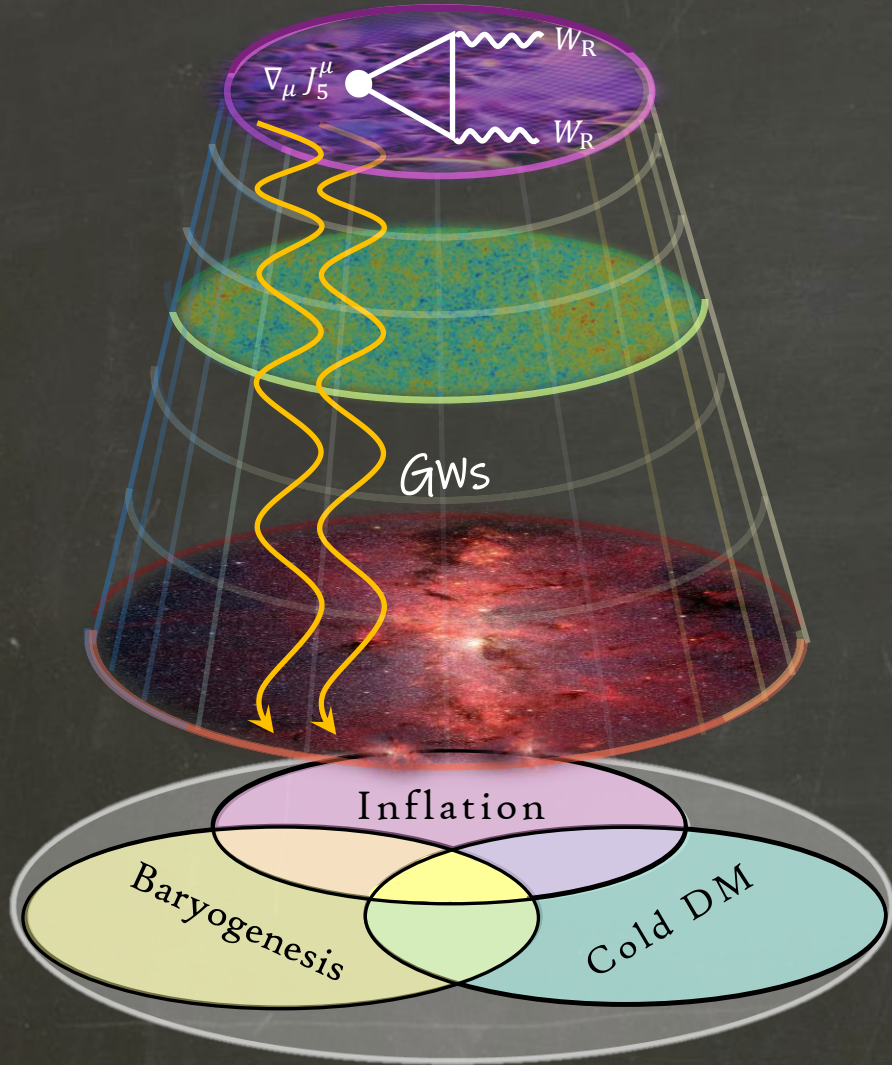


Is our Universe Remnant of Chiral Anomaly in Inflation?

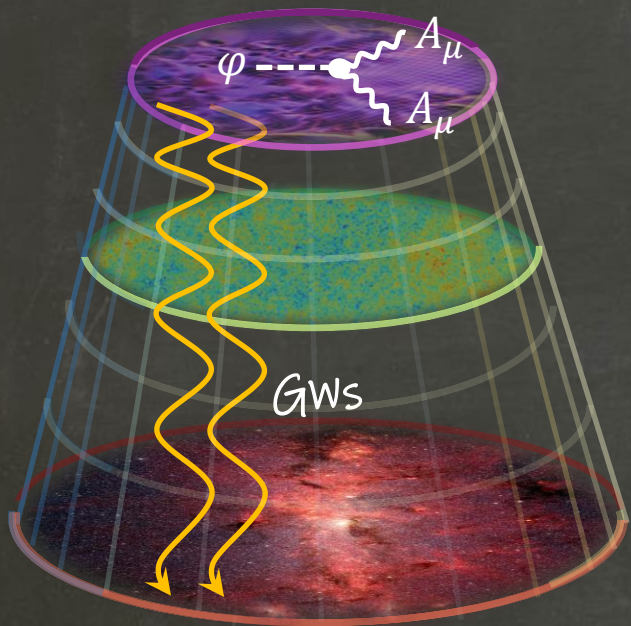
Based on

arXiv:2012.11516 & arXiv:2103.14611

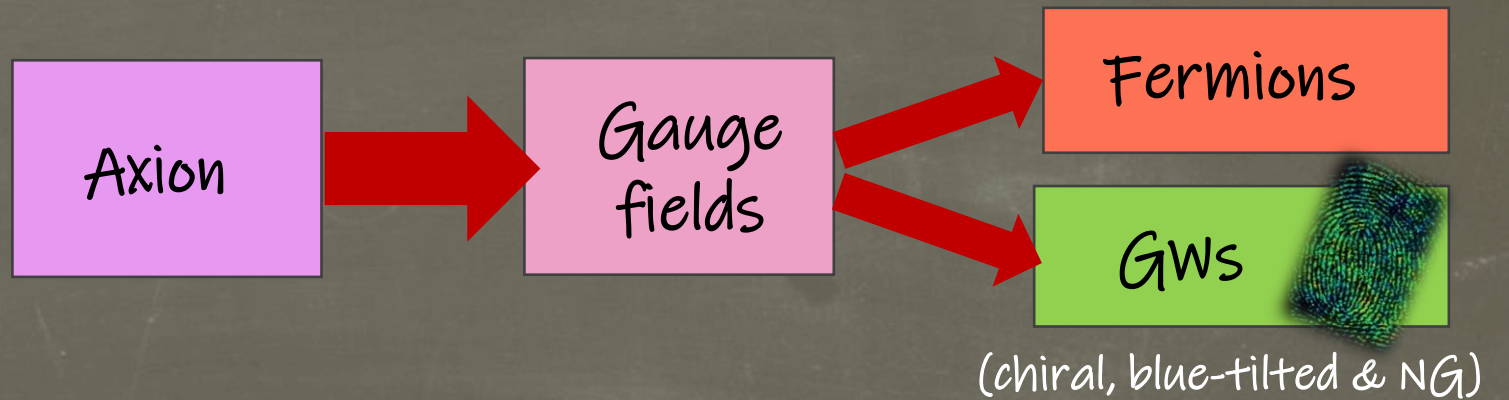
Azadeh Malek-Nejad
CERN



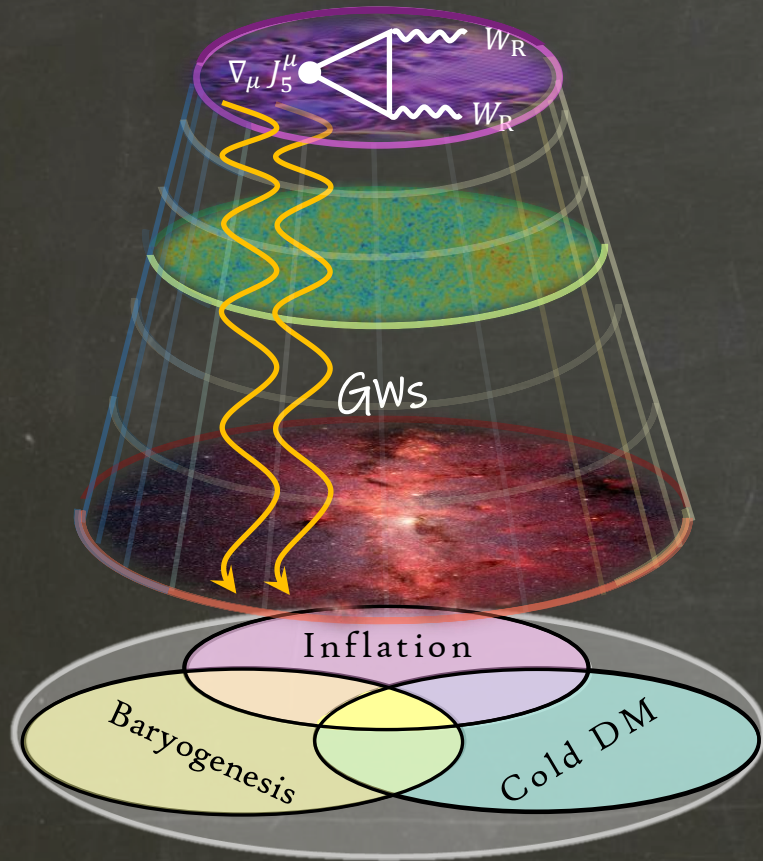
Setup:



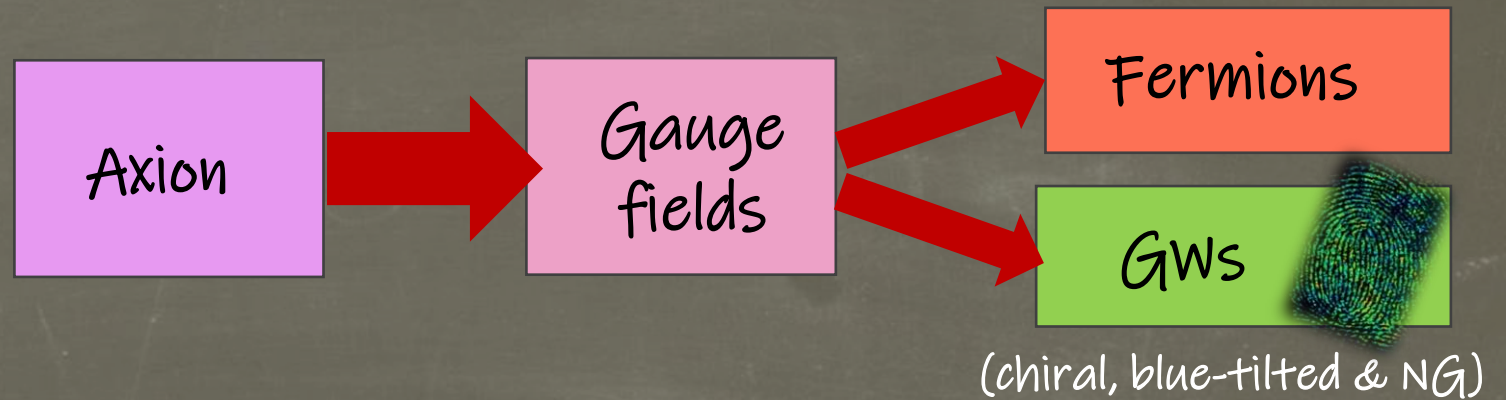
I) Axion-inflation and gauge fields



Setup:



