

# Axionic Electroweak Baryogenesis

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In collaboration with Kwang Sik Jeong (PNU) and Chang Sub Shin (CTPU)

arXiv: 1806.02591, 1811.03294

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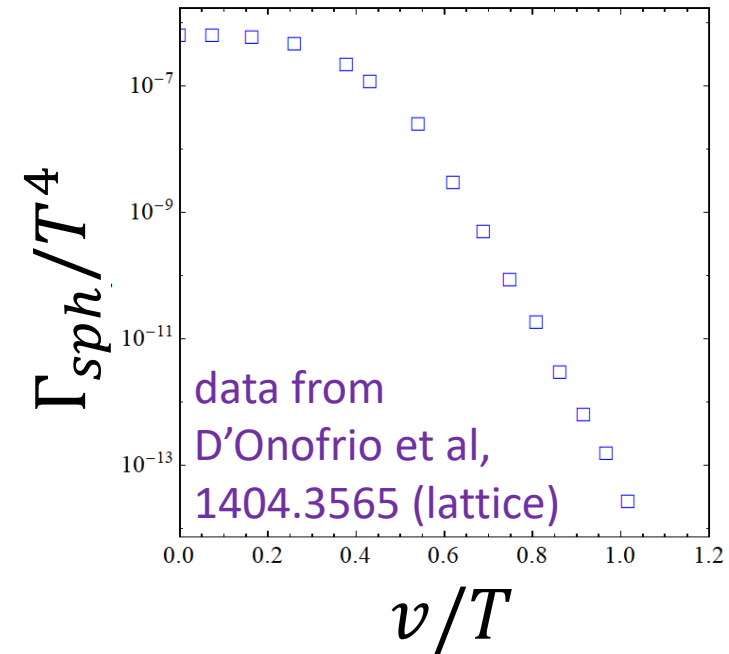
————→ BAU?

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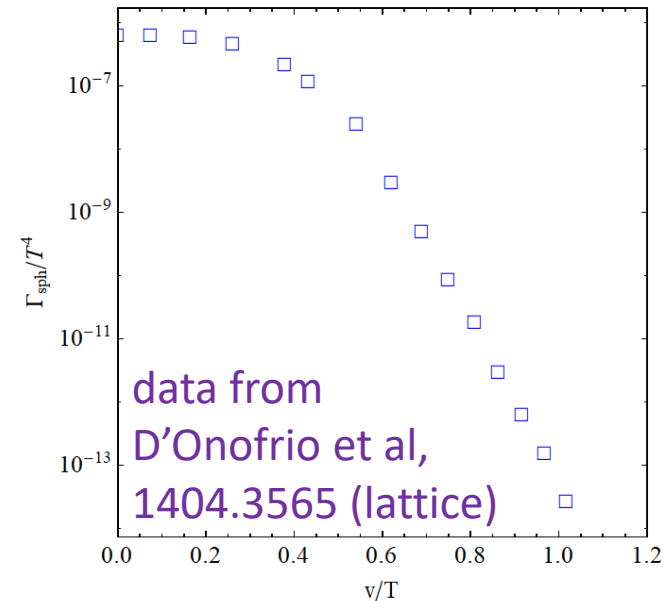
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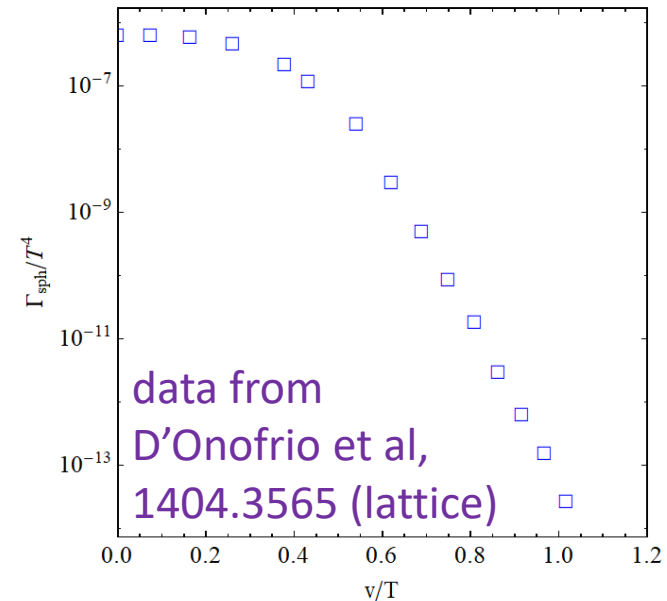
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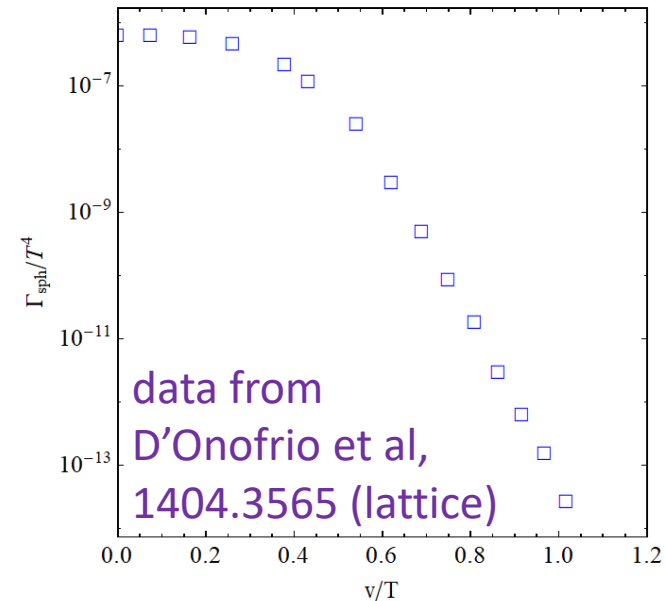
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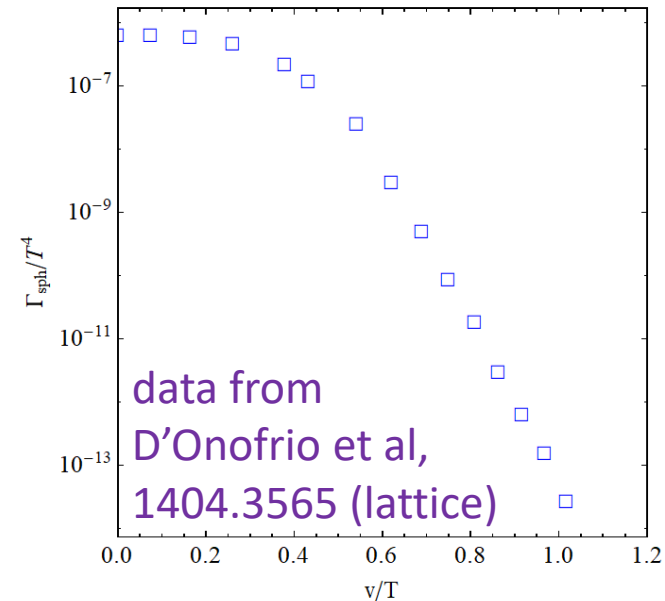
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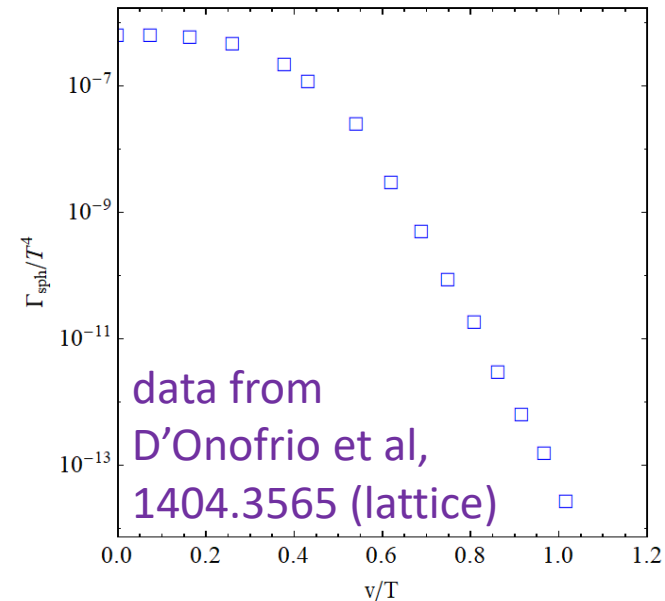
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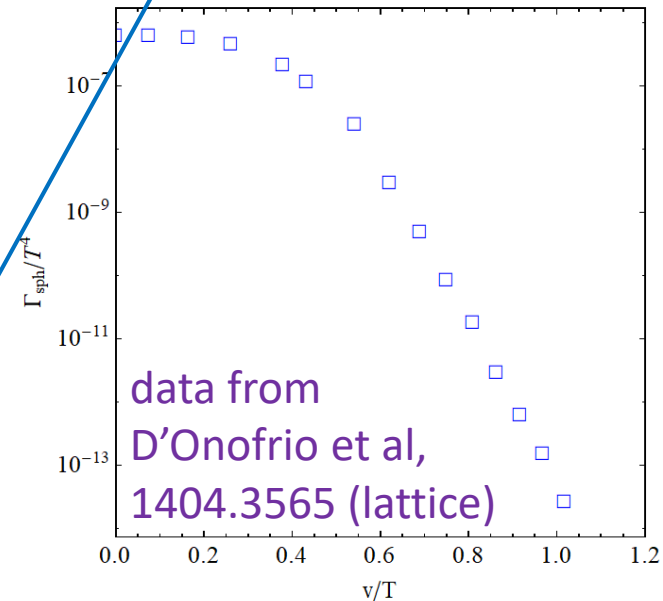
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Key words

**Sphaleron ( $B$  violation)**

**First order EWPT (out of equilibrium)**

**CP violation**

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**First order EWPT (out of equilibrium): Higgs mass should be lighter.**



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New physics  $\Rightarrow$  LHC signal



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Only constraints are getting stronger and stronger...

**Any EWBG model free from EDM or LHC?**

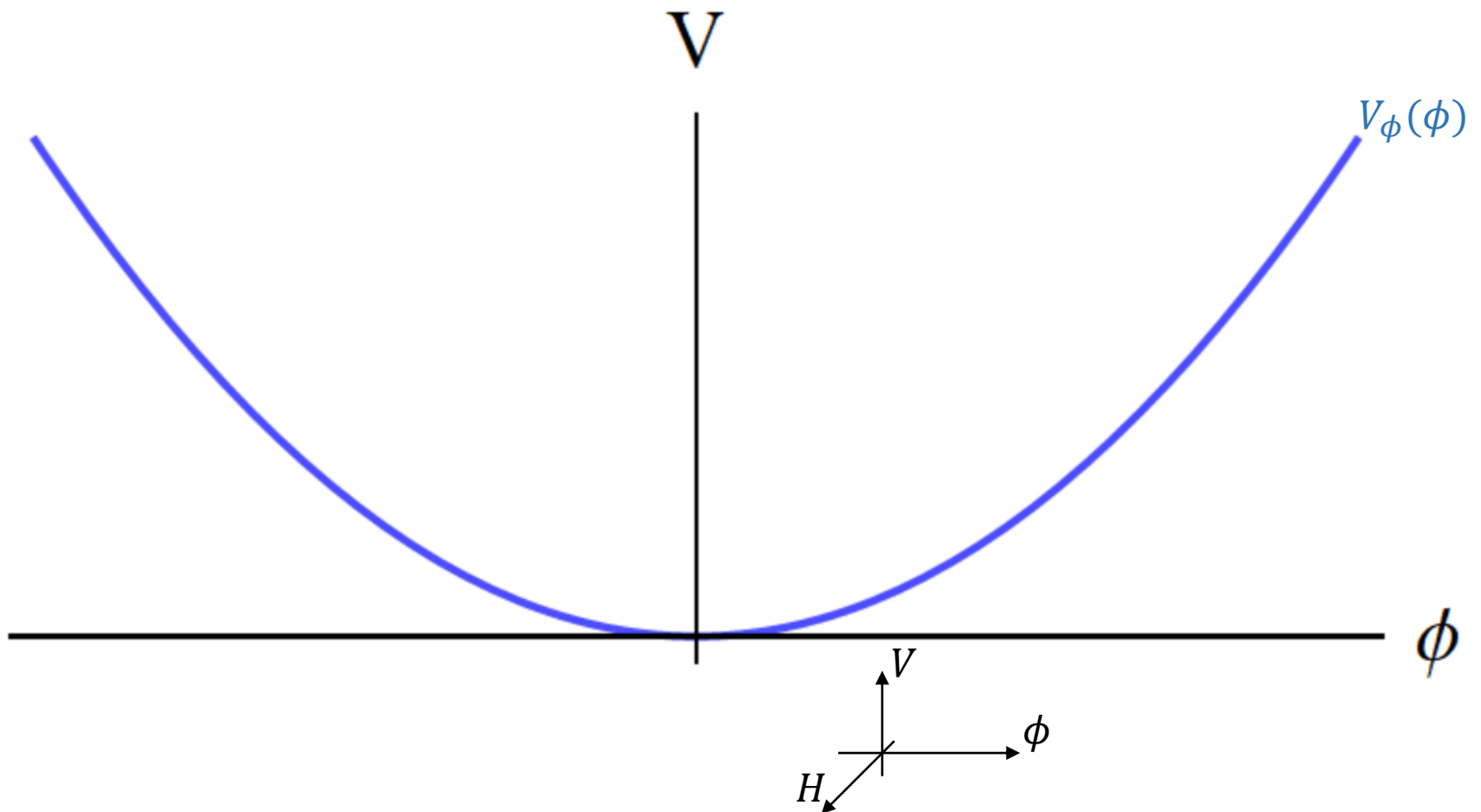
$\Rightarrow$  *One example in this talk*

