Minimal Supergravity Inflation without Slow Gravitino

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arXiv:2104.05731 [hep-th], accepted for publication in Phys. Rev. D.

PASCOS 2021

Broken SUSY in the Early Universe

• Supersymmetry (SUSY) may be a fundamental symmetry of the Nature.

Motivation:





Coupling unification

Dark matter

It must be (spontaneously) broken in the cosmological background.

Usually, the order parameters are $\langle F(\varphi) \rangle$, $\langle D(\varphi) \rangle$. In cosmology, kinetic energy $\langle \phi^2 \rangle$, Hubble expansion H, and temperature T can break SUSY.

- Generic fields receive SUSY breaking (Hubble-induced) mass of $\mathcal{O}(H)$.









Hierarchy problem

Flat inflaton potential

Vacuum stability

Superstring theory

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 - → Possibility for observational effects. "Cosmological Collider"

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[Arkani-Hamed, Maldacena, 1503.08043] etc.

• Fields much heavier than H decouple from inflationary dynamics. cf.) constraints on isocurvature perturbations

e.g.) strong stabilization $d^4\theta$ -



e.g.) nilpotent superfield X satisfying $X^2 = 0$.

X = x +

- $X^2 = 0$
- How about decoupling fermions?

$$\frac{1}{\Lambda^2} |X|^4 \sim \frac{|F^X|^2}{\Lambda^2} |X|^2.$$

For example, [Lee, 1005.2735], [Evans, Garcia, Olive, 1311.0052], etc.

• An incomplete SUSY multiplet can be described by a *constrained superfield*.

$$-\sqrt{2\theta\chi^{X}} + \theta\theta F^{X}$$

$$\rightarrow x = \frac{1}{2F^{X}}\chi^{X}\chi^{X}$$



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• Orthogonal nilpotent superfields X and T:

$$X^2 = X(T - \bar{T}) = 0$$

Stabilizer superfield $X = x + \sqrt{2\theta\chi^X} + \theta\theta F^X$ Inflaton superfield $T = t + \sqrt{2}\theta\chi^T + \theta\theta F^T$

• The only independent dynamical degrees of freedom are χ^{X} (stabilizino) and Ret (inflaton).

The physical spectrum: (real) inflaton, (massive) gravitino, and graviton.

[Ferrara, Kallosh, Thaler, 1512.00545], [Carrasco, Kallosh, Linde, 1512.00546]

• The model is specified by

• The scalar potential is

$$K(T, \bar{T}, X, \bar{X}) = \bar{X}X - \frac{1}{4}(T + \bar{T})^2,$$
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Longitudinal gravitino Lagrangian

$$\mathscr{L} = -\frac{1}{2}\overline{\psi^{\ell}}\left(\gamma^{0}\partial_{0} - \hat{c}_{3/2}\left(\vec{\gamma}\cdot\vec{\nabla}\right) + a\,\widehat{m}_{3/2}\right)$$

$$\widehat{c}_{3/2} \equiv \frac{p_{\text{SB}} - \gamma^0 p_W}{\rho_{\text{SB}}} \qquad \widehat{m}_{3/2} \equiv \frac{3Hp_W + m_{3/2} \left(\rho_{\text{SB}} + 3p_{\text{SB}}\right)}{2\rho_{\text{SB}}}$$

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Phase-space distribution (neglecting backreaction; $m_{3/2} \rightarrow 0$ limit)

$$f_{3/2}(\vec{k},t) = \frac{1}{2} \left(1 + \operatorname{sgn}(c_{3/2}(t))\right)$$



[Hasegawa, Mukaida, Nakayama, Terada, Yamada, 1701.03106], [Kolb, Long, Mcdonough, 2102.10113; 2103.10437]

Inflaton potential & gravitino sound speed



Catastrophic gravitino production

$$a^{3}n_{3/2} \sim 2 \int_{0}^{\Lambda} dk \, \frac{4\pi k^{2}}{(2\pi)^{3}} f_{3/2}(\vec{k}, t) \sim \Lambda^{3}$$

... or breakdown of the effective theory.





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Independent of momentum



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... or breakdown of the effective theory.



In this talk, our aim is **not** to solve this issue.

