Axion theory: Think again

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- 1.Introduction
- 2. "Invisible" axion
- 3.QCD phase transition
- 4. Hierarchy together with "invisible axion"

1. Introduction

With the gauge symmetry as the only symmetry at low energy, chiral fields are the only light fields.

My original contributions were to be found in the future. Some of my examples are

arXiv:1703.10925: PRD96 (2017) 055033

$$Q = \frac{1}{2} : \ell_i = \begin{pmatrix} E_i \\ N_i \end{pmatrix}_{\frac{+1}{2}}, \qquad \begin{matrix} E_{i,-1}^c \\ N_{i,0}^c \end{matrix} \quad (i = 1, 2, 3),$$

$$Q = -\frac{3}{2} : \mathcal{L} = \begin{pmatrix} \mathcal{E} \\ \mathcal{F} \end{pmatrix}_{\frac{-3}{2}}, \qquad \begin{matrix} \mathcal{E}_{i,+1}^c \\ \mathcal{F}_{i,+2}^c \end{matrix},$$

So, there is a good reason that these particles will be discovered at low energy. First, by kinetic mixing!!

(STOSIN)

Weak-Interaction Singlet and Strong CP Invariance

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Strong CP invariance is automatically preserved by a spontaneously broken chiral $U(1)_4$ symmetry. A weak-interaction singlet heavy quark Q a new scalar meson σ^0 , and a very light axion are predicted. Phenomenological implications are also included.

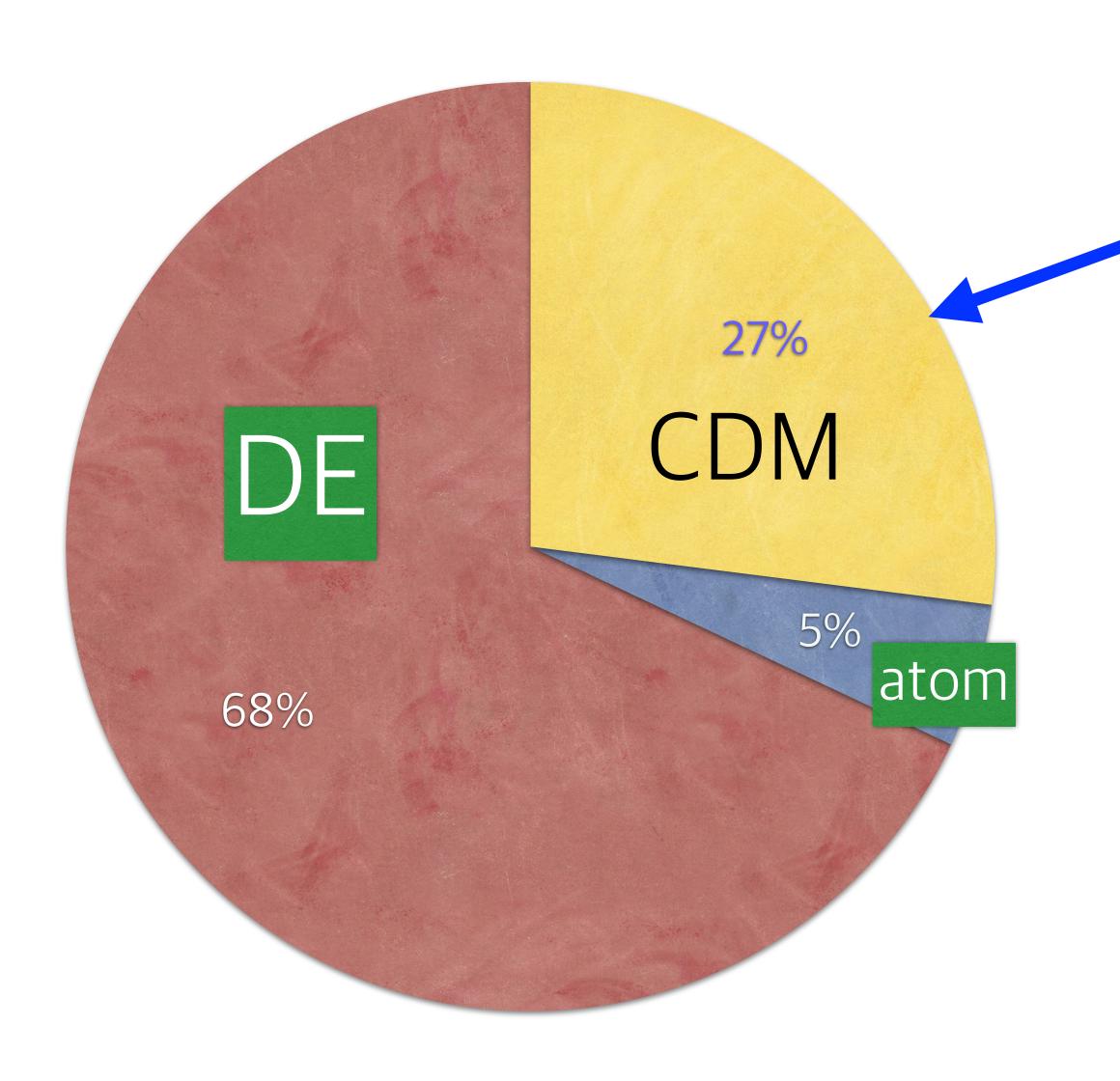
attempts¹⁻⁴ to incorporate the observed made the Lagrangian CP invariant. In gen

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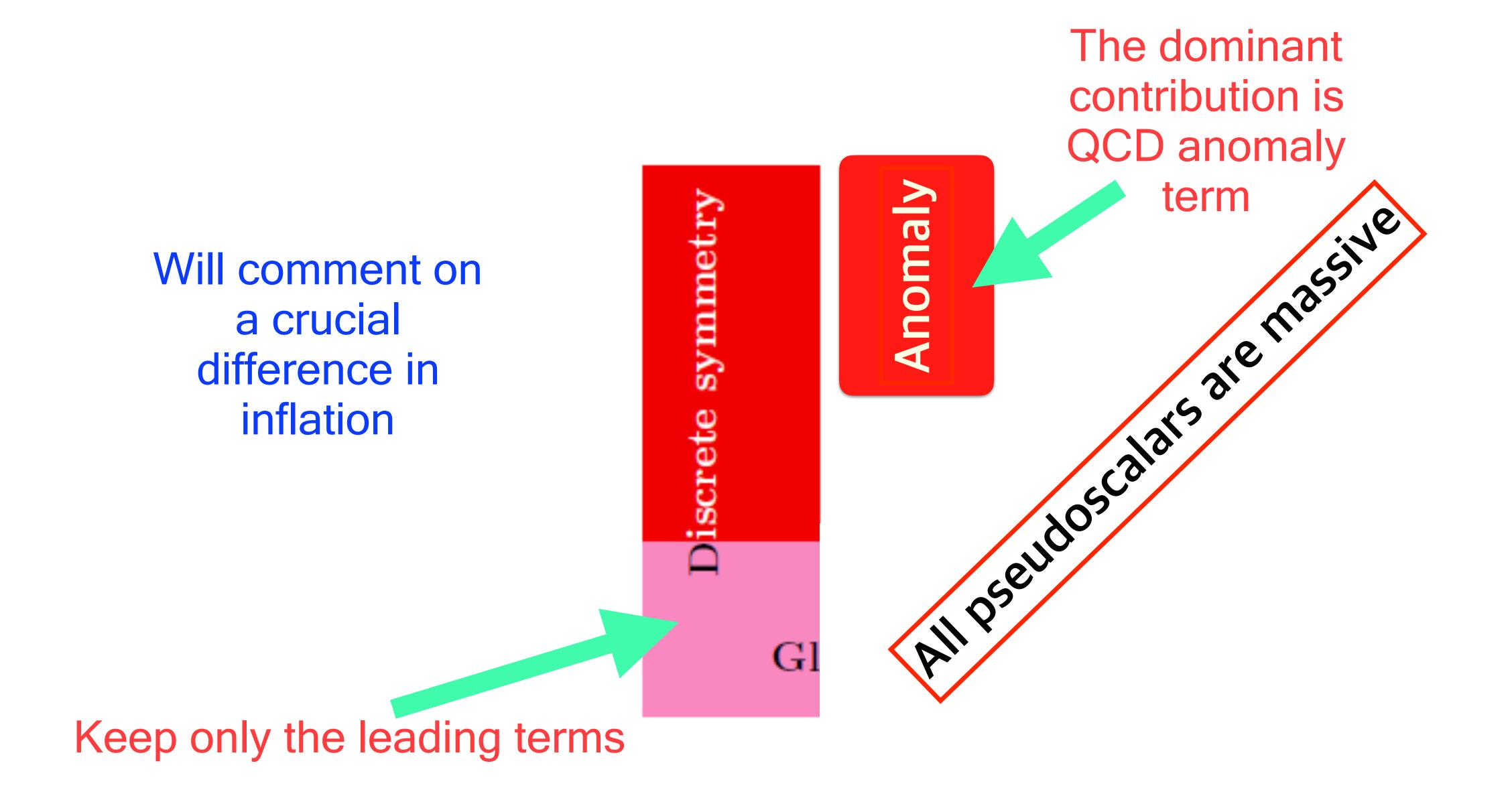
he axion properties, menological implia new scalar σ^0 , and

principle, the colcan be arbitrary. e the same as light is $\frac{2}{3}$ or $-\frac{1}{3}$, the served in high-en-PEP and PETRA, arge is 0, there clor-singlet hadrons thence, the ob-

The new scalar σ^0 .—By the spontaneous symmetry breaking of $U(1)_A$, σ will be split into a scalar boson σ^0 of mass $(2\mu_0)^{1/2}$ and an axion a. This σ^0 is *not* a Higgs meson, because it does not break the gauge symmetry, but the phenomenology of it is similar to the Higgs because of its coupling to quark as m_{Q}/v' . If this scalar mass is $\geq 2m_Q$, we will see spectacular final state of stable particles such as $(Q\overline{u})$ and (Qu). If its mass is $\leq 2m_{\odot}$, the effective interaction through loops $(c/v')F_{\mu\nu}{}^aF^{a\mu\nu}\sigma^0$, with numerical constant c, will describe the decay σ^0 - ordinary hadrons. The order of magnitude of its lifetime is $\tau(\sigma^0)$ $\approx \tau (\pi^{0})(v'/f_{\pi})^{2}(m_{\pi^{0}}/m_{\sigma^{0}})^{3} \approx 2 \times 10^{-10} \text{ sec for } v' \approx 10^{5}$ GeV and $m_{\sigma^0} \approx 10$ GeV. This kind of particle can be identified as a jet in pp high-energy collisions,



"Invisible" axion can be a part of DM



U(1)_{anom} as the symmetry for the "invisible" axion (family symmetry?)

JEK, Kyae, Nam, 1703.05345 [Eur. Phys. J. C77 (2017) 847], JEK, Nam, Semertzidis, 1712.08648 [IJMPA33 (1978) 1830002].

't Hooft mechanism:

If a gauge symmetry and a global symmetry are broken by one complex scalar by the BEHGHK mechanism, then the gauge symmetry is broken and a global symmetry remains unbroken.

