

Deep Learning for the LHC physics

Myeonghun Park

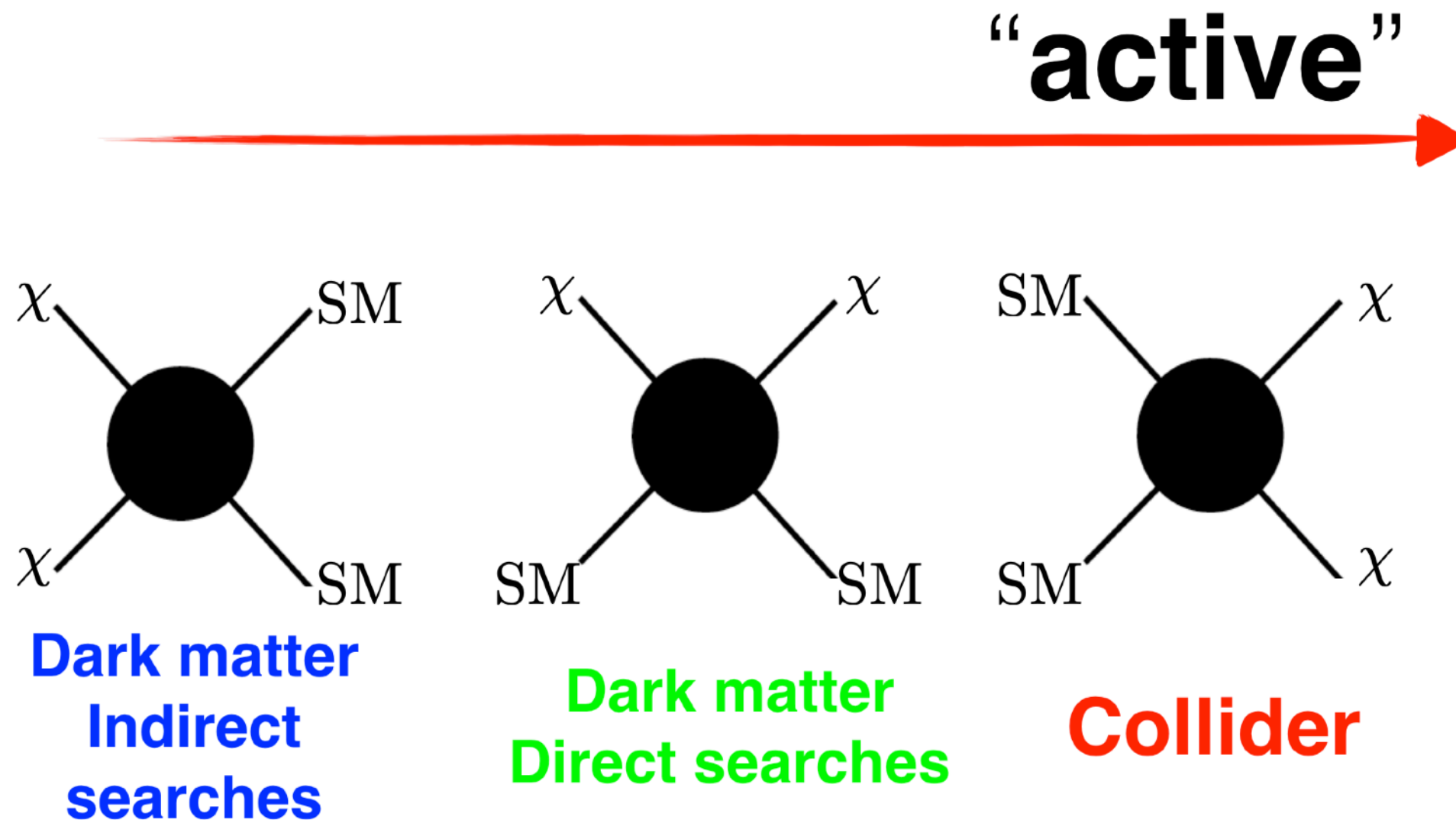


Deep Learning: [arXiv:1904.08549](https://arxiv.org/abs/1904.08549) (JHEP 2019)

IBS-MultiDark-IPPP 2019

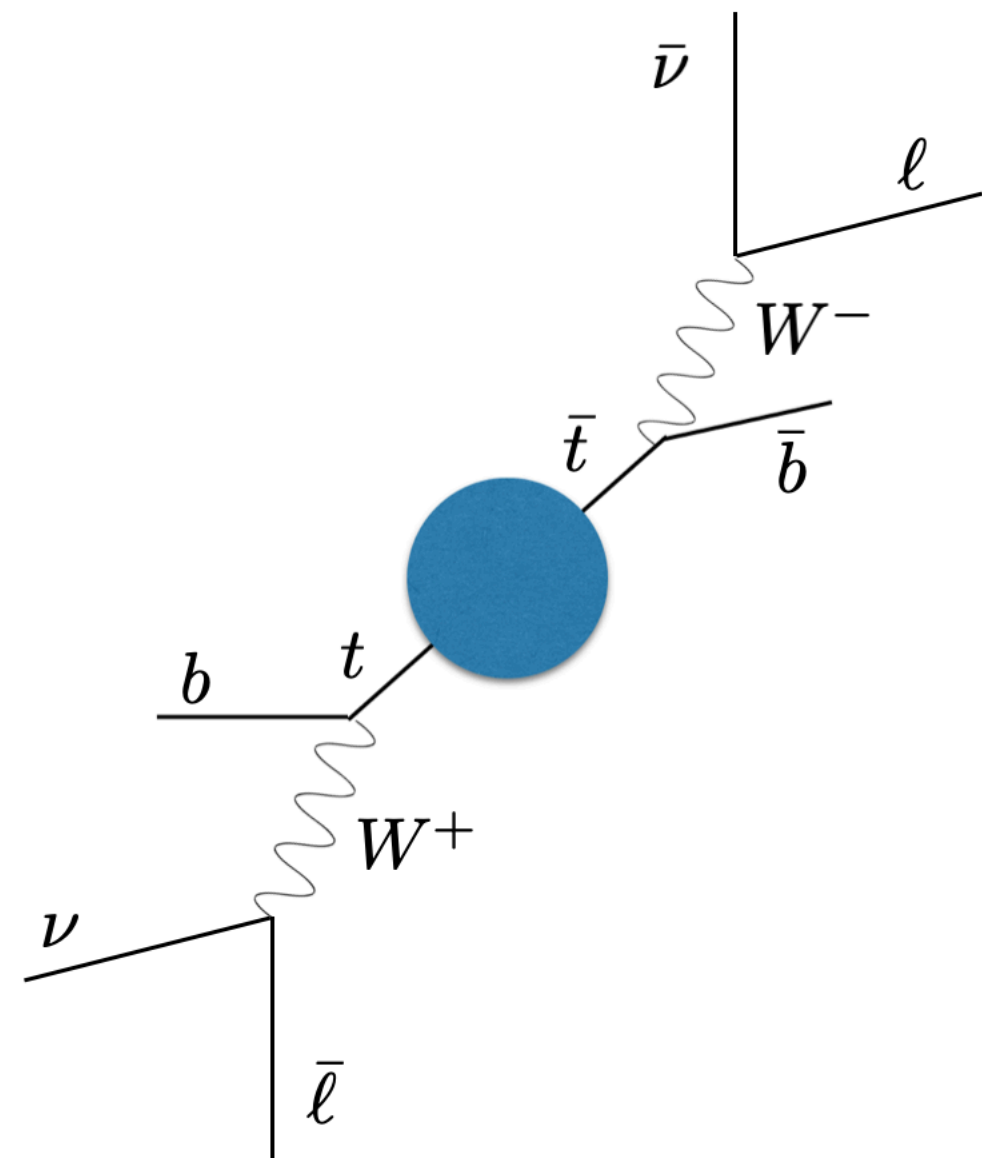
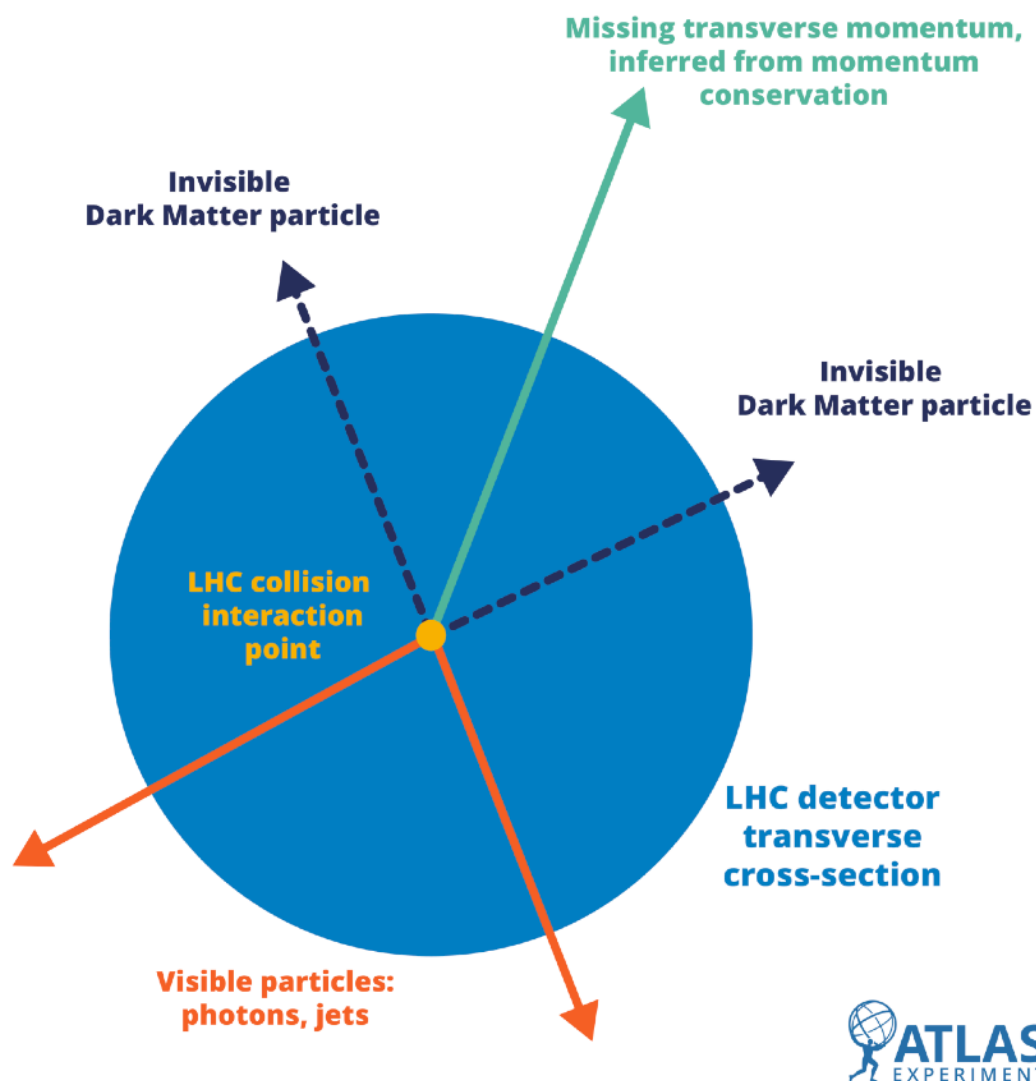
Experimental confirmation of out theoretical expectations

- How a **theory** is beautiful, as a physicist we need to confirm our theory with **experiments**.



- How can we maximize the chance of the LHC ?

- LHC provides complicated data in an unprecedented way.
 - **Huge** QCD / Standard Model backgrounds.
- "Invisible" dark matter provides missing transverse energy
- Neutrinos from $t\bar{t}$ also provides "similar signature"



- LHC provides complicated data in an unprecedented way.
 - **Huge** QCD / Standard Model backgrounds.

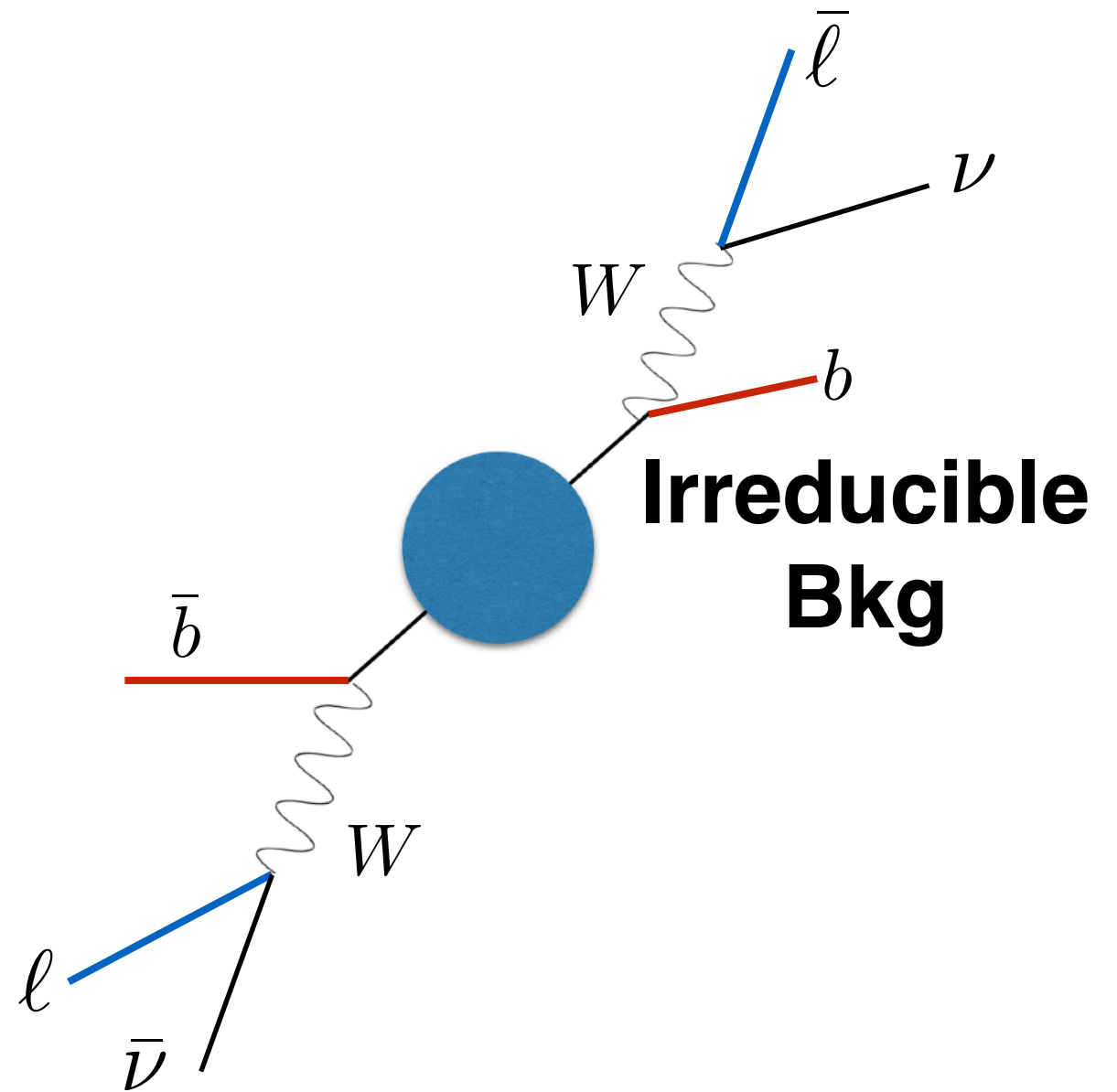
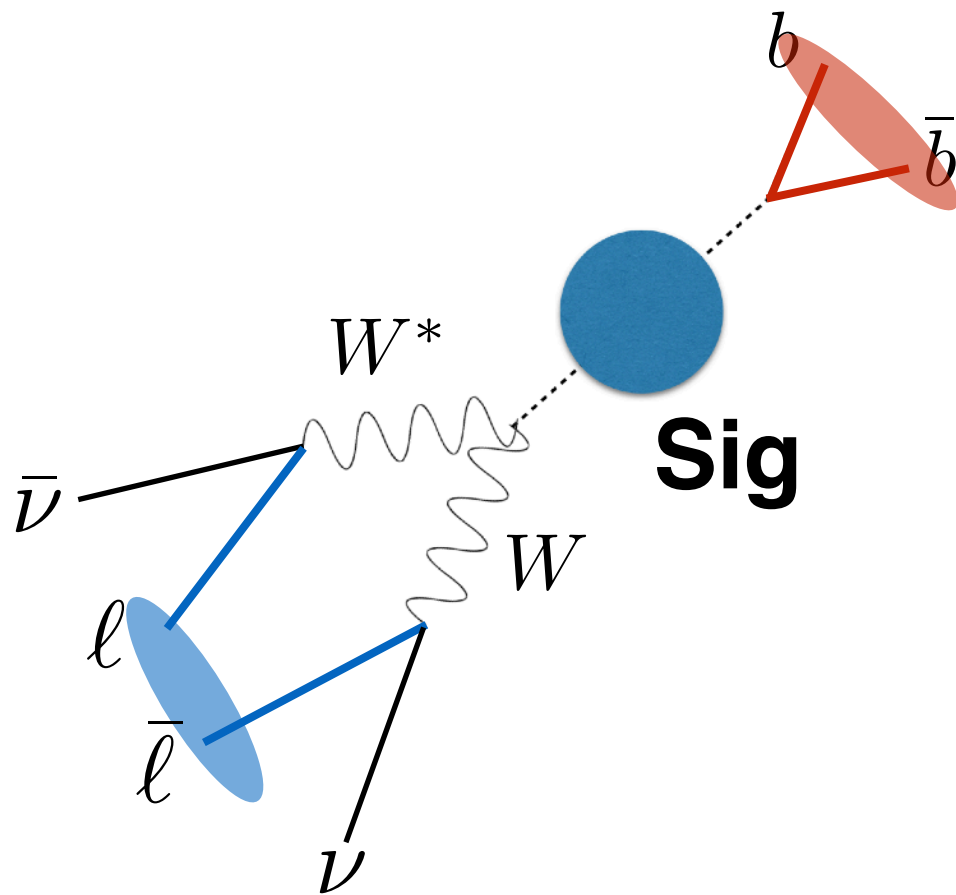
: Efficient way to reduce "unwanted" backgrounds with helps from data science (Deep Learning: DL)

- Neutrinos from $t\bar{t}$ also provides "similar signature"

: To understand DL performance, I will take one example from my recent works. (HH)

- This example is "supervised" Machine Learning

- $pp \rightarrow HH \rightarrow b\bar{b}, \ell\bar{\ell}, \nu\bar{\nu}$

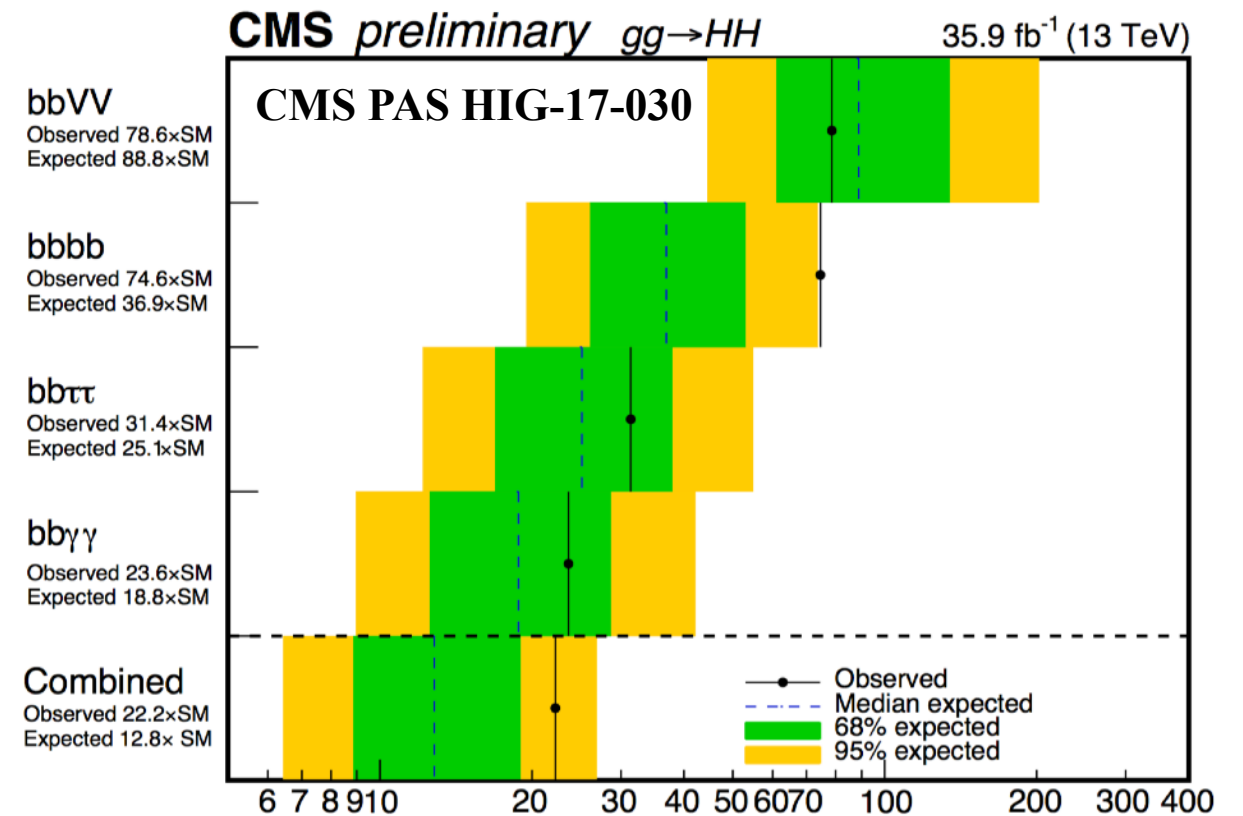


LHC Run 2 result

- Current status from various channels

$h \rightarrow XX$

	bb	WW^*	$\tau\tau$	ZZ^*	$\gamma\gamma$
bb	33%				
WW^*	25%	4.6%			
$\tau\tau$	7.3%	2.7%	0.39%		
ZZ^*	3.1%	1.1%	0.33%	0.069%	
$\gamma\gamma$	0.26%	0.1%	0.028%	0.012%	0.0005%

