

The SIMP Age for Thermal Dark Matter

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H.M. Lee and M.-S. Seo, Phys. Lett. B748, 316;
S.-M. Choi and H.M. Lee, JHEP1509, 063, and arXiv:
1601.03566[hep-ph] (In press, Phys. Lett. B)

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Seoul National University, May 2, 2016

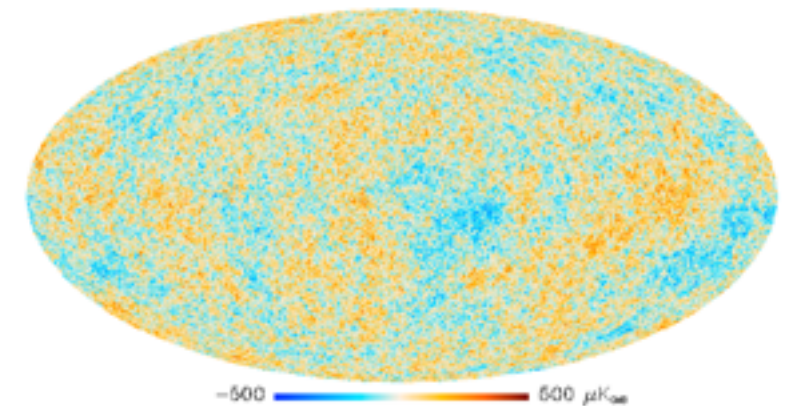
Outline

- SIMP dark matter
- SIMP from dark QCD
- SIMP with discrete symmetries
- Conclusions

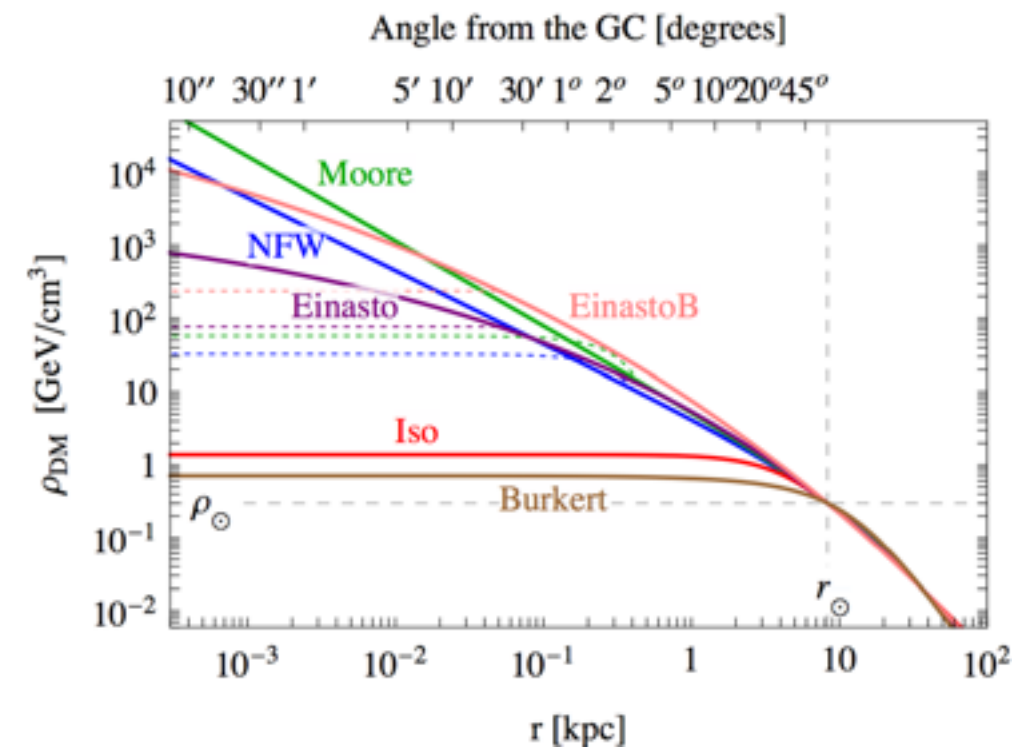
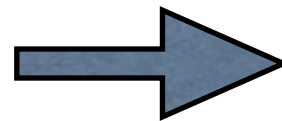
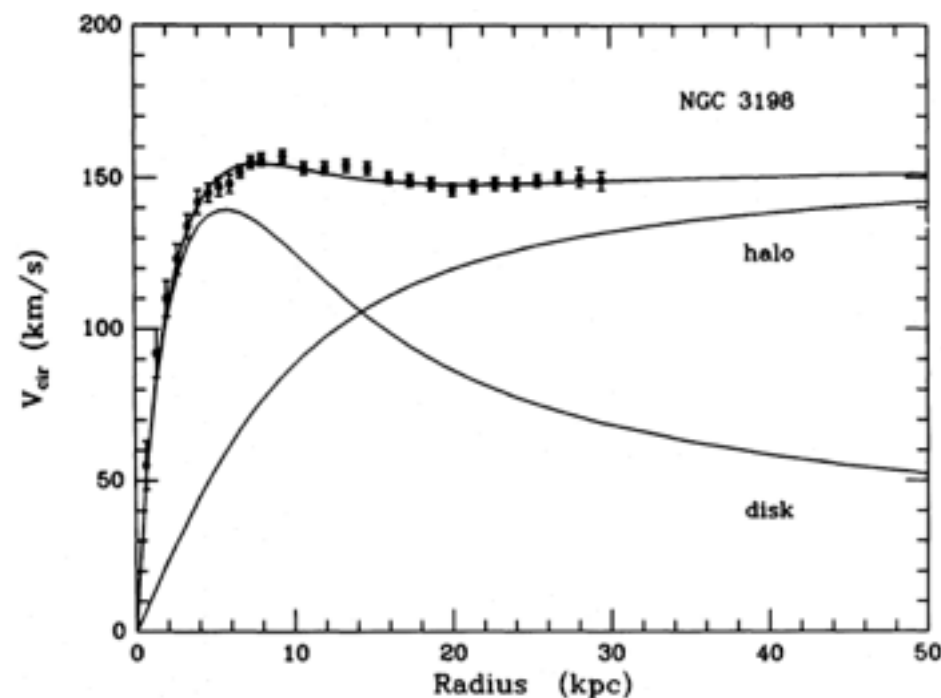
SIMP dark matter

Dark matter everywhere!

Large-scale evidences

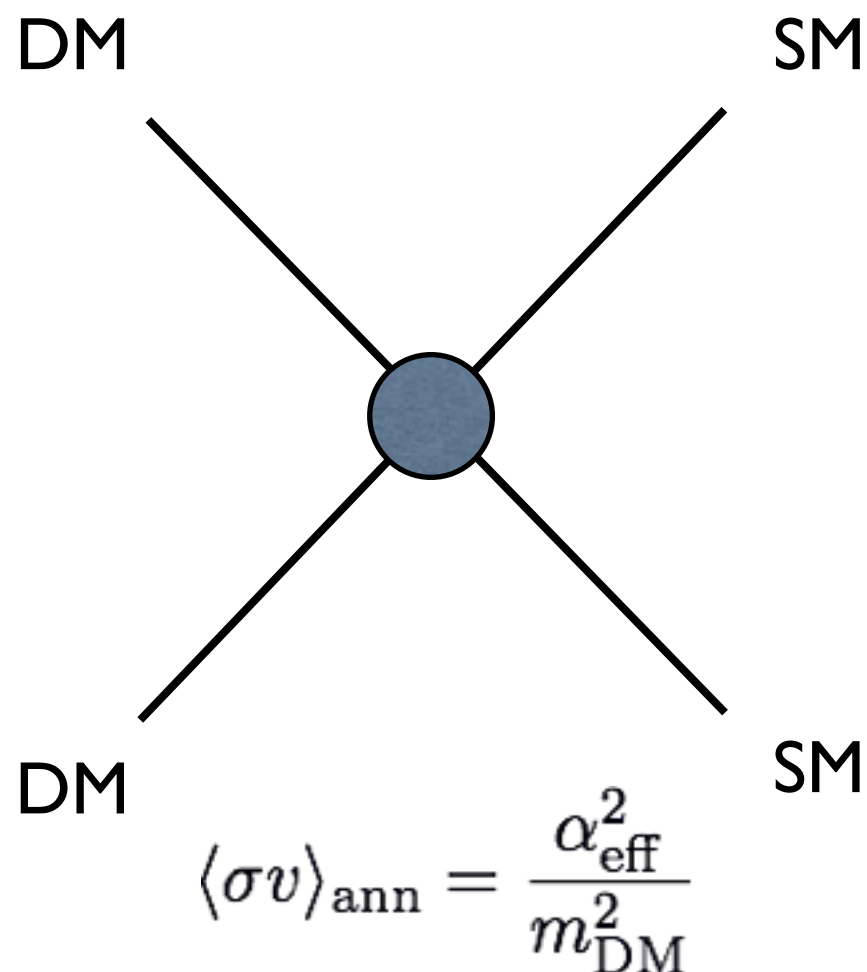


Galaxies (including our Milky Way)



WIMP paradigm

- WIMP DM density relies on chemical equilibrium with $2 \rightarrow 2$ annihilation with weak interactions.