# Contents

- Phase transition structure
- CP violation
- Phenomenology

# First order EWPT with field-dependent Higgs mass

$$V(\phi, H) = \lambda |H|^4 + \mu_h^2(\phi) |H|^2 + V_\phi(\phi)$$

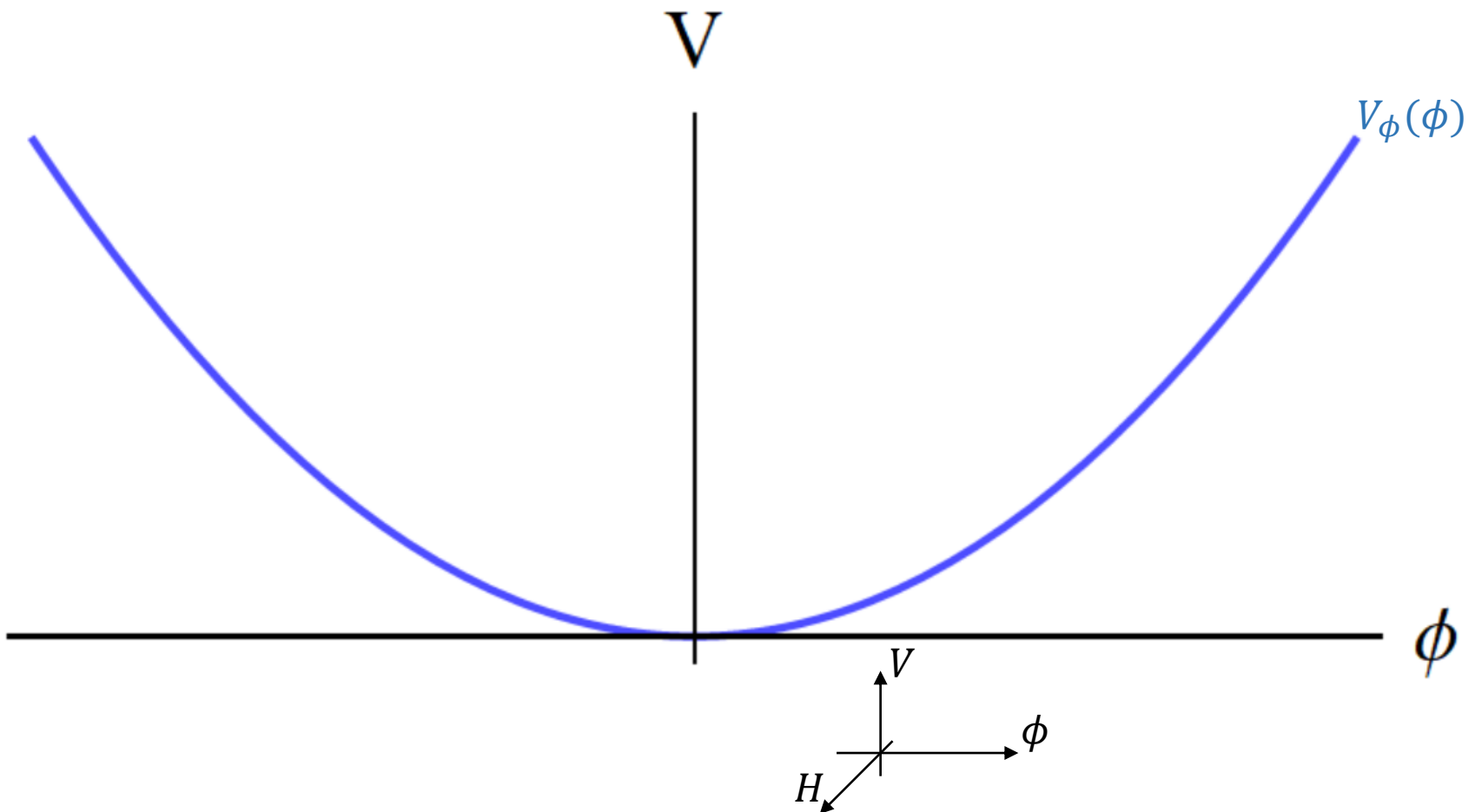




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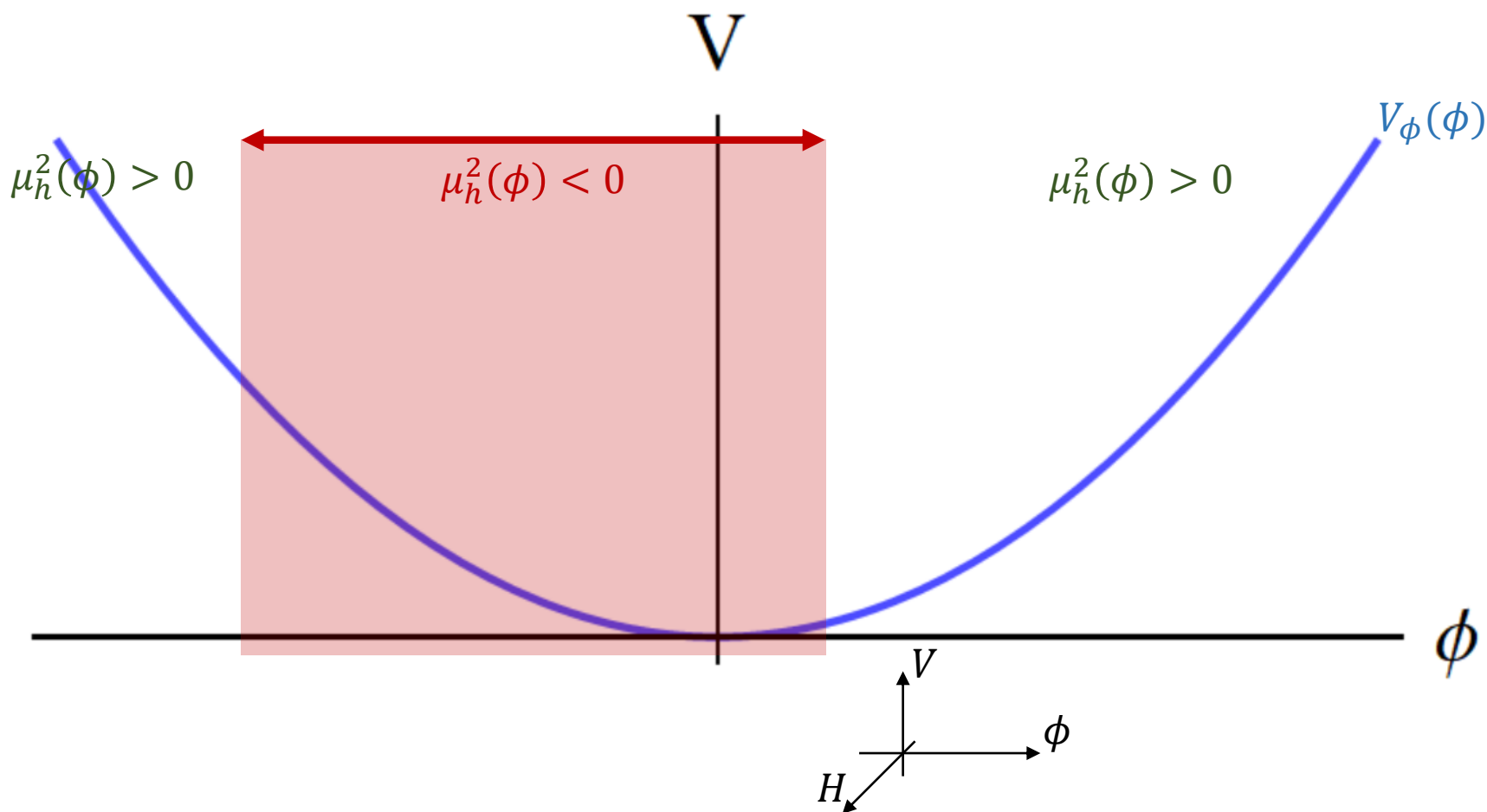
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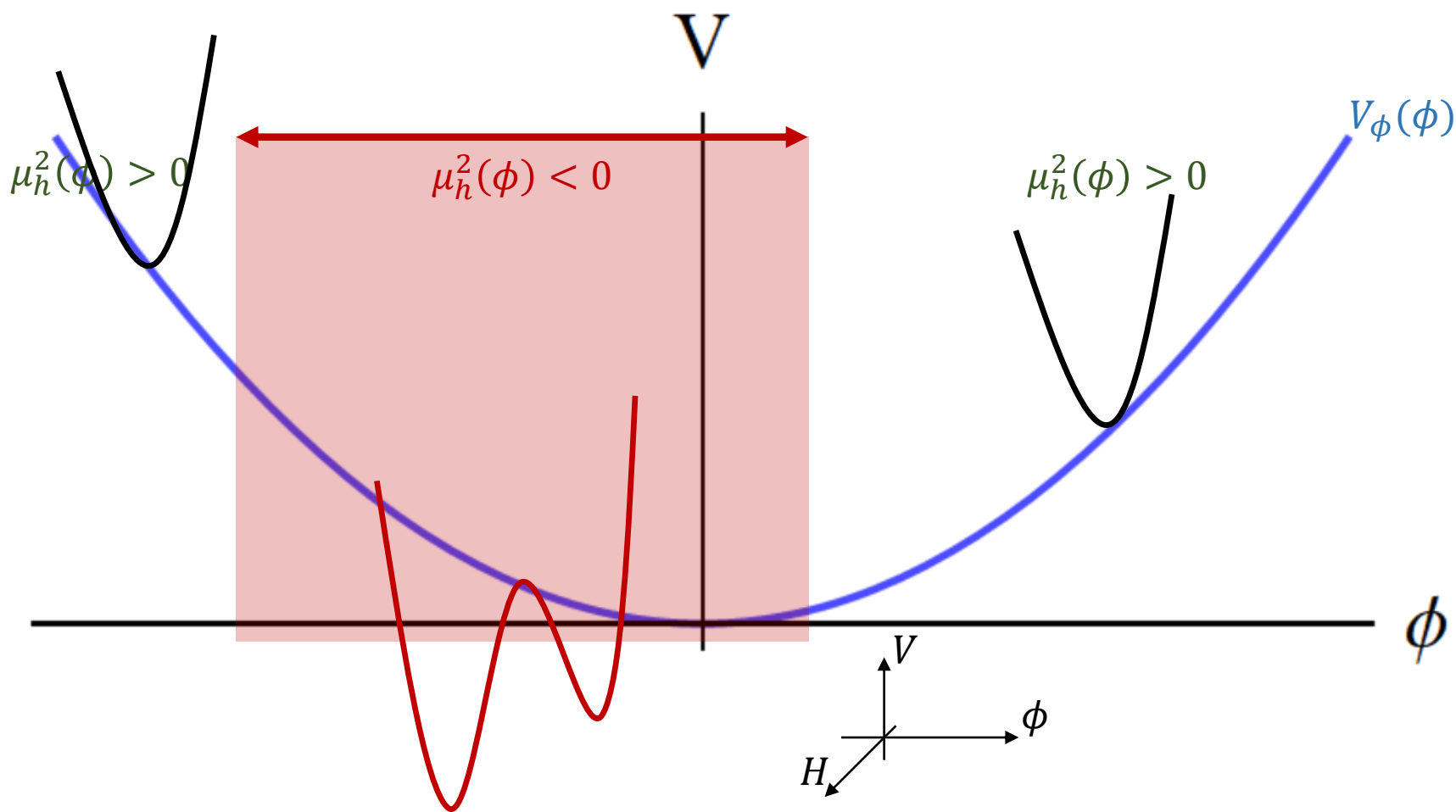
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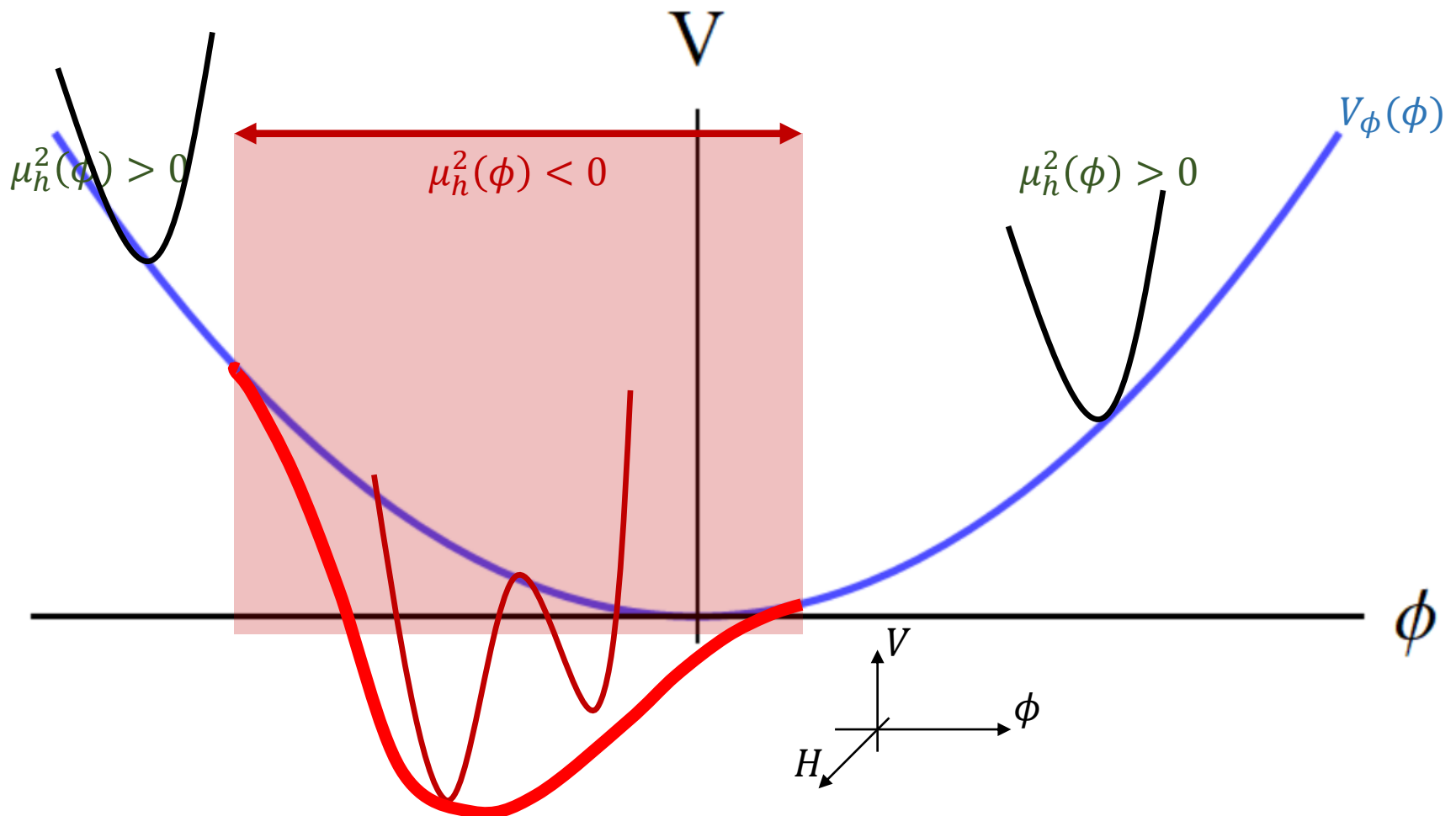
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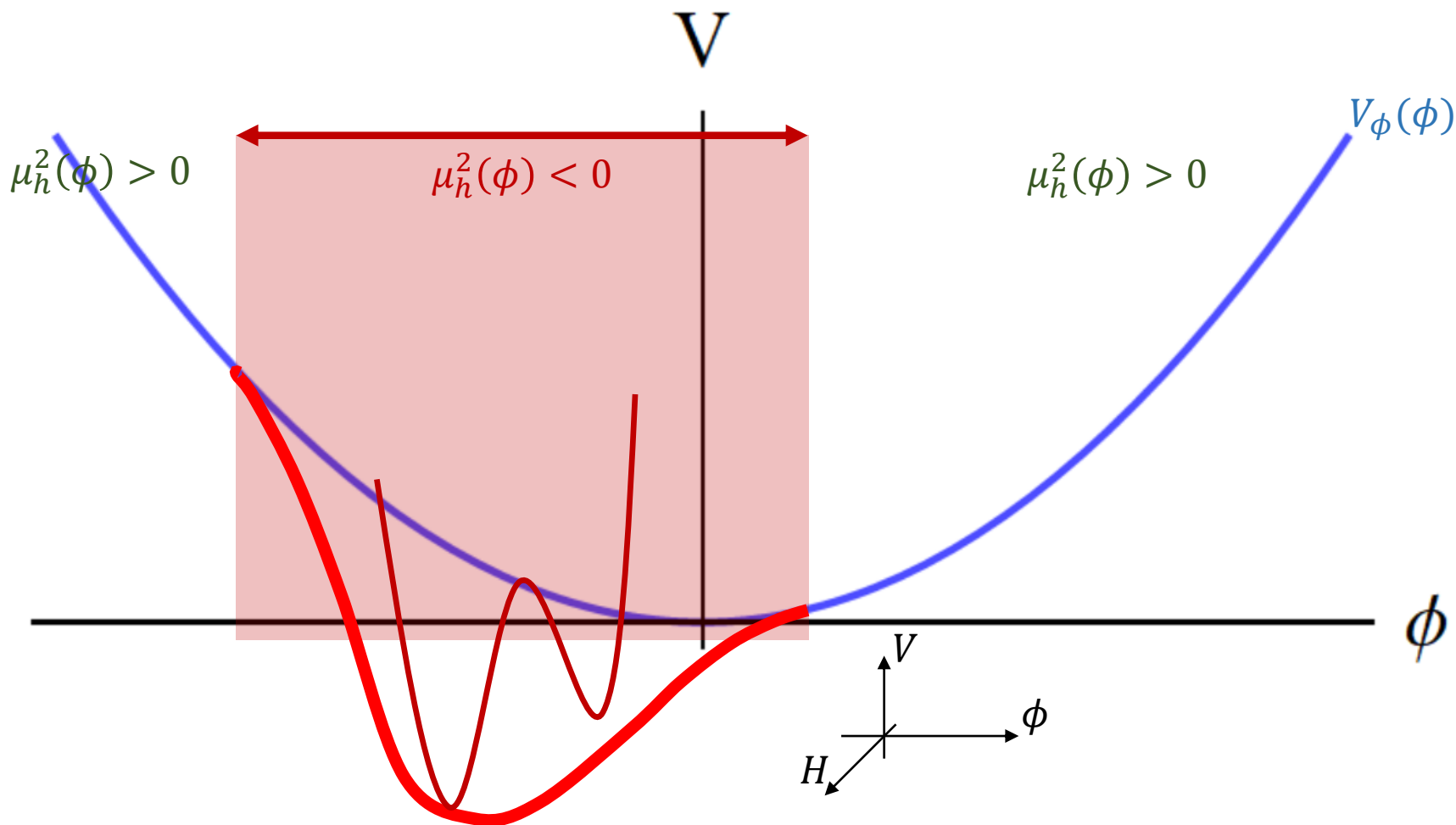


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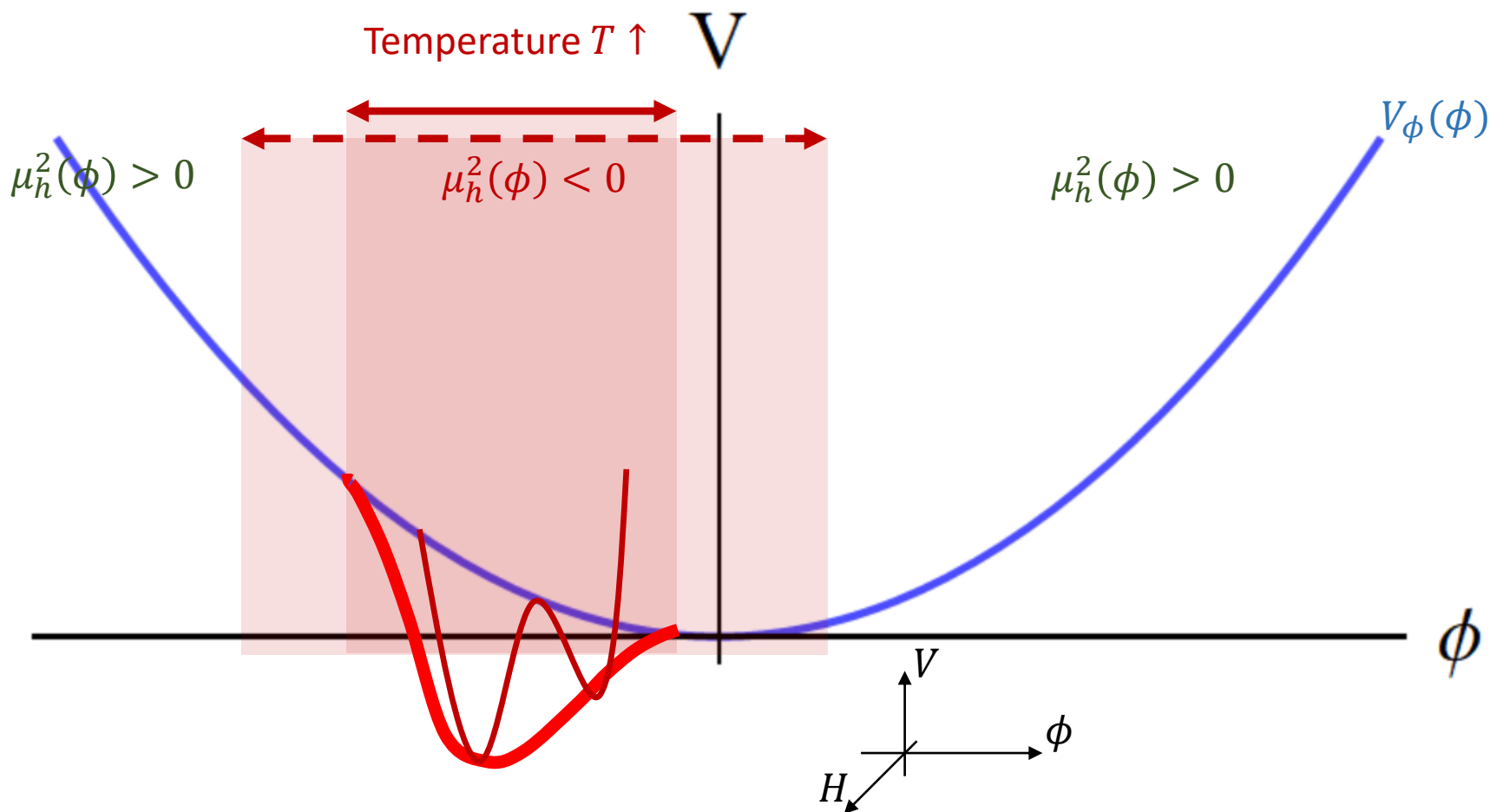
at a finite temperature?