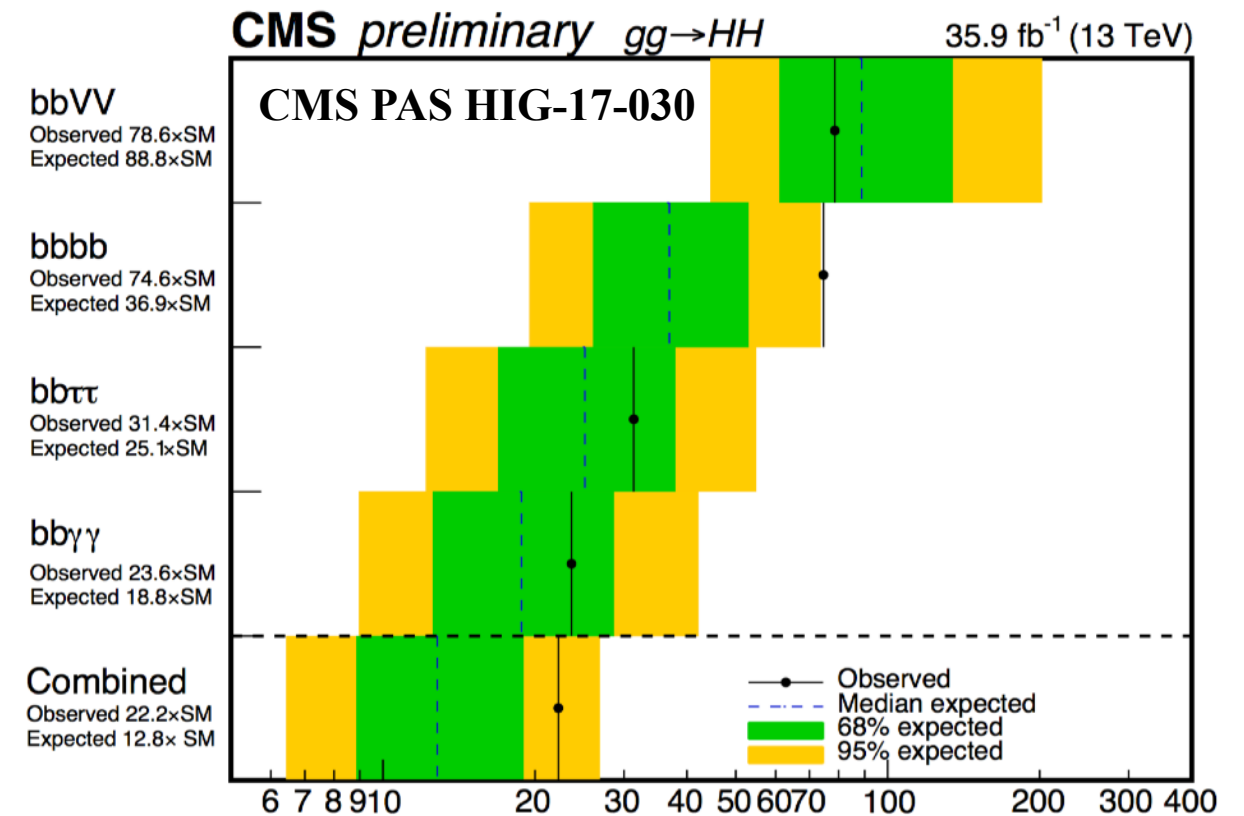


- The driven channel is the "compromised" clean channel.

LHC Run 2 result

- Current status from various channels

		$N(hh)_{SM}$	N_{BKG}	
<i>ATLAS</i>	$bb\gamma\gamma$	8.4	47.1	1.2
<i>CMS</i>	$bb\gamma\gamma$	9	26.9	1.7
	$bb\tau\tau$ (fully-hadronic)	4.9	30.3	0.89
	$bb\tau\tau$ (semi-leptonic)	6.1	122	0.55
	$bbWW^*$ (di-leptonic)	37.1	3875	0.60



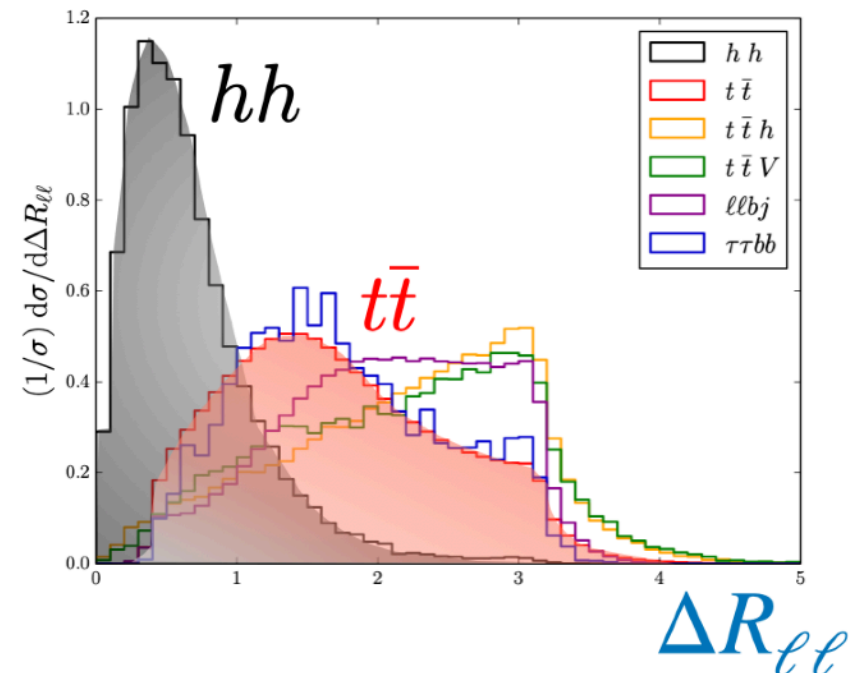
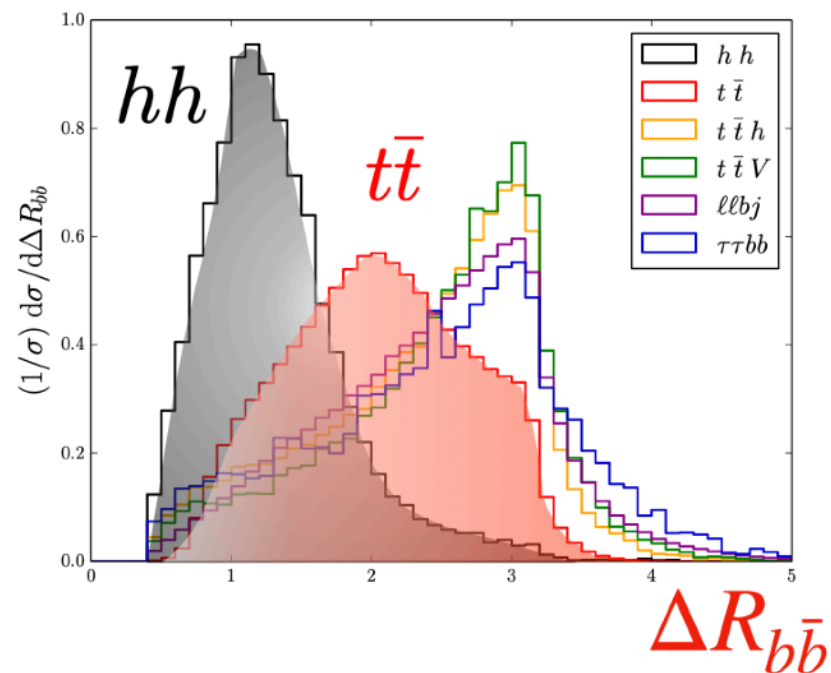
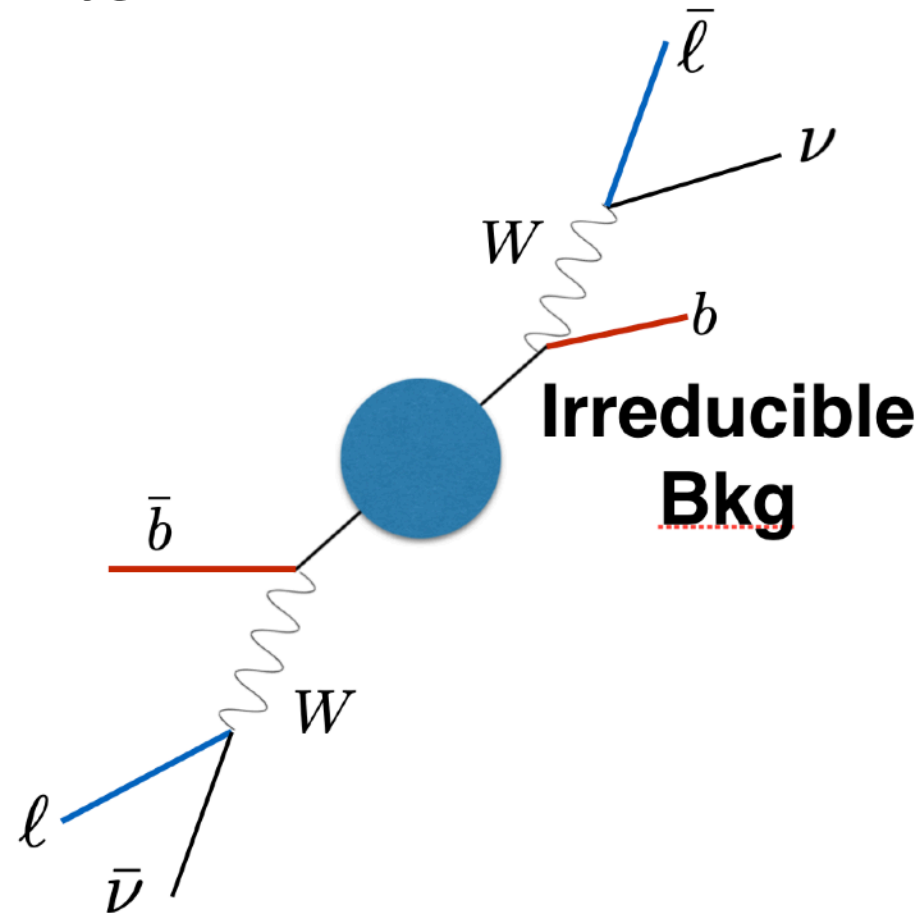
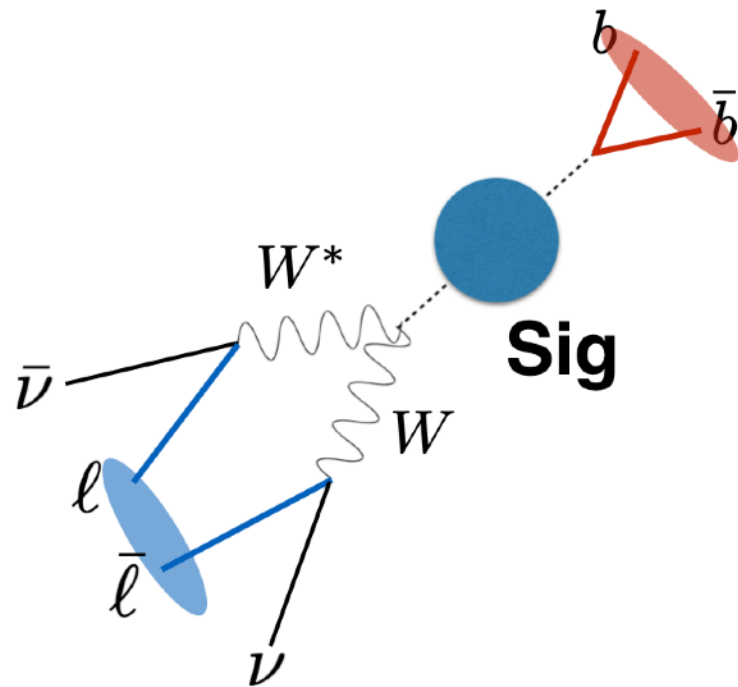
- Why** is $bbVV$ **bad** ? **how** can one **improve** ?

- **Why** is $bbVV$ **bad** ? LHC is the **Top-factory**

$$\frac{\sigma(pp \rightarrow hh \rightarrow b\bar{b} VV^*)}{\sigma(pp \rightarrow t\bar{t} \rightarrow b\bar{b} VV)} \bigg|_{13\text{TeV}} \simeq \frac{31\text{fb}*(25\%)}{215\text{pb}} \simeq \mathcal{O}(10^{-5})$$

Conventional method to design cuts

- From patterns of signal events



Applying **featured variables**

- traditional **ABCD** method



- Applying "**low-level**" kinematic cuts based on event-topology

$$\text{Baseline selections: } \cancel{E}_T > 20 \text{ GeV}, \\ p_T^\ell > 20 \text{ GeV}, \Delta R_{\ell\ell} < 1.0, m_{\ell\ell} < 65 \text{ GeV}, \\ \Delta R_{bb} < 1.3, 95 < m_{bb} < 140 \text{ GeV}$$

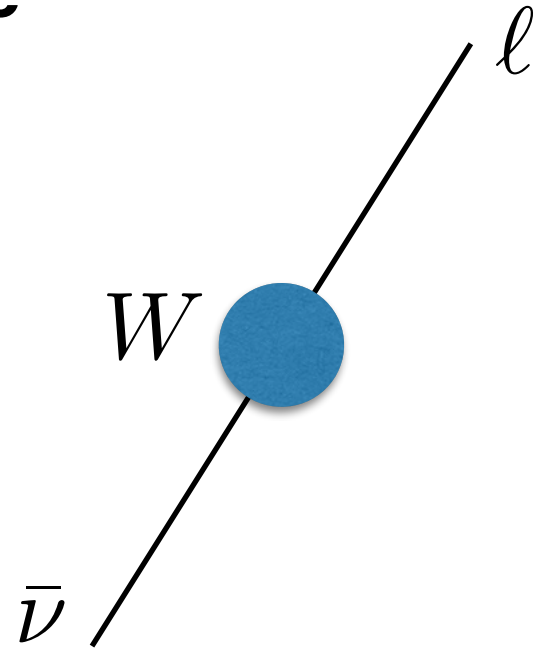
Signal	$t\bar{t}$	$t\bar{t}h$	$t\bar{t}V$	$\ell\bar{\ell}bj$	$\tau\tau bb$	others	σ	$N_{\text{sig}}^{\text{SM}}/N_{\text{bknd}}$
0.0124	1.1724	0.0297	0.0246	0.0158	0.0379	0.00590	0.60	0.00964

$jj\ell\bar{\ell}\nu\bar{\nu}$ backgrounds from QCD+EW

- We may apply the advanced statistical tools to see correlations among "low-level" kinematic variables.
- But the **efficiency based on "low-level cuts" is NOT GOOD**

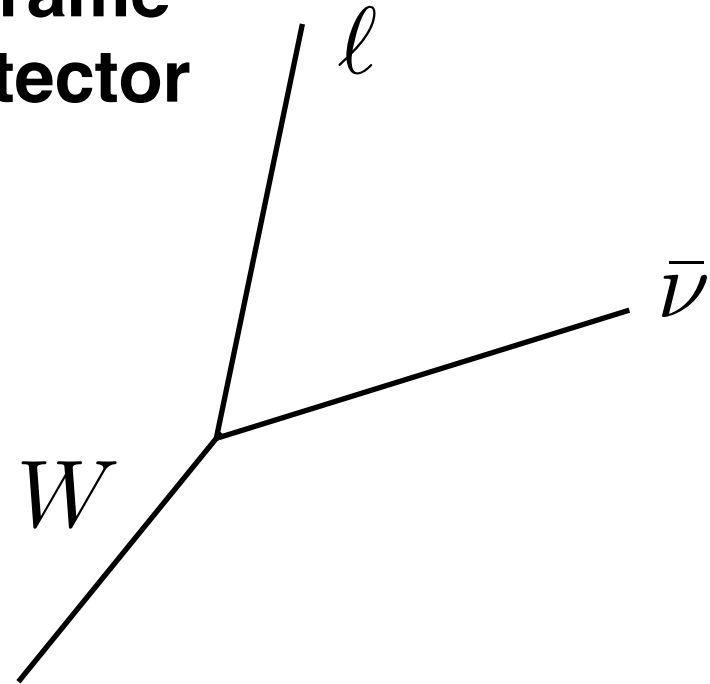
- A **low-level** variable contains various information