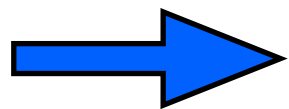
$$\frac{dn_{\text{DM}}}{dt} + 3Hn_{\text{DM}} = -\langle \sigma v \rangle (n_{\text{DM}}^2 - (n_{\text{DM}}^{\text{eq}})^2)$$

WIMP freeze-out:

$$\Gamma_{\text{ann}} = n_{\text{DM}} \langle \sigma v \rangle_{\text{ann}} \sim H = 0.33 g_*^{1/2} \frac{T_F^2}{M_P}$$

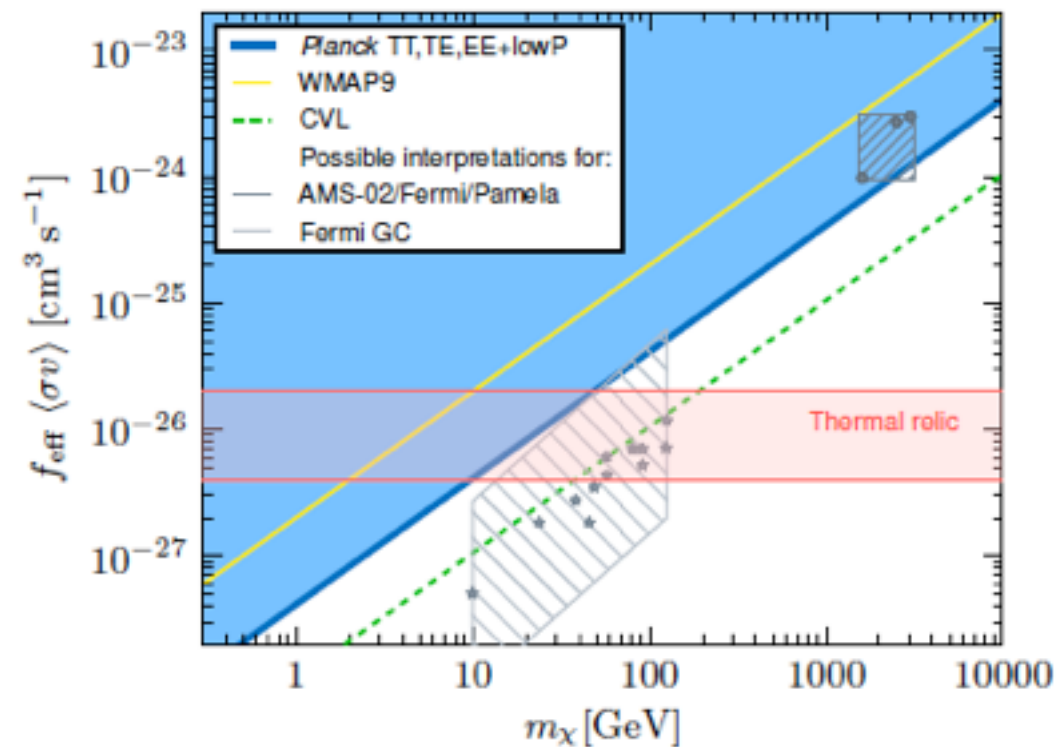
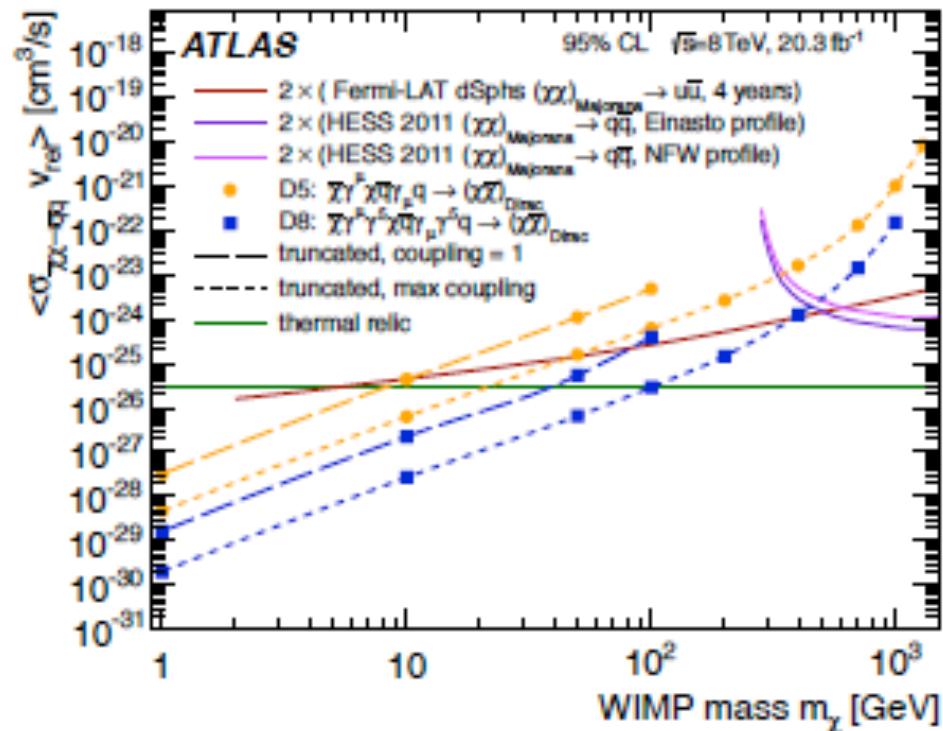
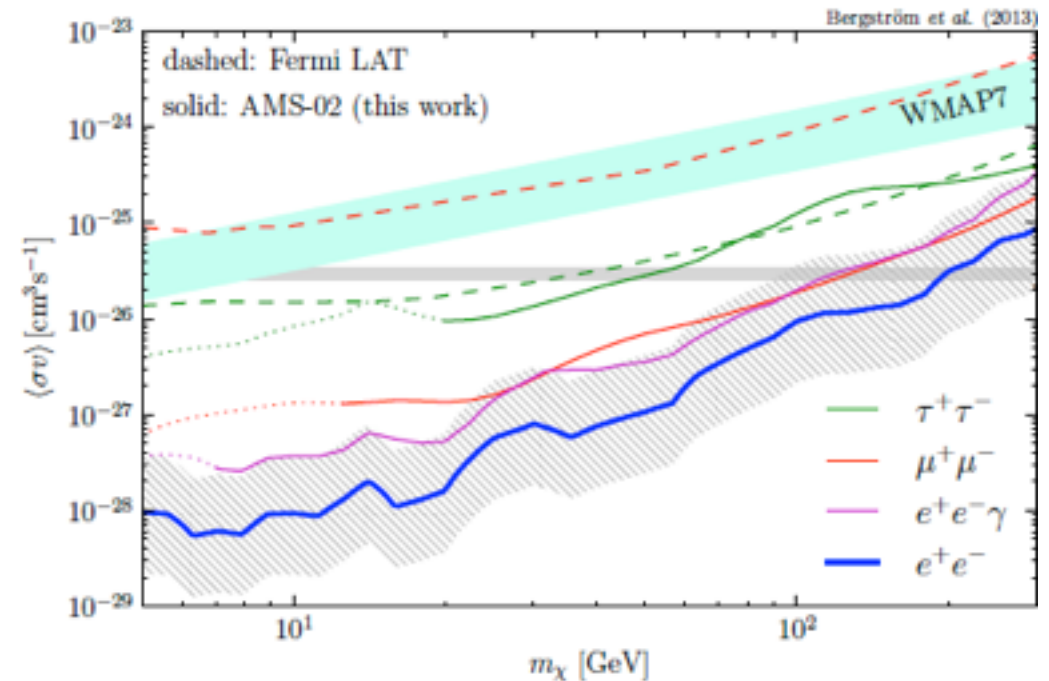
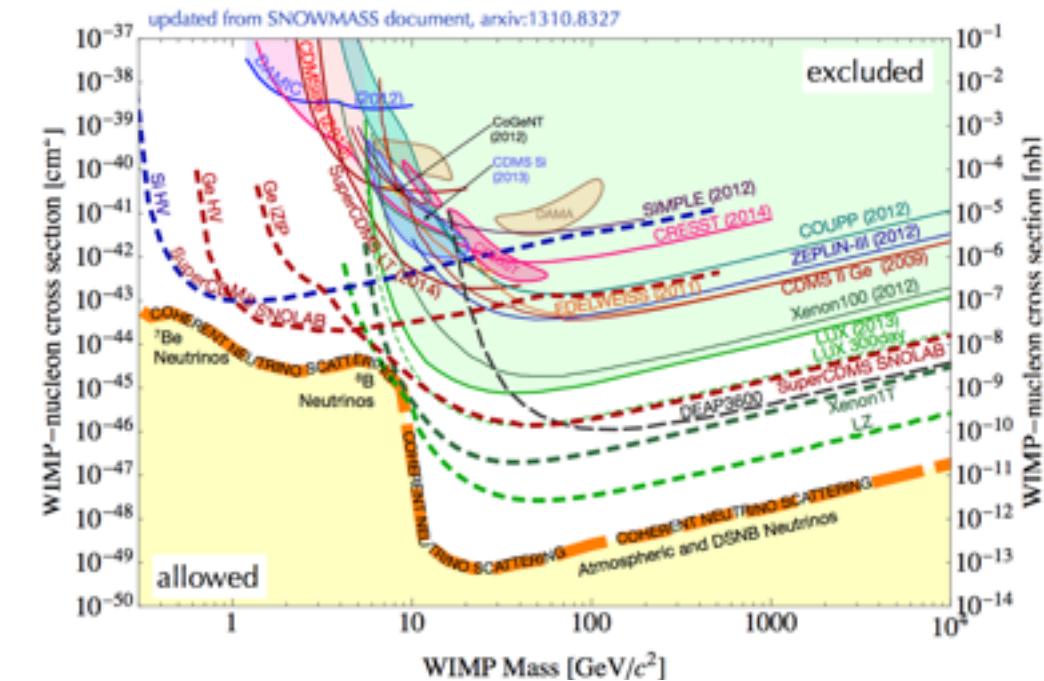
$$\Omega_{\text{DM}} h^2 \sim 0.1 \left(\frac{2 \times 10^{-9} \text{GeV}^{-2}}{(g_*/100)^{1/2} x_F \int_{x_F}^{\infty} x^{-2} \langle \sigma v \rangle dx} \right)$$

