

SOGRO: Superconducting Tensor Gravitational Wave Detector for Mid-Frequencies

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Outline

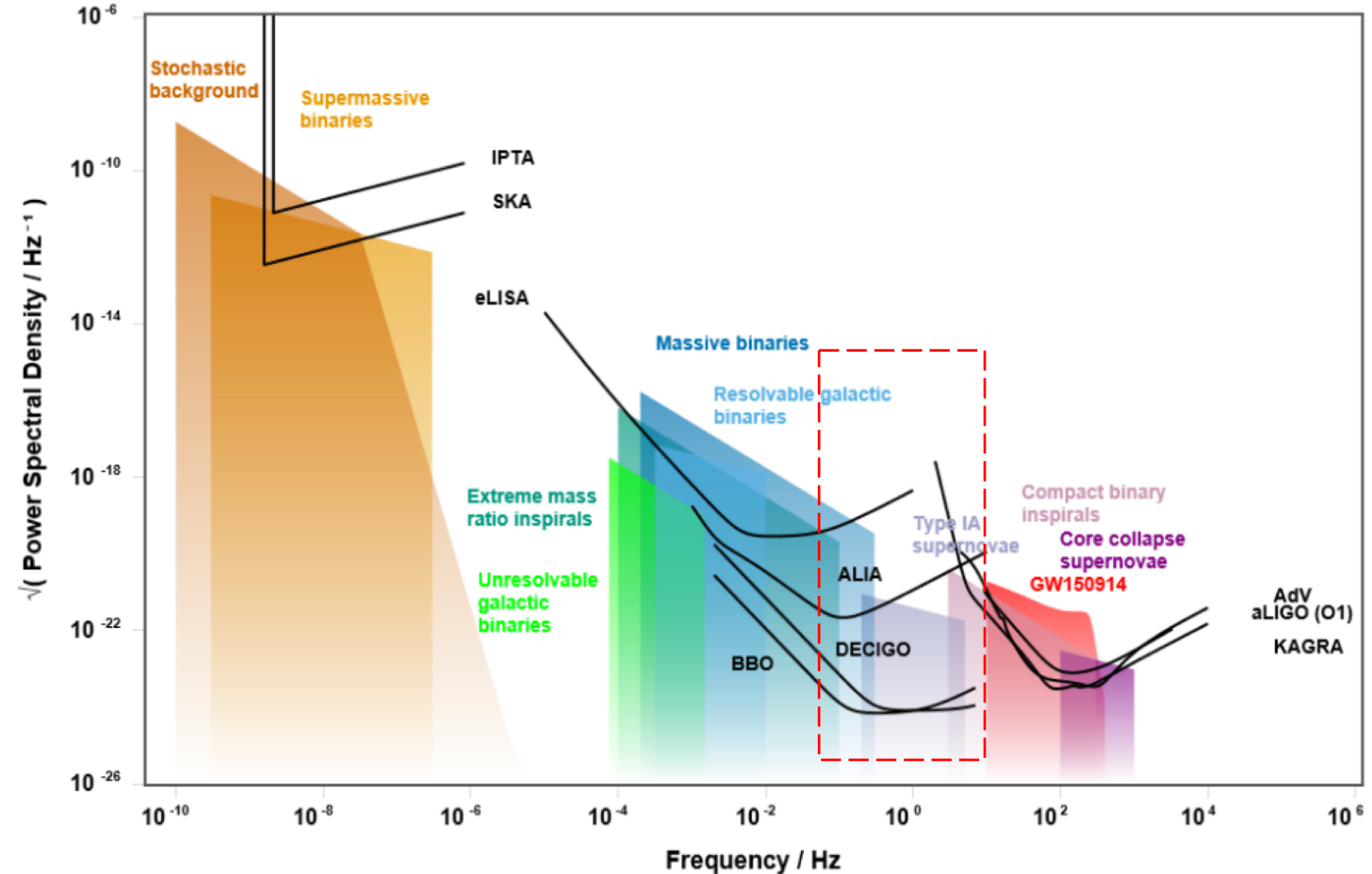
- I. Introduction
- II. Design and Principle
- III. Detector Sensitivity
- IV. Science with SOGRO
- V. Summary and Outlook

I. Introduction

- Detections of GWs in LIGO:
 - 5 BBH & 1 BNS events
- Plans to improve sensitivity:
 - A+ (~22), Voyager (~25), Einstein Telescope (~23), Cosmic Explorer (~27), AAGO, TAIJI, TianQin, etc.
- **Covers 10~1000 Hz only!**
- Multi-wavelength GW astronomy
- Mid-Frequencies (0.1~10 Hz):
 - Space: DECIGO ('01), BBO, ALIA, AMIGO
 - Ground: TOBA ('10), MIGA, ZAIGA

+ **"SOGRO" (~'13)**

✓ Gravitational wave spectrum:

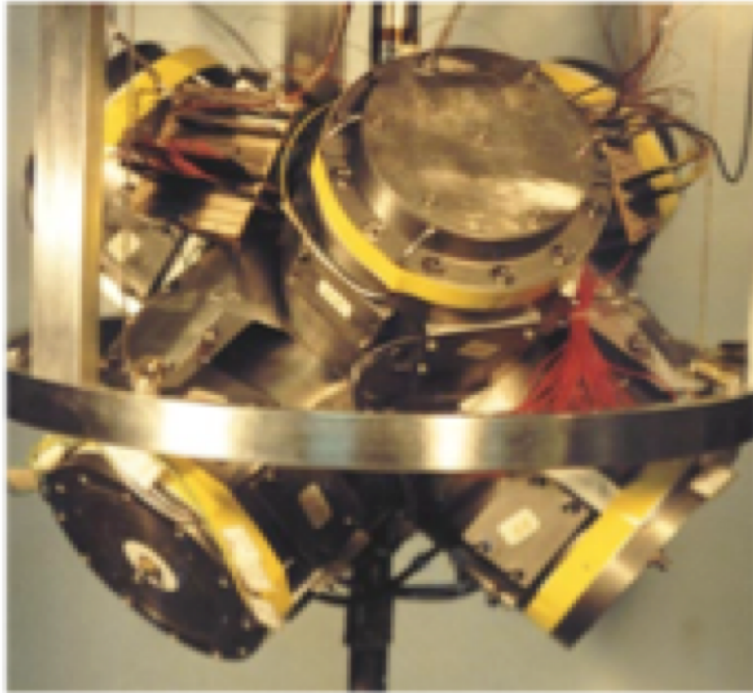


Based on <http://rhcole.com/apps/GWplotter/> by Moore, Cole & Berry

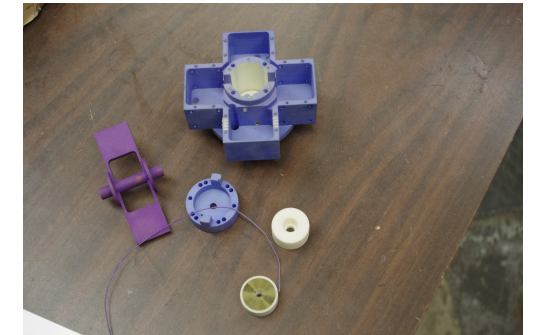
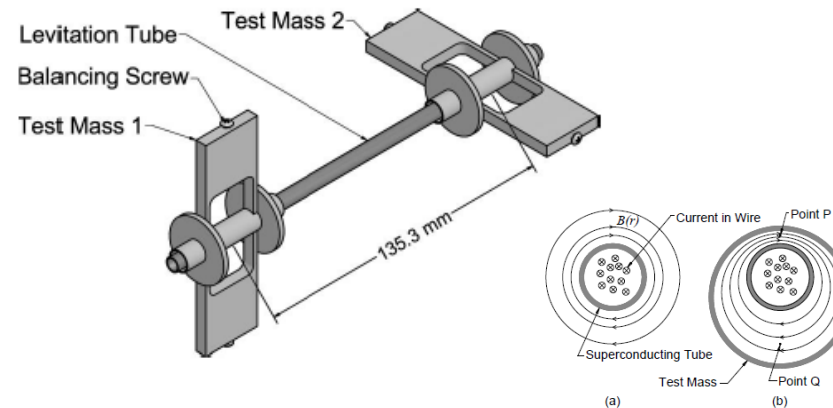
✓ History of SOGRO:

- Wagoner, Will & Paik: 1979
- Superconducting Gravity Gradiometer (SGG):

Ho Jung Paik



Moody, Paik, & Caravan (2002)

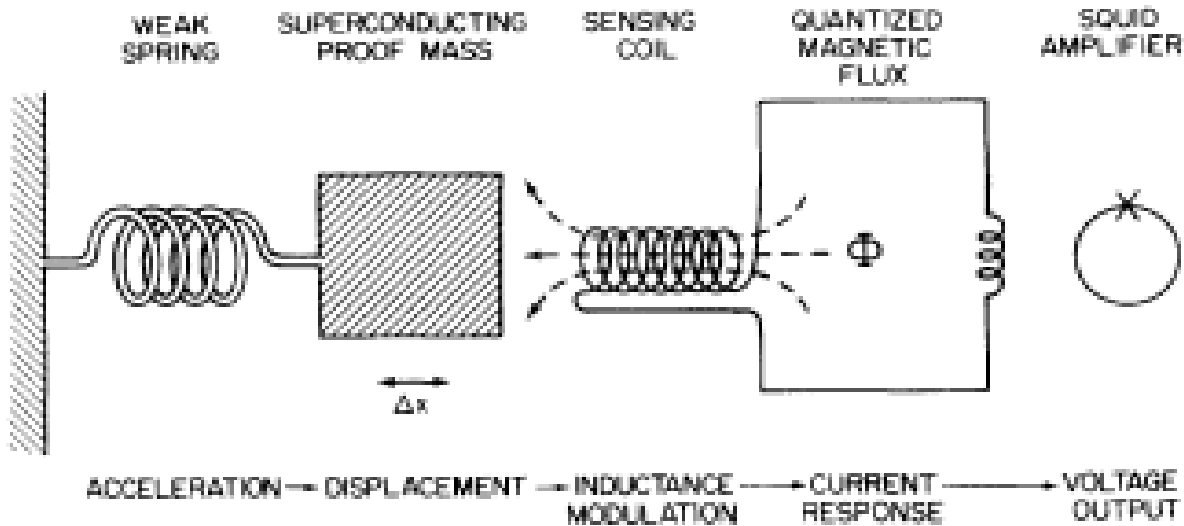


(Picture credit: H-M. Lee)