Rest frame
of W

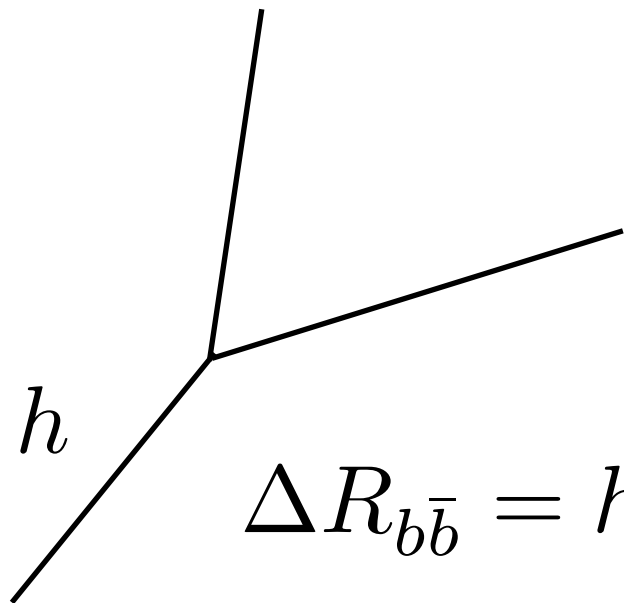


$$P_{t(\ell)} = f(M_W, M_\nu, M_\ell)$$

Lab frame
of Detector

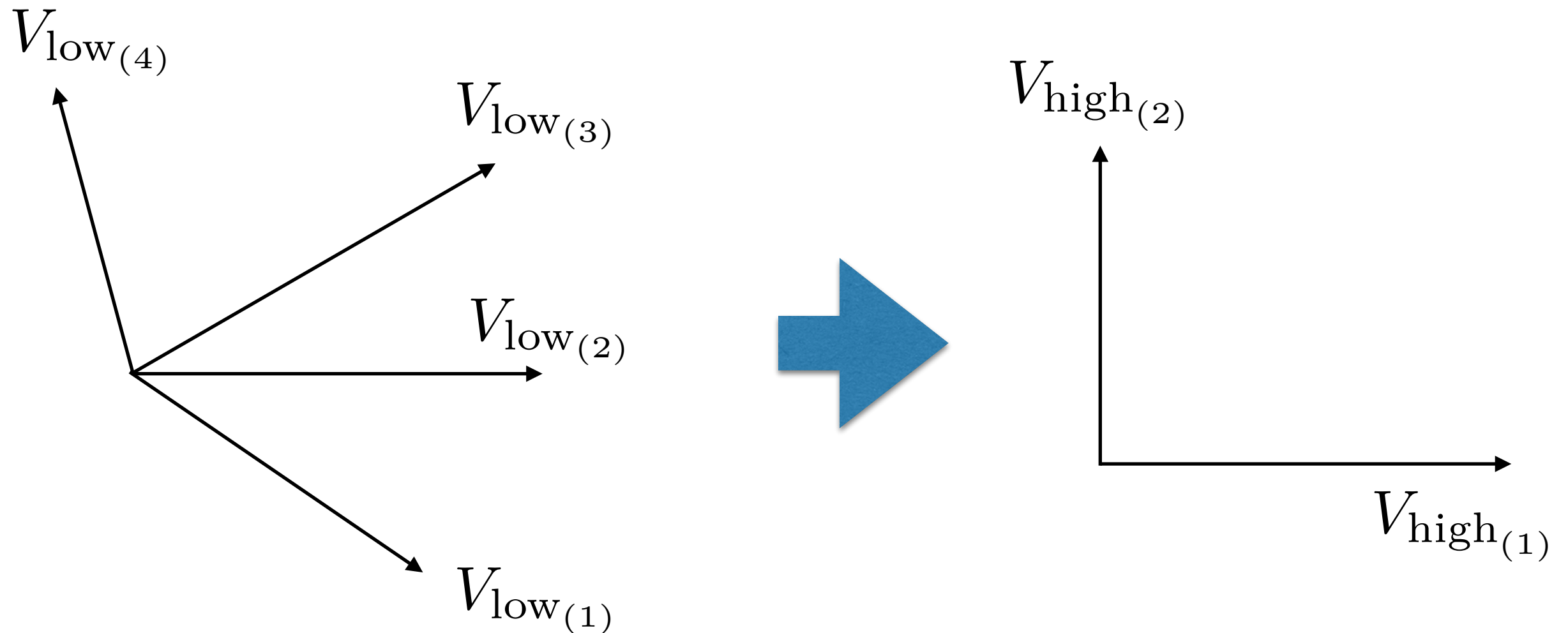


$$P_{t(\ell)} = g(M_W, M_\nu, M_\ell, \eta_W)$$



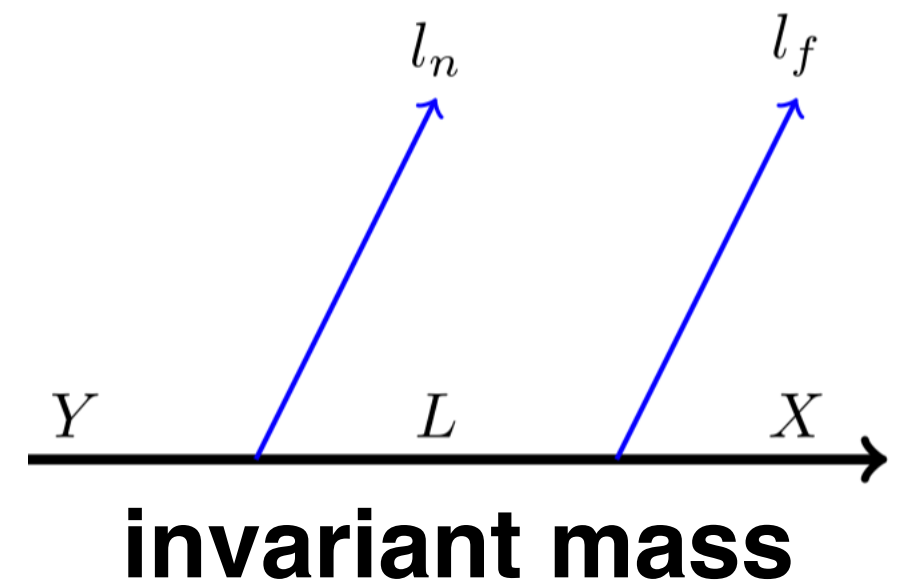
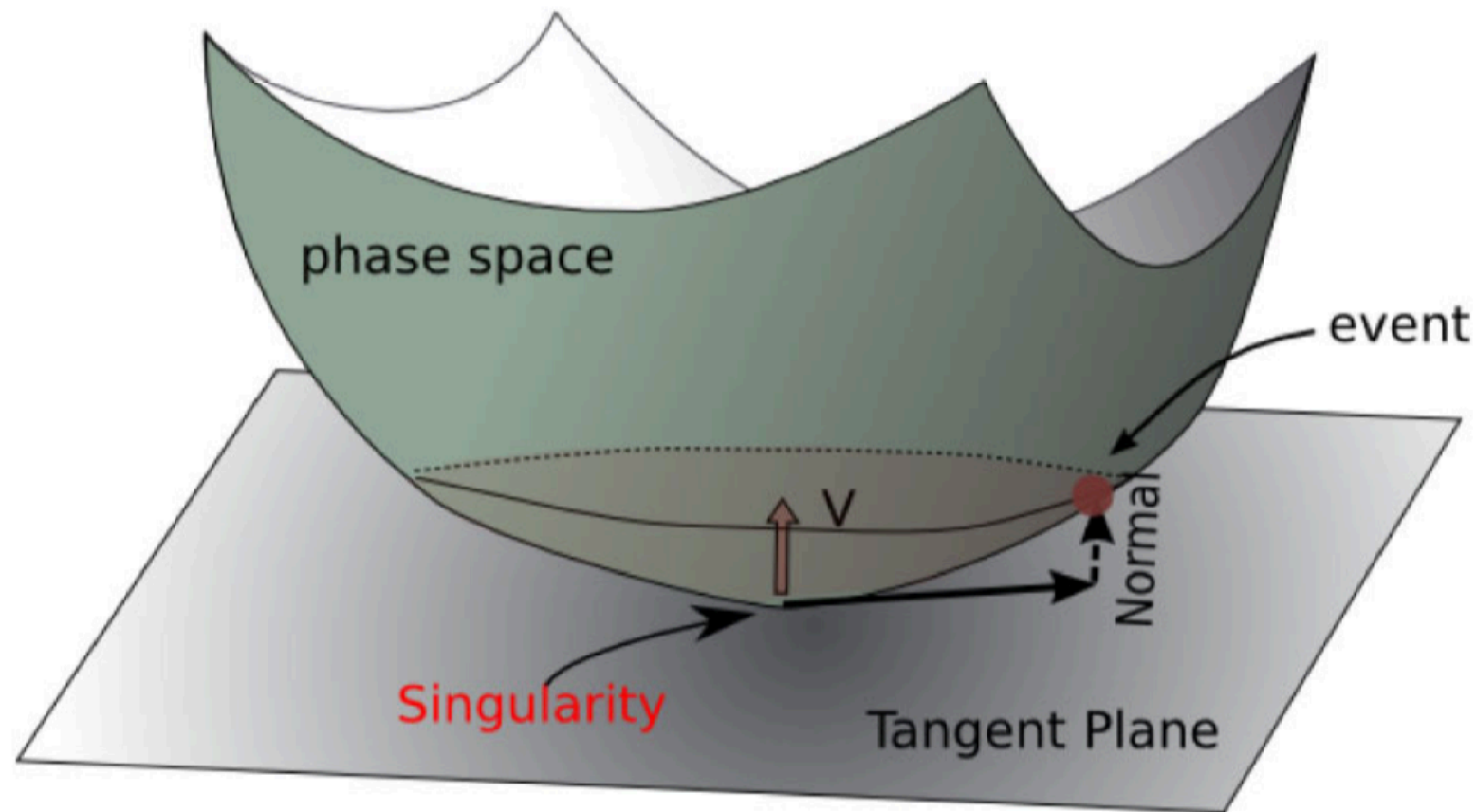
$$\Delta R_{b\bar{b}} = h(M_h, M_b, \eta_h), \quad \eta_h = h'(\sqrt{\hat{s}}, M_h)$$

- We need to "**reduce dimensions**" by finding "**mutually orthogonal variables**" to maximize sensitivity.



example of 2-dim

- Considering "**featured (high-level)**" kinematic cuts based on event-topology
- What are the "**featured**" kinematic variables?
- **Represent** Phase-space / Physics very well (**singular behavior**)



For ttbar Background: A mass variable

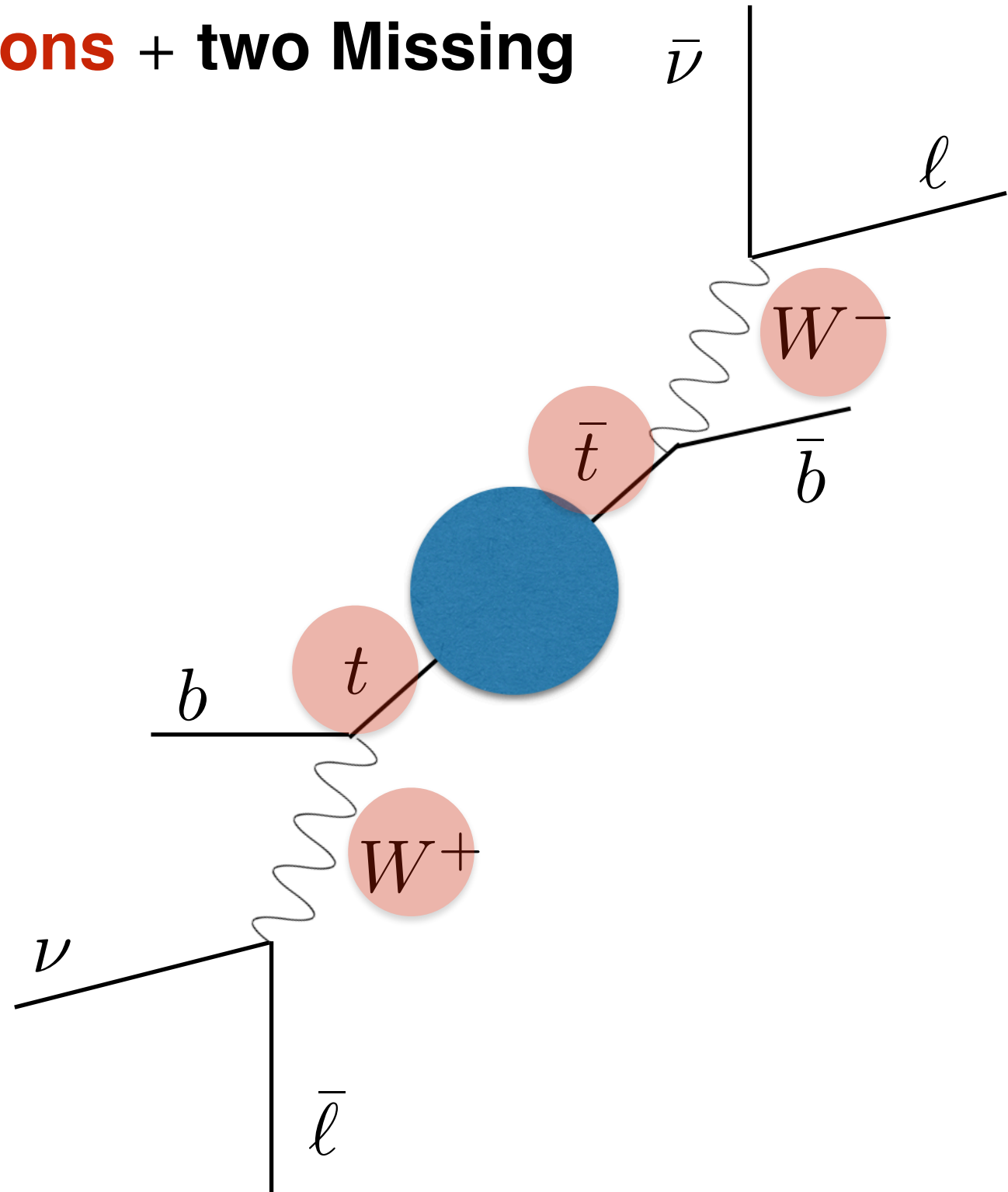
- We have **six unknowns** for two neutrino momentums.
- We have **four mass-shell conditions** + **two Missing Transverse Energy conditions**

$$(p_{\bar{\nu}} + p_{\ell})^2 = m_W^2$$

$$(p_{\bar{\nu}} + p_{\ell} + p_{\bar{b}})^2 = m_{\bar{t}}^2$$

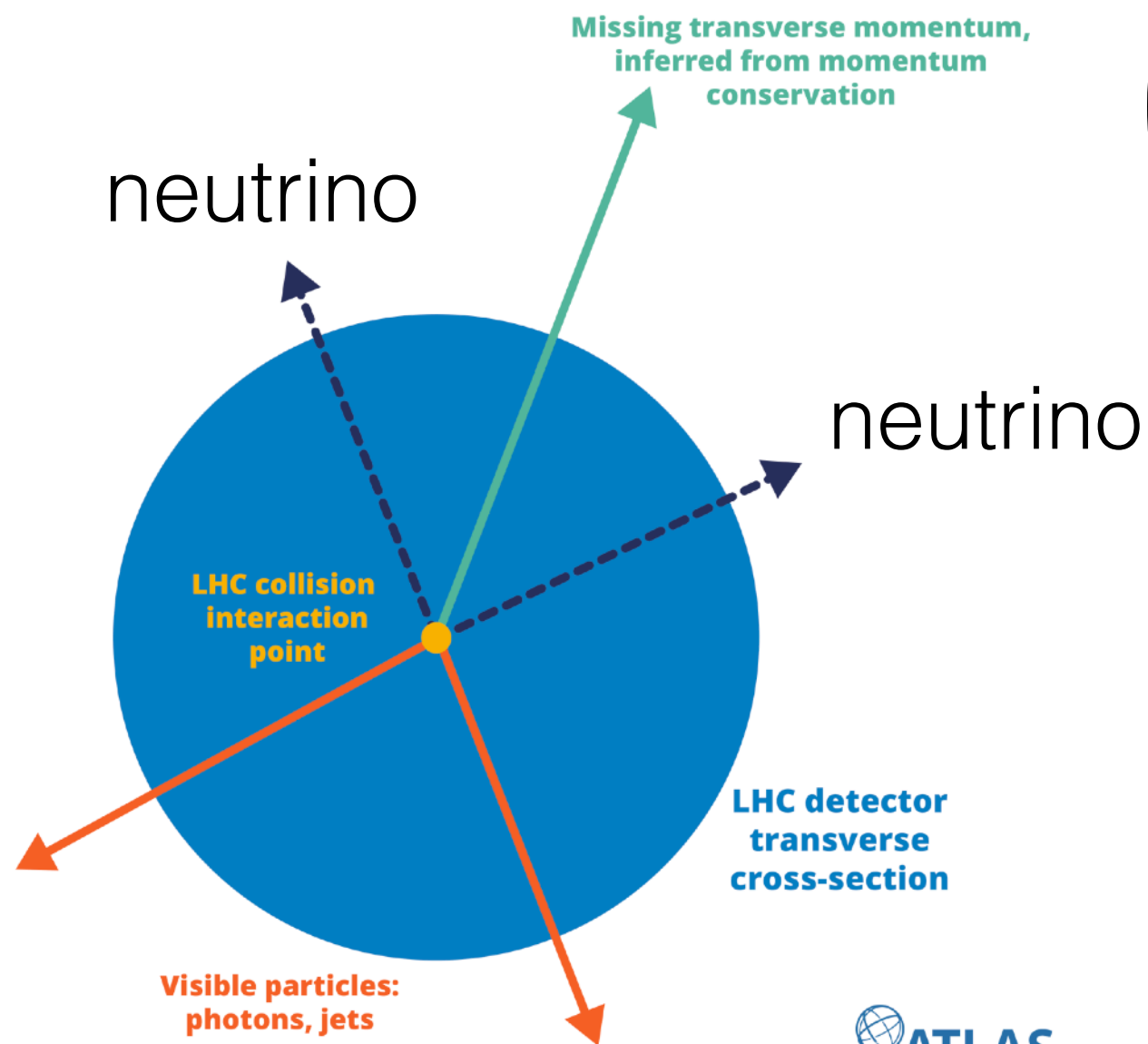
$$(p_{\nu} + p_{\bar{\ell}})^2 = m_W^2$$

$$(p_{\nu} + p_{\bar{\ell}} + p_b)^2 = m_t^2$$

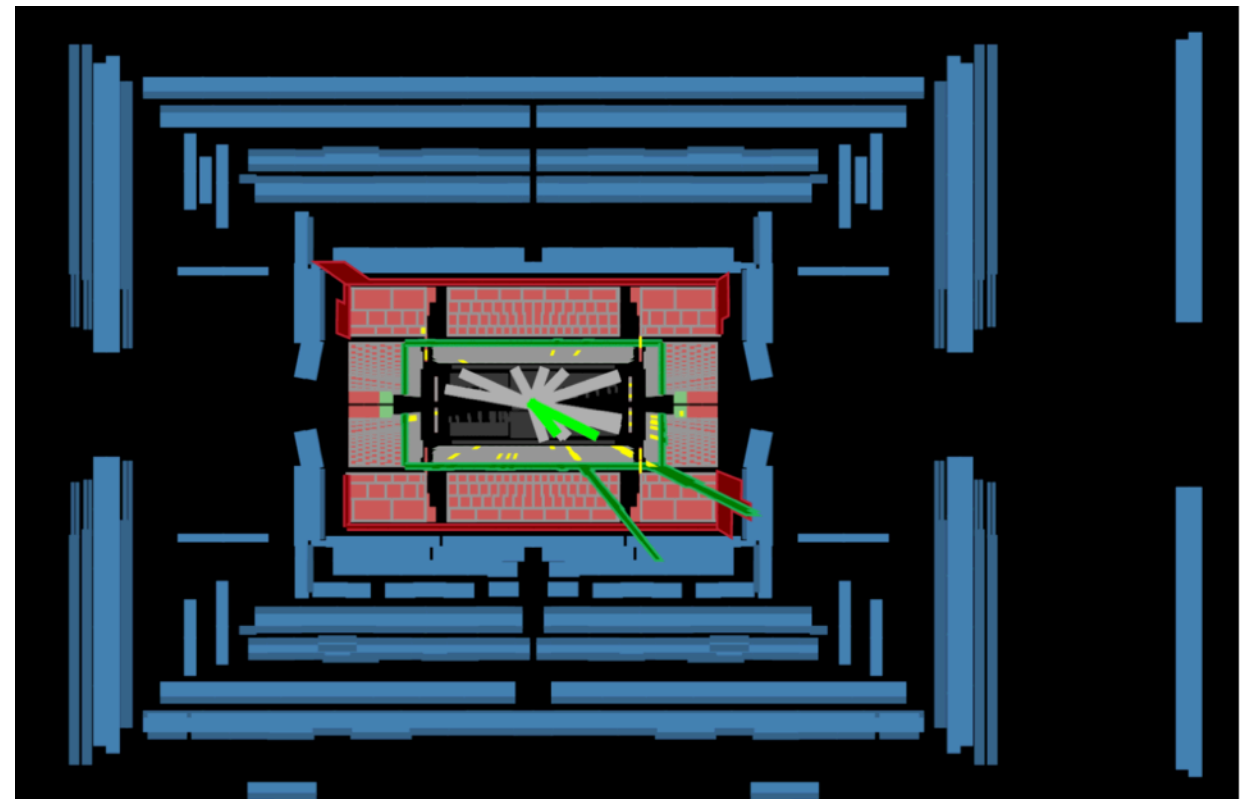


For ttbar Background: A mass variable

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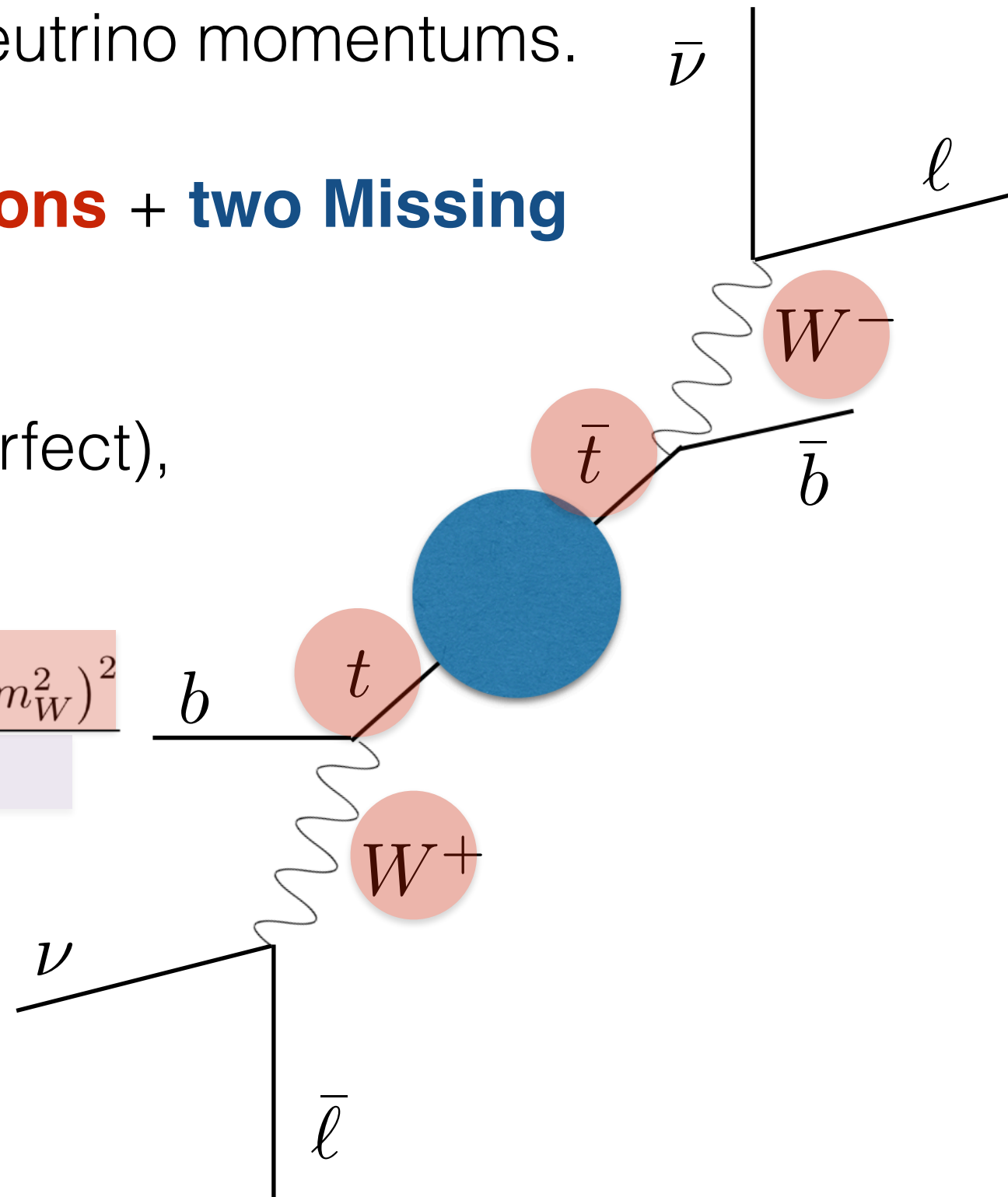
$$\left(\sum_{\text{visible particles}} \vec{P}_T \right) + \left(\sum_{\text{neutrinos}} \vec{P}_T \right) = 0$$



For ttbar Background: A mass variable

- We have **six unknowns** for two neutrino momenta.
- We have **four mass-shell conditions** + **two Missing Transverse Energy conditions**
- In a reality (as a detector is not perfect), we allow some "**smearing**" effects

$$\chi_{ij}^2 \equiv \min_{\vec{p}_T = \vec{p}_{\nu T} + \vec{p}_{\bar{\nu} T}} \left[\frac{(m_{b_i \ell + \nu}^2 - m_t^2)^2}{\sigma_t^4} + \frac{(m_{\ell + \nu}^2 - m_W^2)^2}{\sigma_W^4} + \frac{(m_{b_j \ell - \bar{\nu}}^2 - m_t^2)^2}{\sigma_t^4} + \frac{(m_{\ell - \bar{\nu}}^2 - m_W^2)^2}{\sigma_W^4} \right]$$



Small χ_{ij} (Top-ness) = compatible with a ttbar event topology

For HH signal events: Utilizing Mass information

- We have **six unknowns** for two neutrino momentums.
- We have **two mass-shell conditions** + **two "mass" constraints** + **two Missing Transverse Energy conditions**

