

Phenomenological implication of Continuum Clockwork

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Based on works

1711.06228 with Kiwoon Choi, Sang Hui Im

1711.08270 with Jinn-Ouk Gong

1811.10655 with Kyu Jung Bae, Jeff Kost

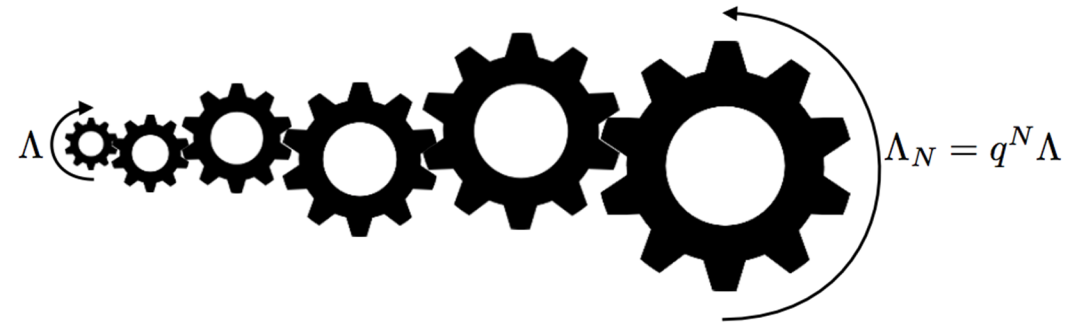
At IBS workshop

Dec. 4, 2018

Outline

Idea of discrete clockwork

- Clockwork axion
- Clockwork photon



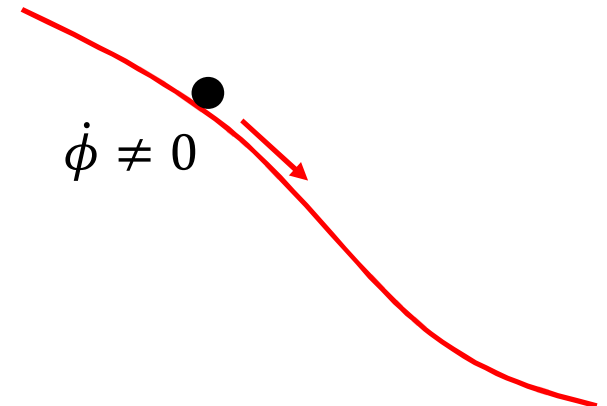
Continuum limit of clockwork

- Realization with 5d Geometry and Bulk/Boundary potentials

Phenomenological application

- Nontrivial wave-function renormalization
- Inflation, baryogenesis and dark matter via rolling Continuum CW ALPs

Conclusions



Idea of discrete clockwork mechanism

KNP mechanism [Kim, Nilles, Peloso 04]

Proposal to obtain a trans-Planckian field excursion in the context of natural inflation

$$\frac{f^2}{2} (\partial_\mu \theta)^2 + \Lambda^4 \cos \theta \quad : \quad a = \theta f \in [0, 2\pi f]$$

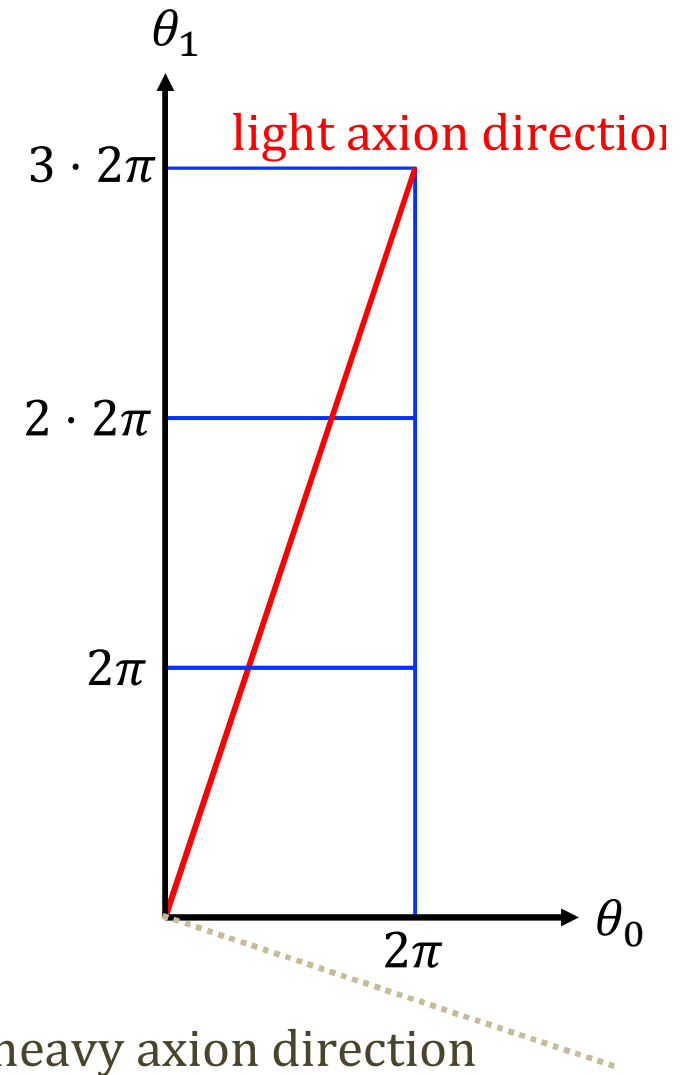
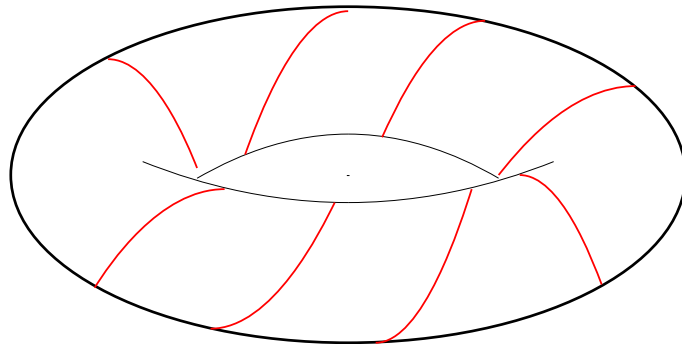
Introducing two axions with ($\Lambda_H \gg \Lambda$)

$$\frac{f^2}{2} \left((\partial_\mu \theta_0)^2 + (\partial_\mu \theta_1)^2 \right) + \Lambda_H^4 \cos(\textcolor{red}{3}\theta_0 - \theta_1) + \Lambda^4 \cos \theta_0$$

Integrating out a heavy mode:

$$\frac{f^2(1 + 1/9)}{2} (\partial_\mu \theta_1)^2 + \Lambda^4 \cos \frac{\theta_1}{\textcolor{red}{3}}$$

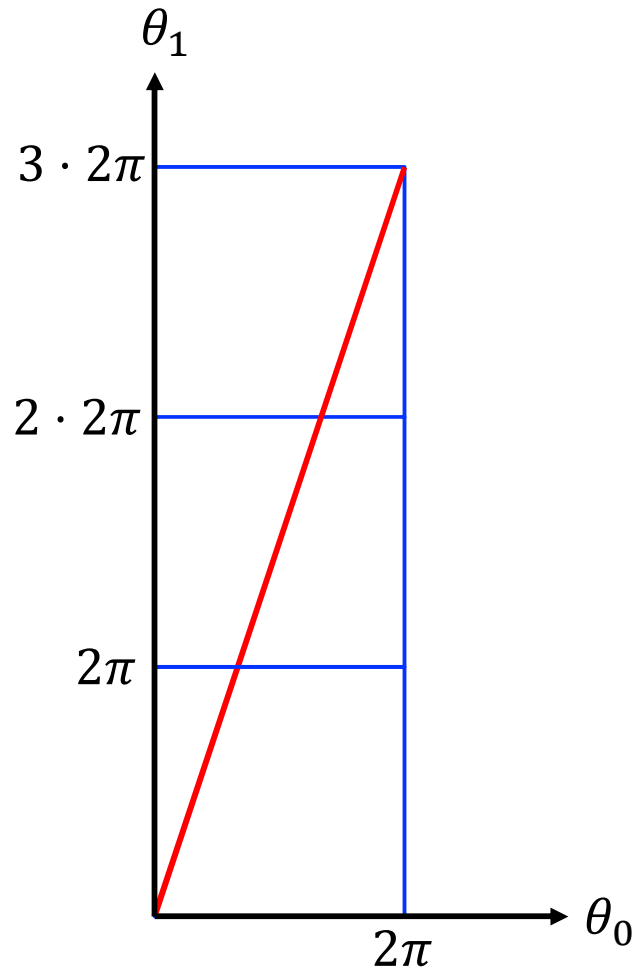
$$: \quad a = \sqrt{1 + 1/9} \theta_1 f \in [0, \textcolor{red}{3} \cdot 2\pi f \sqrt{1 + 1/9}]$$



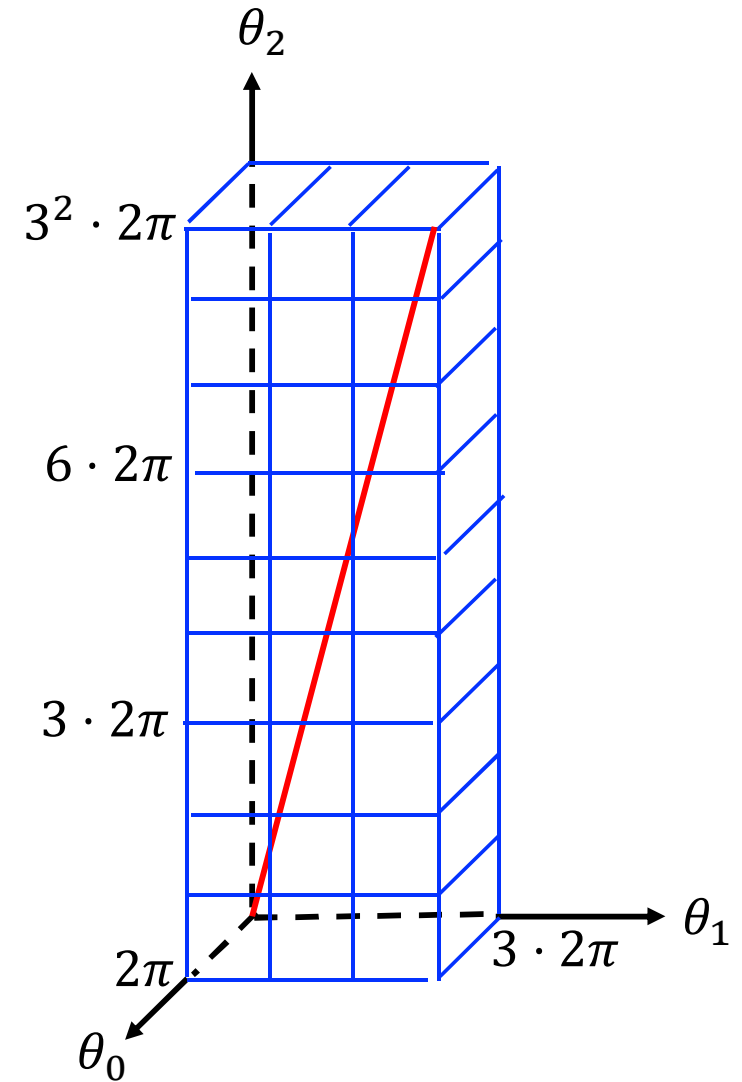
Extending KNP mechanism

Adding one more axion : extending the axion period $\Lambda_H^4 \cos(\textcolor{red}{3}\theta_0 - \theta_1) + \Lambda_H^4 \cos(\textcolor{red}{3}\theta_1 - \theta_2)$

$$\Lambda_H^4 \cos(\textcolor{red}{3}\theta_0 - \theta_1)$$



$$a = \sqrt{1 + 1/9} \theta_1 f \in [0, \textcolor{red}{3} \cdot 2\pi f \sqrt{1 + 1/9}]$$



$$a = \sqrt{1 + 1/9 + 1/81} \theta_2 f$$

$$\in [0, \textcolor{red}{3}^2 \cdot 2\pi f \sqrt{1 + 1/9 + 1/81}]$$

Clockwork axion

[Choi, Kim, Yun 14]