Instead, we propose an alternative model for "Minimal Supergravity Inflation" without the issue.

[Aldabergenov, Chatrabhuti, Isono, 2103.11217] See also [Kuzenko, 1712.09258], [Komargodski, Seiberg, 0907.2441]

See [Aldabergenov, Chatrabhuti, Isono, 2103.11217] for the explicit expression.

 \rightarrow The solution in supergravity would be much complicated...

more precise parametrization: $\Phi = (\phi + i\varphi, 0, -iF^{\Phi}, -F^{\Phi}, -i\partial_{\mu}(\phi + i\varphi), 0, 0)$ constraint: $0 = \frac{i}{8}(\Phi - \bar{\Phi})^3 = \left(\varphi^3, 0, -3\varphi^2 \operatorname{Re} F^{\Phi}, -3\varphi^2 \operatorname{Im} F^{\Phi}, -3\varphi^2 \partial_{\mu}\phi, 0, 3\varphi \left(-\partial^{\mu}\phi \partial_{\mu}\phi - \partial^{\mu}\varphi \partial_{\mu}\varphi + |F^{\Phi}|^2\right)\right)$

We obtain $\varphi = v = \chi^{\Phi} = 0$ in the unitary gauge.

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 \rightarrow The solution in supergravity would be much complicated...

more precise parametrization: $\Phi = (\phi + i\varphi, 0, -iF^{\Phi}, -F^{\Phi}, -i\partial_{\mu}(\phi + i\varphi), 0, 0)$ constraint: $0 = \frac{i}{8}(\Phi - \bar{\Phi})^3 = \left(\varphi^3, 0, -3\varphi^2 \operatorname{Re} F^{\Phi}, -3\varphi^2 \operatorname{Im} F^{\Phi}, -3\varphi^2 \partial_{\mu}\phi, 0, 3\varphi \left(-\partial^{\mu}\phi \partial_{\mu}\phi - \partial^{\mu}\varphi \partial_{\mu}\varphi + |F^{\Phi}|^2\right)\right)$

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In terms of a cubic nilpotent superfield Φ , $(\Phi - \overline{\Phi})^3 = 0$, Kähler potential can be expanded as follows. $K(\Phi,\bar{\Phi}) = K_0(\Phi+\bar{\Phi}) - iK_1(\Phi+\bar{\Phi})(\Phi-\bar{\Phi}) - \frac{1}{2}K_2(\Phi+\bar{\Phi})(\Phi-\bar{\Phi})^2$ $W(\Phi) = W(\Phi)$ Shift symmetry in Kähler potential ($K_0, K_1, K_2 \simeq \text{const.}$); soft explicit breaking in superpotential. For simplicity, let us take $K_0 = 0, K_1 = c$, and $K_2 = 1$. Scalar potential is in supergravity with a single chiral superfield. $V = e^{K} (g^{\bar{\Phi}\Phi} |D_{\Phi}W|^{2} - 3 |W|^{2})$ $= |W_{\Phi}|^{2} + (c^{2} - 3)|W|^{2} + 2c \operatorname{Im}(W\bar{W}_{\bar{\Phi}}).$

Superpotential is generic.

There are several methods to construct inflation potentials

$$W(\Phi) = W_0 \left(e^{\sqrt{3}\Phi} - e^{-\sqrt{3}\Phi} \text{Polynomial} \left(e^{-2\Phi/\sqrt{3}\alpha} \right) \right)$$



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[Roest, Scalisi, 1503.07909]

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[Ketov, Terada, 1406.0252; 1408.6524; 1509.00953; 1606.02817], [Linde, 1504.00663], [Ferrara, Roest, 1608.03709]

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[Akrami et al., Planck 2018, Constraints on inflation]

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Longitudinal gravitino Lagrangian

$$\mathscr{L} = -\frac{1}{2}\overline{\psi^{\ell}}\left(\gamma^{0}\partial_{0} - \hat{c}_{3/2}\left(\vec{\gamma}\cdot\vec{\nabla}\right) + a\,\widehat{m}_{3/2}\right)$$

$$\widehat{c}_{3/2} \equiv \frac{p_{\text{SB}} - \gamma^0 p_W}{\rho_{\text{SB}}} \qquad \widehat{m}_{3/2} \equiv \frac{3Hp_W + m_{3/2} \left(\rho_{\text{SB}} + 3p_{\text{SB}}\right)}{2\rho_{\text{SB}}}$$