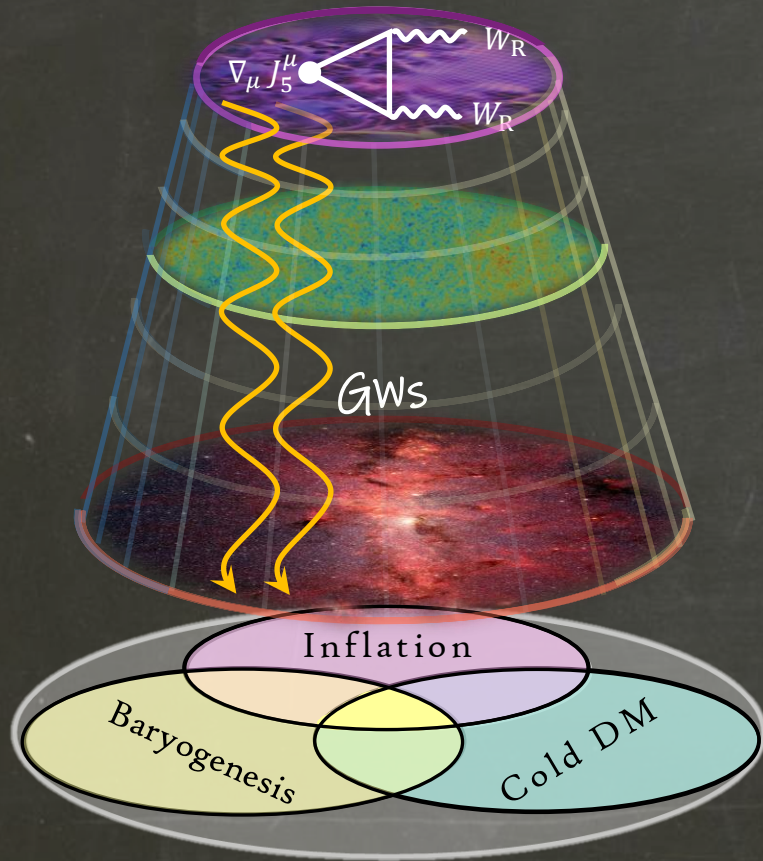
I) Axion-inflation and gauge fields



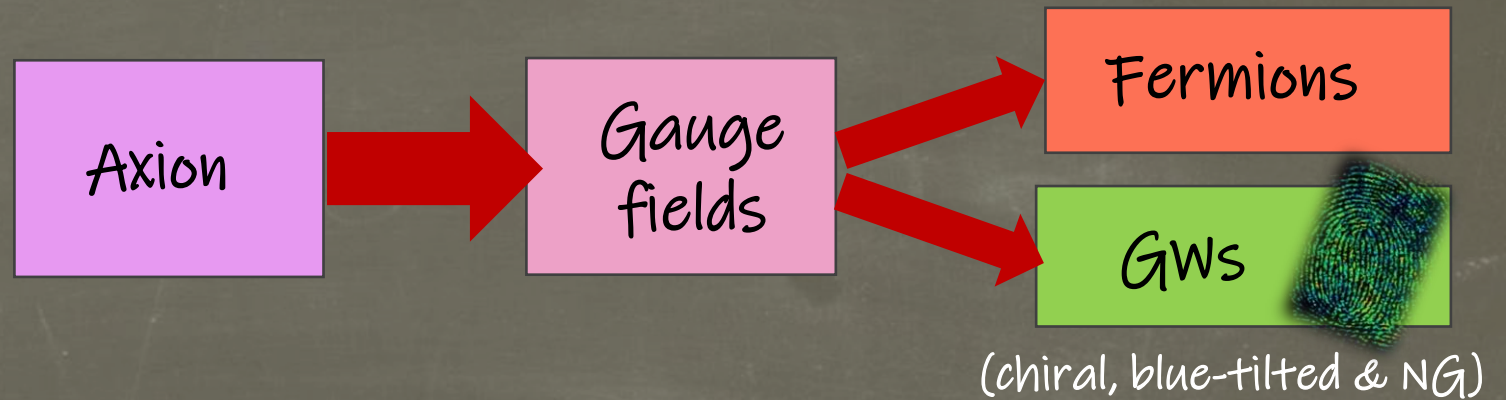
II) Embedding inflation in Left-Right symmetric model

Based on
arXiv:2012.11516 & arXiv:2103.14611

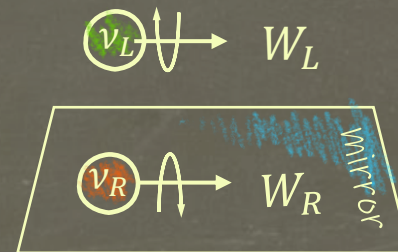
Setup:



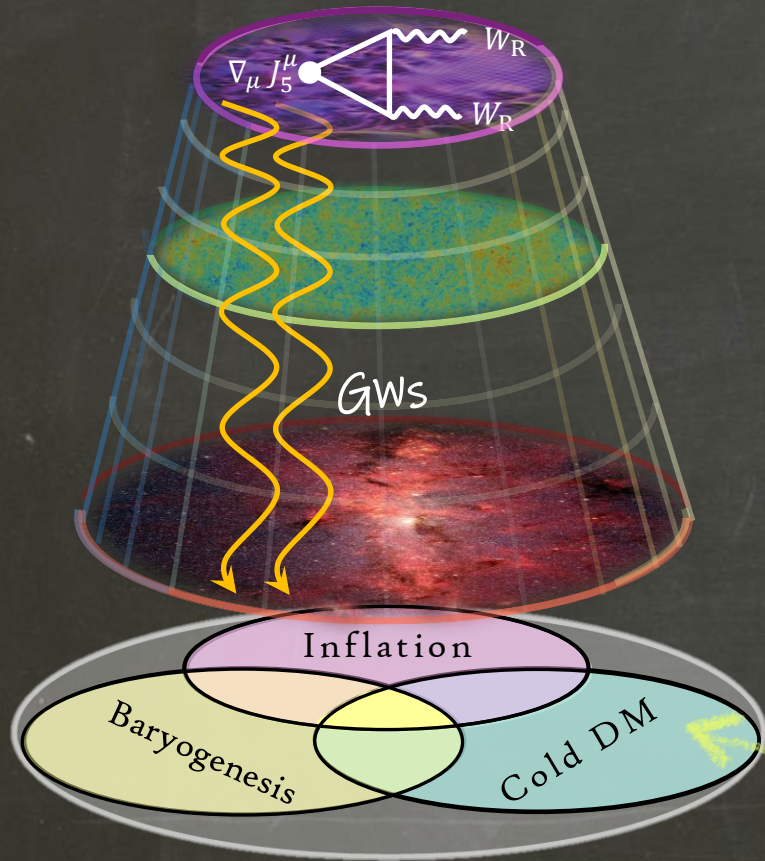
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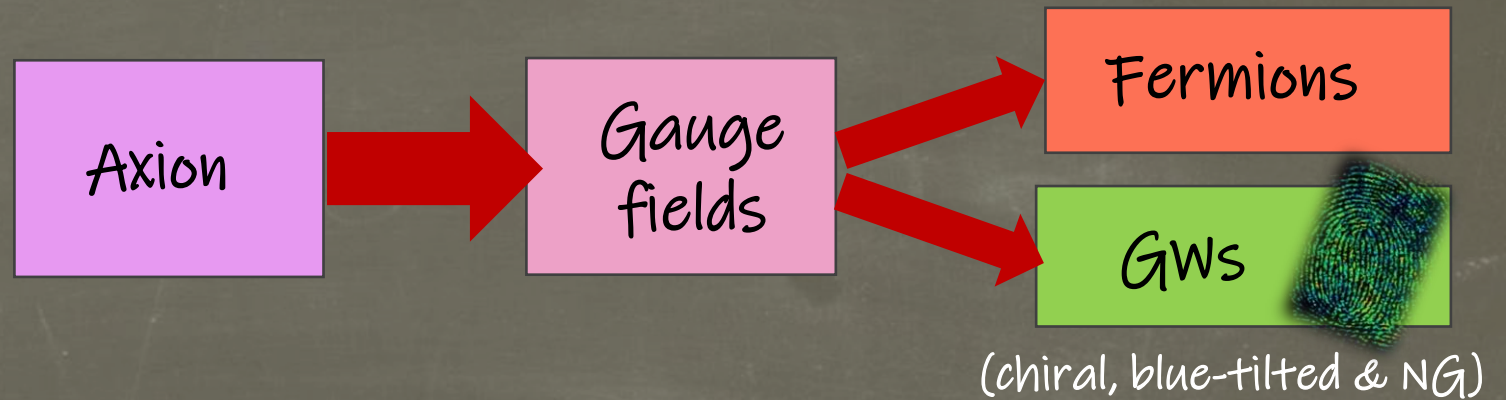
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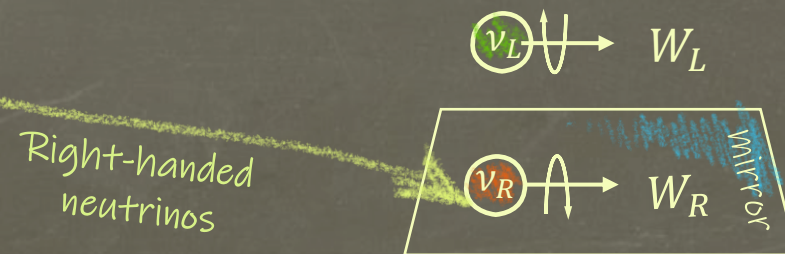
Setup:



I) Axion-inflation and gauge fields



II) Embedding inflation in Left-Right symmetric model



Cosmic Inflation

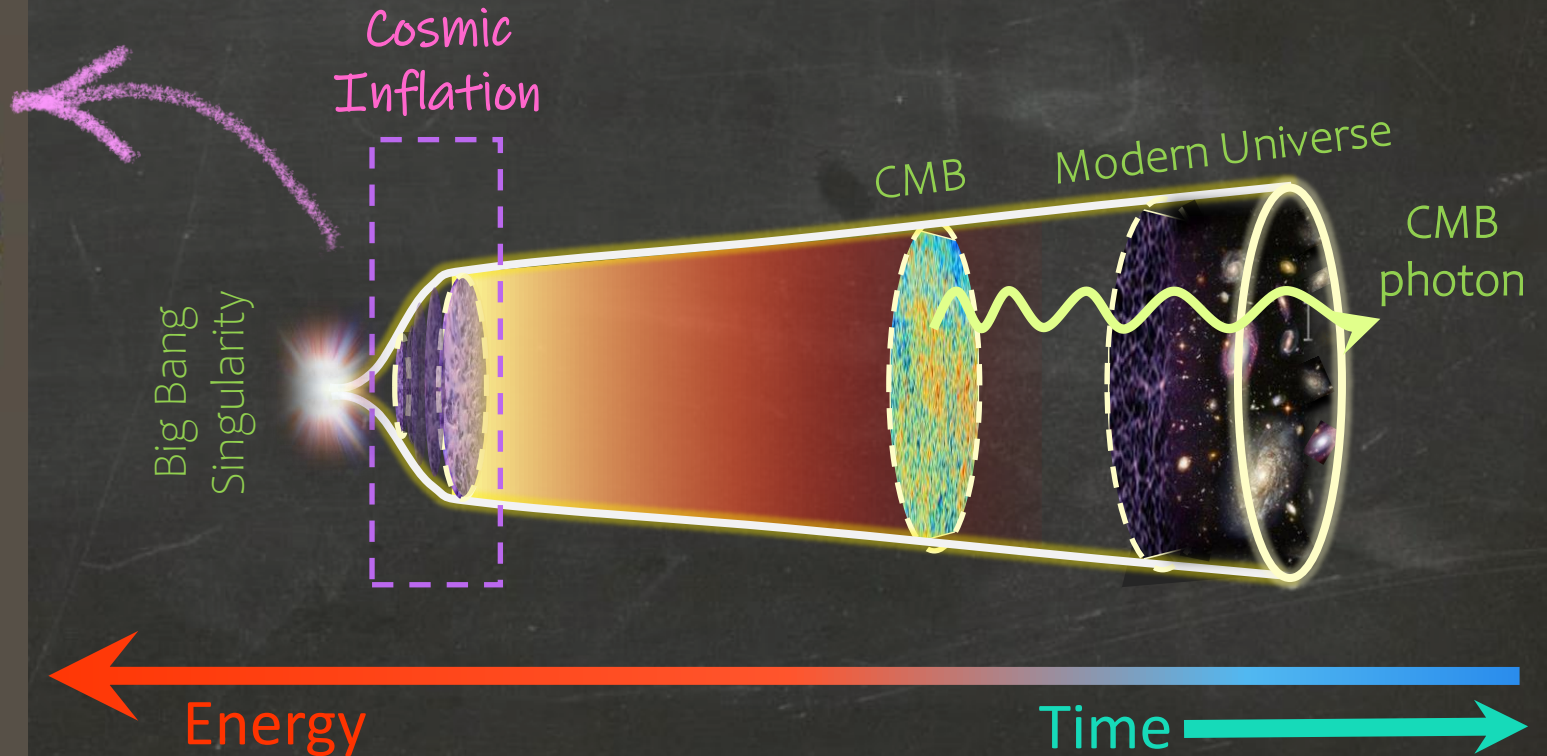
A period of exponential expansion of space shortly after the Big Bang



$$\frac{a_f}{a_i} = e^{60} \approx 10^{26}!$$

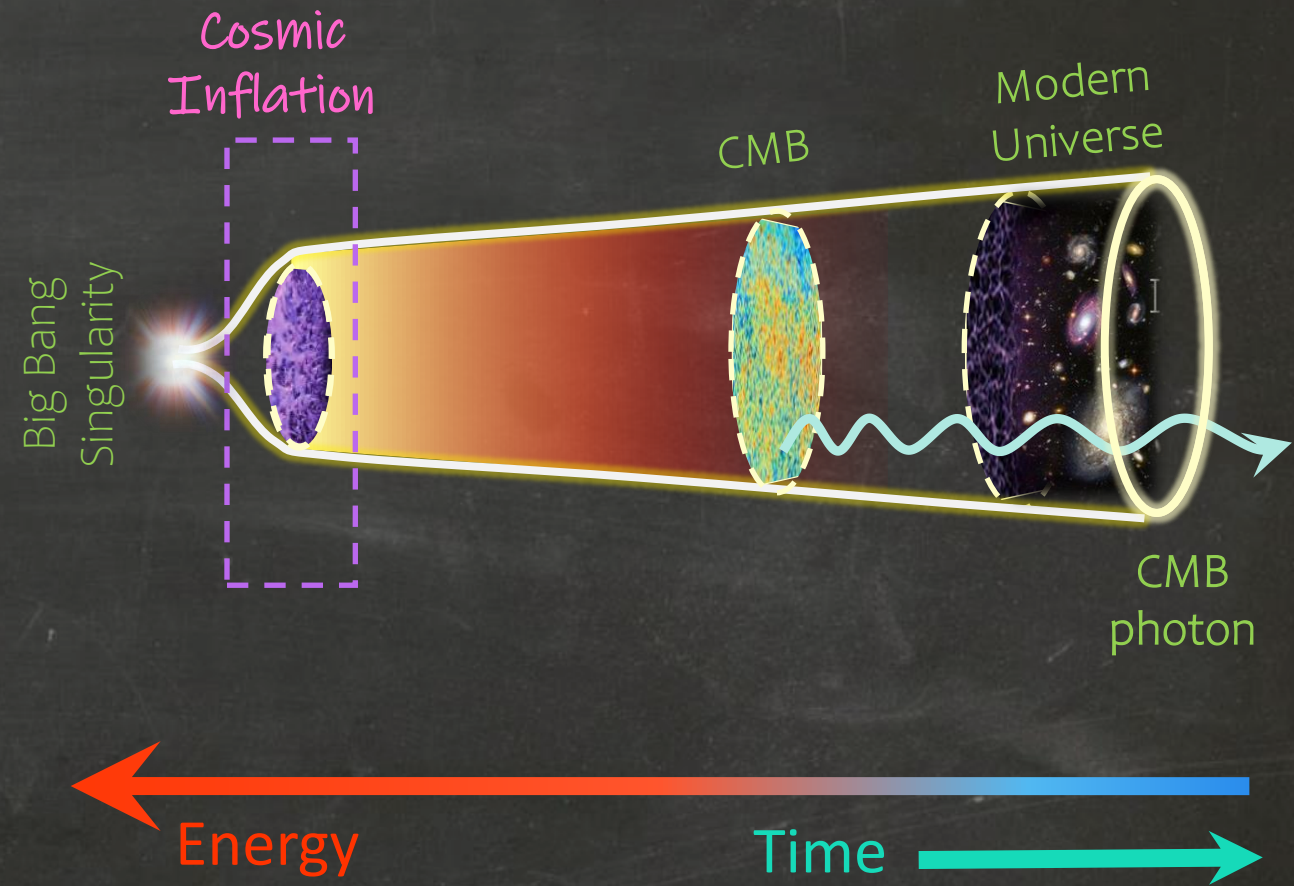
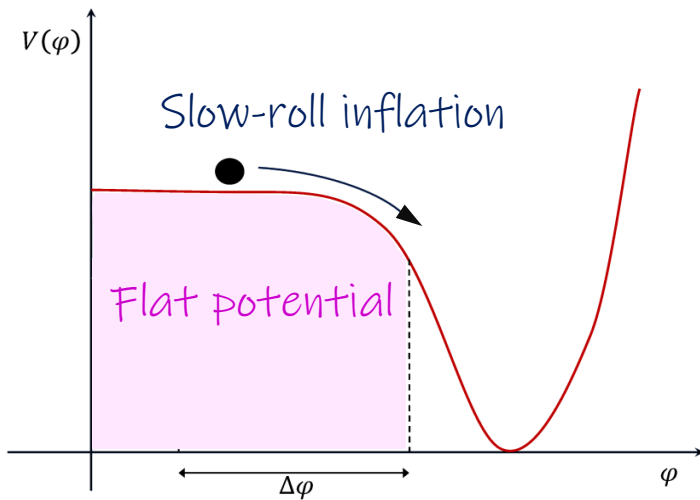
Guth Phys. Rev. D23 (1981)

Linde Phys. Lett. B 108 (1982)



What caused inflation?

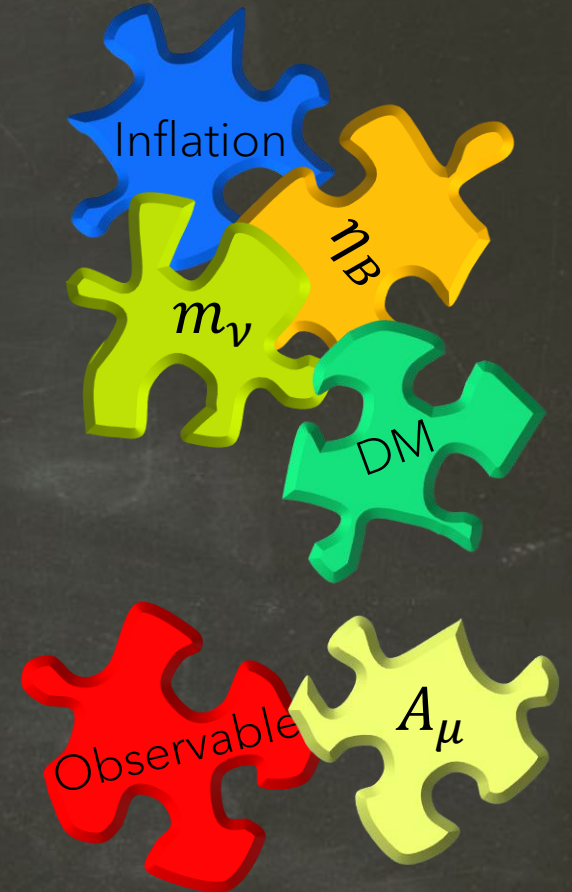
A *scalar field* “slow-rolling” toward its true vacuum provides a simple model for inflation.



Puzzles of SM & Cosmology

- I) Particle physics of Inflation
- II) Origin of matter asymmetry
- III) Origin of Neutrino mass
- IV) Particle nature of DM

Puzzles of
Standard Model of Particle Physics (SM)
& Cosmology Which need
Physics Beyond SM



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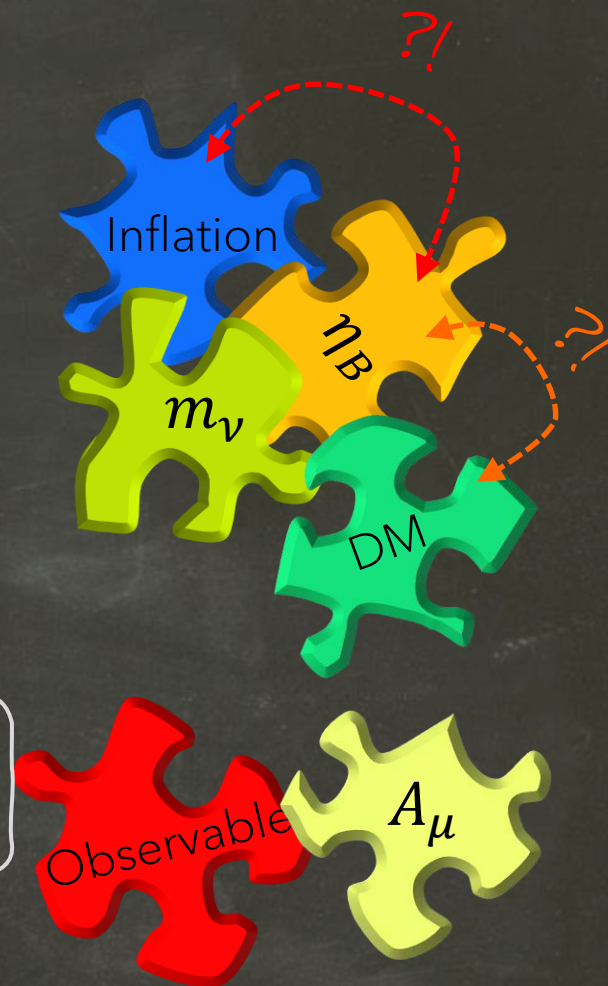
Curious cosmological coincidences $\eta_B \simeq 0.3 P_\zeta$ and $\Omega_{DM} \simeq 5\Omega_B$!