Considering $N+1$ axions with $\sum_{i=0}^{N-1} \Lambda_H^4 \cos(3\theta_i - \theta_{i+1})$

$$f_{eff} = q^N 2\pi f \sqrt{1 + q^{-2} + \dots}$$

$$a = \sqrt{1 + 1/9 \dots + 1/9^N} \theta_N f$$

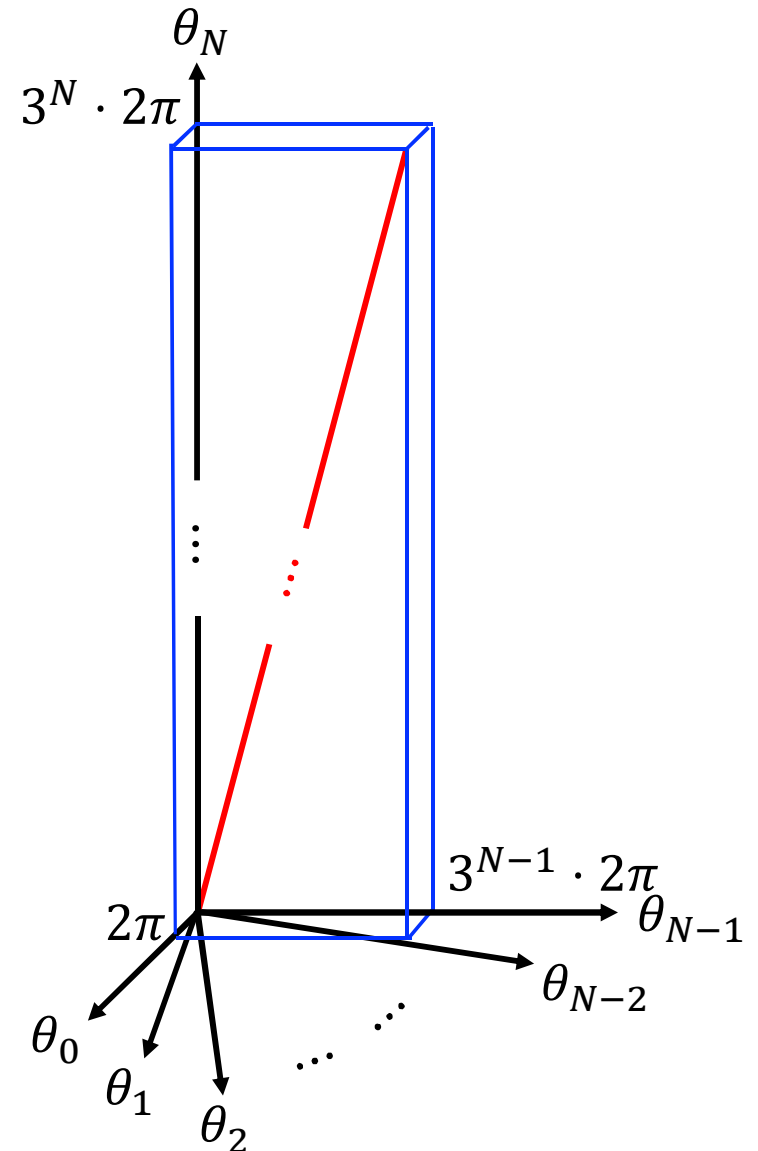
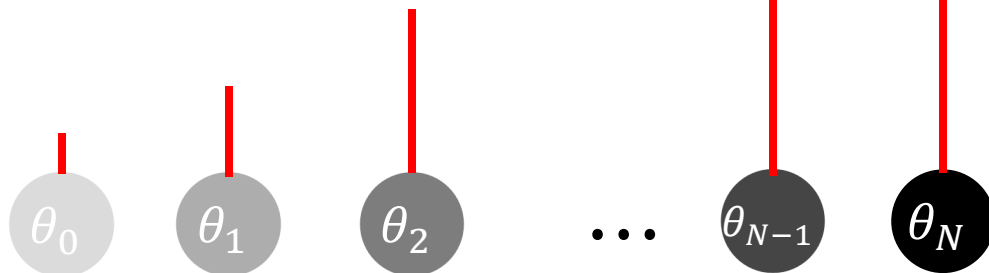
$$\in [0, 3^N \cdot 2\pi f \sqrt{1 + 1/9 \dots + 1/9^N}]$$

Exponential extending of the field excursion

Exponential localization of the lightest mode at the last site

$$\theta_i = q^i \left(\frac{a}{f_{eff}} \right) + \text{heavy modes}$$

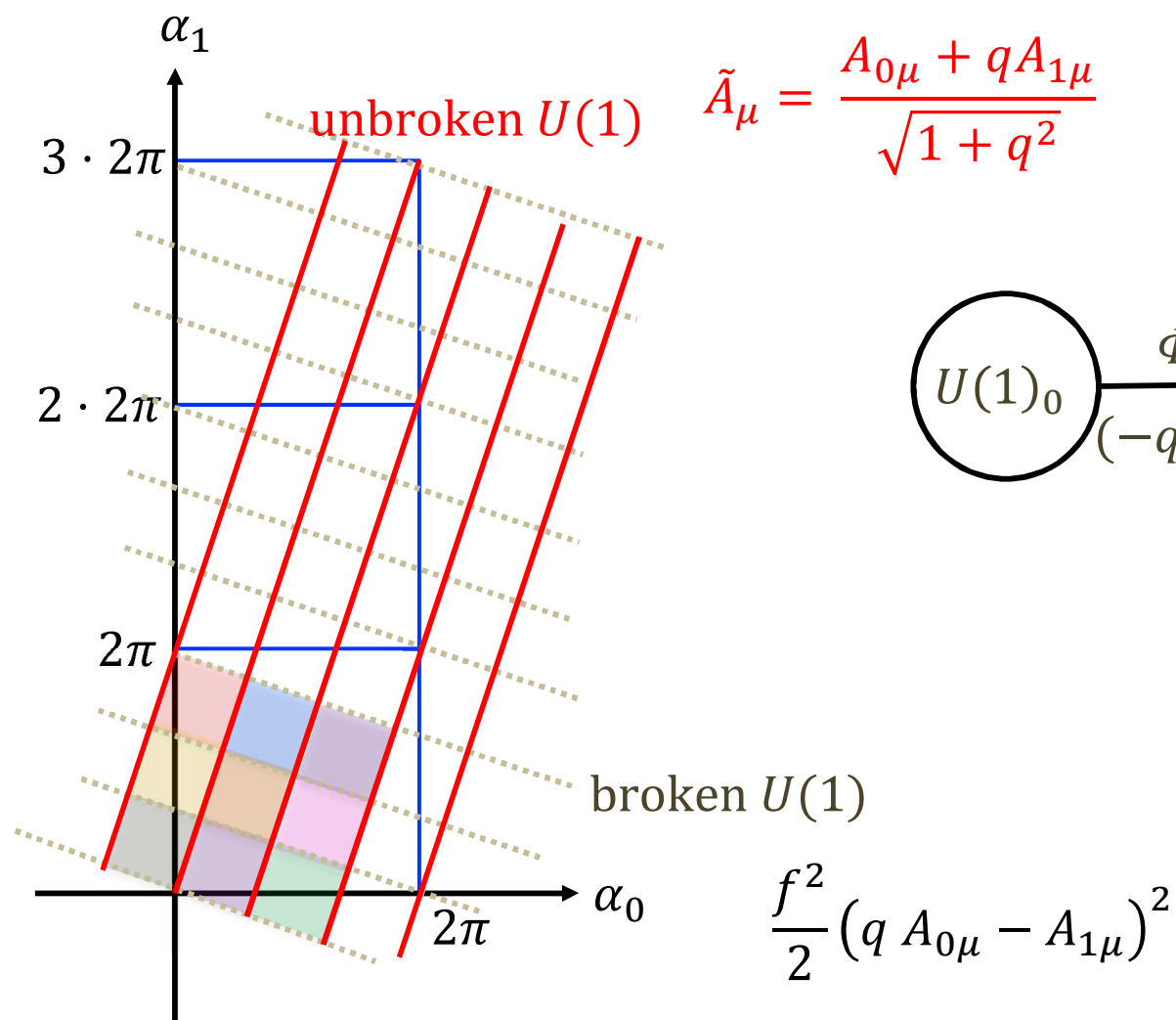
$$\theta_i O(x) \rightarrow \frac{q^i}{f_{eff}} a O(x)$$



Clockwork photon

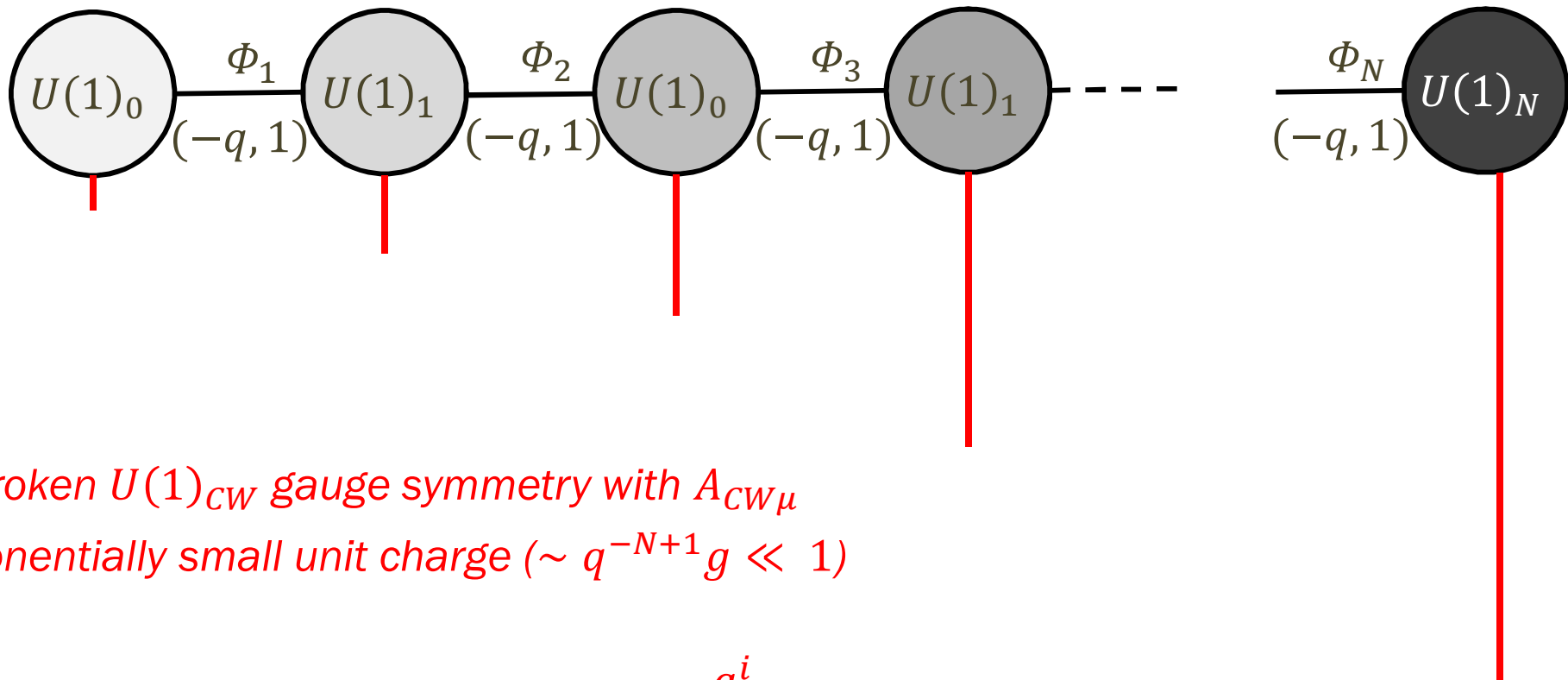
[Saraswat 16]