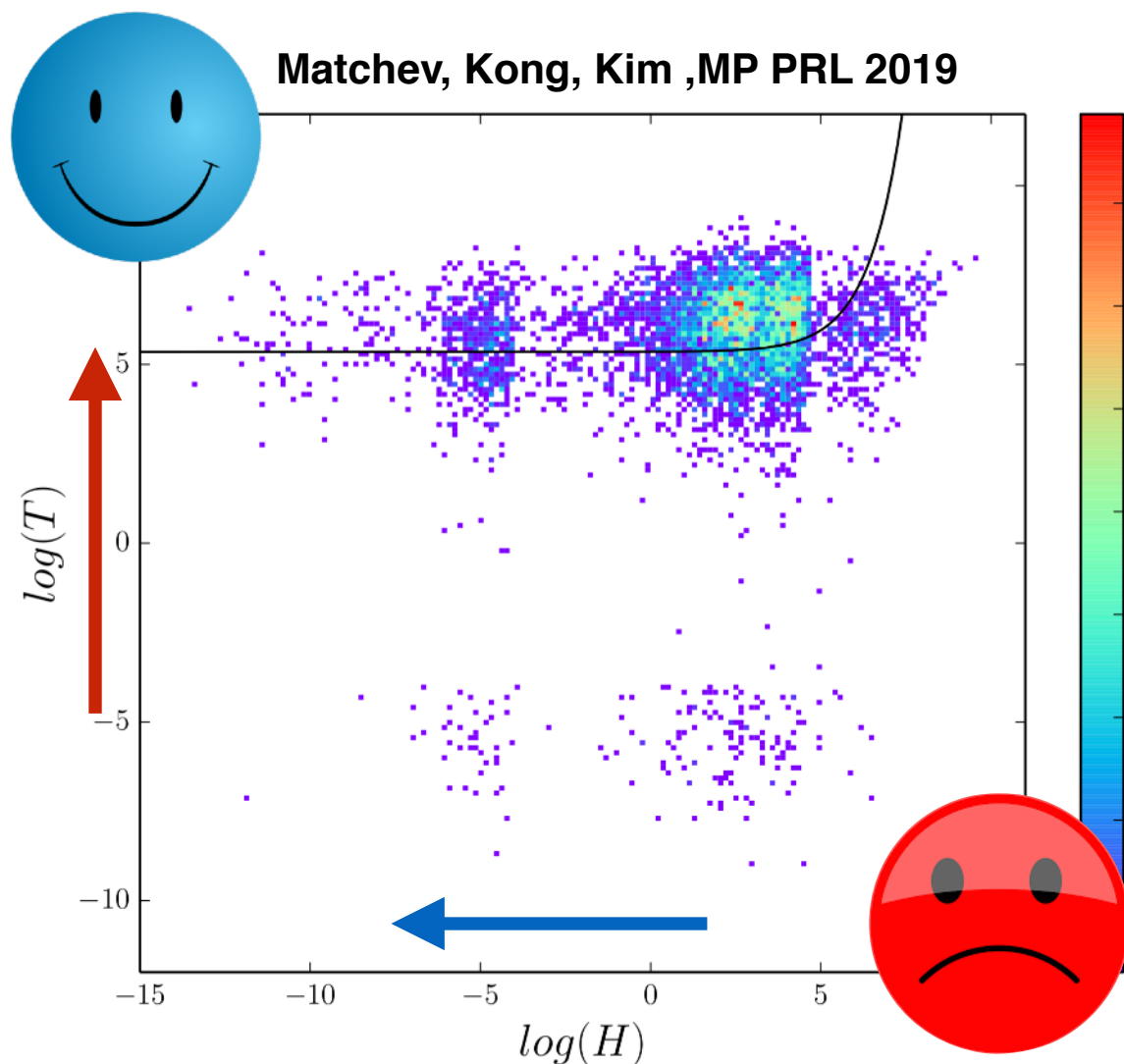
$$\begin{aligned}
 H \equiv \min & \left[\frac{(m_{\ell^+\ell^-\nu\bar{\nu}}^2 - m_h^2)^2}{\sigma_{h_\ell}^4} + \frac{(m_{\nu\bar{\nu}}^2 - m_{\nu\bar{\nu},peak}^2)^2}{\sigma_\nu^4} \right. \\
 & + \min \left(\frac{(m_{\ell^+\nu}^2 - m_W^2)^2}{\sigma_W^4} + \frac{(m_{\ell^-\bar{\nu}}^2 - m_{W^*,peak}^2)^2}{\sigma_{W^*}^4} \right. \\
 & \left. \left. \frac{(m_{\ell^-\bar{\nu}}^2 - m_W^2)^2}{\sigma_W^4} + \frac{(m_{\ell^+\nu}^2 - m_{W^*,peak}^2)^2}{\sigma_{W^*}^4} \right) \right]
 \end{aligned}$$

Small H (Higgs-ness) = compatible with a **Higgs event topology**

HH

Small H (Higgs-ness)
compatible with a **Higgs-topology**

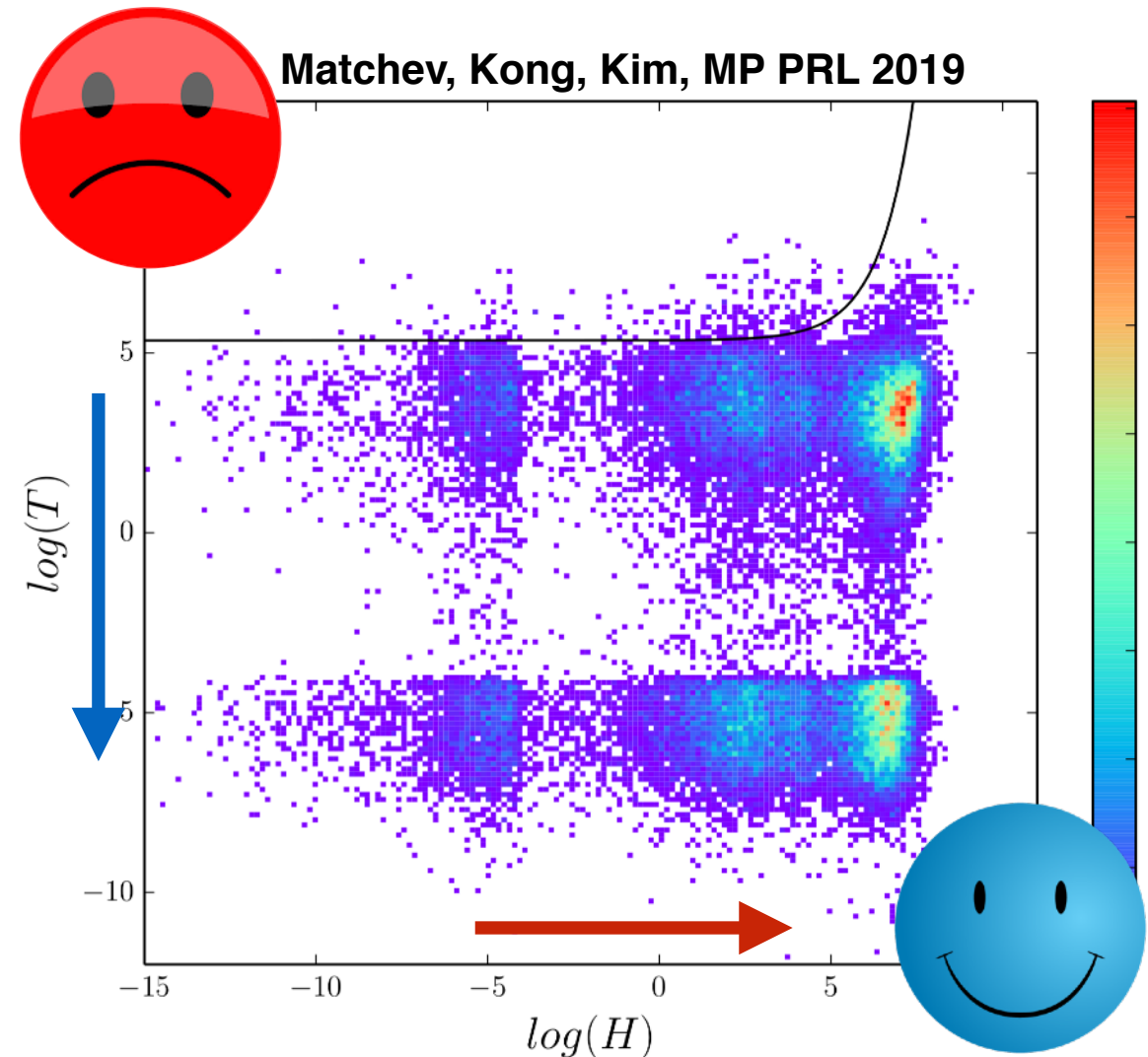
Large χ_{ij} (Top-ness)
NOT compatible with a $t\bar{t}$ -topology



$t\bar{t}$

Large H (Higgs-ness)
NOT compatible with a **Higgs-topology**

Small χ_{ij} (Top-ness)
compatible with a $t\bar{t}$ -topology

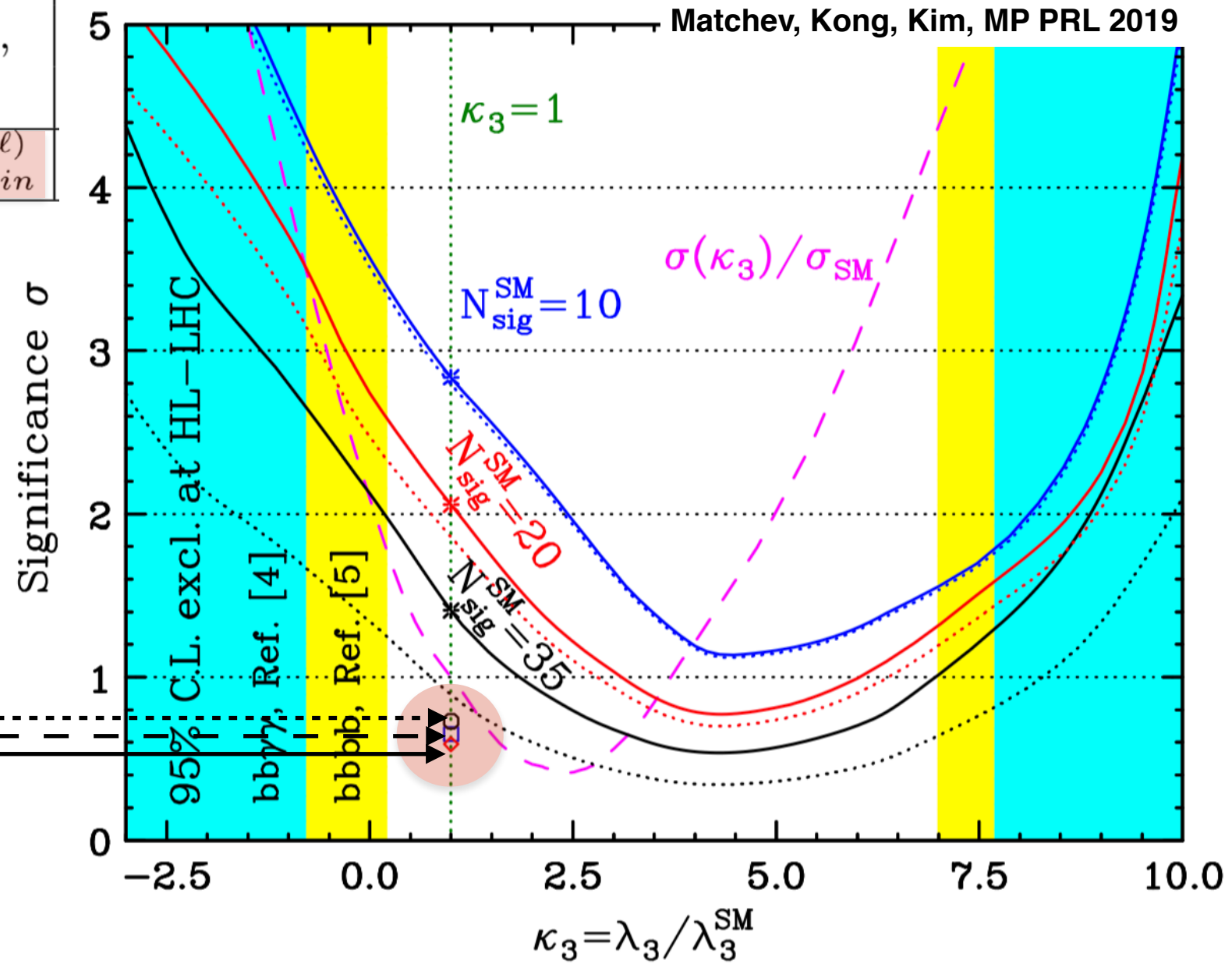


Baseline selections: $\cancel{E}_T > 20$ GeV,
 $p_T^\ell > 20$ GeV, $\Delta R_{\ell\ell} < 1.0$, $m_{\ell\ell} < 65$ GeV,
 $\Delta R_{bb} < 1.3$, $95 < m_{bb} < 140$ GeV

Higgsness \oplus Topness $\oplus M_{T2}^{(b)} \oplus M_{T2}^{(\ell)} \oplus \sqrt{\hat{s}_{min}^{(\ell\ell)}}$



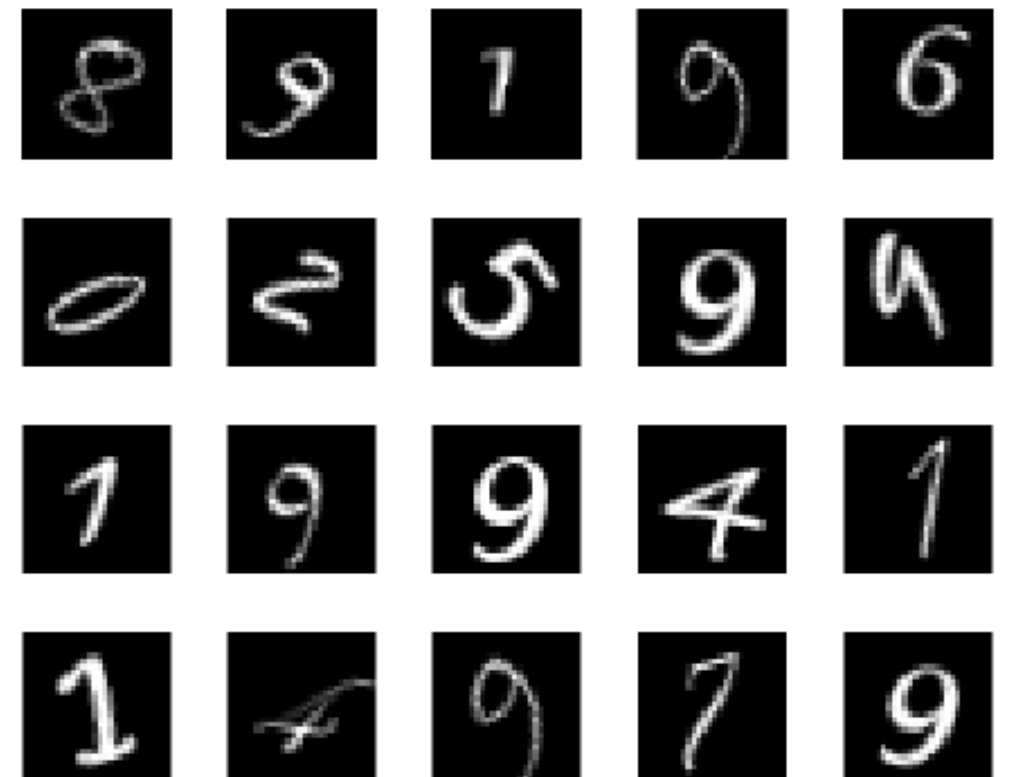
**Orthogonal / singular
variables**



- CMS-PAS-FTR-15-002, Neural Network (NN) with $(p_T, \eta, M_{l\bar{l}}, M_{b\bar{b}}, \Delta R_{l\bar{l}}, \Delta R_{b\bar{b}}, \Delta\phi_{b\bar{b}, l\bar{l}})$
- CMS-PAS-HIG-16-024, BDT based on $(M_{l\bar{l}}, \Delta R_{l\bar{l}}, \Delta R_{jj}, \Delta\phi_{l\bar{l}, jj}, p_T^{l\bar{l}}, p_T^{jj}, \min(\Delta R_{j,l}), M_T)$
- A. Adhikary et.al (1712.05346), BDT based on $(p_T^l, M_{ll}, M_{bb}, \Delta R_{ll}, \Delta R_{bb}, p_T^{bb}, p_T^{ll}, MET)$

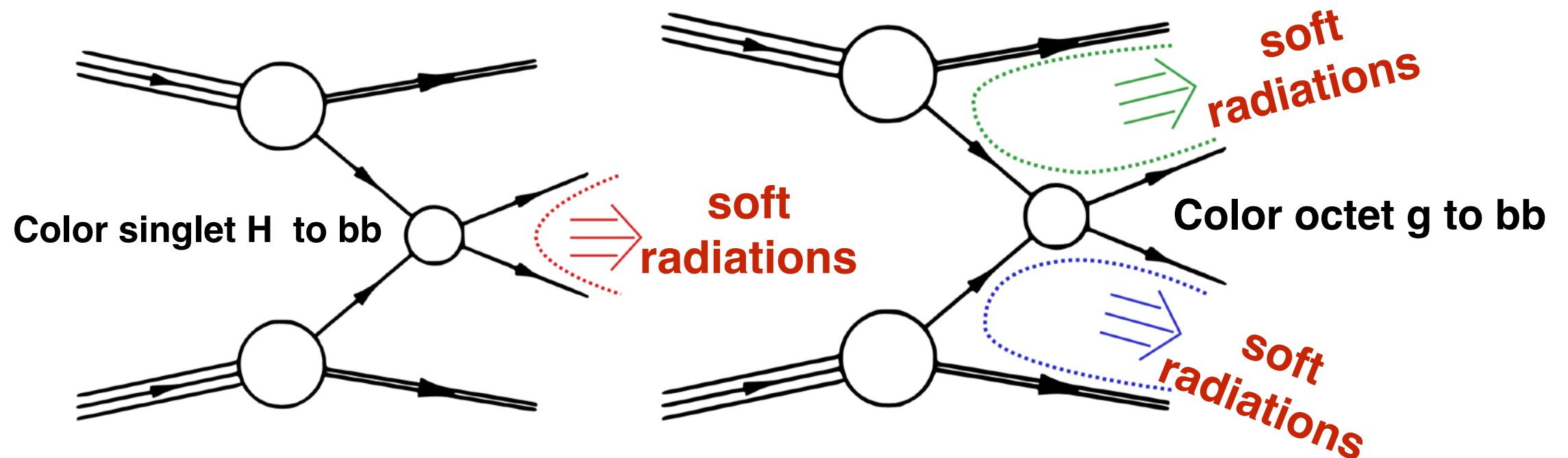
- Mathematically well-designed "feature" variables are very strong even in a ABCD (old) way.
- We can utilize Deep Learning (DL) to maximize correlations among feature variables.

- We can apply DL to utilize "energy deposit patterns" directly
(Pattern recognition in images)



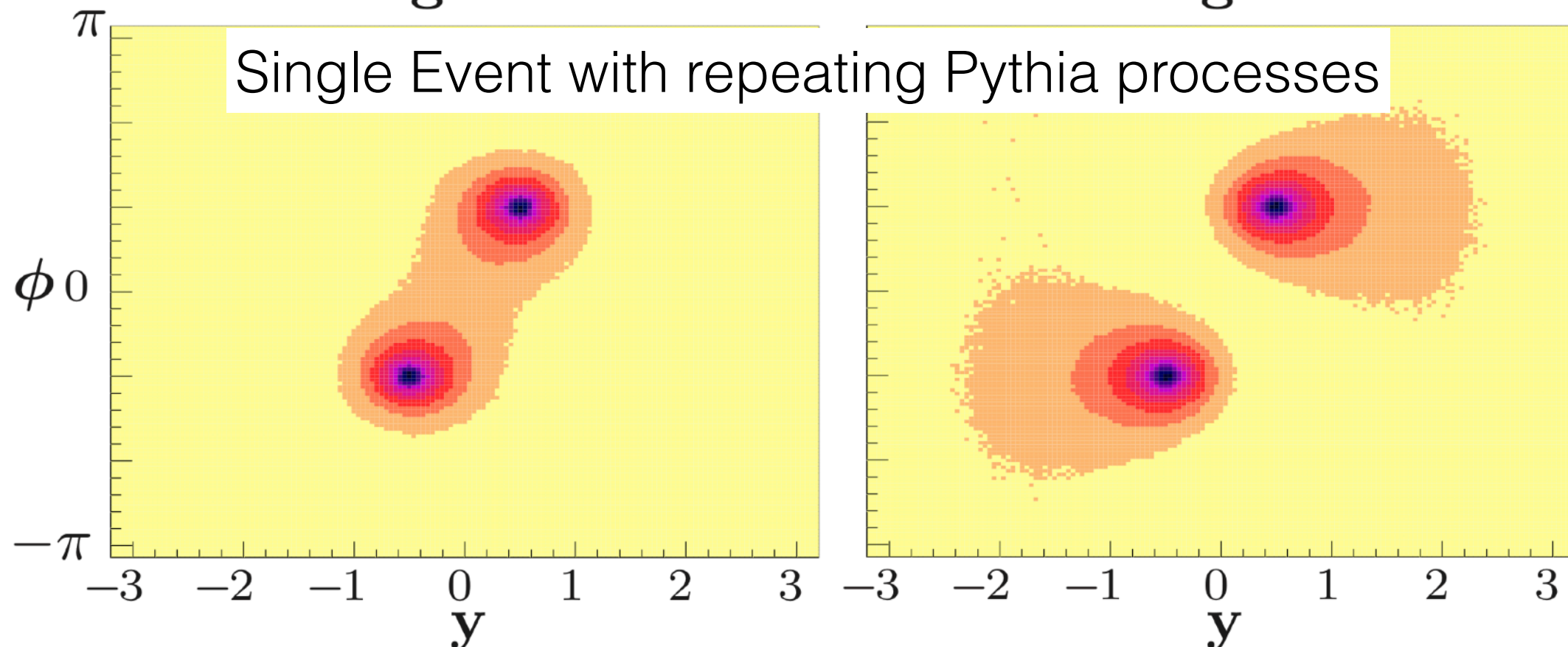
- Consider "**orthogonal**" method to kinematics; **Color-flow**