$$\alpha_{\text{eff}} \sim \frac{1}{30}$$



$$m_{\text{DM}} \sim 1 \text{ TeV}$$

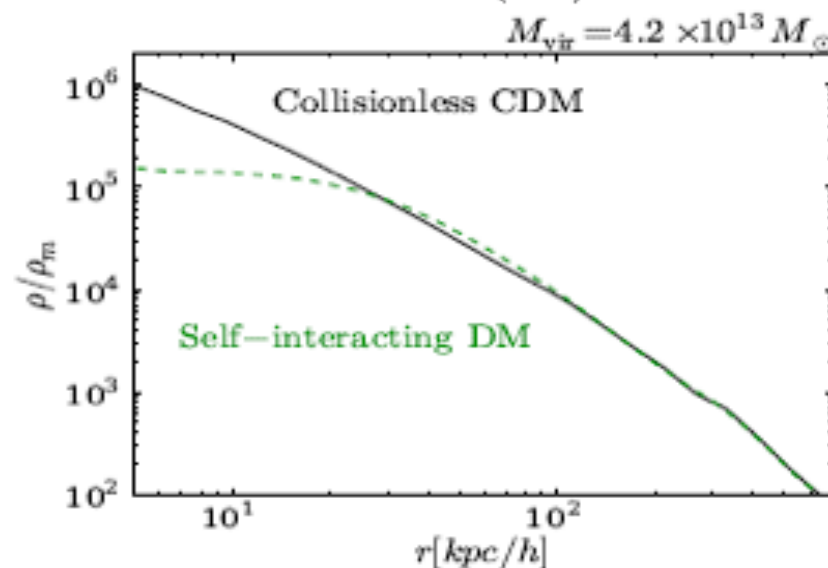
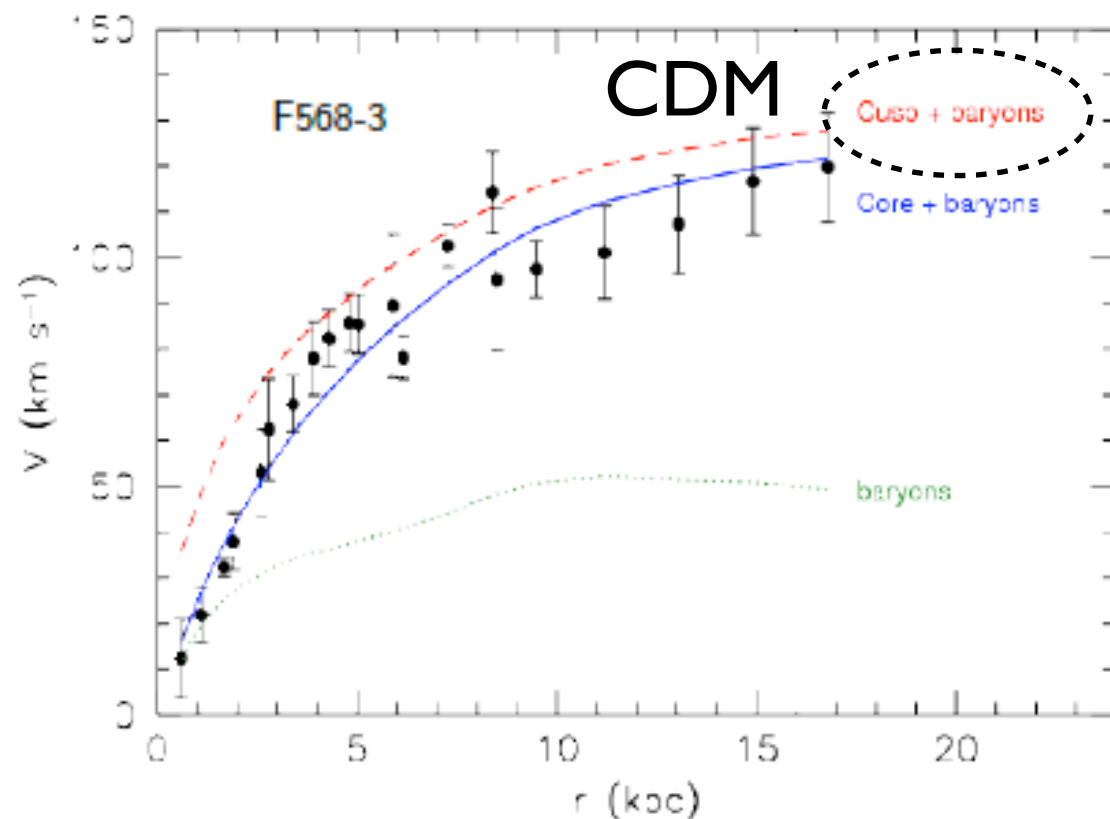
WIMP around the corner?



- A wide range of WIMP masses and interactions has been searched for by complementary searches.