Starting from gauged $U(1)_0 \times U(1)_1$ ($A_{0\mu} \rightarrow A_{0\mu} + g^{-1} \partial_\mu \alpha_0$, $A_{1\mu} \rightarrow A_{1\mu} + g^{-1} \partial_\mu \alpha_1$)
with a bilinear Higgs field: $\Phi_1 \rightarrow \exp[i(\textcolor{red}{q} \alpha_0 - \alpha_1)] \Phi_1$ ($\langle \Phi_1 \rangle = f \neq 0$)



Clockwork photon [Giudice, McCullough 16]

Clockwork $U(1)$ can be constructed by introducing $N+1$ $U(1)$ with N Higgs fields



Unbroken $U(1)_{CW}$ gauge symmetry with $A_{CW\mu}$

Exponentially small unit charge ($\sim q^{-N+1}g \ll 1$)

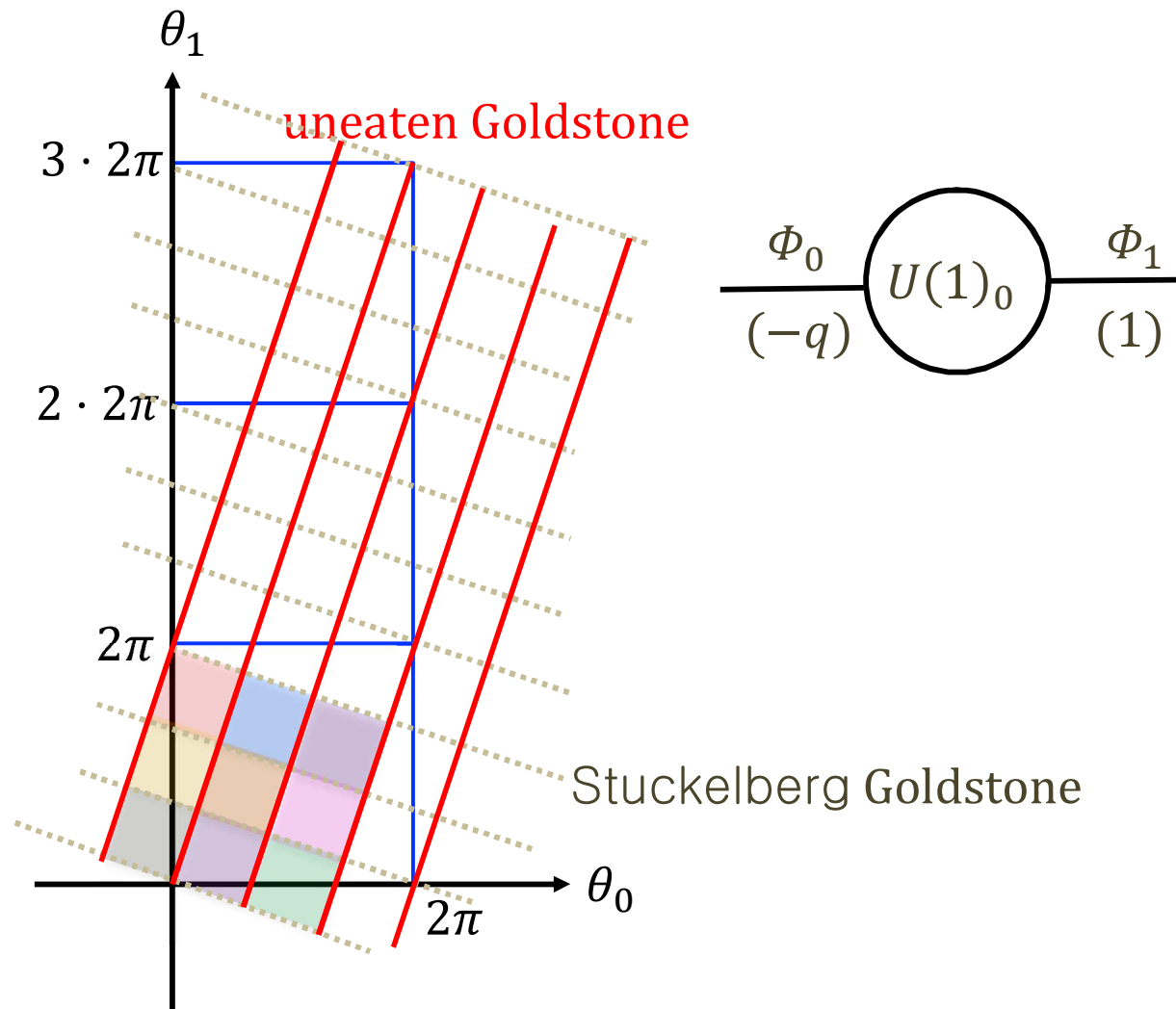
$$A_{i\mu} = \frac{q^i}{\sqrt{1 + q^2 + \dots q^{2N}}} A_{CW\mu} + \text{heavy modes}$$

$$g Q_i A_i^\mu J_{i\mu}(x) \rightarrow \frac{q^i g Q_i}{\sqrt{1 + q^2 + \dots q^{2N}}} A_{CW}^\mu J_{i\mu}(x)$$

Clockwork Goldstone

[Feng, Shiu, Soler, Ye 14]

Two Goldstone boson (θ_0, θ_1), one combination absorbed by the broken $U(1)$ vector field



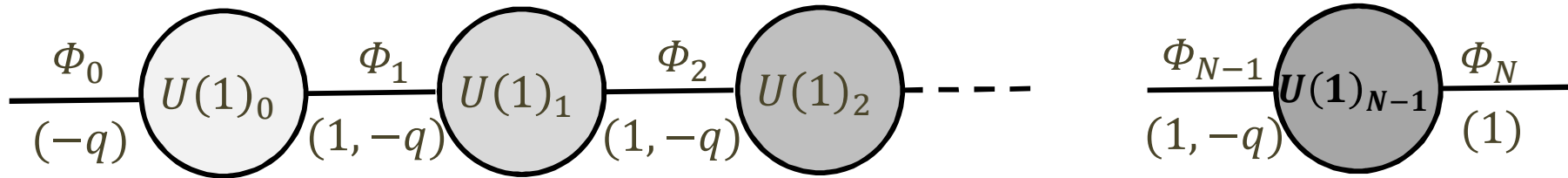
A fundamental domain

Each domains are connected by discrete gauge transformation

Clockwork Goldstone

[Bonnefoy, Dudas, Pokorski 1804.01112]

Among $N+1$ Goldstones, N combinations are eaten by vector bosons for the broken $U(1)$ s.



Uneaten Goldstone mode:

$$a = f \frac{\theta_0 + q \theta_1 \cdots + q^N \theta_N}{\sqrt{1 + q^2 + \cdots + q^{2N}}}$$

The Goldstone boson field period from

$$\theta_0 + q \theta_1 \cdots + q^N \theta_N \in [0, 2\pi] \text{ in a fundamental domain}$$

is exponentially reduced as

$$a \in \left[0, 2\pi f / \sqrt{1 + q^2 + \cdots + q^{2N}} \sim 2\pi f q^{-(N+1)} \right]$$

Applications

For the CW zero mode

- * Exponentially large (small) axion field period
- * Exponentially small $U(1)$ unit charge
- * Couplings of the lightest mode to operators at two different sites are hierarchically different

Inflation, relaxion, QCD axion

[Choi, Kim, Yun 14] [Higaki, Jeong, Kitajima, Takahashi 14,15,16]
[Choi, Im 15] [Farina, Pappadopulo, Rompineve, Tesi 16]
[Kaplan, Rattazzi 15]
[Kehagias, Riotto 17]
[Park, CSS 18]

Gravity [Giudice, McCullough 16]

Neutrino mass [Giudice, McCullough 16]
[Hambye, Teresi, Tytgat 16]
[Park, CSS 17]

Flavors, etc.

Continuum limit of CW

Up to quadratic order

CW mechanism up to quadratic order:

$$-\frac{1}{2} \sum_{i=0}^N (\partial_\mu \phi_i)^2 - \frac{1}{2} \sum_{i=0}^{N-1} M^2 (\phi_{i+1} - q \phi_i)^2$$

Extension to a continuum limit: $\phi_i(x) \Rightarrow \Phi(x, y)$ ($m\pi R \gg 1$)

$$-\frac{1}{2} \int_0^{\pi R} dy \left[(\partial_\mu \Phi)^2 + (\partial_y \Phi - m \Phi)^2 \right]$$

$$m = \frac{q - 1}{\epsilon} \Big|_{q \rightarrow 1, \epsilon \rightarrow 0}$$

Physical interpretation:

- *Nontrivial 5D background geometry*

$$-\frac{1}{2} \int_0^{\pi R} dy \sqrt{-G} G^{MN} \partial_M \Phi \partial_N \Phi$$

$$ds^2 = e^{\frac{4}{3} m y} (dx_\mu dx^\mu + dy^2)$$

$$\Phi \rightarrow e^{m y} \Phi$$

- *Bulk and boundary mass terms in a flat 5D*

[Giudice, McCullough 16]

$$-\frac{1}{2} \int_0^{\pi R} dy \left[(\partial_M \Phi)^2 + m^2 \Phi^2 + 2m \Phi^2 (\delta(y) - \delta(y - \pi R)) \right]$$

[Craig, Garcia, Sutherland 17]

Continuum clockwork axion (1)

[Choi, Im, CSS 17]

Defining frame in 5D is important :

Nontrivial 5D background geometry $\theta \in [0, 2\pi]$

$$ds^2 = e^{\frac{4}{3}m y} (dx_\mu dx^\mu + dy^2)$$

$$\int_0^{\pi R} dy \sqrt{-G} \left(-\frac{f^3}{2} G^{MN} \partial_M \theta \partial_N \theta \right) + \delta(y - y_*) \left(\frac{\theta}{8\pi^2} G \tilde{G} + e^{i\theta} \sqrt{-G_4} O(x) \right)$$

Flat zero mode profile along the 5th dim in the 5D field basis

$$\theta(x, y) = \theta_{CW}(x) + e^{-m y} \sum_{n=1} \text{KK modes}$$

Integrating out KK modes ($\theta_{CW}(x) \equiv \theta(x, y_*)$)

$$\frac{f^3}{4m} (e^{2m\pi R} - 1) (\partial_\mu \theta_{CW})^2 + \frac{\theta_{CW}}{8\pi^2} G \tilde{G} + e^{i\theta_{CW}} \tilde{O}(x)$$