Q _{gauge}	Qglobal	Unbroken X=Q _{global} -Q _{gauge}
1	1	- global – gauge

$$\phi \to e^{i\alpha(x)Q_{\text{gauge}}}e^{i\beta Q_{\text{global}}}\phi$$

the α direction becomes the longitudinal mode of heavy gauge boson. The above transformation can be rewritten as

$$\phi \to e^{i(\alpha(x)+\beta)Q_{\text{gauge}}}e^{i\beta(Q_{\text{global}}-Q_{\text{gauge}})}\phi$$

Redefining the local direction as $\alpha'(x) = \alpha(x) + \beta$, we obtain the transformation

$$\phi \to e^{i\alpha'(x)Q_{\text{gauge}}}e^{i\beta(Q_{\text{global}}-Q_{\text{gauge}})}\phi.$$

$$|D_{\mu}\phi|^{2} = |(\partial_{\mu} - igQ_{a}A_{\mu})\phi|_{\rho=0}^{2} = \frac{1}{2}(\partial_{\mu}a_{\phi})^{2} - gQ_{a}A_{\mu}\partial^{\mu}a_{\phi} + \frac{g^{2}}{2}Q_{a}^{2}v^{2}A_{\mu}^{2}$$
$$= \frac{g^{2}}{2}Q_{a}^{2}v^{2}(A_{\mu} - \frac{1}{gQ_{a}v}\partial^{\mu}a_{\phi})^{2}$$

So, the gauge boson becomes heavy and there remains the x-independent transformation parameter beta. The corresponding charge is a combination:

The MI axion

$$H_{\mu\nu\rho} = M_{MI} \epsilon_{\mu\nu\rho\sigma} \, \partial^{\sigma} a_{MI}.$$

$$\frac{1}{2}\partial^{\mu}a_{MI}\partial_{\mu}a_{MI} + M_{MI}A_{\mu}\partial^{\mu}a_{MI}$$

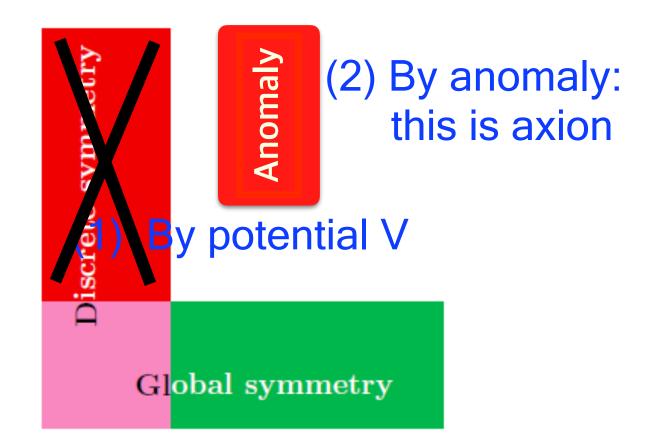
This is the Higgs mechanism, i.e. $a_{\rm MI}$ becomes the longitudinal mode of the gauge boson. [JEK, Kyae, Nam, 1703.05345]

$$\frac{1}{2}(\partial_{\mu}a_{MI})^{2} + M_{MI}A_{\mu}\partial^{\mu}a_{MI} + \frac{1}{2\cdot 3!}A_{\mu}A^{\mu} \to \frac{1}{2}M_{MI}^{2}(A_{\mu} + \frac{1}{M_{MI}}\partial_{\mu}a_{MI})^{2}.$$

It is the 't Hooft mechanism working in the string theory. So, the continuous direction $a_{MI} \rightarrow a_{MI} + (constant)$ survives as a global symmetry at low energy:

"Invisible" axion!! appearing at 10¹⁰⁻¹¹ GeV scale when the global symmetry is broken.

2. Axions



Peccei+Quinn (1977): Chiral symmetry broken ONLY by anomaly

Naming:

Weinberg at Ben Lee Memorial (1977): Higglet Wilczek at Ben Lee Memorial (1977): Axion

JEK(1979): "Very light" axion

Sikivie(1983): Haloscope cavity detector

PQ symmetry

Where is the identification of shifting-theta symmetry?

What have WW done? potential.

Non-Abelian gauge theory

Nonlinear terms in the field strength in non-Abelian gauge groups enable localized field configuration with the identification of S3 in the group space to S3 in the Euclidian space. Instanton solution

$$A_{\mu} = i f(r) g^{-1}(x) \partial_{\mu} g(x)$$

$$g(x) = \frac{x_{4} - i x_{a} \sigma_{a}}{r} = -\frac{i}{r} x_{\mu} \sigma_{\mu}$$

$$g(x)^{-1} = \frac{i}{r} x_{\mu} \bar{\sigma}_{\mu}$$

$$r^{2} = \sum_{i=1}^{4} x_{i}^{2}$$

$$\sigma_{\mu} = (\boldsymbol{\sigma}, i), \quad \bar{\sigma}_{\mu} = (\boldsymbol{\sigma}, -i)$$

Pontryagin index which is a topological number

$$q = \frac{1}{16\pi^2} \int d^4x \, \text{Tr} \, F_{\mu\nu} \tilde{F}_{\mu\nu} = \frac{1}{32\pi^2} \int d^4x \, F^a_{\mu\nu} \tilde{F}^a_{\mu\nu} \, .$$

Since the gauge field configuration has many q values, we construct a gauge invariant instanton configuration: theta vacuum.

[Callan-Dashen-Gross, Jackiw-Rebbi (1976)]

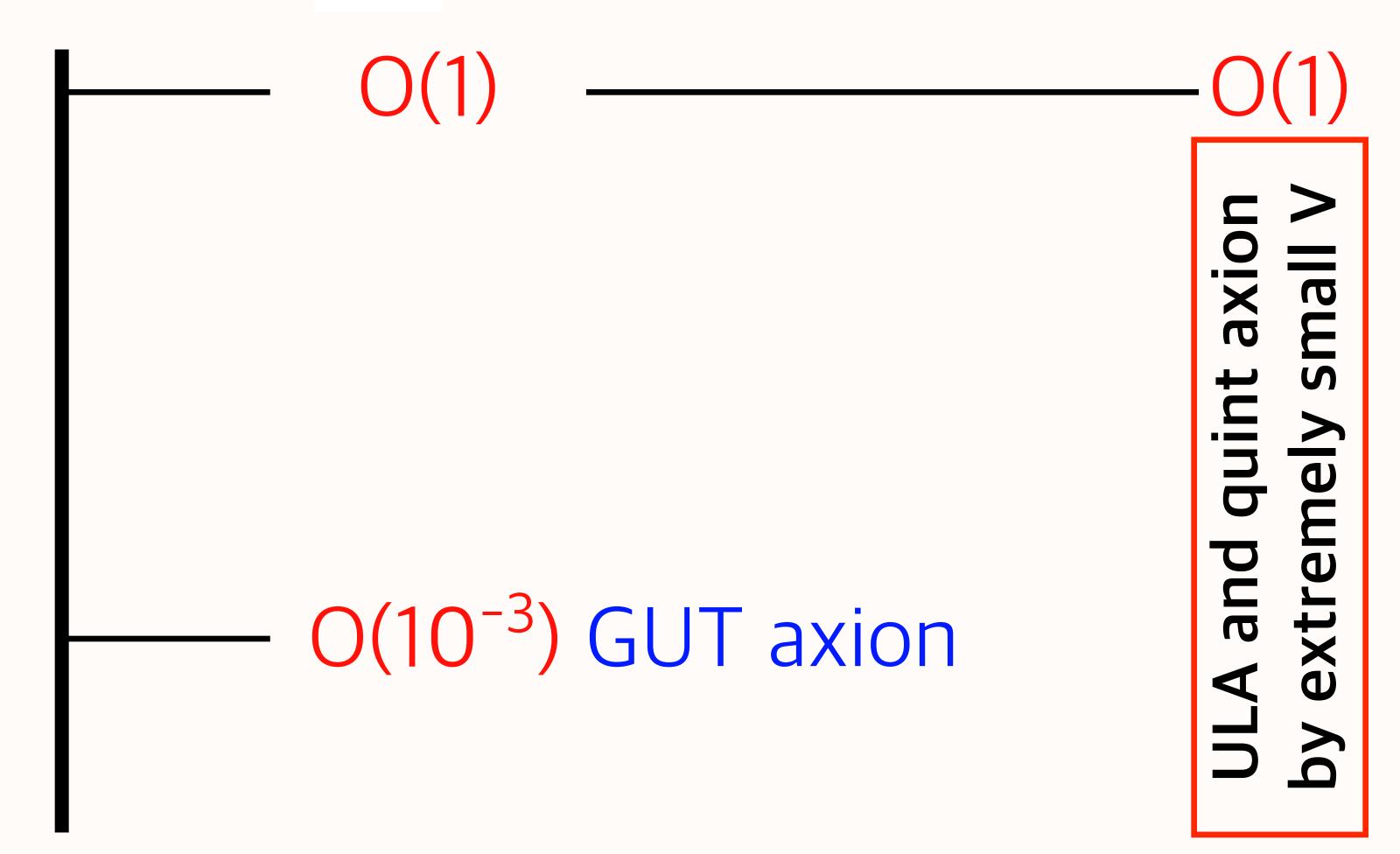
$$|\theta\rangle = \sum_{n=-\infty} e^{in\theta} |n\rangle$$
.

$$\begin{split} \left\langle \theta' \middle| \mathbf{e}^{-Ht} \middle| \theta \right\rangle &= \sum_{n'} \sum_{n} \mathbf{e}^{-\mathrm{i}(n'\theta' - n\theta)} \left\langle n' \middle| \mathbf{e}^{-Ht} \middle| n \right\rangle \\ &= \sum_{n' = -\infty}^{\infty} \mathbf{e}^{-\mathrm{i}n'(\theta' - \theta)} \sum_{q = -\infty}^{\infty} \int \left[\mathrm{d}A_{\mu} \right]_{q} \exp \left\{ -\mathrm{i}q\theta - \int \mathrm{d}^{4}x \, \mathcal{L} \right\} \end{split}$$

This is the CP violating theta term. It is due to gluons of QCD and QCD has the built-in CP violation.

But, there is no hint that CP is violated in strong interactions. Flavor singlet operator gives neutron electric dipole moment of order 10⁻¹⁵ ecm, and experimental bound is 2.1x10⁻²⁶ ecm [C A Baker et al, PRL97 (2006) 131801]. Theta must be less than 10⁻¹⁰. This is a fine-tuning problem.





Solutions of strong CP problem

We start from the observation that CP is anyway violated at the weak interaction level. Start with theta=0 but introduce CP violation to see if it generate the next order of theta less than 10⁻¹⁰. This is calculable models, and CP symmetry at the Lagrangian can be the underlying symmetry. The weak CP violation must be of "spontaneous" a la T D Lee. If we treat couplings given below some scale, say 10¹⁰ GeV, as the given Yukawa couplings, the KM form is the allowed one. However, the Nelson-Barr types cannot escape the high order problem because one can calculate theta at higher orders.

Can we make theta unphysical?

In QM, the phase of wave function A is unobservable since observables are the probability A*A. What can be the required symmetry for the theta term? As the phase symmetry in QM, if there is a shift symmetry of theta, the value of theta is unobservable. Then, look at what can change theta. The chiral transformation of colored fermions, i.e. the phase of a quark(s). For the corresponding current,

$$\partial^{\mu} J_{\mu}^{5} = \frac{2}{32\pi^{2}} G_{\mu\nu}^{a} \tilde{G}^{a\mu\nu} + m_{q} \,\bar{q} \,i\gamma_{5} \,q$$

The theta term is changed by a chiral transformation of some quark field,

$$\theta \rightarrow \theta - 2\alpha$$

For it to be an exact symmetry, the quark must be massless,

$$m_q = 0$$

It is basically the Peccei-Quinn symmetry. But the traditional PQ symmetry involves more.

The PQ mechanism consists of two parts:

- (1) The shift symmetry-QCD-QCD anomaly should be present.
- (2) The shift direction must be properly embedded as a fundamental pseudo scalar field or by a composite pseudoscalar field.

In the PQWW axion, the theta direction is one out of two pseudoscalars because the scheme must break a gauge symmetry also to give Z boson mass. The axion direction is orthogonal to that.

The simplest case is not involving breaking a gauge symmetry. Only break the PQ global symmetry. —-> To introduce the color anomaly only, a heavy quark Q is introduced: the so-called KSVZ model (It is one example, housing axion a in a complex BSM field singlet S [JEK(1979)].)

$$Q_L$$
, Q_R , S
SU(3)xSU(2)xU(1) (3,1,Ne). (3,1,Ne). (1,1,0)
PQ charge 1 -1 2

The KSVZ line in most cross-section vs. m_a line is for neutral one N=0. Spontaneous breaking of PQ creates a.

