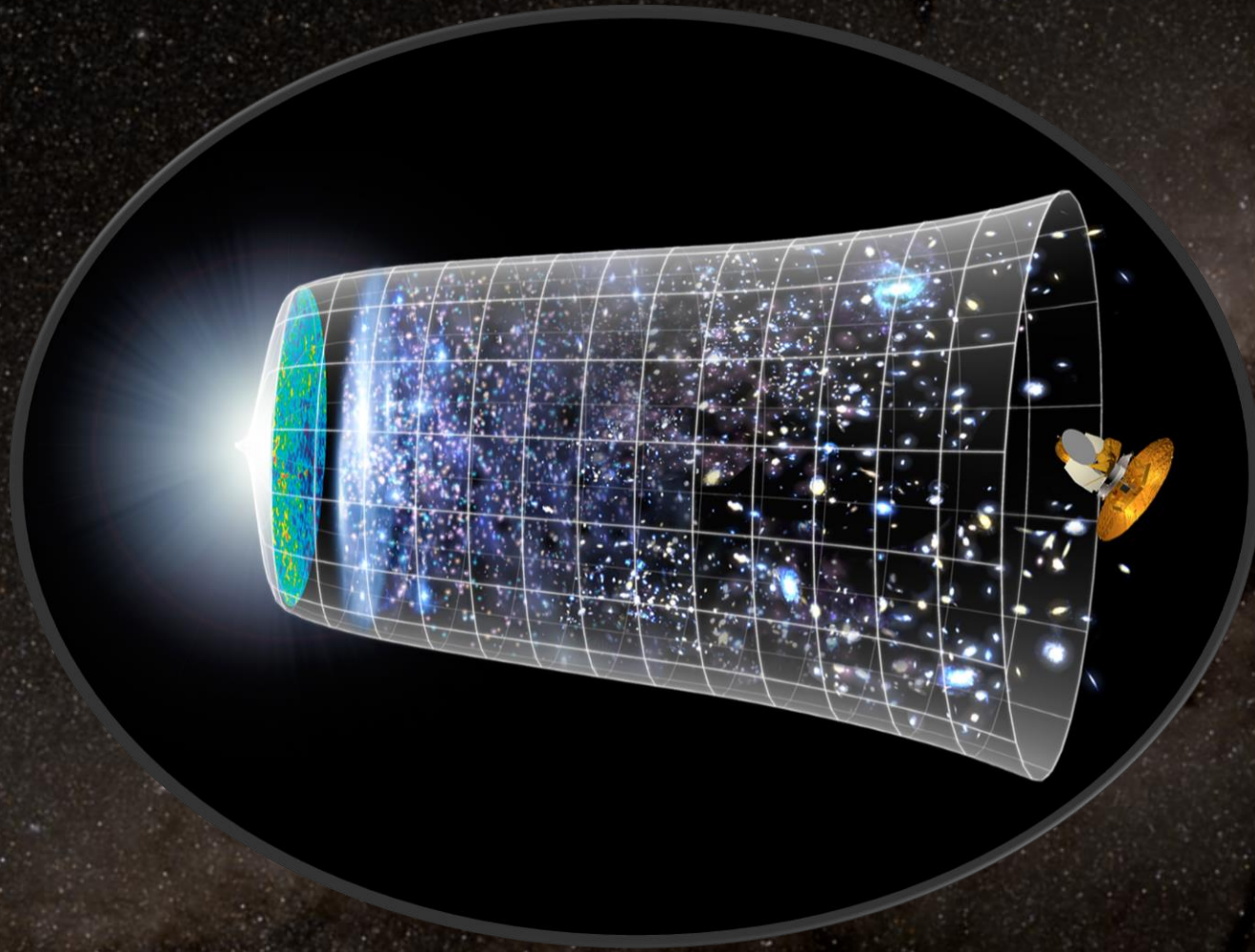


HUBBLE TENSION WITH AN EXTRA RADIATION AND NEUTRINO DEGENERACY

YO TODA

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Osamu Seto, Yo Toda [arXiv:2104.04381](https://arxiv.org/abs/2104.04381) [astro-ph.CO]



The Λ CDM model goes well
in explaining the evolution
of our Universe.