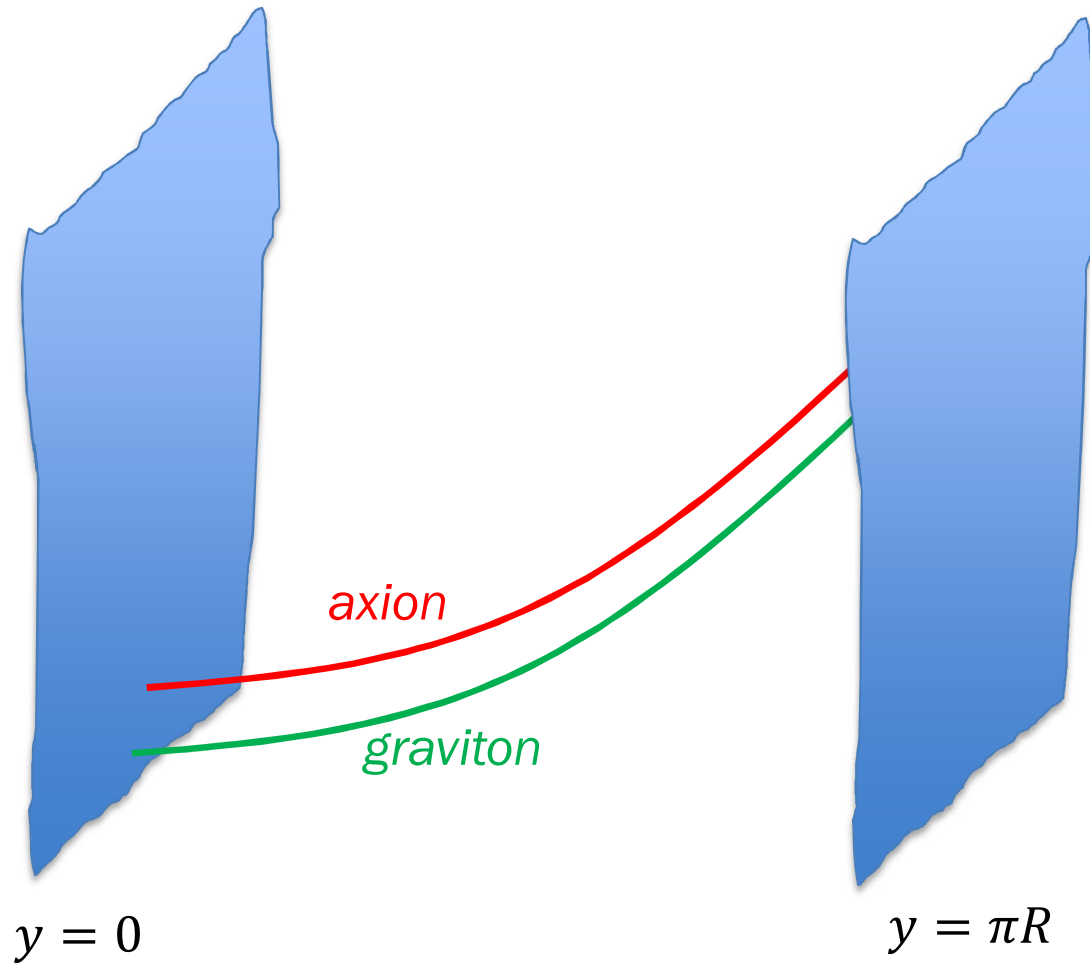
- Axion decay constant : $f_{eff} \simeq \frac{e^{m\pi R}}{\sqrt{2m\pi R}} \sqrt{f^3 \pi R} \gg \sqrt{f^3 \pi R}$

However, $M_{Pl} \simeq \frac{e^{m\pi R}}{\sqrt{2m\pi R}} \sqrt{M_5^3 \pi R} \gg \sqrt{M_5^3 \pi R}$

- No hierarchically different couplings between different branes

$$\left(\frac{f_{eff}}{M_{Pl}} \right)^2 = \left(\frac{f}{M_5} \right)^3$$

Continuum clockwork axion (1)



$$L_5 = \int_0^{\pi R} dy \sqrt{G_5} \simeq \frac{1}{\textcolor{red}{m}} e^{2\textcolor{red}{m}\pi R/3} \gg \pi R \quad \text{Warped large volume}$$

Continuum clockwork axion (2)

[Choi, Im, CSS 17]

Defining frame in 5D is important :

Bulk and boundary mass terms $\theta \in [0, 2\pi]$ with a periodic $V(x) = V(x + 2\pi)$

$$\int_0^{\pi R} dy -\frac{f^3}{2} \left((\partial_\mu \theta)^2 + (\partial_y \theta - m V(\theta))^2 \right) + \delta(y - y_*) \left(\frac{\theta}{8\pi^2} G \tilde{G} + e^{i\theta} O(x) \right)$$

Ex) $V(x) = \sin x = x + O(x^3)$

Localized zero in the 5D field basis at different positions for different $\langle \theta \rangle$

e.g. at $\langle \theta \rangle = 0$, $\partial_y \delta \theta - m \delta \theta$ (localized at $y = \pi R$)

at $\langle \theta \rangle = \pi$, $\partial_y \delta \theta + m \delta \theta$ (localized at $y = 0$)

Integrating out KK modes ($\theta_{CW}(x) \equiv \theta(x, y_*)$)

$$\frac{f^2}{2} Z(\theta_{CW}, y_*) (\partial_\mu \theta_{CW})^2 + \frac{\theta_{CW}}{8\pi^2} G \tilde{G} + e^{i\theta_{CW}} \tilde{O}(x)$$

- Axion decay constant : $f_{eff} \simeq (\sqrt{mR}) \sqrt{f^3 \pi R}$. No exponentially large
- Hierarchically different couplings depending on the axion expectation value

Continuum clockwork axion (2)

$$Z(\theta_{CW}, y_*) =$$

$$\frac{2(f/m) \tanh m\pi R}{\left(1 + \frac{\cosh(m\pi R - 2my_*)}{\cosh m\pi R}\right) - 2 \left(\sinh \frac{(m\pi R - 2my_*)}{\cosh m\pi R}\right) \cos \theta_{CW} - \left(1 - \frac{\cosh(m\pi R - 2my_*)}{\cosh m\pi R}\right) \cos^2 \theta_{CW}}$$

Nontrivial wave-function renormalization

For $m \rightarrow 0$

$$Z(\theta_{CW}, y_*) \rightarrow f\pi R$$

For $m\pi R \gg 1$ (at $y_ = 0$)*

$$Z(\theta_{CW}, y_*) \rightarrow \frac{f}{m(1 + 2 e^{-2m\pi R} - \cos \theta_{CW})}$$

$$\sim \frac{f^3}{2m} \exp(2m\pi R) \text{ at } \theta_{CW} = 0$$

For $m\pi R \gg 1$ (at $y_ = \pi R$)*

$$Z(\theta_{CW}, y_*) \rightarrow \frac{f}{m(1 + 2 e^{-2m\pi R} + \cos \theta_{CW})}$$

$$\sim \frac{f}{2m} \exp(2m\pi R) \text{ at } \theta_{CW} = \pi R$$

Continuum clockwork photon (1)

[Choi, Im, CSS 17]

In nontrivial 5D background $U(1): A_M \rightarrow A_M + \partial_M \alpha \quad \alpha(x, y) \in [0, 2\pi]$

$$\int_0^{\pi R} dy \sqrt{-G} \left(-\frac{1}{4g_5^2} G^{MN} G^{PQ} F_{MP} F_{NQ} \right) + \delta(y - y_*) \left(\sqrt{-G_4} i \bar{\psi} e_a^\mu \gamma^a (\partial_\mu - i A_\mu) \psi \right)$$

Flat zero mode in the 5D field basis $A_\mu(x, y) = A_{CW\mu}(x) + e^{-my} \sum_{n=1} \text{KK modes}$

Integrating out KK modes ($A_{CW}(x) \equiv A(x, y_)$)*

$$-\frac{3}{8g_5^2 m} (e^{2m\pi R/3} - 1) (F_{CW})_{\mu\nu} (F_{CW})^{\mu\nu} + \bar{\tilde{\psi}} i \gamma^\mu (\partial_\mu - i A_{CW\mu}) \tilde{\psi}$$

- Gauge coupling : $g_{eff} \simeq e^{-m\pi R/3} g_5 \sqrt{m} \ll g_5 / \sqrt{\pi R}$

However, for charged fields at a boundary $\frac{m_\psi}{M_5} < \frac{g_5}{\sqrt{R}}, \quad \frac{m_\psi}{M_{Pl}} \leq \frac{M_5}{M_{Pl}} \sim e^{-m\pi R} \ll g_{eff}$

- No hierarchically different couplings for different branes

Continuum clockwork photon (2)

[Choi, Im, CSS 17]

For 5D gauge symmetry,

bulk and boundary mass terms from the Stuckelberg kinetic term ($\theta(x, y) \rightarrow \theta + \alpha$)

$$\int_0^{\pi R} dy \left\{ -\frac{1}{4g^2} F_{MN}^2 - \frac{M^2}{2g^2} (\partial_M \theta - A_M)^2 \left(1 + \frac{2c_1}{M} (\delta(y) - \delta(y - \pi R)) \right) \right\}$$

Integrating out KK modes,

$$-\frac{1}{4} (F_{CW})_{\mu\nu}^2 - \frac{M^2}{2} (1 - c_1^2) (\partial_\mu \theta - A_{CW\mu})^2 + \bar{\psi} i \gamma^\mu (\partial_\mu - i e^{-c_1 M (\pi R - y_*)} A_{CW\mu}) \psi$$

For $c_1^2 = 1$: CW gauge symmetry realizes not as $U(1)_{CW}$ but as \mathbb{R}_{CW} from 5D $U(1)$!

Massless $\phi \equiv M \sqrt{1 - c_1^2} \theta$ decoupled

- Is it really OK? Well.. if starting from the 5D Higgs $H(x, y) = f^3 \left(1 + \frac{\rho(x, y)}{f} \right) e^{i\theta(x, y)}$,

$$\frac{M^2}{2} \left((1 - c_1^2) + c_2 \frac{h(x)}{f} \right) (\partial_\mu \theta - A_{CW\mu})^2$$

$c_1^2 \rightarrow 1$: strong coupling regime (breakdown of perturbative theory) strongly disfavor

Continuum clockwork Goldstone

[Choi 03]

[Choi, Im, CSS 17]

In nontrivial 5D background

[Flacke, Gripaio, March–Russell, Maybury 06]

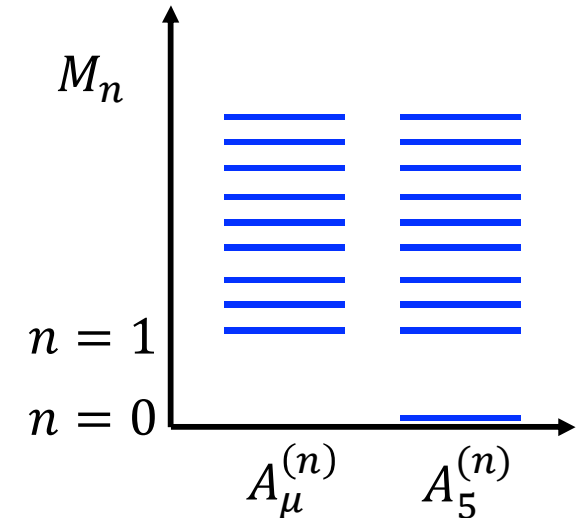
$$\int_0^{\pi R} dy \sqrt{-G} \left(-\frac{1}{4g_5^2} G^{MN} G^{PQ} F_{MP} F_{NQ} \right)$$

Opposite boundary condition $A_\mu(y=0) = A_\mu(\pi R) = 0$:

$$F_{\mu 5}^2 = (\partial_\mu A_5 - \partial_y A_\mu)^2$$

Except zero-mode, all modes becomes massive vector bosons

Integrating out KK modes, $\left(\theta_{CW}(x) = \int_0^{\pi R} dy A_5(x, y) \right)$



