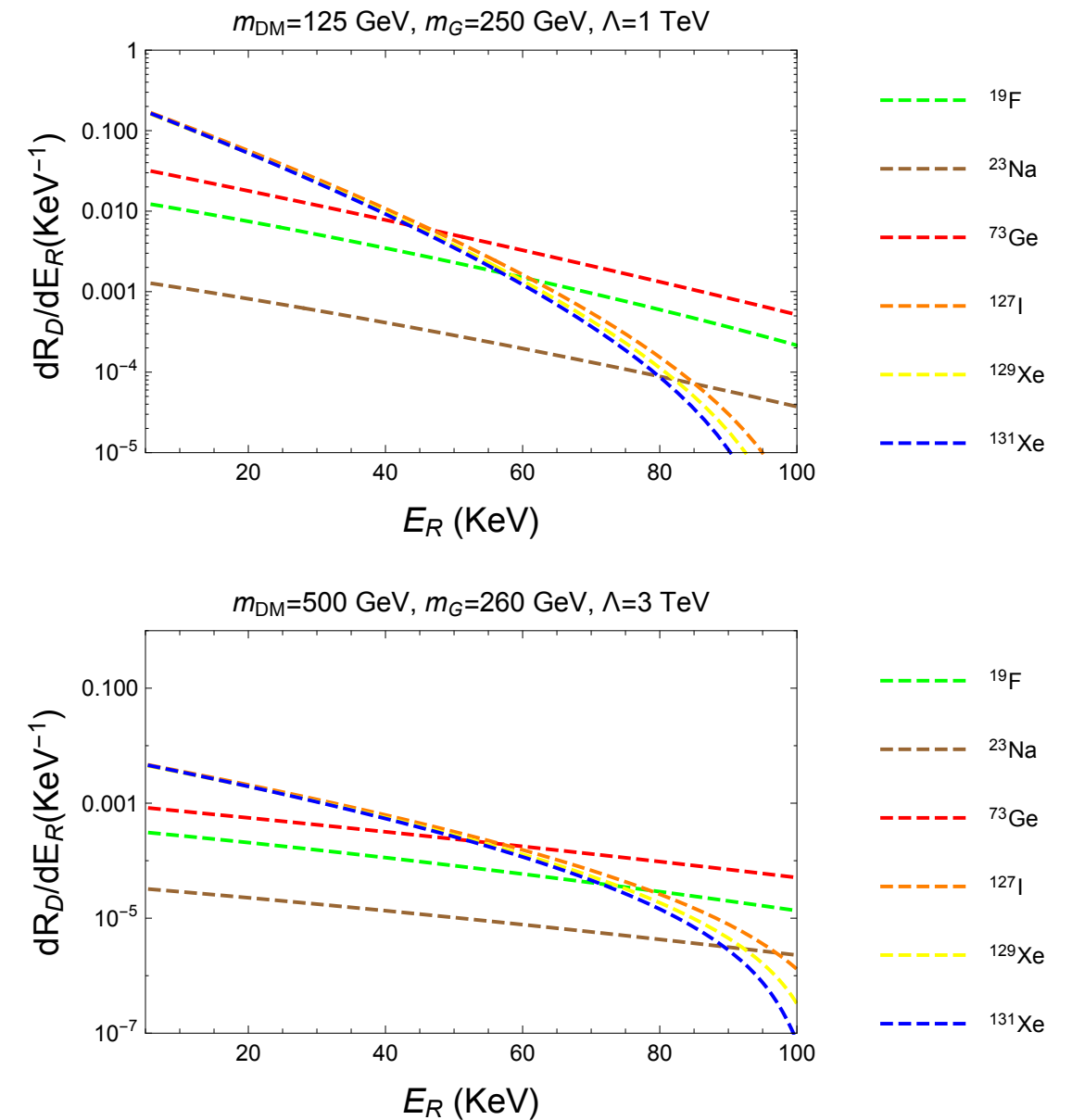
Differential Event Rate

$$\frac{dR_D}{dE_R} \propto \frac{d\sigma}{d\cos\theta} \propto \sum_{i,j} \sum_{N,N'=n,p} c_i^{(N)} c_i^{(N')} F_{ij}^{(N,N')}$$

Current Exp.