But
Hubble Tension

TODAY I WILL

Focus on the Extra radiation and neutrino degeneracy to solve the Hubble tension

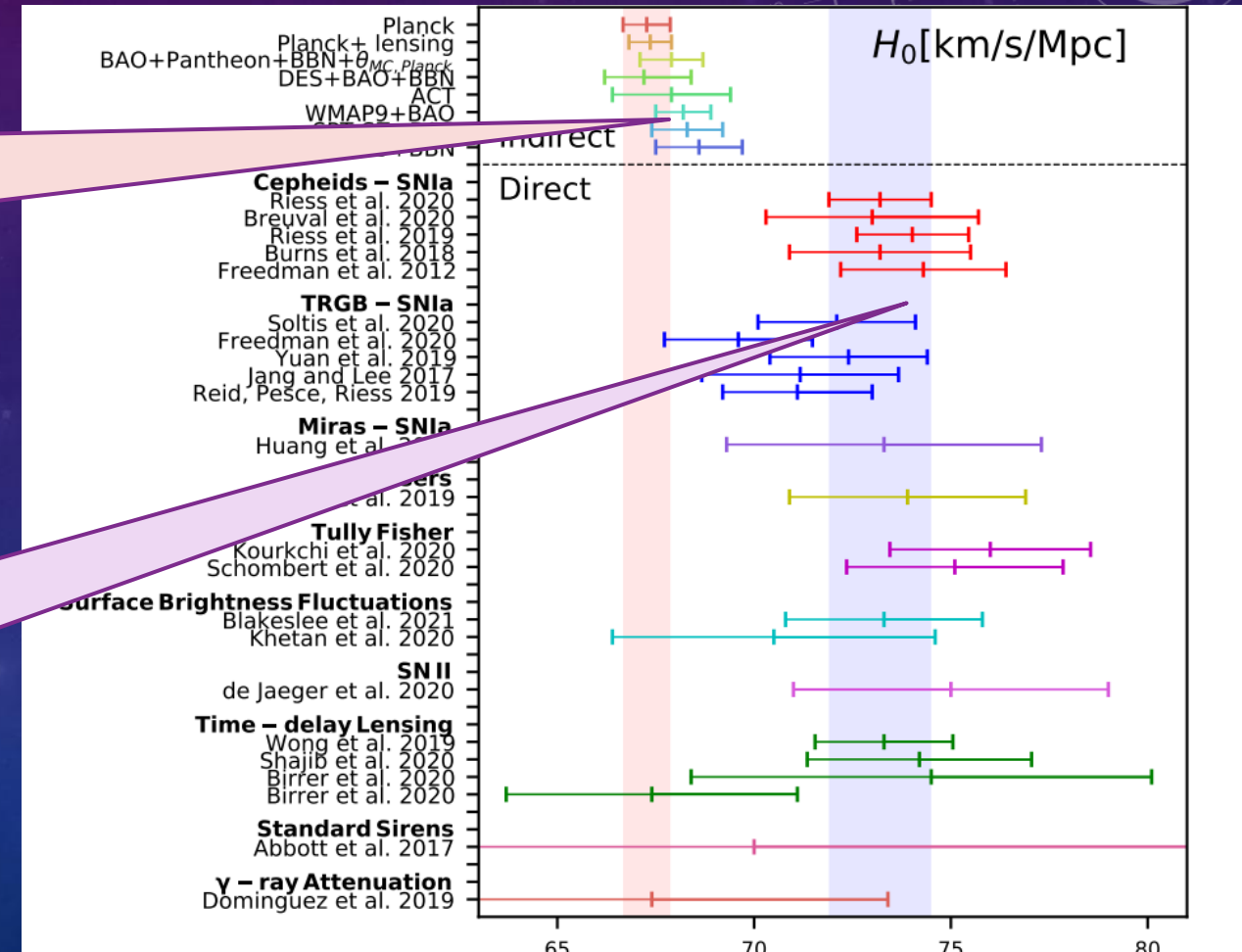
Treat extra radiation parameter N_{eff} as independent of degeneracy ξ because we consider the sterile neutrinos or axions under the degeneracy

Conclude that
the combination of extra radiation and neutrino degeneracy
is the promising solutions

WHAT IS HUBBLE TENSION?

Distant observations suggest
 $H_0 \approx 67$ km/s/Mpc

Local observations suggest
 $H_0 \approx 74$ km/s/Mpc



WHAT IS HUBBLE TENSION?

How is this derived?