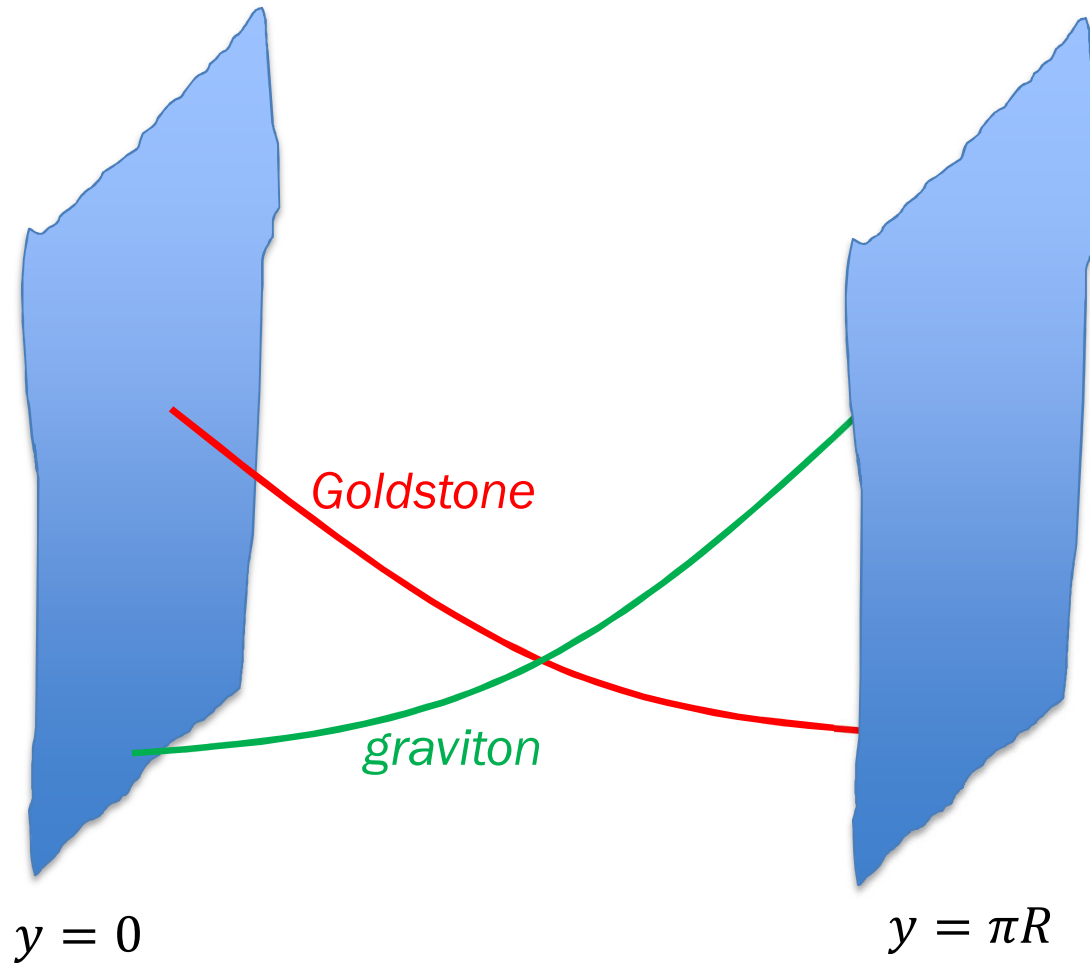
The zero mode kinetic term becomes

$$\mathcal{L}_{eff} = -\frac{m}{3g_5^2} \frac{(\partial_\mu \theta_{CW})^2}{(1 - e^{-2m\pi R/3})}$$

- Axion decay constant : $f_{eff} \simeq \sqrt{\frac{m}{g_5^2}} \leq M_5$ $\left(\frac{f_{eff}}{M_{Pl}} \right) \sim e^{-m\pi R}$

Similar to the masses of low KK modes $(f_{eff}/M_{KK}(n=1, 2, \dots) \sim 1/\sqrt{m\pi R})$

Continuum clockwork Goldstone



(Generalized) Linear Dilaton

The nontrivial 5D background

[Antoniadis, Arvanitaki, Dimopoulos, Givon 11]

$$ds^2 = e^{\frac{4}{3}my} (dx_\mu dx^\mu + dy^2)$$

can be obtained from Linear Dilaton Model ($\xi = 1, \Lambda_5, \Lambda_4 < 0$)

$$\int_0^{\pi R} dy \sqrt{-G} e^{\xi S} \left(\frac{M_5^3}{2} R + \frac{M_5^3}{2} G^{MN} \partial_M S \partial_N S - \Lambda_5 - \frac{\Lambda_4}{\sqrt{G_{55}}} (\delta(y) - \delta(y - \pi R)) \right)$$

In the Einstein frame, ($c = \xi / \sqrt{4\xi^2 - 3}$)

$$\int_0^{\pi R} dy \sqrt{-G} \left(\frac{M_5^3}{2} R - \frac{M_5^3}{2} G^{MN} \partial_M S \partial_N S - e^{-2cs/\sqrt{3}} \Lambda_5 - \frac{e^{-cs/\sqrt{3}} \Lambda_4}{\sqrt{G_{55}}} (\delta(y) - \delta(y - \pi R)) \right)$$

[Choi, Im, CSS 17]

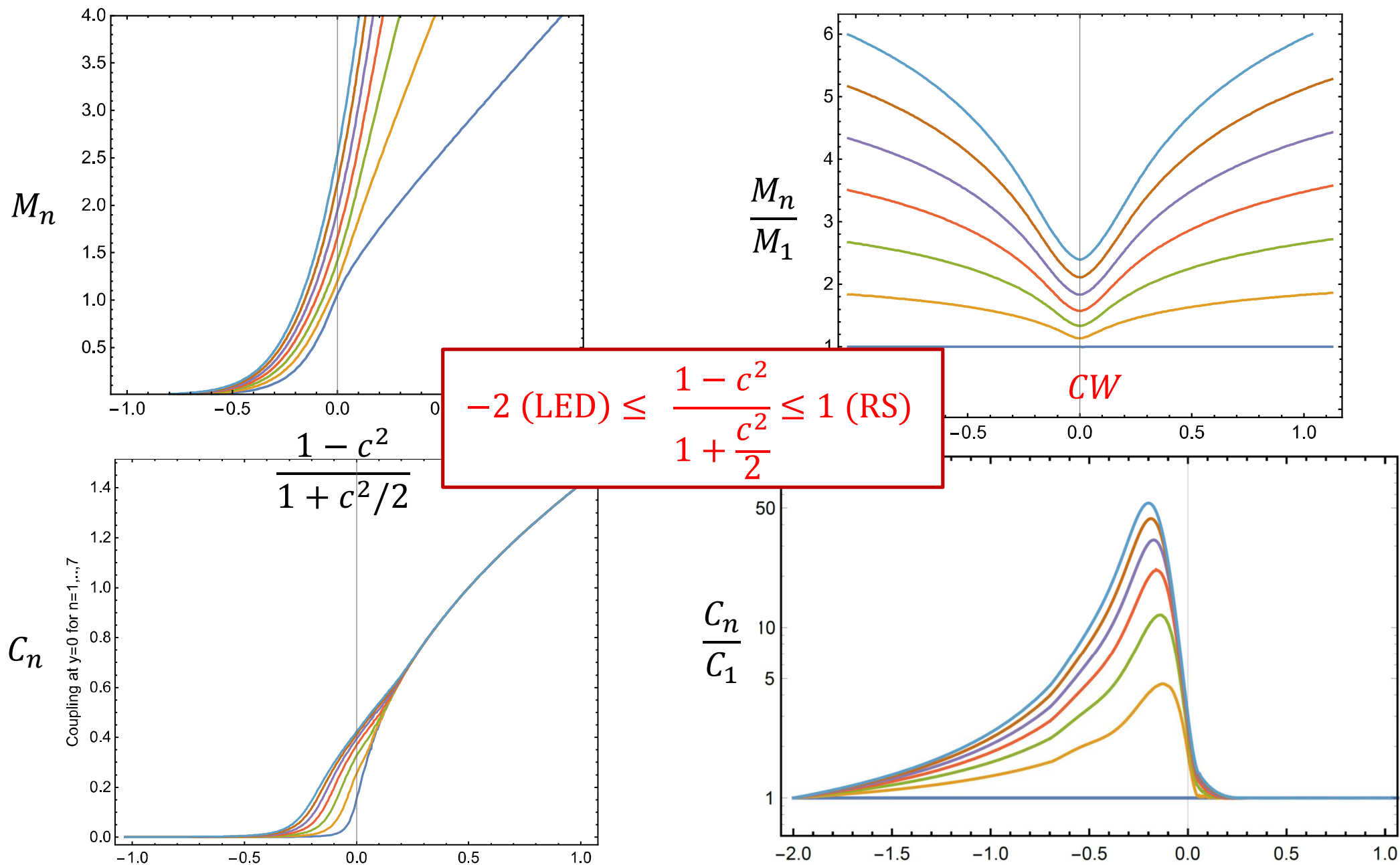
For $\xi \neq 1 (c \neq 1)$, more general metric realized $ds^2 = e^{2k_1 y} dx_\mu dx^\mu + e^{2c^2 k_1 y} dy^2$

$$k_1 = \sqrt{\frac{2\Lambda_5}{3(c^2 - 4)}}$$

(Generalized) Linear Dilaton

[Choi, Im, CSS 17]

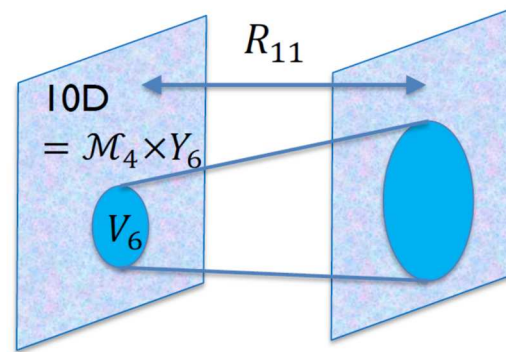
KK spectrum and couplings



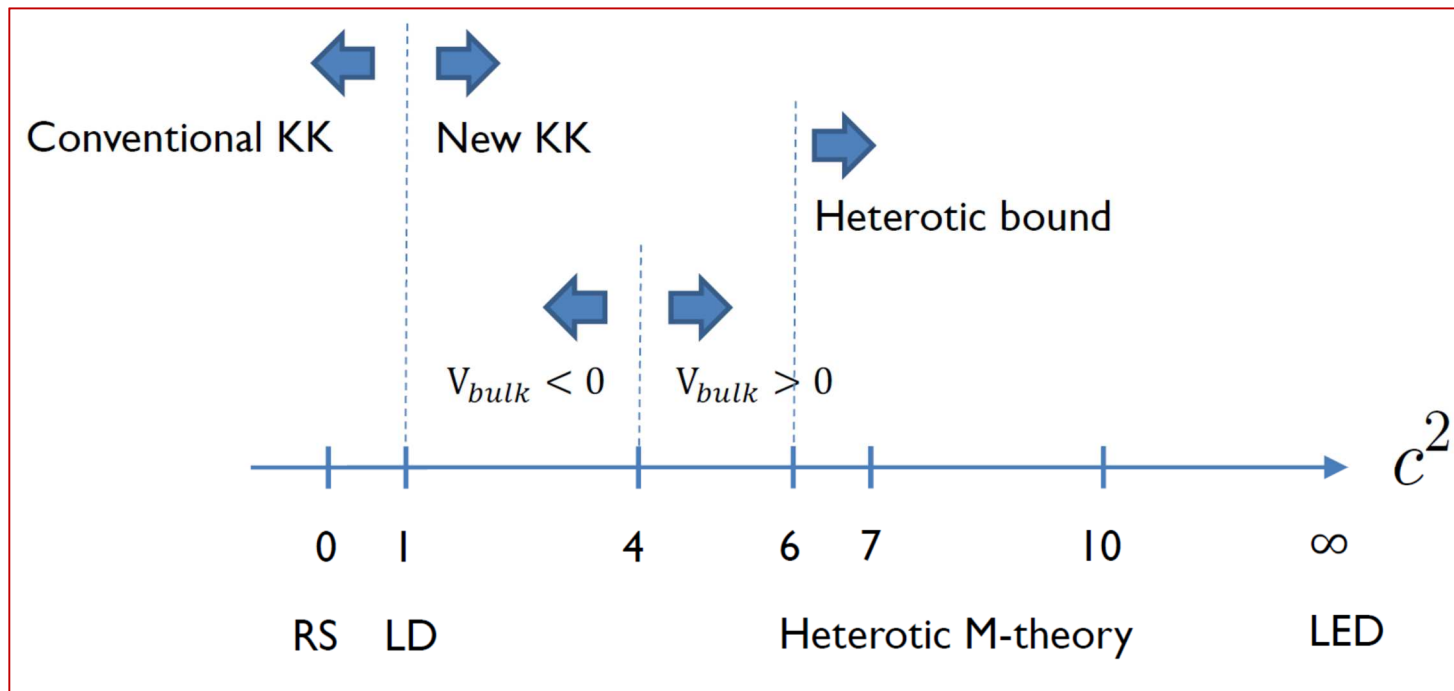
(Generalized) Linear Dilaton

Can we realize $c^2 > 1$? In *heterotic M-theory* $c^2 \geq 6$ is obtained

[Im, Nilles, Olechowski 1811.11838]