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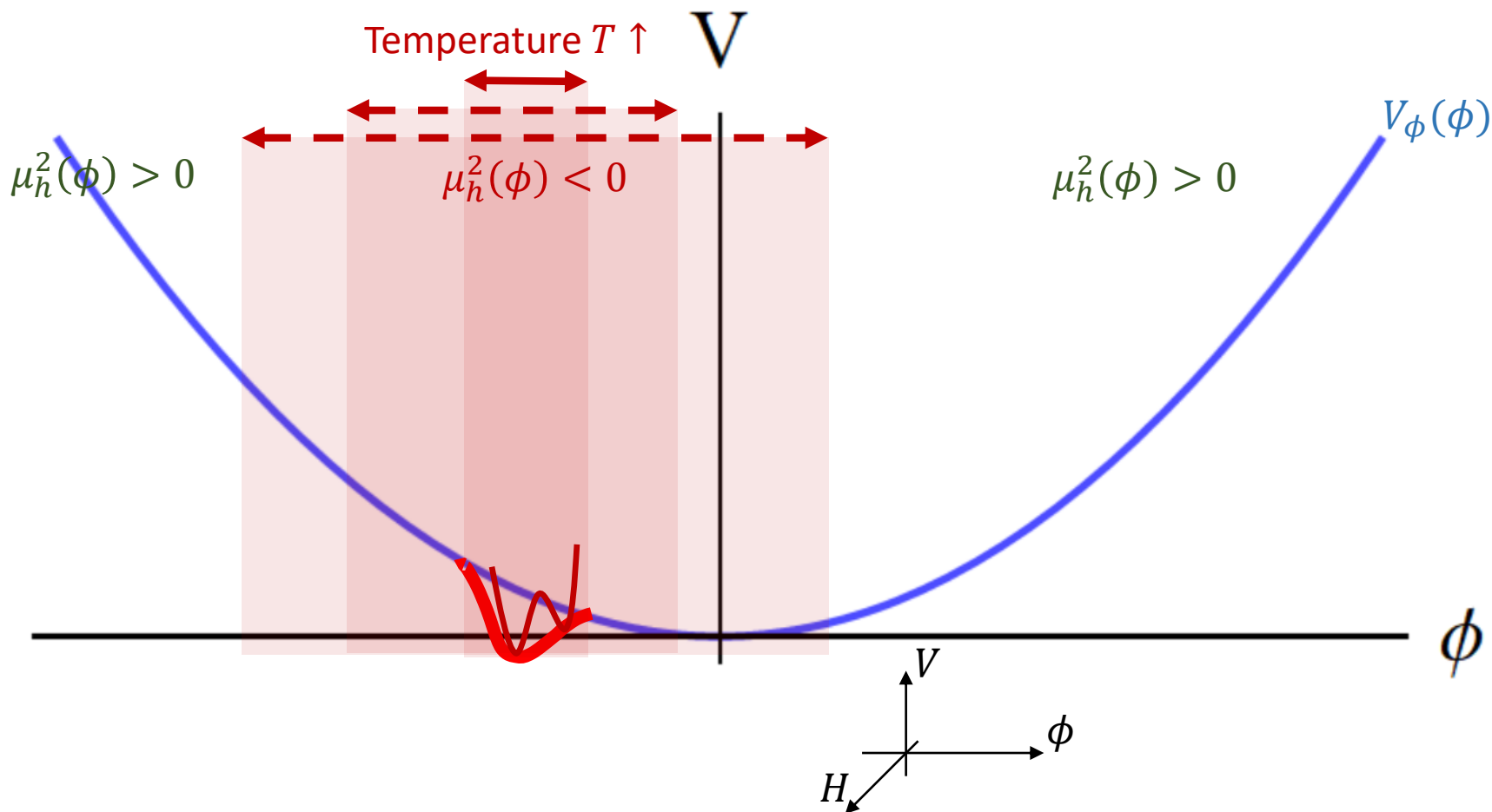
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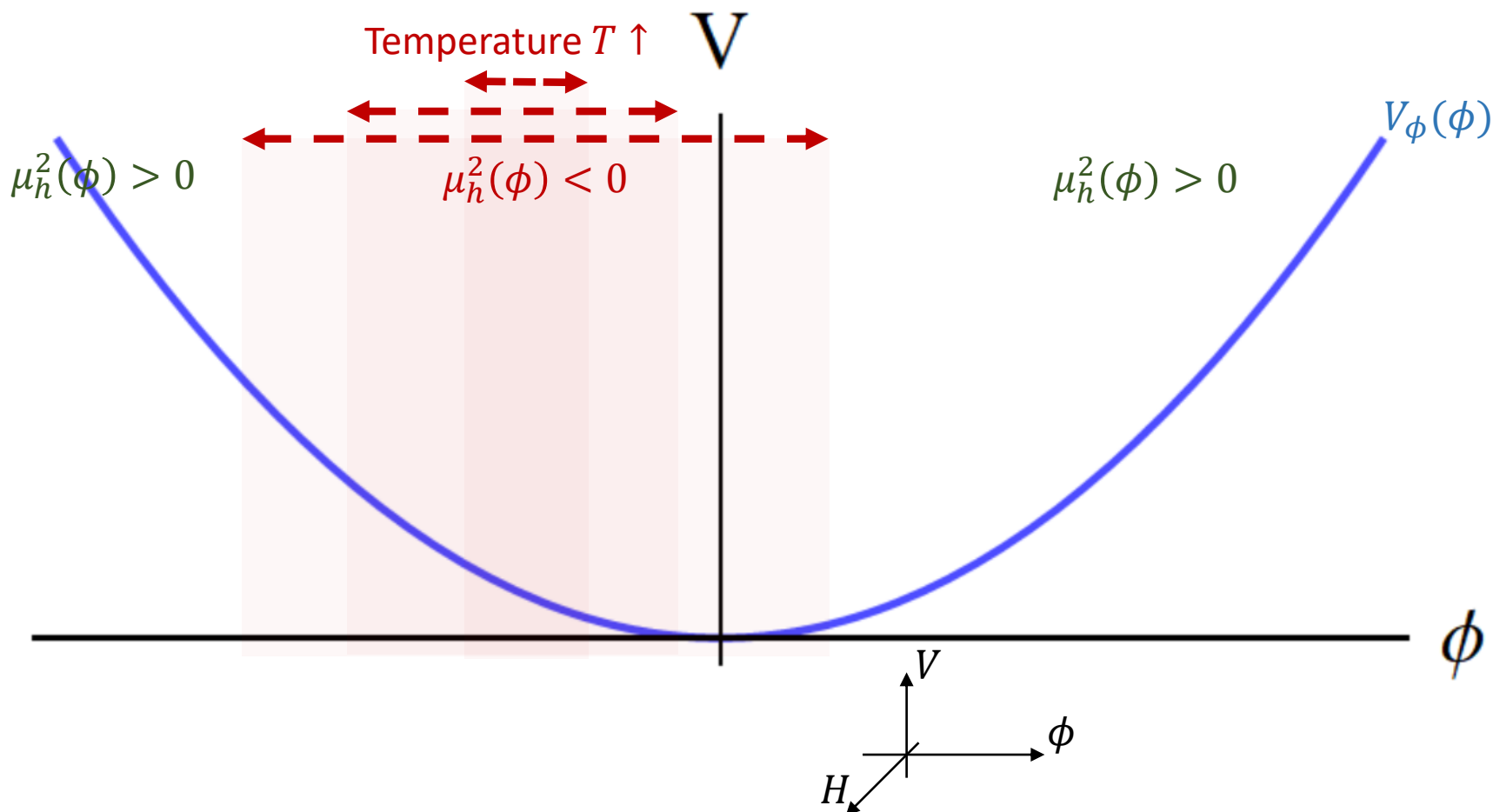
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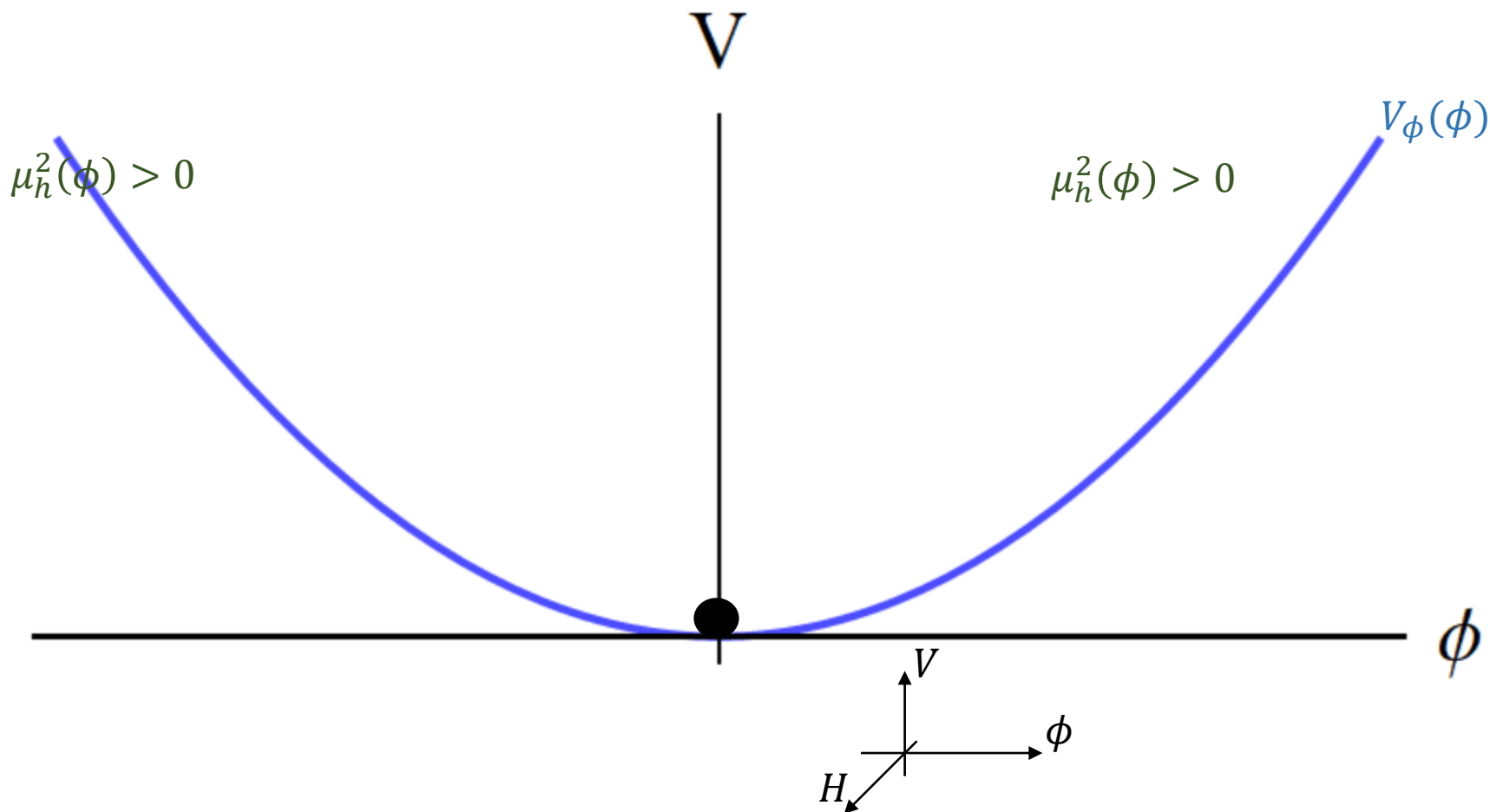




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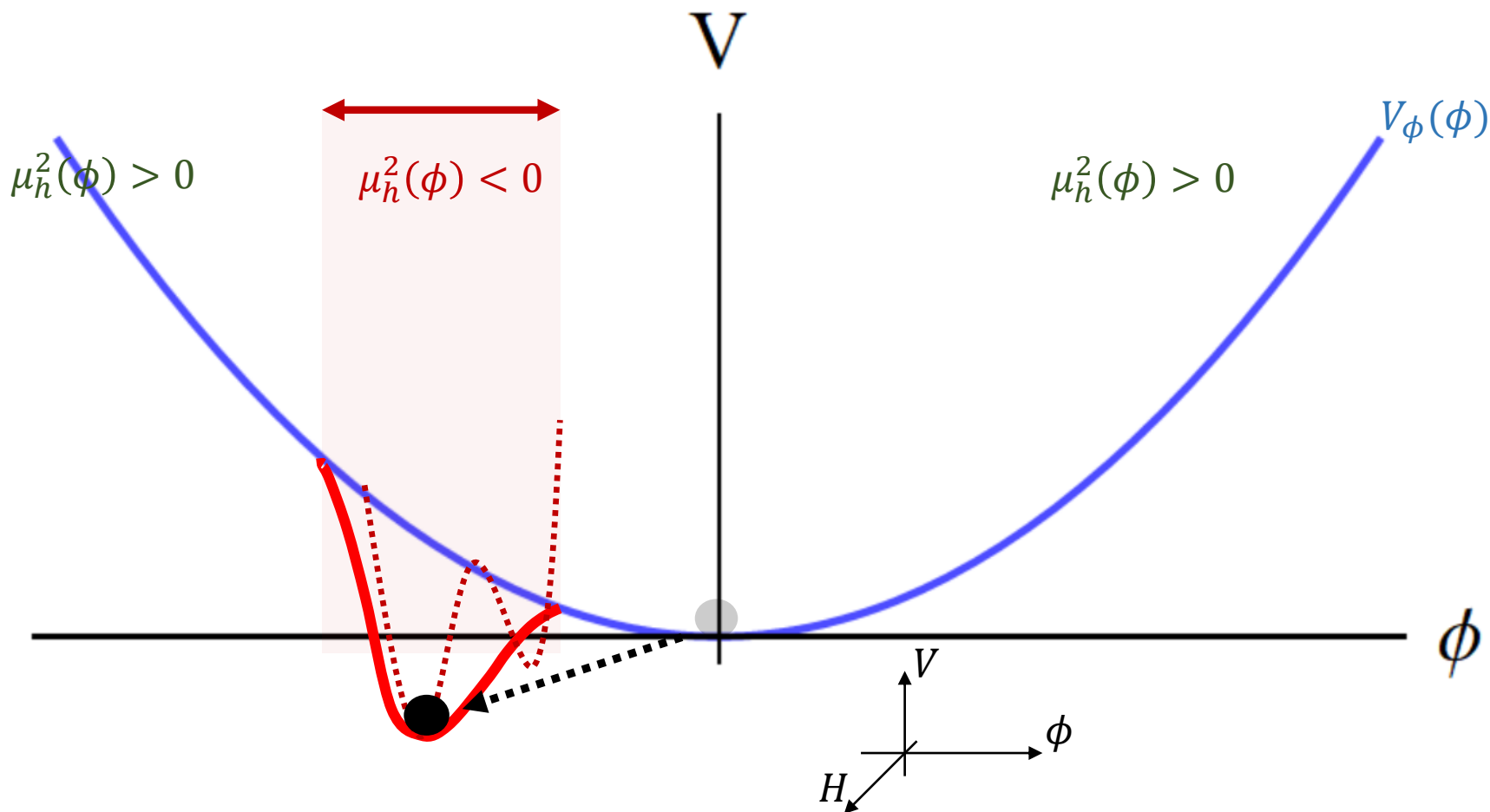
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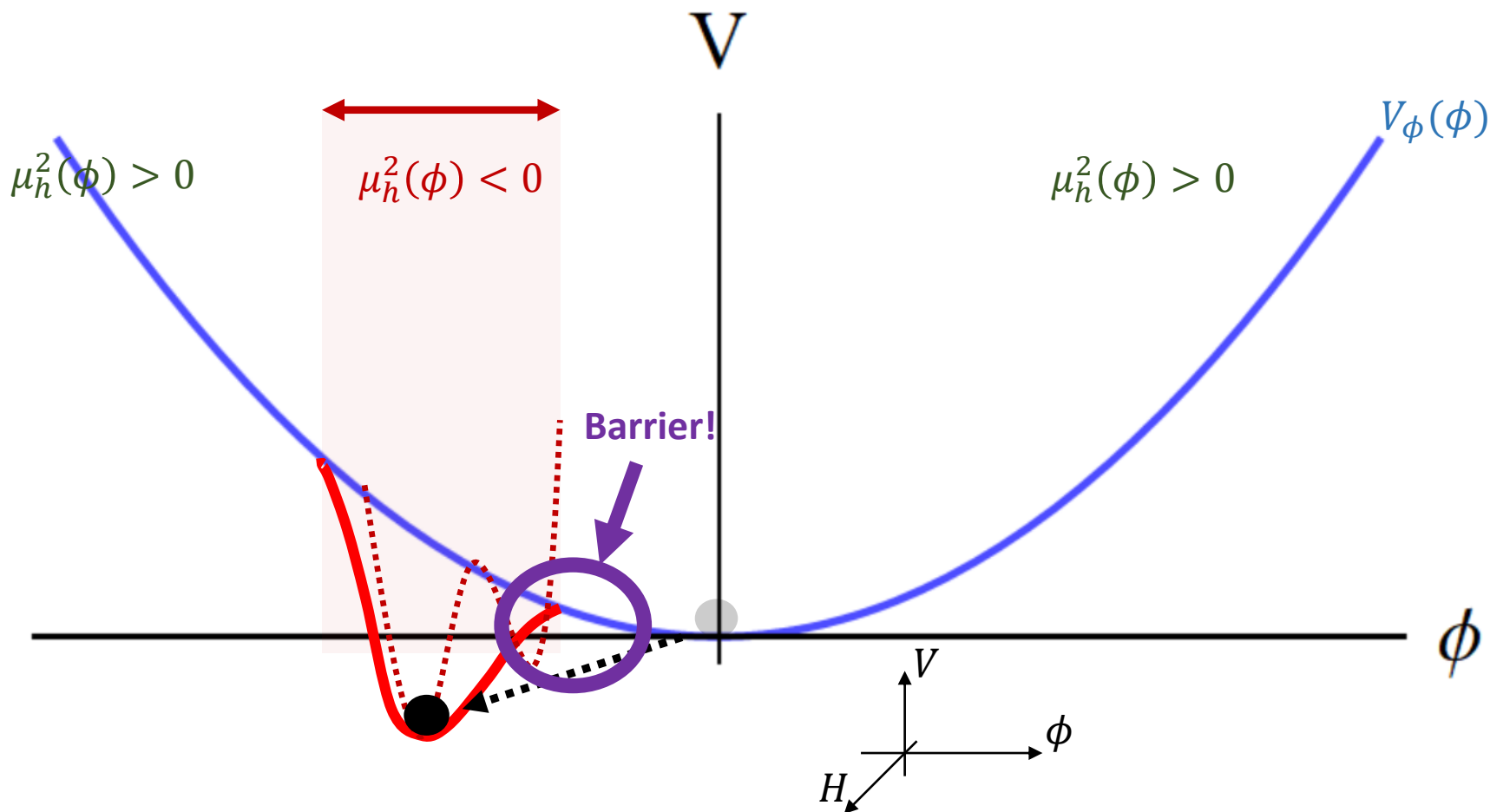
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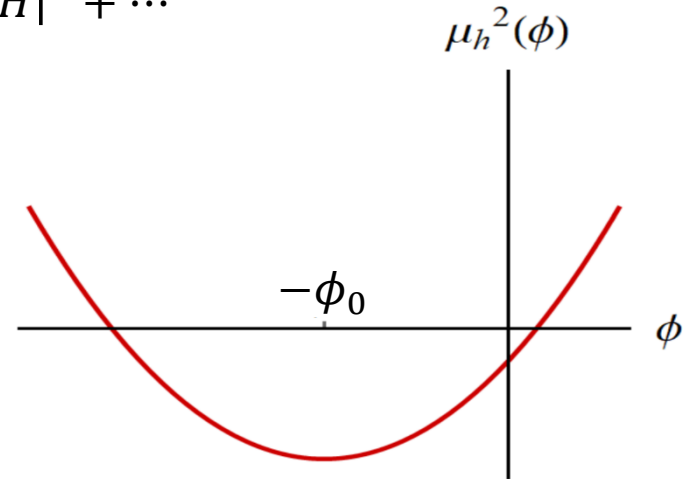
Conditions for  $\mu_h^2(\phi)$  ?

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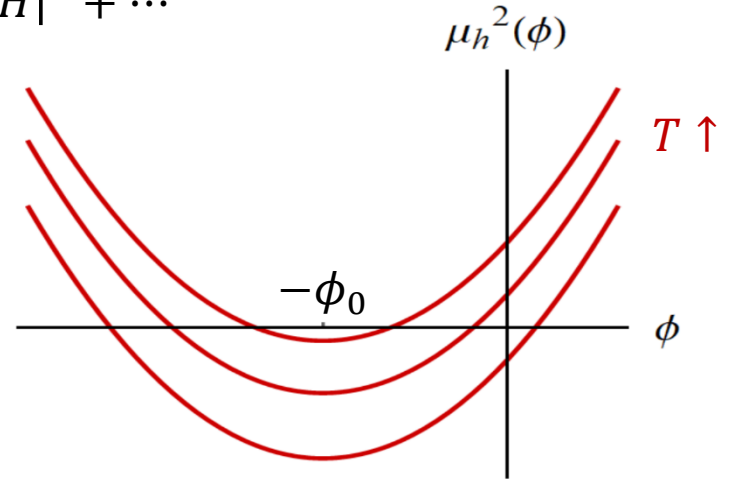


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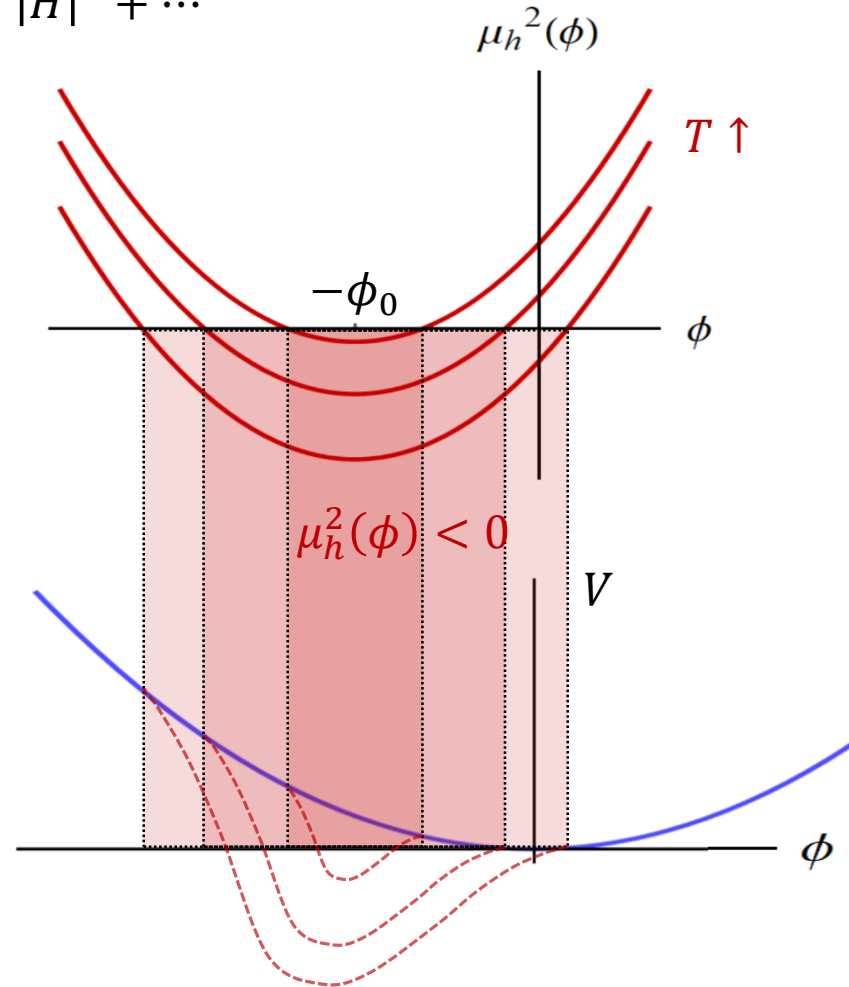