Distant observations suggest
 $H_0 \approx 67$ km/s/Mpc

Local observations suggest
 $H_0 \approx 74$ km/s/Mpc

This tension may indicate
Beyond Λ CDM Physics

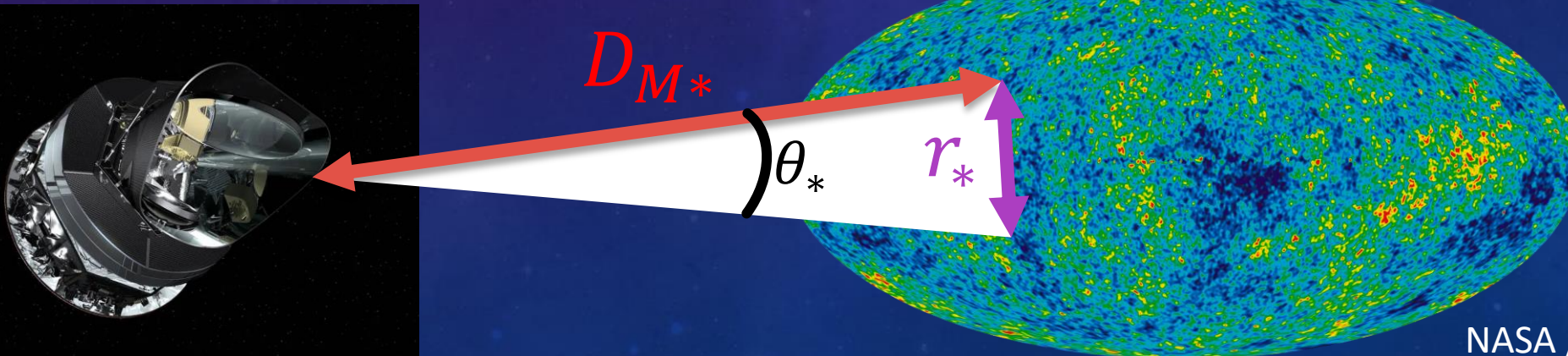
ANGULAR SIZE OF THE SOUND HORIZON

Directly Measured

$$\text{Angular Size : } \theta_* = \frac{r_*}{D_{M*}} = (1.0411 \pm 0.0003) \times 10^{-2}$$

$$r_* = \int_0^{t_*} \frac{c_s d\tilde{t}}{a(\tilde{t})} : \text{comoving sound horizon at the recombination}$$

$$D_{M*} = \int_{t_*}^{t_0} \frac{d\tilde{t}}{a(\tilde{t})} : \text{comoving angular diameter distance}$$



ANGULAR SIZE OF THE SOUND HORIZON

Directly Measured

$$\text{Angular Size : } \theta_* = \frac{r_*}{D_{M*}} = (1.0411 \pm 0.0003) \times 10^{-2}$$

$$\propto H_0 \frac{1}{\sqrt{\rho \text{ in the early universe}}}$$

$$\therefore \frac{dt}{a(t)} = \frac{dz}{H_0 \sqrt{\rho(z)/\rho_0}}$$

ρ : energy density

TO INCREASE H_0 ...