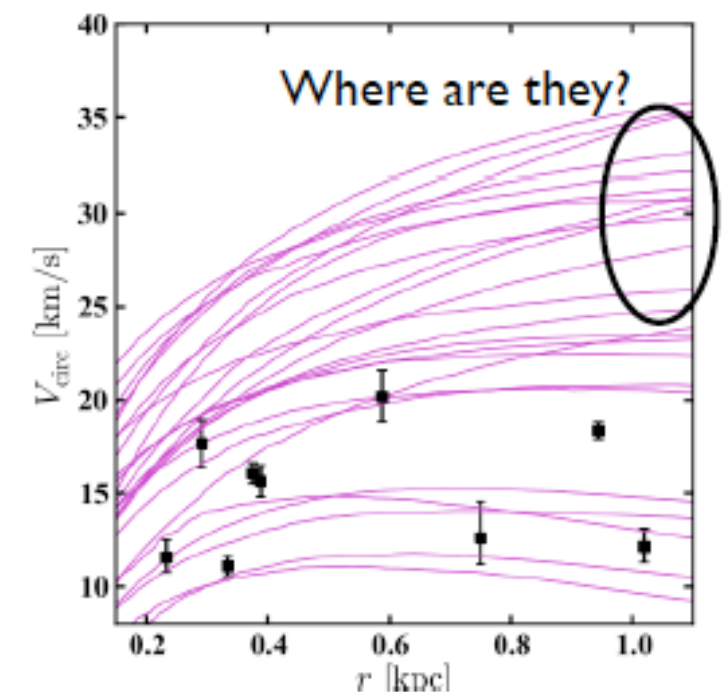
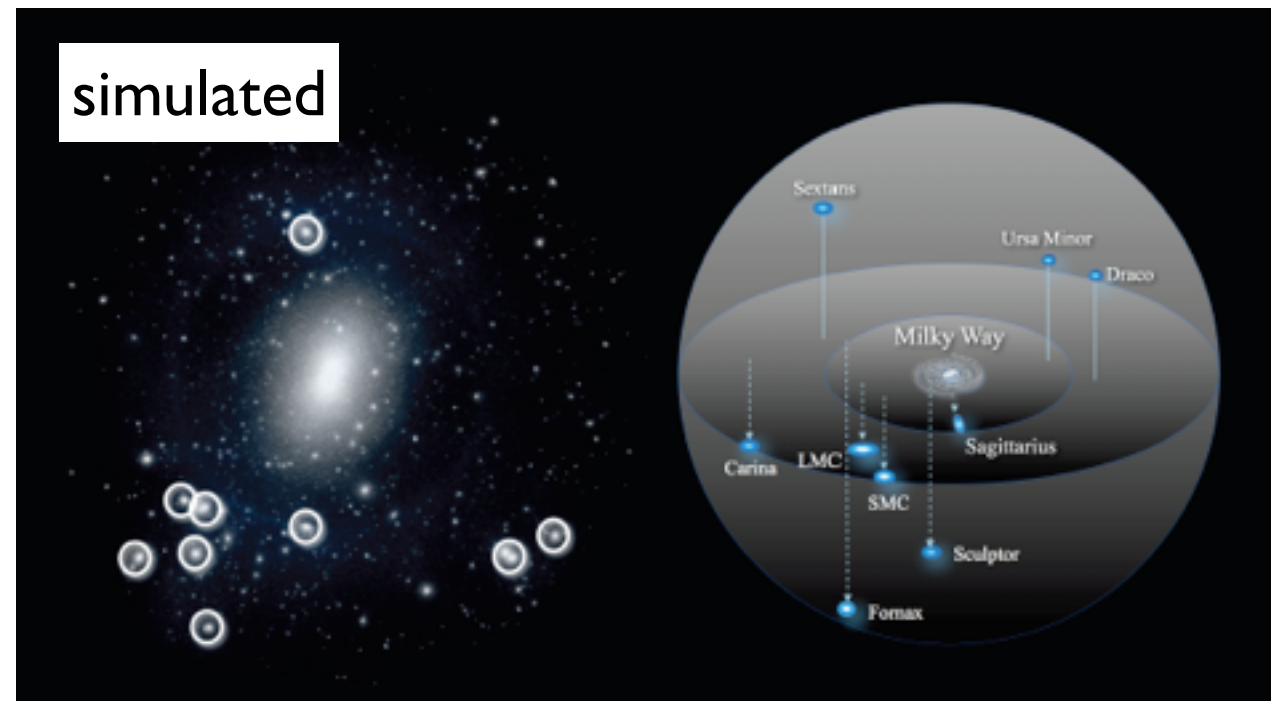
Small-scale problems

- **Core-cusp:** Simulation with CDM (cusp) overshoots galaxy rotation curves.
- **Too-big-to-fail:** Simulation predicts too much mass for dwarf galaxies (subhalos).



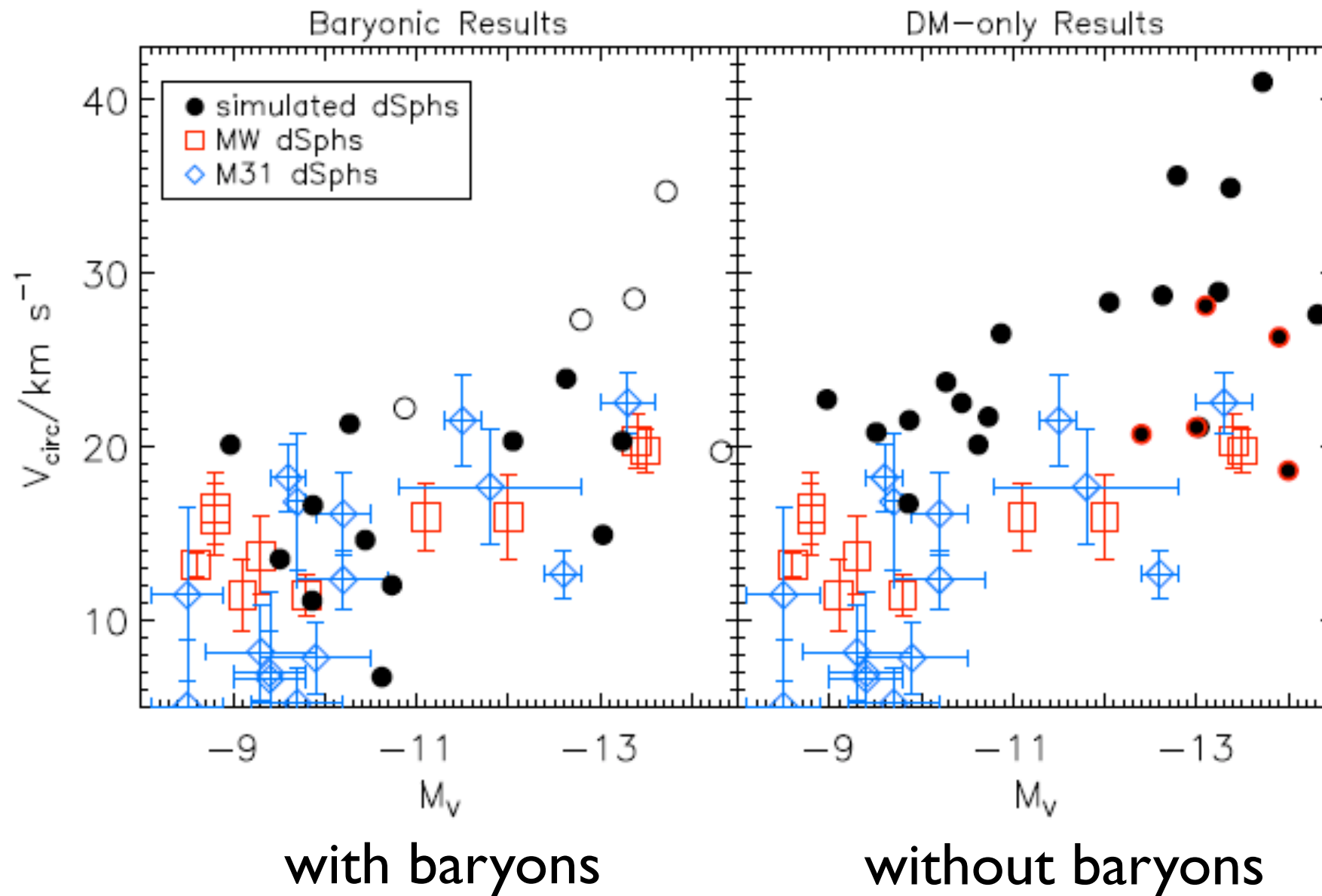
$$V \sim \sqrt{\frac{GM_{<}}{r}}$$

rotation curves
of dSphs



dSphs with baryons?

[Brooks & Zolotov, 2012]



DM + baryons (SN feedback) erase small structures.

But, many dwarf galaxies: lack of baryons?

DM self-interactions

- DM self-interactions solve small-scale problems for

$$\sigma_{\text{self}}/m_{\text{DM}} = 0.1 - 10 \text{ cm}^2/\text{g}$$

cf. WIMP DM: $\sigma_{\text{self}}/m_{\text{WIMP}} \sim 10^{-11} \text{ GeV}^{-3} \sim 10^{-14} \text{ cm}^2/\text{g}$.

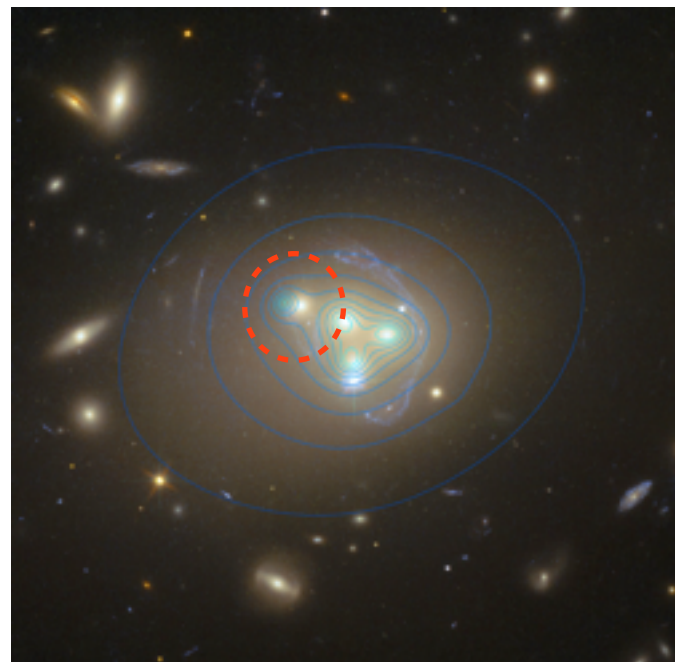
- DM sub-halo lags, due to drag force (“long-range”) or large momentum transfer (“contact”).