$$\eta_B = \frac{n_B - n_{\bar{B}}}{n_\gamma} \approx 6 \times 10^{-10}$$

Baryon to Photon Ratio Today

$$P_{\zeta} = \frac{1}{2\epsilon} \left(\frac{1}{2\pi} \frac{H}{M_{pl}} \right)^2 \approx 2 \times 10^{-9}$$

Curvature Power Spectrum in Inflation



Puzzles of SM & Cosmology

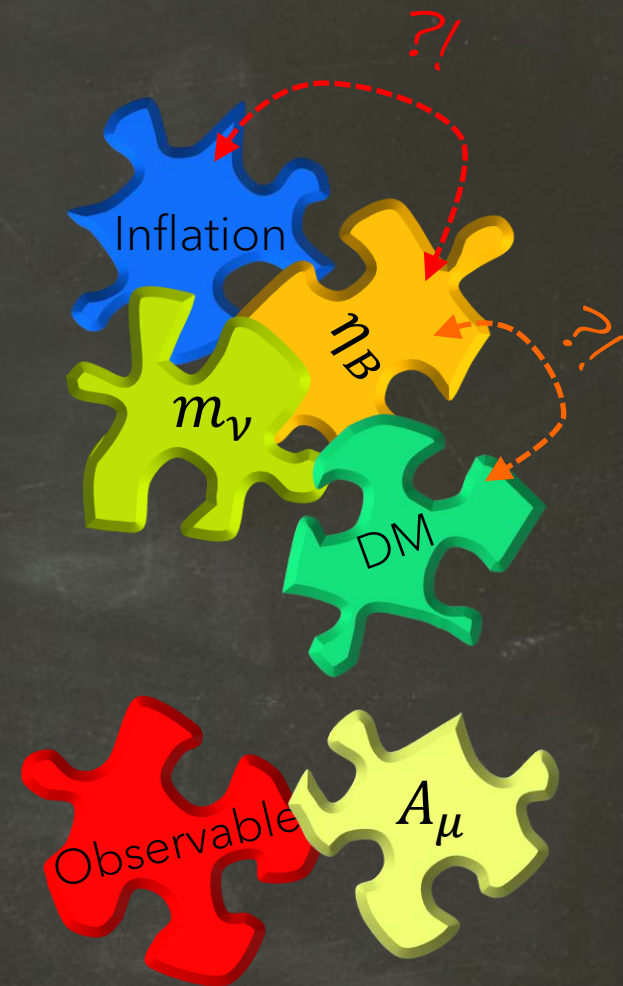
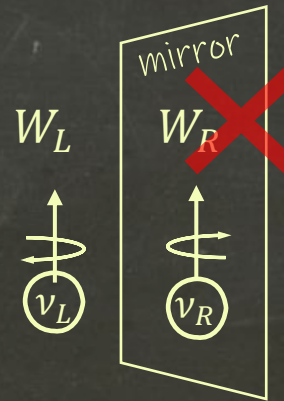
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Puzzles of
Standard Model of Particle Physics (SM)
& Cosmology Which need
Physics Beyond SM

Curious cosmological coincidences $\eta_B \simeq 0.3 P_z$ and $\Omega_{DM} \simeq 5\Omega_B$!

- 1. Ad hoc parity violation
- 2. Accidental B-L global symmetry
- 3. Vacuum Stability problem

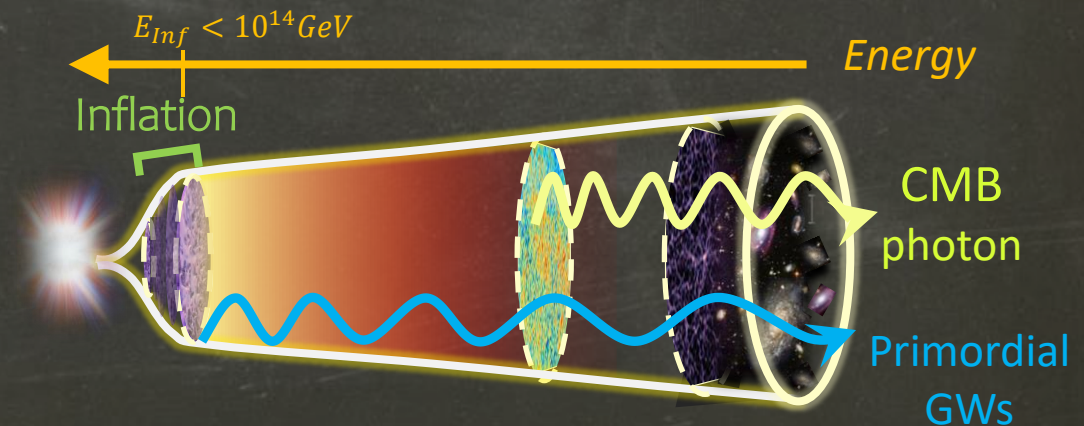
SM as a particle physics model
also faces some *conceptual* issues



As Yet

- Observations are in perfect agreement with Inflation.
- The Particle Physics of Inflation is still unknown.
- The Standard models of inflation are based on Scalars.

Inflation Particle Physics: a scalar field beyond the SM.



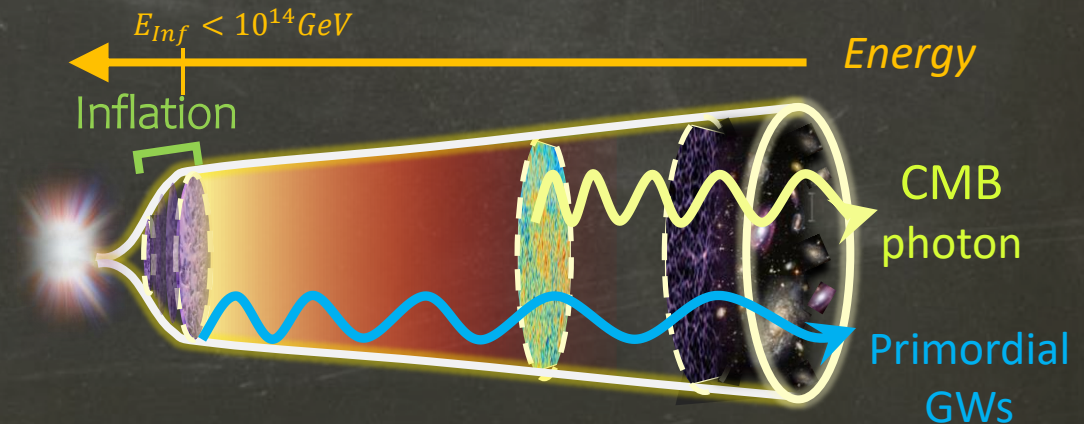
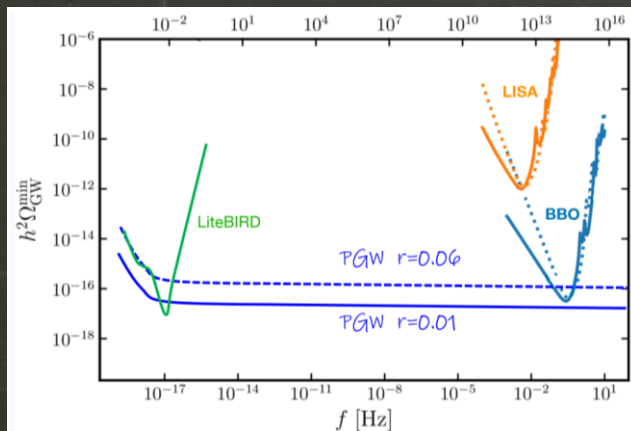
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Inflation Particle Physics: *a scalar field beyond the SM.*

- Primordial Gravitational Waves (PGW):

Vacuum fluctuations: unpolarized, red-tilted, and nearly Gaussian.

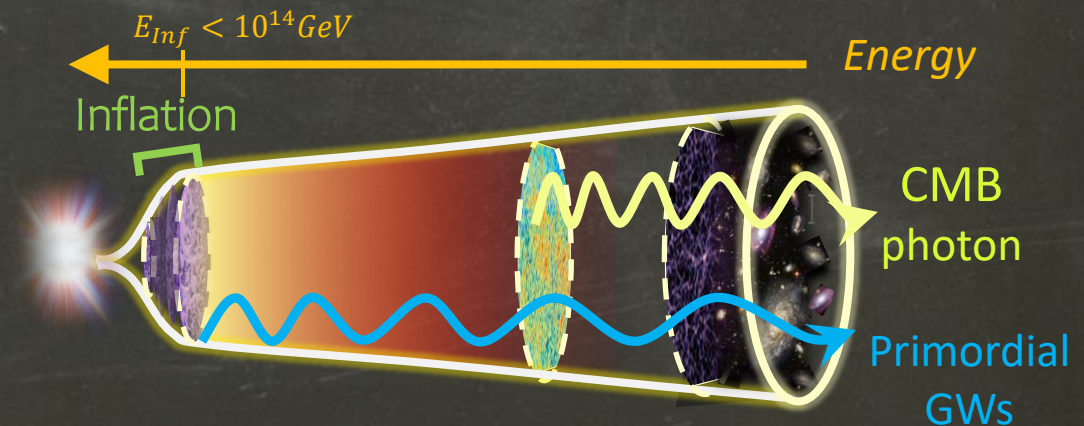


As Yet

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- The Particle Physics of Inflation is still unknown.
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What about Gauge Fields?!

- Inflation happened at highest energy scales observable!
- They are building blocks of particle physics, SM & beyond.
- What do they do in inflation?!



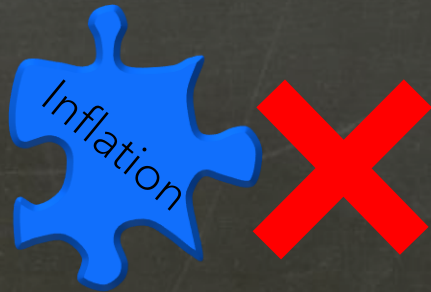
Gauge Fields & Inflation



Challenges:

Gauge fields given by Yang-Mills

dilutes like radiation $A_\mu \sim 1/a$

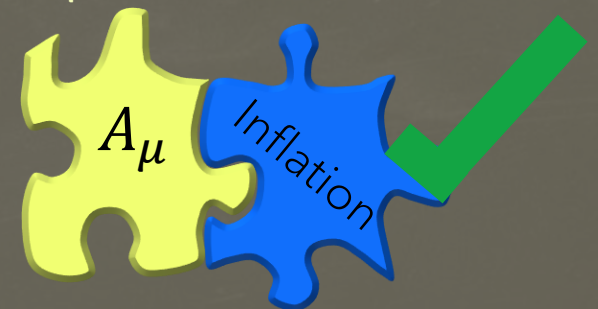


Gauge fields coupled to inflaton
are generated in inflation.

$$\frac{\lambda}{8f} F \tilde{F} \varphi \quad \text{Axion}$$

(Axion fields are naturally
coupled to gauge fields.)