Increase ρ in the early universe

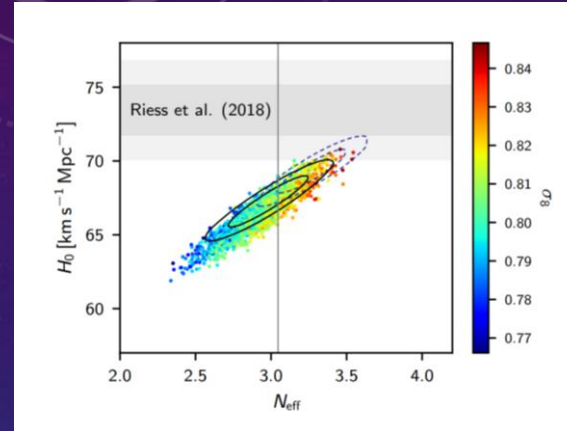
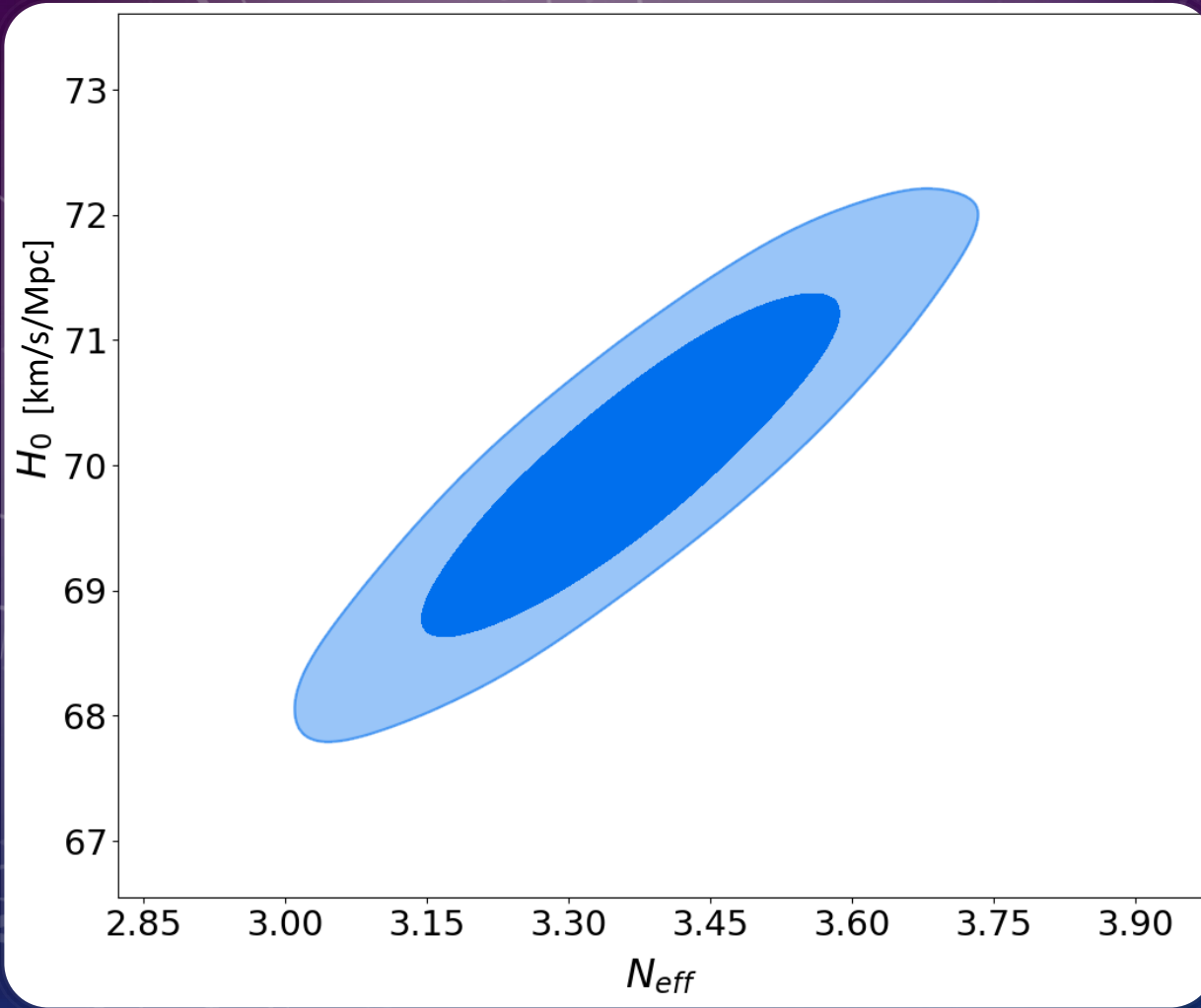
EXTRA RADIATION

The relativistic degrees of freedom N_{eff}
(increased by dark radiation, axion, sterile neutrino ...)

$$\rho_{\text{radiation}} = \left(\underset{\text{photon}}{1} + \frac{7}{8} \left(\frac{4}{11} \right)^{\frac{4}{3}} \underset{\text{Neutrino} + \alpha}{N_{\text{eff}}} \right) * \rho_{\text{photon}}$$

$$N_{\text{eff}} = \underset{\text{neutrino}}{3} + \underset{e^+e^- \text{ annihilation}}{0.046} + (\text{Extra contribution})$$