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The (standard) gravitino problem

[Pagels, Primack, PRL 48 (1982) 223], [Weinberg PRL 48 (1982) 1303] [Khlopov, Linde, PLB 138 (1984), 265], [Ellis, Kim, Nanopoulos, PLB 145 (1984]

- Thermal production
- Nonthermal production

Assuming that the inflaton remains to be the dominant source of the SUSY breaking (otherwise, we need to consider mixing of fermions) and that $m_{\phi} \gg m_{3/2}$ for simplicity,

$$\Gamma(\phi \to \psi_{3/2} \psi_{3/2}) \simeq \frac{m_{\phi}^5}{96\pi m_{3/2}^2 M_{\rm P}^2}.$$

[Endo, Hamaguchi, Takahashi, hep-ph/0602061], [Nakamura, Yamaguchi, hep-ph/0602081]

- Effects on light element abundance
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To avoid these problems,

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The (standard) gravitino problem

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The (standard) gravitino problem

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 $\boldsymbol{\mathcal{W}}^{\iota}$

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The (standard) gravitino problem

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Assuming that the inflaton remains to be the dominant source of the SUSY breaking (otherwise, we need to consider mixing of fermions) and that $m_{\phi} \gg m_{3/2}$ for simplicity,

$$\Gamma(\phi \to \psi_{3/2} \psi_{3/2}) \simeq \frac{m_{\phi}^5}{96\pi m_{3/2}^2 M_{\rm P}^2}$$

[Endo, Hamaguchi, Takahashi, hep-ph/0602061], [Nakamura, Yamaguchi, hep-ph/0602081]

- Effects on light element abundance
- Overproduction of dark matter
- To avoid these problems,
 - $m_{\phi} \lesssim 2m_{3/2}$
 - Entropy production
 - R-parity violation, etc.



[Terada, "Minimal Supergravity Inflation without Slow Gravitino", 2104.05731 [hep-th]]

- We propose an alternative realization of "Minimal Supergravity Inflation"
- In our model, gravitino is NOT slow, $|\hat{c}_{3/2}|^2 = 1$. Therefore, there is NO anomalous production issue.
- Neverthelss, there is the (standard) gravitino problem.

where only degrees of freedom are a (real) inflaton, gravitino, and graviton.

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Advertisement: Massless Preheating and Electroweak Vacuum Metastability

J. Kost, C.S. Shin, T. Terada

arXiv: 2105.06939 [hep-ph]

We forgot to submit the abstract by the PASCOS deadline...





Cubic Nilpotent Superfield, in more detail

[Aldabergenov, Chatrabhuti, Isono, 2103.11217]

A chiral superfield **S** can be expanded as follows: $\mathbf{S} = S + \sqrt{2}\theta\chi + \theta\theta F$, $S = \phi + i\phi$. The constraint, $(S + \bar{S})^3 = 0$, is solved for the real part of the bosonic component, $\Sigma \equiv S + \bar{S}$.

$$\Sigma = \chi^2 \beta + \chi^2 + \chi^2 \beta + \chi^2 + \chi^2 \beta + \chi^2$$

where $U \equiv 2(|F|^2 - \partial_{\mu} \varphi \partial^{\mu} \varphi)$, and β is defined as

$$\beta \equiv \frac{\bar{F}}{U} + \frac{i\bar{\chi}}{U^2} \left(\bar{F}\bar{\sigma}^{\mu}\partial_{\mu}\chi - \partial_{\mu}\varphi\partial^{\mu}\bar{\chi} + 2\partial_{\mu}\varphi\bar{\sigma}^{\mu\nu}\partial_{\nu}\bar{\chi} - \frac{\bar{\chi}^2}{2U^3} \left(F\partial_{\mu}\bar{\chi}\bar{\sigma}^{\mu\nu}\partial_{\nu}\bar{\chi} + \bar{F}\partial_{\mu}\chi\sigma^{\mu\nu}\partial_{\nu}\chi + F\partial_{\mu}\chi\sigma^{\mu\nu}\partial_{\nu}\chi + F\partial_{\mu}\chi\sigma^{\mu\nu}\partial_{\mu}\chi + F\partial_{\mu}\chi\sigma^{\mu}\partial_{\mu}\chi + F\partial_{\mu}\chi\phi^{\mu}\partial_{\mu}\chi + F\partial_{\mu}\chi$$