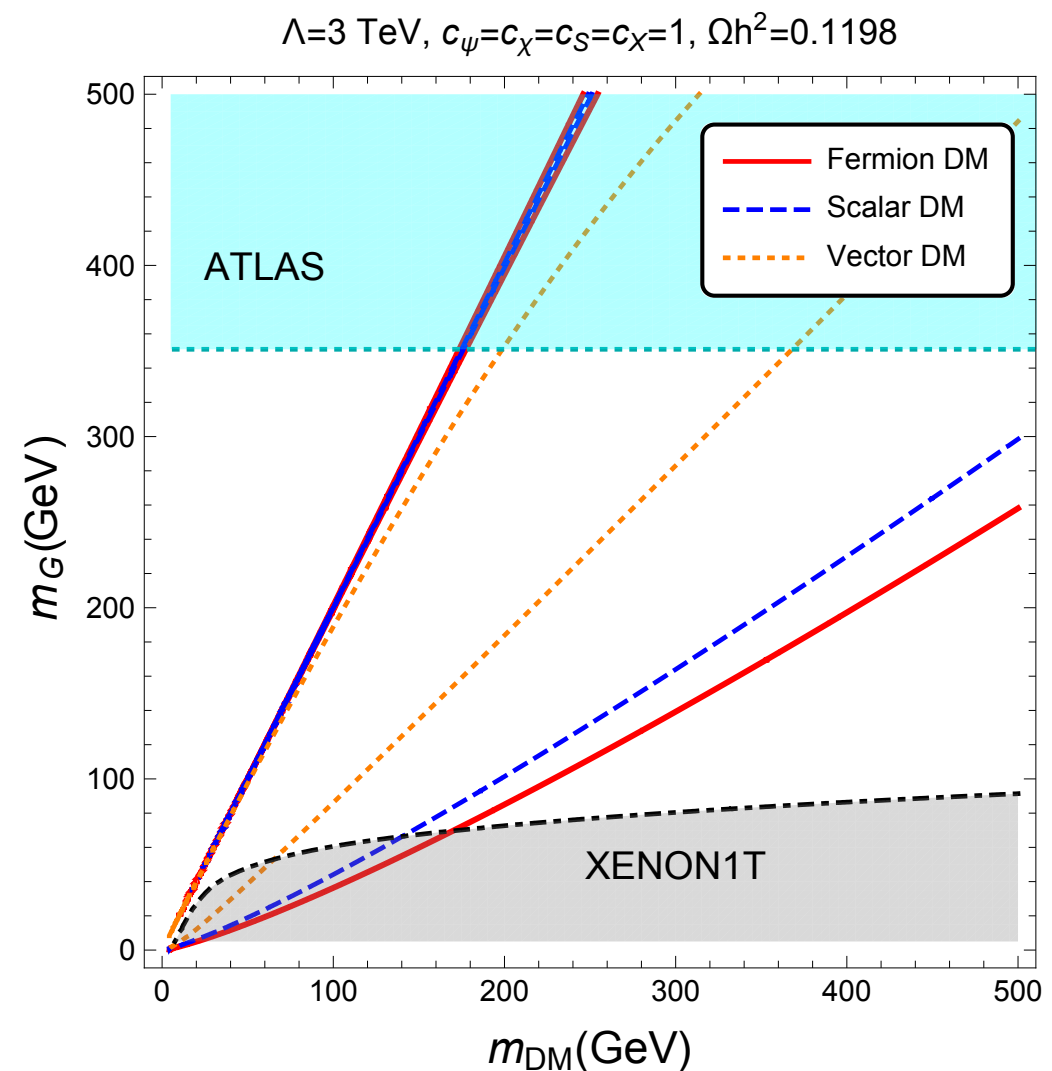
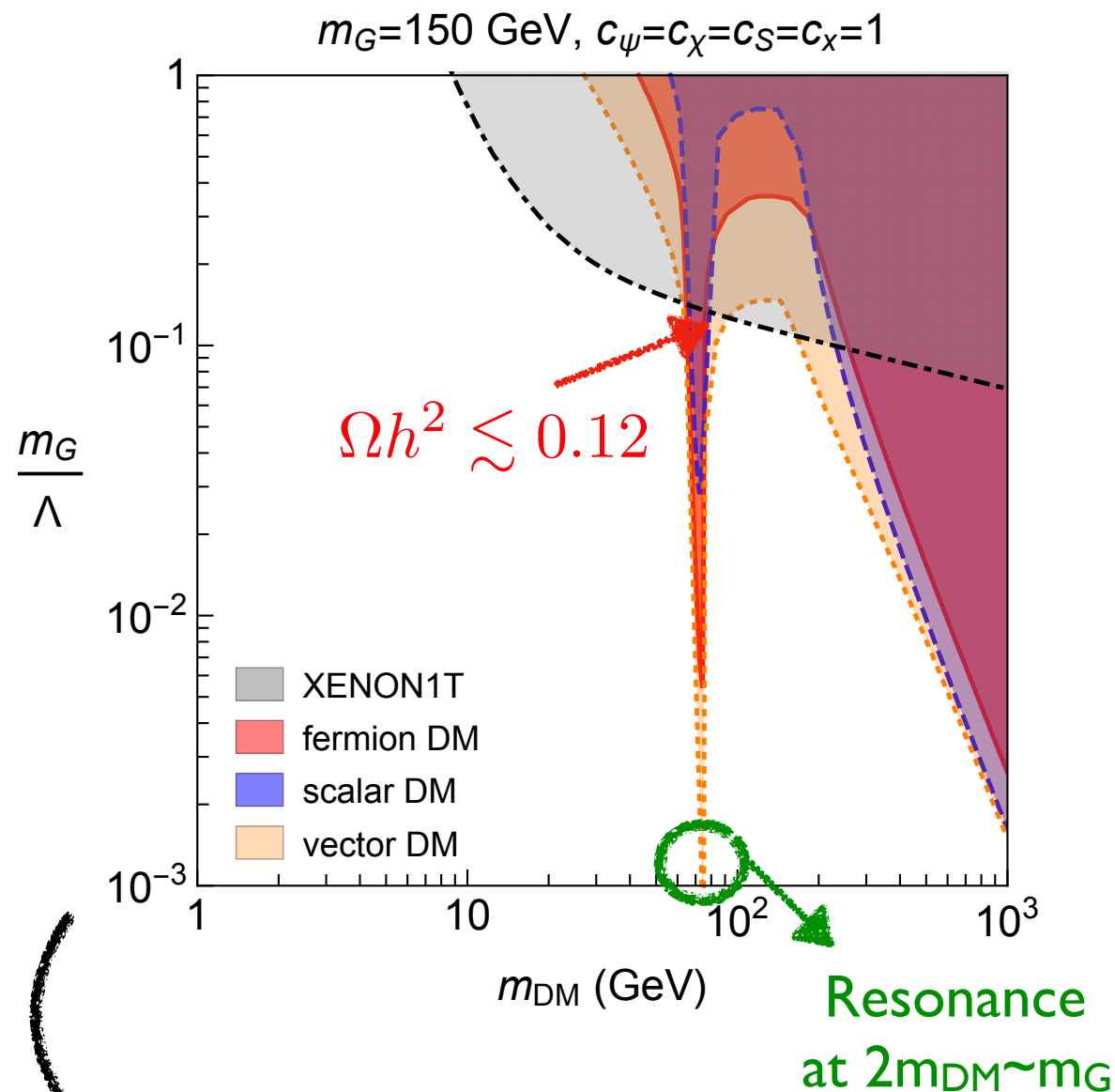


Mock Exp.



Relic Density Condition

Dark matter can annihilate into SM quarks or Spin-2 particles



- The relic region below $m_{\text{DM}} = 250 \text{ GeV}$ is excluded by direct detection, except the resonance region.
- If we consider gluon contribution, relic density lines will be lower.

Dark Matter Relic Density - Bounds

- The same spin-independent scattering cross section for all the spins of DM

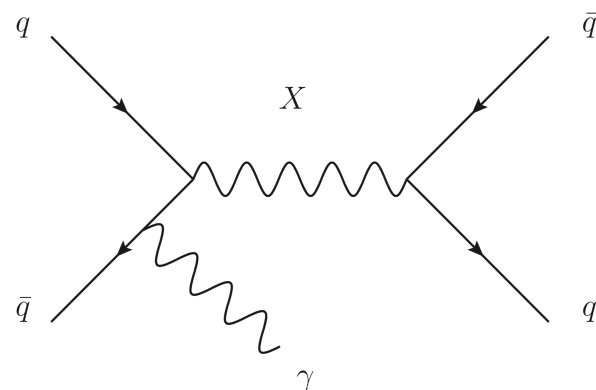
$$\sigma_{\text{DM}-N}^{\text{SI}} = \frac{\mu_N^2}{\pi A^2} (Z f_p^{\text{DM}} + (A - Z) f_n^{\text{DM}})^2$$

$$f_{p,n}^{\text{DM}} = \frac{c_{\text{DM}} m_N m_{\text{DM}}}{4m_G^2 \Lambda^2} \left(\sum_{\psi=u,d,s,c,b} 3c_\psi (\psi(2) + \bar{\psi}(2)) + \sum_{\psi=u,d,s} \frac{1}{3} c_\psi f_{T\psi}^{p,n} \right)$$