$$R_{11} \gg V_6^{1/6} \sim \frac{1}{M_{11}}$$



From Sang Hui's talk slides

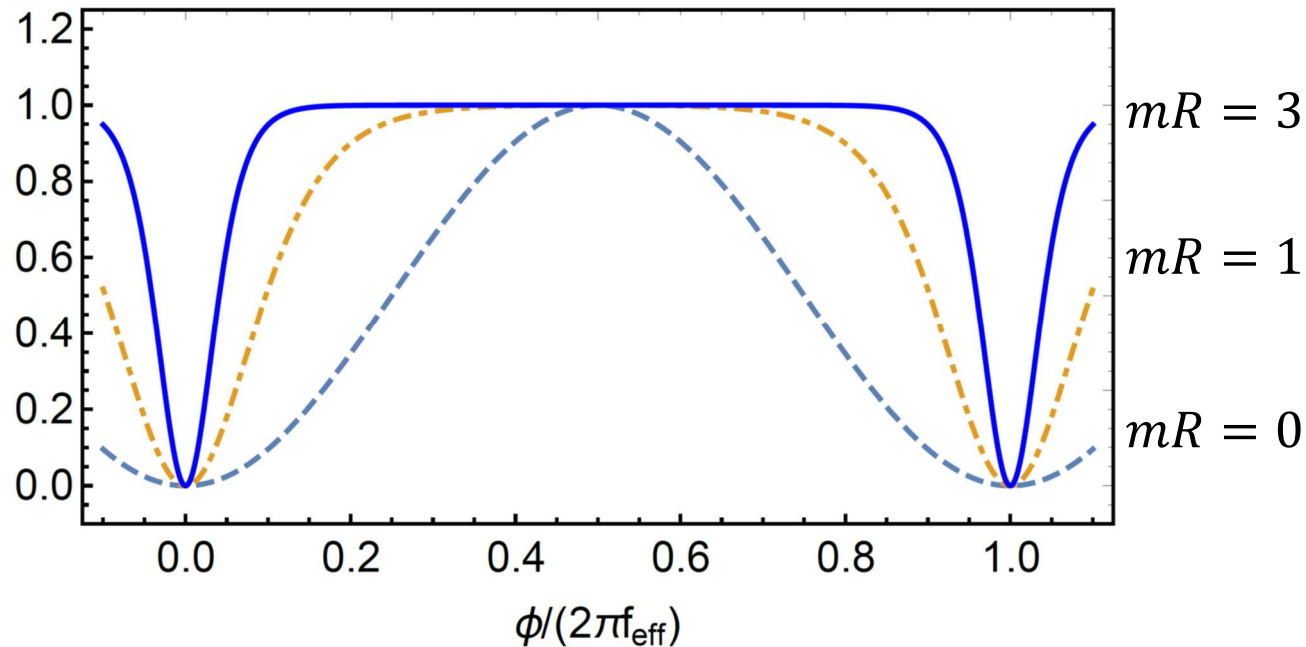
Phenomenological application of CCW axioms

Deform the axion potential

Nontrivial wave-function renormalization

$$-\frac{f^2}{2} \mathbf{Z}(\theta_{CW}, y_*) (\partial_\mu \theta_{CW})^2 + \Lambda^4 \cos \theta_{CW} = \frac{1}{2} (\partial_\mu \phi)^2 + \Lambda^4 \cos \theta_{CW}[\phi]$$

E.g. for $y_* = \pi R$, $Z(\theta_{CW} = 0, \pi R) \sim O(1)$, $Z(\theta_{CW} = \pi, \pi R) \sim e^{2m\pi R} \gg 1$

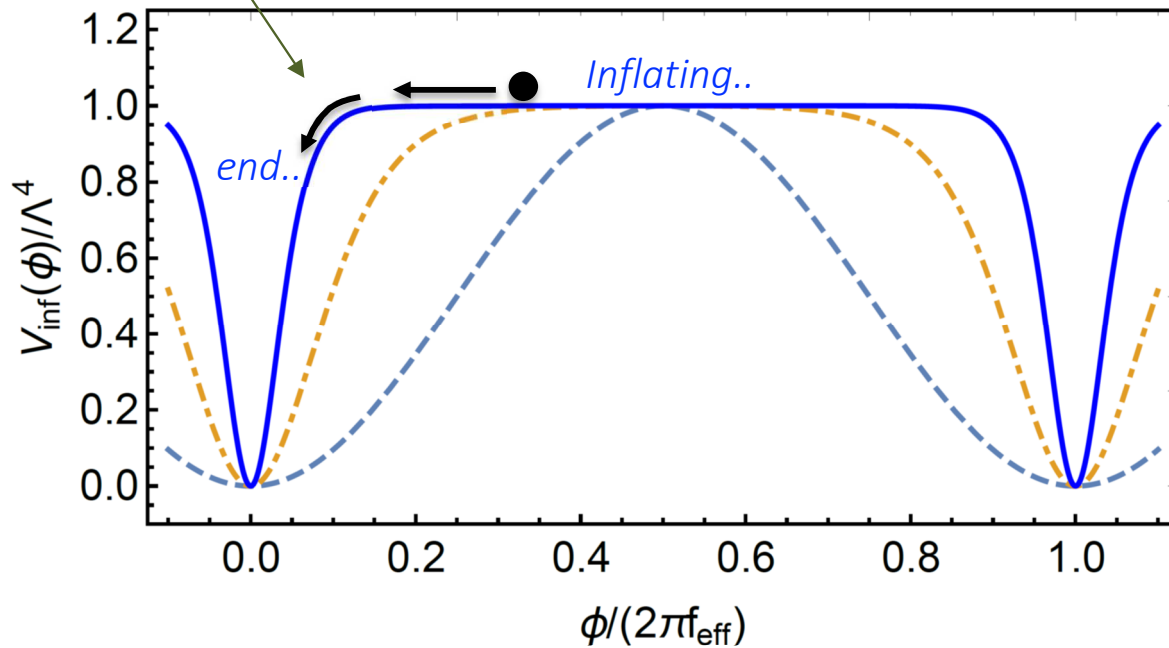


Natural Cliff Inflation

[Gong, CSS 17]

The slope of the potential around the extremum is exponentially sensitive to $m\pi R$.

$\tanh^2\left(\frac{\phi}{2f}\right)$ Approximately, for $e^{m\pi R} \gg 1$
: same type of Higgs (R^2) inflation with a much smaller f ($\ll M_{\text{Pl}}$)



($m=0$: vanilla natural inflation)

Slow roll parameters: $\epsilon = \frac{M_{\text{Pl}}^2}{2} \left(\frac{V'}{V} \right)^2$, $\eta = M_{\text{Pl}}^2 \frac{V''}{V}$

Observables

Amplitude of the curvature perturbation: $A_{\mathcal{R}} = \frac{V}{24\pi^2 M_{\text{Pl}}^4 \epsilon}$, spectral tilt: $n_{\mathcal{R}} = 1 - 6\epsilon + 2\eta$
tensor to scalar ratio: $r = 16\epsilon$

Natural **Cliff** Inflation

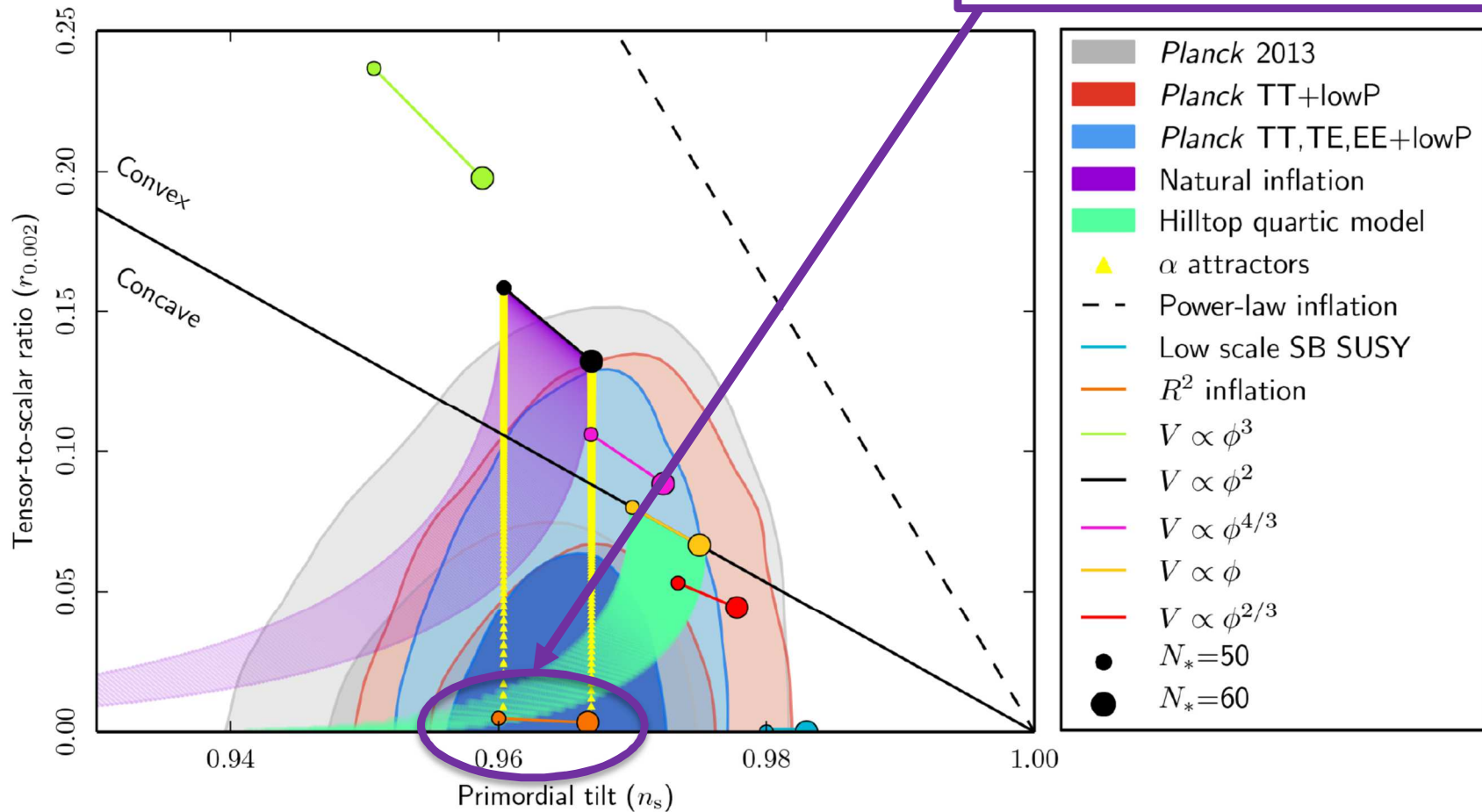
[Gong, CSS 17]