Bounds (Bullet cluster)

$$\sigma_{\text{self}}/m_{\text{DM}} < 1 \text{ cm}^2/\text{g}$$



Hints (Abell 3827: one DM sub-halo lags behind the galaxy.



off-set:

$$\Delta = 1.62^{+0.47}_{-0.49} \text{ kpc}$$

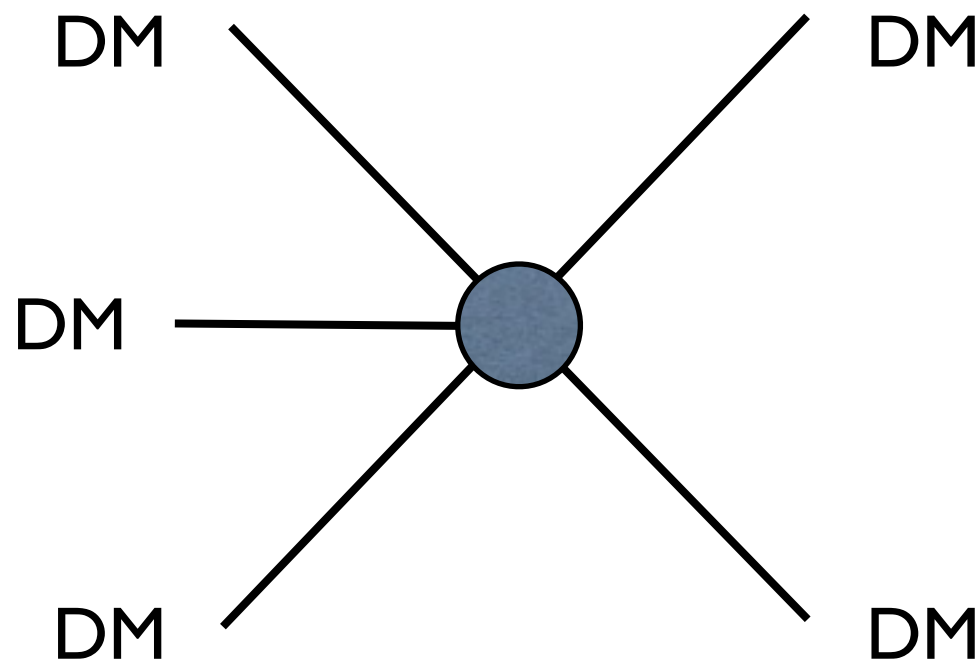
[Massey et al(2015)]

$$\sigma_{\text{self}}/m_{\text{DM}} \sim 2 \times 10^{-4} \text{ cm}^2/\text{g}$$

SIMP paradigm

- Strong Interacting Massive Particles(SIMP) are based on chemical equilibrium with $3 \rightarrow 2$ self-annihilation between themselves.

[Hochberg et al, 2014;
S.-M.Choi, HML, 2016]



$$\frac{dn_{\text{DM}}}{dt} + 3Hn_{\text{DM}} = \boxed{\begin{aligned} & -\langle\sigma v^2\rangle_{3\rightarrow 2} (n_{\text{DM}}^3 - n_{\text{DM}}^2 n_{\text{DM}}^{\text{eq}}) \\ & -\langle\sigma v\rangle_{2\rightarrow 2} (n_{\text{DM}}^2 - (n_{\text{DM}}^{\text{eq}})^2) \end{aligned}}$$

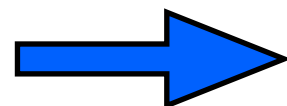
Freeze-out of $3 \rightarrow 2$ process:

$$\Gamma_{3\rightarrow 2} = n_{\text{DM}}^2 \langle\sigma v^2\rangle_{3\rightarrow 2} \sim H(T_F)$$

$$\langle\sigma v^2\rangle_{3\rightarrow 2} = \frac{\alpha_{\text{eff}}^3}{m_{\text{DM}}^5}$$

$$\Omega_{\text{DM}} h^2 \sim 0.1 \left(\frac{9 \times 10^{-10} \text{GeV}^{-2}}{(g_*/10.45)^{3/4} \left(\frac{m_{\text{DM}}^2}{M_P} \int_{x_F}^{\infty} x^{-5} \langle\sigma v^2\rangle dx \right)^{1/2}} \right)$$

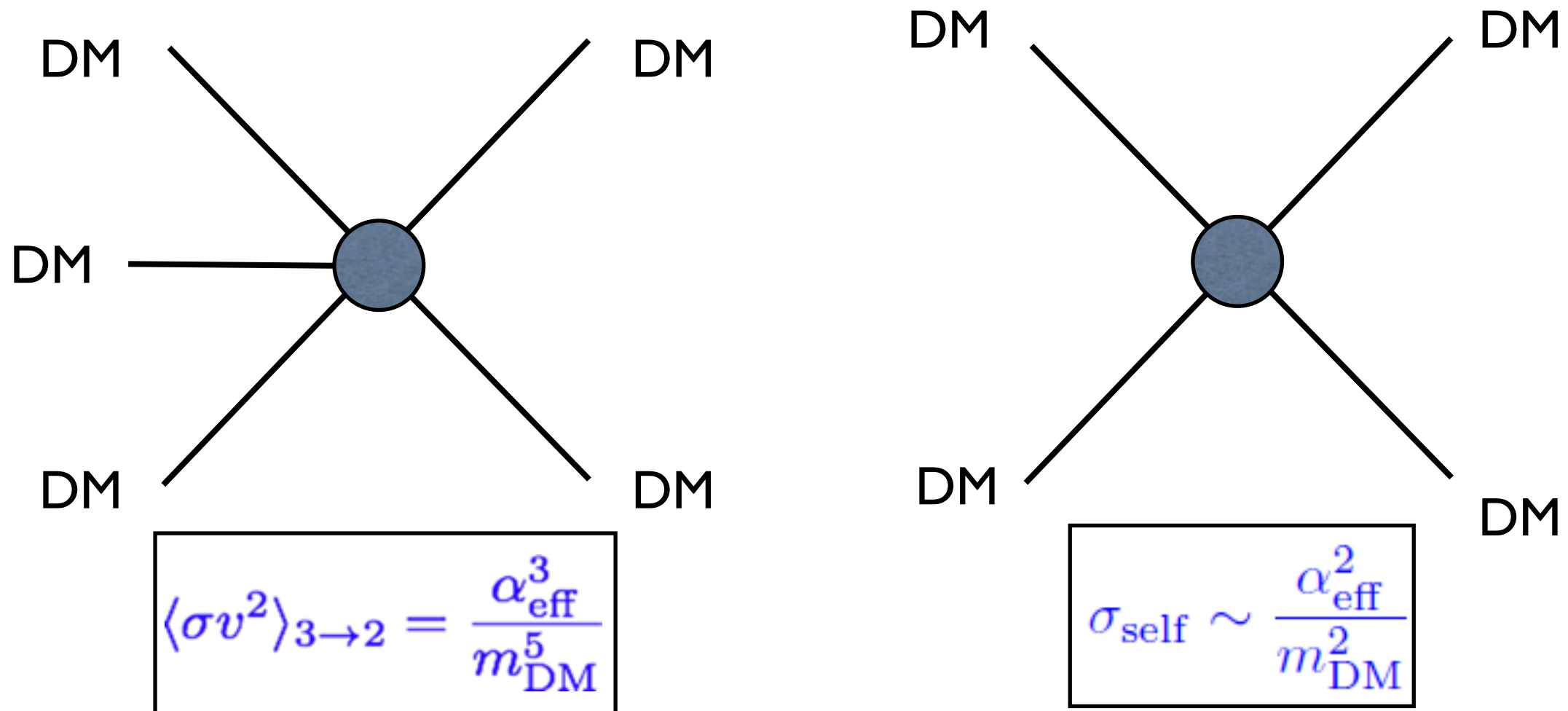
$$\alpha_{\text{eff}} = 1 - 30$$



$$m_{\text{DM}} = 40 - 1000 \text{ MeV}$$

Large SIMP self-interaction

- SIMP DM predicts typically large self-interactions.