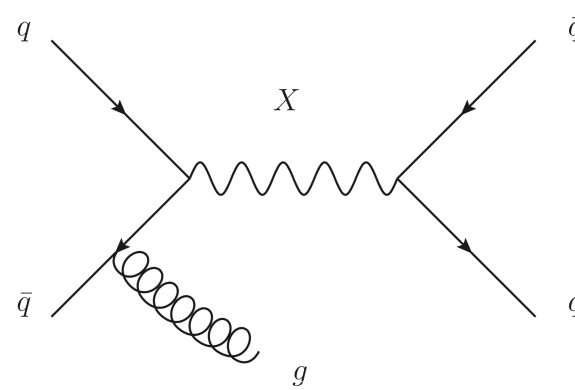
c.f.-scalar med. (Higgs portal) $f_{p,n}^{\text{DM}} = m_N \left(\sum_{\psi=u,d,s} f_{T\psi}^{p,n} \frac{\mathcal{M}_\psi}{m_\psi} + \frac{2}{27} f_H^{p,n} \sum_{\psi=c,b,t} \frac{\mathcal{M}_\psi}{m_\psi} \right)$

Y. Mambrini (1108.0671)

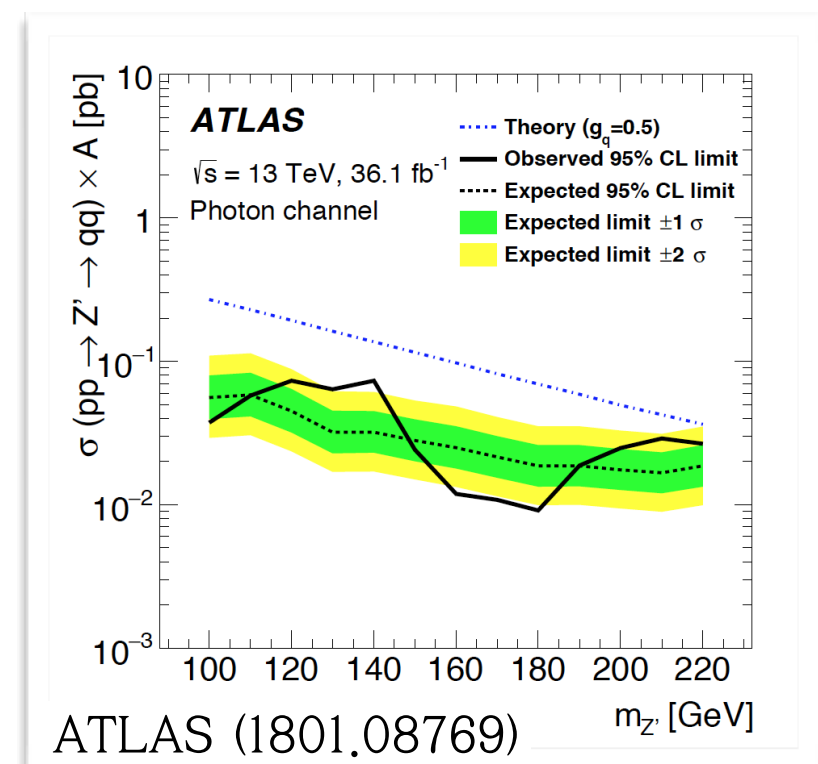
- ATLAS dijet constraints to $BR(G \rightarrow q\bar{q})$.