- ✓ Measure the relative motion of test masses
- ✓ Magnetic levitation, SQUID sensor
- ✓ Test mass: 25 kg, Size: ~15 cm
- ✓ Sensitivity: $\sim 2 \times 10^{-11} s^{-2} Hz^{-1/2}$
- ✓ Developed for over 30 years at U. of Maryland

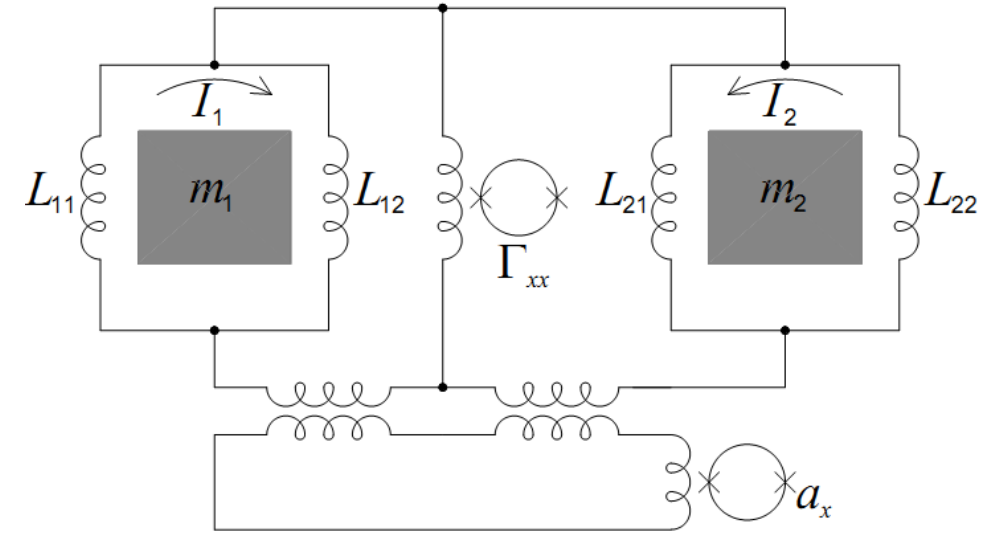
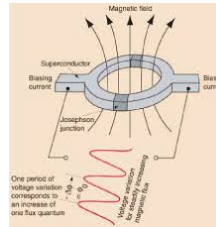
II. Design and Principle

✓ **Basic principle:** Chan & Paik ('87)

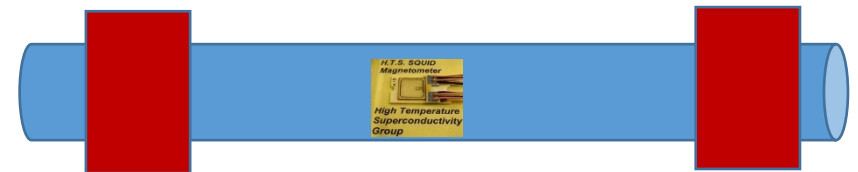


Test mass motion

- ➔ Induced current at sensing coil
- ➔ Measure flux at SQUID

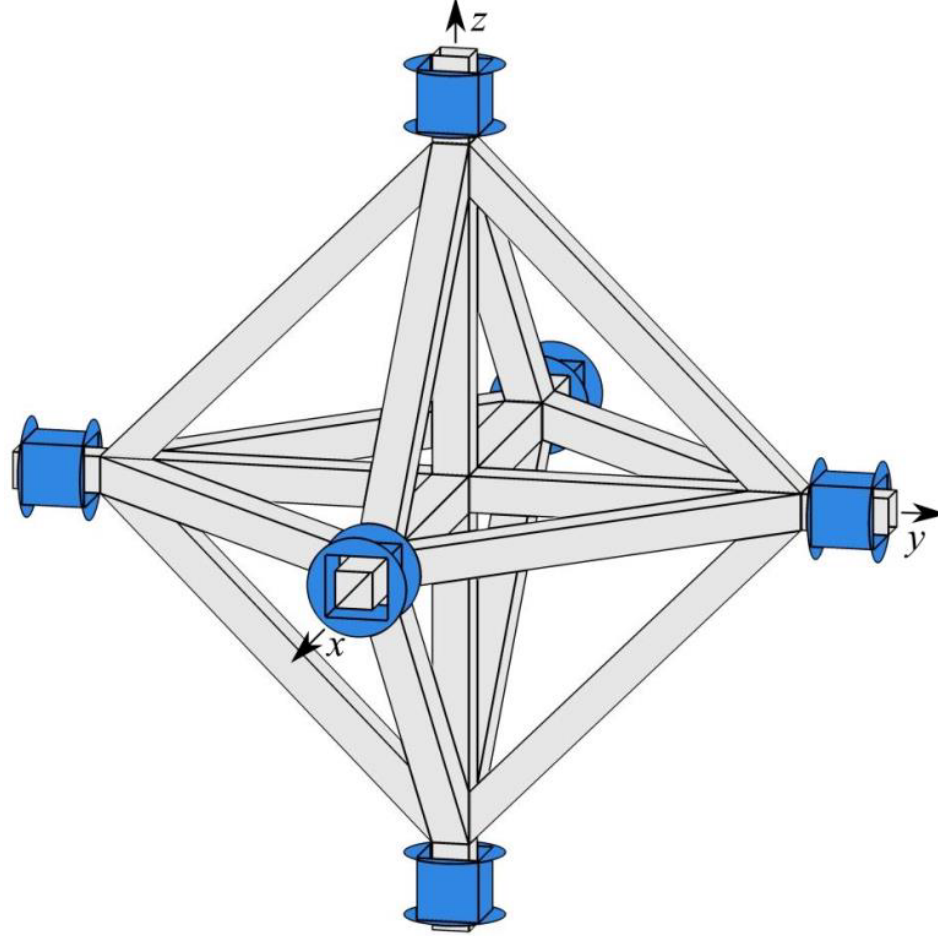
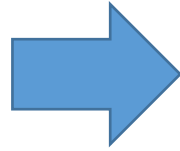
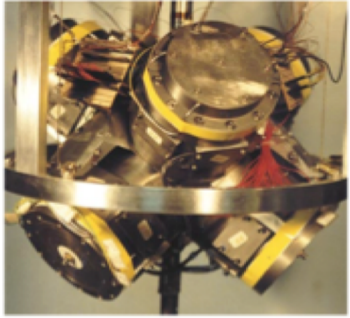


➔ **Sensitive to relative motions only!!**



- Sensing coils & SQUIDs are mounted on the rigid stick.
- Two masses are freely moving.

✓ Platform design:



- Combining 6 test masses, a tensor GW detector is formed;

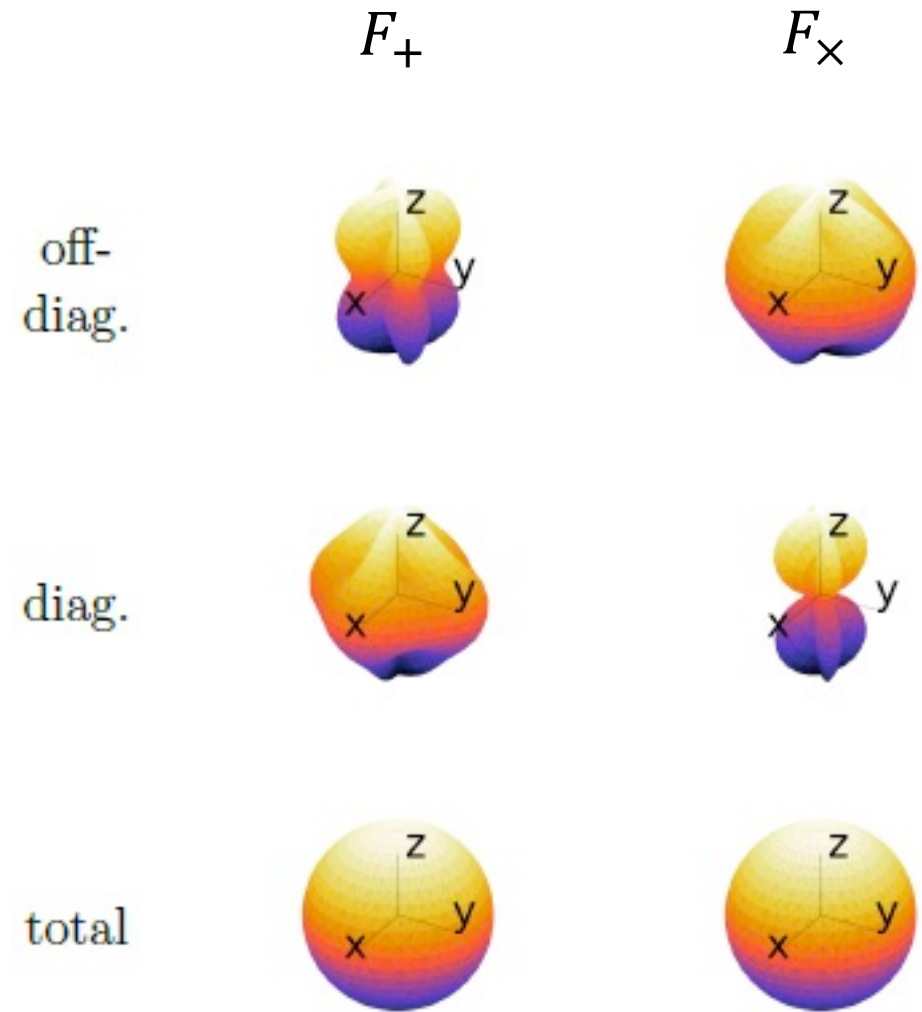
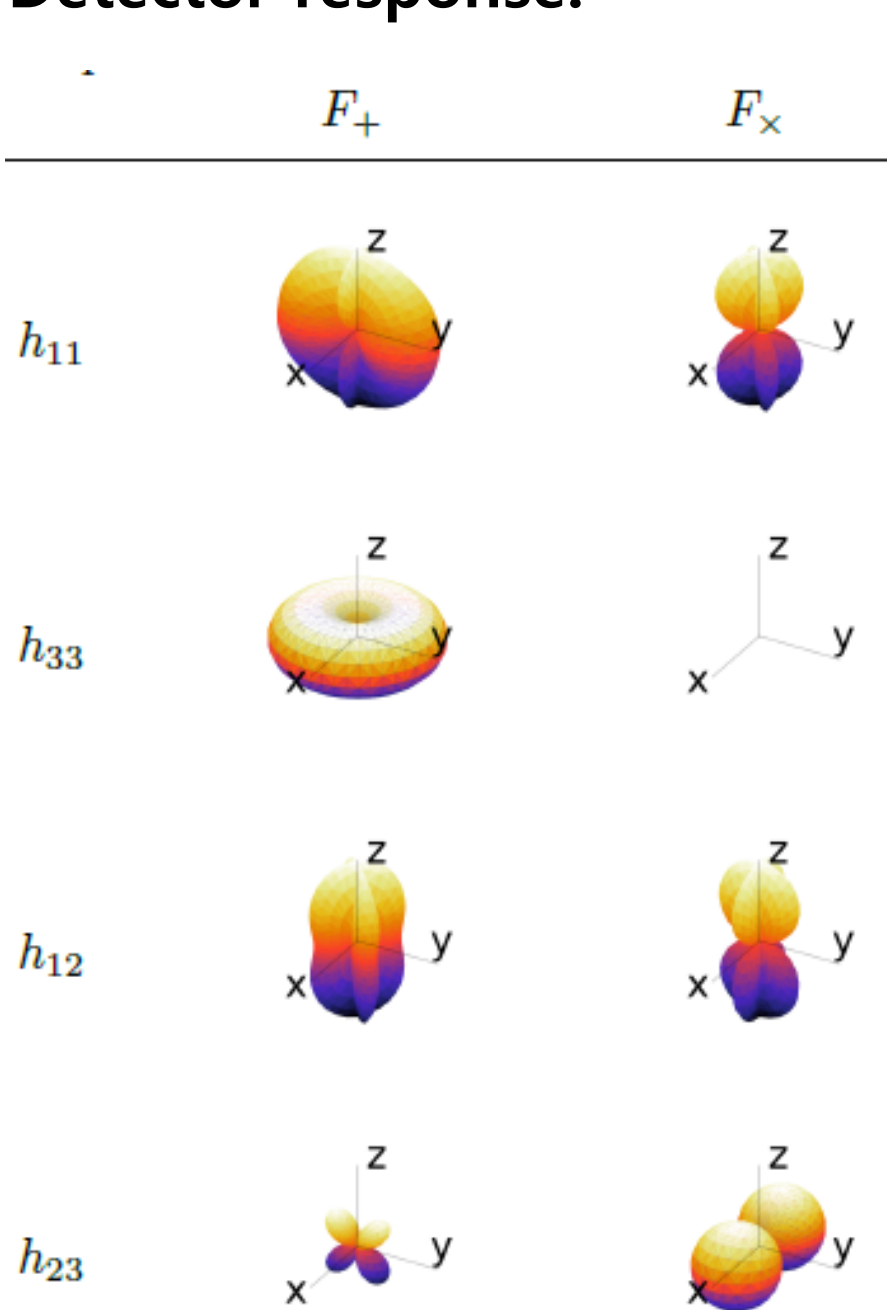
$$h_{ii}(t) = \frac{2}{L} [x_{+ii}(t) - x_{-ii}(t)]$$