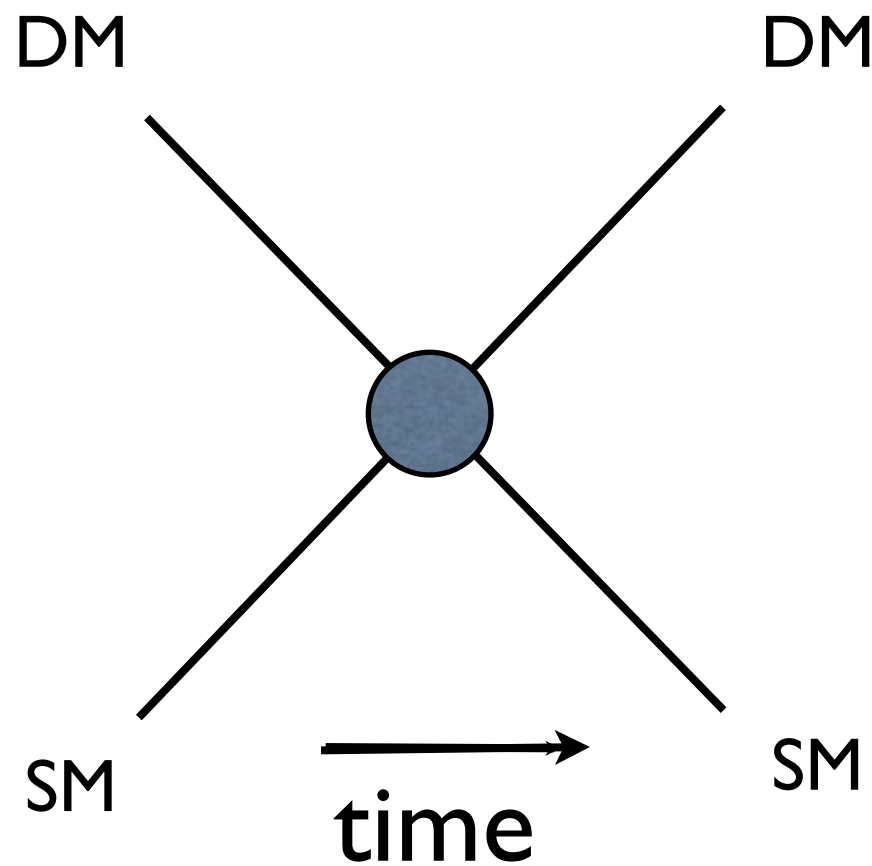


$\Rightarrow \frac{\sigma_{\text{self}}}{m_{\text{DM}}} = 4 \times 10^3 \text{ GeV}^{-3} \left(\frac{100 \text{ MeV}}{m_{\text{DM}}} \right)^3 \left(\frac{\alpha_{\text{eff}}}{2} \right)^2 \simeq \left(\frac{5}{\alpha_{\text{eff}}} \right) 1 \text{ cm}^2/\text{g}$
relic density

Note: Bullet cluster & spherical halo shapes.

$$\frac{\sigma_{\text{self}}}{m_{\text{DM}}} < 1 \text{ cm}^2/\text{g} = 4.6 \times 10^3 \text{ GeV}^{-3}$$

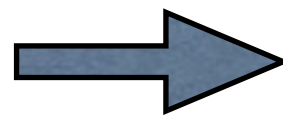
SIMP - SM interactions



- SIMP in $3 \rightarrow 2$ process must be equilibrated for structure formation.
[de Laix et al, 1995]

SIMP loses heat by kinetic scattering even with tiny interaction to SM bath:

$$\langle \sigma v \rangle_{\text{kin}} = \frac{\epsilon_1^2}{m_{\text{DM}}^2}; \quad n_{\text{SM}} \langle \sigma v \rangle_{\text{kin}} > H(T_F)$$



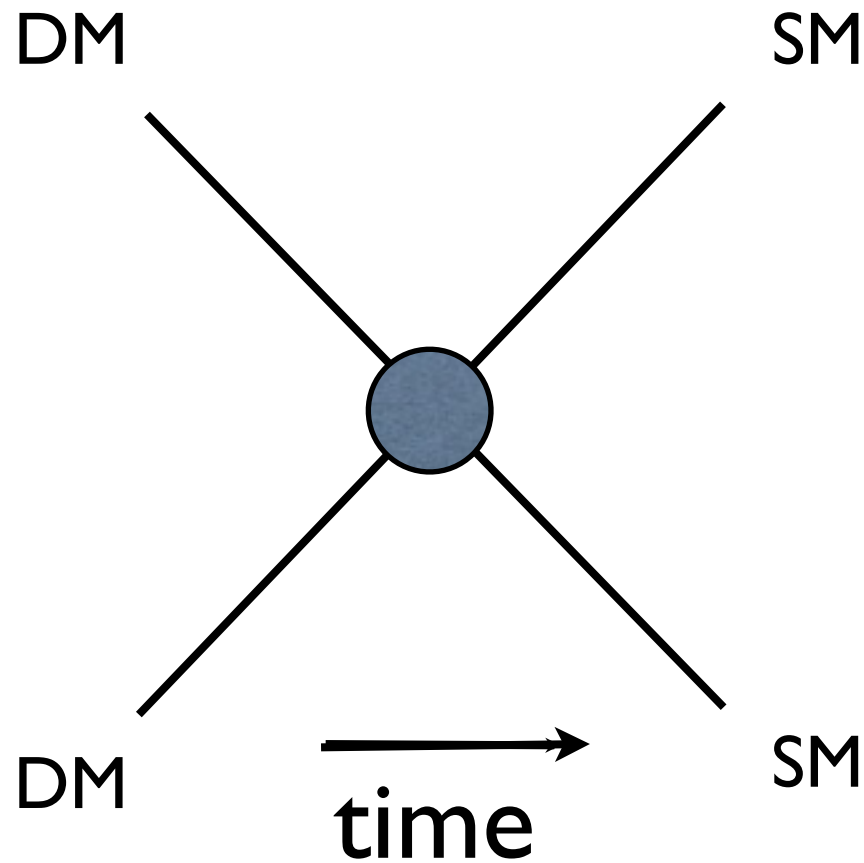
$$\epsilon_1 \gtrsim 0.9 \times 10^{-9} \alpha_{\text{eff}}^{1/2}$$

- SIMP can be also thermalized by dark thermal bath.

But, dark temperature is an extra parameter!

cf. Higher-order SIMP ($4 \rightarrow 2$) predicts lighter DM (sub-MeV) SIMP:
necessary to introduce a small dark temperature due to bound on N_{eff} .

SIMP conditions



- Crossing symmetry of kinetic scattering leads to $2 \rightarrow 2$ DM annihilation, which is sub-dominant if

$$\langle \sigma v \rangle_{\text{ann}} = \frac{\epsilon_2^2}{m_{\text{DM}}^2};$$

$$n_{\text{SM}} \langle \sigma v \rangle_{\text{kin}} < n_{\text{DM}} \langle \sigma v^2 \rangle_{3 \rightarrow 2}$$

$$\epsilon_2 \sim \epsilon_1$$

$$\epsilon_1 \lesssim 2.4 \times 10^{-6} \alpha_{\text{eff}}$$

- SIMP conditions:

$$0.9 \times 10^{-9} \alpha_{\text{eff}}^{1/2} \lesssim \epsilon_{1,2} \lesssim 2.4 \times 10^{-6} \alpha_{\text{eff}}$$

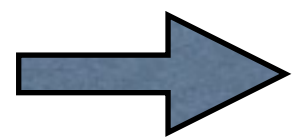
lose heat!

$3 \rightarrow 2$ wins!

SIMP from dark QCD

Dark QCD and dark matter

- Dark flavor symmetry $G = \text{SU}(N_f) \times \text{SU}(N_f)$ is broken down to $H = \text{SU}(N_f)$ by $\text{SU}(N_c)$ QCD-like condensation.



Dark mesons are naturally light and stable due to flavor symmetry.