Lagrangians with a PQ symmetry

KSVZ
$$\mathcal{L}_Q = -f \, \overline{Q}_L Q_R \, \sigma + \text{h.c.}$$

Renormalizable couplings

$$V = \frac{\lambda}{4} (\sigma^* \sigma)^2 - \frac{\mu^2}{2} \sigma^* \sigma + \lambda_1 \sigma^2 H_u H_d + \cdots$$

To have $<H>/f_a = 10^{-8}$, one needs a fine-tuning of order 10^{-16} .



$$PQ: -1-1 \quad 1 \quad 1$$

$$\frac{H_u H_d}{M} \quad \sigma \quad \sigma$$

The PQ symmetry is used to allow the electroweak scale mu [K-Nilles (1984)].

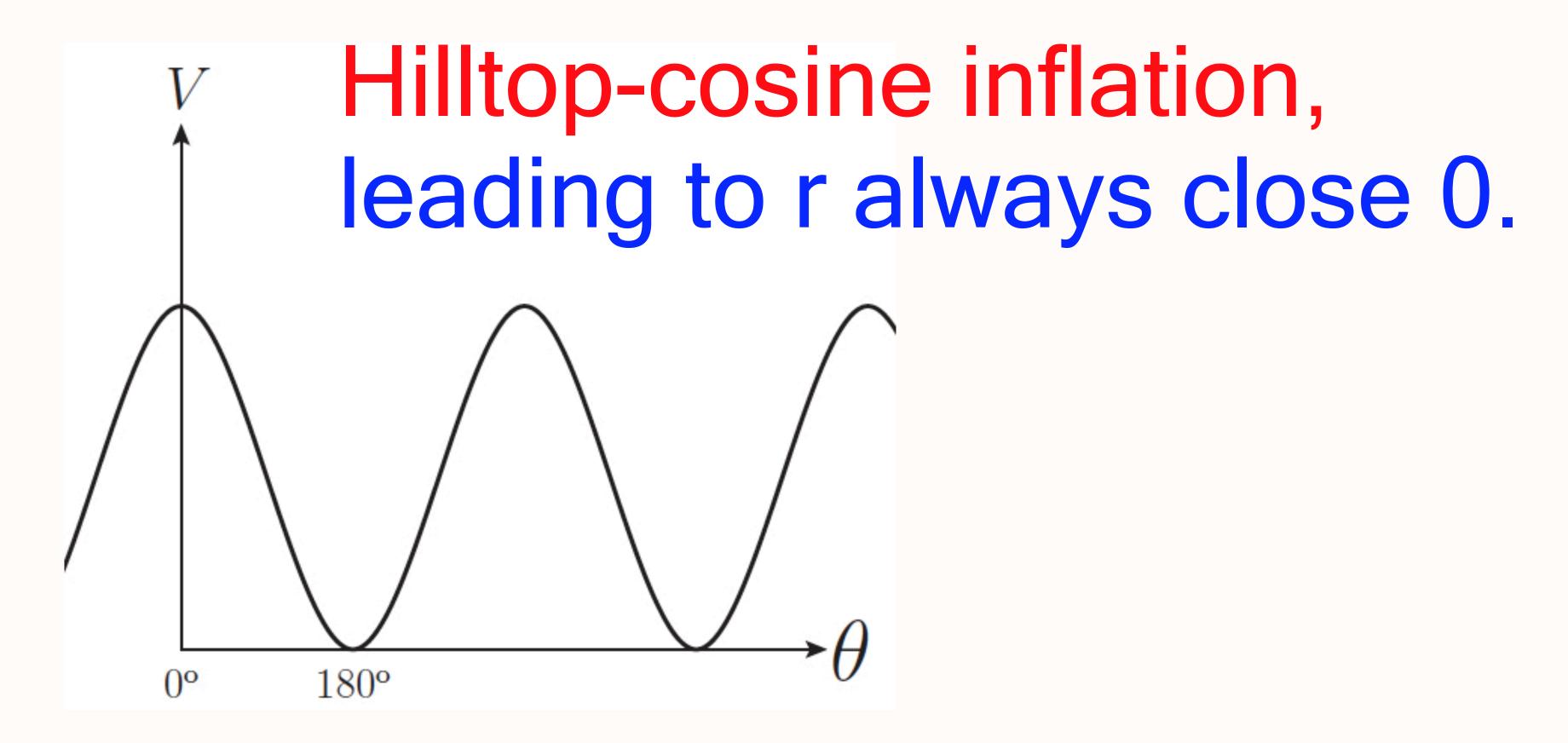
If a global U(1) symmetry is spontaneously broken, the minimum is at 0 or 180°.

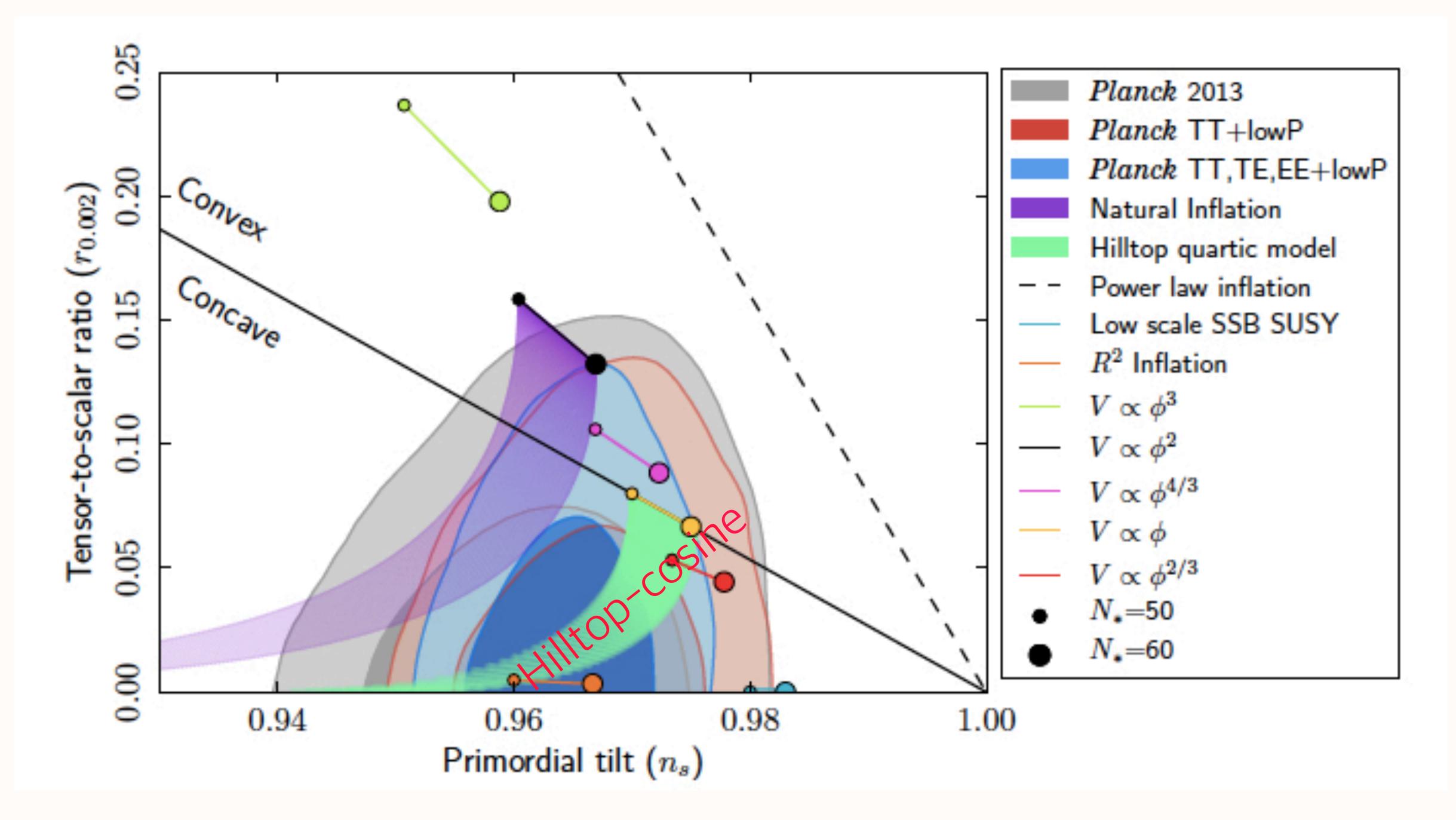
$$V = V_{\text{sym}} + m^3 \sigma + m^{*3} \sigma *$$
$$= \sqrt{2} |m|^3 v \cos(\alpha + c)$$

$$\sigma = \frac{v}{\sqrt{2}}e^{i\alpha}, \quad m^3 = |m|^3 e^{ic}$$

What Vafa and Witten showed is that 0 is the minimum for axion (breaking is only by anomaly without breaking from V).

If we include pseudo scalars from spontaneously broken U(1), not by the anomaly but by V, then 180° can be a minimum depending on parameters. I suggest to classify the inflationary scenario of this type as





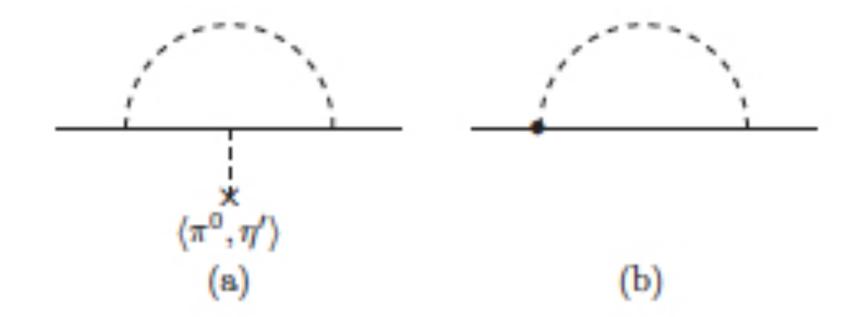


FIG. 4. Loop corrections for $\bar{n}n$ -meson coupling. Insertion of the CP violation effect by VEVs of π^0 and η' in (a). They can be transferred to one vertex shown as a bullet in (b). With this bullet, CP violation is present because of a mismatch between the CP-conserving RHS vertex and CP-violating LHS vertex.

$$\begin{split} -\,V &= m_u v^3 \cos(\theta_\pi + \theta_{\eta'}) + m_d v^3 \cos(-\,\theta_\pi + \theta_{\eta'}) \\ &+ \frac{v^9}{K^5} \cos[2\,\theta_{\eta'} - (c_2^u + c_2^d + c_3)\,\theta] \\ &+ m_u \frac{\Lambda_u^2 v^6}{K^5} \cos[-\,\theta_\pi + \theta_{\eta'} - (c_2^u + c_2^d + c_3)\,\theta] \\ &+ m_d \frac{\Lambda_d^2 v^6}{K^5} \cos[\,\theta_\pi + \theta_{\eta'} - (c_2^u + c_2^d + c_3)\,\theta], \end{split}$$

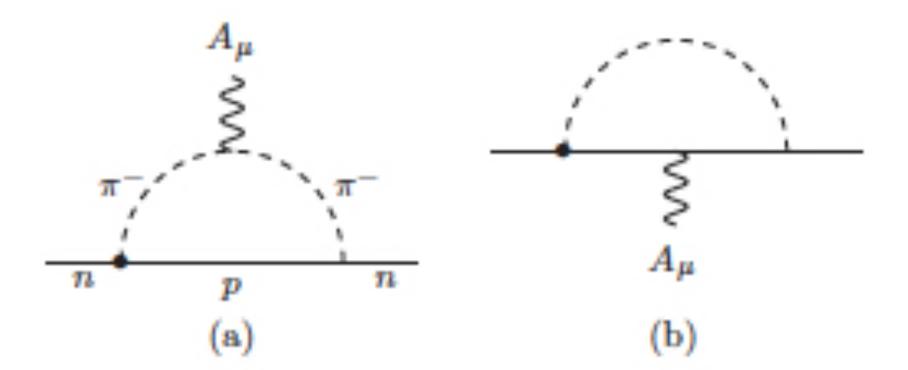


FIG. 5. Diagrams contributing to the NEDM with the bullet representing the CP violation effect. (a) is the physically observable contribution.