$$h_{ij}(t) = \frac{1}{L} \left\{ [x_{+ij}(t) - x_{-ij}(t)] - [x_{-ji}(t) - x_{+ji}(t)] \right\}, i \neq j$$

➔ "Diagonal" channel, "In-line component", or
XX mode

➔ "Off-diagonal" channel, "Cross component",
or XY mode

✓ Detector response:

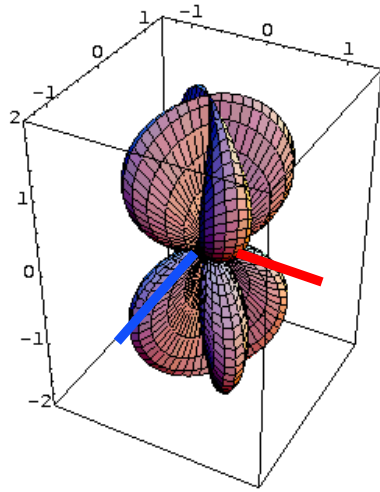


➔ NO LOSS OF INFORMATION
IN SOGRO!

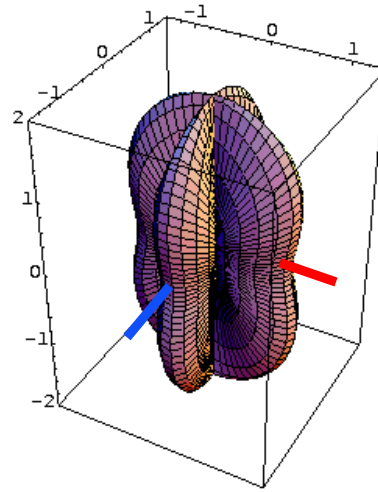
Antenna pattern

LIGO

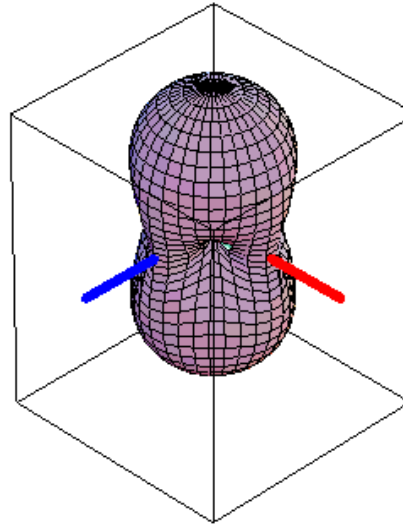
× polarization



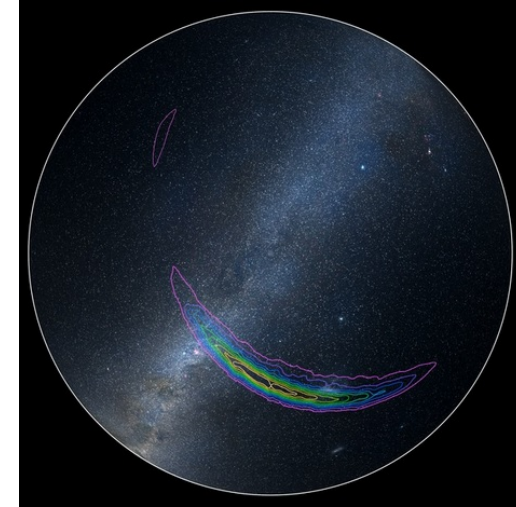
+ polarization



rms sensitivity

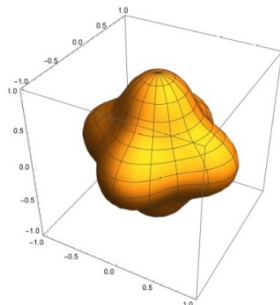


Sky location of GW150914

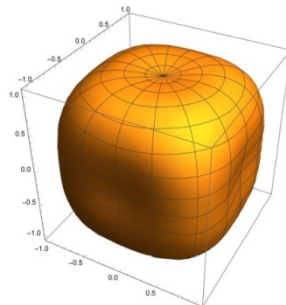


SOGRO

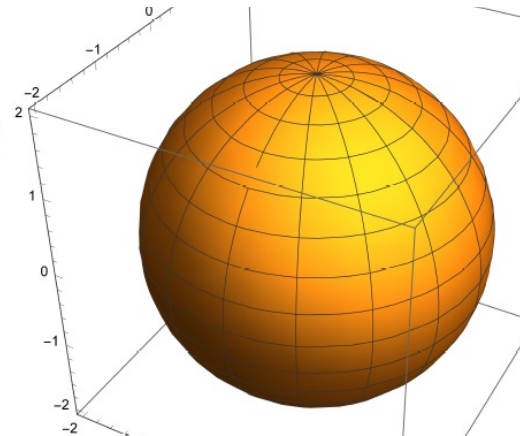
Diagonal



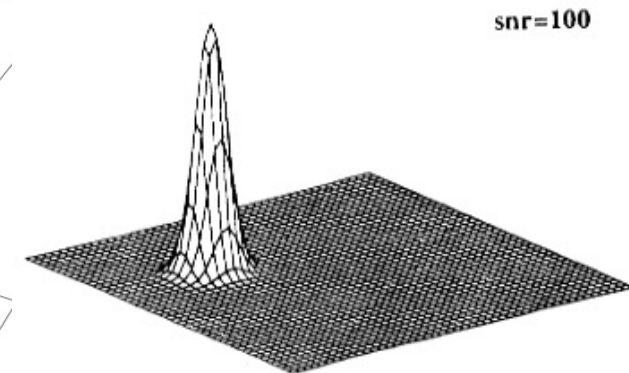
Off-diagonal



Total



Sky location by SOGRO

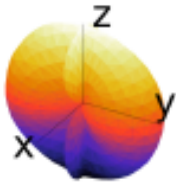
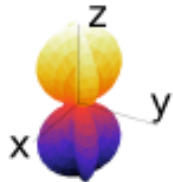
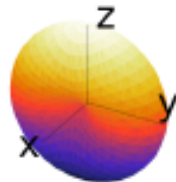
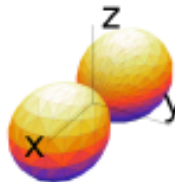
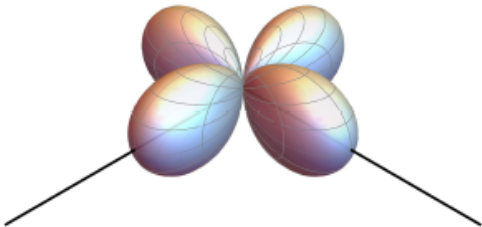
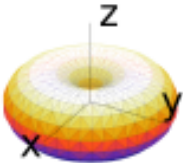
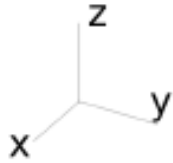
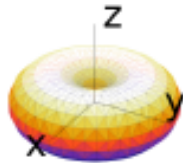
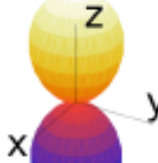
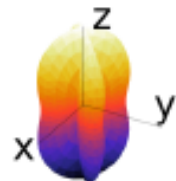
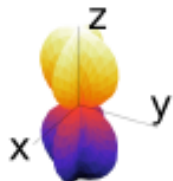
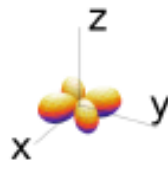
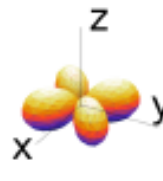
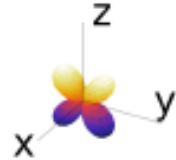
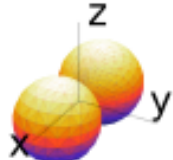
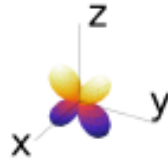
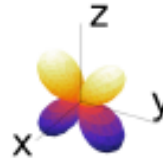


(Slide credit: Paik '16)

- Thus, the source direction (θ, ϕ) and GW polarizations can be determined by a single antenna.