Gauge field A_μ
(active in inflation)



Challenges:

Gauge fields given by Yang-Mills

dilutes like radiation $A_\mu \sim 1/a$

Spatial isotropy & homogeneity

U(1) vacuum A_μ

$$A_i = Q(t) \delta_i^3$$



Gauge fields coupled to inflaton
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$$\frac{\lambda}{8f} F \tilde{F} \varphi \quad \text{Axion}$$

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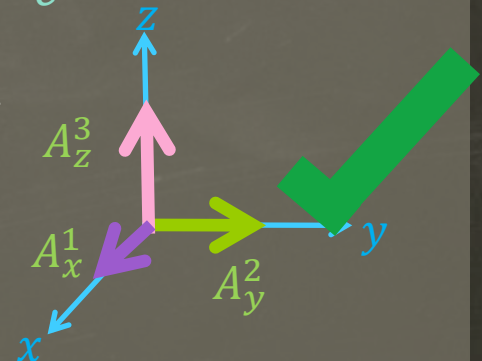
A.M. & Sheikh-Jabbari, 2011

$$\text{SU(2) vacuum } A_\mu = A_\mu^a T_a$$

$$[T_a, T_b] = i \varepsilon^{abc} T_c$$

Spatially isotropic

$$A_i^a = Q(t) \delta_i^a$$



so(3) & su(2) are isomorphic

SU(2)-Axion Model Building

- **Gauge-flation** A. M., & Sheikh-Jabbari, 2011

$$S_{Gf} = \int d^4x \sqrt{-g} \left(-\frac{R}{2} - \frac{1}{4} F^2 + \frac{\kappa}{384} (F\tilde{F})^2 \right)$$

- **Chromo-natural** P. Adshead, M. Wyman, 2012

$$S_{Cn} = \int d^4x \sqrt{-g} \left(-\frac{R}{2} - \frac{1}{2} \left((\partial_\mu \varphi)^2 - \mu^4 \left(1 + \cos\left(\frac{\varphi}{f}\right) \right) \right) \right) - \frac{1}{4} F^2 - \frac{\lambda}{8f} \varphi F\tilde{F}$$

Inspired by them, several different models with SU(2) fields have been proposed & studied.

An incomplete list of Different Realizations of the $SU(2)$ -Axion Inflation:

1. **A. M.** and M. M. Sheikh-Jabbari, Phys. Rev. D 84:043515, 2011 [[arXiv:1102.1513](#)]

2. P. Adshead, M. Wyman, Phys. Rev. Lett.(2012) [[arXiv:1202.2366](#)]

3. **A. M.** JHEP 07 (2016) 104 [[arXiv:1604.03327](#)]

4. C. M. Nieto and Y. Rodriguez Mod. Phys. Lett. A31 (2016) [[arXiv:1602.07197](#)]

5. E. Dimastrogiovanni, M. Fasiello, and T. Fujita JCAP 1701 (2017) [[arXiv:1608.04216](#)]

6. P. Adshead, E. Martinec, E. I. Sfakianakis, and M. Wyman JHEP 12 (2016) 137 [[arXiv:1609.04025](#)]

7. P. Adshead and E. I. Sfakianakis JHEP 08 (2017) 130 [[arXiv:1705.03024](#)]

8. R. R. Caldwell and C. Devulder Phys. Rev. D97 (2018) [[arXiv:1706.03765](#)]

9. E. McDonough, S. Alexander, JCAP11 (2018) 030 [[arXiv:1806.05684](#)]

10. L. Mirzaghali, E. Komatsu, K. D. Lozanov, and Y. Watanabe, [[arXiv:2003.04350](#)]

11. Y. Watanabe, E. Komatsu, [[arXiv:2004.04350](#)]

12. J. Holland, I. Zavala, G. Tasinato, [[arXiv:2009.00653](#)]

13.

A. M. , **$SU(2)$ R –axion inflation** [[arXiv:2012.11516](#)]

Oksana Iarygina, Evangelos I. Sfakianakis, [[arXiv:2105.06972](#)]

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SU(2)-Axion inflation has a very rich phenomenology:

- A new mechanism for generation of Primordial Gravitational Waves
- All Sakharov conditions are satisfied in inflation: a new baryogenesis mechanism
- Particle Production in inflation by Schwinger effect and chiral anomaly

P. Adshead et. al 2013

Dimastrogiovanni et. al 2013

A. M. et. al, 2013

A. M. 2014 & A.M. 2016

R. Caldwell et. al 2017

K. Lozanov, A. M, E. Komatsu 2017,

L. Mirzaghali, A. M, K. Lozanov 2019,

Domcke et al 2019, A.M. 2019

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Axion Monodromy or any mechanism that gives a flat potential

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New Tensorial mode in SU(2) Gauge Field

- $\delta A_i^a = (B_+(t, k)e_{ij}^+(\vec{k}) + B_-(t, k)e_{ij}^-(\vec{k})) \delta_j^a$

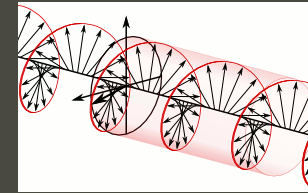
$$B_{\pm}'' + \underbrace{\left[k^2 \mp \delta_c k \mathcal{H} + \frac{m^2}{H^2} \mathcal{H}^2 - \frac{a''}{a} \right]}_{\text{effective frequency}} B_{\pm} \approx 0$$

effective frequency

(δ_c and $\frac{m^2}{H^2}$ are positive, given by BG)

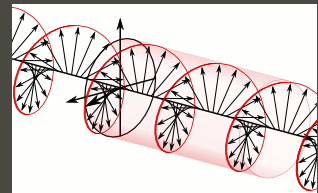
Right-handed

Circular polarizations



B_+

Left-handed



B_-

$B_{\pm}$ is a new tensorial mode in the perturbed SU(2) gauge field!

A.M. & Sheikh-Jabbari, 2011

Vacuum structure

Axion field $\langle \phi \rangle$

($\delta_c > 0$)

Slow-roll A

Slow-roll A_p

Parity

($\delta_c < 0$)

New Tensorial mode in SU(2) Gauge Field

- $\delta A_i^a = (B_+(t, k)e_{ij}^+(\vec{k}) + B_-(t, k)e_{ij}^-(\vec{k})) \delta_j^a$

$$B_{\pm}'' + \underbrace{\left[k^2 \mp \delta_c k \mathcal{H} + \frac{m^2}{H^2} \mathcal{H}^2 - \frac{a''}{a} \right]}_{\text{effective frequency}} B_{\pm} \approx 0$$

(δ_c and $\frac{m^2}{H^2}$ are positive, given by BG)

For $\delta_c > 0$

Short tachyonic growth of B_+



Chiral Field

$$n_B \sim \frac{H^3}{6\pi^2} \delta_c^3 e^{\frac{(2-\sqrt{2})\pi}{2} \delta_c}$$

Particle Production

A. M. and E. Komatsu, 2018

Vacuum structure

Axion field $\langle \phi \rangle$

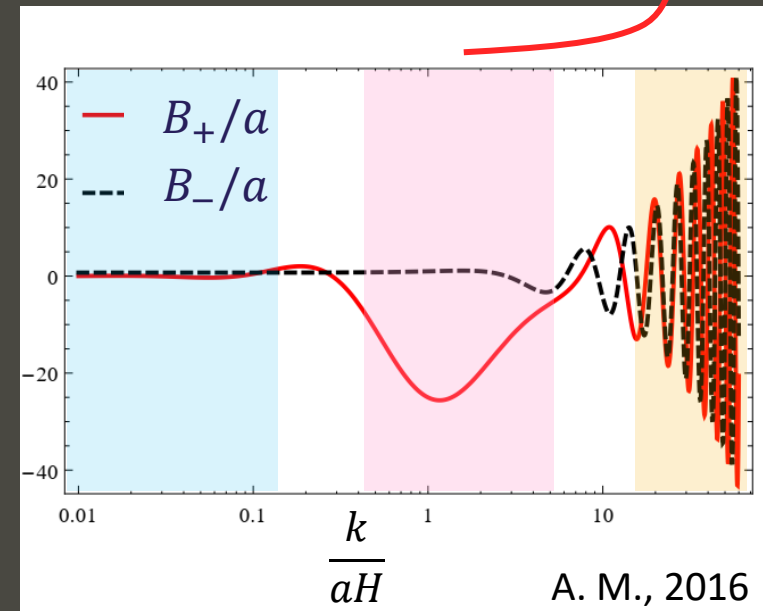
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A. M., 2016

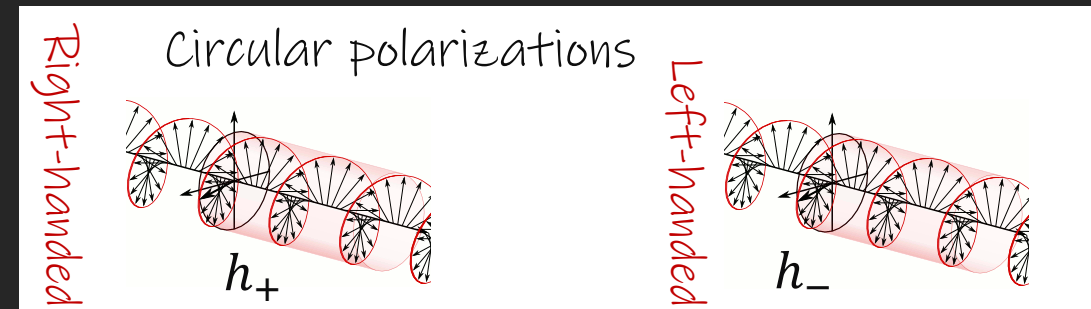
Gauge Field sources Primordial GWs

- $\delta A_i^a = (B_+(t, k)e_{ij}^+(\vec{k}) + B_-(t, k)e_{ij}^-(\vec{k})) \delta_j^a$
- The field equation: $B_\pm'' + [k^2 \mp \delta_c k \mathcal{H} + \frac{m^2}{H^2} \mathcal{H}^2 - \frac{a''}{a}] B_\pm \approx 0$