Crewther et al. (1979)

$$\overline{g_{\pi NN}} = -\bar{\theta} \frac{2(m_{\Xi} - m_{\Sigma})m_u m_d}{f_{\pi}(m_u + m_d)(2m_s - m_u - m_d)} \approx -0.023\bar{\theta},$$

$$\overline{g_{\pi NN}} = -\bar{\theta} \frac{Z}{(1+Z)} \simeq -\frac{\bar{\theta}}{3}$$
 Kim-Carosi missed a factor: The pion neutron

coupling

$$\frac{d_n}{e} = \frac{g_{\pi nn}\overline{g_{\pi nn}}}{4\pi^2 m_n} \ln\left(\frac{m_n}{m_\pi}\right) = \frac{2g_{\pi nn}^2}{4\pi^2 m_n} \frac{\bar{\theta}}{3} \ln\left(\frac{m_n}{m_\pi}\right)$$

$$=\frac{3.60}{m_n}\bar{\theta} = \bar{\theta} \quad 0.76 \times 10^{-13} \,\mathrm{cm}$$

$$\rightarrow \bar{\theta} \lesssim 2.8 \times 10^{-13}$$

3. QCD phase transition

JEK+S Kim, 1805.08153

Before
$$\begin{cases} \rho = \frac{\pi^2}{30} g_*^i T^4 \\ s = \frac{2\pi^2}{45} g_*^i T^3 \end{cases}$$

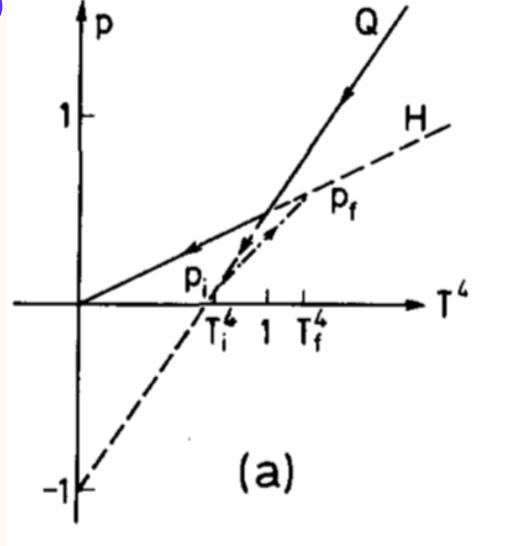
$$\text{After } \begin{cases} \rho = \frac{\pi^2}{30} g_*^f T^4 \\ s = \frac{2\pi^2}{45} g_*^f T^3 \end{cases}$$

$$g_*^i = 51.25, \ g_*^f = 17.25.$$

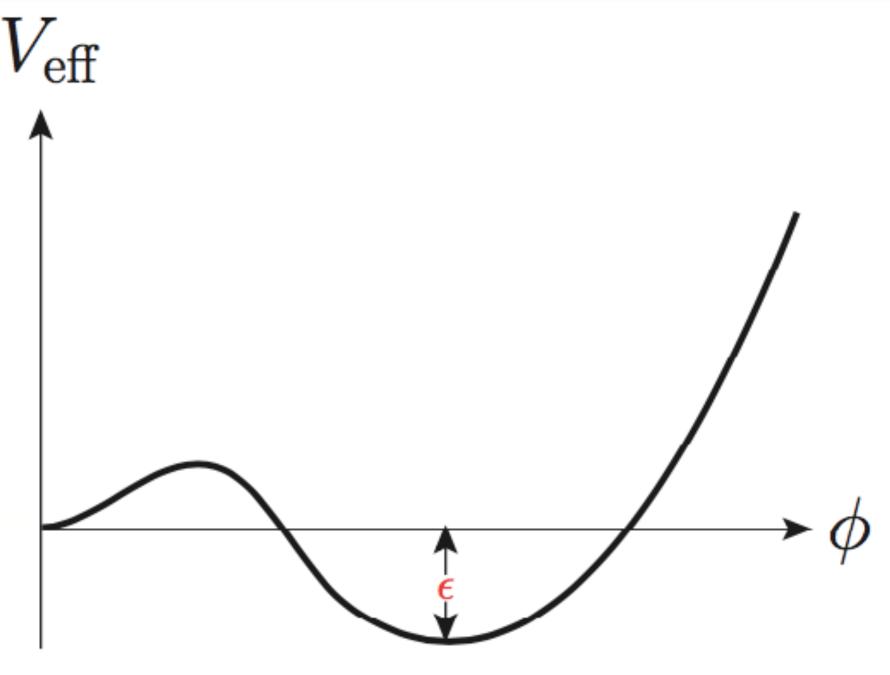
37, for hadrons only

DeGrand and callaborators studied QCD phase transition and axion since 1984 with MIT bag model. This calculation

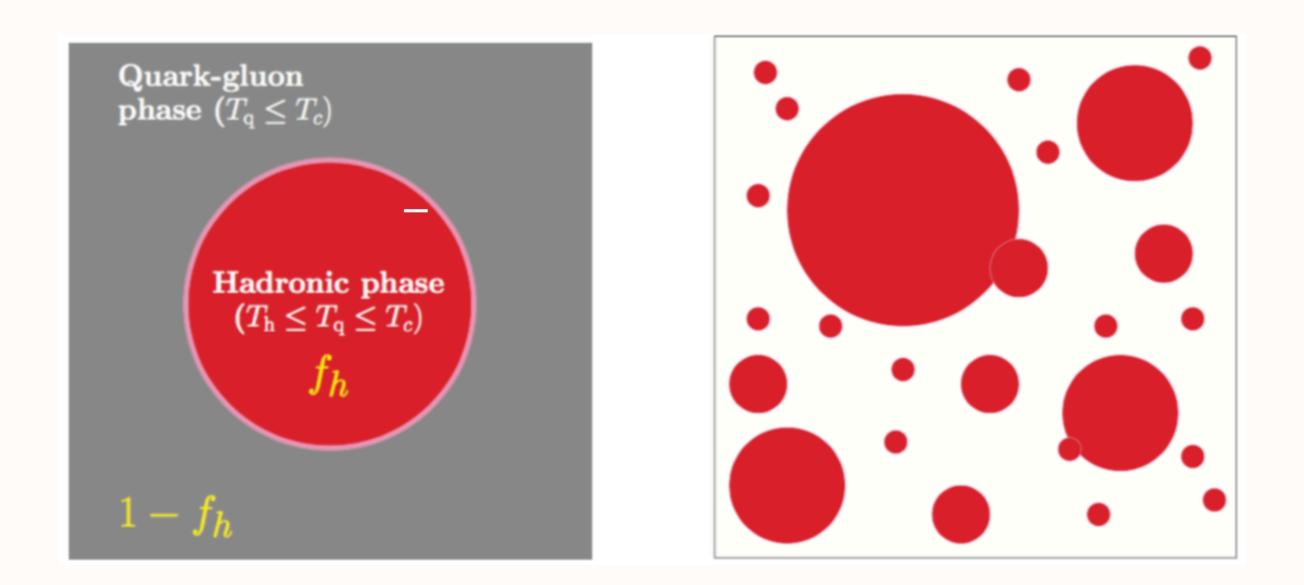
has a complicated behavio



Kolb and Turner studied with a phenomenological Lagrangian with ϵ parameter.



We calculate the phase transition from the first principles.



Here, we study the following two parameter differential equation on the fraction of h-phase in the evolving universe.

$$\frac{df_h}{dt} = \alpha(1 - f_h) + \frac{3}{(1 + Cf_h(1 - f_h))(t + R_i)}f_h$$

It is possible to calculate it because the critical temperature is pinned down now at 165+-5 MeV in the lattice community.

- Knowledge on the axion mass is important.
- Susceptibility χ is important.

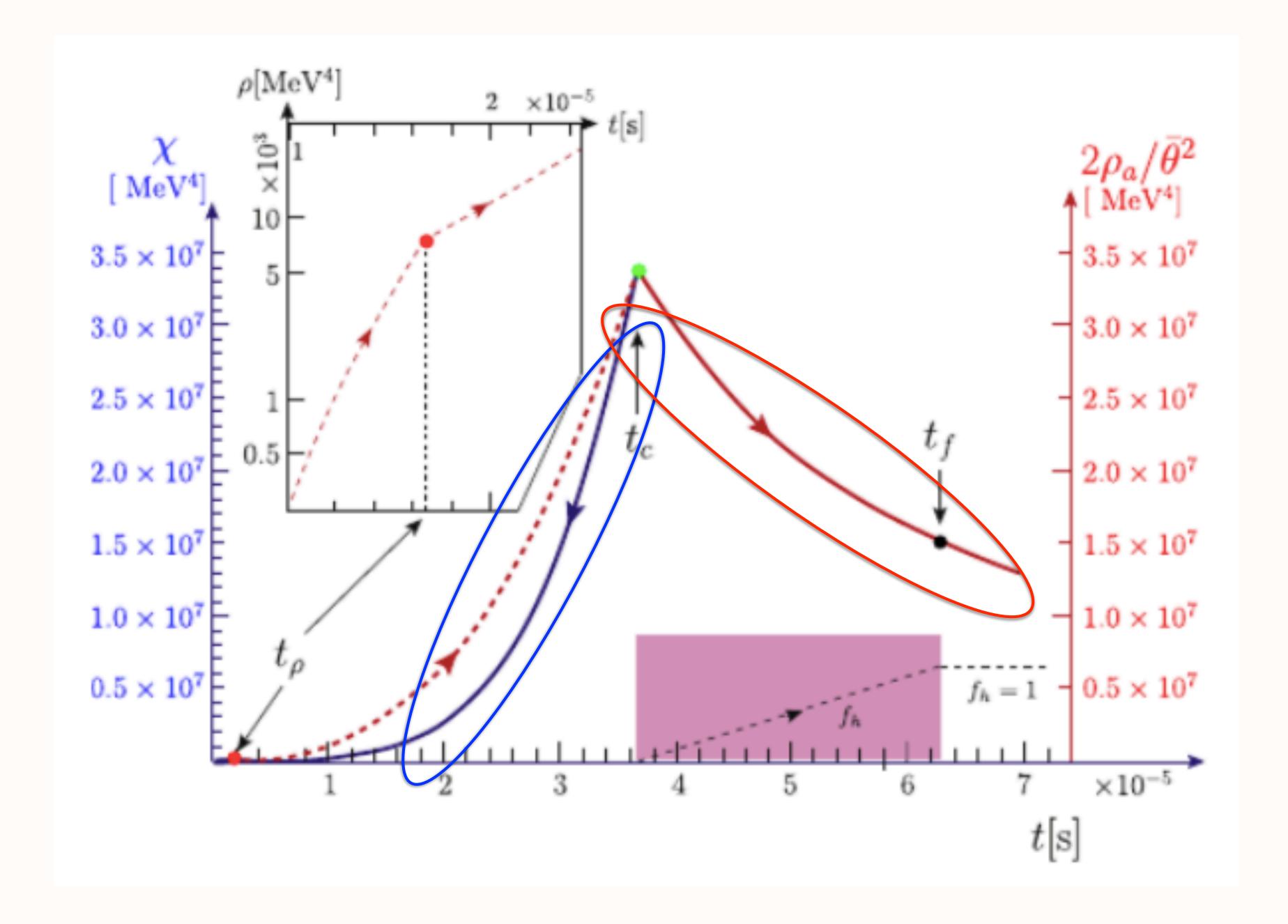
Quark and gluon phase with Λ_{QCD} :

$$f_a^2 m_a^2 = \frac{(\sin^2 \bar{\theta} / \bar{\theta}^2)}{2Z \cos \bar{\theta} + 1 + Z^2} m_u^2 \Lambda_{\text{QCD}}^2 \left(\frac{1}{2} \bar{\theta}^2\right),$$