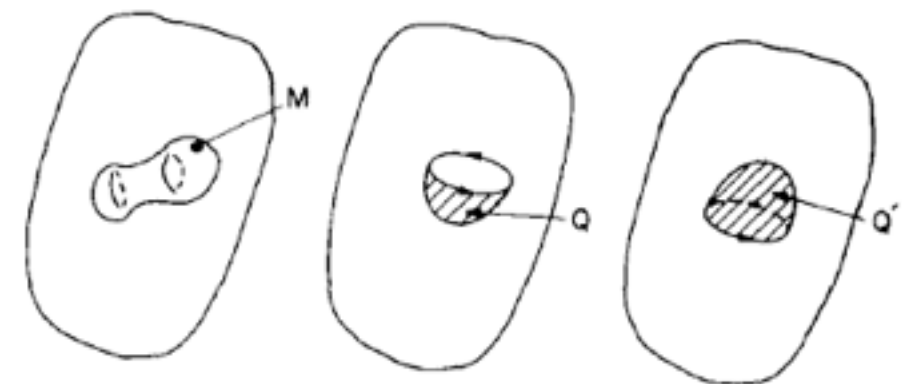
- Effective action for dark mesons contains a 5-point self-interaction from **Wess-Zumino-Witten term for $\pi_5(G/H) = \mathbb{Z}$ (i.e. $N_f \geq 3$)**.

[Wess, Zumino, 1971; Witten, 1983]

$$U = e^{2i\pi/F}, \quad \pi \equiv \pi^a T^a$$

$$\mathcal{L}_{WZW} = \frac{2N_c}{15\pi^2} \epsilon^{\mu\nu\rho\sigma} \text{Tr}[\pi \partial_\mu \pi \partial_\nu \pi \partial_\rho \pi \partial_\sigma \pi]$$

$$N_f = 3 : \pi = \frac{\sqrt{2}}{F} \begin{bmatrix} \frac{1}{\sqrt{2}}\tilde{\pi}_0 + \frac{1}{\sqrt{6}}\tilde{\eta}^0 & \tilde{\pi}^+ & \tilde{K}^+ \\ \tilde{\pi}^- & -\frac{1}{\sqrt{2}}\tilde{\pi}_0 + \frac{1}{\sqrt{6}}\tilde{\eta}^0 & \tilde{K}^0 \\ \tilde{K}^- & \tilde{K}^0 & -\sqrt{\frac{2}{3}}\tilde{\eta}^0 \end{bmatrix}.$$

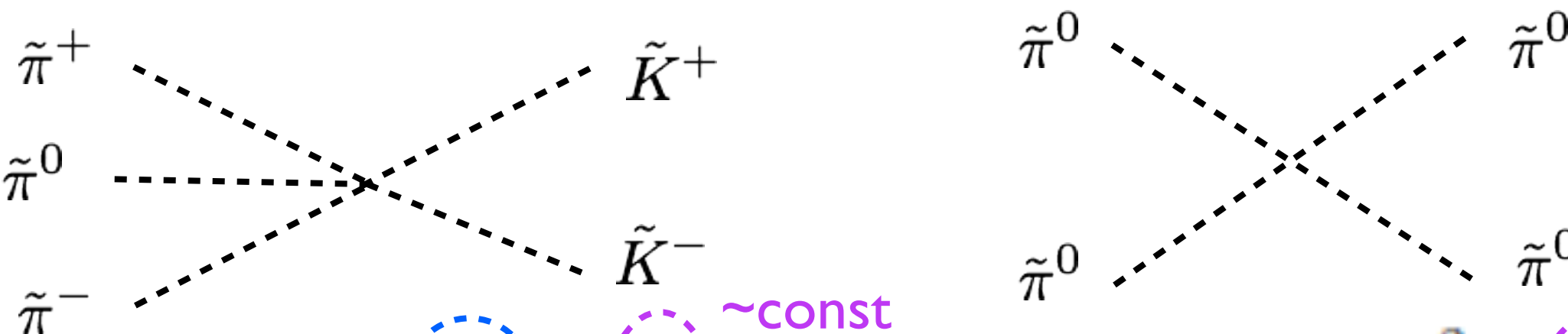


N_c : topological invariant of 5-sphere ($Q+Q'$) in $\text{SU}(3)$

SIMP from WZW

- “Large color group” leads to strong 5-point interactions while satisfying bounds on self-interactions.

[Hochberg et al, 2014]

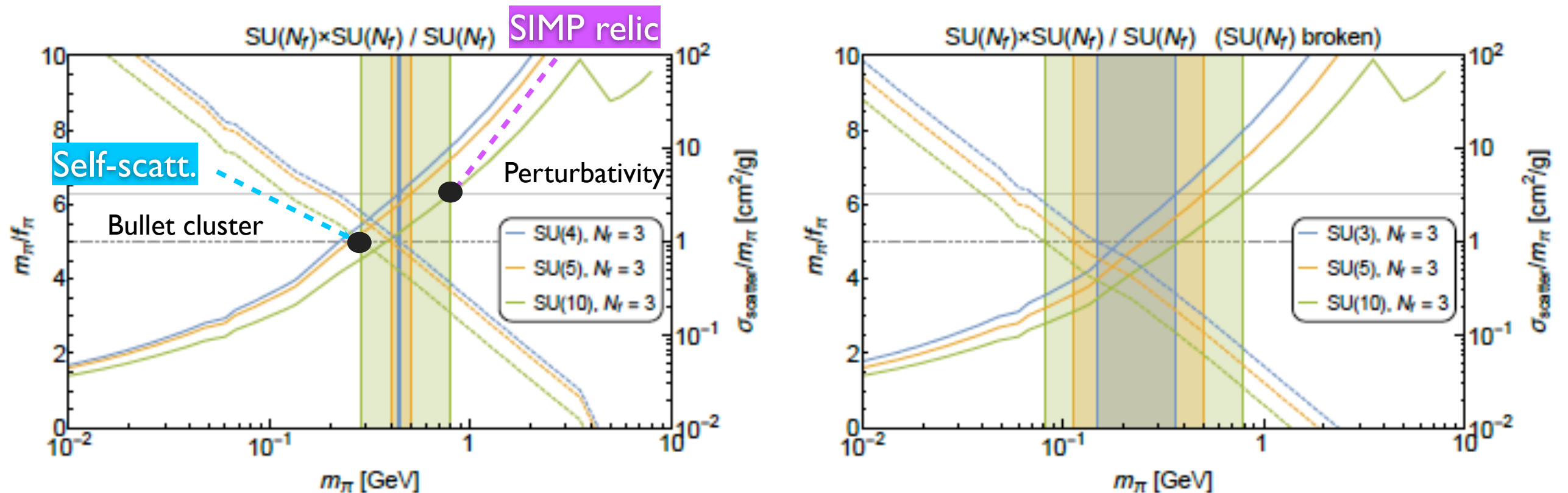


$$\langle \sigma v^2 \rangle_{3 \rightarrow 2} = \frac{5\sqrt{5}N_c^2 m_\pi^5}{2\pi^5 F^{10}} \frac{t^2}{N_\pi^3} \left(\frac{T_F}{m_\pi} \right)^2 \sim \text{const}$$

$$\sigma_{\text{self}} = \frac{m_\pi^2}{32\pi F^4} \frac{a^2}{N_\pi^2} \sim \text{const}$$

G_c	G_f/H	N_π	t^2	$N_f^2 a^2$
$SU(N_c)$	$\frac{SU(N_f) \times SU(N_f)}{SU(N_f)}$ ($N_f \geq 3$)	$N_f^2 - 1$	$\frac{4}{3}N_f(N_f^2 - 1)(N_f^2 - 4)$	$8(N_f - 1)(N_f + 1)(3N_f^4 - 2N_f^2 + 6)$
$SO(N_c)$	$SU(N_f)/SO(N_f)$ ($N_f \geq 3$)	$\frac{1}{2}(N_f + 2)(N_f - 1)$	$\frac{1}{12}N_f(N_f^2 - 1)(N_f^2 - 4)$	$(N_f - 1)(N_f + 2)(3N_f^4 + 7N_f^3 - 2N_f^2 - 12N_f + 24)$
$Sp(N_c)$	$SU(2N_f)/Sp(2N_f)$ ($N_f \geq 2$)	$(2N_f + 1)(N_f - 1)$	$\frac{2}{3}N_f(N_f^2 - 1)(4N_f^2 - 1)$	$4(N_f - 1)(2N_f + 1)(6N_f^4 - 7N_f^3 - N_f^2 + 3N_f + 3)$

SIMP parameter space



[Hochberg, Kuflik, Murayama, Volansky, Wacker, 2014]



Bullet cluster, Halo shape

$$\sigma_{\text{self}}/m_{\text{DM}} < 1 \text{ cm}^2/\text{g}$$

Perturbativity

$$m_{\pi}/f_{\pi} < 2\pi$$

$N_c > 3$ is required due to bounds on self-scattering.

Similar results for $SU(N_f)/SO(N_f)$ or $SU(2N_f)/Sp(2N_f)$.