- That sourced the GWs

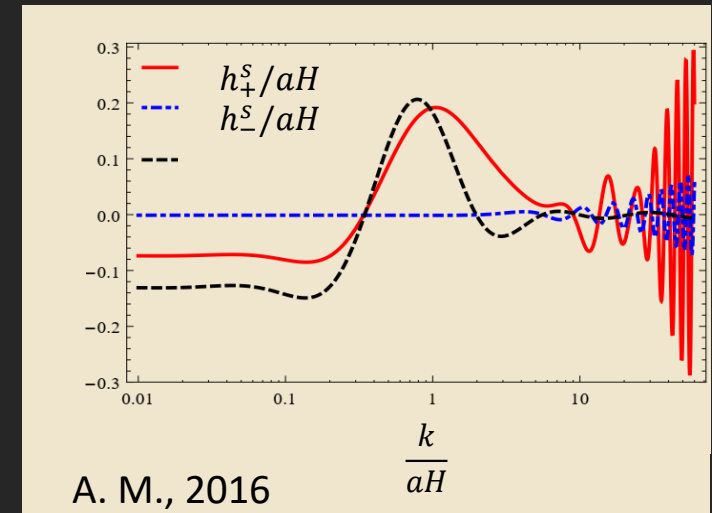
$$h_\pm'' + [k^2 - \frac{a''}{a}] h_\pm = \mathcal{H}^2 \Pi_\pm[B_\pm]$$



- Gravitational waves have two uncorrelated terms



$$h_\pm = \underbrace{h_\pm^{vac}}_{\substack{\text{Vacuum GWs} \\ \text{unpolarized} \\ h_+^{vac} = h_-^{vac}}} + \underbrace{h_\pm^s}_{\substack{\text{Sourced by } B_\pm \\ \text{Polarized} \\ h_+^s \neq h_-^s}}$$



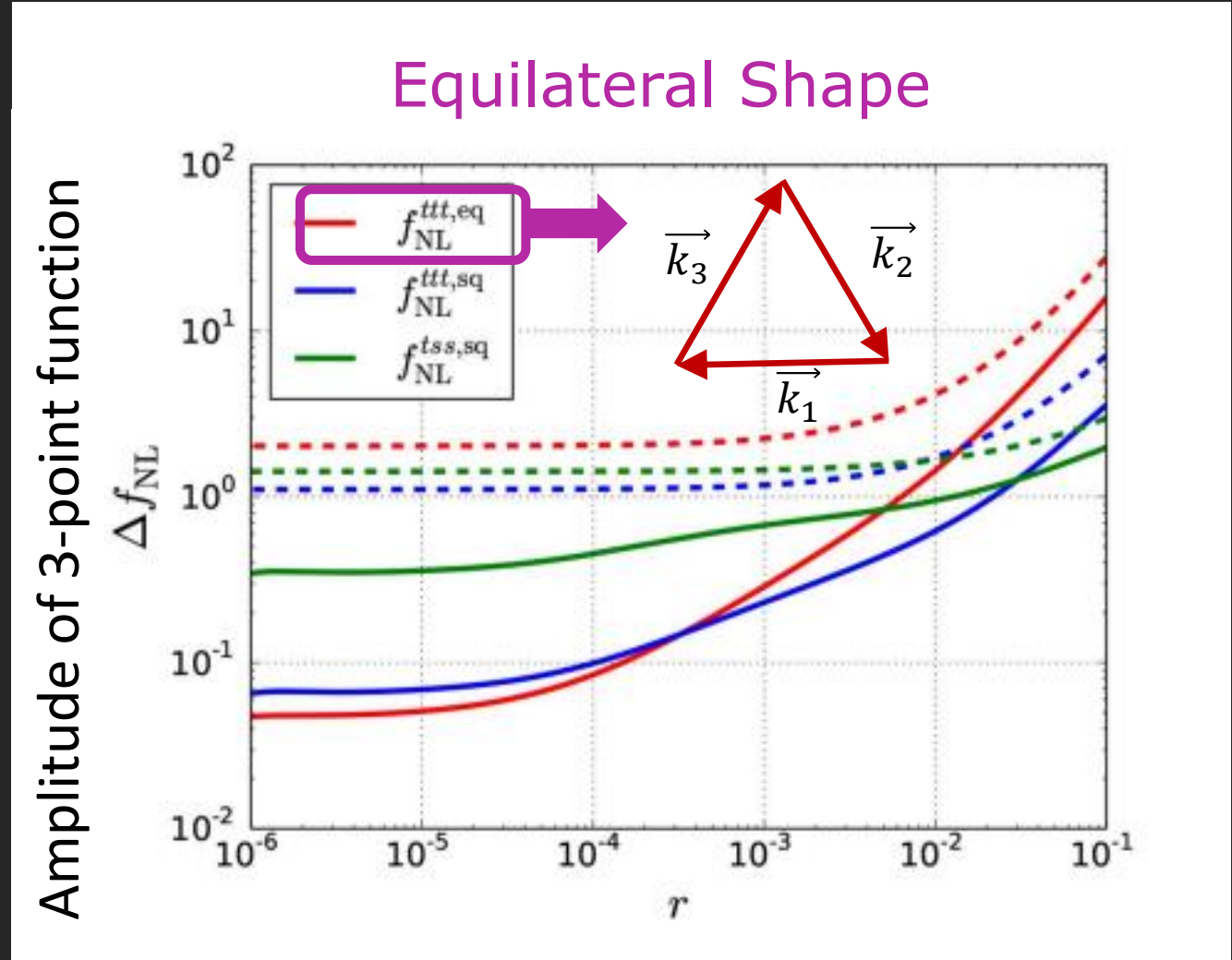
Novel Observable Signature: CMB

- The sourced tensor modes is Highly non-Gaussian.

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu - \underbrace{ig [A_\mu, A_\nu]}_{\text{Self-interaction}}$$

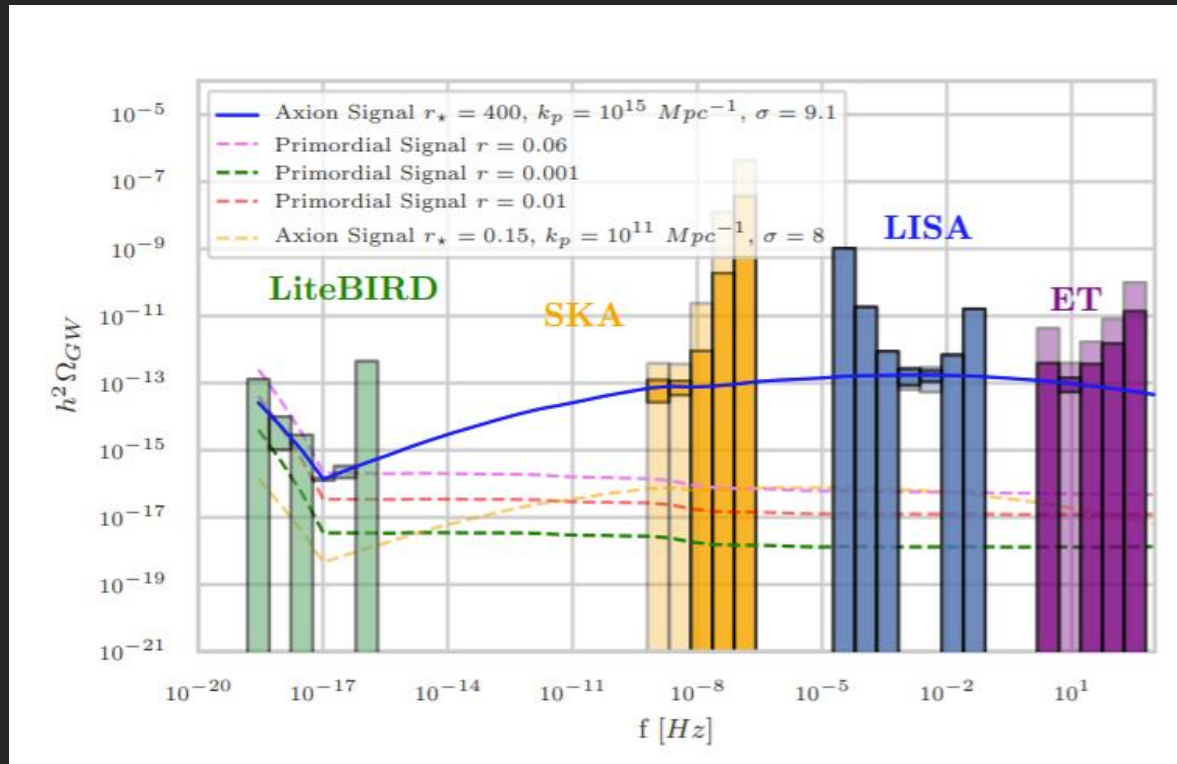
Agrawal, Fujita, Komatsu 2018

- That can be probe with future CMB missions., e.g. *Litebird* and *CMB-S4*!



Novel Observable Signature: Beyond CMB

Detection of this background is an excellent target for all GW experiments across at least 21 decades in frequencies.



P. Campeti, E. Komatsu, D. Poletti, C. Baccigalupi 2020

How to Connect Inflaton to SM?



How to Connect it to the SM?

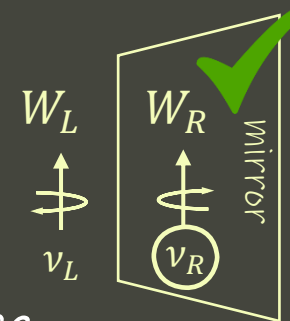
Let us Extend SM Gauge Symmetry by an $SU(2)_R$ and couple it to Axion Inflaton!

- Left-Right Symmetric Model + axion!

$$SU(2)_R \times SU(2)_L \times U(1)_{B-L} \longrightarrow SU(2)_L \times U(1)_Y$$

Left-Right Symmetric

SM Left-handed Weak force



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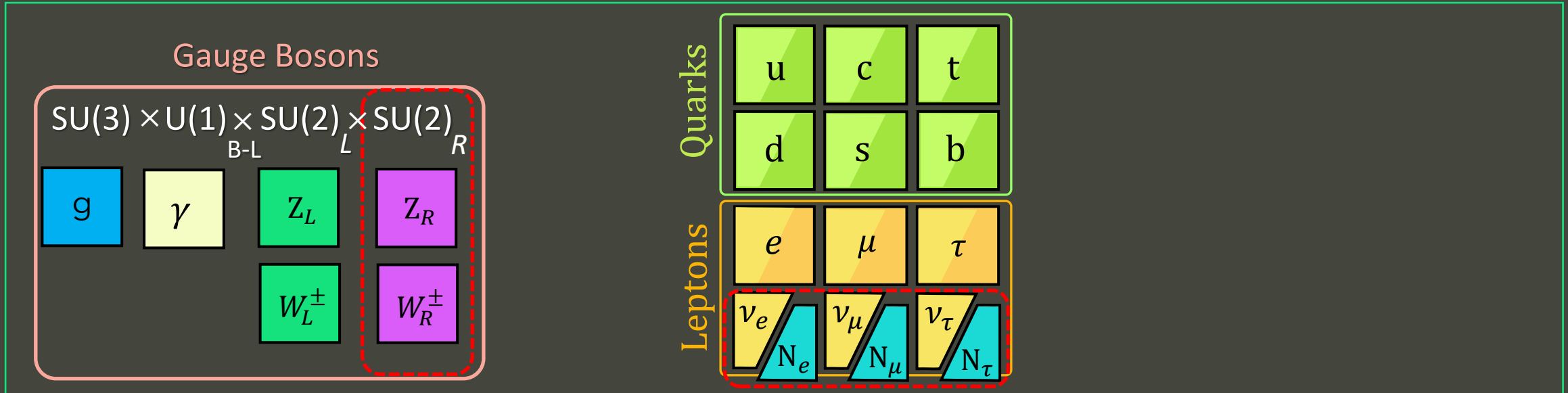
Gauge field is $SU(2)_R$