Hadronic phase in terms of $f_{\pi^0}^2 m_{\pi^0}^2$:

$$f_a^2 m_a^2 = \frac{Z(\sin^2 \bar{\theta} / \bar{\theta}^2)}{2Z \cos \bar{\theta} + 1 + Z^2} f_{\pi^0}^2 m_{\pi^0}^2 \left(\frac{1}{2} \bar{\theta}^2\right),$$

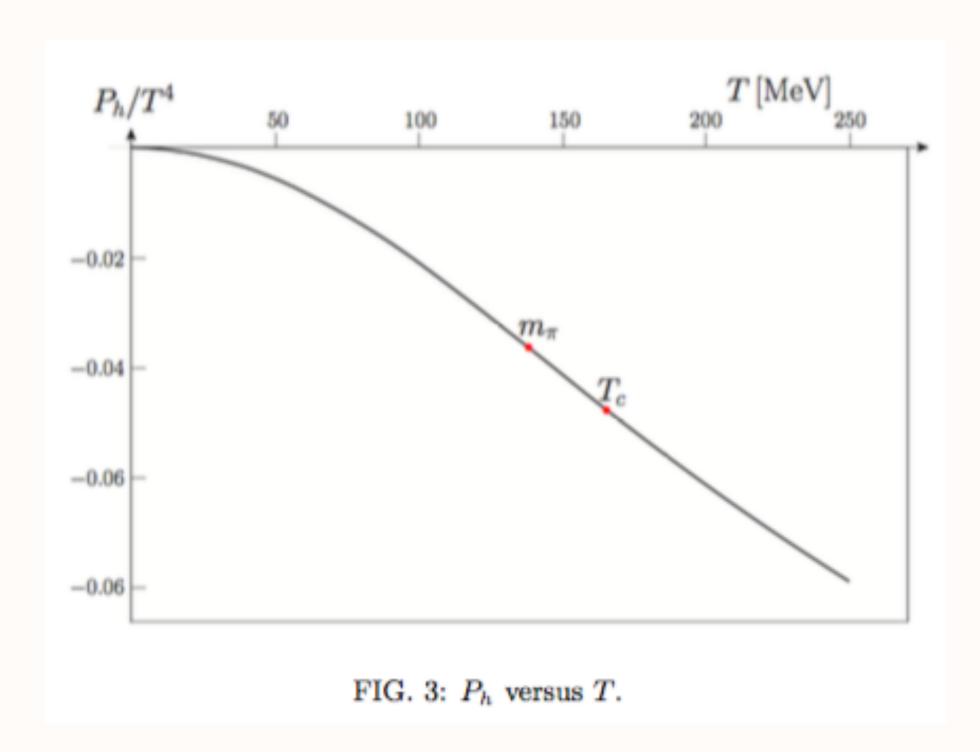
Lattice susceptibility
$$\chi$$
: $f_a^2 m_a^2 = \chi \left(\frac{1}{2}\bar{\theta}^2\right)$,



There are two aspects in this study: (1) the strong interaction, (2) axion energy density evolution in the evolving Universe.

At and below Tc, the quark-gluon phase and the hadronic phase coexist. So, at Tc we know what is the energy density in the q&g-phase. And pressure is just 1/3 of it. So, we know the pressure of h-phase since the pressures are the same during the 1st order phase transition.

Now, at Tc the pion pressure is known. So, it is known below Tc also.



We used Eq. (8.55) of Huang's book, "Statistical Mechanics", in realtivistic form.

 $dU=dQ-PdV+\mu dN,$ Used in the 1st law $dA=-SdT-PdV+\mu dN,$ Used in the evolveing Univ.

 $dG = -SdT + VdP + \mu dN$

During the 1st order(cross-over) phase transition, the Gibbs free energy is conserved. At the same temperature and pressure. We know

P of massless quarks and gluons at temperatures T, 1/3 of energy density.

Now, we have to know P of massive pions at and below Tc.

• In the expanding Universe, the free energy is conserved,

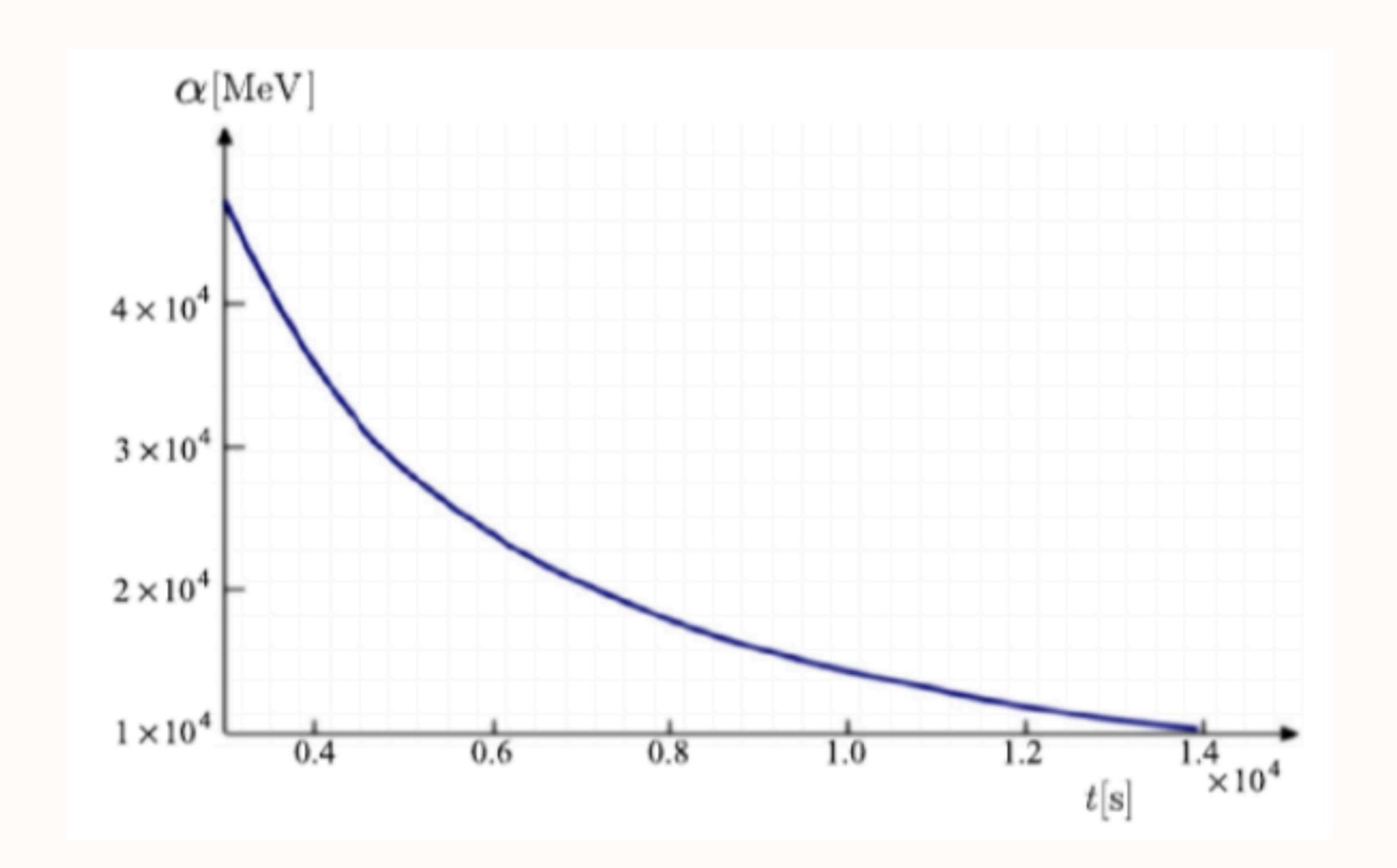
$$(-SdT - PdV + \mu dN)_q + (-SdT - PdV + \mu dN)_h = 0.$$