ISR photon + dijet



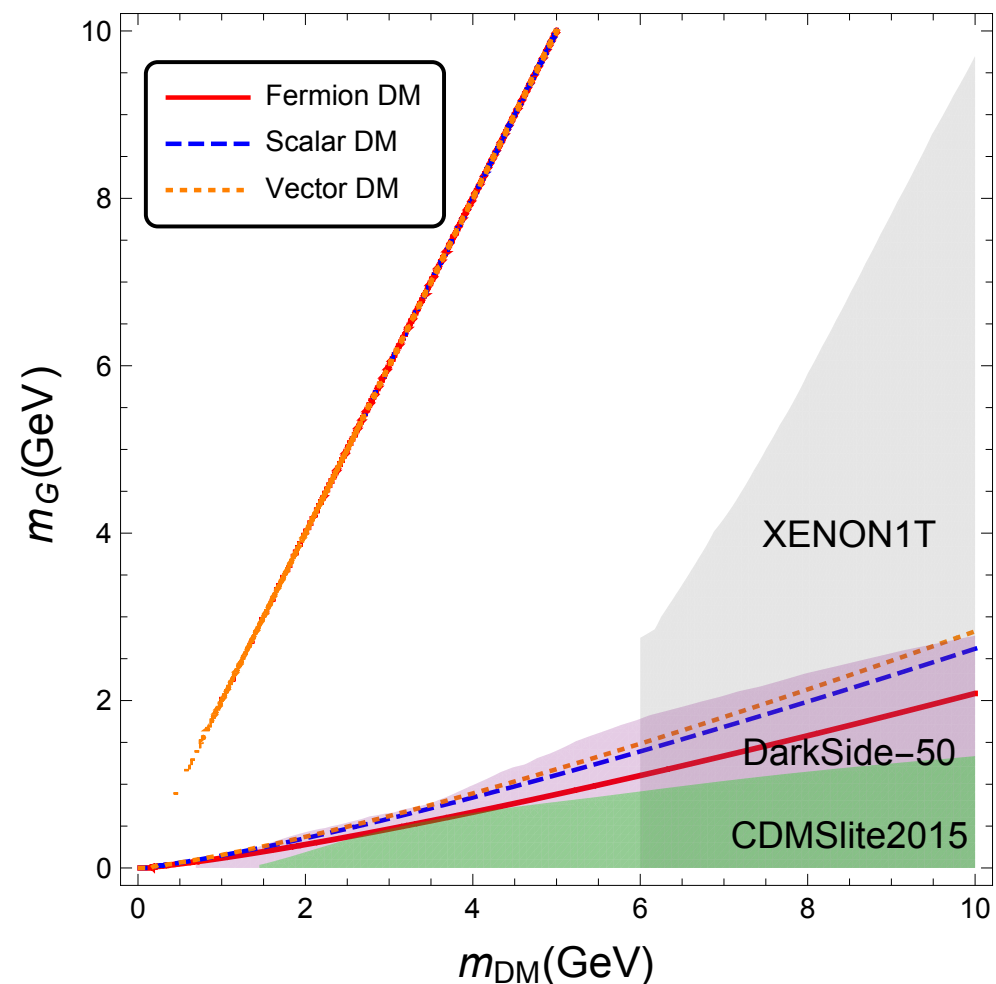
ISR jet + dijet



Dark Matter Relic Density - Light DM

$$m_{\text{DM}} \lesssim 10 \text{ GeV}$$

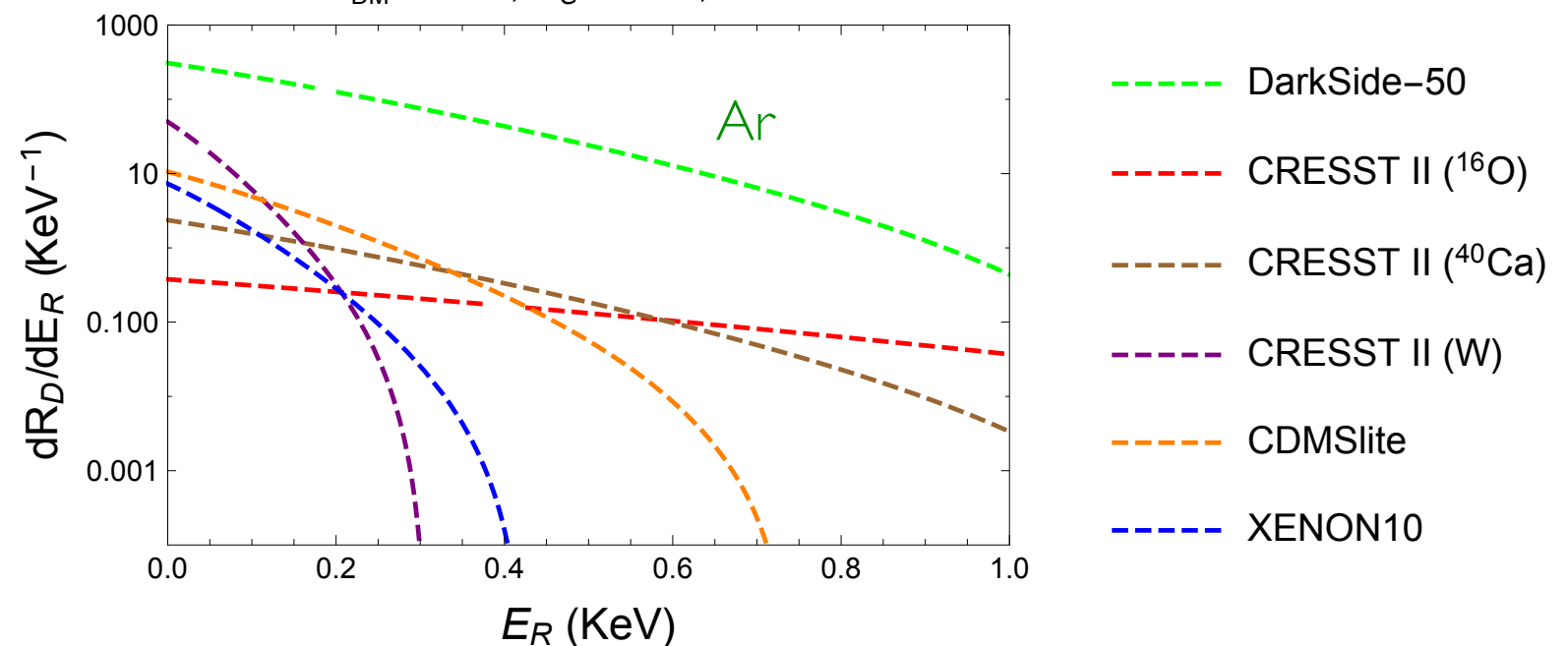
$\Lambda=3 \text{ TeV}, c_\psi=c_\chi=c_S=c_X=1, \Omega h^2=0.1198$



Relic density condition
Mediator resonances become important.

Light dark matter experiments constrain strongly : DarkSide-50, CDMSlite and so on.

$m_{\text{DM}}=2 \text{ GeV}, m_G=4 \text{ GeV}, \Lambda=1 \text{ TeV}$



Differential event rates for fermion DM
in the current direct detection experiments

Summary

- We have introduced the effective operators up to dimension-8 due to the massive spin-2 mediator and the effective Lagrangian using gravitational form factors.
- We show the differential event rates for DM-nucleon scattering via spin-2 mediator.
- The relic density condition is constrained by direct detection and LHC dijet searches.
- When the gluon coupling is sizable, we have to consider gluon contribution - work in progress

Back up

Effective Operators

**Interactions
involving spin-0 or 1 mediator**

$$\begin{aligned}
 \text{LO} \rightarrow \mathcal{O}_1 &= 1_\chi 1_N \\
 \mathcal{O}_2 &= (v^\perp)^2 \\
 \mathcal{O}_3 &= i\vec{S}_N \cdot \left(\frac{\vec{q}}{m_N} \times \vec{v}^\perp\right) \\
 \text{LO} \rightarrow \mathcal{O}_4 &= \vec{S}_\chi \cdot \vec{S}_N \\
 \mathcal{O}_5 &= i\vec{S}_\chi \cdot \left(\frac{\vec{q}}{m_N} \times \vec{v}^\perp\right) \\
 \mathcal{O}_6 &= \left(\vec{S}_\chi \cdot \frac{\vec{q}}{m_N}\right) \left(\vec{S}_N \cdot \frac{\vec{q}}{m_N}\right) \\
 \text{NLO} \left\{ \begin{array}{l} \mathcal{O}_7 = \vec{S}_N \cdot \vec{v}^\perp \\ \mathcal{O}_8 = \vec{S}_\chi \cdot \vec{v}^\perp \end{array} \right.
 \end{aligned}$$

**Other interactions
not involving spin-0 or 1 mediator**

$$\begin{aligned}
 \text{NLO} \rightarrow \mathcal{O}_{12} &= \vec{S}_\chi \cdot (\vec{S}_N \times \vec{v}^\perp) \\
 \mathcal{O}_{13} &= i(\vec{S}_\chi \cdot \vec{v}^\perp) \left(\vec{S}_N \cdot \frac{\vec{q}}{m_N}\right) \\
 \mathcal{O}_{14} &= i\left(\vec{S}_\chi \cdot \frac{\vec{q}}{m_N}\right) (\vec{S}_N \cdot \vec{v}^\perp) \\
 \mathcal{O}_{15} &= -\left(\vec{S}_\chi \cdot \frac{\vec{q}}{m_N}\right) \left((\vec{S}_N \times \vec{v}^\perp) \cdot \frac{\vec{q}}{m_N}\right) \\
 \mathcal{O}_{16} &= -\left((\vec{S}_\chi \times \vec{v}^\perp) \cdot \frac{\vec{q}}{m_N}\right) \left(\vec{S}_N \cdot \frac{\vec{q}}{m_N}\right).
 \end{aligned}$$



$$\mathcal{O}_{16} = \mathcal{O}_{15} + \frac{\vec{q}^2}{m_N^2} \mathcal{O}_{12},$$