The slope of the potential around the extremum is exponentially sensitive to $m\pi R$.

$$N_e = \frac{1}{M_{Pl}} \frac{1}{2\pi} \int_{\phi_f}^{\phi_i} \frac{d\phi}{\sqrt{\epsilon}} \approx \left(\frac{f}{2M_{Pl}} \right)^2 \exp \left(\frac{\phi_i}{f} \right)$$

$$n_R \approx 1 - \frac{2}{N_e}, \quad r \approx \frac{8}{N_e^2} \left(\frac{f}{M_{Pl}} \right)^2$$

PLANCK 2013(2015)



Natural **Cliff** Inflation

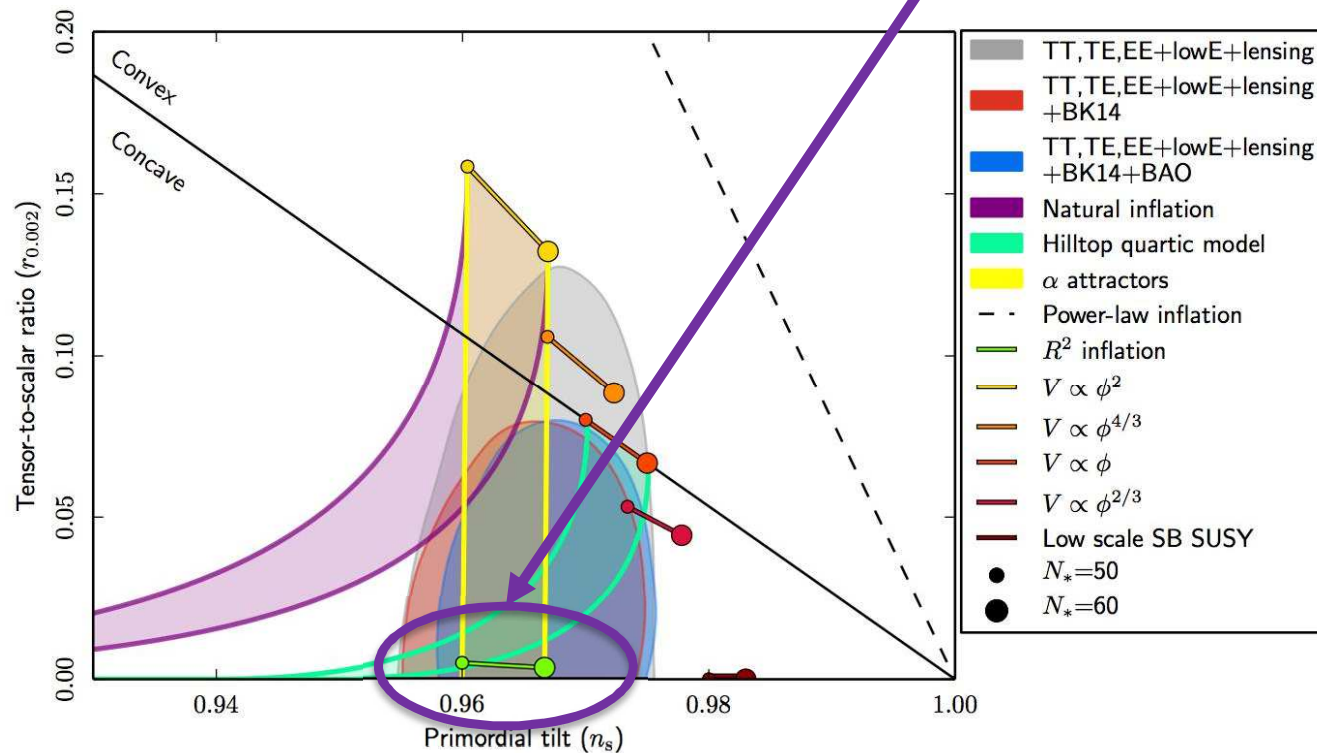
[Gong, CSS 17]

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$$n_R \approx 1 - \frac{2}{N_e}, \quad r \approx \frac{8}{N_e^2} \left(\frac{f}{M_{Pl}} \right)^2$$

PLANCK 2018

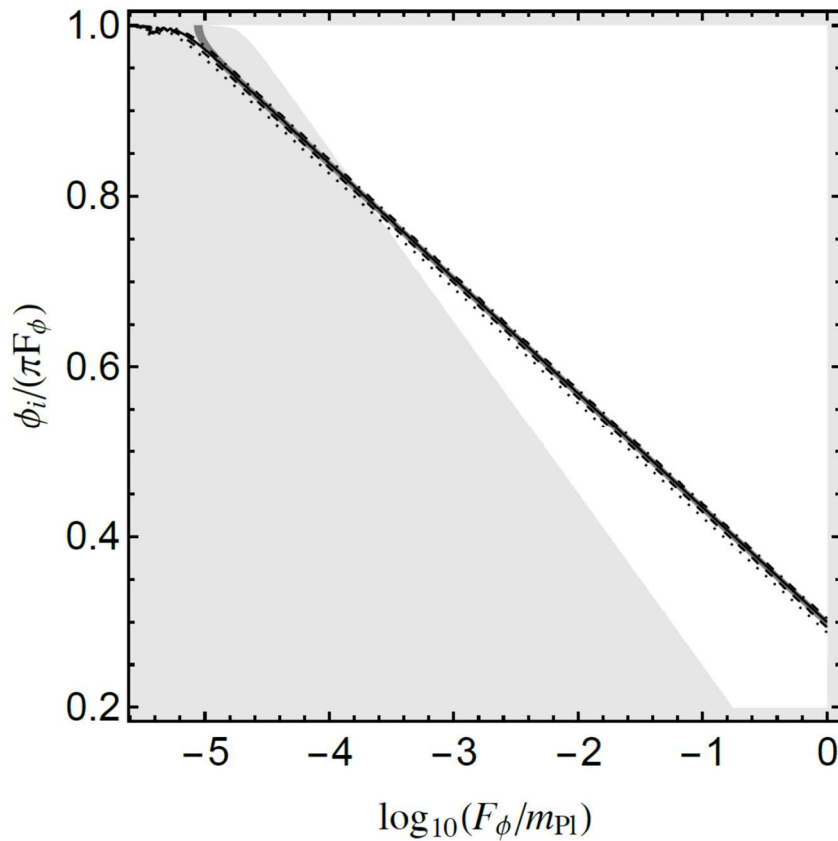


Natural Cliff Inflation [Gong, CSS 17]

Inflation with a *sub-Planckian periodic potential* can be achieved *without tuning of initial position of ϕ_i* .

$$N_e = \frac{1}{M_{Pl}} \frac{1}{2\pi} \int_{\phi_f}^{\phi_i} \frac{d\phi}{\sqrt{\epsilon}} \approx \left(\frac{f}{2M_{Pl}} \right)^2 \exp \left(\frac{\phi_i}{f} \right)$$

$$n_R \approx 1 - \frac{2}{N_e}, \quad r \approx \frac{8}{N_e^2} \left(\frac{f}{M_{Pl}} \right)^2$$



$$F_\phi = f_{\text{eff}} \simeq 10f_*$$

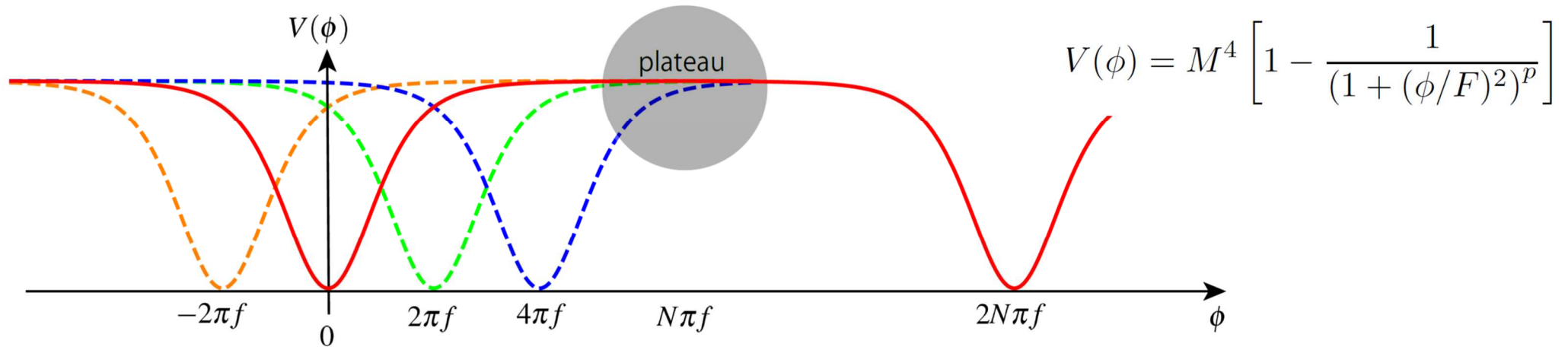
FIG. 2. The number of e -folds N and the spectral index n_R in the $\log_{10}(F_\phi/m_{Pl})$ - $\phi_i/(\pi F_\phi)$ plane. We set $N = 40$ (dotted), 50 (dashed), 60 (solid) and 70 (dot-dashed), and $0.96 < n_R < 0.97$ (dark shade). $r < 0.07$ is satisfied everywhere shown in this plot. The regime beyond the perturbative constraint $\Lambda^4/(2f_5^3 m) > 0.1$ (light shade) is also shown.

Reheating can be done by boundary interactions between the inflaton and the photons in the SM.

$$\int d^5x \sqrt{-g} \delta(y - y_b) c_\gamma \theta(x, y) F_{\mu\nu}(x) \tilde{F}_{\mu\nu}(x) \Rightarrow \delta \mathcal{L}_{\text{eff}} = \frac{c_\gamma}{f} e^{-m(\pi R - y_b)} \delta\phi F \tilde{F}$$

Comparing with other deformed Natural Inf.

Scalar potentials induced by an anomalous coupling between the inflaton and a confining large N pure Yang-Mills gauge group [Nomura et.al. 1706.08522, 1711.10490]

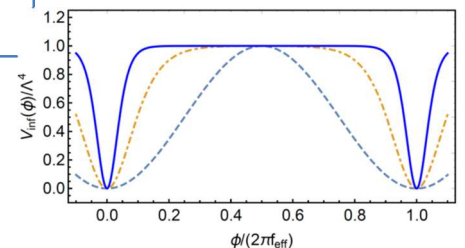


$$-\frac{1}{2}(\partial_\mu \phi)^2 - V_{\text{pure}}(\phi) + \frac{\phi}{8\pi^2 f} (F_{\mu\nu} \tilde{F}^{\mu\nu})_{SM}$$

N multi branches (tunneling is allowed), field independent coupling to the SM

$$-\frac{1}{2}(\partial_\mu \phi)^2 - \Lambda^4(1 - \cos \theta_{CW}[\phi]) + \frac{\theta_{CW}[\phi]}{8\pi^2} (F_{\mu\nu} \tilde{F}^{\mu\nu})_{SM}$$

One branch, field dependent coupling to the SM
: different (p)reheating history



Spontaneous baryogenesis and dark matter

[Bae, Kost, CSS 1811.10655]