➔ “Spherical Antenna”

- **SOGRO**: Superconducting **O**mnidirectional
Gravitational **R**adiation **O**bservatory

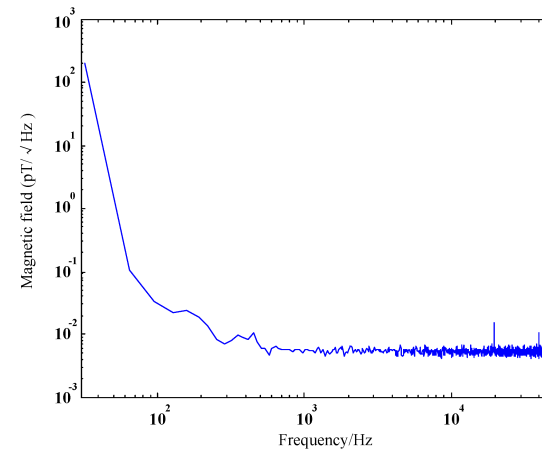
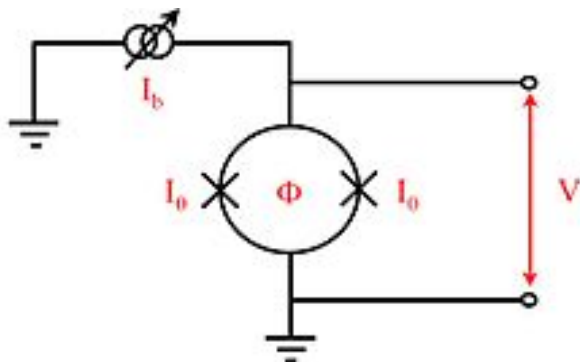
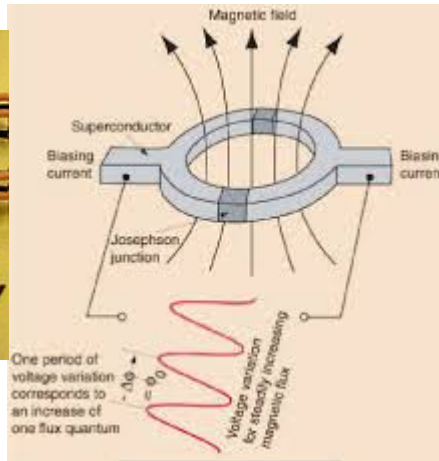
Comp.	Tensor modes		Scalar modes (in alternative gravity theories)		
	F_+	F_\times	F_b	F_ℓ	
h_{11}					 <p>✓ Degeneracy for Breathing and Longitudinal modes in LIGO: Isi, Pitkin & Weinstein ('17)</p> <p>✓ LIGO $\equiv h_{11} - h_{22}$</p>
h_{33}					
h_{12}					
h_{23}					

III. Detector Sensitivity

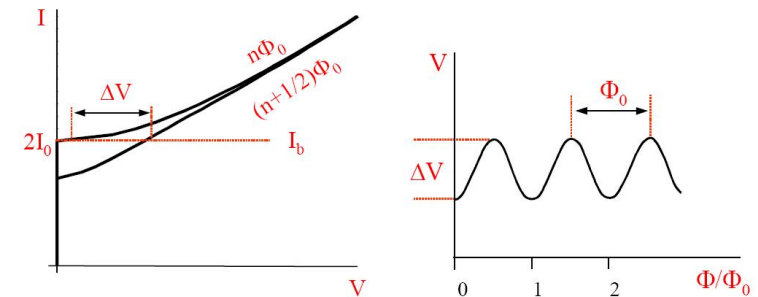
✓ **Variance:** $\Delta L \sim 10^{-20} \times 50m = 5 \times 10^{-19} m$

✓ **SQUID**

"SQUIDs are sensitive enough to measure [fields](#) as low as 5 [aT](#) ($5 \times 10^{-18} T$) with a few days of averaged measurements. Their noise levels are as low as $3 \text{ fT} \cdot \text{Hz}^{-1/2}$."



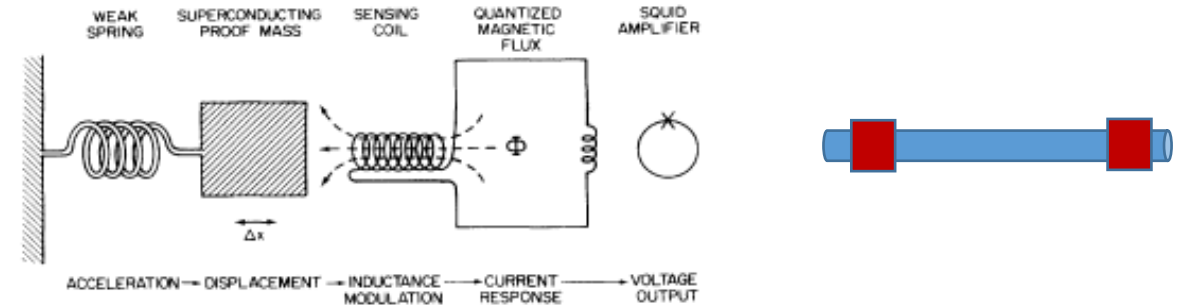
$$\Delta V = \frac{R}{L} \cdot \Delta \Phi$$



From Wikipedia

✓ Main noise sources:

- Antenna noise: Test mass
- Amplifier noise: SQUID



$$S_h(f) = \frac{32}{ML^2\omega^4} \left\{ \frac{k_B T \omega_D}{Q_D} + \frac{|\omega^2 - \omega_D^2|}{2\omega_p} \left(1 + \frac{1}{\beta^2} \right)^{1/2} k_B T_N \right\}, \quad k_B T_N = n\hbar\omega_p$$

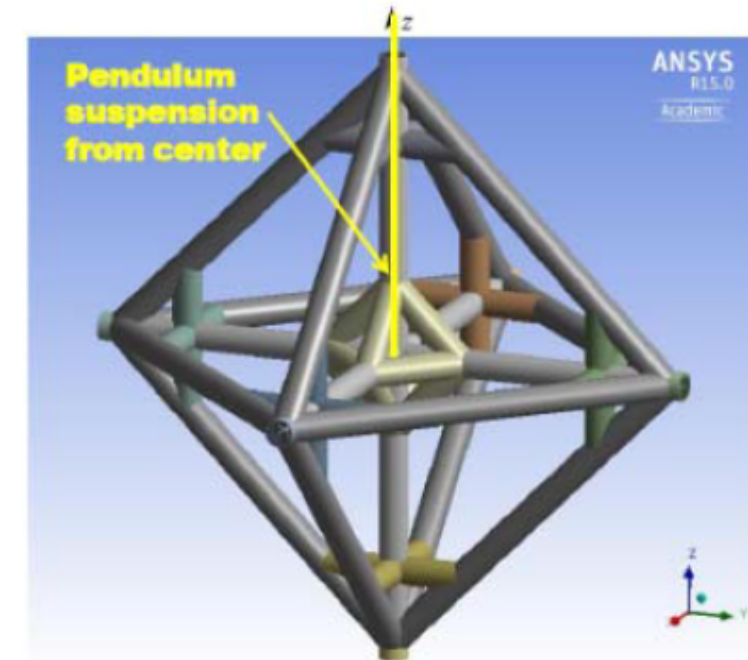
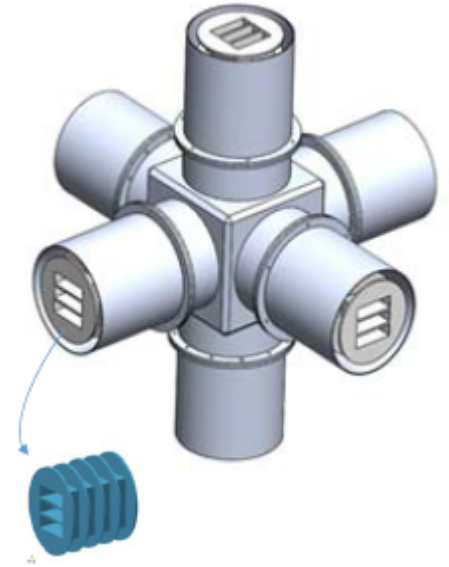
- Platform thermal noise

$$S_{\xi, \omega_0}(f) = \frac{16}{m_{\text{eff}} L^2 \omega_0^2 Q_{\text{pl}} \omega} \frac{4k_B T_{\text{pl}}}{(1 - \omega^2/\omega_0^2)^2 + 1/Q_{\text{pl}}^2}. \quad S_{\xi}(f) = \sum_i S_{\xi, \omega_{0i}}(f)$$