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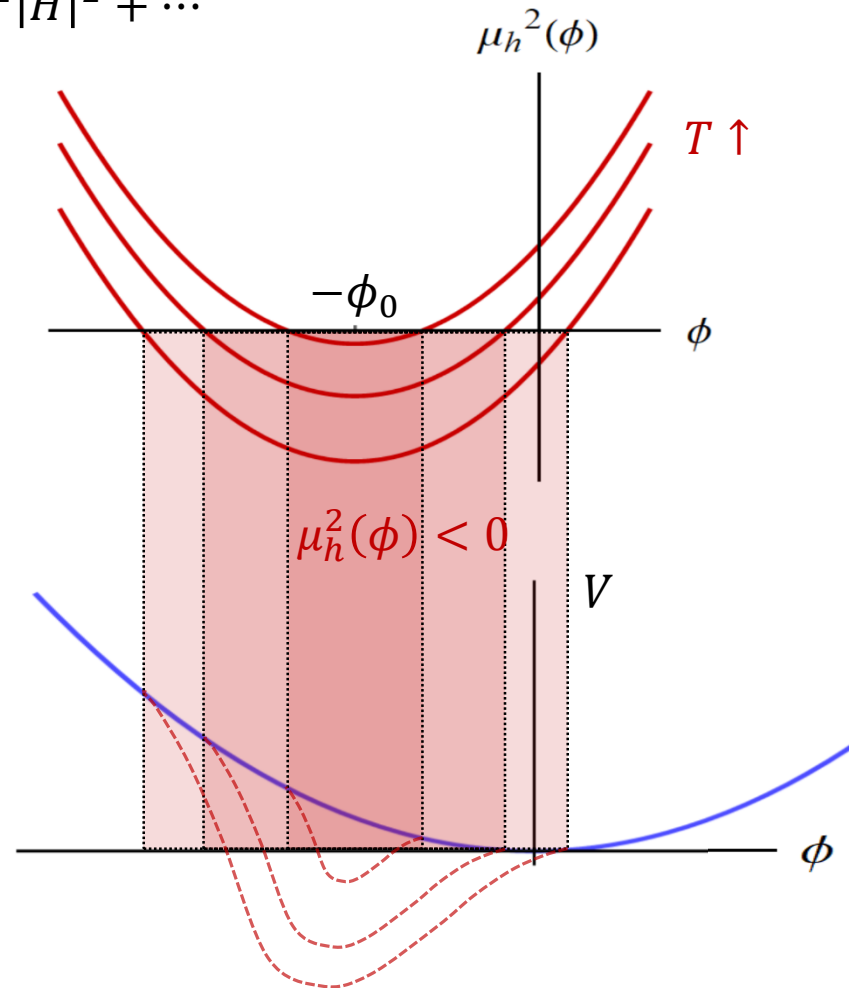
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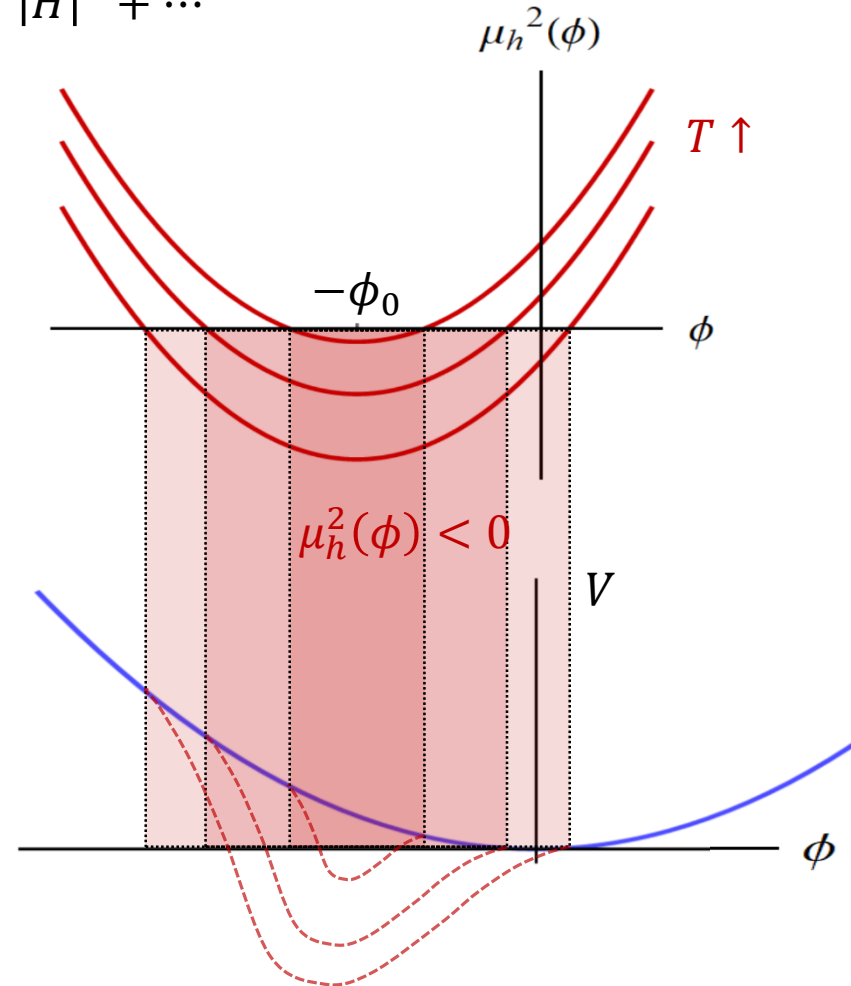
**Conditions? weakly coupled limit?**

For Higgs mass and vev,

$$\mu_0 \simeq \sqrt{\lambda} v_h = 88 \text{ GeV} \sim O(m_w)$$

For a strongly first-order EWPT,

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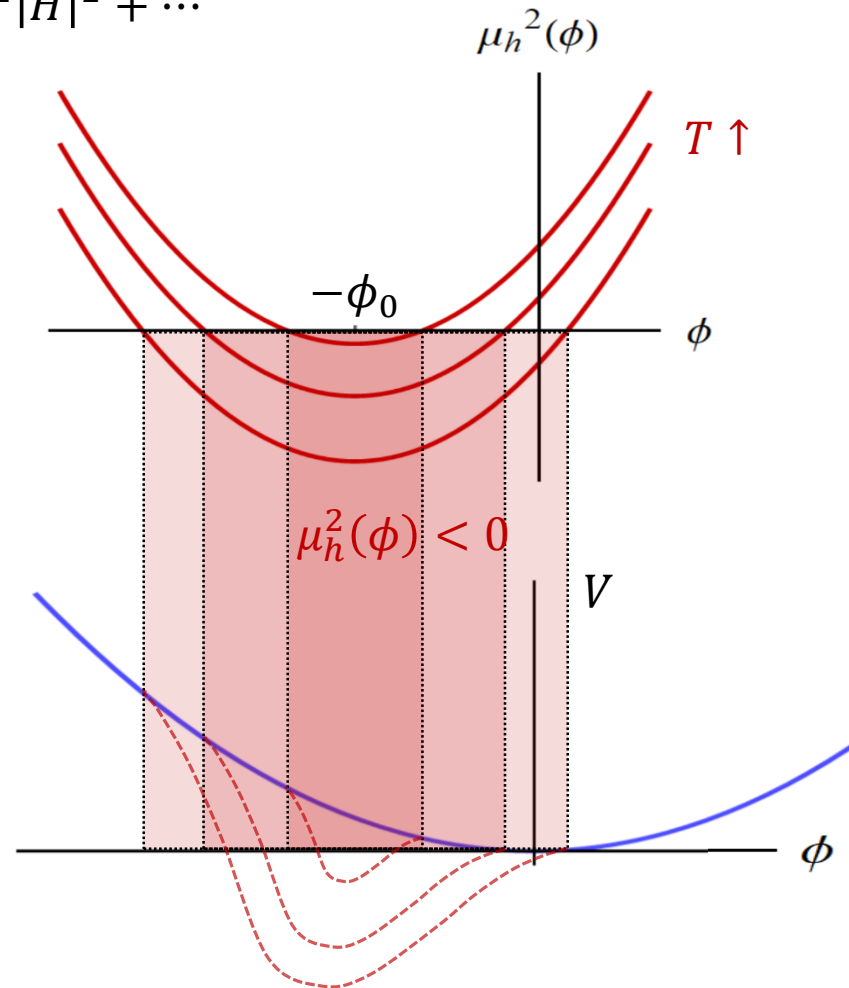
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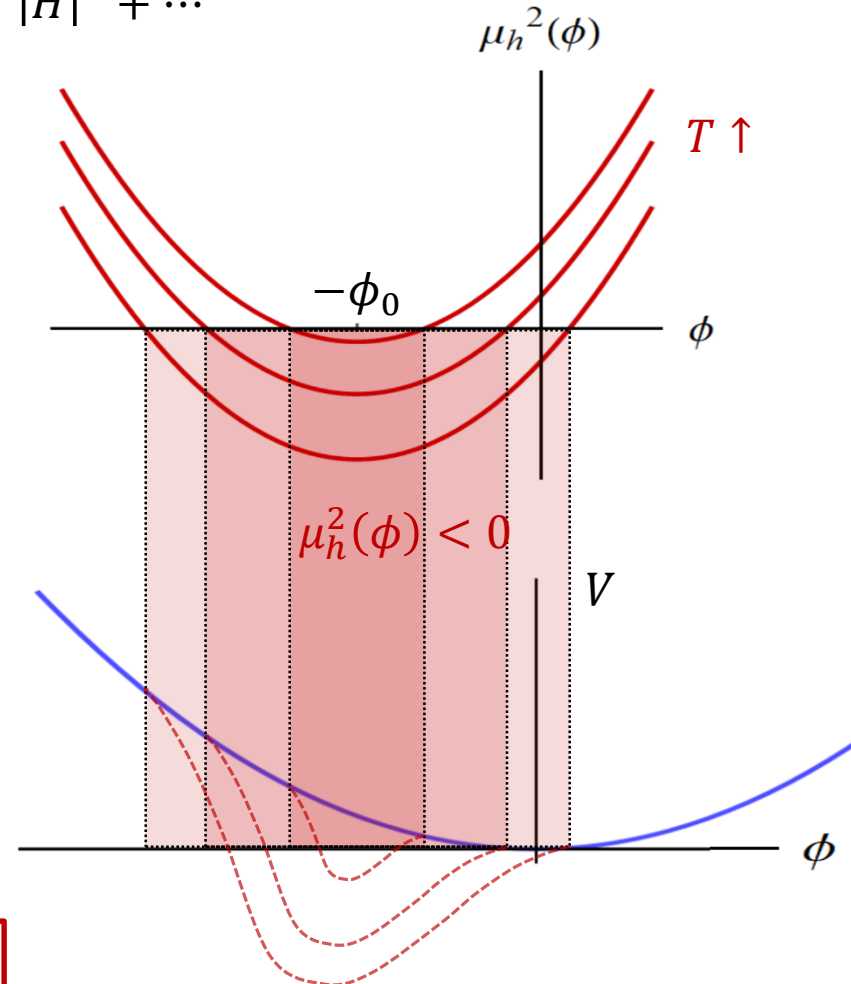
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Weakly coupled limit:  $\frac{m_w^2}{\phi_0^2} \lesssim \lambda_{\text{mix}} \ll 1$  ?

**Easily satisfied if  $\phi = \text{ALP}$**



# First order EWPT with an ALP

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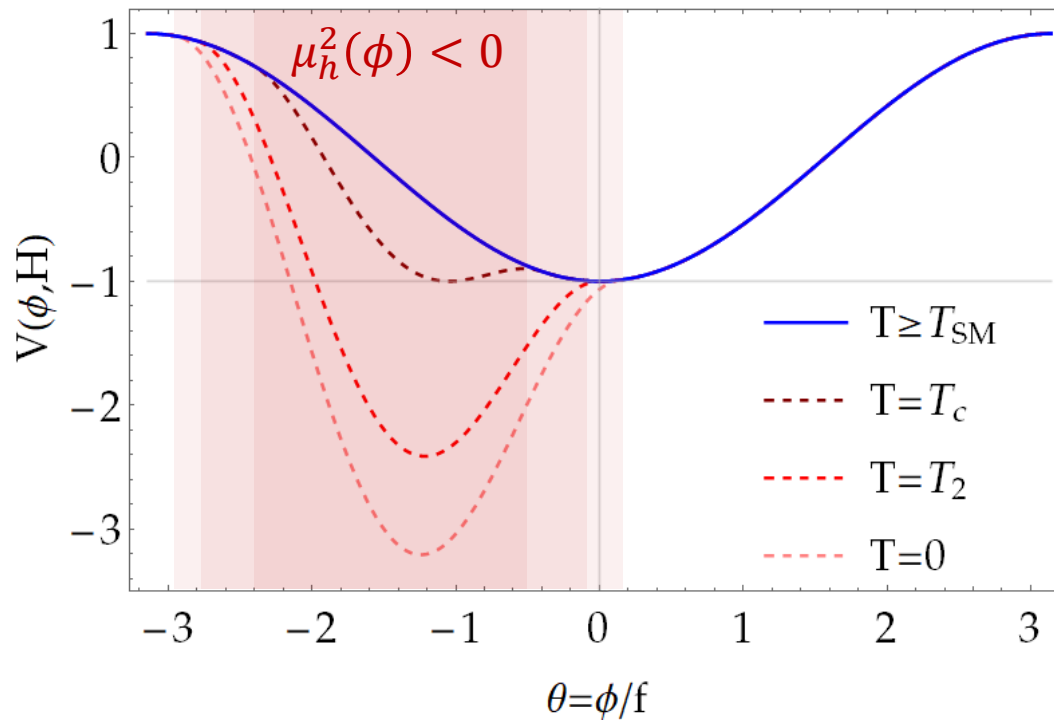
Our model)  $\mu_h^2 = M^2 \cos\left(\frac{\phi}{f} + \alpha\right) - \mu_0^2, \quad V_\phi(\phi) = -\Lambda^4 \cos\left(\frac{\phi}{f}\right)$

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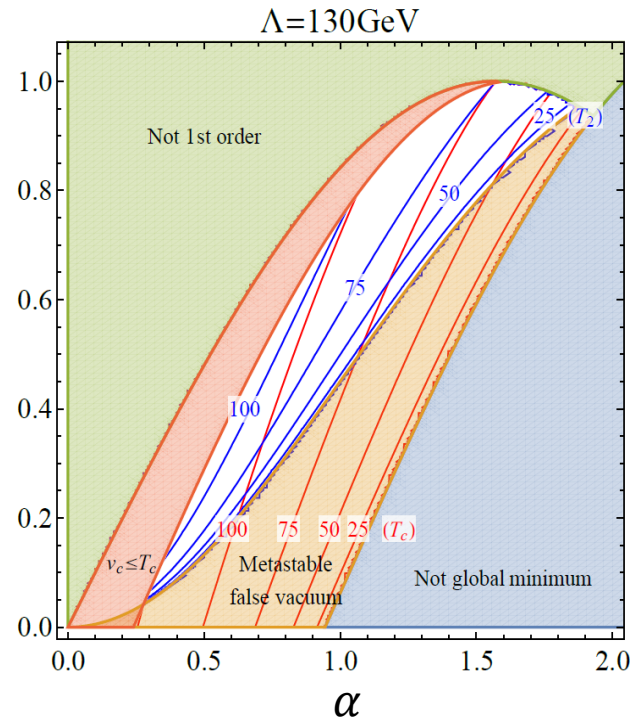
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(the potential is written in terms of  $\theta = \phi/f$ , not  $\phi$  and  $f$ , individually)

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$T_c$  : critical temperature  
 $T_2$  : barrier disappearing temperature

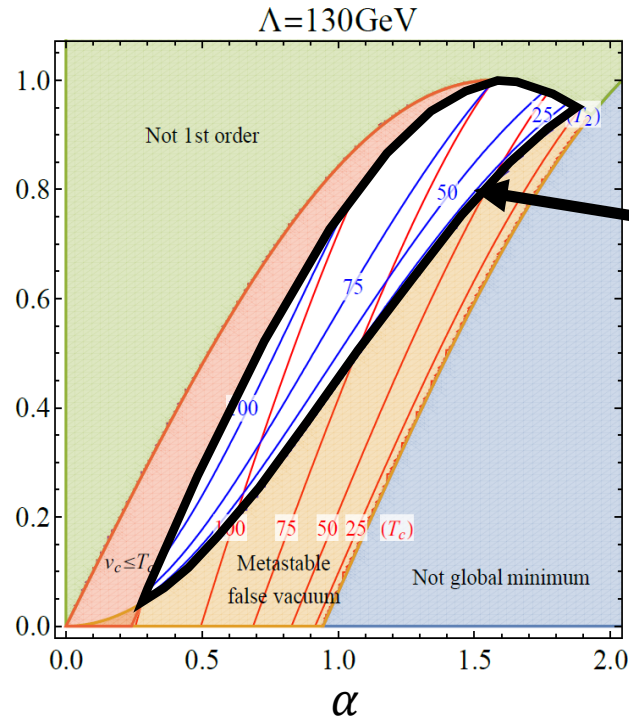
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Suitable for EWBG  
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Weakly coupled limit: simply large  $f \gg m_w$

$$\left( \frac{m_w^2}{\phi_0^2} \lesssim \lambda_{\text{mix}} \ll 1 \right)$$





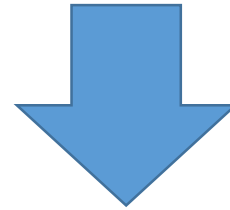
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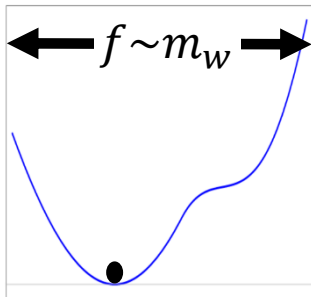


**It changes many things!!**

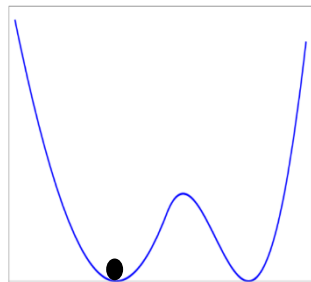
How?