EXTRA RADIATION RELIEVE THE HUBBLE TENSION



Planck 2018 results VI

arxiv:1807.06209

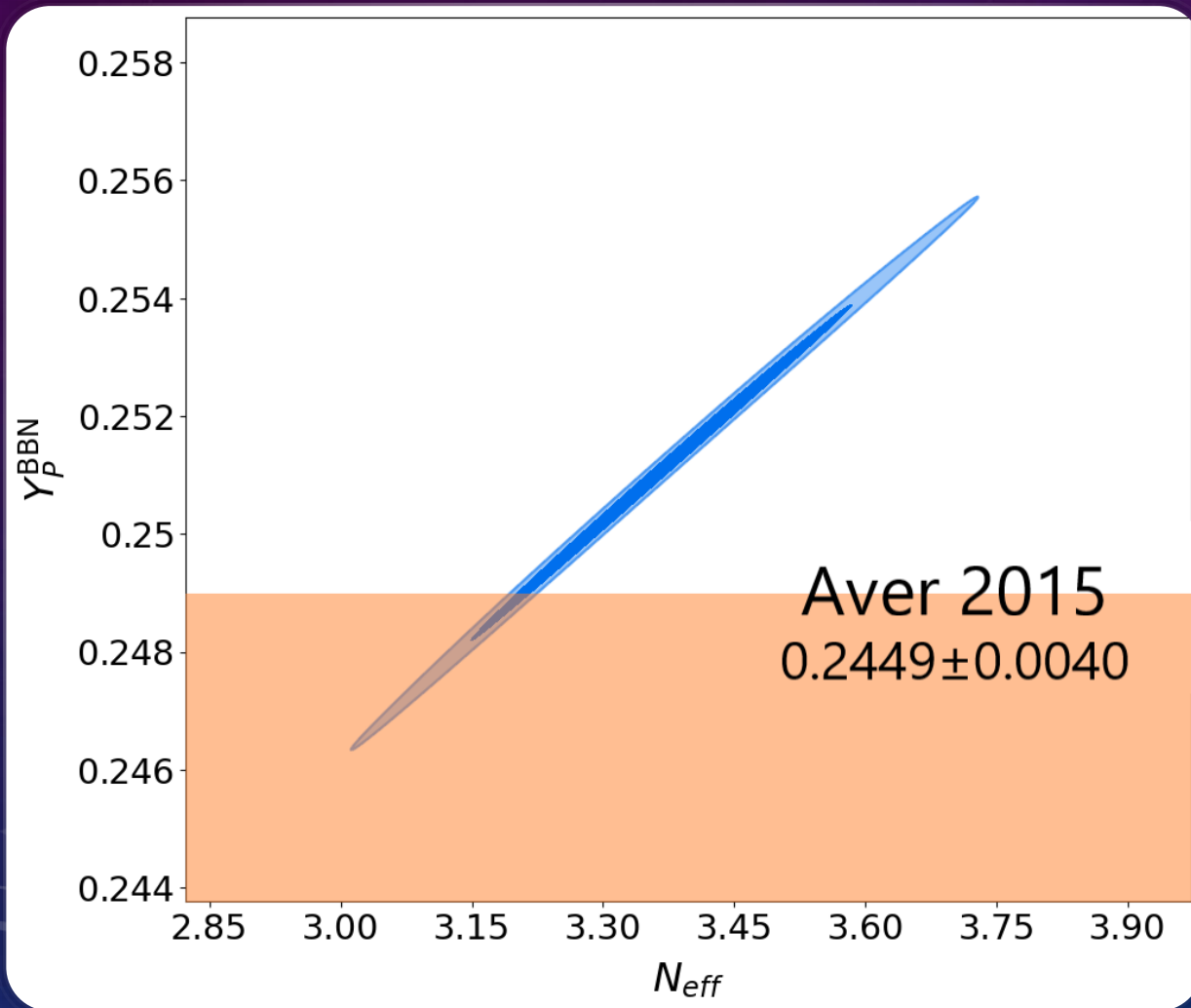
CMB only

Higher N_{eff}
increase H_0

$$N_{\text{eff}} = 3.046 + (\text{Extra contribution})$$

Planck + Pantheon + BAO + R19

N_{eff} VS. HELIUM MASS FRACTION Y_P MEASUREMENT



Larger N_{eff}
increase Y_P

$$N_{\text{eff}} = 3.046 + (\text{Extra contribution})$$

Planck + Pantheon + BAO + R19

NEUTRINO DEGENERACY

The degeneracy parameter $\xi_i = \frac{\mu_{\nu i}}{T_\nu}$ ($i = e, \mu, \tau$)