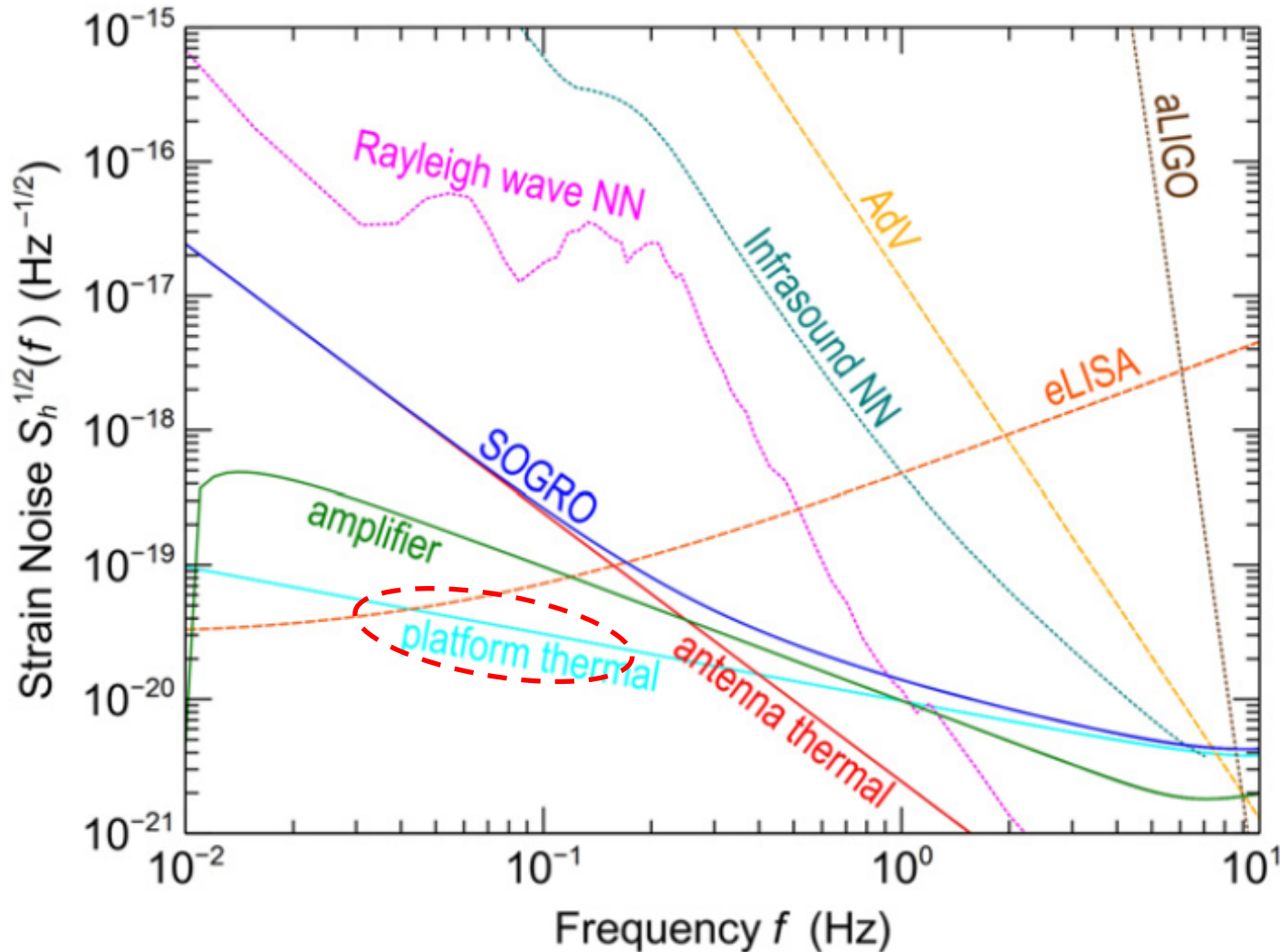
- Newtonian noise

✓ Design parameters:

Parameter	pSOGRO	aSOGRO	Method employed
Each test mass M	100 kg	5 ton	Multiple-layer Nb shell
Arm-length L	2 m	50 m	Rigid platform
Antenna temperature T	0.1 K	0.1 K	He ³ – He ⁴ dilution refrigerator
Platform temperature T_{pl}	0.1 K	4.2 K	Large cryogenic chamber and cooling system
Platform quality factor Q_{pl}	10^6	10^7	Al platform structure
DM frequency f_D	0.01 Hz	0.01 Hz	Magnetic levitation (horizontal only)
DM quality factor Q_D	10^8	10^8	Surface polished pure Nb
Pump frequency f_p	50 kHz	50 kHz	Tuned capacitor bridge transducer
Amplifier noise no. n	5	2	Two-stage dc SQUID
Detector noise $S_h^{1/2}(f)$	$8 \times 10^{-19} \text{ Hz}^{-1/2}$	$4.5 \times 10^{-21} \text{ Hz}^{-1/2}$	Best sensitivity at 1Hz

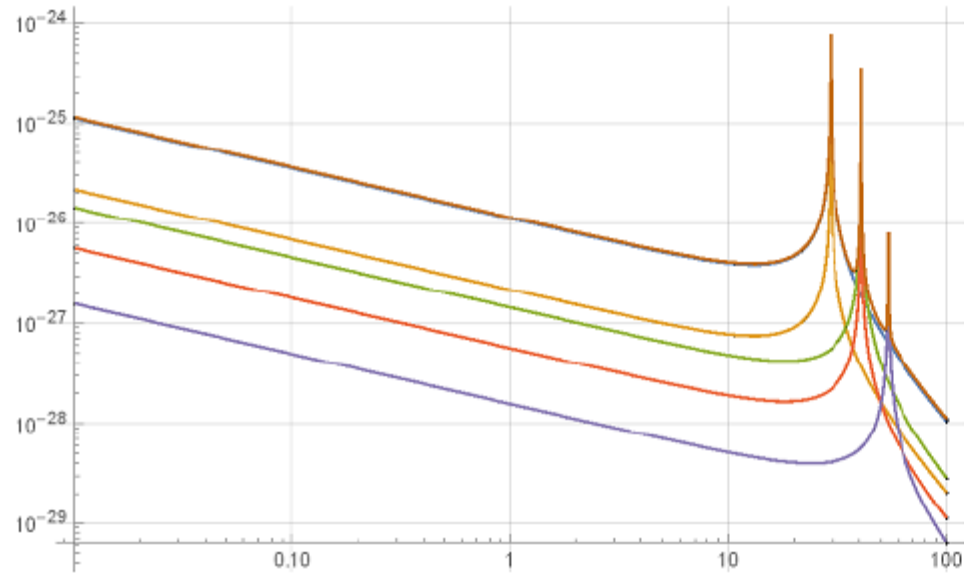


✓ Noise budget:

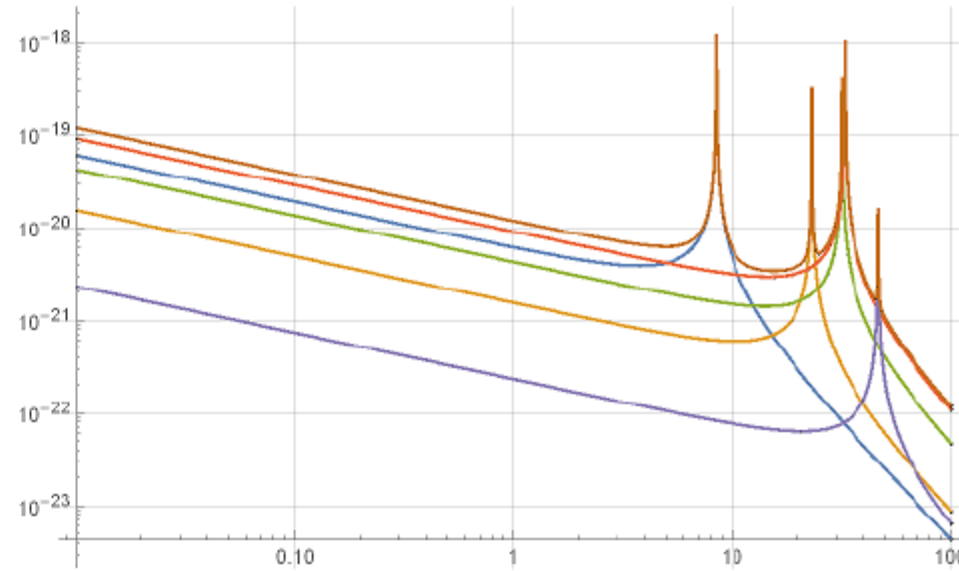


- Understanding its characteristic features is essential for designing the whole experiments.
- Goal: Find out the optimal design(s) for the platform which satisfies (all) desired requirements.
- So, we have investigated the thermal noise features of various SOGRO platforms, and report some preliminary results.

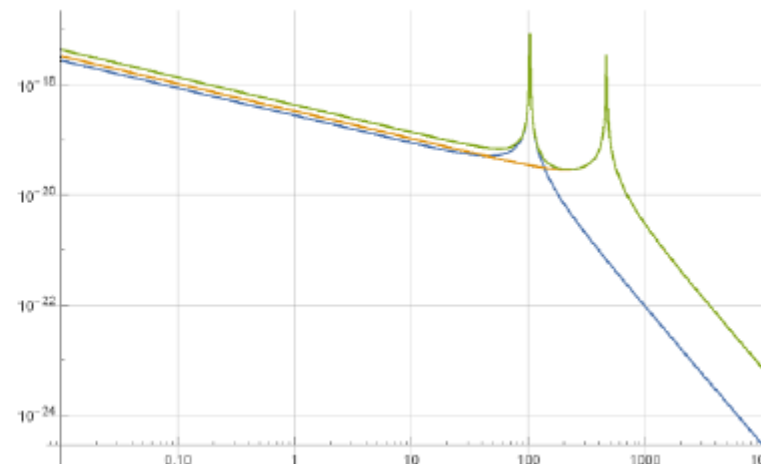
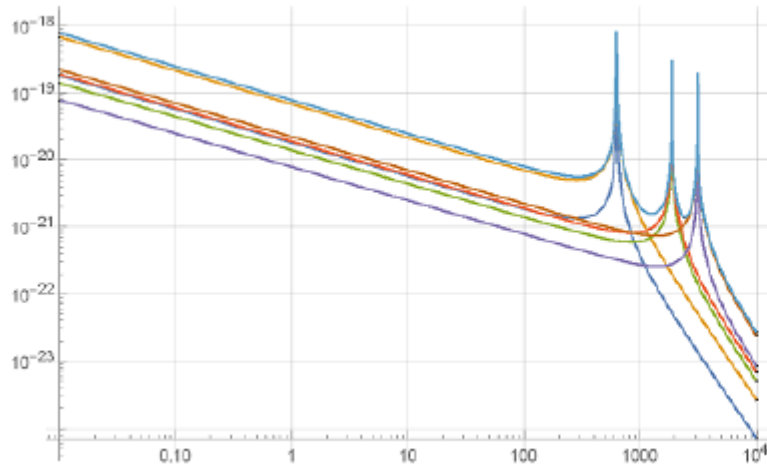
✓ Platform strain noise: Pre-stressed modal analyses using ANSYS