# What changes at large $f$ ?

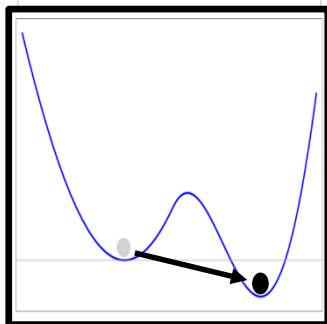
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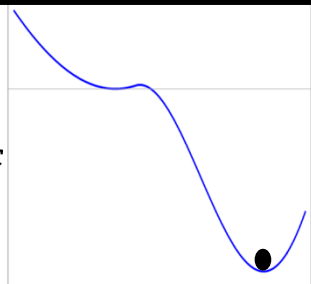
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$$T \lesssim T_c$$

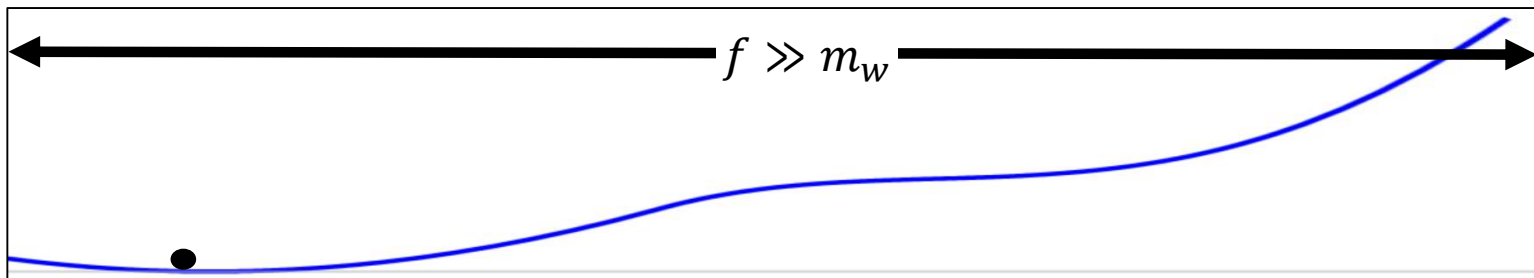


$$T_2 \lesssim T < T_c$$

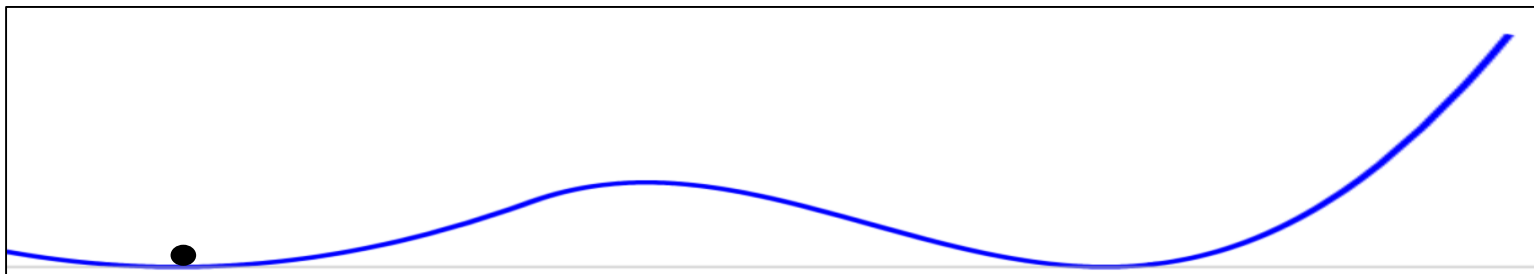


# What changes at large $f$ ?

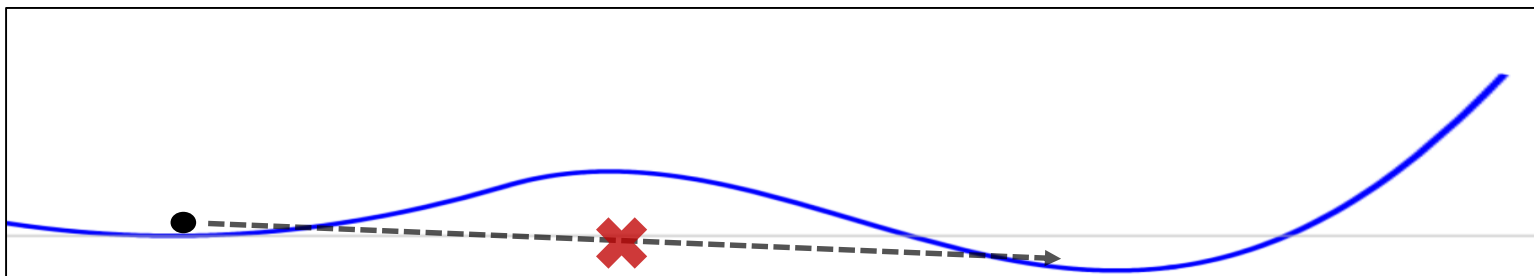
$$T > T_c$$



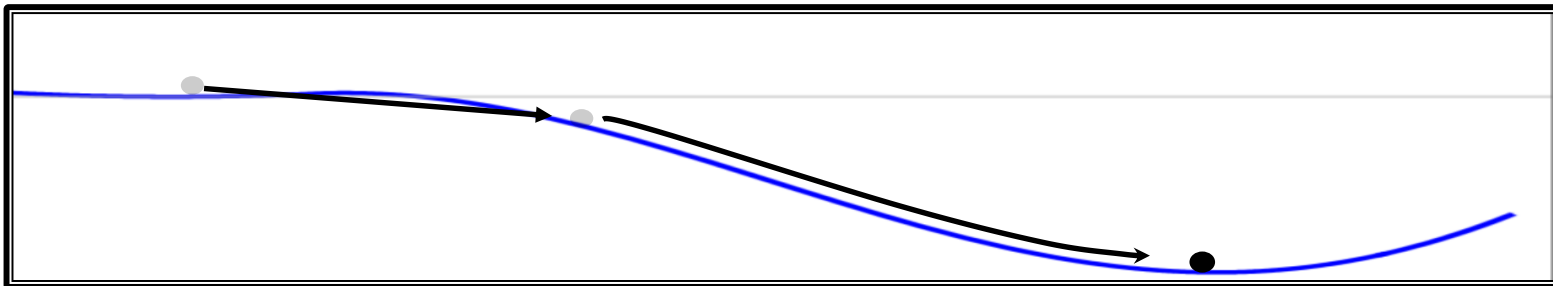
$$T = T_c$$



$$T \lesssim T_c$$



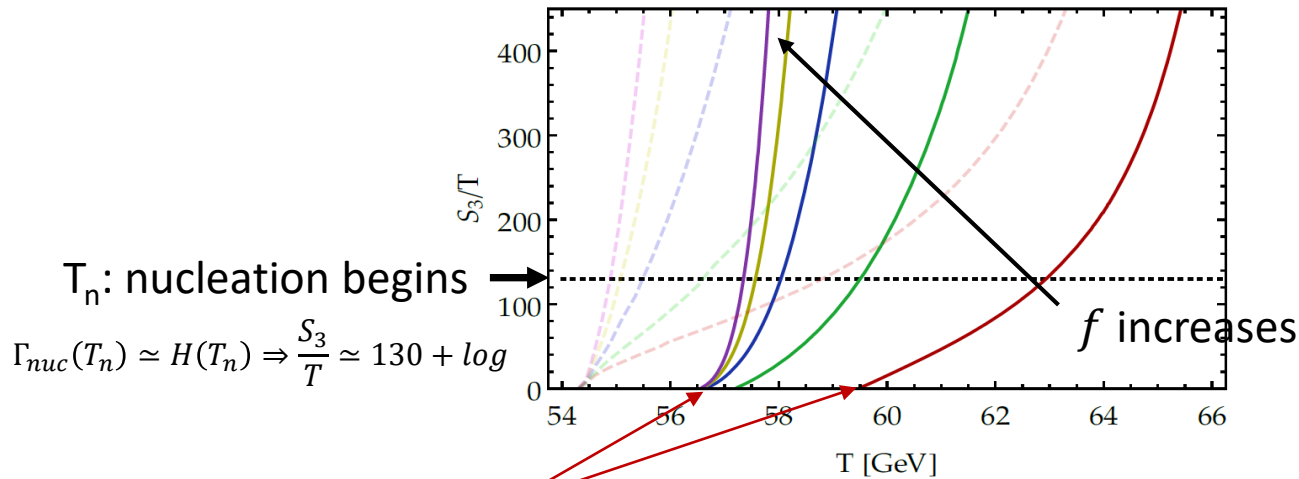
$$T_2 \lesssim T < T_c$$



# What changes at large $f$ ?

Critical action:  $S_3 = 4\pi \int r^2 dr \left( \left( \frac{dh}{dr} \right)^2 + \left( \frac{d\phi}{dr} \right)^2 + V(h, \theta) \right)$

$$= 4\pi f^3 \int x^2 dx \left( \frac{h'^2}{2f^2} + \frac{\theta'^2}{2} + V(h, \theta) \right) \propto f^3, \quad x \equiv \frac{r}{f}, \quad ' \equiv \frac{d}{dx}$$



**$T_2$ : barrier disappearing temperature**

$$S_3/T \propto (T - T_2)^n f^3$$

$$\Rightarrow T_n \simeq T_2, \quad \Delta t_{PT} \simeq \frac{6}{\beta} \propto f^{3/n} \quad \text{where } \beta = d(S_3/T)/dt|_{T=T_n}$$



Is  $f$  really irrelevant?

ans: NO

One obvious change: **the physical field distance between two local minima  $\propto f$ .**

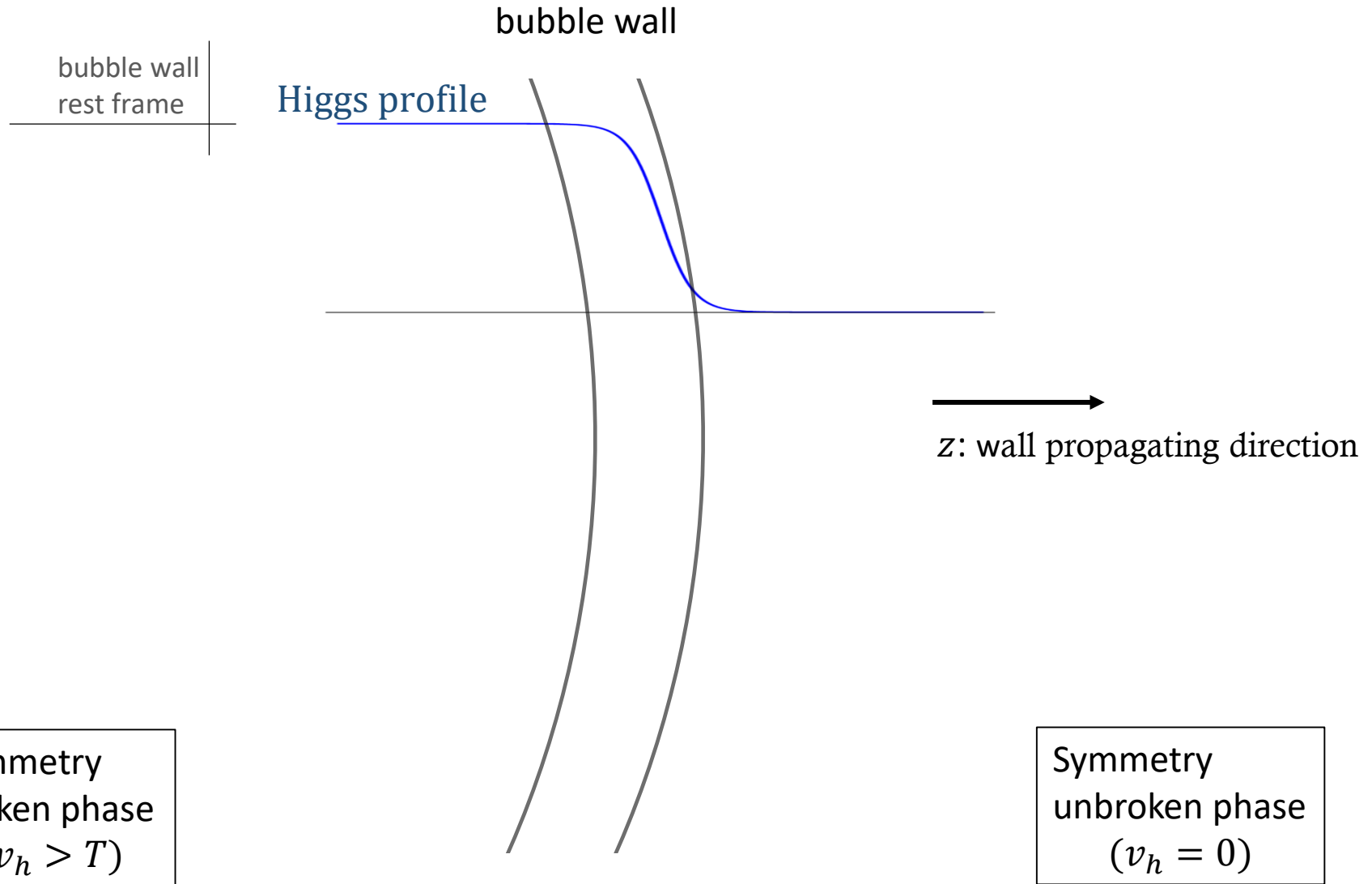
$\Rightarrow$  Phase transition is delayed (i.e. supercooling occurs):  $T_n \simeq T_2 < T_c$



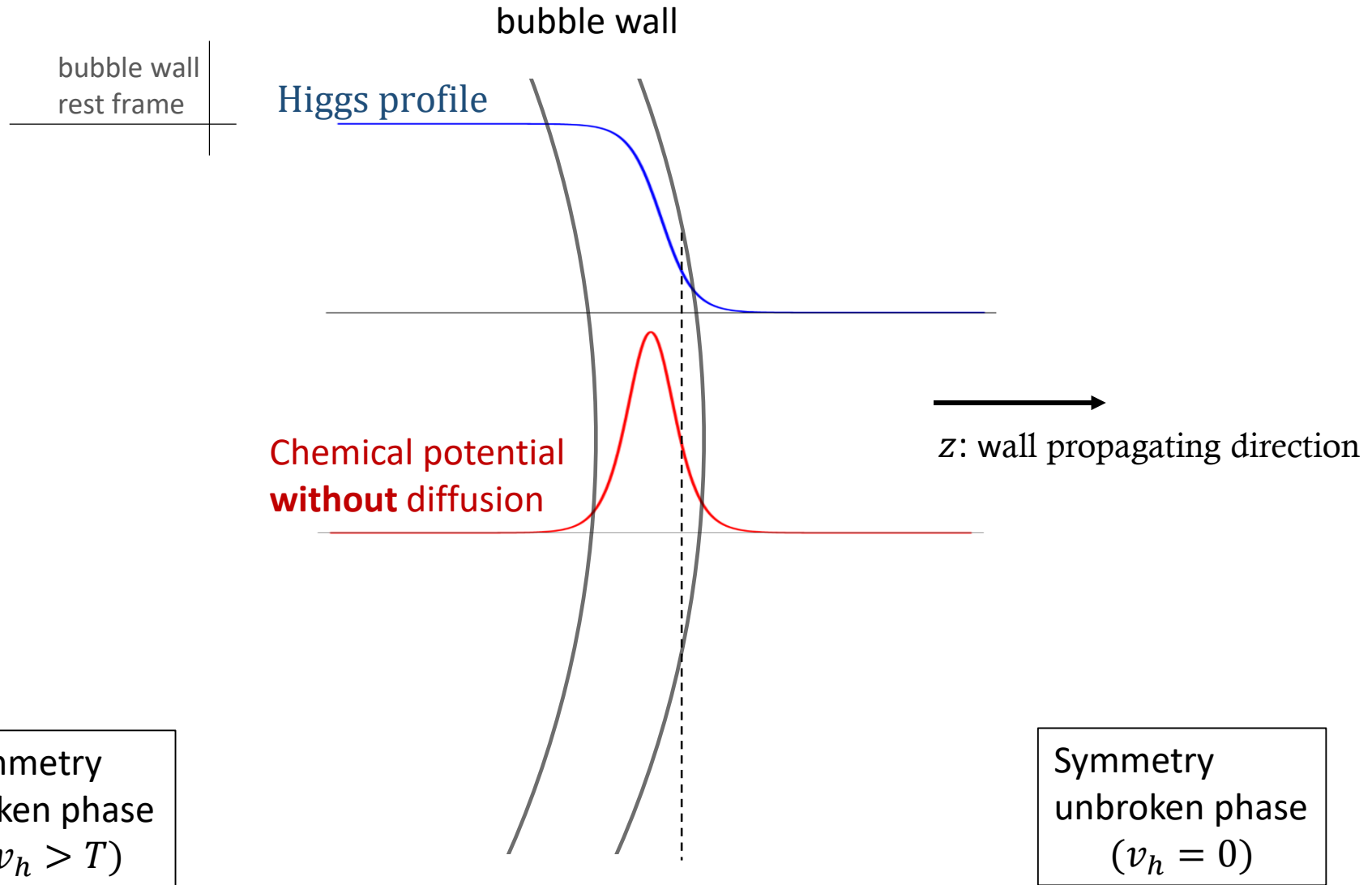
How does it affect baryogenesis?