 $- \bar{\chi}^2 \bar{\beta} + \frac{2}{II} \chi \sigma^\mu \bar{\chi} \partial_\mu \varphi,$

 $\partial_{\nu}\chi$

 $\vdash \partial_{\mu}\varphi\partial_{\nu}\chi\left(2\sigma^{\mu}\eta^{\nu\rho}-\sigma^{\nu}\eta^{\rho\mu}-\sigma^{\rho}\eta^{\mu\nu}-i\epsilon^{\mu\nu\rho\sigma}\sigma_{\sigma}\right)\partial_{\rho}\bar{\chi}\right).$

Proof of $|\hat{c}_{3/2}| = c$

$$|\hat{c}_{3/2}|^2 = \frac{p_{\text{SB}}^2 + |p_W|^2}{\rho_{\text{SB}}^2} = \frac{\left(\frac{1}{2}\dot{\phi}^2 - |F^{\Phi}|^2\right)^2 + \left|\sqrt{2}F^{\Phi}\dot{\phi}\right|^2}{\left(\frac{1}{2}\dot{\phi}^2 + |F^{\Phi}|^2\right)^2} = 1.$$

chiral superfield. This fact is well known.

The gravitino sound speed equals the speed of light when the inflation sector is composed of a single

[Kallosh, Kofman, Linde, Van Proeyen, hep-th/9907124; hep-th/0006179] [Giudice, Tkachev, Riotto, hep-ph/9907510; hep-ph/9911302] See also [Nilles, Peloso, Sorbo, hep-ph/0102264; hep-th/0103202] [Ema, Mukaida, Nakayama, Terada, 1609.04716]

[Hasegawa, Mukaida, Nakayama, Terada, Yamada, 1701.03106]

Gravitino mode expansion (Dirac rep.)



Let us begin with the simplest case: $g(\Phi) = m_{3/2}M$

Further, let us consider the limit $m_{3/2} \rightarrow 0$ to allow (Of course, this limit restores SUSY, so we cannot take this

The sign change of the sound speed switches the

$$f_{3/2}(\overrightarrow{k};t) \equiv \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \widehat{m}_{3/2}(t) \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^+(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) \right) \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^+(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^+(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) \right) \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^+(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) \right) \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^+(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) \right) \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^+(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) \right) \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^+(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) \right) \right) \right)$$

Equation of motion for this
For H.c. Equation of motion for this

$$c_{3/2}u'' - c'_{3/2}u' + c_{3/2}\widetilde{\omega}_k^2 u = 0$$

 $\widetilde{\omega}_k^2 \equiv a^2 \omega_k^2 - ic_{3/2}(a \,\widehat{m}_{3/2}/c_{3/2})'$
where $c_{3/2} \equiv (p_{\text{SB}} + ip_W)/\rho_{\text{SB}}$ and $\omega_k \equiv \sqrt{\widehat{m}_{3/2}^2 + |c_{3/2}k/a|^2}$
 \mathcal{M}_P^2 (const.). $\Rightarrow p_W = 0$, and $c_{3/2} = c_{3/2}^* = w_{\text{SB}}(=p_{\text{SB}}/\rho_{\text{SB}})$
an analytic solution: $u(\eta) = \frac{1}{\sqrt{2}} \exp\left[ik \int_0^{\eta} d\eta' c_{3/2}(\eta')\right]$
e positive and negative frequency modes.

 $+\frac{1}{2} = \frac{1}{2} \left(1 + \operatorname{sgn} \left(c_{3/2}(t) \right) \right) \quad \leftarrow \text{Momentum independent!!}$



[Hasegawa, Mukaida, Nakayama, Terada, Yamada, 1701.03106]

Gravitino mode expansion (Dirac rep.)



Let us begin with the simplest case: $g(\Phi) = m_{3/2}N$

Our orders-of-magnitude estimates and conclusions would not be affected.