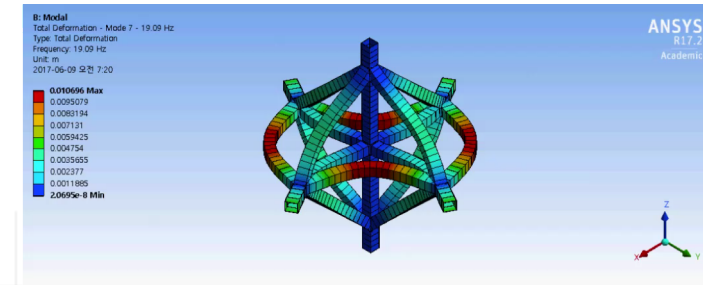
XX-Modes



XY-Modes



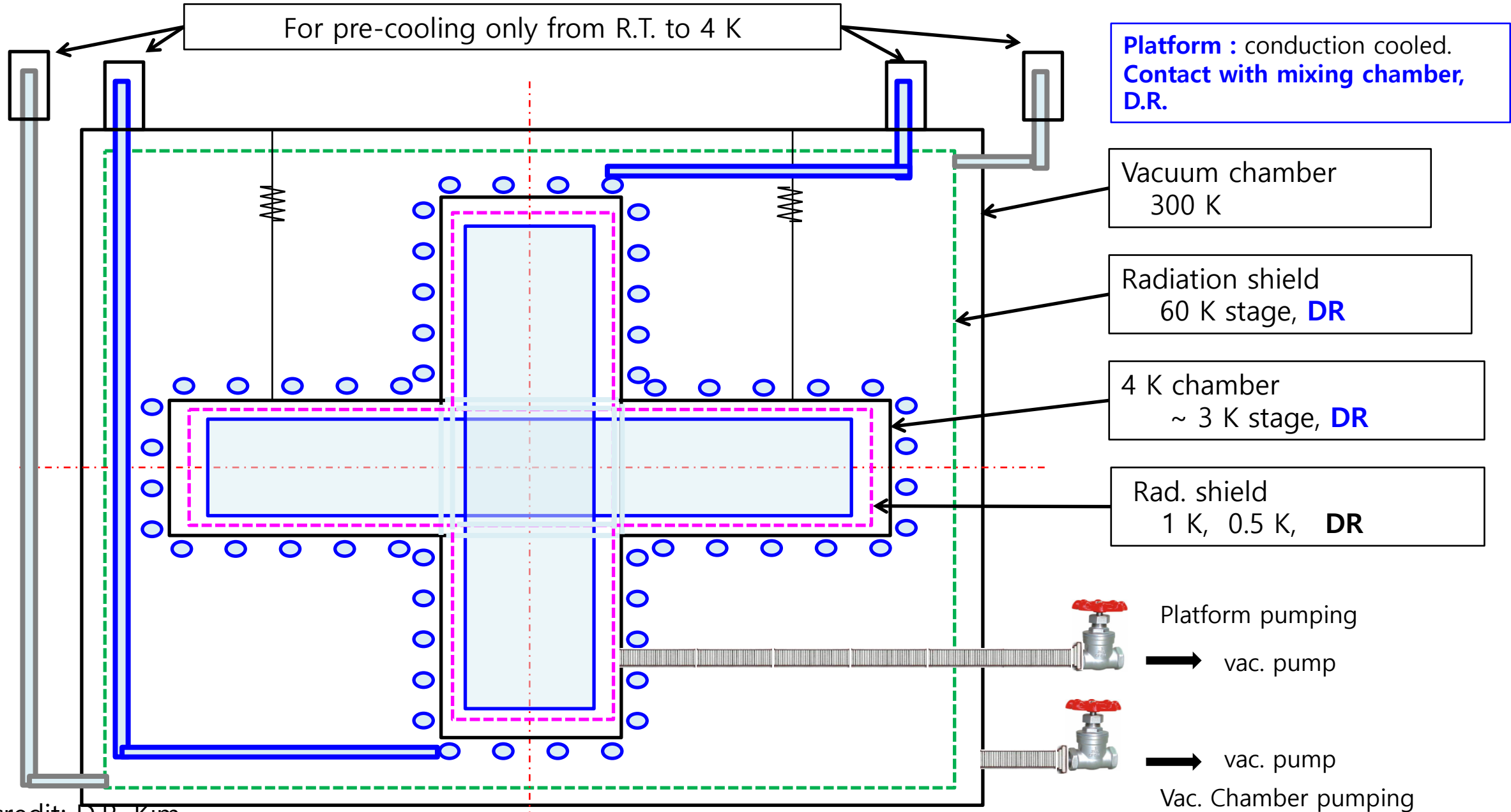
aSOGRO



Mode 7 @ 19.09Hz : Scissor mode

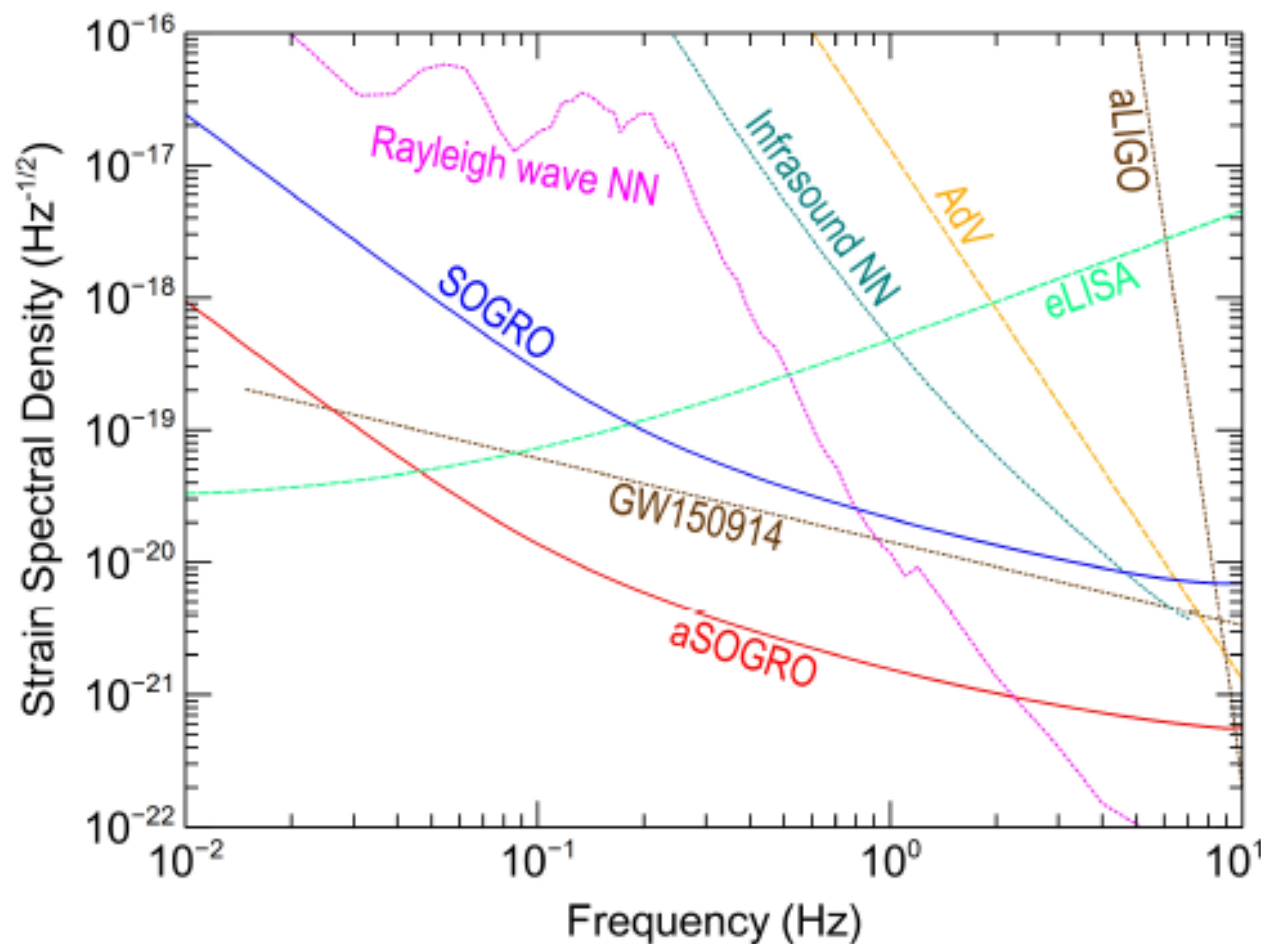
pSOGRO

✓ Concept for Cooling SOGRO System – 2nd Stage : 0.1 K

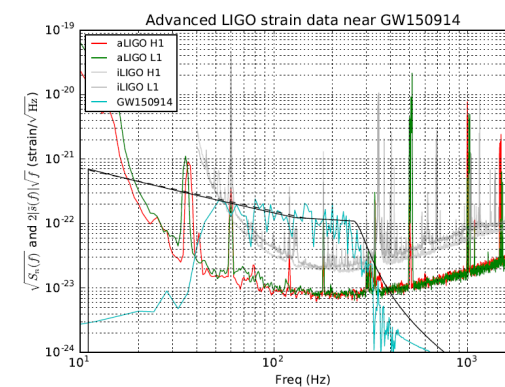


IV. Science with SOGRO

1) Inspiralling BBH:

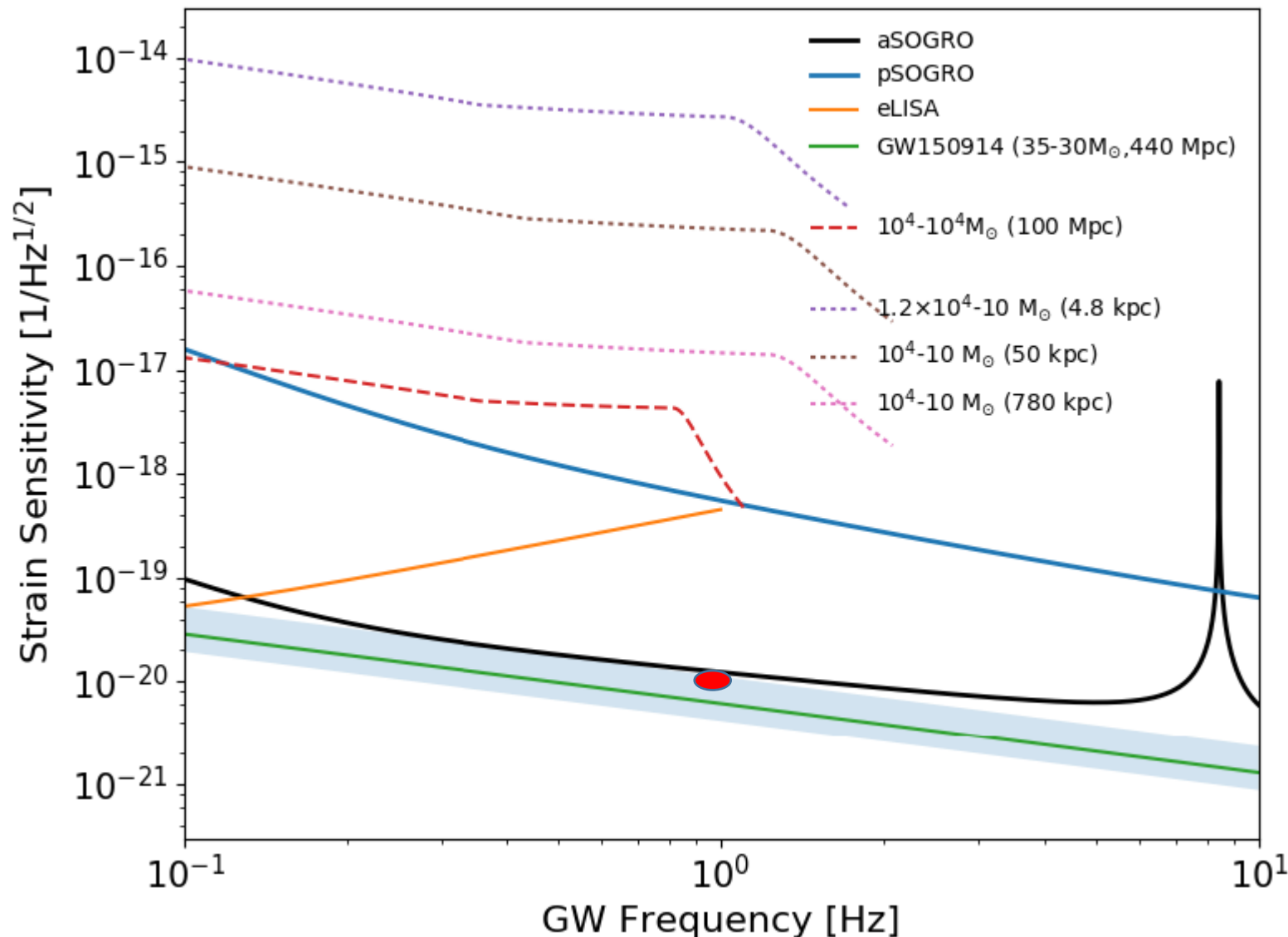


~ 10 days



Observed for ~.2s

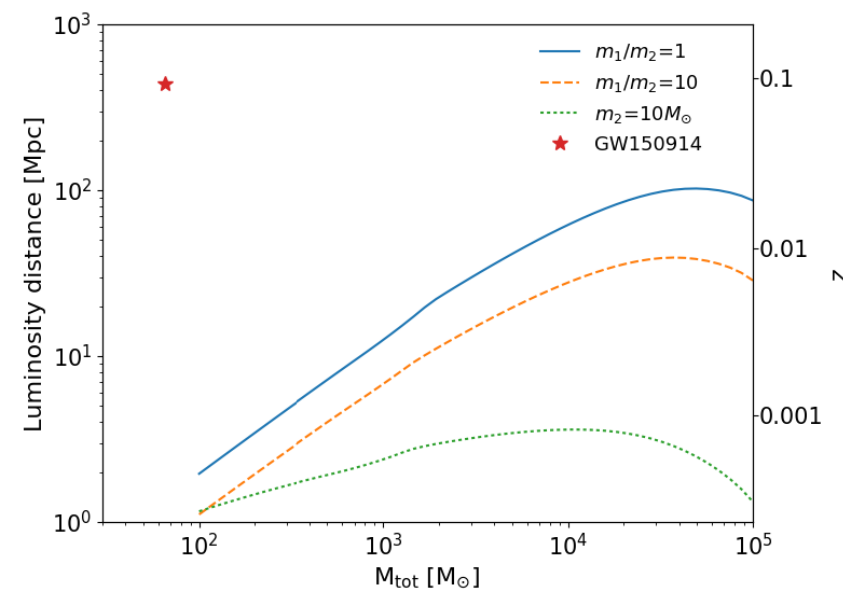
2) IMBH binary inspirals and mergers:



$$f_{ISCO,GW} = \frac{1}{\pi} \left(\frac{1}{6} \right)^{1.5} \frac{c^3}{GM} \sim \frac{4396}{M/M_{\odot}} \text{ [Hz]}$$

✓ Obs. Time: 0.5 hrs ~ 1.2 days

✓ Event rate: 0.001~4.8 per yr



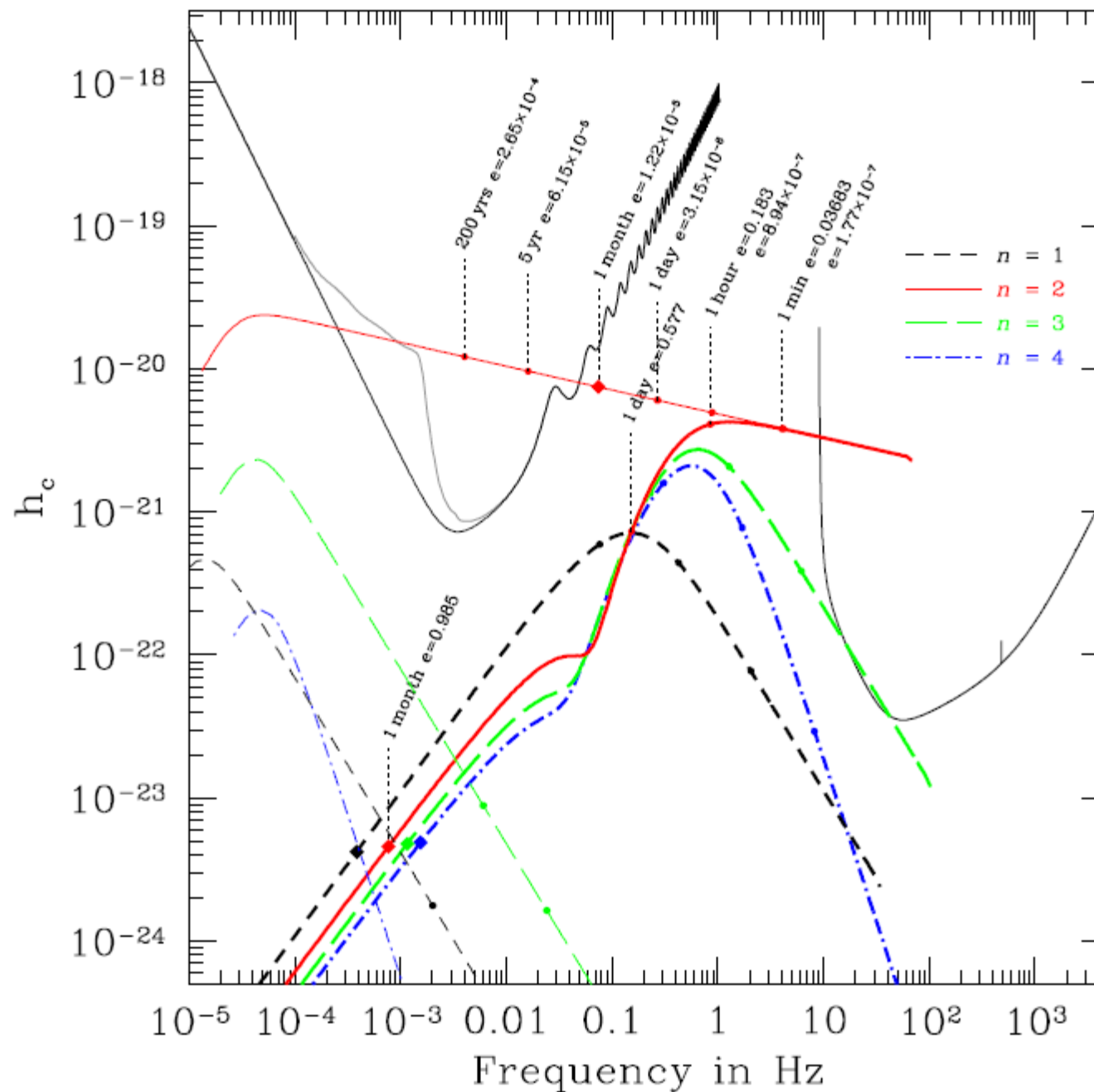
✓ X. Chen & P. Amaro-Seoane ('17):

“Formation of stellar-mass binary
black holes”