e.g. diffusion effect

# Diffusion effect around bubble wall

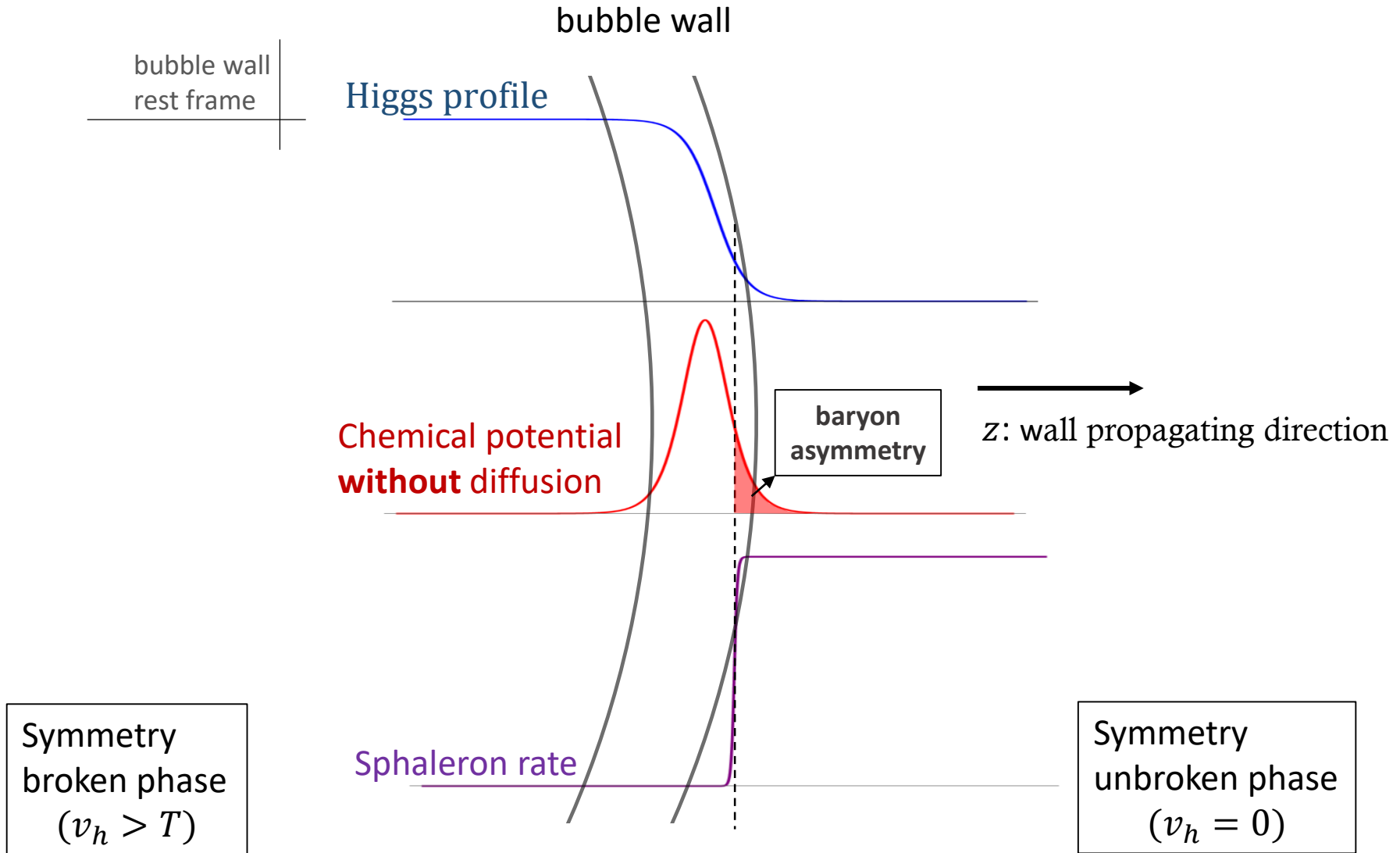


# Diffusion effect around bubble wall

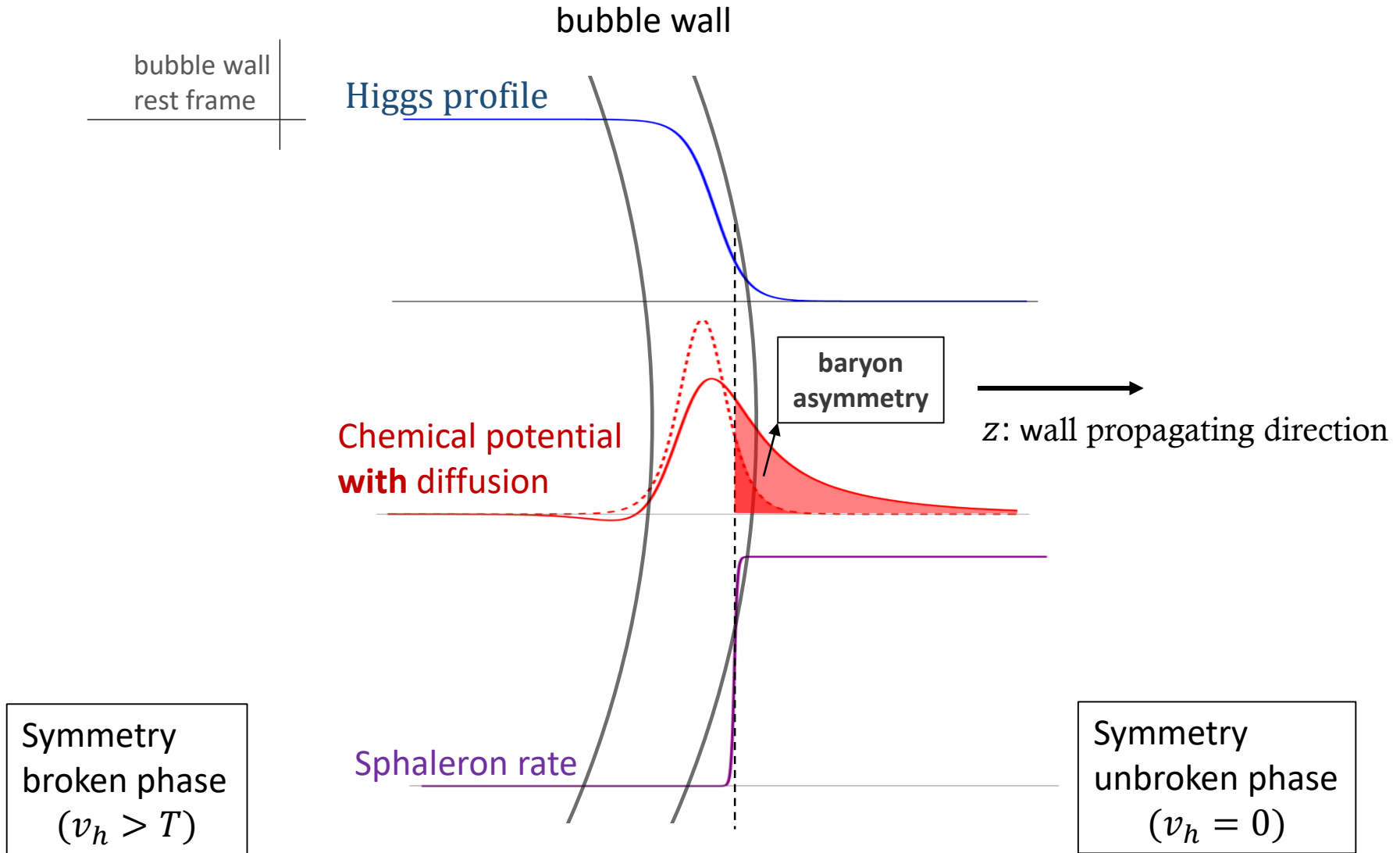




# Diffusion effect around bubble wall



# Diffusion effect around bubble wall



**Whether the diffusion effect can give a significant enhancement  
is determined by**

$L_w v_w$  vs Diffusion length scale ( $\simeq O(100)/T_n$ )

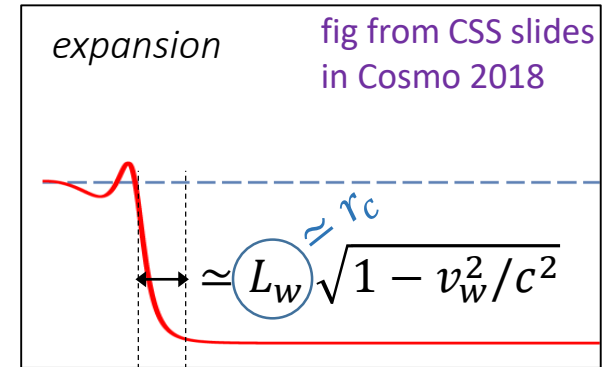
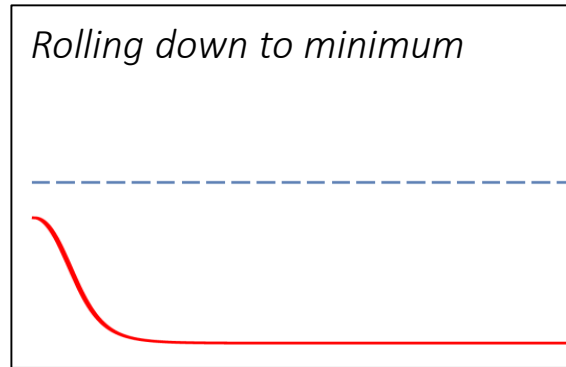
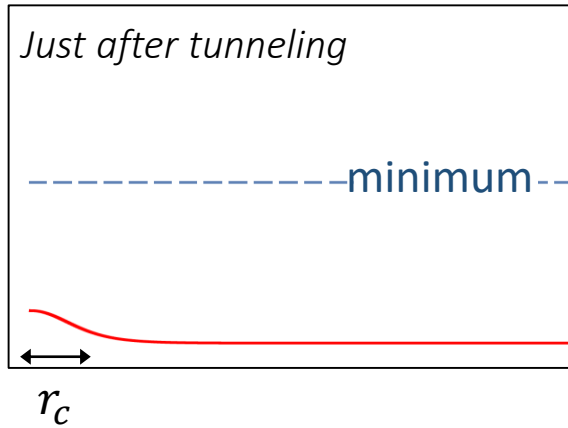
**Whether the diffusion effect can give a significant enhancement  
is determined by**

$$\begin{array}{c} L_w v_w \text{ vs Diffusion length scale } (\simeq O(100)/T_n) \\ \uparrow \quad \uparrow \\ \propto f \quad \mid \\ \sim \text{independent of } f \end{array}$$

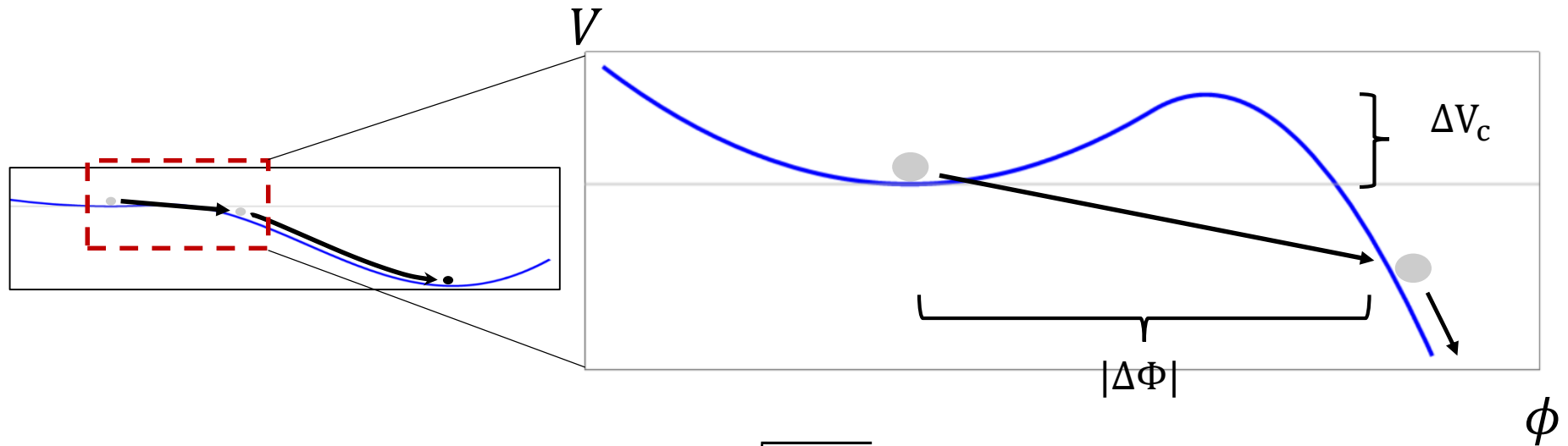
# Bubble wall width

Whether diffusion can be a significant effect is determined by two quantities:

$L_w$  : approximated by a critical bubble size  $r_c$



# Bubble wall width

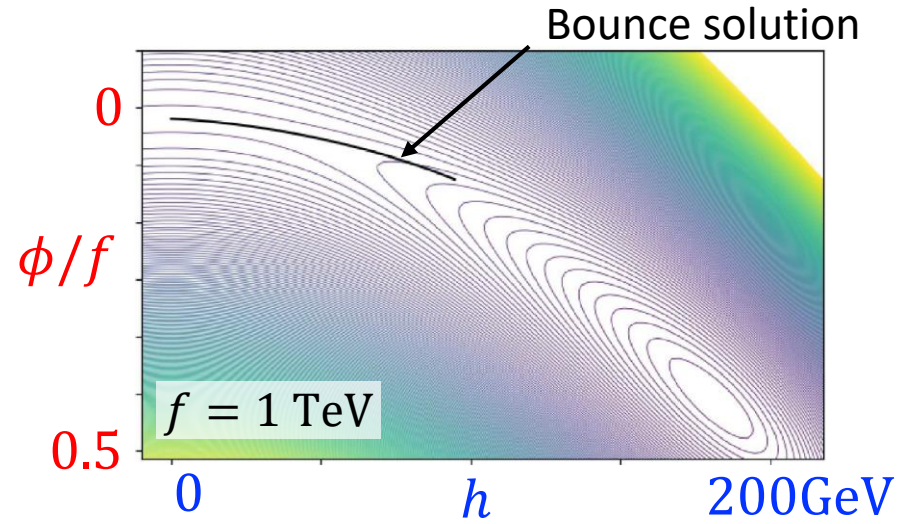


$$\Rightarrow L_w \sim r_c \sim \sqrt{\frac{|\Delta\Phi|^2}{8\Delta V}} \sim \frac{f}{m_w^2}$$

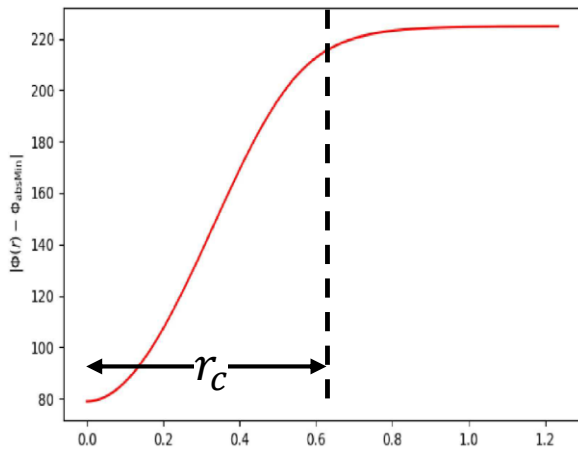
(rough estimation)

# Bubble wall width

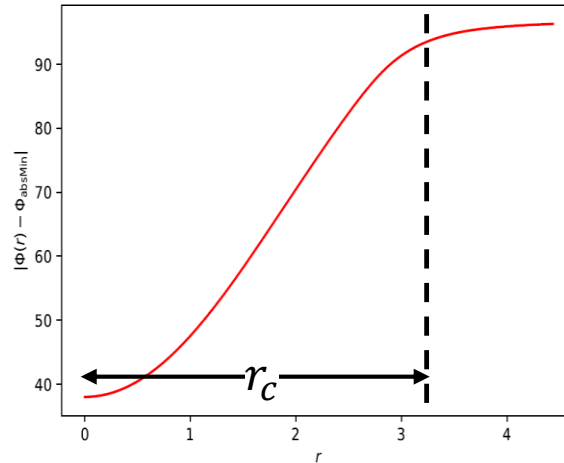
We also checked  $r_c$ , numerically.  
CosmoTransitions ([Wainwright, 1109.4189](#)):  
bounce solution, bubble profile, critical action



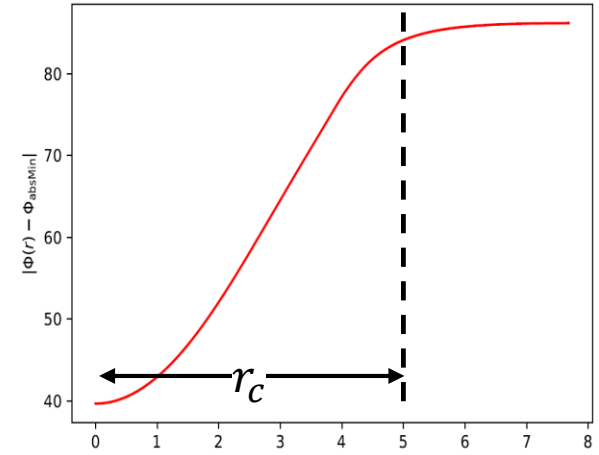
$f = 1 \text{ TeV}, L_w \simeq 10/T_n$



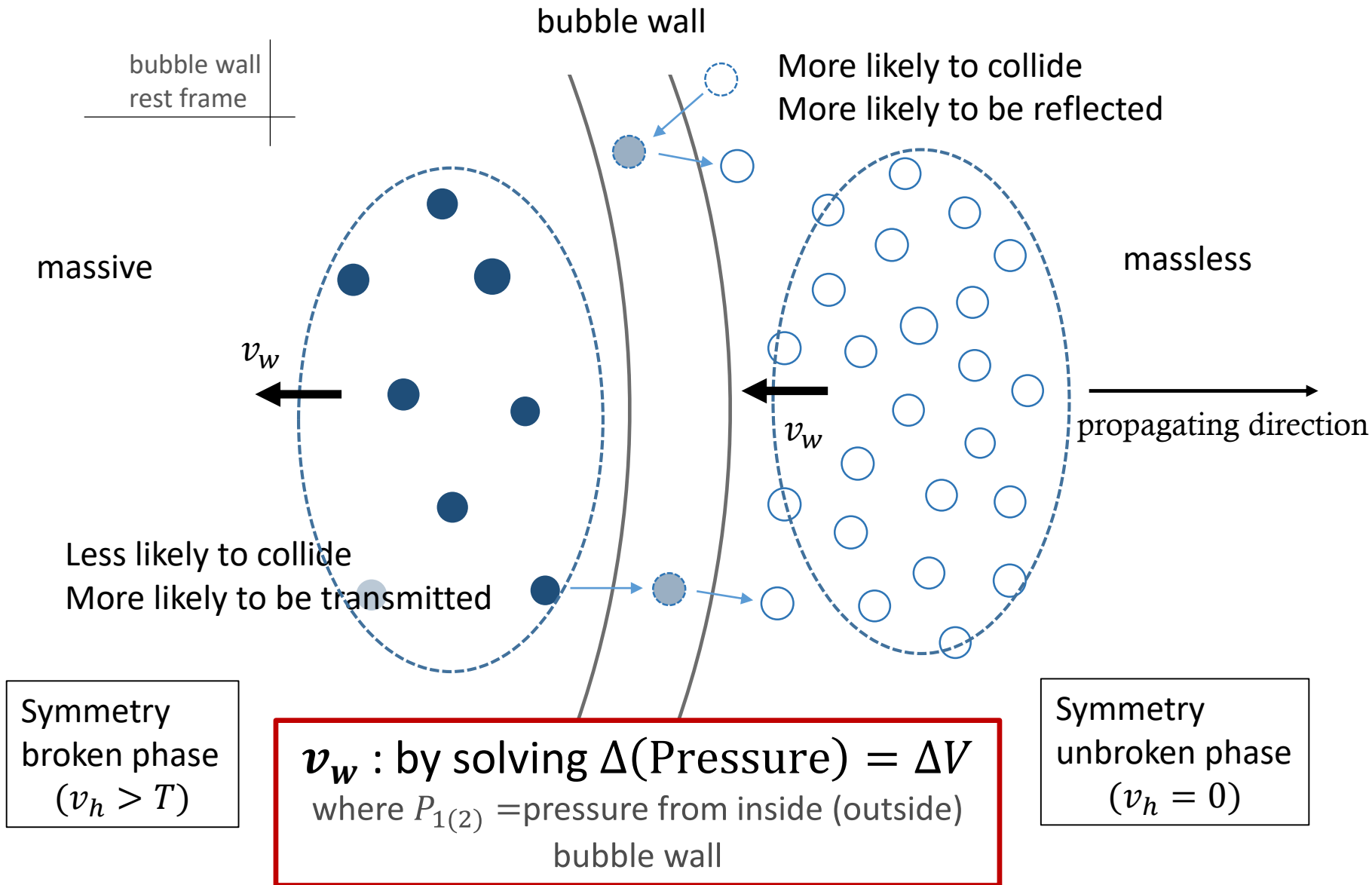
$f = 10 \text{ TeV}, L_w \simeq 50/T_n$



$f = 20 \text{ TeV}, L_w \simeq 80/T_n$



# Bubble wall velocity





# Bubble wall velocity

$$\Delta P = \text{Pressure from outside} - \text{Pressure from inside} = \Delta V$$

$$\Rightarrow v_w \simeq O(0.1), \text{ numerically}$$

**Here,  $f$  does not seem to play anything.**

# Whether diffusion gives a significant effect

$$v_w L_w T_n \sim \frac{f}{m_w} \text{ vs Diffusion length scale} \times T_n (\simeq O(100))$$

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$\Rightarrow$   $f \lesssim O(10 - 100 \text{ TeV})$ : diffusion is important  
 $f \gtrsim O(10 - 100 \text{ TeV})$ : diffusion is unimportant

# Whether diffusion gives a significant effect

$$v_w L_w T_n \sim \frac{f}{m_w} \text{ vs Diffusion length scale} \times T_n (\simeq O(100))$$

varying top Yukawa model  
where diffusion formalism is  
well-established

1806.02591

$\Rightarrow$   $f \lesssim O(10 - 100 \text{ TeV})$ : diffusion is important  
 $f \gtrsim O(10 - 100 \text{ TeV})$ : diffusion is unimportant

weak anomalous coupling  
( $\theta W \tilde{W}$  coupling)

1811.03294

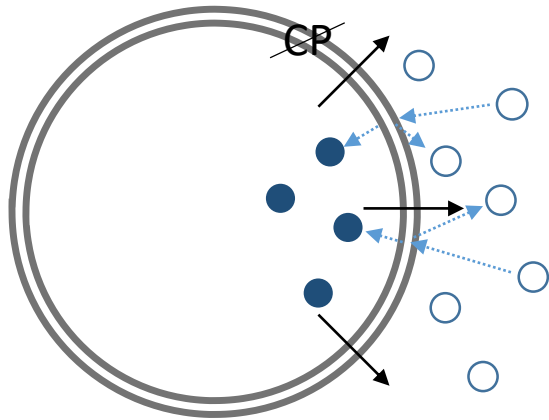
# Charge transport mechanism

$$L_{CPV} = (y_t + x_t e^{i\theta}) \bar{q}_{L3} t_R H$$

$f \lesssim O(10 - 100 \text{ TeV})$ : diffusion is important

Transport mechanism is well-studied in a complex top quark mass scenario:  $m_t(z) \bar{q}_{L3} t_R H$

$$m_t(z) = (y_t + x_t e^{i\theta(z)}) \equiv m(z) e^{i\theta(z)}$$



$$\Rightarrow F_z = -\frac{(m^2)'}{2E_0} \pm \frac{(m^2 \Theta')'}{2E_0 E_{0z}} \mp s \frac{\Theta' m^2 (m^2)'}{4E_0^3 E_{0z}}$$