$\mu_{\nu i}$: chemical potential for neutrino ν_i

T_ν : temperature of neutrinos

Number Densities of
neutrinos and antineutrinos

Distribution functions

$$f_\nu = \frac{1}{\exp(p/T_\nu - \xi_i) + 1}$$

$$f_{\bar{\nu}} = \frac{1}{\exp(p/T_\nu + \xi_i) + 1}$$

$$n_{\nu i} + n_{\bar{\nu} i} \propto T_{\nu i}^3 (2(\xi_i/\pi)^2 + (\xi_i/\pi)^4) \rightarrow N_{\text{eff}}$$

$$n_{\nu i} - n_{\bar{\nu} i} \propto T_{\nu i}^3 (\pi^2 \xi_i + \xi_i^3) \rightarrow \text{BBN}$$

Positive electron neutrino degeneracy



$$n_{\nu_e} - n_{\bar{\nu}_e} \propto T_{\nu_e}^3 (\pi^2 \xi_e + \xi_e^3)$$

More neutrinos than antineutrinos



The process $p + \bar{\nu}_e \rightarrow n + e^+$ is suppressed than $n + \nu_e \rightarrow p + e^-$



Neutron-to-proton ratio decrease



Helium mass fraction Y_p Decrease

Number Densities of neutrinos and antineutrinos

$$n_{\nu_i} + n_{\bar{\nu}_i} \propto T_{\nu_i}^3 (2(\xi_i/\pi)^2 + (\xi_i/\pi)^4)$$

$$\rightarrow \Delta N_{\text{eff}} = \frac{15}{7} \sum_i \left(2 \left(\frac{\xi_i}{\pi} \right)^2 + \left(\frac{\xi_i}{\pi} \right)^4 \right)$$

We consider

$$|\xi_i| \leq 0.06 \rightarrow |\Delta N_{\text{eff}}| < 0.01 \quad \text{Neglegeble}$$