Energy-Momentum Tensor

- The energy momentum tensor depends on the **spin** and is function of its **momentums**

Fermion DM $\left(\begin{array}{l} T^{\chi} = -\frac{1}{4}\bar{u}_{\chi}(k_2)\left(-6(\not{k}_1 + \not{k}_2) + 16m_{\chi}\right)u_{\chi}(k_1) \\ \tilde{T}_{\mu\nu}^{\chi} = -\frac{1}{4}\bar{u}_{\chi}(k_2)\left(\gamma_{\mu}(k_{1\nu} + k_{2\nu}) + \gamma_{\nu}(k_{1\mu} + k_{2\mu}) - \frac{1}{2}\eta_{\mu\nu}(\not{k}_1 + \not{k}_2)\right)u_{\chi}(k_1) \end{array} \right.$

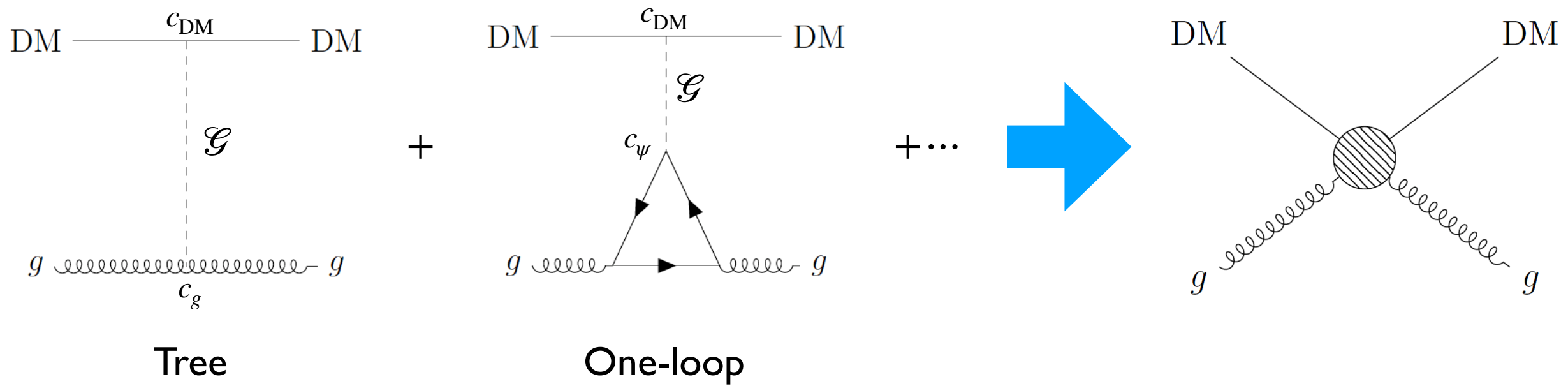
Scalar DM $\left(\begin{array}{l} T^S = -(4m_S^2 - 2(k_1 \cdot k_2)) \\ \tilde{T}_{\mu\nu}^S = -\left(k_{1\mu}k_{2\nu} + k_{2\mu}k_{1\nu} - \frac{1}{2}\eta_{\mu\nu}(k_1 \cdot k_2)\right) \end{array} \right.$ in the momentum space

Vector DM $\left(\begin{array}{l} T^X = 2m_X^2\eta_{\alpha\beta}\epsilon^{\alpha}(k_1)\epsilon^{*\beta}(k_2) \\ \tilde{T}_{\mu\nu}^X = -\left(m_X^2C_{\mu\nu,\alpha\beta} + W_{\mu\nu,\alpha\beta} + \frac{1}{2}m_X^2\eta_{\mu\nu}\eta_{\alpha\beta}\right)\epsilon^{\alpha}(k_1)\epsilon^{*\beta}(k_2) \end{array} \right.$

where $C_{\mu\nu,\alpha\beta} \equiv \eta_{\mu\alpha}\eta_{\nu\beta} + \eta_{\nu\alpha}\eta_{\mu\beta} - \eta_{\mu\nu}\eta_{\alpha\beta}$

$$W_{\mu\nu,\alpha\beta} \equiv -\eta_{\alpha\beta}k_{1\mu}k_{2\nu} - \eta_{\mu\alpha}(k_1 \cdot k_2 \eta_{\nu\beta} - k_{1\beta}k_{2\nu}) + \eta_{\mu\beta}k_{1\nu}k_{2\alpha} - \frac{1}{2}\eta_{\mu\nu}(k_{1\beta}k_{2\alpha} - k_1 \cdot k_2 \eta_{\alpha\beta}) + (\mu \leftrightarrow \nu).$$

Gluon contribution



Trace part : $f_{TG} \approx 1 - \sum_{u,d,s} f_{Tq}$ for scalar current

Trace-free : $\langle N(p) | \tilde{T}_{\mu\nu}^g | N(p) \rangle = \frac{1}{m_N} \left(p_\mu p_\nu - \frac{1}{4} m_N^2 g_{\mu\nu} \right) G(2) \bar{u}_N(p) u_N(p), \quad G(2) = \int_0^1 dx \, x g(x)$

G(2)=0.48 at the m_Z scale using CTEQ parton distribution

DM annihilation cross section

$$S_{\text{DM}} = \frac{1}{2}$$

H. M. Lee, M. Park and V. Sanz (1306.4107)

$$(\sigma v)_{\chi\bar{\chi} \rightarrow \psi\bar{\psi}} = v^2 \cdot \frac{N_c c_\chi^2 c_\psi^2}{72\pi\Lambda^4} \frac{m_\chi^6}{(4m_\chi^2 - m_G^2)^2 + \Gamma_G^2 m_G^2} \left(1 - \frac{m_\psi^2}{m_\chi^2}\right)^{\frac{3}{2}} \left(3 + \frac{2m_\psi^2}{m_\chi^2}\right)$$

$$(\sigma v)_{\chi\bar{\chi} \rightarrow GG} = \frac{c_\chi^4 m_\chi^2}{16\pi\Lambda^4} \frac{(1 - r_\chi)^{\frac{7}{2}}}{r_\chi^4 (2 - r_\chi)^2} \quad r_\chi = \left(\frac{m_G}{m_\chi}\right)^2$$

$$S_{\text{DM}} = 0$$

$$(\sigma v)_{SS \rightarrow \psi\bar{\psi}} = v^4 \cdot \frac{N_c c_S^2 c_\psi^2}{360\pi\Lambda^4} \frac{m_S^6}{(m_G^2 - 4m_S^2)^2 + \Gamma_G^2 m_G^2} \left(1 - \frac{m_\psi^2}{m_S^2}\right)^{\frac{3}{2}} \left(3 + \frac{2m_\psi^2}{m_S^2}\right)$$