$\Rightarrow$  Boltzmann equations in the wall rest frame  
(with  $f = f_0 + \delta f$ )

$$\begin{aligned} v_w K_1 \mu'_2 + v_w K_2 (m^2)' \mu_2 + u'_2 - \langle C[f] \rangle &= S_\mu \\ -K_4 \mu'_2 + v_2 \tilde{K}_5 u'_2 + v_w \tilde{K}_6 (m^2)' u_2 - \langle \frac{p_z}{E_0} C[f] \rangle &= S_\theta + S_u \end{aligned}$$

where

Formalisms are well-established in

Joyce et. al., 9408339

Fromme, Huber, 0604159

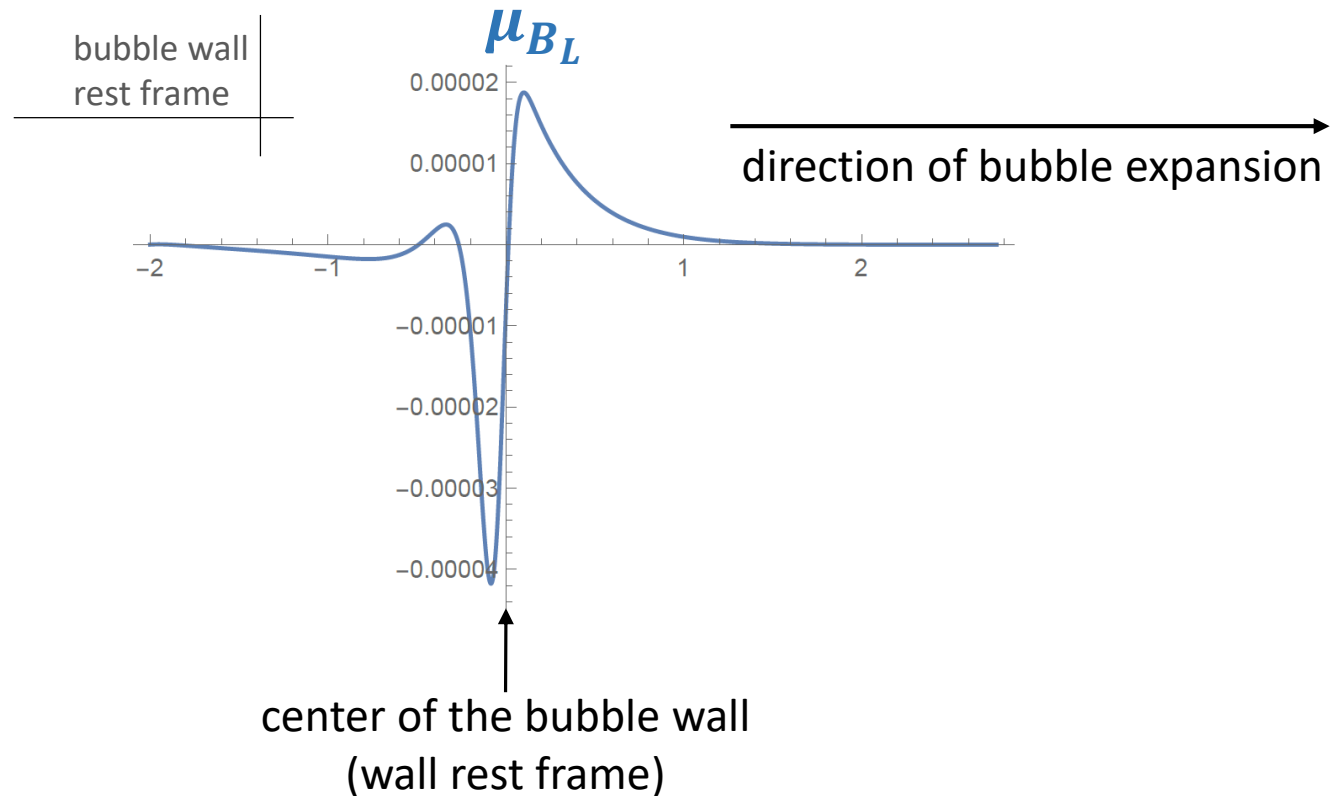
Konstandin et. al., 1706.08534

$$\begin{aligned} S_\mu &= K_7 \Theta' m^2 \mu'_1 \\ S_\theta &= -v_w K_8 (m^2 \Theta')' + v_w K_9 \Theta' m^2 (m^2)' \\ S_u &= -\tilde{K}_{10} m^2 \Theta' u'_1 \end{aligned}$$

# Charge transport mechanism

$$L_{CPV} = (y_t + x_t e^{i\theta}) \bar{q}_{L3} t_R H$$

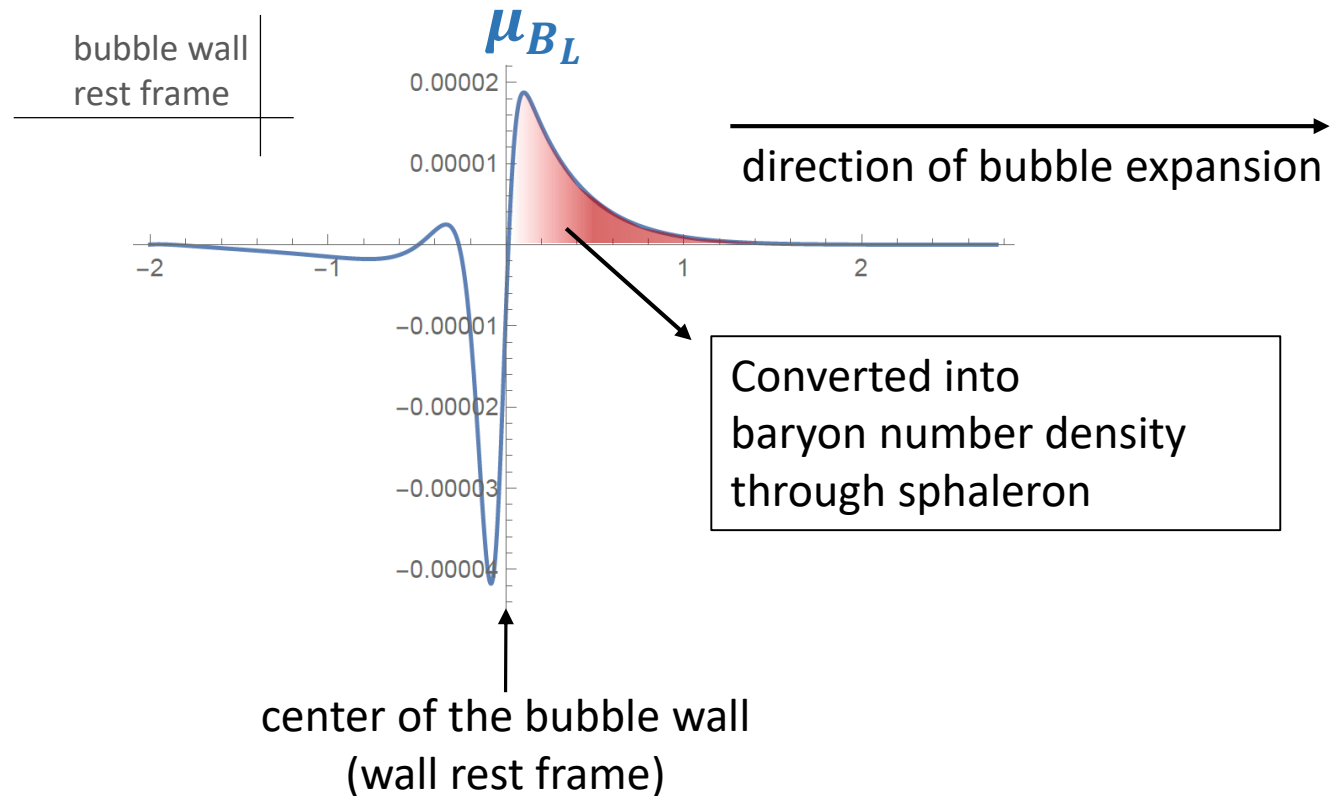
After solving Boltzmann equations,  
the chemical potential of left-handed baryon is obtained



# Charge transport mechanism

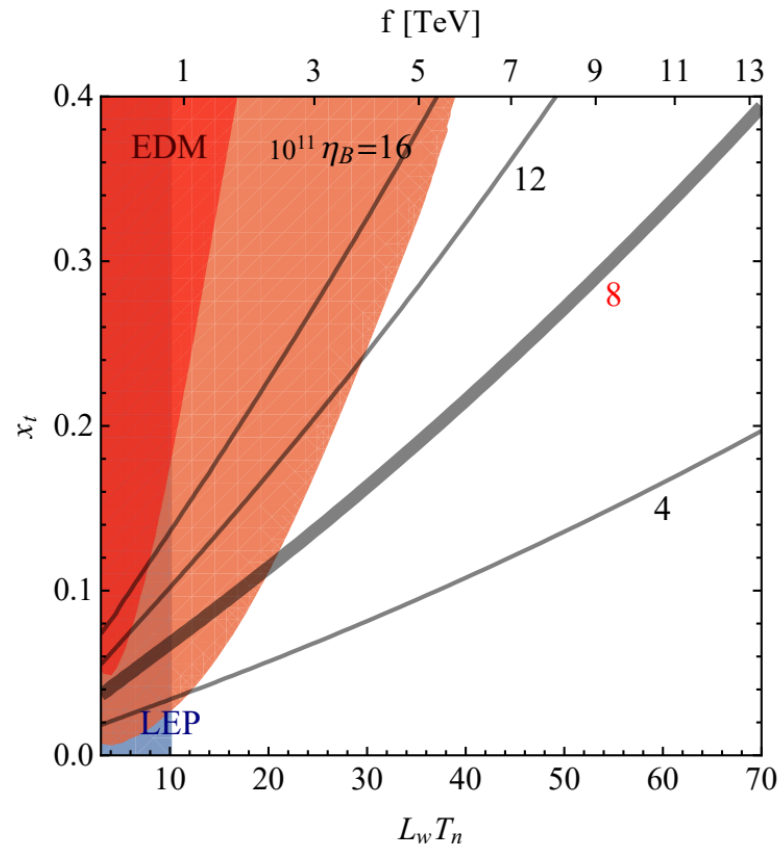
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# Charge transport mechanism

$$L_{CPV} = (y_t + x_t e^{i\theta}) \bar{q}_{L3} t_R H$$



## Benchmark parameters

$$\begin{aligned}\Lambda &= 130 \text{ GeV}, \\ \alpha &= 1.4, \\ M &= 103 \text{ GeV}\end{aligned}$$

$$\begin{aligned}T_c &\simeq 68 \text{ GeV} \\ T_n &\simeq T_2 \simeq 54 \text{ GeV} \\ v_w &\simeq 0.07\end{aligned}$$

- ✓ For an UV completion,  $x_t \lesssim 0.3$ .
- ✓ large  $f$   $\left\{ \begin{array}{l} \Rightarrow \text{large } L_w \Rightarrow \text{small } \eta_B \Rightarrow \text{requires larger } x_t \\ \Rightarrow \text{smaller couplings (this is what I want)} \end{array} \right.$



# Adiabatic electroweak baryogenesis

If  $f > \mathcal{O}(10 - 100 \text{ TeV})$ , diffusion effect is negligible.

(Particles in the plasma do not have enough time to transport from the wall to the outside.)

(They feel like that the Higgs vev changes in time, homogeneously.)

$$L_{CPV} = \frac{g_2^2}{32\pi^2} \theta W_{\mu\nu} \tilde{W}^{\mu\nu} = \theta \partial_\mu J_{CS}^\mu \rightarrow -\partial_\mu \theta J_{CS}^\mu \sim -\partial_t \theta N_{CS} \rightarrow \mu_{CS} = \partial_t \theta$$

$$\Gamma_{sph} \equiv 2 \lim_{\mu \rightarrow 0} \frac{\dot{N}_{CS} T}{\mu_{CS} V} \Rightarrow \dot{n}_{CS} = \frac{1}{2} \frac{\Gamma_{sph}}{T} \mu_{CS} \left( 1 - \frac{n_{CS}}{n_{CS}^{(eq)}} \right) \Rightarrow \dot{n}_B = \frac{3}{2} \frac{\Gamma_{sph}}{T} \dot{\theta} \left( 1 - \frac{n_B}{n_B^{(eq)}} \right)$$

$$n_B^{(eq)} = \frac{13}{2} \dot{\theta}$$

$$\Gamma_{sph} \simeq 18 \alpha_w^5 T^4 \Rightarrow n_B \simeq 27 \alpha_w^5 T_n^3 (\Delta\theta) e^{-K_\phi}$$

$K_\phi$  becomes order one when  $f > 10^{6-7} \text{ GeV}$

# Adiabatic electroweak baryogenesis

$$\dot{n}_B = \frac{3}{2} \frac{\Gamma_{sph}}{T} \dot{\theta} \left( 1 - \frac{n_B}{n_B^{(eq)}} \right) \Rightarrow n_B \simeq 27 \alpha_w^5 T_n^3 (\Delta\theta) e^{-K\phi}$$

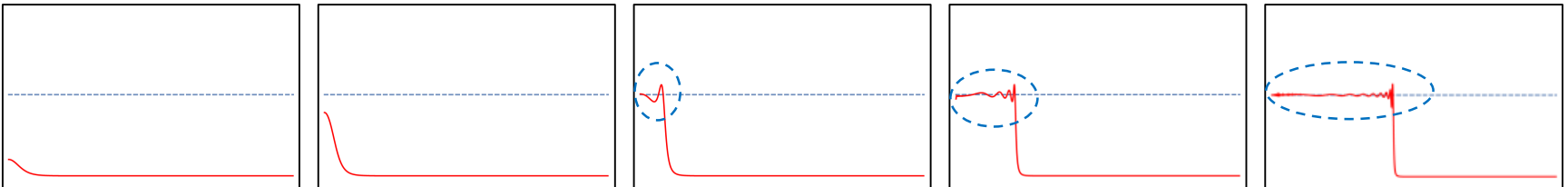
$$n_B^{(eq)} = \frac{13}{2} \dot{\theta}$$

Large suppression if  $f > 10^{6-7} \text{ GeV}$

Two contributions to  $K_\phi$

1. When  $f \uparrow$ ,  $\delta t_{PT} \simeq 1/m_\phi \uparrow$  (i.e. time scale increases)  
 $\Rightarrow \dot{\theta} \downarrow \Rightarrow n_B^{(eq)} \downarrow$

2. Oscillation after tunneling does not stop (small dissipation rate).



# Adiabatic electroweak baryogenesis

$$\dot{n}_B = \frac{3}{2} \frac{\Gamma_{sph}}{T} \dot{\theta} \left( 1 - \frac{n_B}{n_B^{(eq)}} \right) \Rightarrow n_B \simeq 27 \alpha_w^5 T_n^3 (\Delta\theta) e^{-K\phi}$$

$$n_B^{(eq)} = \frac{13}{2} \dot{\theta}$$

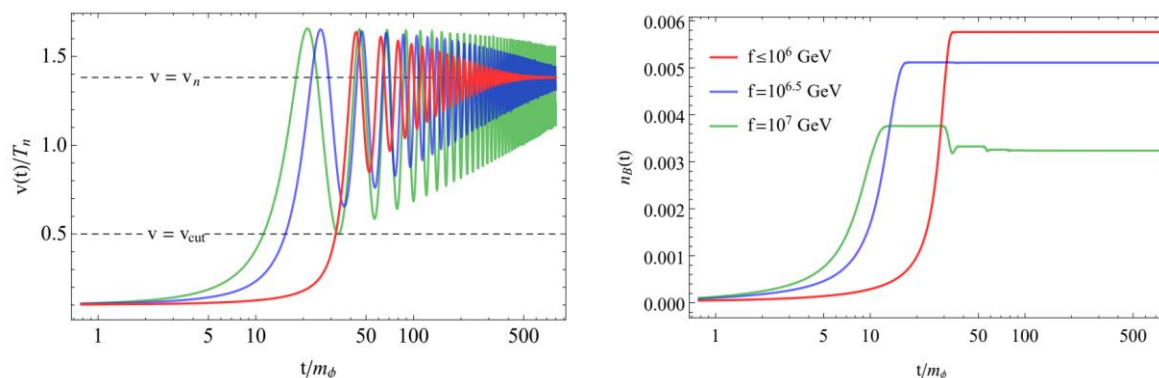
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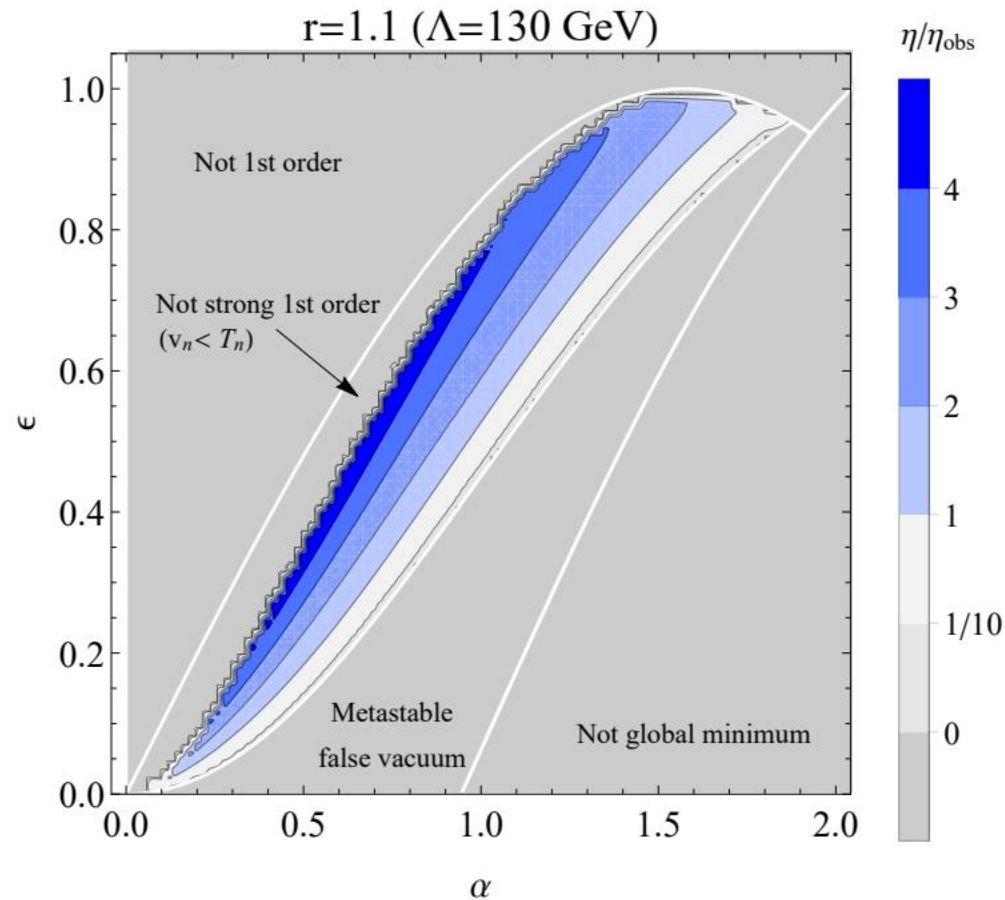
$$\Rightarrow \dot{\theta} \downarrow \Rightarrow n_B^{(eq)} \downarrow$$

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# Adiabatic electroweak baryogenesis

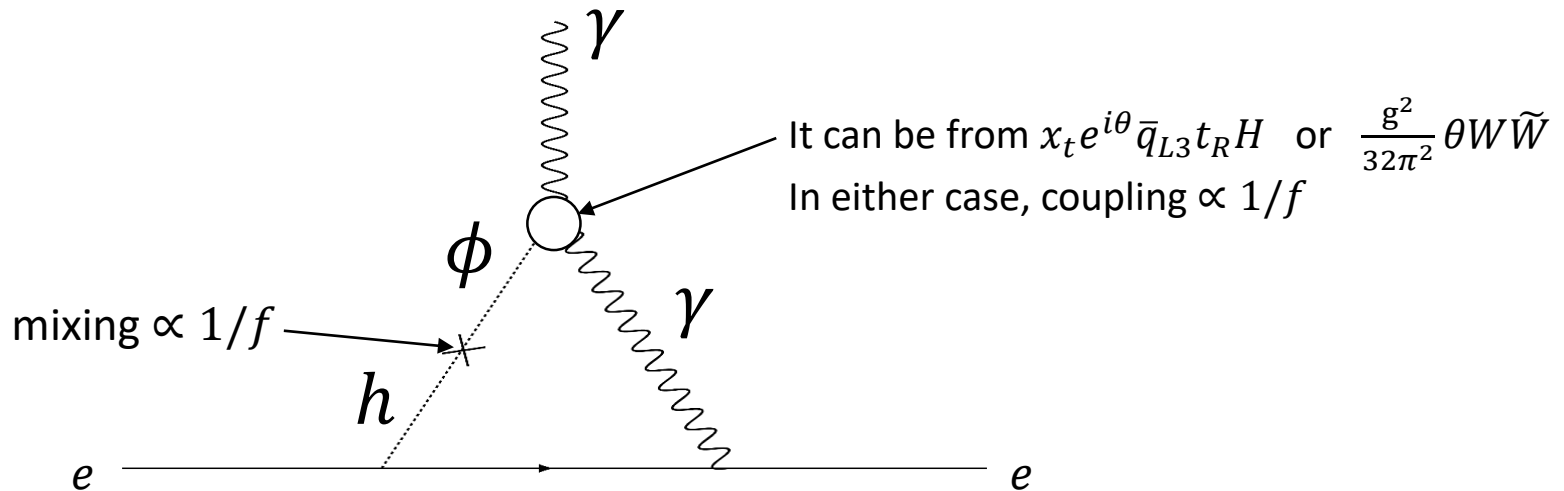
$f < 10^{6-7} \text{ GeV}$  can naturally explain the observed baryon asymmetry.