Jason Gallicchio, Matthew D. Schwartz, PRL 105:022001, 2010

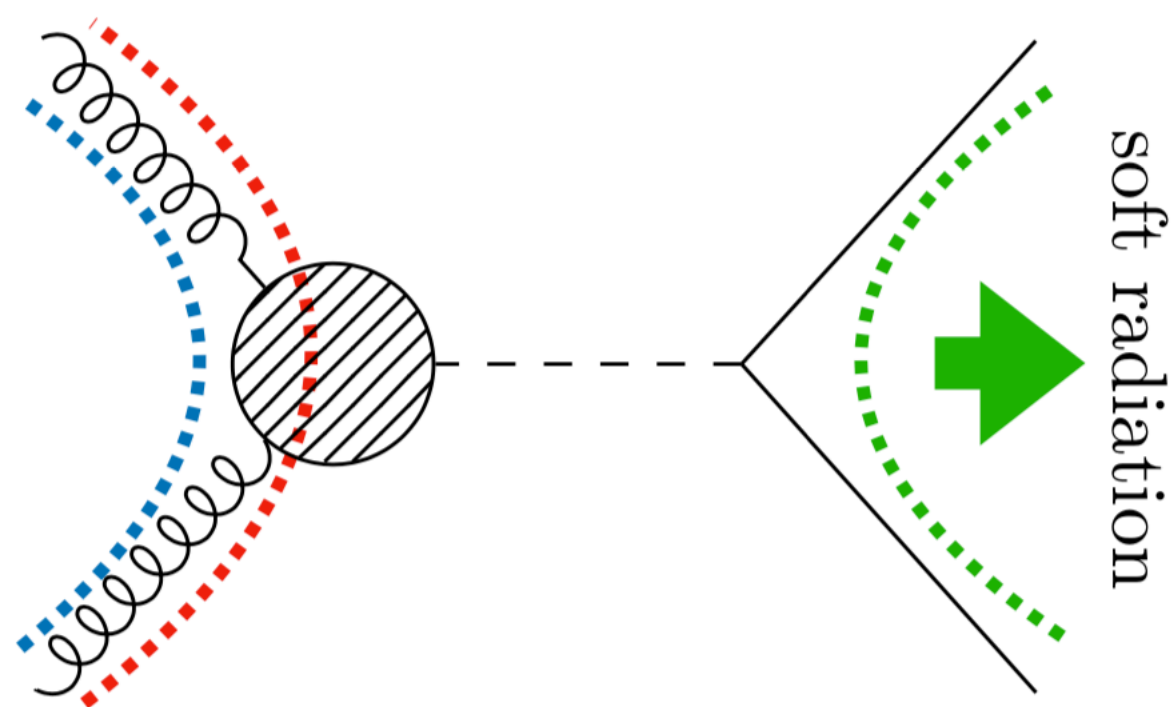


Signal

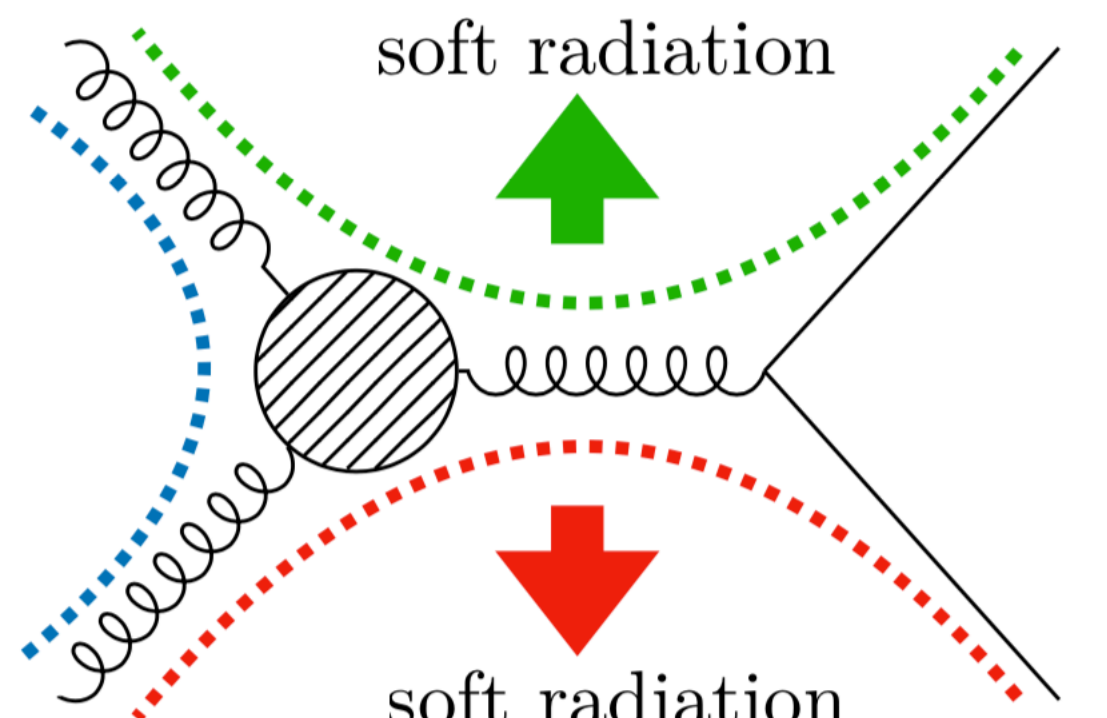
Background



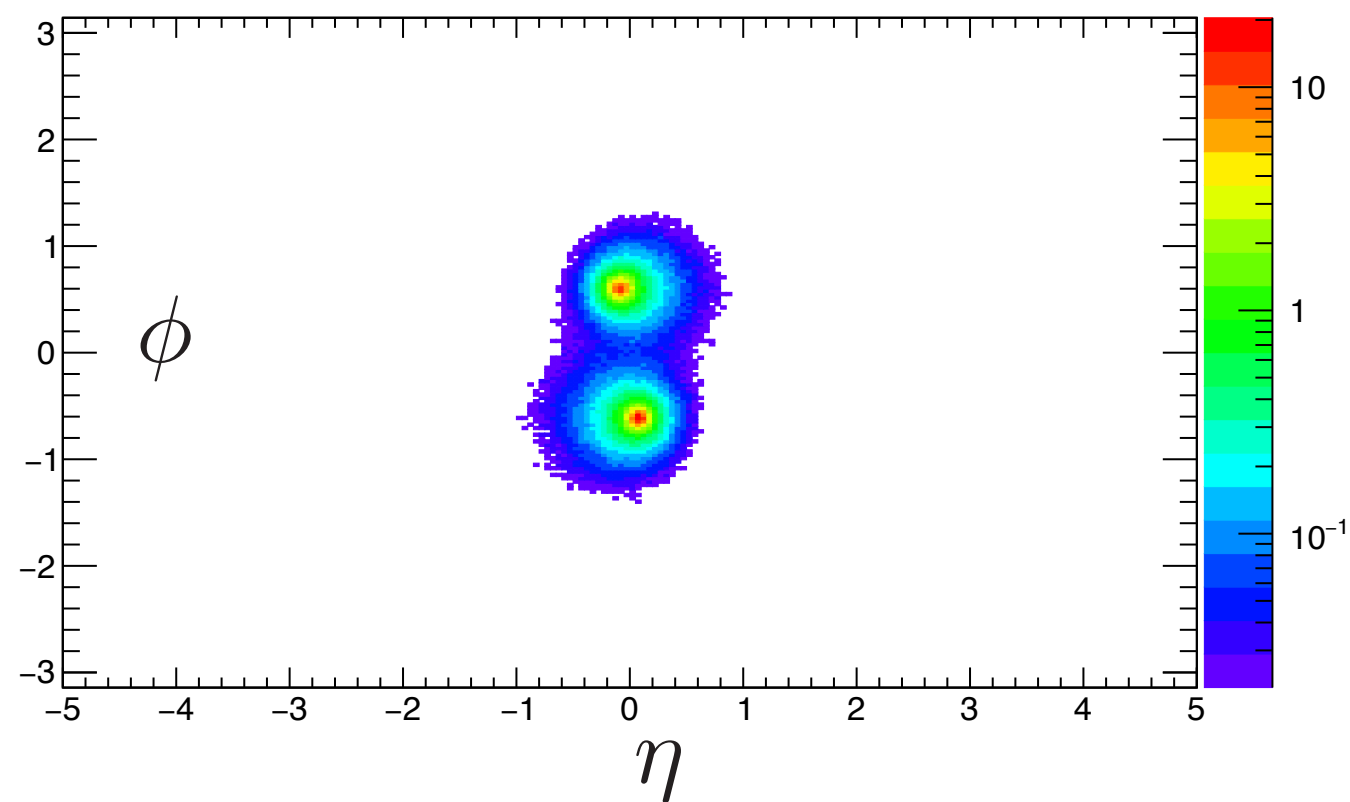
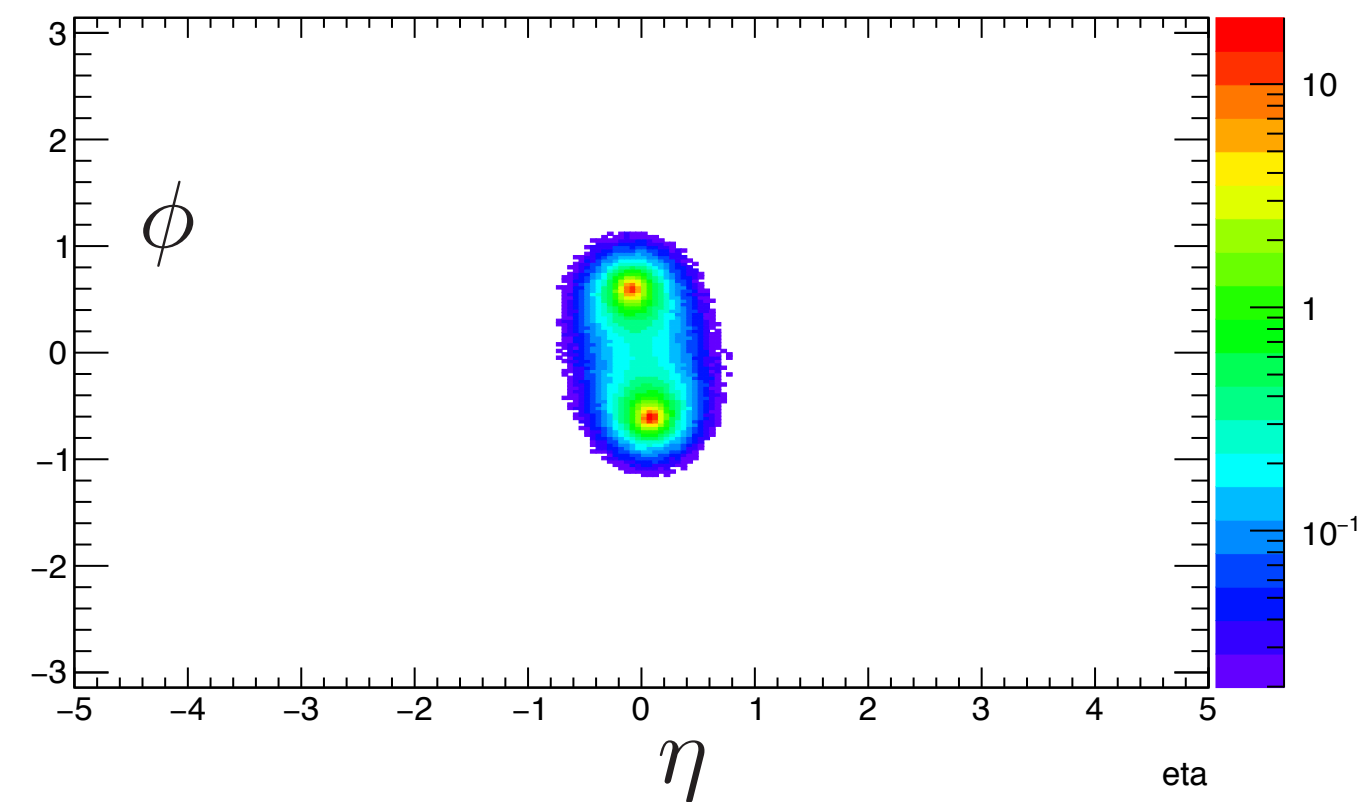
- Consider "**orthogonal**" method to kinematics; **QCD Color-flow**



p_T

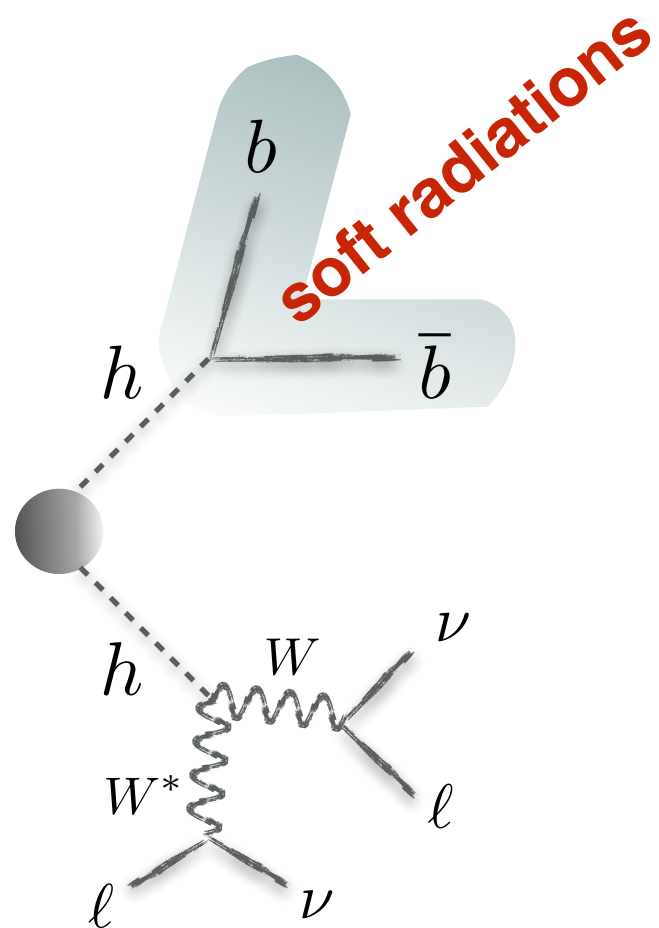


p_T

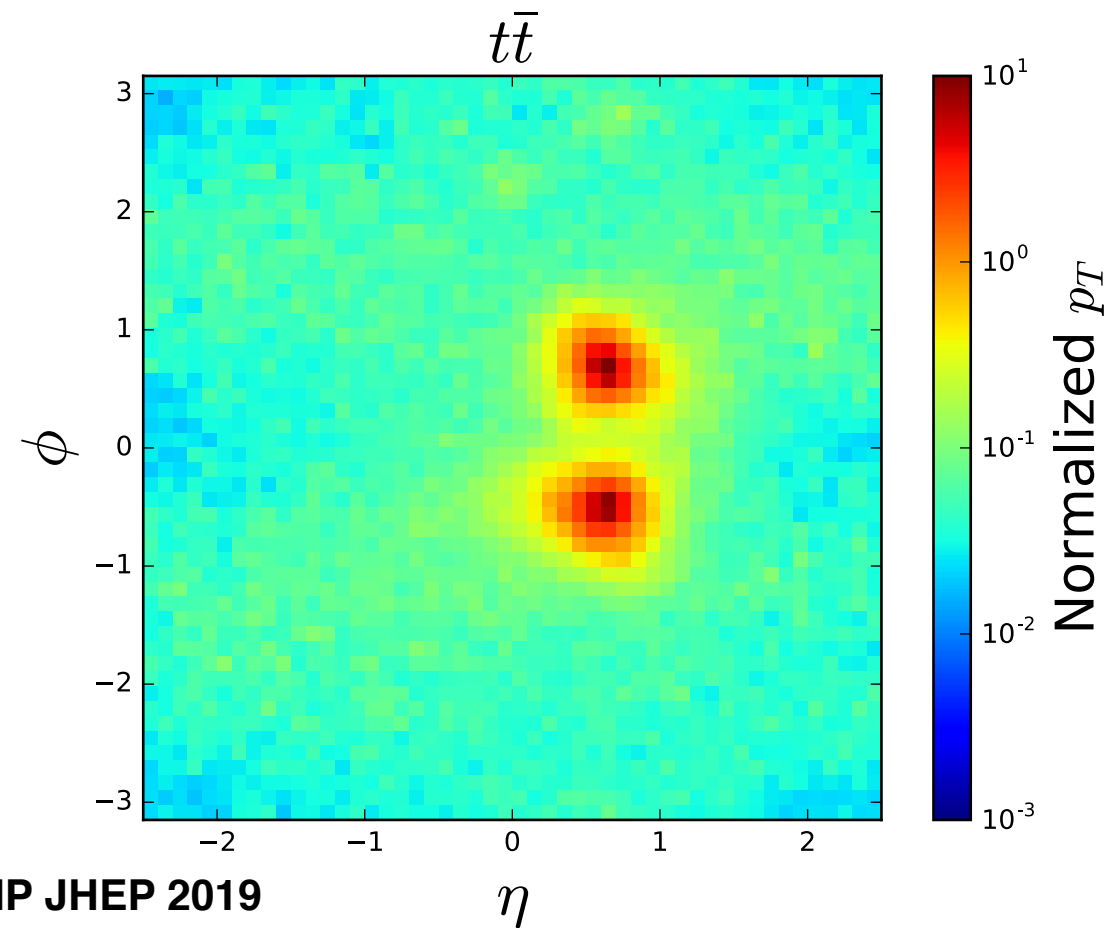
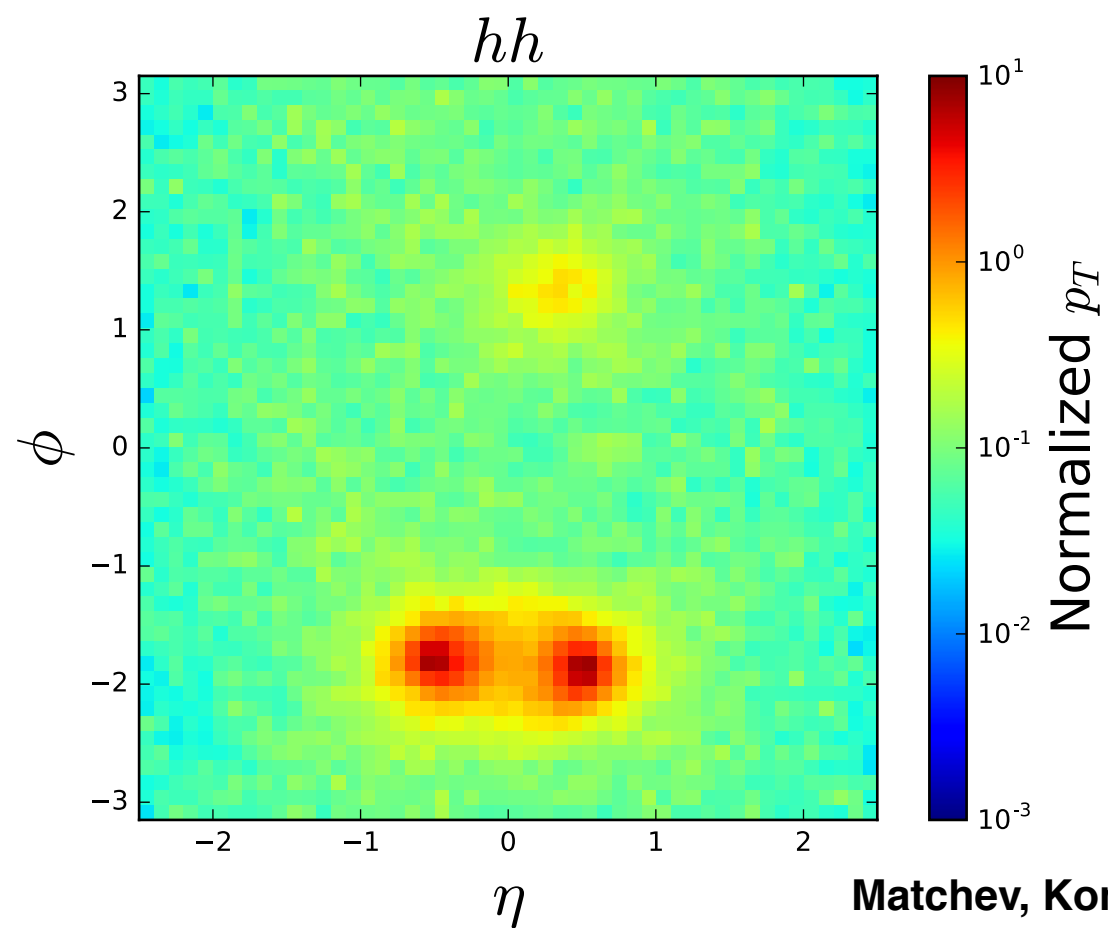
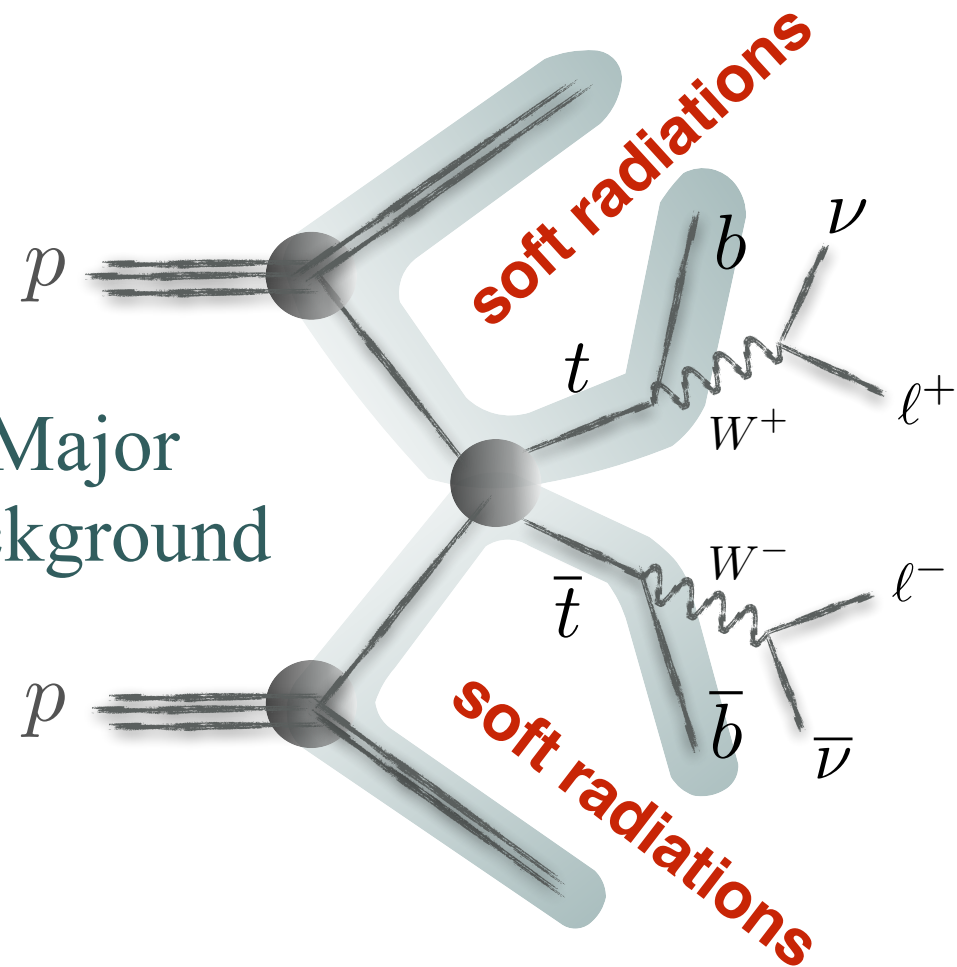