$$(\sigma v)_{SS \rightarrow GG} = \frac{4c_S^4 m_S^2}{9\pi\Lambda^4} \frac{(1 - r_S)^{\frac{9}{2}}}{r_S^4 (2 - r_S)^2} \quad r_S = \left(\frac{m_G}{m_S}\right)^2$$

$$S_{\text{DM}} = 1$$

s-wave → constrained by indirect detection

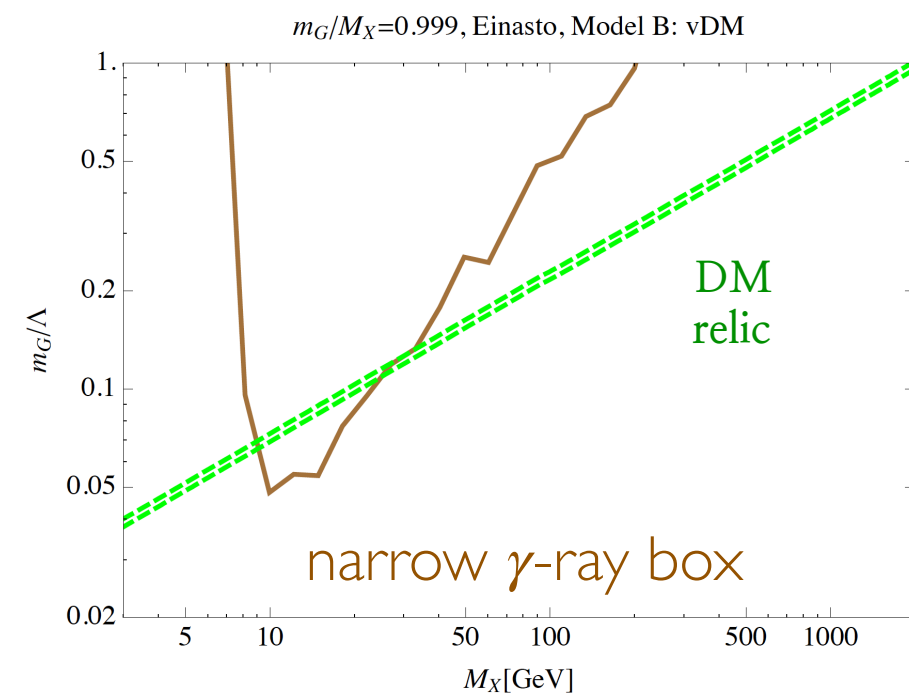
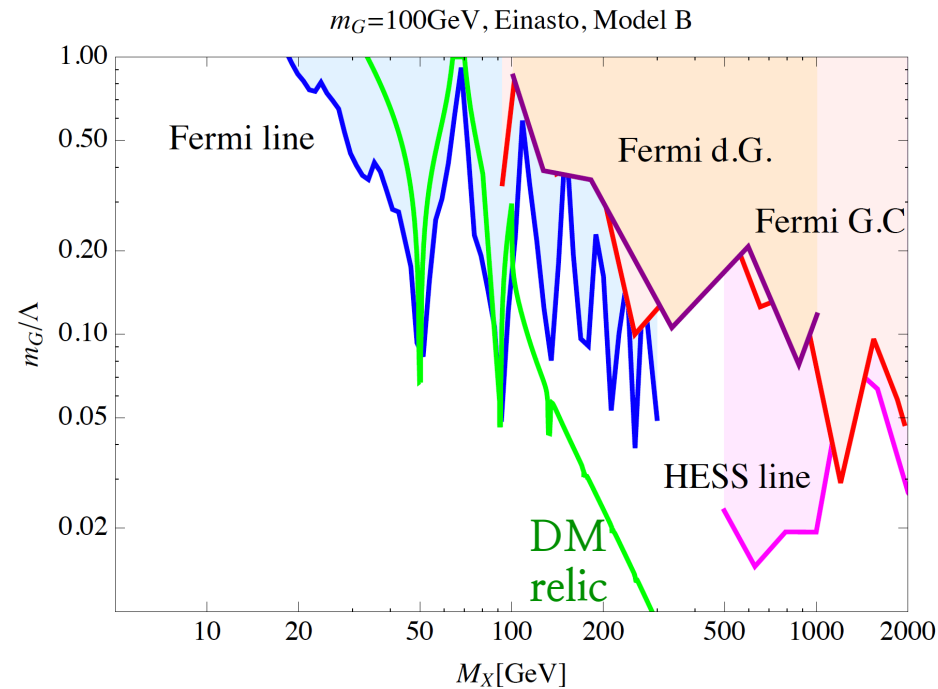
$$(\sigma v)_{XX \rightarrow \psi\bar{\psi}} = \frac{4N_c c_X^2 c_\psi^2}{27\pi\Lambda^4} \frac{m_X^6}{(4m_X^2 - m_G^2)^2 + \Gamma_G^2 m_G^2} \left(1 - \frac{m_\psi^2}{m_X^2}\right)^{\frac{3}{2}} \left(3 + \frac{2m_\psi^2}{m_X^2}\right) \quad r_X = \left(\frac{m_G}{m_X}\right)^2$$

$$(\sigma v)_{XX \rightarrow GG} = \frac{c_X^4 m_X^2}{324\pi\Lambda^4} \frac{\sqrt{1 - r_X}}{r_X^4 (2 - r_X)^2} \left(176 + 192r_X + 1404r_X^2 - 3108r_X^3 + 1105r_X^4 + 362r_X^5 + 34r_X^6\right)$$