A. M. arXiv: 2012.11516

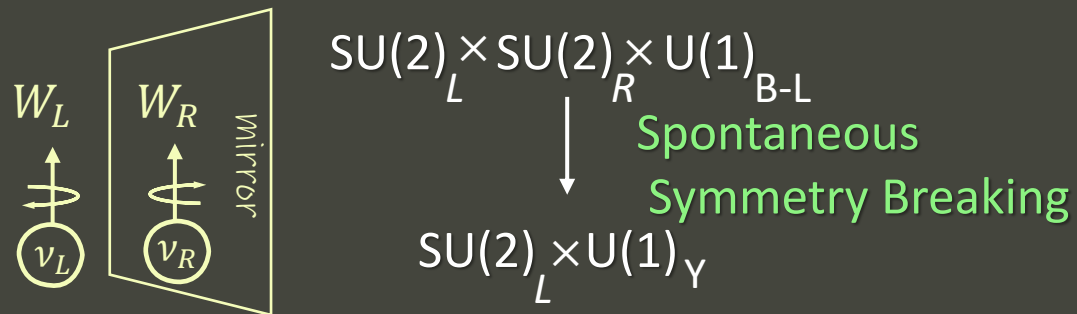
A.M. arXiv:2103.14611

Left-Right Symmetric Model

- An $SU(2)$ -gauge extension of SM with 3 Right-handed Neutrinos coupled to it.

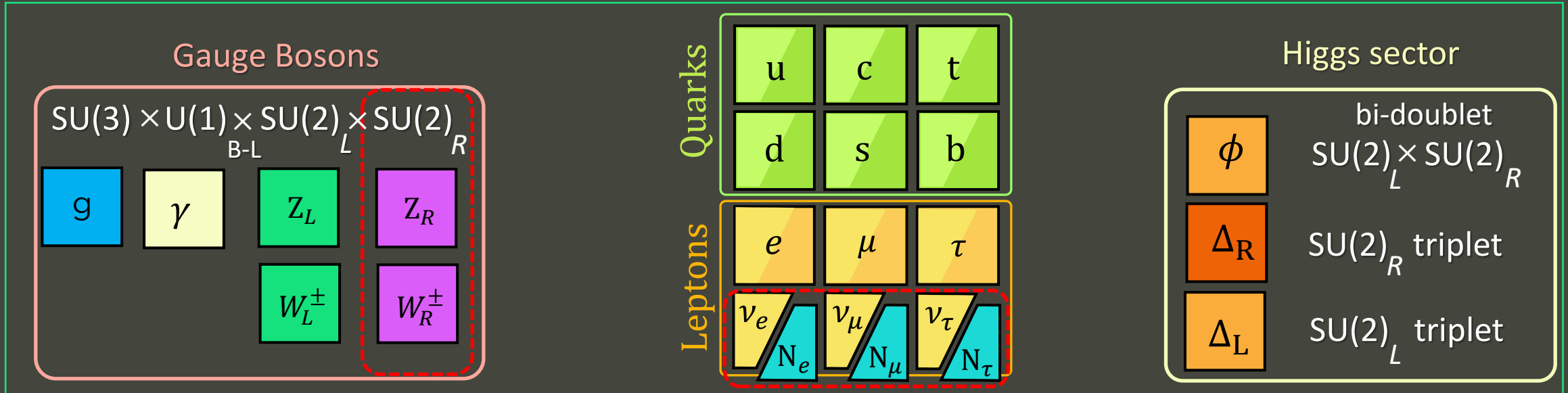


J. C. Pati and A. Salam, Phys. Rev. D 10, 275-289 (1974) R. N. Mohapatra and J. C. Pati, Phys. Rev. D 11, 2558 (1975) G. Senjanovic and R. N. Mohapatra, Phys. Rev. D 12, 1502 (1975)

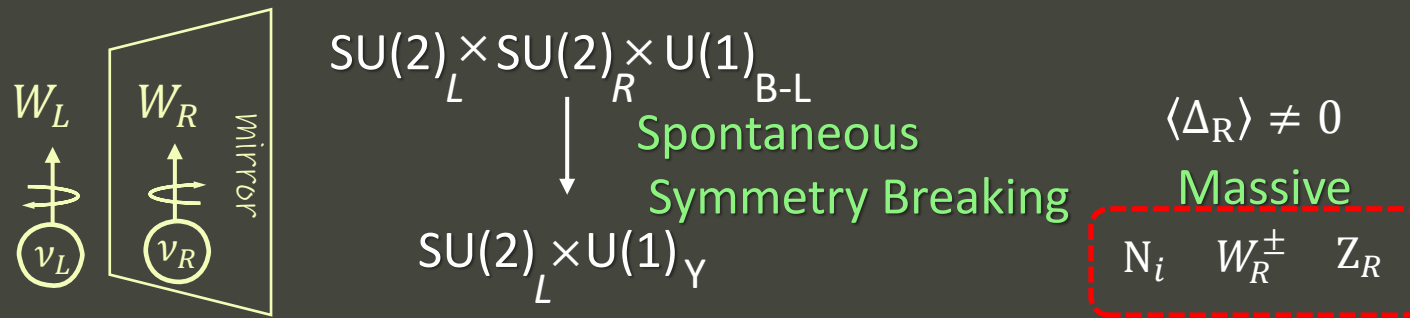


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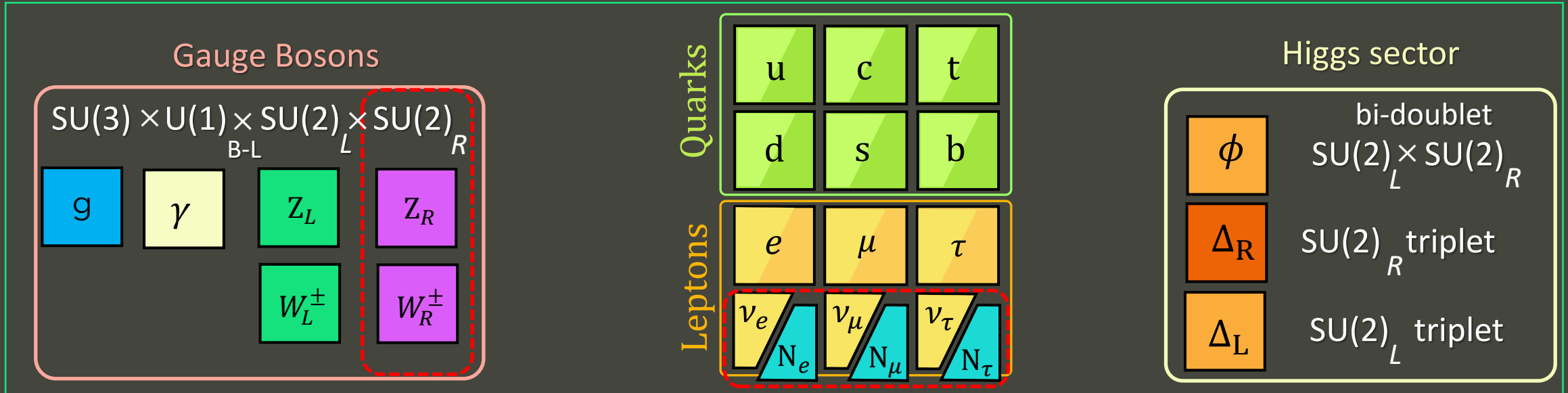


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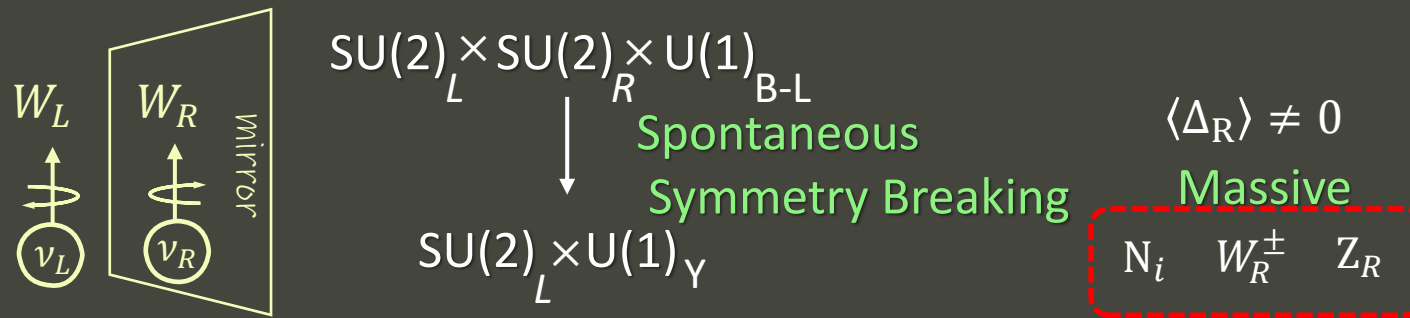


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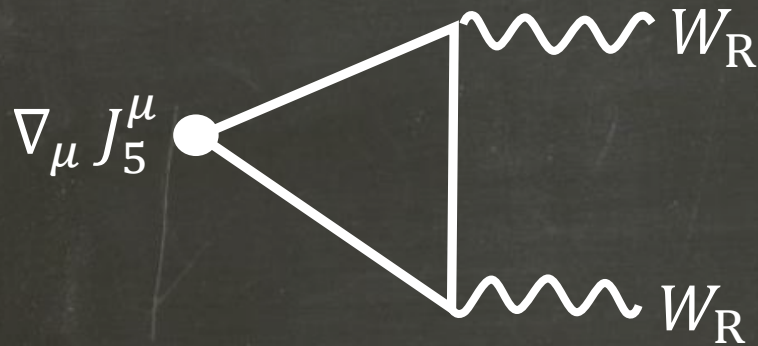
- Ad hoc parity violation
- Accidental B-L global symmetry
- Vacuum Stability problem

Lepton & quark Production in Inflation

- Left-handed fermions are diluted by inflation, BUT
- Right-handed fermions are generated by $SU(2)_R$ gauge field:



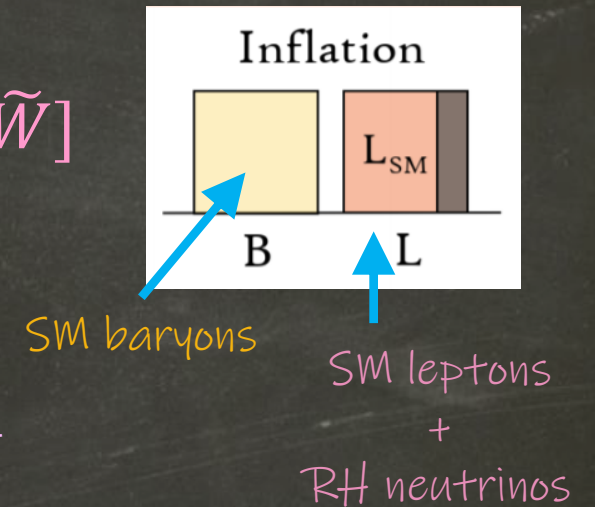
The key ingredient is the Chiral anomaly of $SU(2)_R$ in inflation:



$$\nabla_\mu J_B^\mu = \nabla_\mu J_L^\mu = \frac{g^2}{16\pi^2} \text{tr}[W\tilde{W}]$$

$$n_B = n_L = \alpha_{inf}(\xi) H^3$$

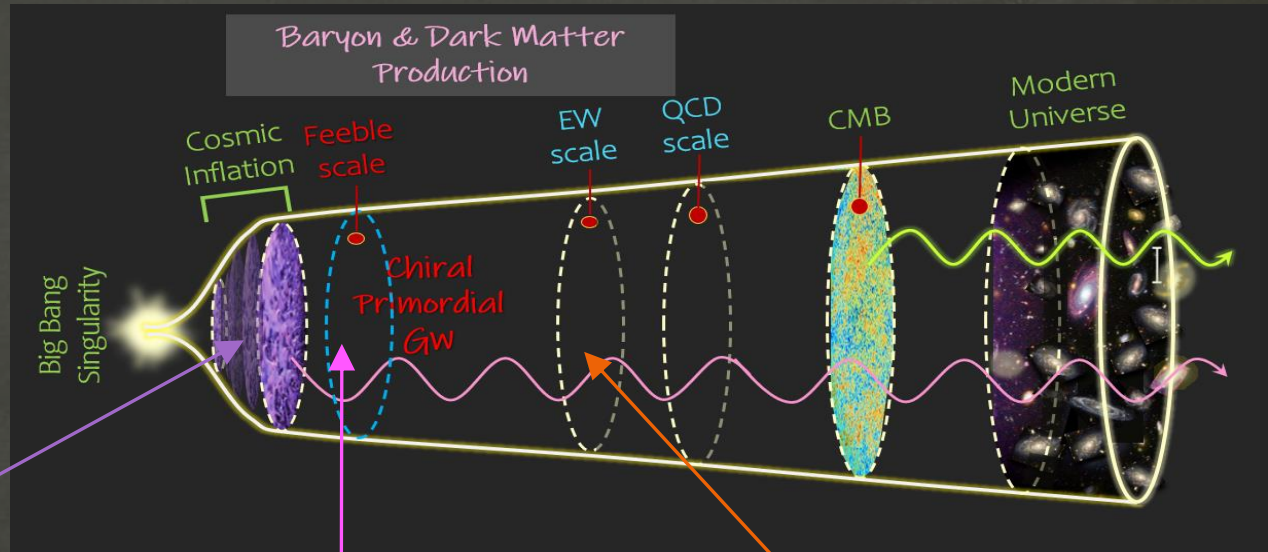
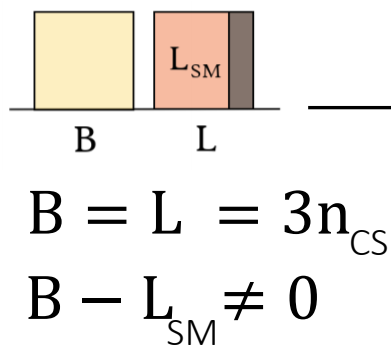
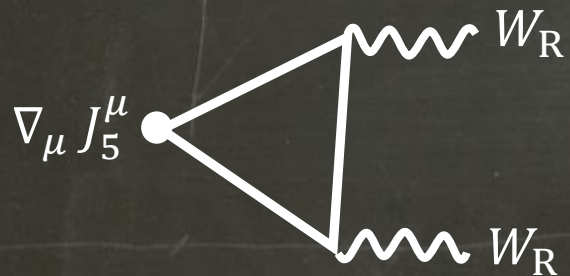
$$\alpha_{inf}(\xi) \sim \frac{g^2}{(2\pi)^4} e^{2\pi\xi}$$



Summary of the mechanism:

Quarks	u	c	t
	d	s	b
Leptons	e	μ	τ
	ν_e N_e	ν_μ N_μ	ν_τ N_τ

Chiral anomaly of $SU(2)_R$ in inflation



Freezeout of N_1

EW scale

$\Omega_{N_1} \approx 2.8 \frac{m_{N_1}}{m_p} \Omega_B$
 $m_{N_1} \simeq 1.8 m_p = 1.7 \text{ GeV.}$
 $\eta_B^0 \approx 3 \left(\frac{g_{\text{eff}}}{100} \right)^{\frac{3}{4}} \frac{\alpha_{\text{inf}}}{(\delta_{\text{reh}})^{\frac{3}{4}}} \left(\frac{H}{M_{\text{Pl}}} \right)^{\frac{3}{2}}$

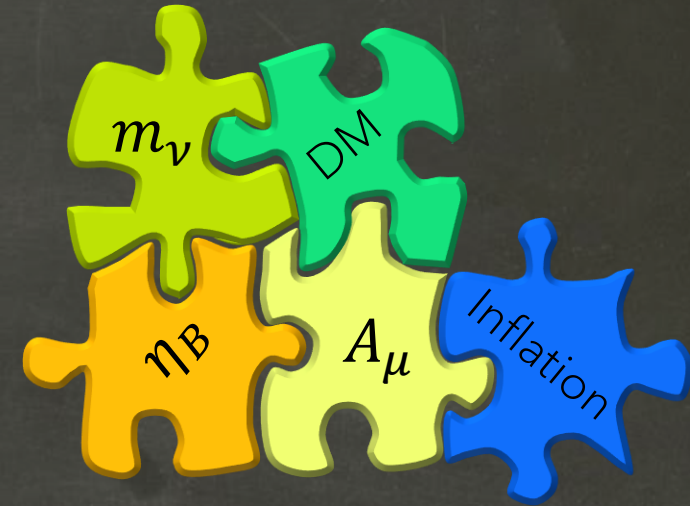
Gauge fields are expected to contribute in physics of axion-inflation.

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Compelling Consequences:

This Set-up is a **complete BSM** that can solve **I-IV**:

- I) Particle physics of Inflation
- II) Origin of matter asymmetry
- III) Origin of Neutrino mass
- IV) Particle nature of DM

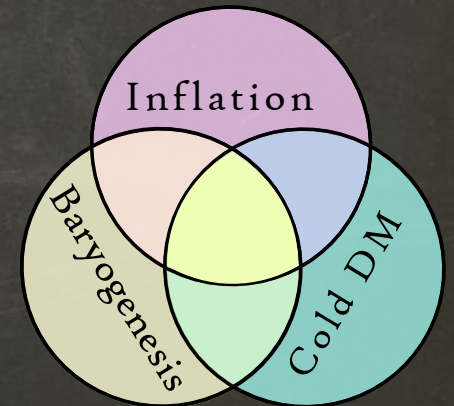
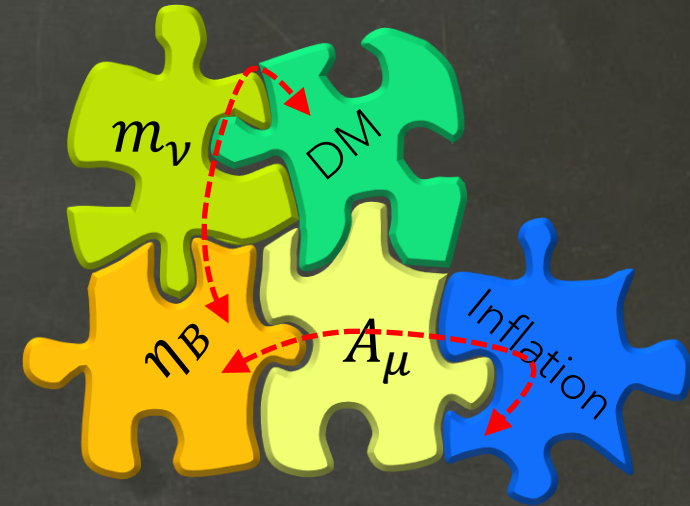


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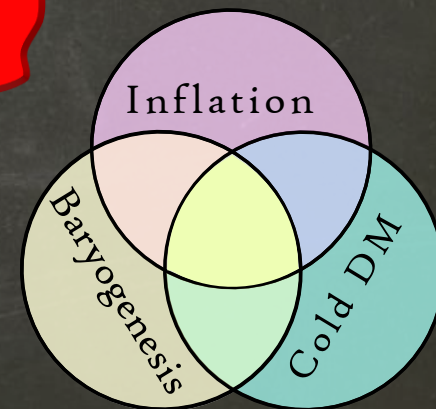
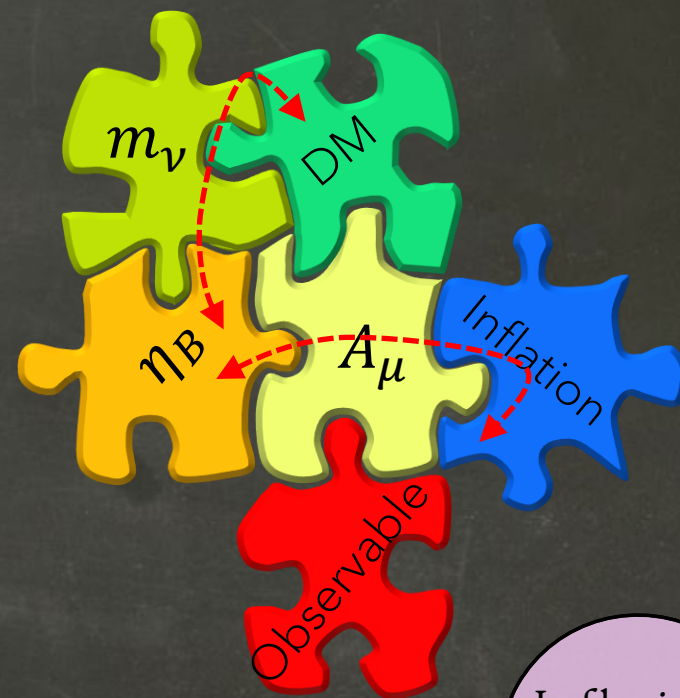
So naturally explains **cosmological coincidences** $\eta_B \simeq 0.3 P_\zeta$ and $\Omega_{DM} \simeq 5\Omega_B$!

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So naturally explains **cosmological coincidences** $\eta_B \simeq 0.3 P_\zeta$ and $\Omega_{DM} \simeq 5\Omega_B$!

It comes with a cosmological smoking gun on **Primordial GW**.

Questions?!