and

Extra radiation $\Delta N_{\text{eff}} \sim 0.5$

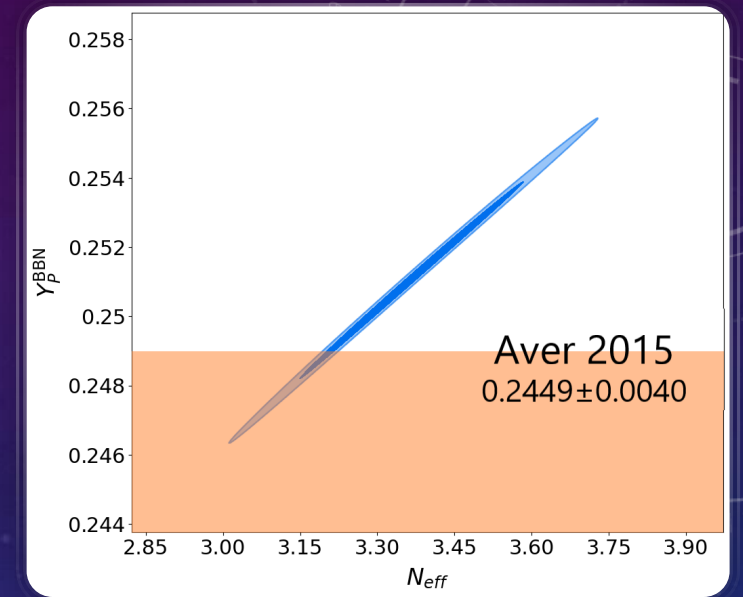
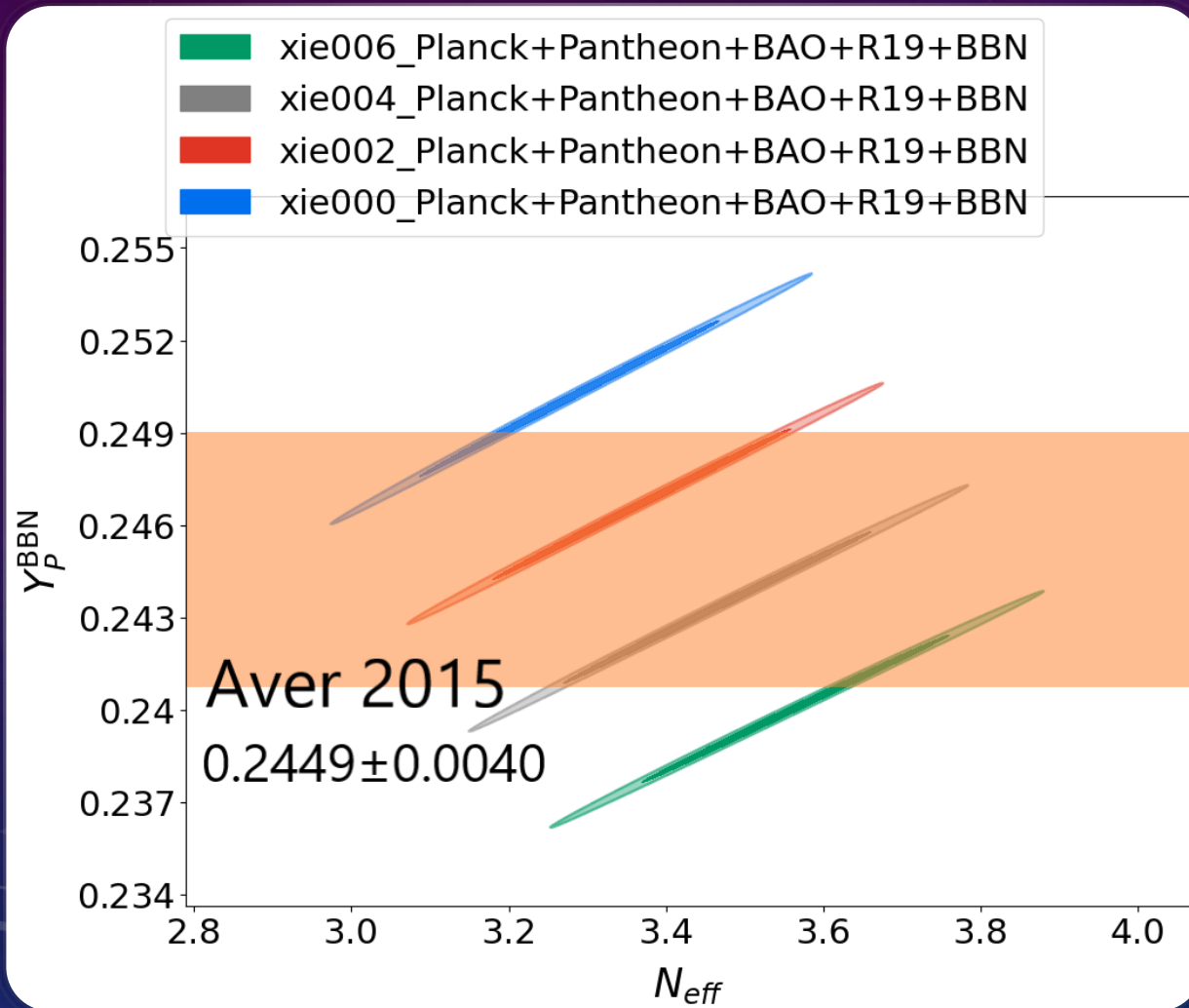
Next, I will show the results of analysis of