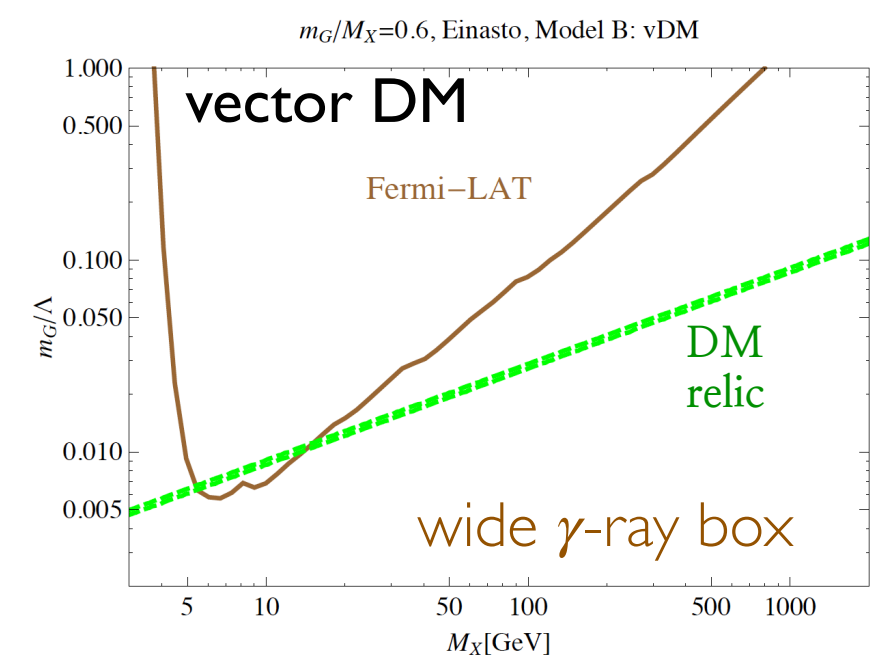
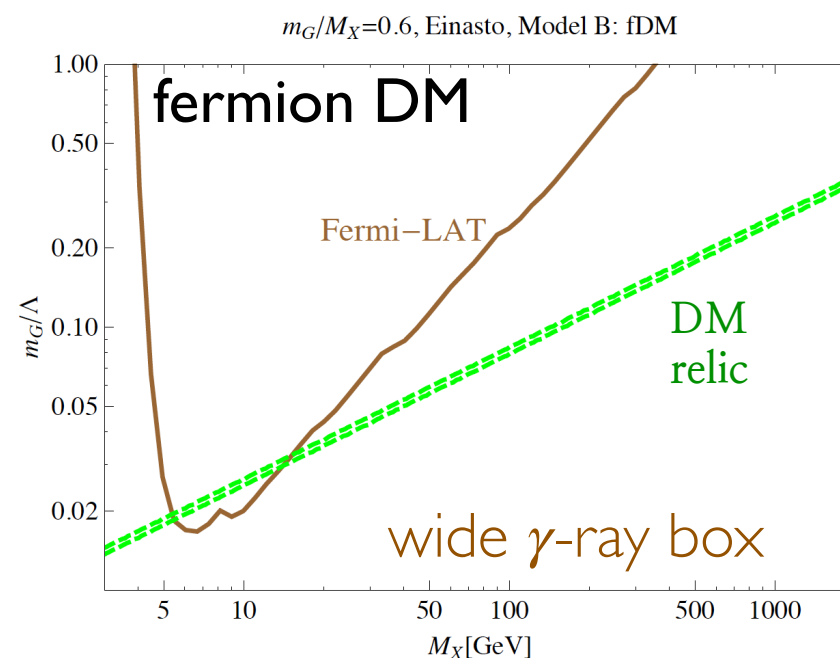
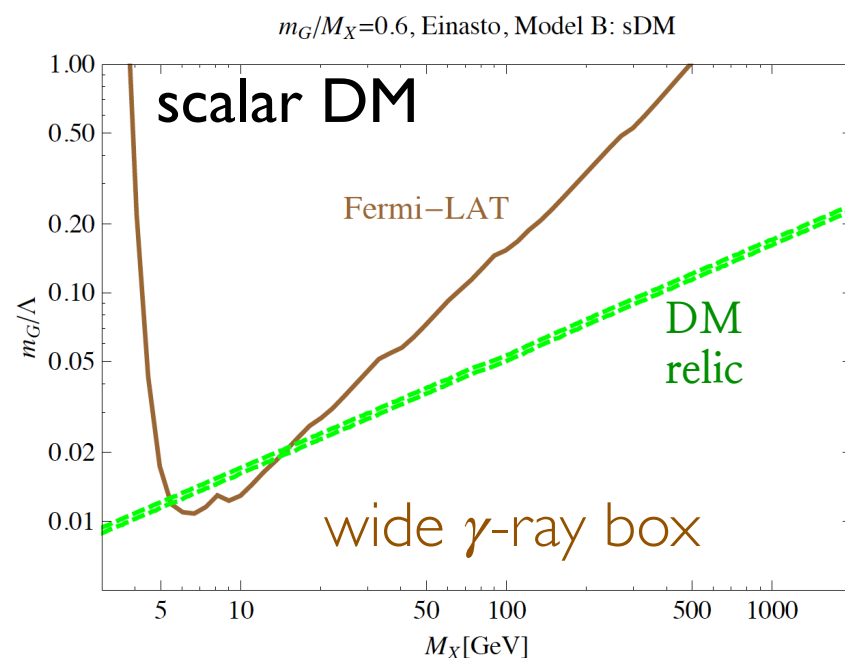
Indirect Detection

H. M. Lee, M. Park and V. Sanz (1401.5301)

vector DM



Astrophysical bounds are DM spin-dependent.
Therefore, we can distinguish DM spins from Indirect detection.



Spin-dependent cross section

- WIMP model-independent formula

$$\sigma_p^{\text{lim(A)}} = \sigma_A^{\text{lim}} \frac{\mu_p^2}{\mu_A^2} \frac{1}{C_A^p/C_p}, \quad \sigma_n^{\text{lim(A)}} = \sigma_A^{\text{lim}} \frac{\mu_n^2}{\mu_A^2} \frac{1}{C_A^n/C_n}$$