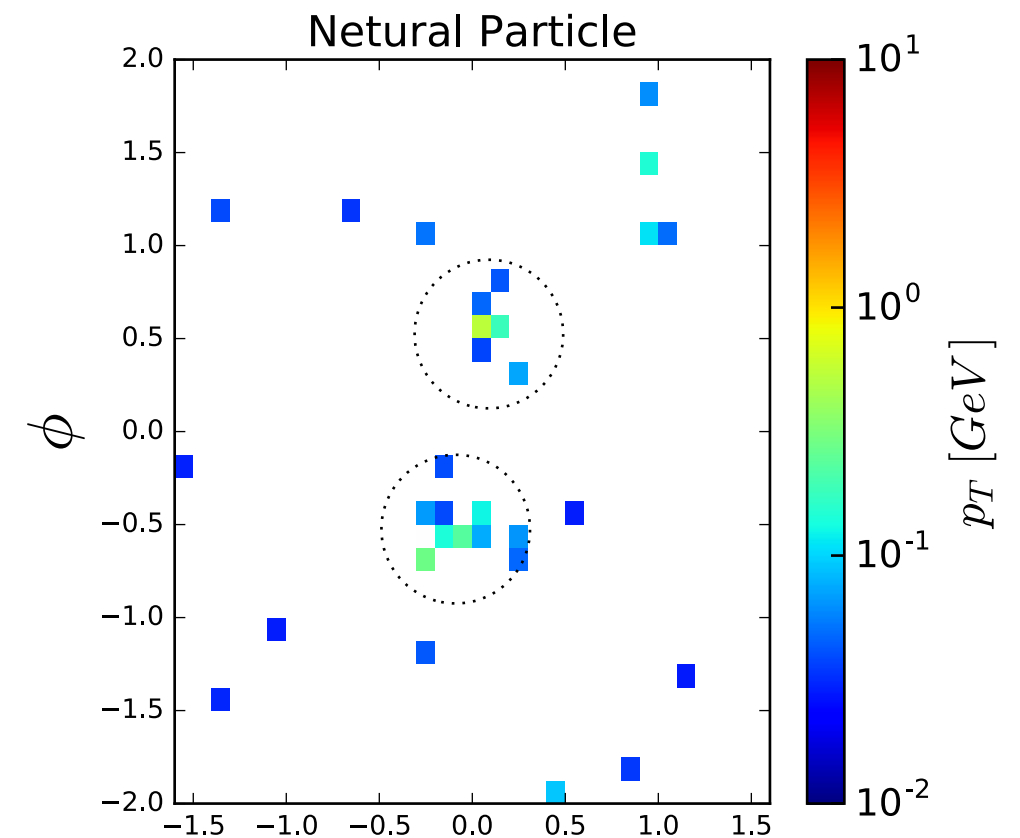
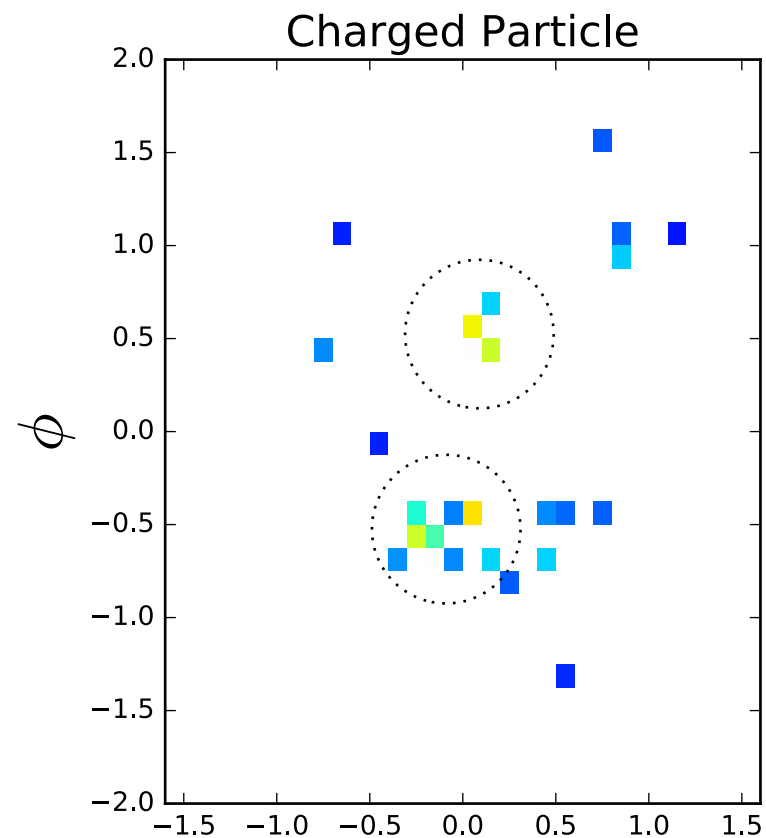
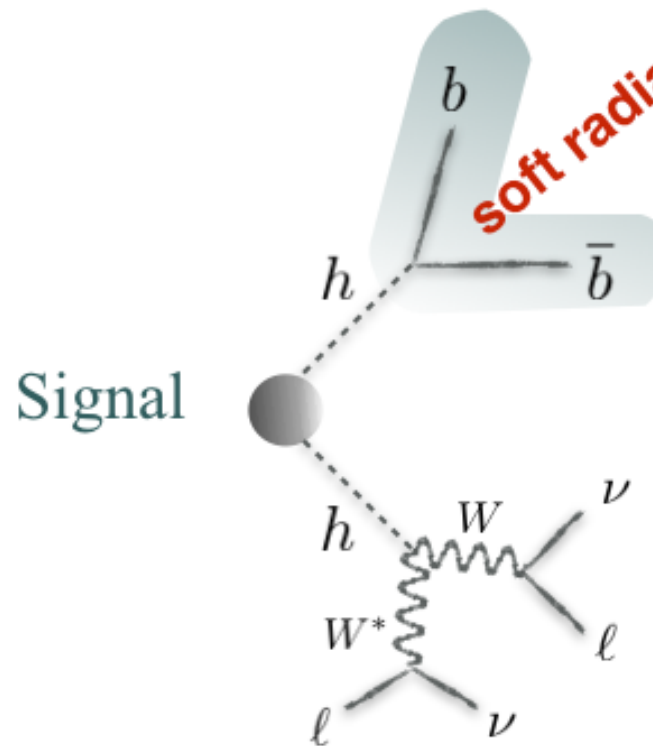
Energy deposits

Signal

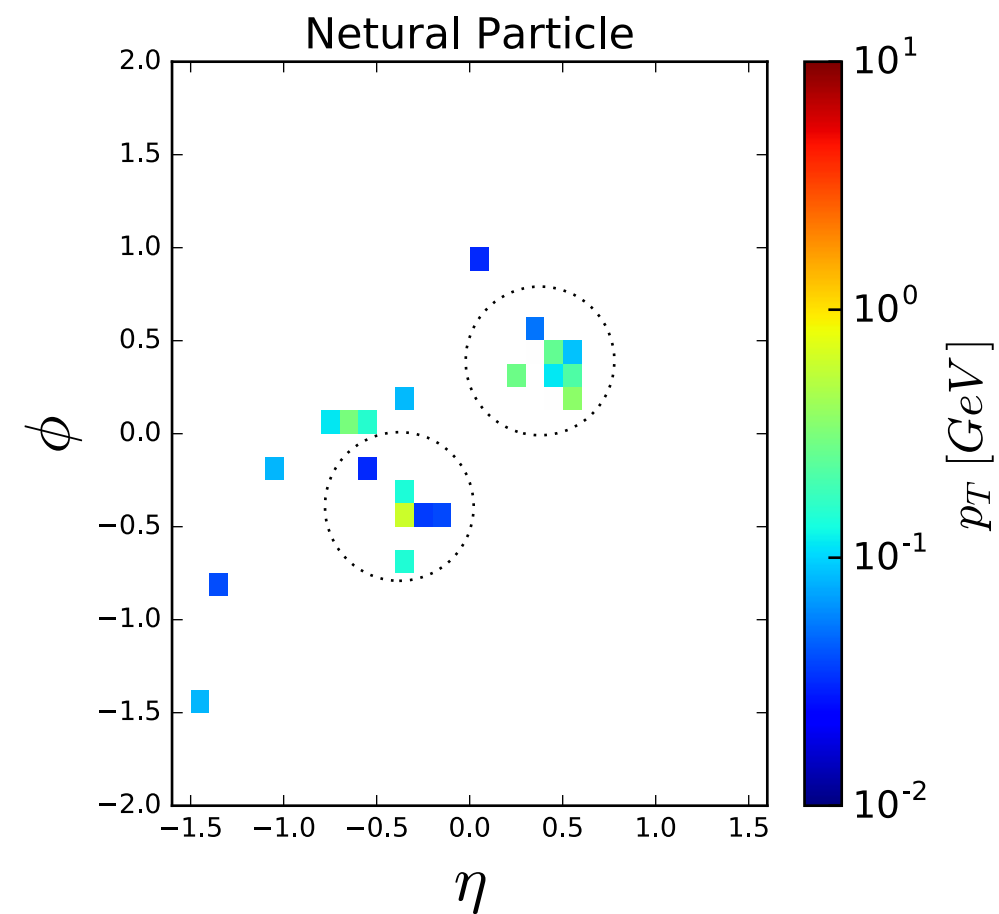
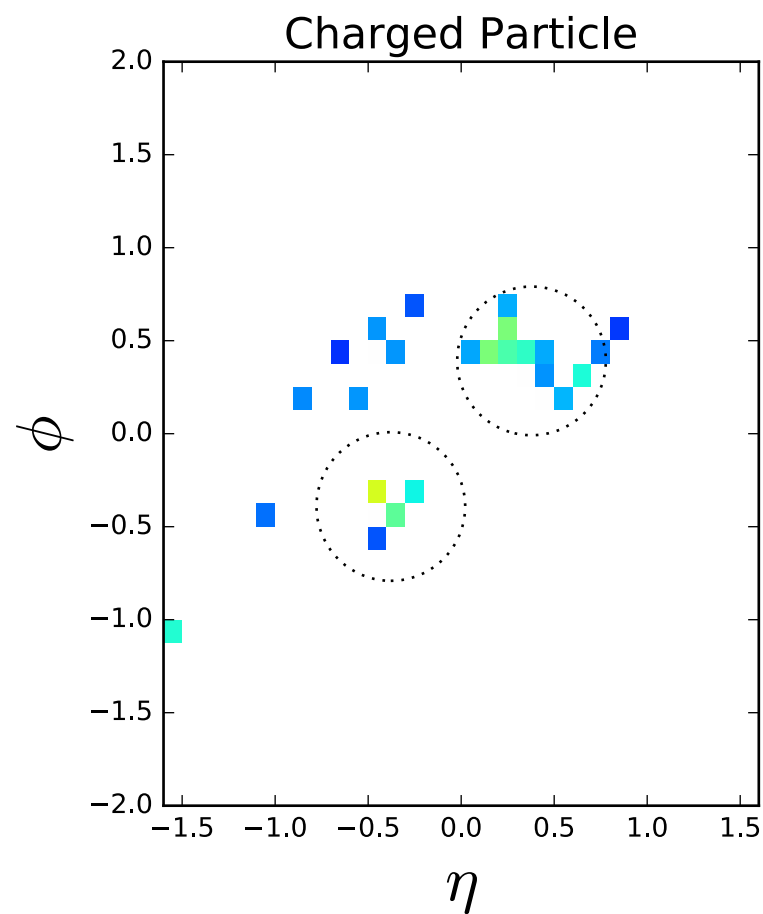
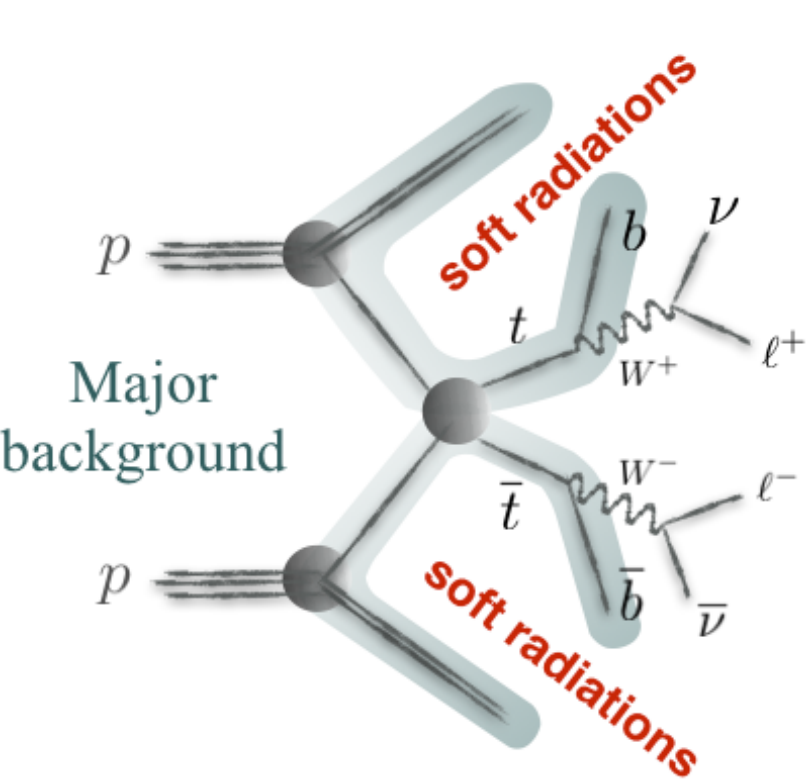


Major background





Not easy to determine event by event basis

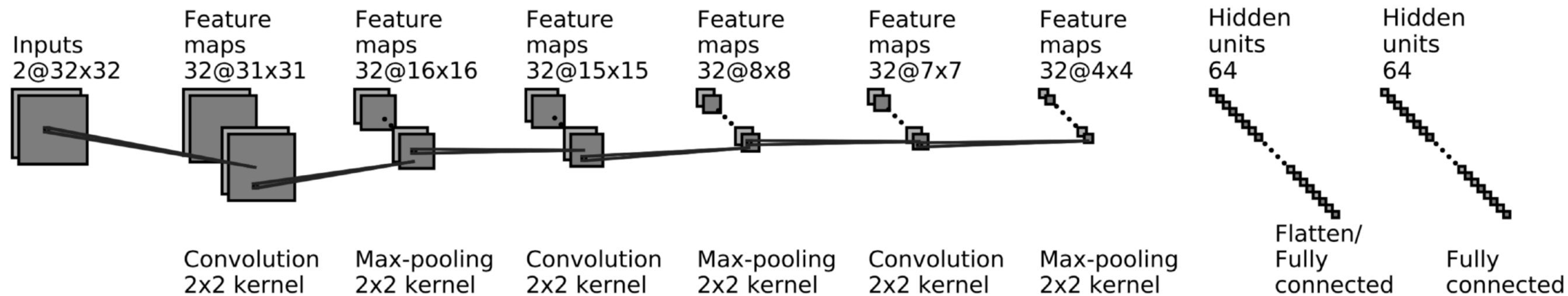


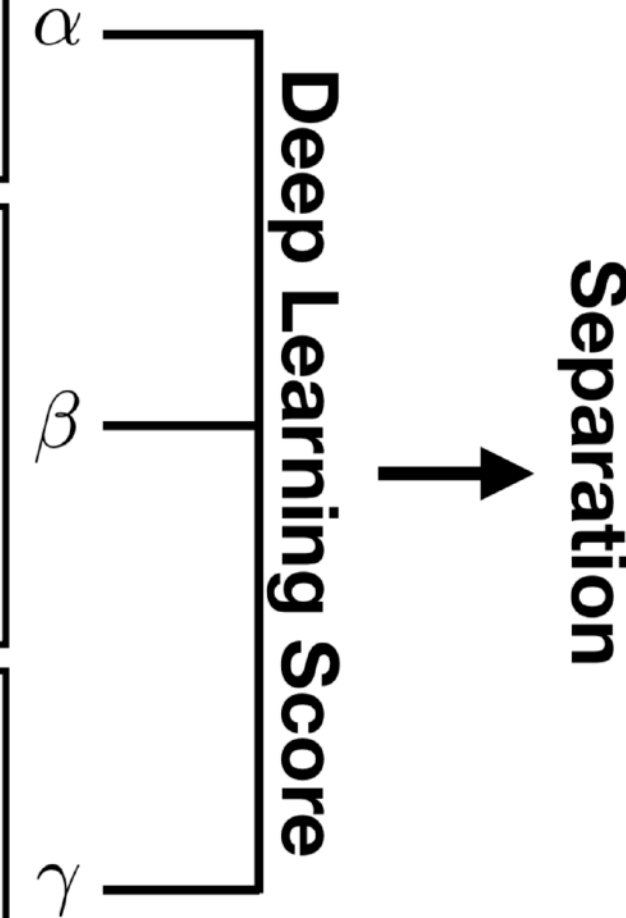
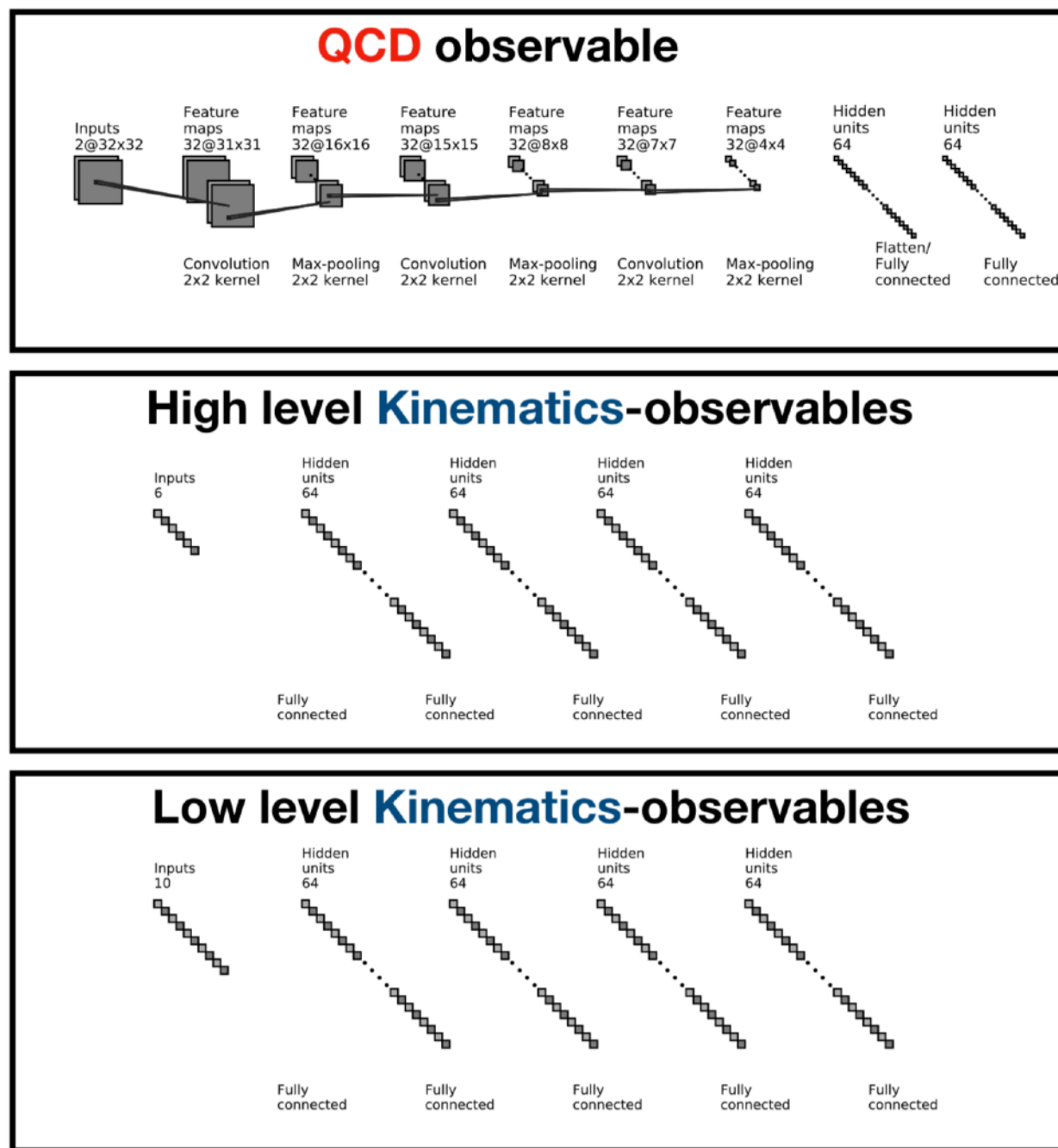
Maximizing information with Deep Neural Network

- For **jet-image**, we use 32x32 pixels for $-2.5 < \eta < 2.5$, $-\pi < \phi < \pi$.