The sign change of the sound speed switches the positive and negative frequency modes.

$$f_{3/2}(\overrightarrow{k};t) \equiv \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \widehat{m}_{3/2}(t) \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) - \frac{1}{2\omega_k(t)} \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^{+*}(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^+(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) \right) \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^+(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^+(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) \right) \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^+(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) \right) \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^+(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) \right) \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^+(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) \right) \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^+(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) \right) \right) + \frac{1}{2\omega_k(t)} \left(2\mathrm{Im} \left(u_{\overrightarrow{k}}^+(t)\dot{u}_{\overrightarrow{k}}^+(t) \right) \right) \right)$$

Equation of motion for this
- H.c.
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$$\widetilde{\omega}_{k}^{2} \equiv a^{2}\omega_{k}^{2} - ic_{3/2}(a\,\widehat{m}_{3/2}/c_{3/2})'$$
where $c_{3/2} \equiv (p_{\text{SB}} + ip_{W})/\rho_{\text{SB}}$ and $\omega_{k} \equiv \sqrt{\widehat{m}_{3/2}^{2} + |c_{3/2}k/a|^{2}}$

$$\mathcal{M}_{\text{P}}^{2} \text{ (const.).} \Rightarrow p_{W} = 0 \text{, and } c_{3/2} = c_{3/2}^{*} = w_{\text{SB}}(=p_{\text{SB}}/\rho_{\text{SB}})$$

Restoring $m_{3/2} (\ll H)$ smears the sharp edge of $f_{3/2}$ and modulates the oscillation in a longer time scale $m_{3/2}^{-1}$.

 $+\frac{1}{2} = \frac{1}{2} \left(1 + \operatorname{sgn} \left(c_{3/2}(t) \right) \right) \leftarrow \text{Momentum independent!!}$



[Hasegawa, Mukaida, Nakayama, Terada, Yamada, 1701.03106]

Dirac Sea filled up to $k \to \infty$?

Possibilities

- (A) The effective theory breaks down, and the linearized SUSY theory is needed.
- (B) The particle production phenomenon is real, and it is valid up to some UV cutoff scale Λ .

(Expected) unitarity bound

$$\Lambda_{\rm UB} = \left(M_{\rm P}^2 \left(H^2 + m_{3/2}^2 \right) \right)^{1/4}$$

[Kallosh, Kofman, Linde, Van Proeyen, hep-th/0006179] [Dall'Agata, Zwirner, 1411.2605] [Ferrara, Kallosh, Thaler, 1512.00545] [Kahn, Roberts, Thaler, 1504.05958] [Carrasco, Kallosh, Linde, 1512.00546] [Delacretaz, Gorbenko, Senatore, 1610.04227] [Casalbuoni, De Curtis, Dominici, Feruglio, Gatto, Phys.Lett.B216 (1989) 325, erratum: PLB229 (1980) 439]

Gravitino number density

 $a^{3}n_{3/2} \sim 2 \int_{0}^{\Lambda} dk \frac{4\pi k^{2}}{(2\pi)^{3}} f_{3/2}(\vec{k};t) \sim \Lambda^{3}$

Gravitino energy density

$$\rho_{3/2} \sim a^{-4} \Lambda^4 \lesssim \Lambda_{\rm UB}^4 \sim 3 H^2 M_{\rm P}^2 = \rho$$

A substantial fraction of the energy density is transferred to gravitinos.



[Hasegawa, Mukaida, Nakayama, Terada, Yamada, 1701.03106]

<u>Alternative understanding based on the standard technique of preheating</u>

Field redefinition to remove the γ^0 -dependence of the sound speed parameter: Longitudinal gravitino Lagrangian

$$\mathcal{L} = -\frac{1}{2}\overline{\tilde{\psi}^{\ell}}\left(\gamma^{0}\partial_{0} - |c_{3/2}|\left(\vec{\gamma}\cdot\vec{\nabla}\right) + a(\widehat{m}_{3/2} - \theta')\right)\tilde{\psi}^{\ell}$$

where $\tan 2\theta = -p_W/p_{SB}$. The effective mass oscillates like spikes.

Particle production is now understood as being caused by the non-adiabaticity of the oscillating mass.

Consider more general cases with $|g_{\Phi}| \neq 0$.