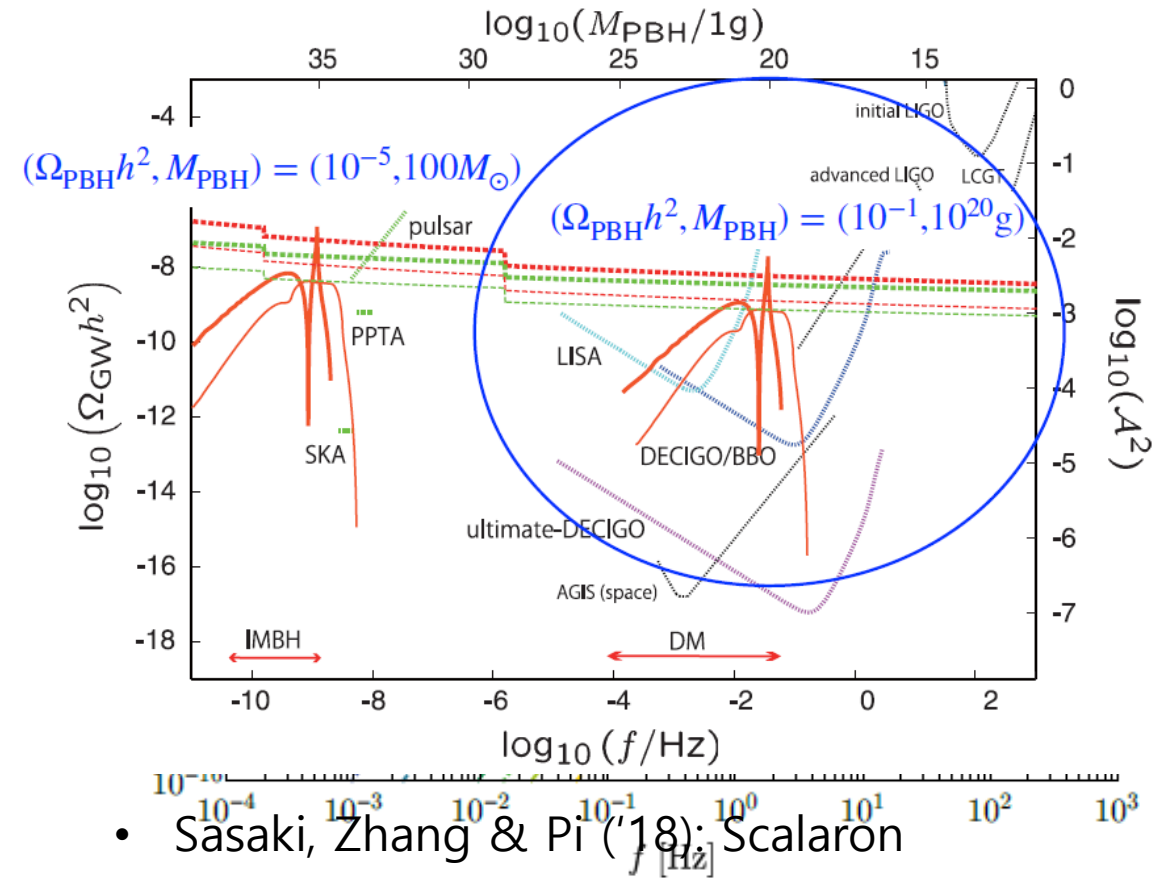
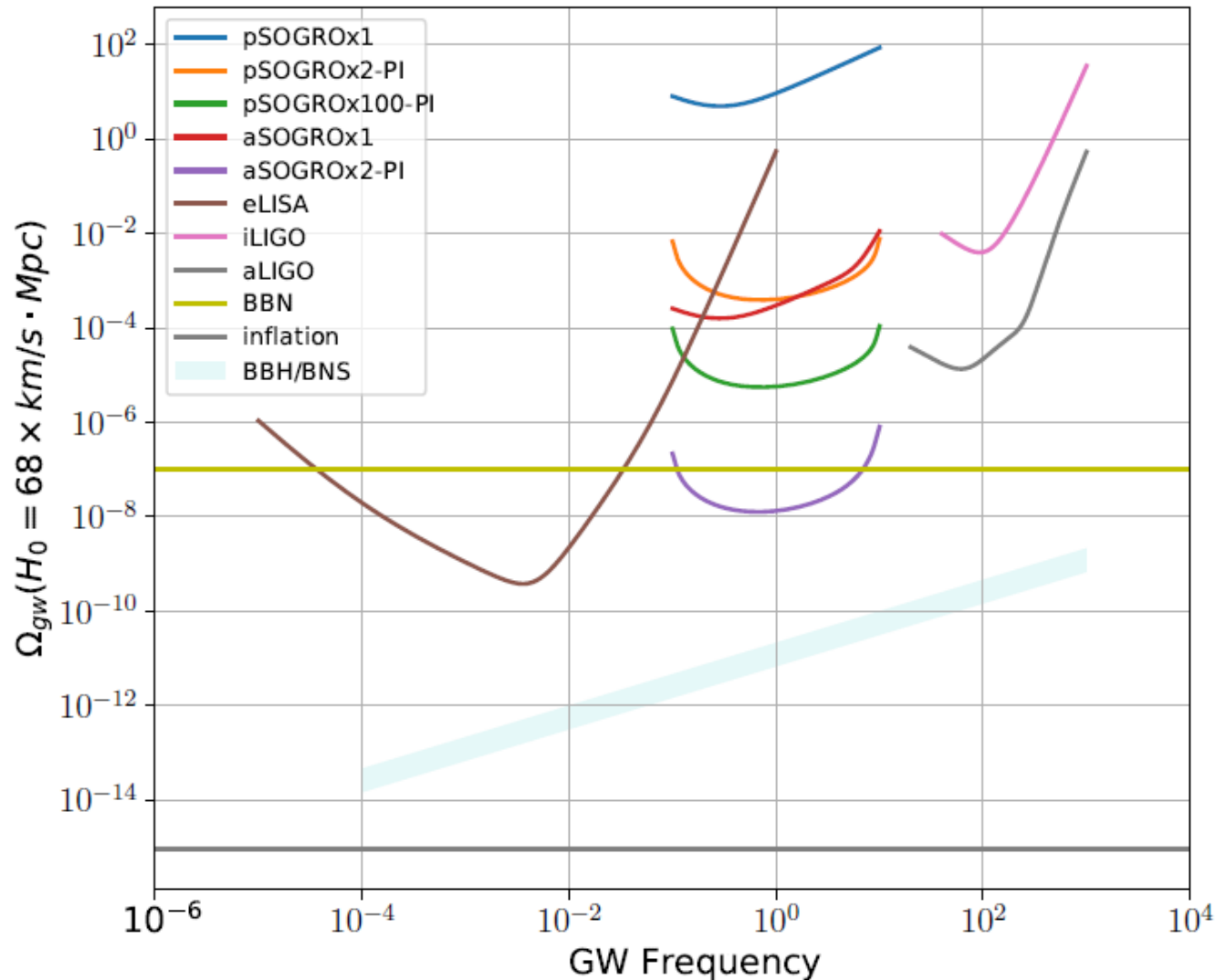
Binary star evolution

vs

**Dynamical interactions in dense
stellar systems**



3) Stochastic Gravitational Wave Background:

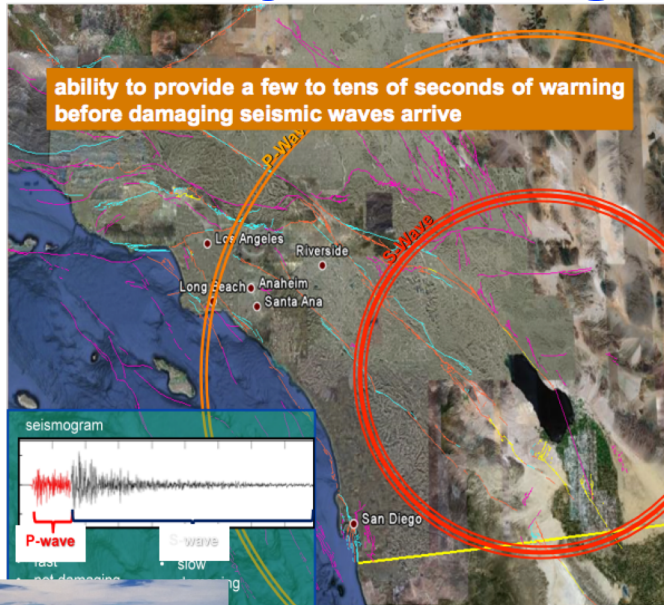


- Sasaki, Zhang & Pi ('18): "Scalaron"
- Espinosa, Racco & Riotto ('18): "SM Higgs instability"

✓ **Build multi detectors!!**

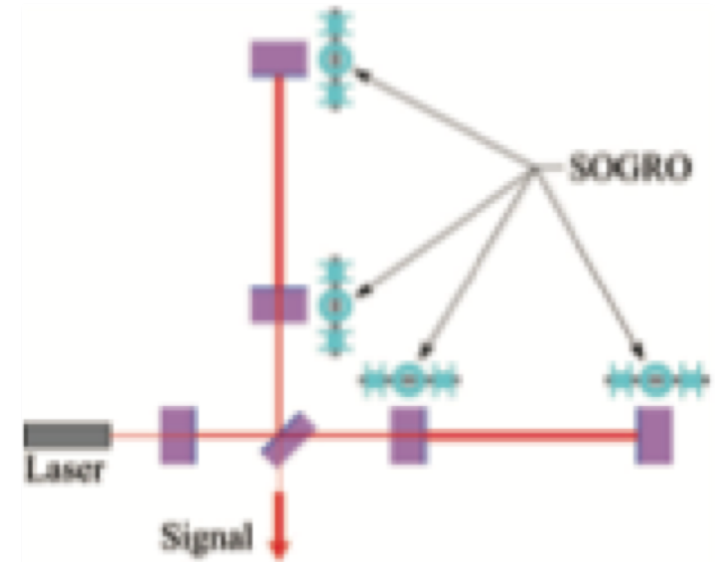
4) Other applications:

Fastest Earthquake Early Warning



✓ Saves ~10 s for Kyungjoo-Busan (~76 km)

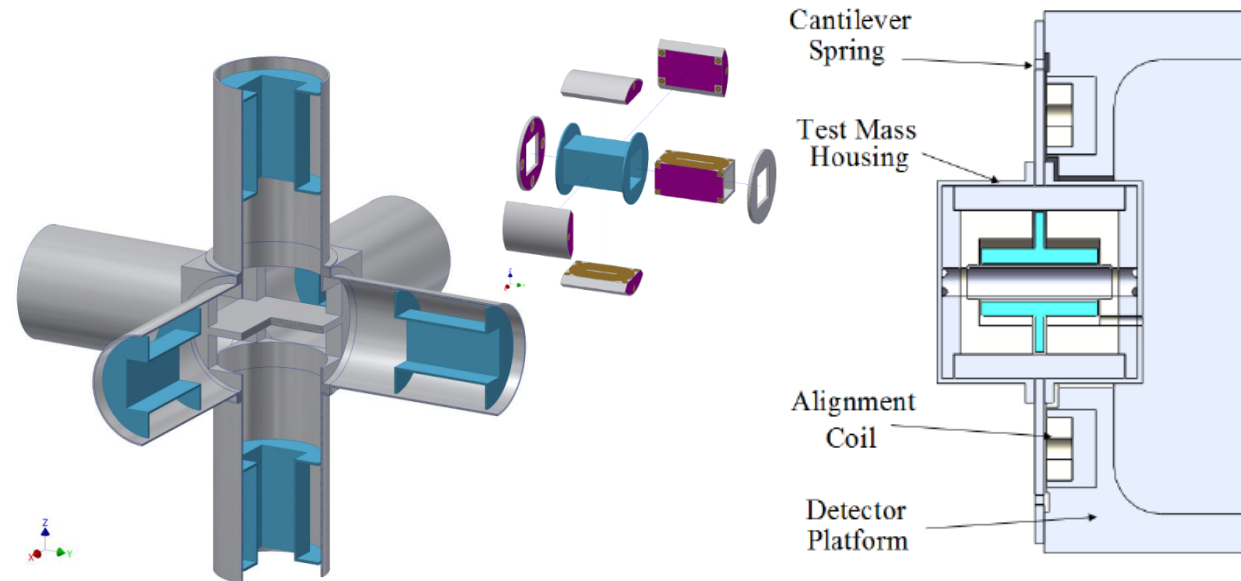
Improve aLIGO sensitivity at low freqs.



(Based on figures by H. Paik & C. Kim)

V. Summary and Outlook

- Design, principles and sciences are briefly introduced for the project of developing a superconducting mid-frequency gravitational wave telescope (SOGRO).
- Although our pilot study shows some feasibility of SOGRO, there remain many technical and theoretical challenges.
- Budget estimation for pSOGRO:
 - ~30 M\$ in total for 6 years
- We hope that it should be realized sometime in the future.



$1/10^{(-21)}$ OF THANKS!