Input channels for **CNN** are divided into two with particle flow:

- Neutral particles
- Charged particles



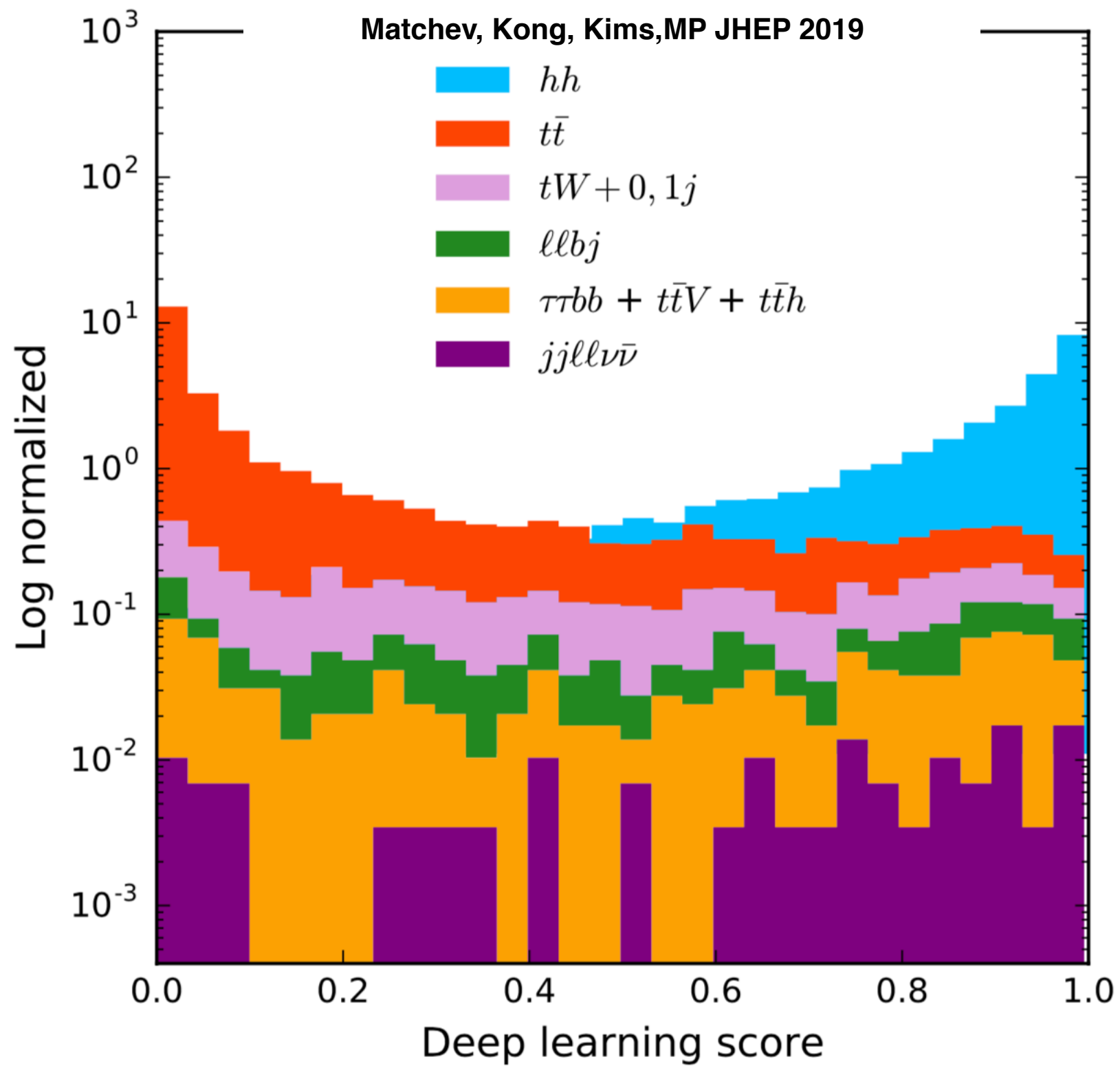


6 High Level Variables

Input data: $\sqrt{\hat{s}}_{\min}^{(\bar{b}, b, \bar{\ell}, \ell)}$ $\sqrt{\hat{s}}_{\min}^{(\bar{\ell}, \ell)}$ M_{T2}^b M_{T2}^{ℓ} Higgsness, Topness (feature variables)

10 Low Level Variables

Input data: MET $p_{\bar{\ell}}^t$ p_{ℓ}^t $\Delta R_{(\bar{\ell}, \ell)}$ $M_{(\bar{b}, b)}$ $p_{(\bar{b}, b)}^t$ $\Delta R_{(\bar{b}, b)}$ $M_{(\bar{\ell}, \ell)}$ $p_{(\bar{\ell}, \ell)}^t$, $\Delta\phi_{\{(\bar{\ell}, \ell), (\bar{b}, b)\}}$



"Backgrounds as stacked Histogram"

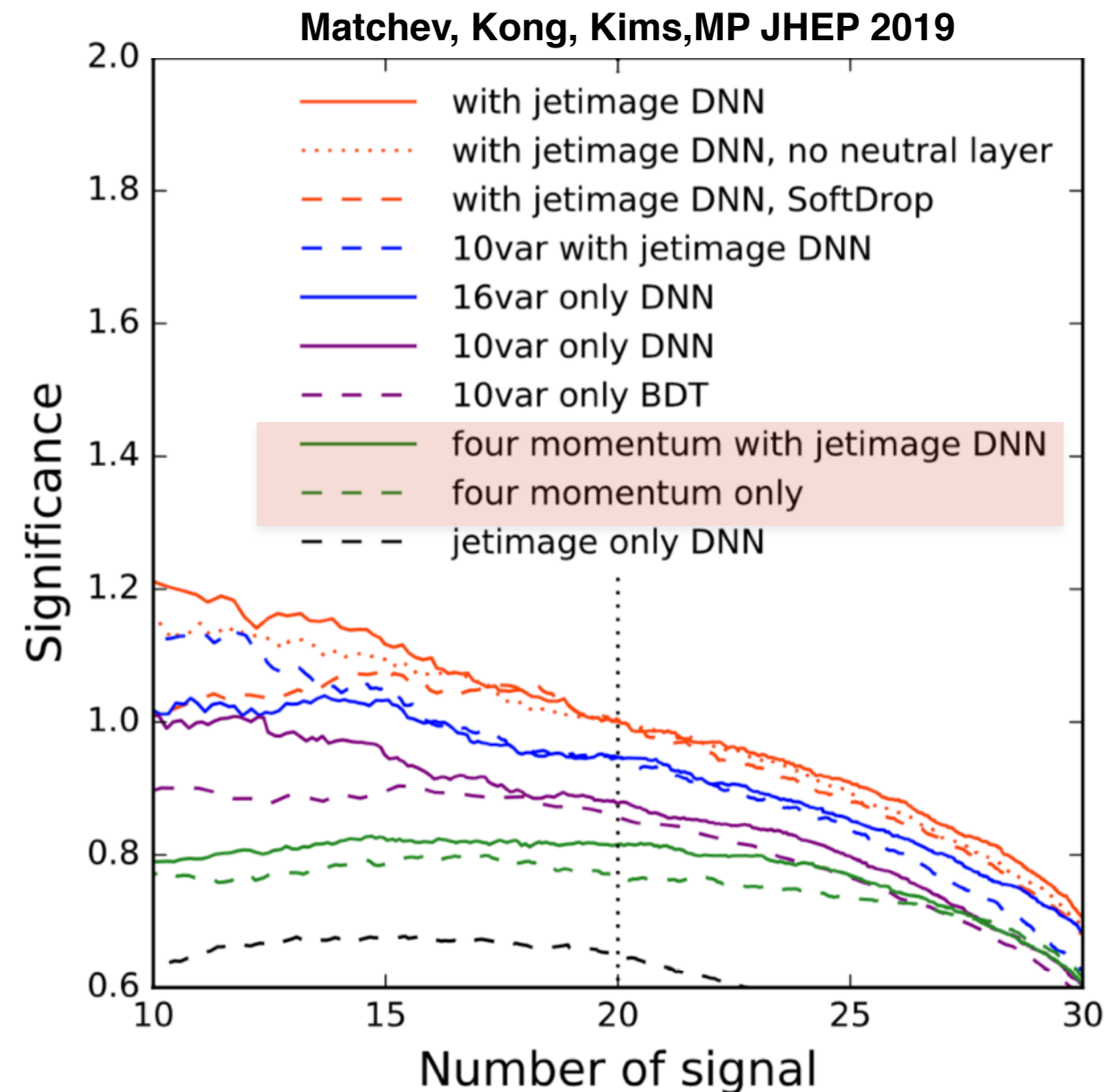
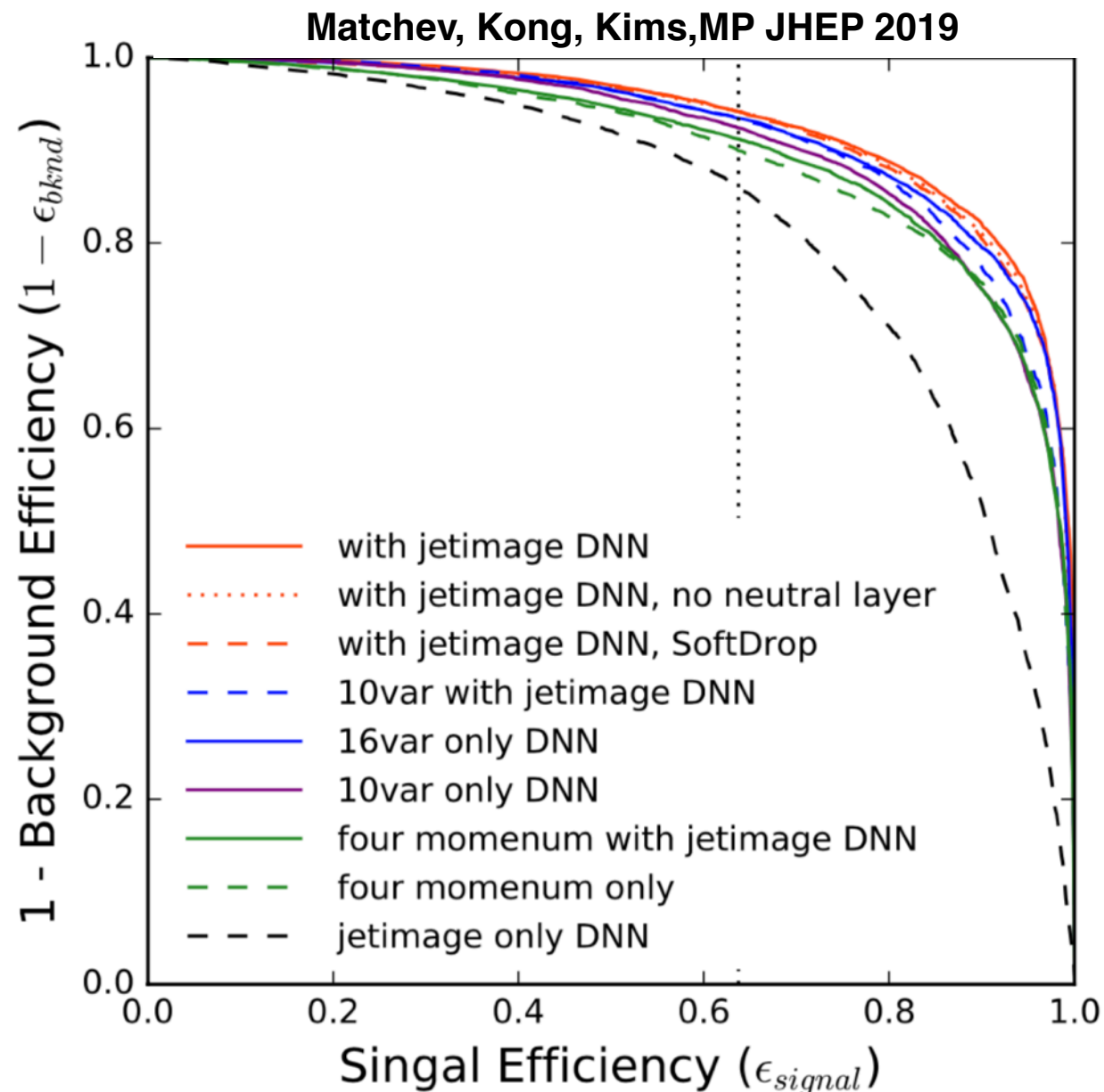
- To estimate effects from **pileup** removal (important in using QCD info),

0. No additional processes.

1. we apply SoftDrop to a fat-jet ($R=1.2$ anti-Kt)

2. we use "charged layer only"

(Various pile-up removers use "longitudinal vertex information through tracking")



Difficulties in DL

- Feature learning (data preprocessing)
 - Is it really necessary if we have smart DL ?
- In the case of Dark matter searches,
 - For a given model, we have no idea about parameters (mass of mediator, dark matter)
 - There would be Dark matter model which we have not thought about.

Difficulties in preparing MC

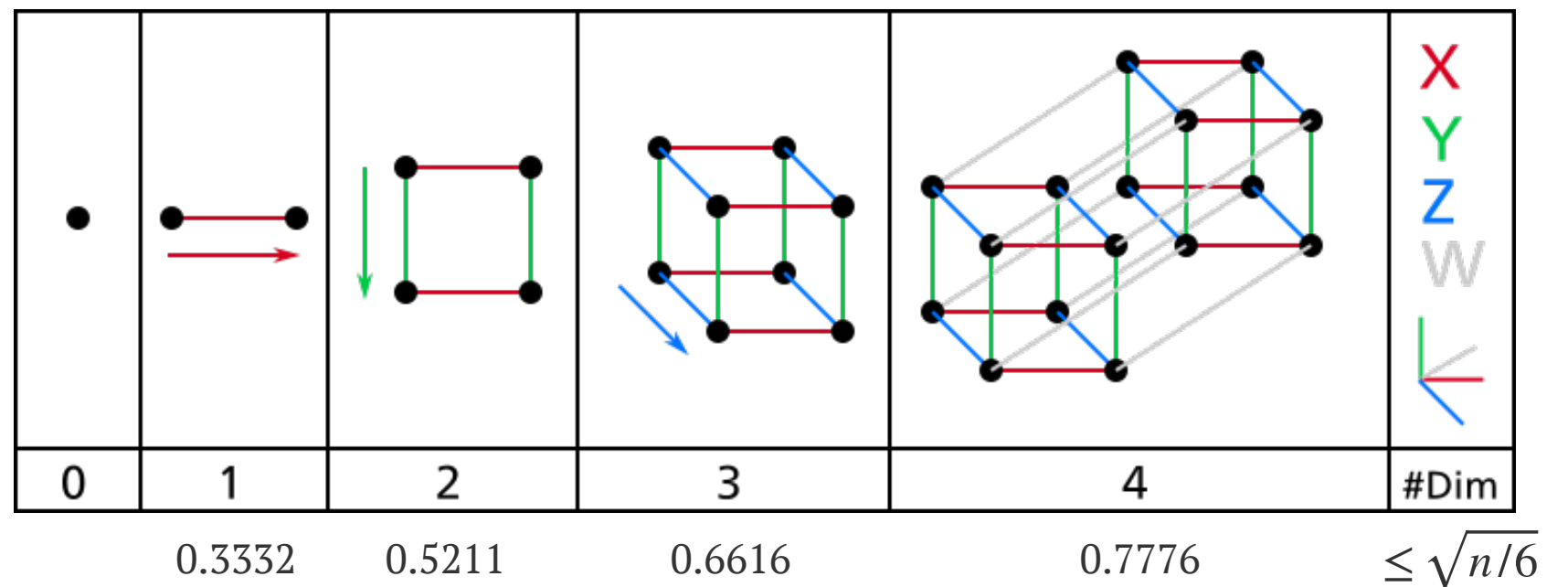
$\sigma(\text{fb})$	Signal	$t\bar{t}$	$t\bar{t}h$	$t\bar{t}V$	$\ell\bar{\ell}bj$	$\tau\tau bb$	$tw + j$	$jj\ell\ell\nu\nu$	σ	S/B
Baseline cuts: $p_T > 20 \text{ GeV}$, $p_{T,\ell} > 20 \text{ GeV}$, $\Delta R_{\ell\ell} < 1.0$, $p_{T,b} > 30 \text{ GeV}$, $\Delta R_{bb} < 1.3$, $m_{\ell\ell} < 65 \text{ GeV}$, $95 < m_{bb} < 140 \text{ GeV}$	0.648	953.6 $\times 10^3$	611.3	1.71 $\times 10^3$	71.17 $\times 10^3$	3.289 $\times 10^3$	5.107 $\times 10^3$	8.819 $\times 10^3$		
	0.01046	1.8855	0.0269	0.0179	0.0697	0.0250	0.2209	0.0113	0.38	0.0046
jet-image DL	0.00667	0.1817	0.0133	0.00793	0.0245	0.0129	0.0671	0.00854	0.65	0.021
10 low-level variables DL	0.00668	0.0806	0.00897	0.00435	0.0163	0.00876	0.0462	0.00578	0.88	0.039
16 variables DL	0.00667	0.0662	0.00948	0.00358	0.0170	0.00747	0.0387	0.00402	0.95	0.046
10 variables + jet-image DL	0.00667	0.0693	0.00897	0.00435	0.0178	0.00722	0.0359	0.00352	0.95	0.045
16 variables + jet-image DL	0.00668	0.0607	0.00769	0.00281	0.0173	0.00799	0.0317	0.00402	1.0	0.051

- To generate backgrounds properly, we need to make HUGE Monte Carlo samples
- Preparing "Good enough" MC samples for testing is **NOT EASY**.
- Thus, we should find very good features (High-level observables)

Curse of dimensionality problem (1957)

n-dim cubic with
length 1

average distance
between two points



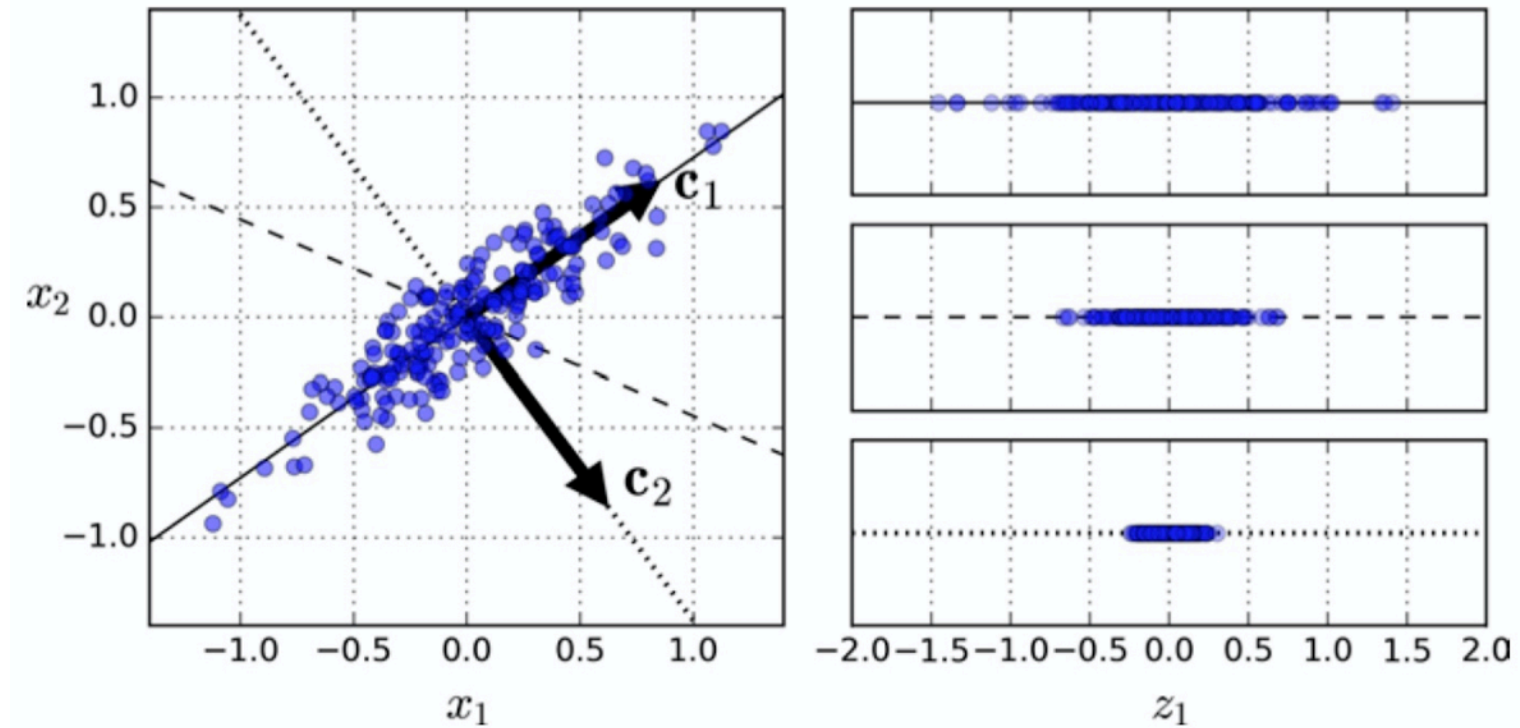
- If we increase density by a conventional grid method, number of points for n -dimension is proportional to d^n where d -distance in one dimension.

$$P||E_{\text{training}}(f_{\text{estimator}}) - E_{\text{test}}(f_{\text{estimator}})| > \epsilon|| \leq N_{\text{hypothesis}} e^{-2\epsilon^2 N_{\text{training}}}$$

"Hoeffding inequality" (from a textbook)

- There have been various methods to resolve this issue.