Gravitinos are produced up to $k_{\text{max}} \sim \min \left[\Lambda, \frac{M_{\text{P}}^2 H^2 m_{\phi}}{|g_{\Phi}|^2} \right]$. However, "standard" gravitino problem remains.

$$\psi^{\ell} = e^{\theta \gamma^0} \tilde{\psi}^{\ell}$$



[Hasegawa, Mukaida, Nakayama, Terada, Yamada, 1701.03106]

Particle production and annihilation



... Can we hope that the produced gravitinos disappear?

It is hard to imagine the exact cancellation because of the cosmic expansion. Gravitinos are diluted with time-dependent Hubble factor, so the annihilation will be incomplete.

[Hasegawa, Mukaida, Nakayama, Terada, Yamada, 1701.03106]

What is the essence of the anomalous/catastrophic production?

In the standard case without constraints, the fermion gradient terms can be diagonalized:

$$\mathscr{L}_{\text{grad}} = -\frac{1}{2} \begin{pmatrix} \overline{\psi^{\ell}} & \overline{v_{\perp}} \end{pmatrix} \begin{pmatrix} i \overrightarrow{\gamma} \cdot \overrightarrow{k} \end{pmatrix} \widehat{\mathscr{C}}_{3/2} \begin{pmatrix} \psi^{\ell} \\ v_{\perp} \end{pmatrix}$$

[Kallosh, Kofman, Linde, Van Proeyen, hep-th/9907124; hep-th/0006179] [Giudice, Tkachev, Riotto, hep-ph/9907510; hep-ph/9911302] [Nilles, Peloso, Sorbo, hep-ph/0102264; hep-th/0103202] [Ema, Mukaida, Nakayama, Terada, 1609.04716] [Dudas, Garcia, Mambrini, Olive, Peloso, Verner, 2104.03749] [Antoniadis, Benakli, Ke, 2105.03784]

The whole matrix satisfies $|\mathscr{C}_{3/2}|^2 = 1$ and can be diagonalized into the unit matrix.

The anomalous/catastrophic gravitino production can be interpreted as the brute-force intervention to the diagonalization process by the constraints. \rightarrow Inflatino (or other relevant fermions) should not be removed from the spectrum.



Gravitino Abundance

Partial decay rate (for $m_{3/2} \ll m_{\phi}$) $\Gamma(\phi \to \psi_{3/2})$

Gravitino yield $Y_{3/2} \equiv \frac{n_{3/2}}{s} = \frac{3I_{\rm R}}{2m_{\phi}} \text{Br}(\phi \to \psi_{3/2}\psi_{3/2})$ ← Suppose the branching fraction is small. We have also neglected a possible dilution effect during gravitinos are relativistic and after the end of $=\frac{m_{\phi}^4}{64\pi m_{3/2}^2 T_{\rm R} M_{\rm P}} \left(\frac{90}{\pi^2 g_*(T_{\rm R})}\right)^{1/2}$ the production at $H \sim m_{3/2}$ for simplicity. $= 4.4 \times 10^{-5} \left(\frac{m_{\phi}}{10^{12} \,\mathrm{GeV}} \right)^4$

Some possibilities to avoid the gravitino problem:



$$(w_{3/2}) \simeq \frac{m_{\phi}^5}{96\pi m_{3/2}^2 M_{\rm P}^2}$$

It can easily lead to a gravitino-dominated Universe!

$$\left(\frac{m_{3/2}}{10^{11}\,\mathrm{GeV}}\right)^{-2} \left(\frac{T_{\mathrm{R}}}{10^{9}\,\mathrm{GeV}}\right)^{-1} \left(\frac{g_{*}}{200}\right)^{-1/2}$$

- (1) Reheating by gravitino decay.
- (2) Kinematically too heavy gravitinos.
- (3) Entropy production.
- (4) R-parity violation.