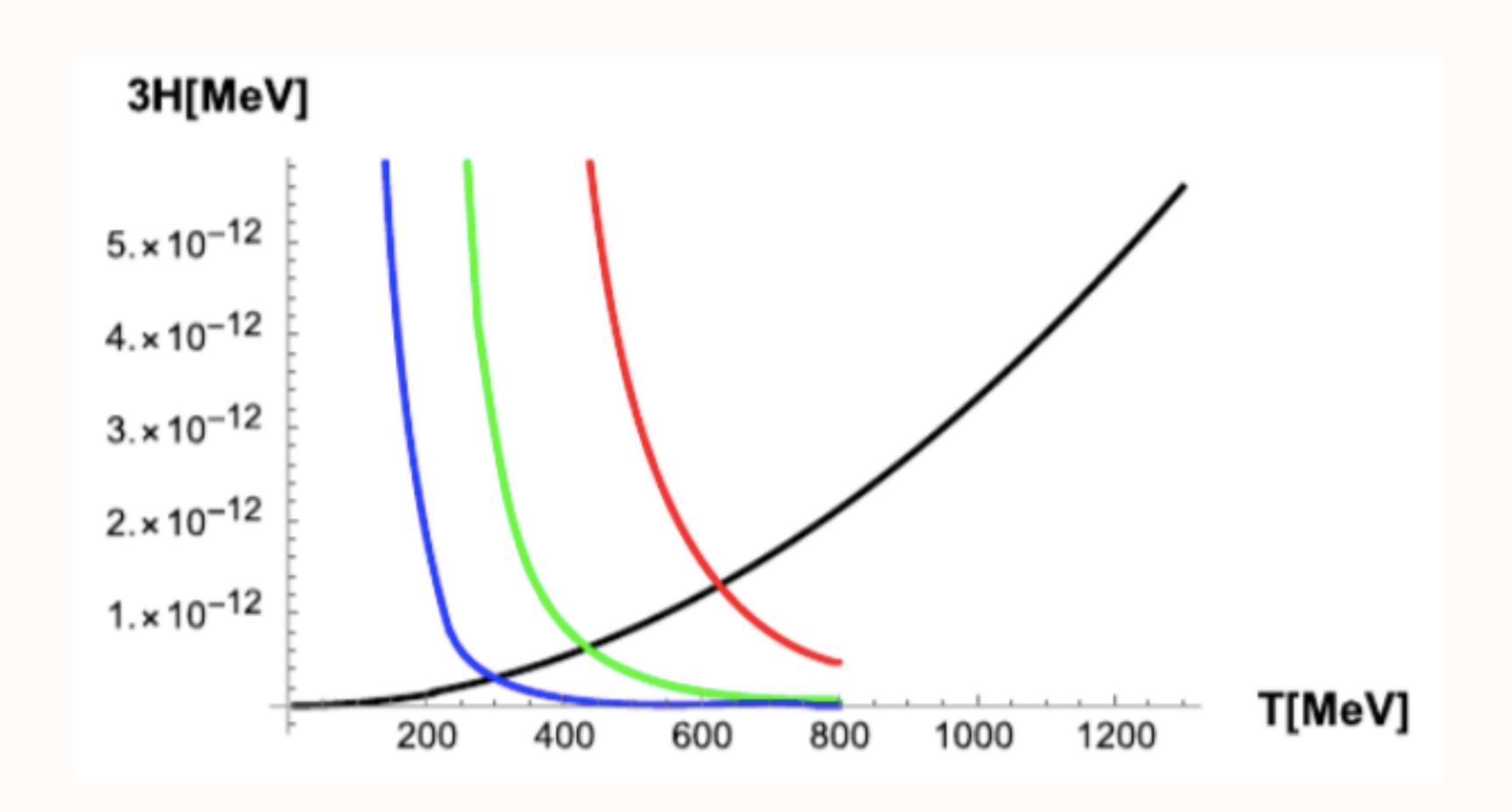
Using $dV_q = -dV_h$,

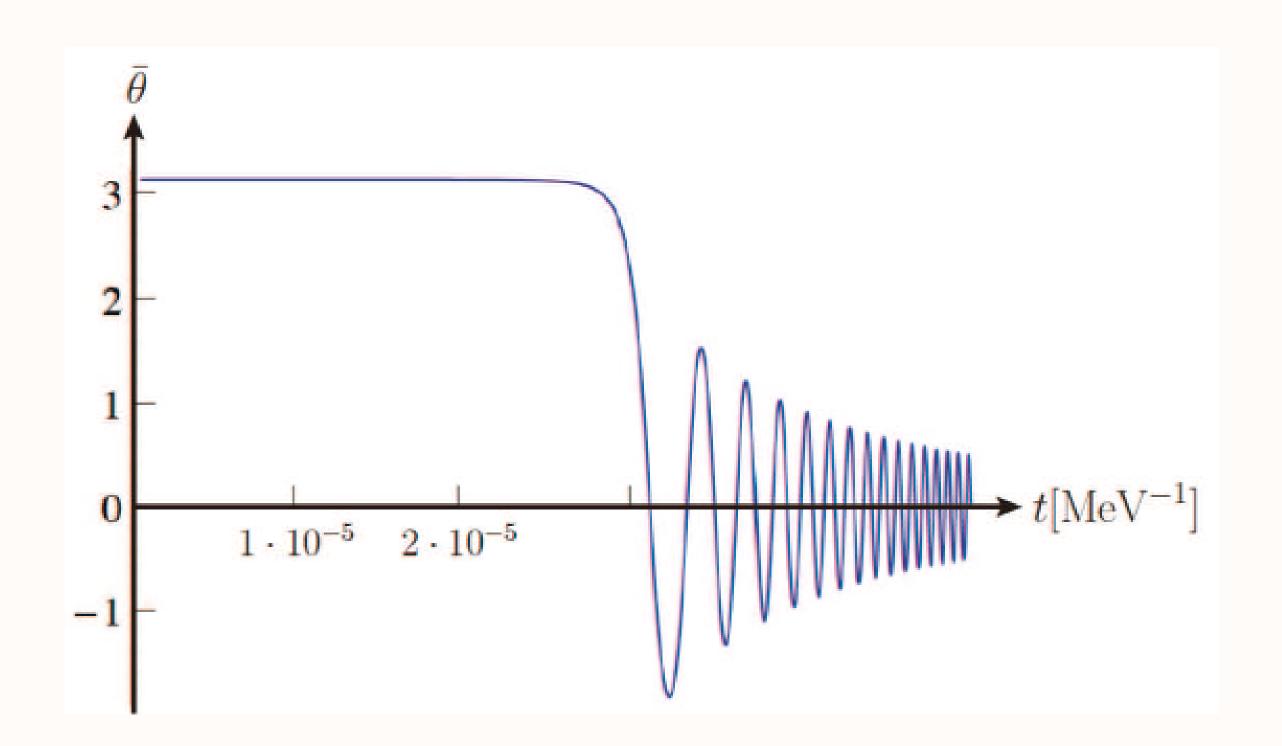
$$(P_h - P_q)dV_h = (S_q - S_h)dT + \mu_h dN_h - \mu_q dN_q = (S_q - S_h)dT.$$

$$\frac{1}{V}\frac{dV_h}{dt} = \frac{(S_q - S_h)}{(P_h - P_q)}\frac{dT}{dt}.$$

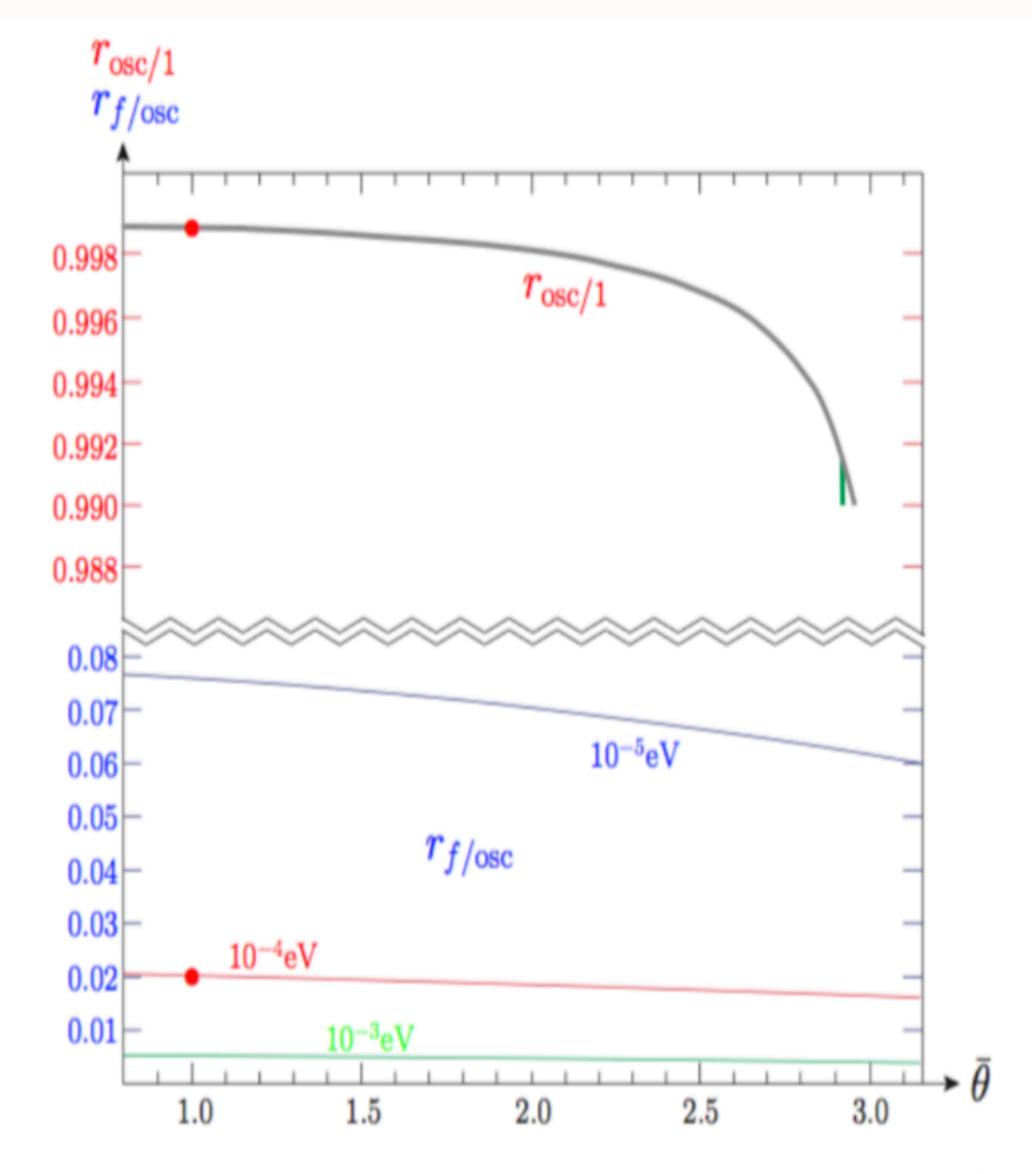
$$\alpha(T) = \frac{(S_q - S_h)}{(P_h - P_q)} \frac{dT}{dt} \approx \frac{-37\pi^2}{45(P_h - P_q)} \frac{T^6}{\text{MeV}}, \text{ with } T^2 t_{[\text{s}]} \simeq \text{MeV}.$$







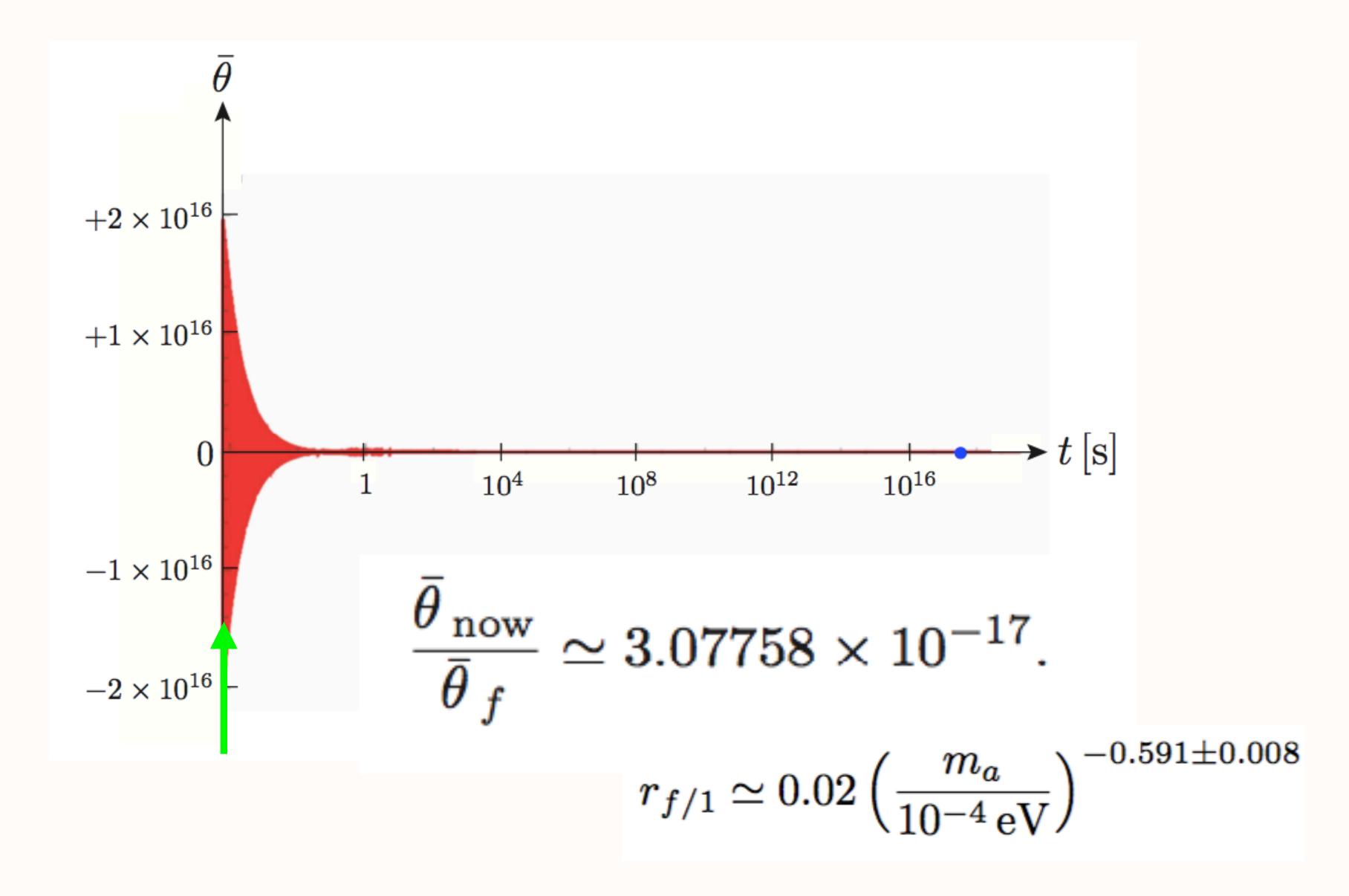
Show movie for m_a independence



$$\bar{\theta}_{\mathrm{now}} \simeq \bar{\theta}_1 \cdot r_{f/1} \cdot \left(\frac{\bar{\theta}_{\mathrm{now}}}{\bar{\theta}_f} \right)$$

$$r_{f/1} \simeq 0.02 \left(\frac{m_a}{10^{-4} \, \mathrm{eV}} \right)^{-0.591 \pm 0.008}$$

FIG. 7: The ratios $r_{\text{osc/1}} \equiv \bar{\theta}_{\text{osc}}/\bar{\theta}_1$ and $r_{f/\text{osc}} \equiv \bar{\theta}_f/\bar{\theta}_{\text{osc}}$ as functions of $\bar{\theta}_1$ for three $m_a(0) (= 10^{-3} \,\text{eV(green)}, 10^{-4} \,\text{eV(red)}, 10^{-5} \,\text{eV(blue)}$. In the upper figure, these curves are almost overlapping (shown as gray) except the green for a large $\bar{\theta}_1$. [See also Supplement.] t_{osc} is the time of the 1st oscillation after which the harmonic motion is a good description. Different T_1 's are used for different $m_a(0)$, as presented in Fig. 4.