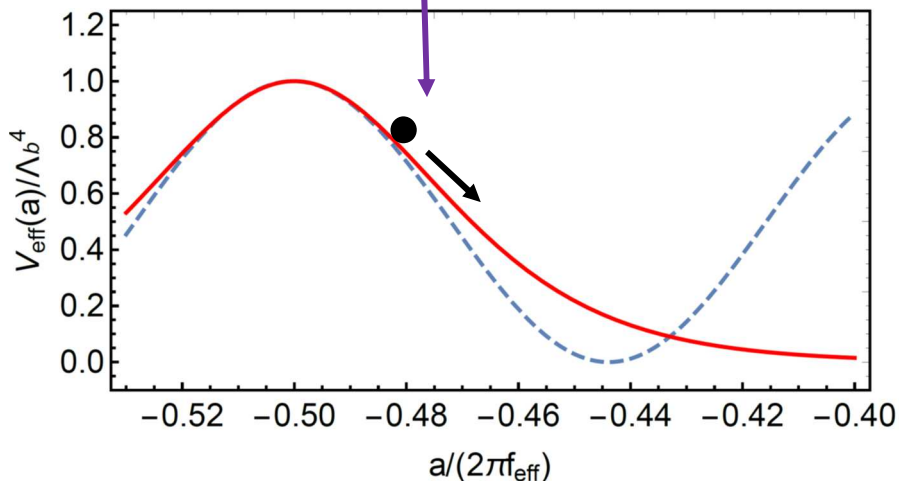
If the CCW axion couples to $SU(2)_L \times U(1)_Y$ gauge fields,

$$-\frac{1}{2}(\partial_\mu \phi)^2 - \Lambda^4(1 - \cos \theta_{CW}[\phi]) + \frac{\theta_{CW}[\phi]}{8\pi^2} (c_1 W \tilde{W} + c_2 B \tilde{B})$$

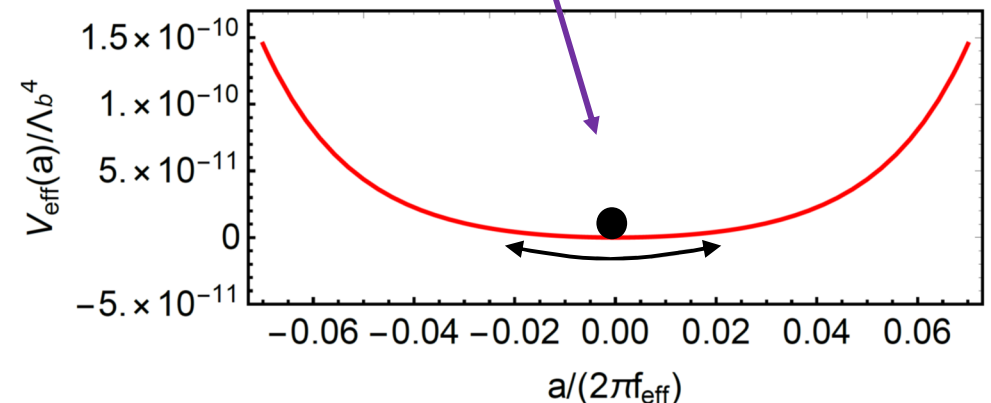
the rolling axion can generate a baryon asymmetry due to B+L anomaly

$$(\partial_\mu J_B^\mu) = \frac{N_f}{8\pi^2} (W_{\mu\nu} \tilde{W}^{\mu\nu} - B_{\mu\nu} \tilde{B}^{\mu\nu})$$

Most of baryon asymmetry is generated during this period

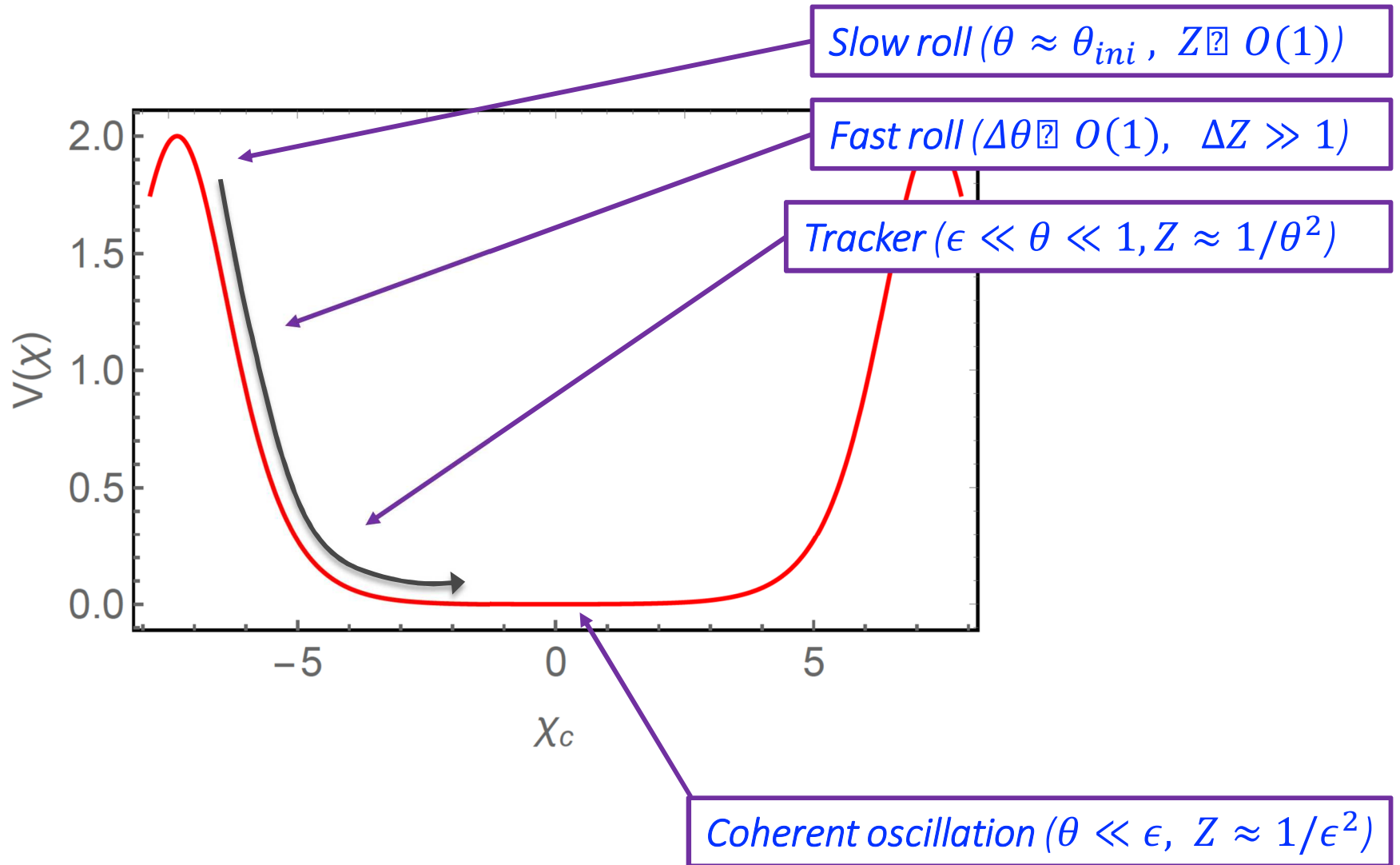


Coherent oscillation gives the dark matter abundance ?



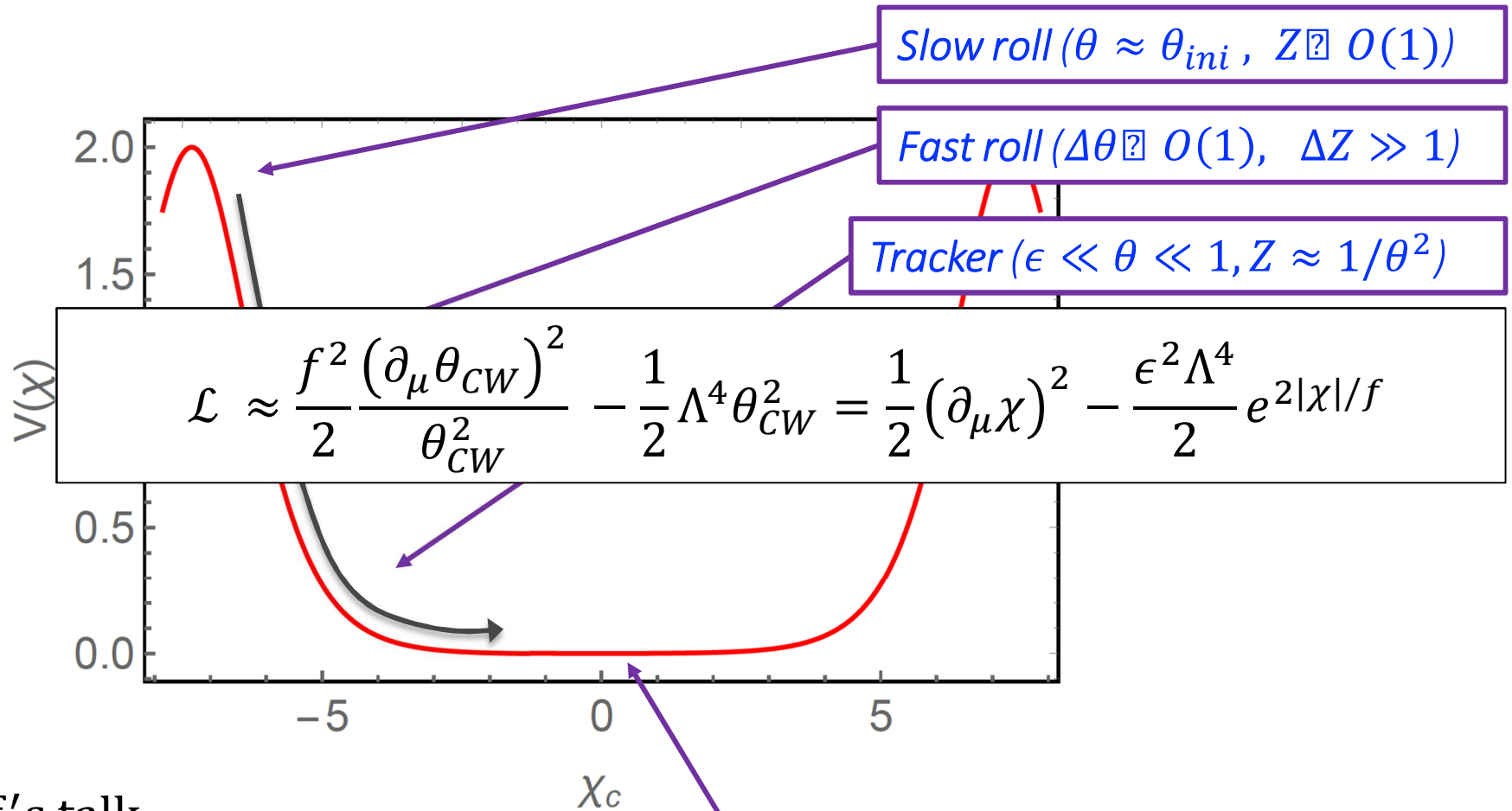
$$Z(\theta_{cW}) \sim 1/(1 + \epsilon^2 - \cos \theta_{cW})$$

The Journey with the rolling axion (in the canonical field basis) [Bae, Kost, CSS 1811.10655]



$$Z(\theta_{CW}) \sim 1/(1 + \epsilon^2 - \cos \theta_{CW})$$

The Journey with the rolling axion (in the canonical field basis) [Bae, Kost, CSS 1811.10655]



See Jeff's talk

Coherent oscillation ($\theta \ll \epsilon$, $Z \approx 1/\epsilon^2$)

$$\mathcal{L} \approx \frac{f^2}{2} \frac{(\partial_\mu \theta_{CW})^2}{\epsilon^2} - \frac{1}{2} \Lambda^4 \theta_{CW}^2 = \frac{1}{2} (\partial_\mu \chi)^2 - \frac{\epsilon^2 \Lambda^4}{2f^2} \chi^2$$

Conclusions

- *Discrete clockwork has very special features*
- *Natural extension to the continuum limit via 5D theory construction shows similar feature (spectrum and couplings relative to different KK modes). However the global structure is quite different*
- *Continuum clockwork axion is an example to provide a nontrivial wave-function*
- *Inflation, baryogenesis and dark matter could be related with rolling axion with deformed potential by CCW mechanism*