Inflation Model: Example 1

Kähler potential $K(\Phi, \bar{\Phi}) = -\frac{1}{2} \left(\Phi - \bar{\Phi} \right)^2$ **Superpotential** where α , $W_0 > 0$ as a convention, and $F(x) \equiv \sum f_n x^n$ is a real holomorphic function ($f_n \in \mathbb{R}$). n=0We impose 3 conditions (parametrization): 120

(1) The origin of the field is a stationary point (minimum) V'(0) = 0. (2) The small cosmological constant $V(0) = \Lambda$. (3) The tunable SUSY breaking parameter $F(1) = 1 - \delta$. Truncating at $n = 2, f_0, f_1$, and f_2 can be solved in terms of α , δ , and Λ . Inflaton mass in terms of gravitino mass and cosmological constant

$$m_{\phi}^{2} = \frac{4(2+9\sqrt{\alpha}+9\alpha)}{3\alpha\delta} \left((2-\delta)m_{3/2}\sqrt{3(3m_{3/2}^{2}+\Lambda)} - \delta(3m_{3/2}^{2}+\Lambda) \right)$$

The gravitino is heavier than the inflaton for $\delta \simeq 1$ and for $\delta \lesssim -8\alpha^{-1}(2+9\sqrt{\alpha}+9\alpha)$.

[Roest, Scalisi, 1503.07909]

$$W(\Phi) = W_0 \left(e^{\sqrt{3}\Phi} - e^{-\sqrt{3}\Phi} F\left(e^{-\frac{2\Phi}{\sqrt{3}\alpha}} \right) \right)$$



Inflation Model: Example 2

Kähler potential $K(\Phi, \bar{\Phi}) = -ic(\Phi - \bar{\Phi}) - \frac{1}{2}(\Phi - \bar{\Phi})^2$

where c, μ , and a are real, but $b = b_R + ib_I$ is complex. Scalar potential

$$V = \mu^2 \left((c^2 - 3) \left(b_{\rm R} - e^{-a\phi} \right)^2 + \left(cb_{\rm I} - \sqrt{2}ae^{-a\phi} \right)^2 - 3b_{\rm I}^2 \right)$$

VEV of the inflaton

Inflaton mass

$$e^{-a\phi} = \frac{(c^2 - 3)b_{\rm R} - \sqrt{2}acb_{\rm I}}{c^2 + 2a^2 - 3} \qquad \qquad m_{\phi}^2 = \frac{2a^2\mu^2 \left((c^2 - 3)b_{\rm R} - \sqrt{2}acb_{\rm I}\right)^2}{c^2 + 2a^2 - 3} \qquad \qquad |m_{3/2}|^2 = \mu^2 \left|\frac{a\left(2ab_{\rm R} + \sqrt{2}cb_{\rm I}\right)}{c^2 + 2a^2 - 3} + ib_{\rm R}^2\right|^2 = \mu^2 \left|\frac{a\left(2ab_{\rm R} + \sqrt{2}cb_{\rm I}\right)}{c^2 + 2a^2 - 3} + ib_{\rm R}^2\right|^2 = \mu^2 \left|\frac{a\left(2ab_{\rm R} + \sqrt{2}cb_{\rm I}\right)}{c^2 + 2a^2 - 3}\right|^2 + ib_{\rm R}^2 + ib_{\rm R}^2$$

We can require that the form of the potential is V =

Inflaton decay into gravitinos is kinematically forbid

[Ketov, Terada, 1406.0252]

Superpotential

$$W(\Phi) = \mu \left(b - e^{-\sqrt{2}a\Phi} \right)$$

Gravitino mass

$$= \frac{m_{\phi}^2}{2a^2}(1 - e^{-a\phi})^2 + \Lambda \text{ and solve for } b_{\rm R} \text{ and } b_{\rm I}.$$

dden for $0 < c^2 - 3 \leq \mathcal{O}(1)$.
same as α -attractors,
generalizing Starobinsky model
and Higgs inflation.



Gravitino and Swampland

Some Swampland conjectures about gravitinos were proposed recently. These are not the topic of this talk.

> Gravitino Swampland conjecture [Kolb, Long, Mcdonough, 2102.10113; 2103.10437] Gravitino sound speed should not vanish.

Gravitino mass conjecture[Cribiori, Lust, Scalisi, 2104.08288]Gravitino distance conjecture[Castellano, Font, Herraez, Ibáñez, 2104.10181]

The limit of vanishing gravitino mass corresponds to an infinite distance. An infinite tower of states become light in the limit, and the EFT breaks down.