From t_f to t_{now}: (JEK, S. Kim, Nam, 1803.03517)

 3.07758×10^{-17}

We calculated a new number F_{now}.

The final factor is

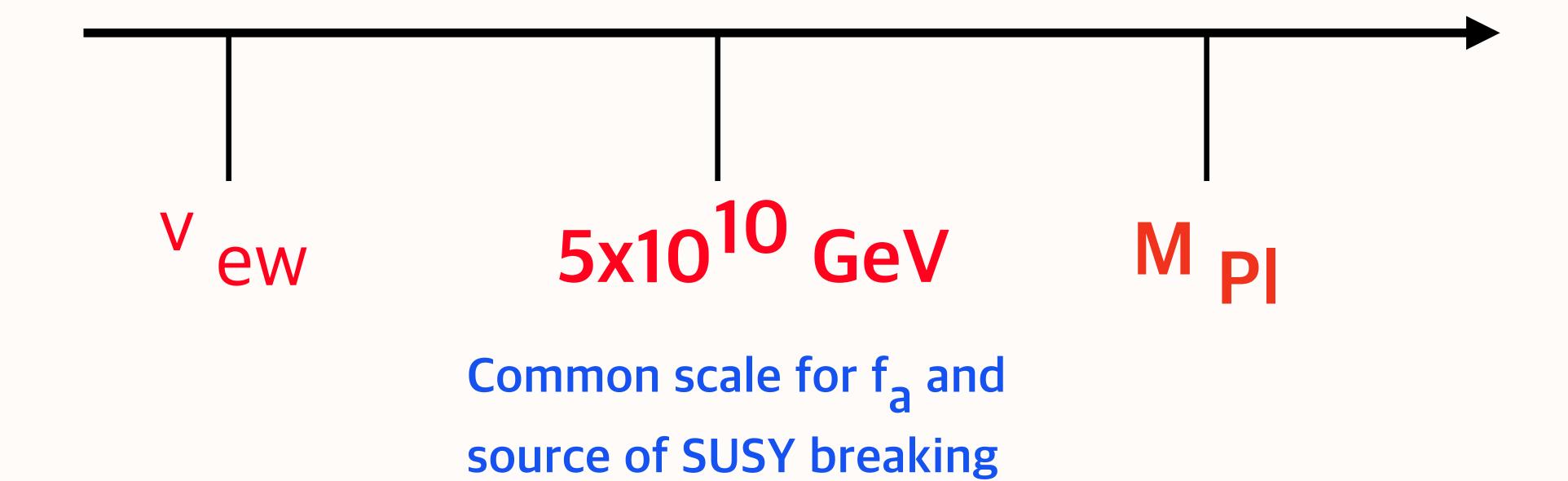
$$\bar{\theta}_{\text{now}} \simeq \bar{\theta}_1 \cdot r_{f/1} \cdot \left(\frac{\bar{\theta}_{\text{now}}}{\bar{\theta}_f}\right) = 0.62 \times 10^{-18} \bar{\theta}_1$$

4. Hierarchy together with "invisible" axion

May be related to —nepLowEenergyScales

JEK+Kyae, 1904.07371

Chirality is the one. Chirality ensures small scales.



Mass scales:

Planck mass 2.44x10¹⁸ GeV

Next scale defines physics disciplines
Particle physics 246 GeV
Strong Interaction 300 MeV
Nuclear physics 7 MeV

Atomic physics 1 eV
Condensed matter phys 10⁻³ eV

Mass hierarchy:

(Planck mass)/(EW scale) 10¹⁶ (GUT mass)/(EW scale) 10¹⁴

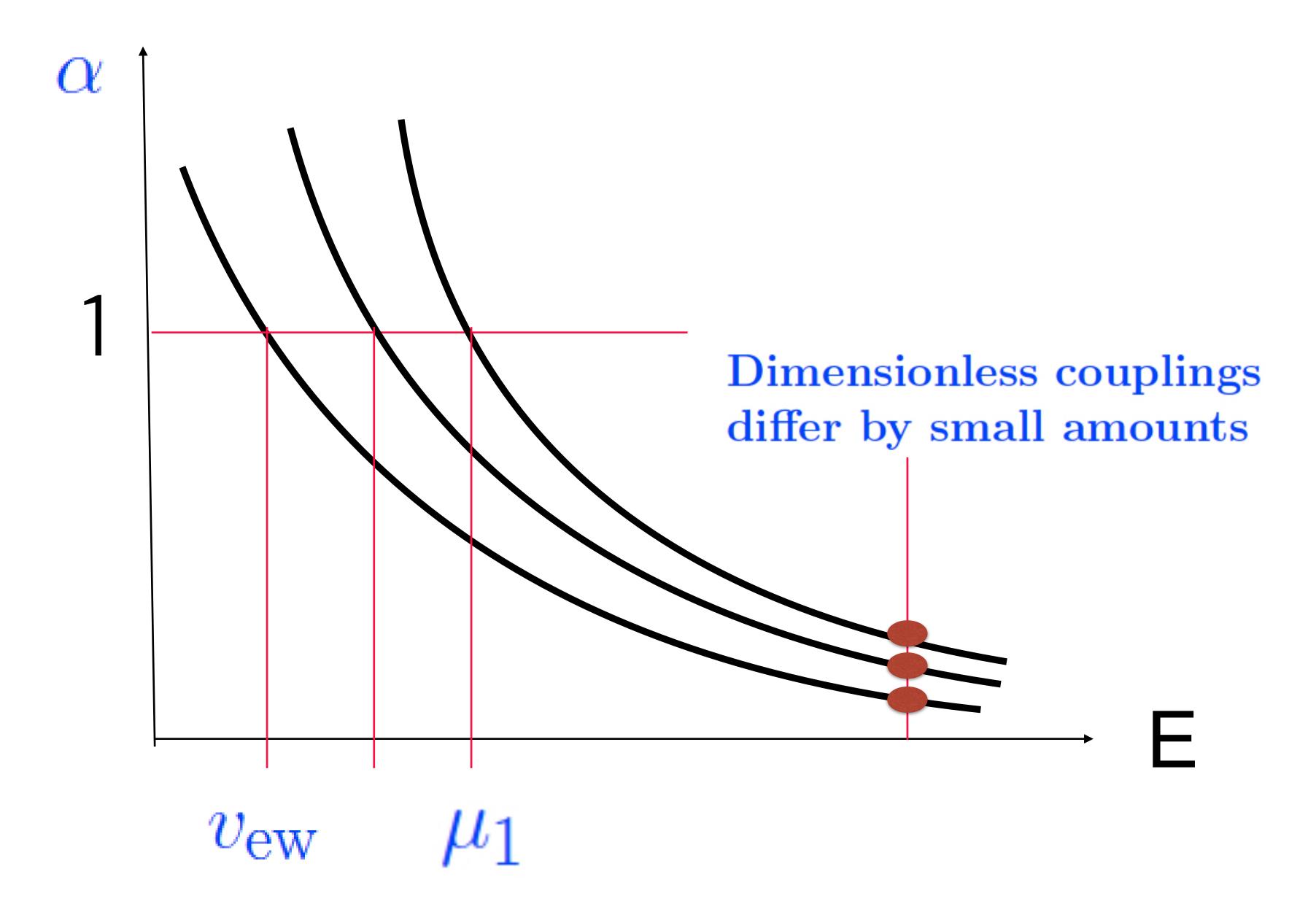
$$V = -M^2 \Sigma^* \Sigma - v_{\text{ew}}^2 H^{\dagger} H + \cdots$$

In the potential V, the scalar (mass)² parameters have the ratio of 10²⁸.

Why is there such a large ratio of parameters? Including loop corrections? TeV is the cutoff.

This was pointed out by S.Weinberg after the GUT models were proposed. The GUT models must have parameters such that the Higgs mechanism breaks both SU(5) and SU(2)xU(1) SM.

An exponential hierarchy obtained by dimensional transmutation.



1st confining force:

Technicolor confines at 3 TeV: Susskind and Weinberg 1979.

exponential 3 TeV= M_{GUT} x e⁻⁴⁰.

Dimensional transmutation, e.g. 300 MeV

But it failed in flavor physics, by extended technicolor,

through S and T parameter constraints.

Yukawa couplings are definitely needed: scalars are needed definitely.

SUSY idea: 1981~

Supergravity phenomenology: 1983~

Supersymmetry: LSP added for DM candidate: 1984~

SUSY breaking needed: Needed for SM partners ~(TeV)²,

Source of SUSY breaking: 10¹³ GeV, by Gaugino condensation

L = SUSY terms + SUSY breaking soft terms of O(TeV²)

Gaugino condensation by R=0 singlet:

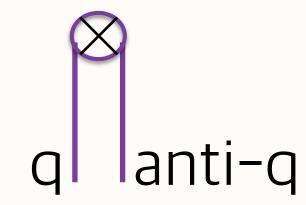
Nilles(1982),

Derendinger-Ibanes-Nilles(85),

Dine-Rohm-Seiberg-Witten(85)

Condensation of q and anti-q in QCD:

 $(300 \text{ MeV})^3$



Similarly, gauginos in SUSY theory may condense: Gaugino condensation. (10¹³GeV)³

Then, scalar (mass)² parameters in the SM feel this breaking by gravity effects: (10¹³GeV)³ / (Planck mass)² ~ TeV

How come, "Is there such source of 10¹³GeV confining force? Is there really "gaugino condensation"?

DIN, DRSW.

SQCD before, SGUT now

SUSY SU(N) gauge theory with L-handed q and R-handed q. $SU(N_C)$ gauge group $SU(N_f)xSU(N_f)$ flavor group (global) Introducing a vector-like representation.

Studied extensively by Seiberg and his collaborators, and many more. These focussed on duality and not obtained SUSY breaking from the gauge theory.

Anomaly free theories.

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fundamentals: [1] one contra-variant index, [2] two contra-variant index, etc.
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SU(3): only quarks or anti-quarks

SU(4): only quarks or anti-quarks plus [2]=self-dual (removed)

SU(5): the smallest gauge group to have a chiral representation, [2] + [4] which is anomaly free. Due to Georgi's criteria, this is the simplest example.

 $[2] = \Psi^{\alpha\beta} : \Psi^{\alpha\beta} = -\Psi^{\beta\alpha}$ In conclusion, we have found that in theories with chiral fermions the presence of several currents which do not fall into a vector/axial vector classification

 $\Psi^{\alpha\beta}$ \oplus brings about strong constraints on SUSY vacua. These constraints, once coupled to reliable small-size instanton effects, lead in certain cases to a contradiction.

suggested a Even the SQCD way out of a vacuum at infinity appears to be blocked leaving us with the only possibility of a non-supersymmetric ground state.

> In the near future further calculations should not fail to provide a complete systematics of the circumstances under which spontaneous SUSY breaking take place.

Our model (took 36 years):

Generation of M

JEK+Kyae: 1904.07371 "A model for dynamical SUSY breaking"

SU(5) representation:
[2] + [1] + 2[4] which is anomaly free.