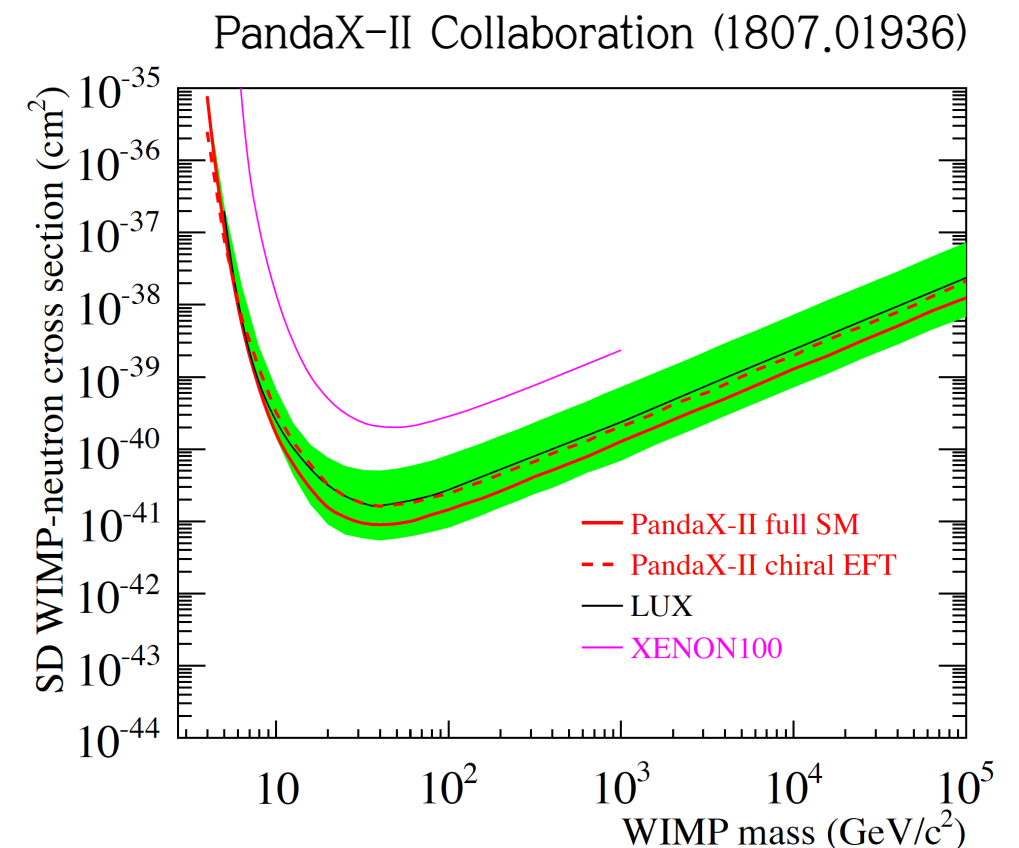
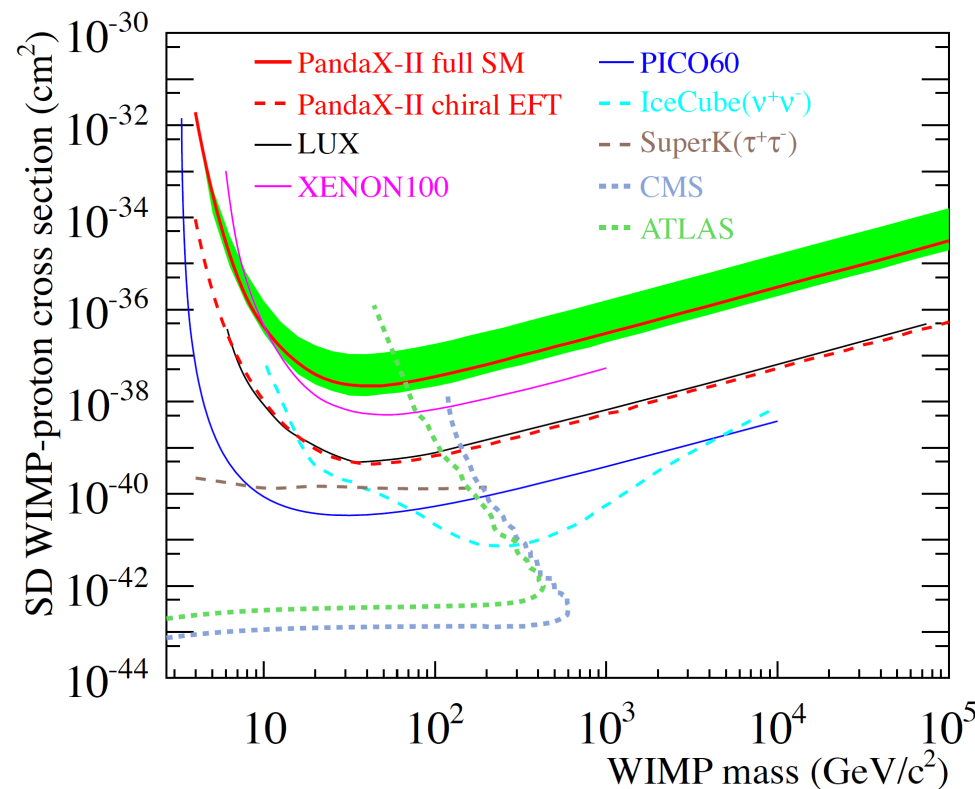
with assuming that $\sigma_A \simeq \sigma_A^n$ and $\sigma_A \simeq \sigma_A^p$

$$\text{where } \frac{C_A^p}{C_p} = \frac{4}{3} \langle S_p \rangle^2 \frac{J+1}{J}, \quad \frac{C_A^n}{C_n} = \frac{4}{3} \langle S_n \rangle^2 \frac{J+1}{J}$$

P. Gondolo et al (hep-ph/0005041)

Nucleus	Z	J	$\langle S_p \rangle$	$\langle S_n \rangle$	C_A^p/C_p	C_A^n/C_n
^{19}F	9	1/2	0.477	-0.004	9.10×10^{-1}	6.40×10^{-5}
^{23}Na	11	3/2	0.248	0.020	1.37×10^{-1}	8.89×10^{-4}
^{73}Ge	32	9/2	0.030	0.378	1.47×10^{-3}	2.33×10^{-1}
^{127}I	53	5/2	0.309	0.075	1.78×10^{-1}	1.05×10^{-2}
^{129}Xe	54	1/2	0.028	0.359	3.14×10^{-3}	5.16×10^{-1}
^{131}Xe	54	3/2	-0.009	-0.227	1.80×10^{-4}	1.15×10^{-1}

^{27}Al , ^{29}Si , ^{35}Cl , ^{39}K , ^{93}Nb , ^{125}Te also ...



Inelastic scattering

L. Baudis et al (1309.0825)

- Start from energy, momentum conservation for WIMP-nucleus scattering

$$\frac{q_i^2}{2m_\chi} = \frac{q_f^2}{2m_\chi} + E_R + E^*, \quad \vec{q} = \vec{q}_i - \vec{q}_f \quad \text{with} \quad E_R = \frac{q^2}{2m_A}.$$



WIMP initial,
final momentum

$$q^2 - (2\mu_A v_i \cos \beta)q + 2\mu_A E^* = 0 \quad \text{with} \quad v_i = \frac{q_i}{m_\chi} \quad \text{and} \quad \beta \text{ is the angle between } q_i, q$$

- From the solution, we can derive the minimum and maximum recoil energy.

$$E_{R,\min(\max)} = \frac{(\mu_A v_i)^2}{2m_A} \left(1 \mp \sqrt{1 - \frac{2E^*}{\mu_A v_i^2}} \right)^2, \quad v_{\min} = \sqrt{2E^*/\mu_A}$$

- Experiments can search for a total energy deposition, $E_{\text{obs}} = f(E_R) \times E_R + E^*$

$f(E_R)$ is an energy-dependent quenching factor for nuclear recoils.

Only this fraction of the nuclear recoil energy will be transferred to electronic excitations.

- Therefore, we need to calculate $\frac{dR_D}{dE_{\text{obs}}}$ instead of $\frac{dR_D}{dE_R}$.