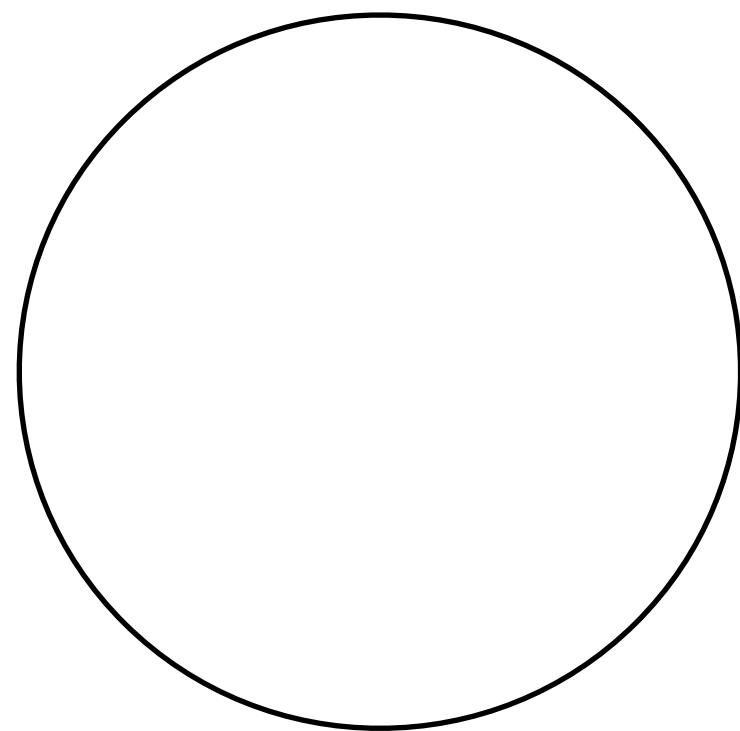
- Principal Component Analysis (PCA)



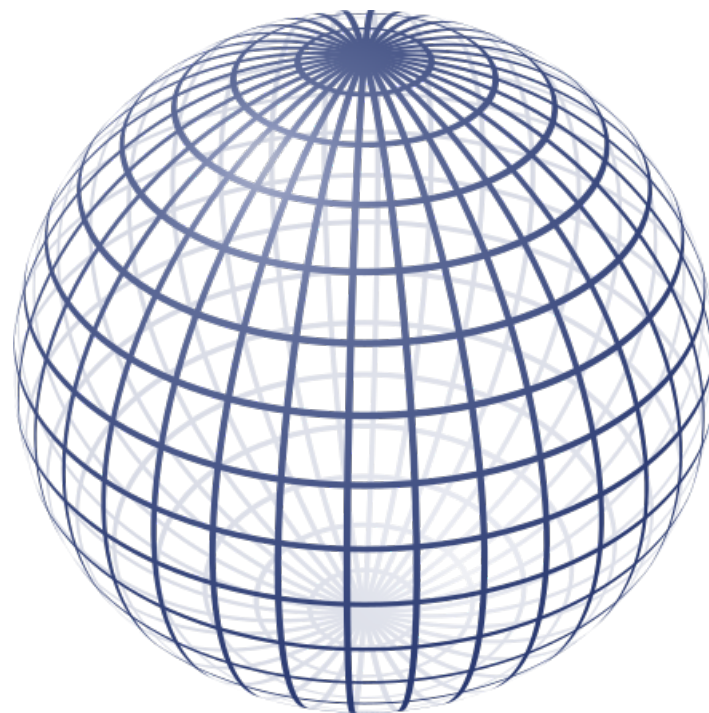
- Manifold learning



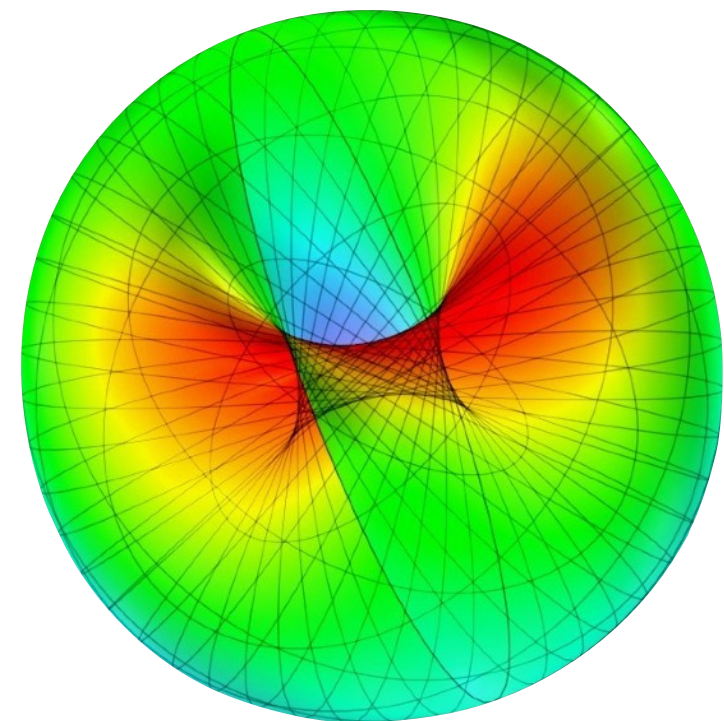
- But, **feature variable** in our hands (HEP) are not simple function of raw data. The transformation is **highly non-linear**.
 - we try to find a good DL architecture... **also** ...
 - we design feature variables for the input of DL



S^1



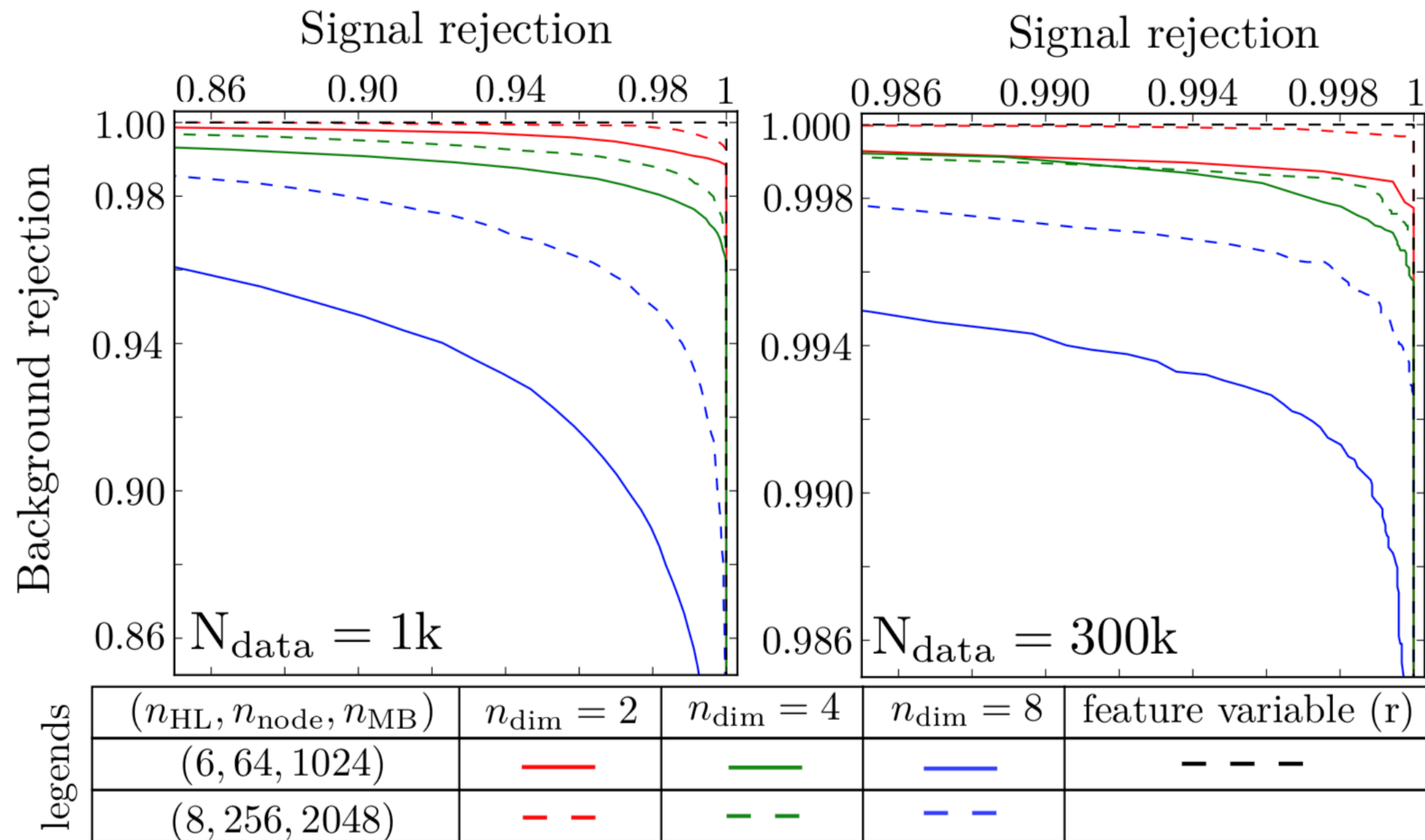
S^2



Projection of S^3 into R^3

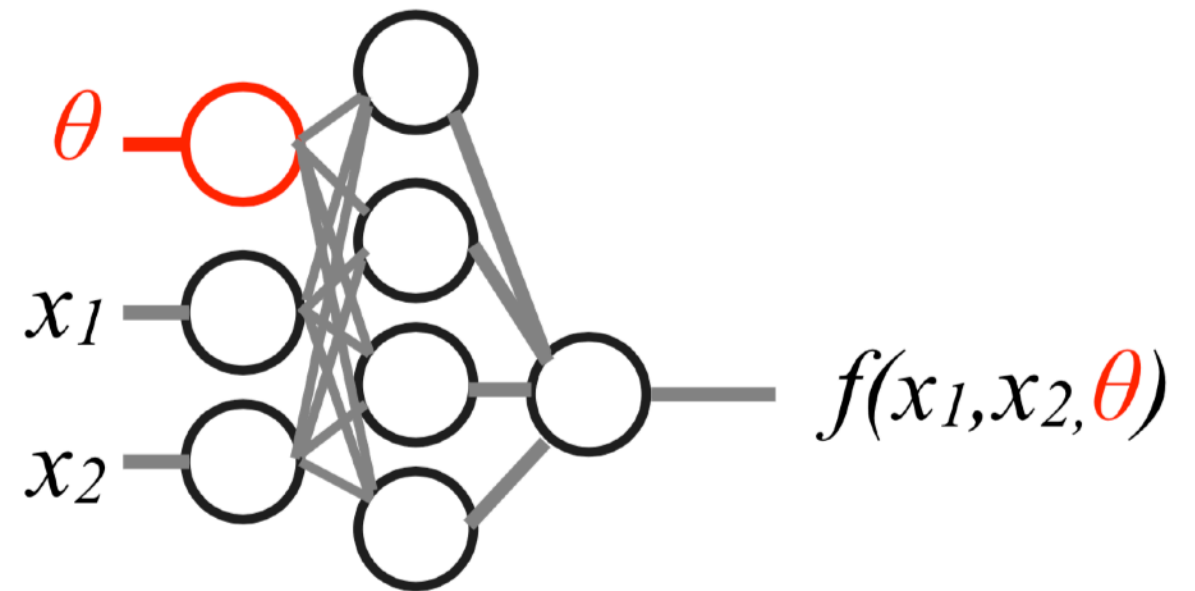
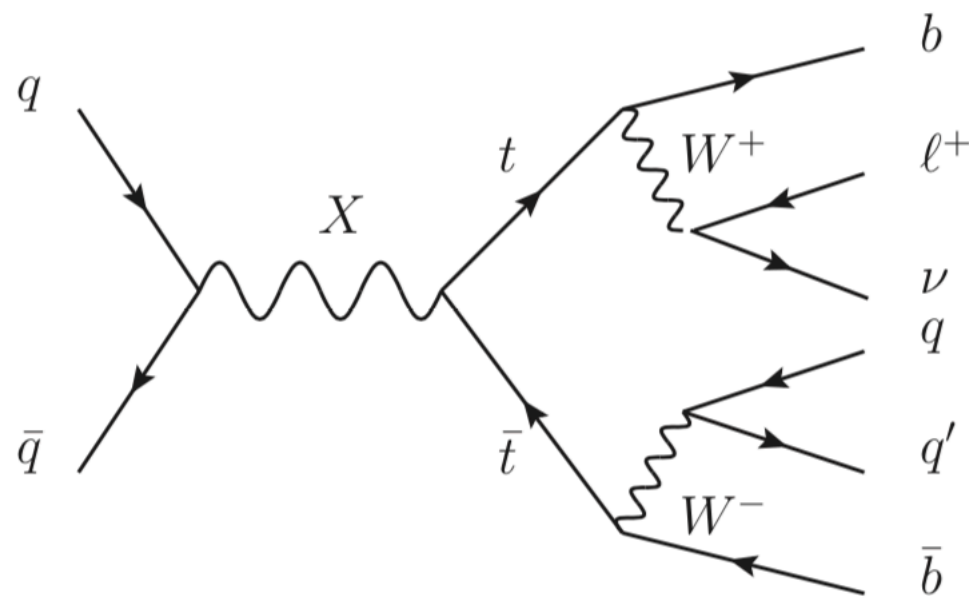
• • •

- Inside n-sphere: Signal events
Outside n-sphere: Backgrounds.
- Featured variable: Radius.
Raw observable: coordinate

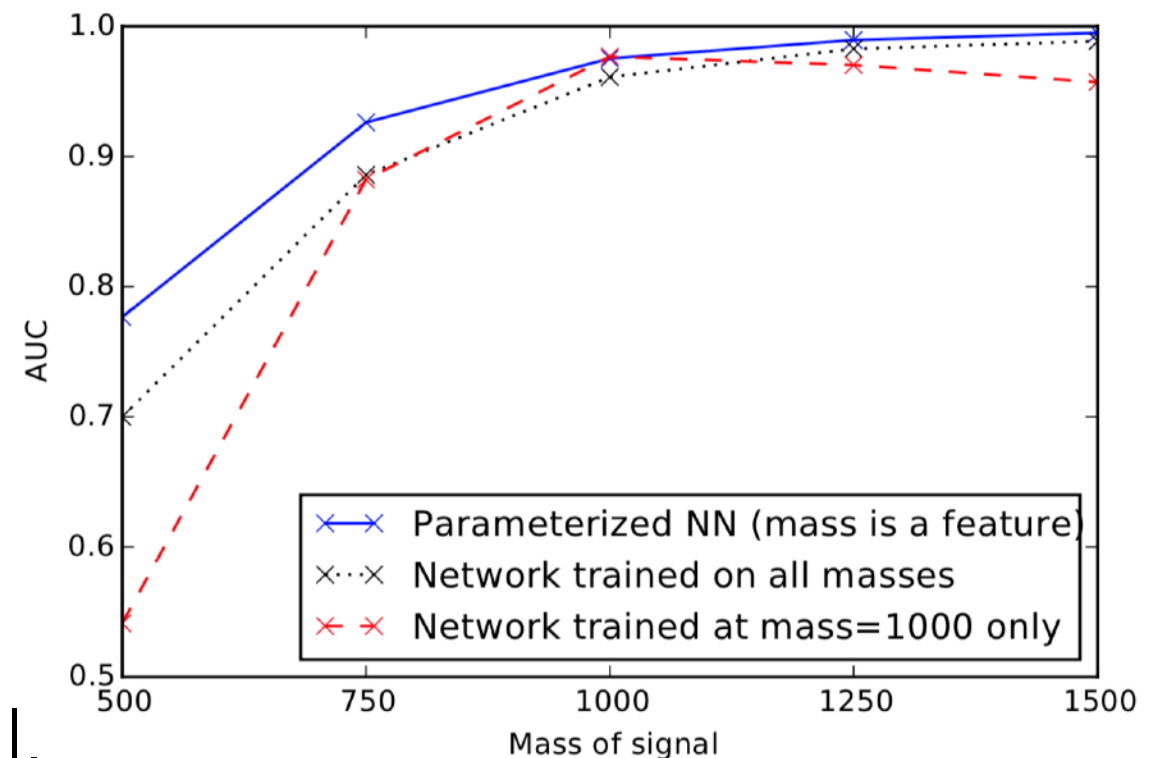


- Featured variables are effective in learning with few data.
- Featured variable: Radius.
Raw observable: coordinate

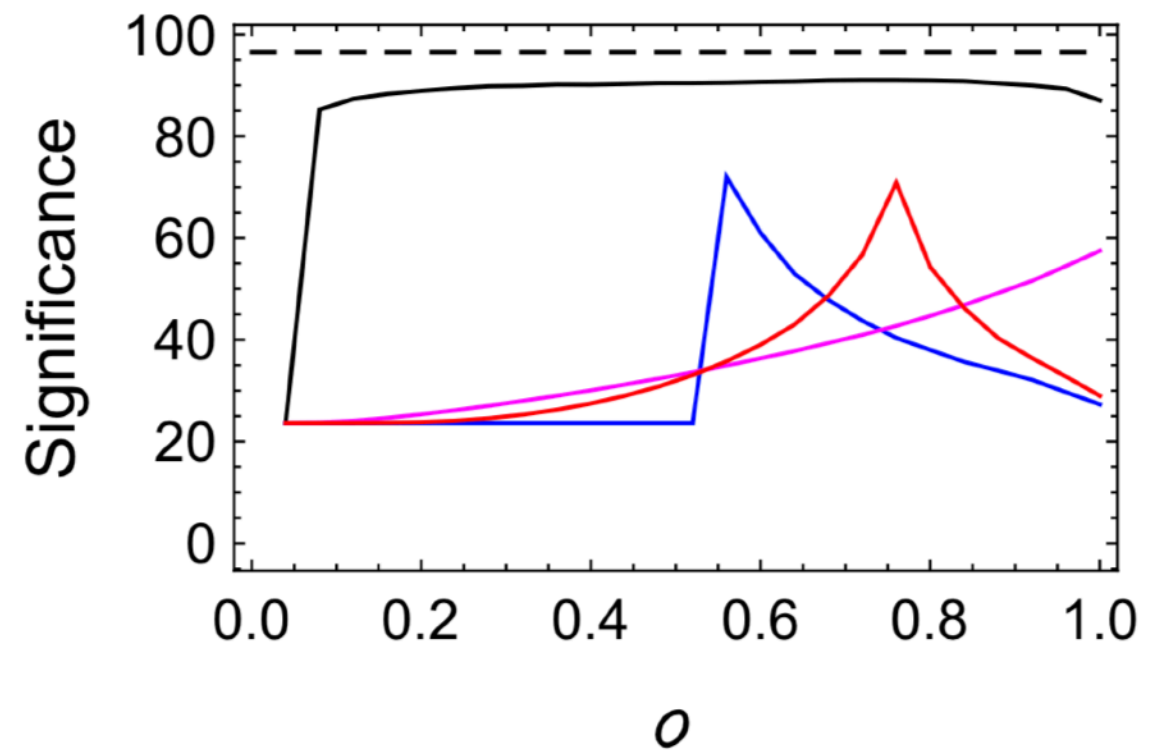
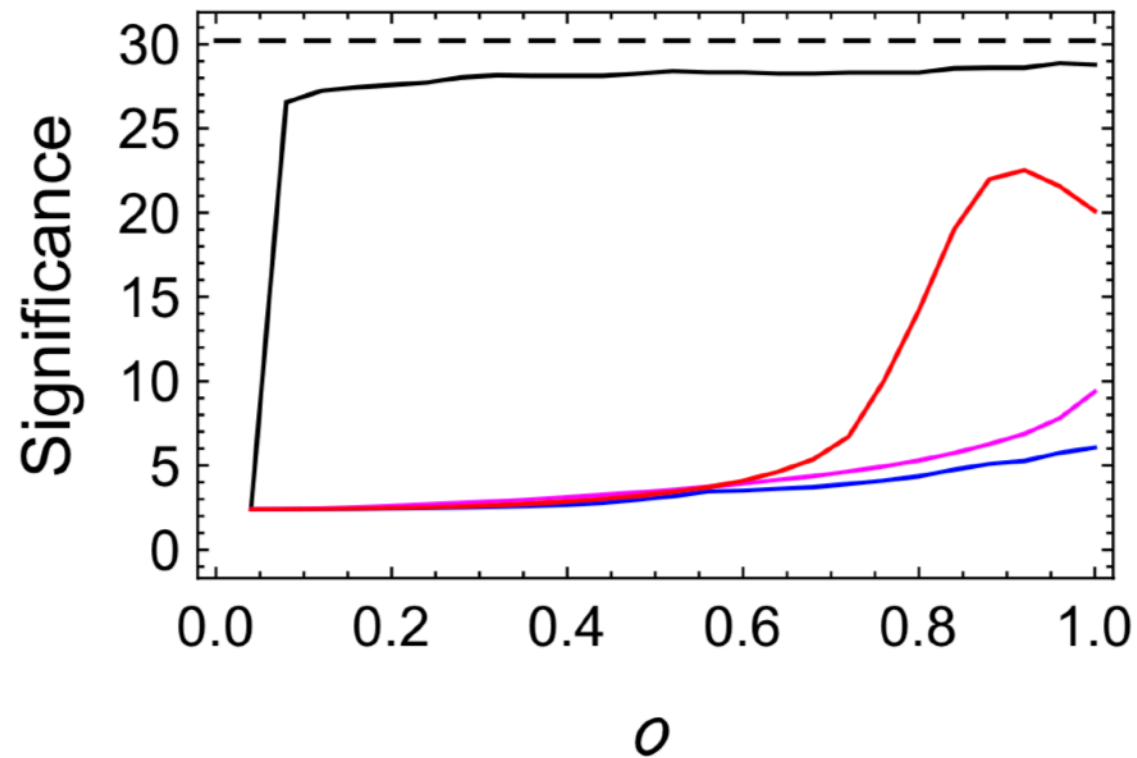
Out of parameter problem



- Parameterized NN:
A single neural network with the true mass, as an input feature.



Out of Model ambiguity problem



X1	$m_T = m_{\bar{T}} 1.2 \text{ TeV}, \text{BR}(T \rightarrow W_l^+ b) = 50 \%$	0.152
X2	$m_{Z'} = 3 \text{ TeV}, g_{Z'} = g_Z, \text{BR}(Z' \rightarrow t\bar{t}) = 16.7 \%$	1.55

- Based on autoencoder, find an anomaly away from Standard Model (backgrounds) expectations.

arXiv:1807.10261 by Tao Liu et.al.

Conclusions

- Various DL algorithms can enhance searches at the LHC
- When we are targeting a specific NP scenario, we can maximize a sensitivity by aggressively utilizing "**feature variables**" through DL.
 - reducing the issue of Dimensionality.
- When we don't have any preferred parameter in a given model, still DL would provide the best performance.
- When we don't have any MODEL in our mind, DL can provide a "good" results via an anomaly detection....
 - We need to check what kind of models we have missed so far !