Now we can construct superpotential terms,

$$W_0 \ni \frac{1}{4} \bar{\Psi}^{\alpha\beta} \psi_{2\alpha}^i \psi_{2\beta}^j \epsilon_{ij}, \ \bar{\psi}_1^{\alpha} \psi_{2\alpha}^i D_{1i}, \ \frac{1}{5!} \bar{\Psi}^{\alpha\beta} \bar{\Psi}^{\gamma\delta} \bar{\psi}_1^{\epsilon} \epsilon_{\alpha\beta\gamma\delta\epsilon},$$

This is not possible with Meurice-Veneziano. In ours, one U(1) remaining.

$$U(1)_{\bar{\Psi}} + 2U(1)_{\psi_2} = 0,$$

 $U(1)_{\bar{\psi}_1} + U(1)_{\psi_2} + U(1)_{D_1} = 0,$
 $2U(1)_{\bar{\psi}_1} + U(1)_{\bar{\psi}_1} = 0.$

 $SU(5)_{gauge}$ -singlet chial fields,

$$\phi = \frac{1}{5!} \bar{\Psi}^{\alpha\beta} \bar{\Psi}^{\gamma\delta} \bar{\psi}_{1}^{\epsilon} \, \epsilon_{\alpha\beta\gamma\delta\epsilon}, \, \, \Phi_{i} = \bar{\psi}_{1}^{\alpha} \psi_{2\alpha i}.$$

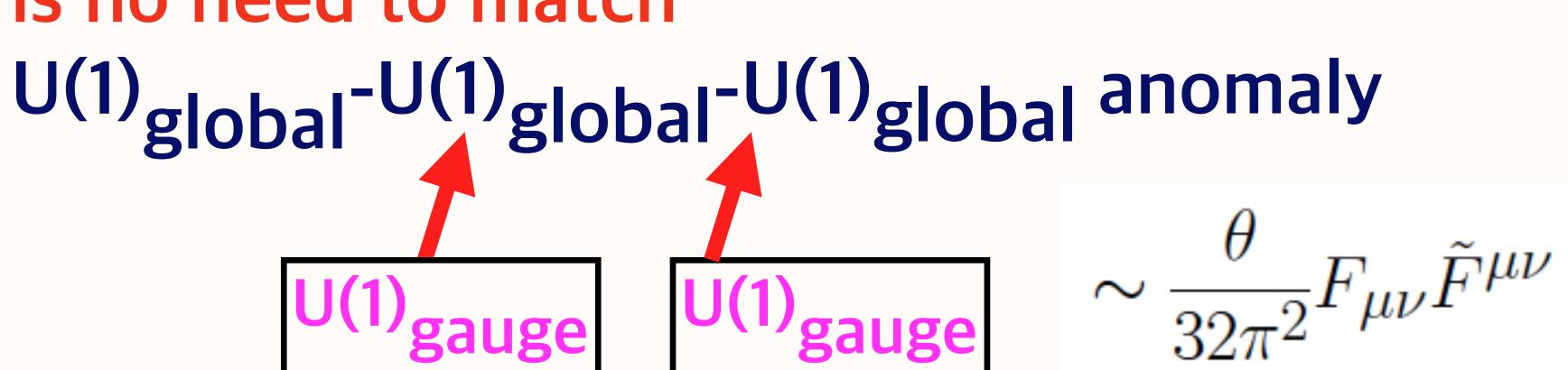
U(1)_{global}-SU(2)_{gauge}-SU(2)_{gauge} anomaly below conf. scale
As in axion physics theta term is considered by triangle loops.

$$\sim \frac{\theta}{32\pi^2} F_{\mu\nu}^a \tilde{F}^{a\,\mu\nu}$$

Confinement of SU(2) leads to this anomaly, due to instanton calculus, even if we integrate out the SU(2) charged fermions. If we consider infinite spacetime, gauged SU(2) is like global SU(2). So, we satisfy

For U(1), we do not have the instanton argument, and there

is no need to match



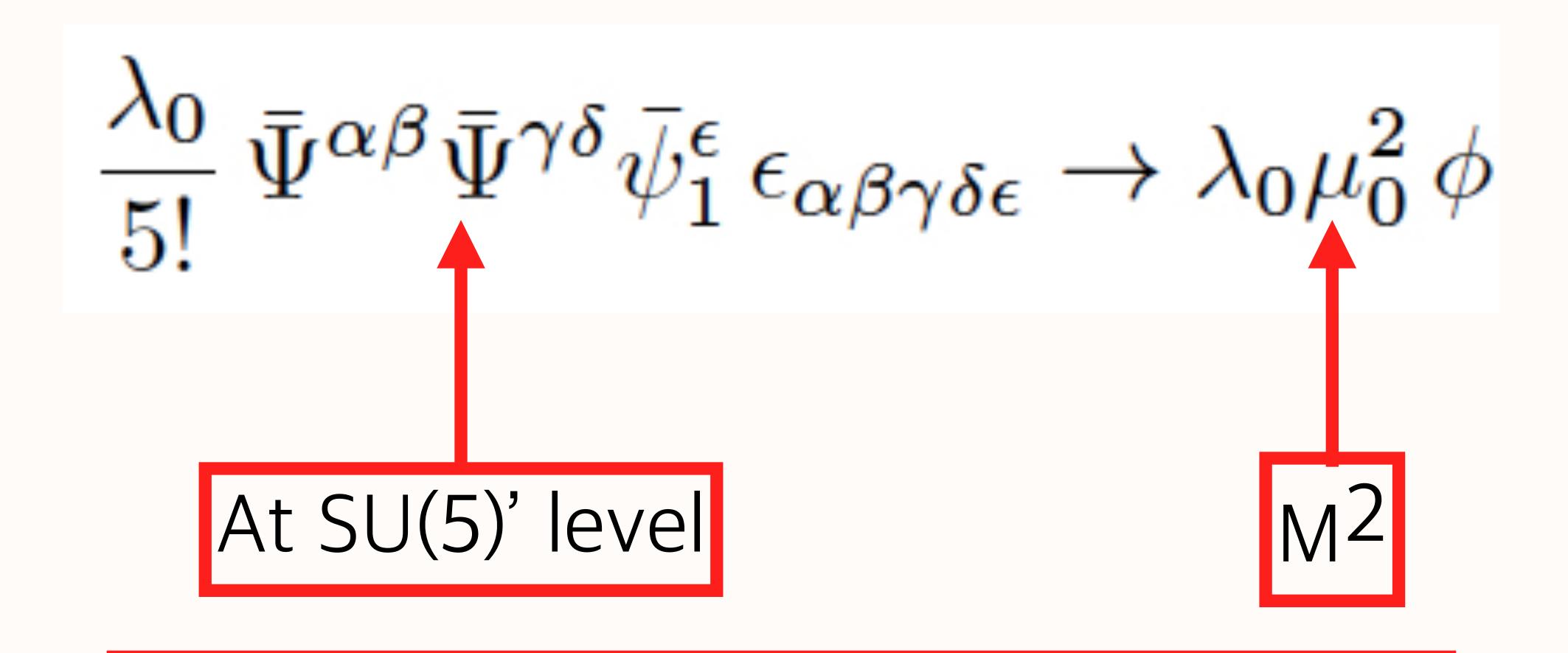
Even if we consider it, we know that it is a total derivative.

$$\begin{split} & \propto \theta \frac{1}{4} \epsilon_{\mu\nu\rho\sigma} (\partial_{\mu} A_{\nu} - \partial_{\nu} A_{\mu}) (\partial_{\rho} A_{\sigma} - \partial_{\sigma} A_{\rho}) = \theta \epsilon_{\mu\nu\rho\sigma} (\partial_{\mu} A_{\nu}) (\partial_{\rho} A_{\sigma}) \\ & = \partial_{\rho} [\theta \epsilon_{\mu\nu\rho\sigma} (\partial_{\mu} A_{\nu}) (A_{\sigma})] - [\partial_{\rho} (\theta \epsilon_{\mu\nu\rho\sigma} \partial_{\mu} A_{\nu})] (A_{\sigma}) \\ & = \partial_{\rho} [\theta \epsilon_{\mu\nu\rho\sigma} (\partial_{\mu} A_{\nu}) (A_{\sigma})] - [\theta \epsilon_{\mu\nu\rho\sigma} \partial_{\rho} \partial_{\mu} A_{\nu}] (A_{\sigma}) \\ & = \partial_{\rho} [\theta \epsilon_{\mu\nu\rho\sigma} (\partial_{\mu} A_{\nu}) (A_{\sigma})] \end{split}$$

	$2\ell(R_{SU(5)})$	SU(2)	$U(1)_{ar{\Psi}}$	$U(1)_{\bar{\psi}_1}$	$U(1)_{\psi_2}$	$U(1)_{D_1}$	$U(1)_{AF}$	$U(1)_R$	dimension
v	0	0	0	0	0	0	0	+1	1/2
$\bar{\Psi} \sim (\overline{\bf 10}, \bf 1)$		1	+1	0	0	0	-1	+1	1
fermion	+3	1	+1	0	0	0	-1	0	1
$ar{\psi}_1 \sim (\overline{f 5}, {f 1})$	-	1	0	+1	0	0	+2	0	1
fermion	+1	1	0	+1	0	0	+2	-1	
$\psi_2 \sim ({f 5},{f 2})$, -	2	0	0	+1	0	$+\frac{1}{2}$	$+\frac{1}{2}$	1
fermion	$+1 \times 2$	2	0	0	+1	0	$+\frac{1}{2}$	$-\frac{1}{2}$	
$D \sim (1, 2)$	· —	2	0	0	0	+1	$-\frac{5}{2}$	$+\frac{3}{2}$	1
fermion	$+1 \times 2$	2	0	0	0	+1	$-\frac{5}{2}$	$+\frac{1}{2}$	-
$W^a \sim \lambda^a$	0	<u> </u>	0	0	0	0	0	+1	3 2
Λ^b		<u></u>		_	-	_	-	$\frac{2b}{3}$	b
ϕ		1	_	_	1-1	1	-5	+2	1
fermion	_	1	· —	_	-	_	-5	+1	1
Φ_i	1 - 1 - 1	2	1	_	-	_	$+\frac{5}{2}$	$+\frac{1}{2}$	1
fermion	/ \tau	2	A	200	77 -		$+\frac{5}{2}$	$-\frac{1}{2}$,
\boldsymbol{S}	<u></u>	1	0	0	0	0	0	+2	1
fermion	1/2/19	1	0	0	0	0	0	+1	_
$D^i \sim (1,2)$		2	_	_	_	+1	$-\frac{5}{2}$	$+\frac{3}{2}$	1
fermion		2	_	-	1 1 - 1	+1	$-\frac{5}{2}$	$+\frac{1}{2}$	<u></u>

The superpotential consistent with SU(2)_{global} x U(1)_{global} is

$$\begin{split} W &= M^2 \phi + \frac{N_c(N_c^2-1)}{32\pi^2} \mu_0^2 S \left(1 - a \log \frac{\Lambda^3}{S\mu_0^2}\right) + b M \Phi_i D^i, \\ \frac{\partial W}{\partial \phi} &= 0: \ M^2 = 0, \\ \frac{\partial W}{\partial \Phi_i} &= 0: \ D^i = 0, \\ \frac{\partial W}{\partial D^i} &= SUSY \ \text{is}_0 \text{broken by the 'O Raifeartaigh mechanism!!!} \\ \text{This is shown here for the first time.} \\ \frac{\partial W}{\partial S} \text{Soft we}_0^2 \text{have}_0 \text{-solution} \text{ for the gauge hierarchy problem.} \end{split}$$



If lambda0 is nonzero, M² is nonzero

Common scale for SUSY breaking and fa

So, if the hidden SU(5)' confines at 10 GeV - 5x10 GeV, the SUSY breaking scale for SM partners is above 1 TeV.

In particular, the lower end 5x10 - 10 GeV is particularly interesting because it is the anticipated axion scale, which is the most difficult region for axion search.

The SU(5)' confinement provides this region because of the scalar condensation, rather than gaugino condensation.

In our case, the confinement scale by singlet composite scalar is somewhere between 5x10¹⁰ GeV—10¹² GeV. Not at 10¹³ GeV.

With this, M_{SUSY} can be raised to the scale of the little hierarchy. The super partner scale at a TeV needs a^{1/2}x5x10¹⁰ GeV for the confinement scale. 6 TeV needs 10¹¹ GeV confinement scale.

5. Conclusion

- 1. Axion theory discussed.
- 2. "Invisible" axion from string is commented.
- 3. How this intermediate scale is realized is proved by a SU(5)' confining force.
- 4. This can be used for the little hierarchy with fine-tuning of order less than 100.

Randall: To discover one, one should be an expert

in model building [APS Denver, April, 2019]