EXTRA RADIATION ΔN_{eff}

AND

ELECTRON NEUTRINO DEGENERACY ξ_e

Y_P VS. N_{eff} WITH THE DEGENERACY ξ_e



Larger N_{eff}
increase Y_P

Larger ξ_e
decrease Y_P

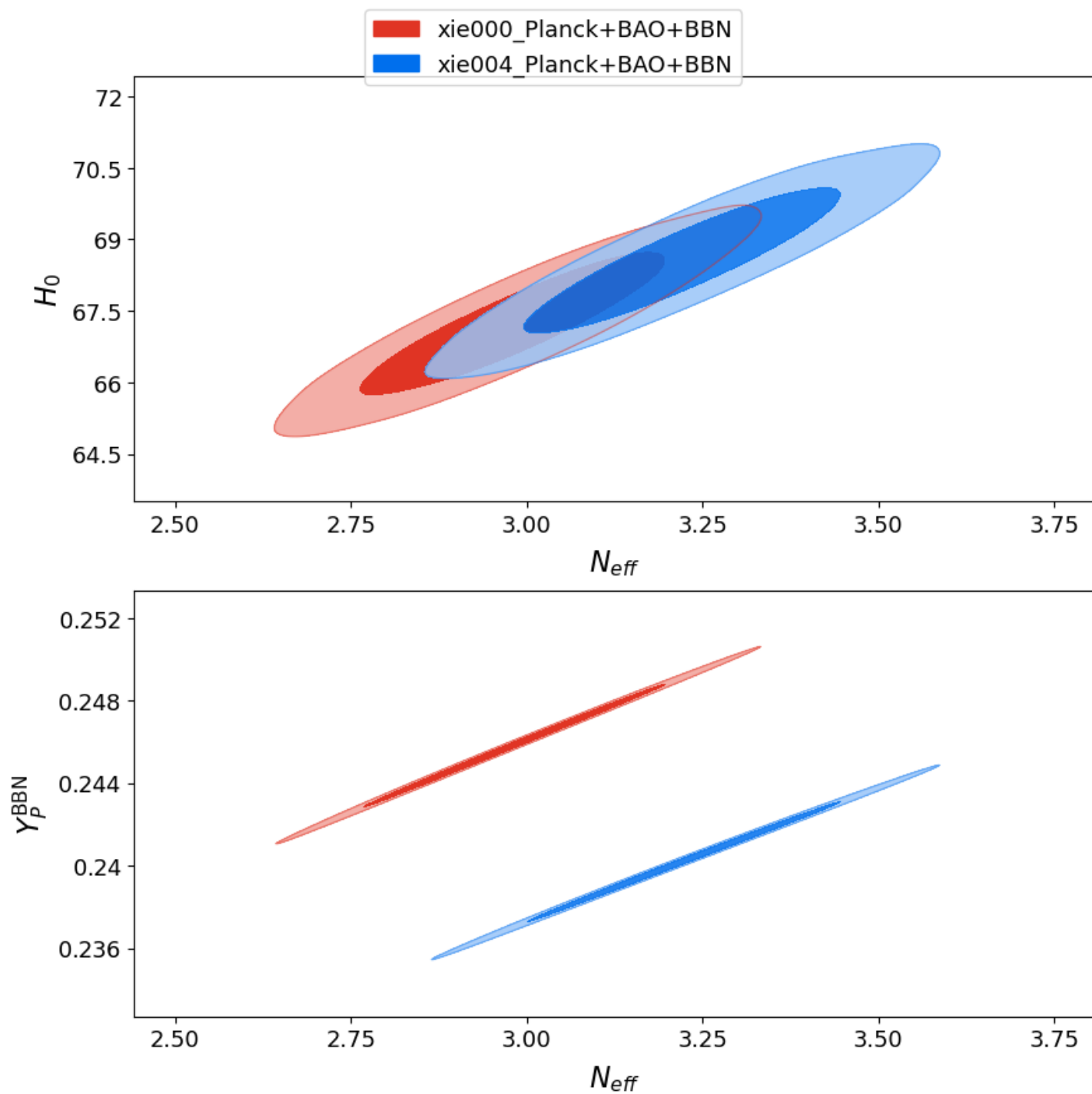
BEST-FIT

Parameter	Λ CDM	$\xi_e=0$	$\xi_e=0.02$	$\xi_e=0.04$	$\xi_e=0.06$
N_{eff}	3.046	3.243	3.31264	3.45451	3.63353
H_0	68.218	69.632	69.7162	70.2582	71.701
Y_P	0.2468	0.2497	0.2460	0.2432	0.2410
χ^2_{Cooke17}	0.2977	0.1036	0.0611	0.0015	6.62848e-06
χ^2_{Aver15}	0.2161	1.4540	0.0753	0.1725	0.9673
χ^2_{H074p03}	16.7501	9.5927	9.2288	7.0555	2.6900
χ^2_{JLA}	1034.77	1034.74	1034.74	1034.75	1034.81
χ^2_{prior}	4.5083	4.3142	2.3132	3.1993	7.2315
χ^2_{CMB}	2779.73	2781.6	2783.9	2782.84	2783.71
χ^2_{BAO}	5.2445	5.8010	5.4053	5.3761	6.5744
χ^2_{total}	3841.52	3837.61	3835.72	3833.39	3836.22

Y_P
measurement

Local (direct)
 H_0
measurement

No Local Measurements
w/ and w/o
degeneracy ξ_e



TAKE-HOME MESSAGE

- The combination of **Extra radiation** and **Neutrino degeneracy** are the **promising** solution of the **Hubble tension**
- **Non-zero degenerate $\xi_e = 0.04$ and extra radiation $N_{\text{eff}} = 3.45$** is the best-fit at the combination of **CMB, BBN, BAO** and the **local** measurements
- The **model of particle physics** which takes **large neutrino degenerate** and **extra radiation** is worth constructing

Thank you for your kind attention!

Osamu Seto, Yo Toda [arXiv:2104.04381 \[astro-ph.CO\]](#)

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