# Phenomenological constraints

# EDM constraints

- Generally, electron EDM constraint (ACME II) provides the most stringent obstacle.
- Our axion coupling is suppressed by  $1/f$ , so it is not so severe.
- there are other ways bypassing the constraint: e.g. dynamical CP violation (F. Huang, M. Zhang, Z. Qian)  
cancellation mechanism (E. Senaha)



$$\text{EDM} \propto 1/f^2$$

for the top transport case:  $f \gtrsim 3 \text{ TeV}$

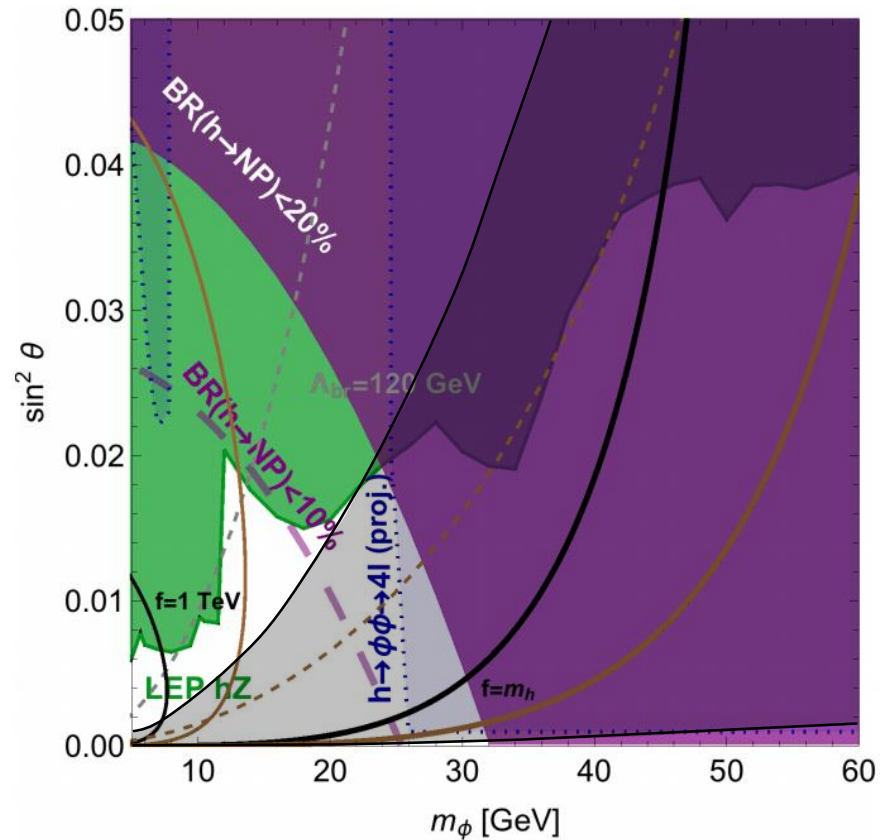
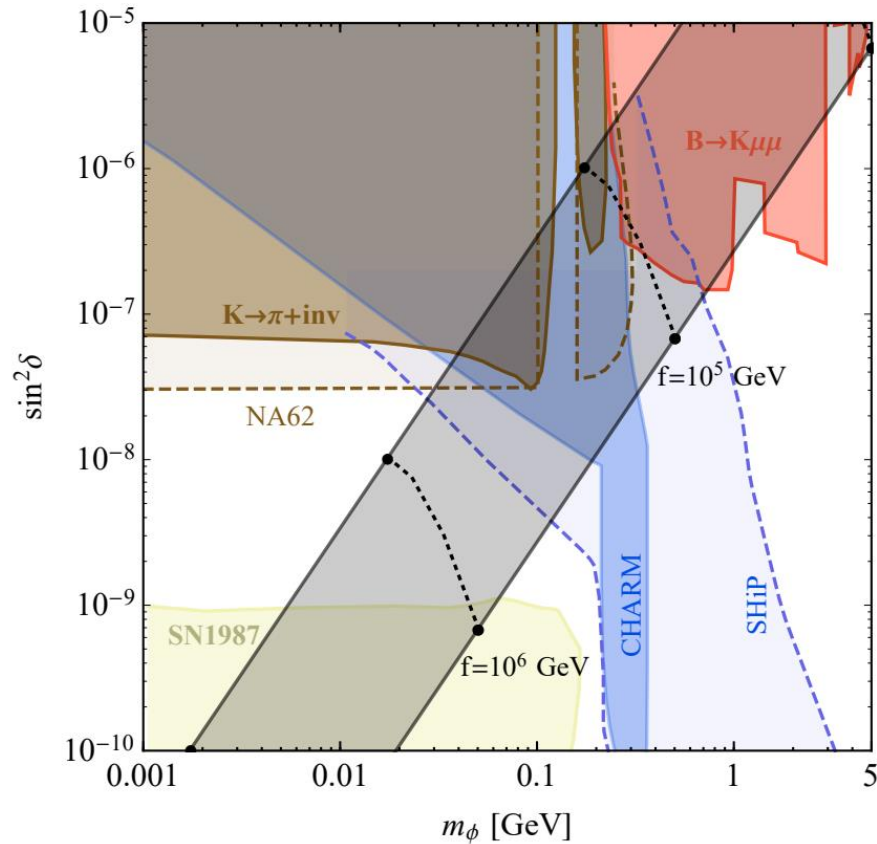
for the weak anomaly case:  $f \gtrsim 5 \text{ TeV}$

cf. condition for baryon asymmetry:  $f \lesssim 10^{6-7} \text{ GeV}$

How can we test the model?  
→ALP Searches

# ALP-Higgs mixing

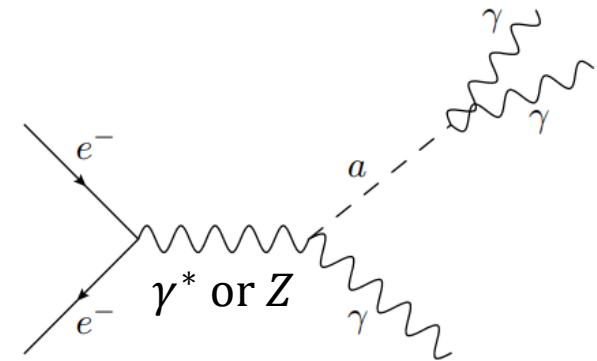
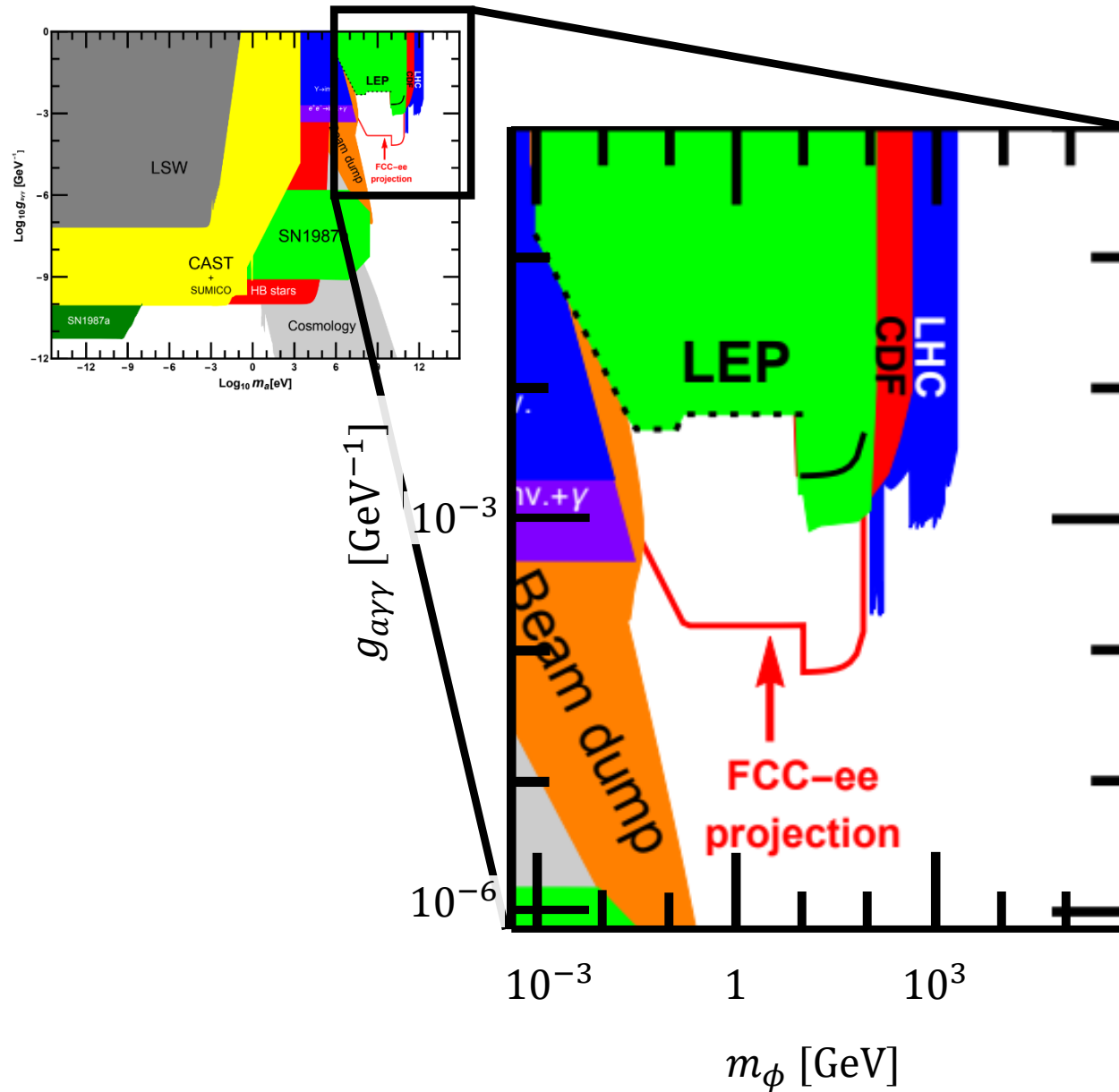
Flacke et. al., 1610.02025  
Choi, Im, 1610.00680



$\rightarrow 5 \text{ MeV} \lesssim m_\phi \lesssim 100 \text{ MeV or } 5 \text{ GeV} \lesssim m_\phi \lesssim 25 \text{ GeV}$

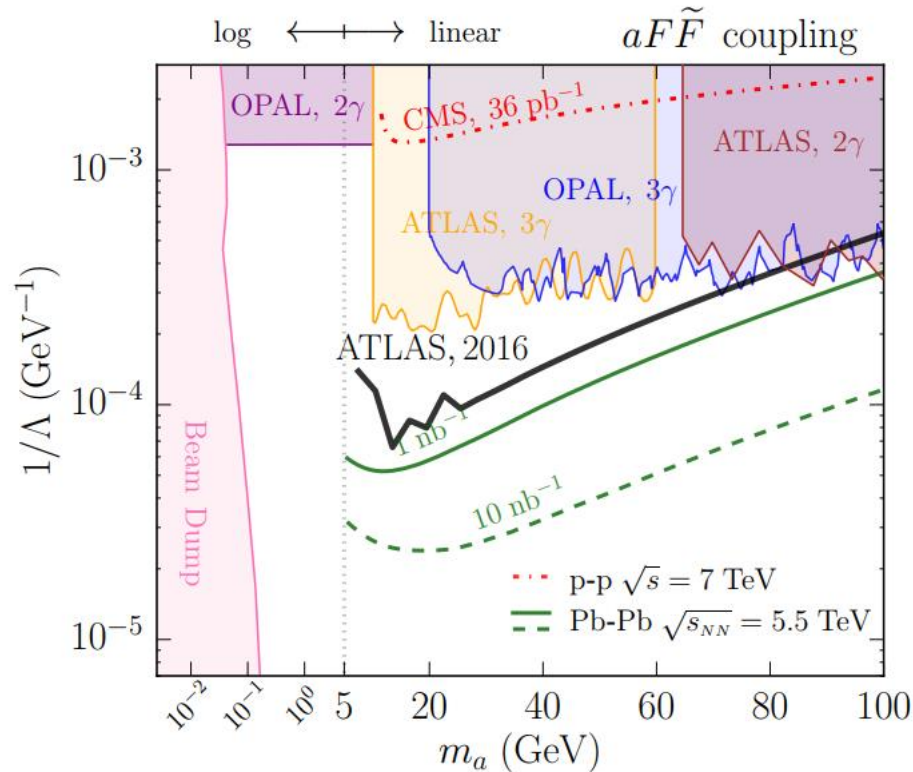


# ALP Searches at future lepton colliders

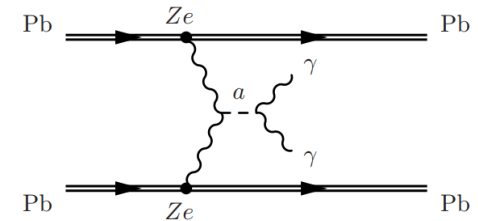


Jaeckel, Spannowsky,  
1509.00476

# ALP Searches at heavy ion collision



Diphoton resonance search  
at heavy ion collision



Knapen, Lin, Lou, Melia,  
1607.06083

# Summary

We considered an ALP extended Higgs sector where EWBG is realized.

- Strong first order phase transition is possible
  - ✓ ALP dependent Higgs mass drives a first order phase transition, independently of  $f$ .
  - ✓ large  $f \rightarrow$  weakly coupled limit.
- How large can  $f$  be?
  - ✓ **It depends on CPV operator.**
  - ✓ **If diffusion is required (top transport):**  $L_w \propto f \Rightarrow n_B \propto 1/f^\# \Rightarrow f < 10 \text{ TeV}$ .
  - ✓ **Weak anomalous coupling :** wash-out term  $\rightarrow f < 10^{6-7} \text{ GeV}$
- Phenomenology
  - ✓  $\text{EDM} \propto 1/f^2 \Rightarrow \begin{cases} \text{top transport: } f > 3 \text{ TeV} \\ \text{weak anomalous coupling: } f > 5 \text{ TeV} \end{cases}$
  - ✓ ALP searches from ALP-Higgs mixing  $\Rightarrow \begin{cases} 5 \text{ GeV} \lesssim m_\phi \lesssim 25 \text{ GeV} \Leftarrow \text{lepton collider?} \\ \hspace{10em} \text{heavy ion collision?} \\ 5 \text{ MeV} \lesssim m_\phi \lesssim 100 \text{ MeV} \Leftarrow ?? \text{ not clear} \\ \hspace{15em} \text{at current stage} \end{cases}$

**Thank you for your attention!**

**Back up slides**

# Diffusion effect around bubble wall

It is well-known that a diffusion effect (so-called charge transport mechanism) around bubble wall helps the electroweak baryogenesis. (Joyce et. al. 9401351, Cohen et. al. 9406345)

In a wall rest frame, CP violation occurs proportionally to  $\partial_z h$  (with  $z$  =coordinate along the bubble wall), and it drives a nonzero baryon number chemical potential.

If there is no diffusion effect, chemical potential is nonzero **only at the wall** ( $\partial_z h \neq 0$ ), while sphaleron rate is exponentially suppressed  $\left(\exp\left(-\frac{h}{T}\right)\right)$ .

If there is a diffusion effect, chemical potential is **spread away** and becomes **nonzero outside bubble wall** where sphaleron rate is not suppressed.

# UV Completion

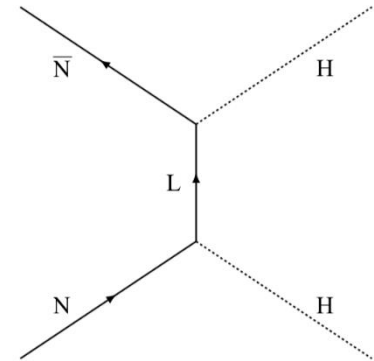
Similar to relaxion models  
(Graham, Kaplan, Rajendran, 1504.07551)

Vector-like lepton pair  $L, L^c$  and singlet pair  $N, N^c$   
charged under hidden non-Abelian gauge group,

$$-L = y H L N^c + y' H^\dagger L^c N + m_N N N^c + m_L L L^c + \text{h.c.}$$

$$m_N \ll \Lambda_{con} \ll m_L,$$

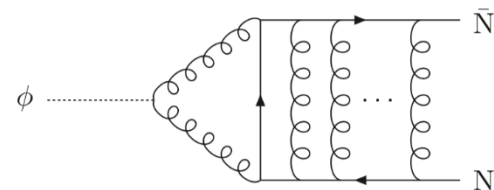
$$-L_{eff} \rightarrow \left( m_N + \frac{y y'}{m_L} |H|^2 \right) N N^c$$



Confinement  $\rightarrow$  axion- $\eta'$  mixing  $\rightarrow \langle N N^c \rangle \sim \Lambda_{con}^3 e^{i\phi/f}$ ,

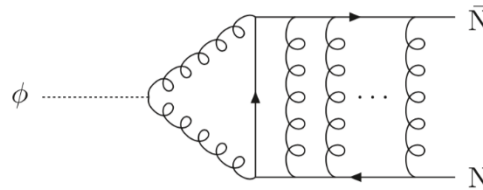
$$-L_{eff} \rightarrow m_N \Lambda_{con}^3 \cos \frac{\phi}{f} + \frac{y y'}{m_L} \Lambda_{con}^3 |H|^2 \cos \left( \frac{\phi}{f} + \alpha \right)$$

$$\alpha = \text{Arg} \left( \frac{y y' m_N}{m_L} \right)$$



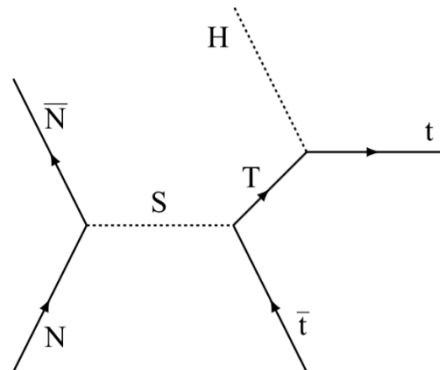
# UV Completion for $(y_t + x_t e^{i\theta}) \bar{q}_{L3} t_R H$

Hidden sector confinement  $\rightarrow$  axion- $\eta'$  mixing  $\rightarrow \langle N N^c \rangle \sim \Lambda_{con}^3 e^{i\theta}$ .



We need a contact interaction between  $N N^c \bar{q}_{L3} t_R H$ .

One example :



$$x_t \simeq \frac{\Lambda_{con}^3}{m_S^2 m_T}$$