WZW with Z'

- Introduce a massive Z' under which **dark quarks are vector-like** and **SM particles are neutral**.
- Modified WZW with U(1)': [Witten, 1983]

$$S = S_0(D_\mu U, D_\mu U^{-1}) + S_{\text{WZW}}(U, U^{-1}) - eN_c \int d^4x A'_\mu J^\mu + \frac{ie^2 N_c}{24\pi^2} \int d^4x \epsilon^{\mu\nu\rho\sigma} \partial_\mu A'^\nu A'_\rho \text{Tr}[Q^2 \partial_\sigma U U^{-1} + Q^2 U^{-1} \partial_\sigma U + Q U Q U^{-1} \partial_\sigma U U^{-1}],$$

Noether current:

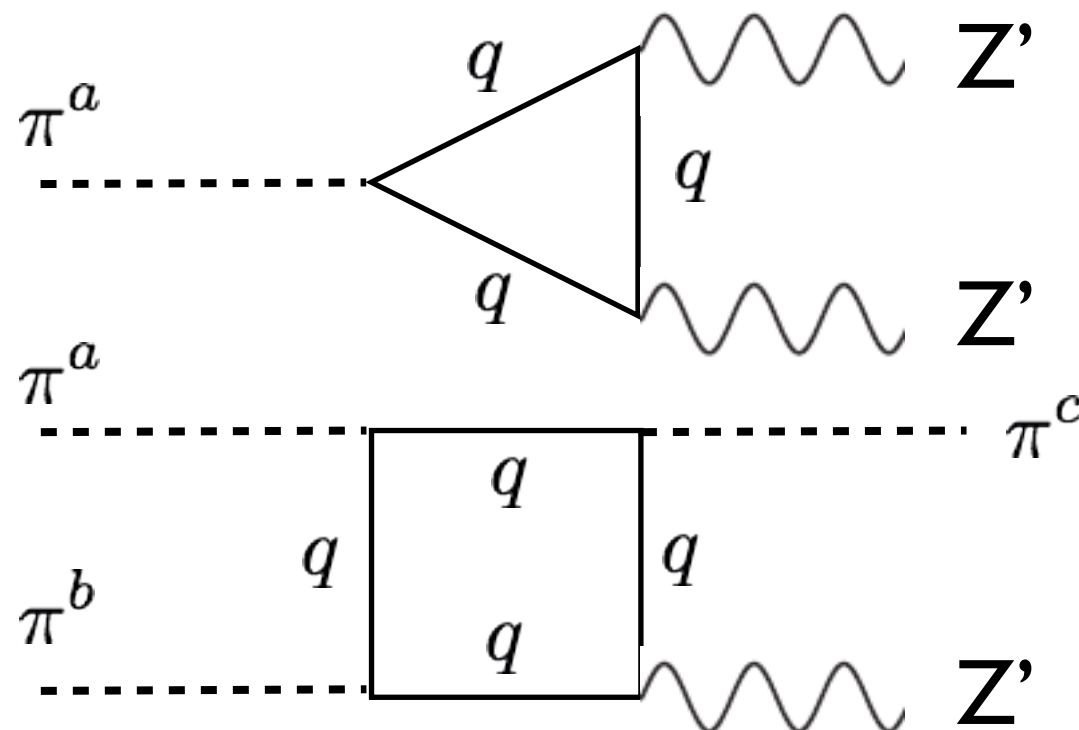
$$J^\mu = \frac{1}{48\pi^2} \epsilon^{\mu\nu\rho\sigma} \text{Tr}[Q \partial_\nu U U^{-1} \partial_\rho U U^{-1} \partial_\sigma U U^{-1} + Q U^{-1} \partial_\nu U U^{-1} \partial_\rho U U^{-1} \partial_\sigma U]$$

AVV anomalies.

➡ **Meson decay**

AAAV anomalies.

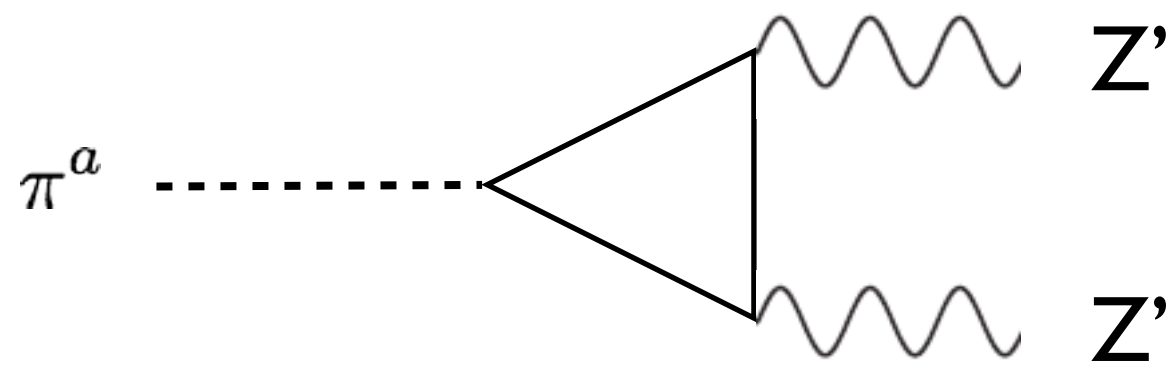
➡ **2 → 2 ann**



Stability of dark mesons

[HML, Seo, 2015]

- Stability of dark neutral mesons requires the **cancellation of AVV anomalies**.



$$\propto \text{Tr}(Q_D^2 T^a) = 0$$

if $Q_D^2 = I$.

→ $Q_D = \begin{pmatrix} \frac{1}{3} & 0 & 0 \\ 0 & -\frac{1}{3} & 0 \\ 0 & 0 & -\frac{1}{3} \end{pmatrix}$: **flavor non-universal charges**
 cf. QCD: $Q = \text{diag}(2/3, -1/3, -1/3)$

$$D_\mu U = \partial_\mu U + ig_D [Q_D, U] Z'_\mu; \quad \tilde{\pi}^\pm, \tilde{K}^\pm : \pm 2/3 \text{ charges.}$$

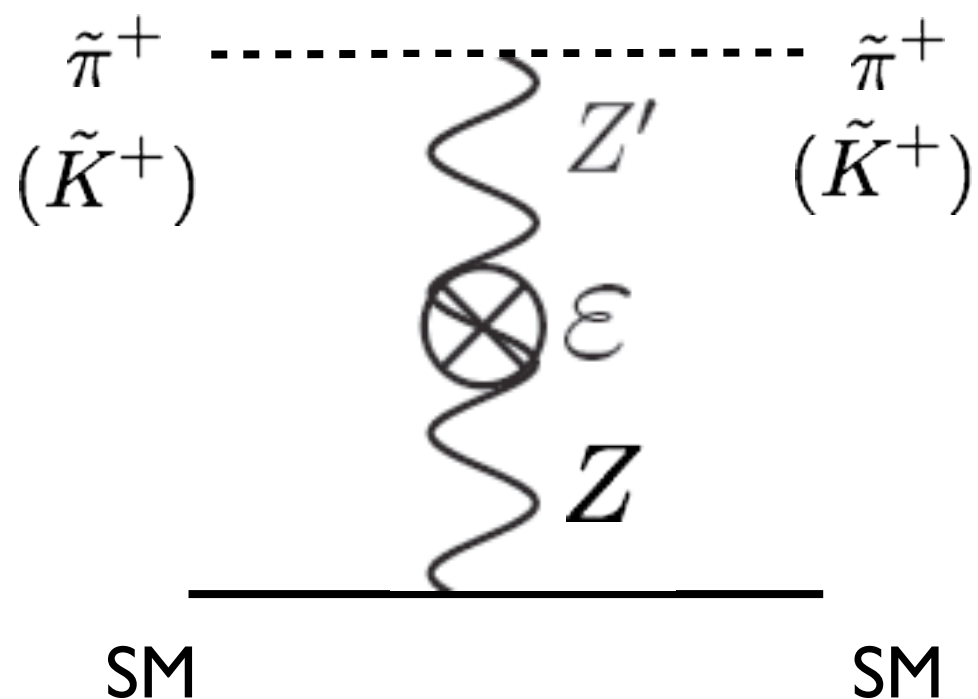
- Mass splitting generated by non-universal charges is constrained for SIMP annihilation:

$$\Delta m_\pi^2 \sim \frac{\alpha_D \Lambda^4}{F^2} \sim \alpha_D F^2 \lesssim \frac{m_\pi^2}{x_F^2} : \quad \alpha_D \lesssim 0.01 \left(\frac{m_\pi}{F} \right)^2.$$

Equilibrium via Z' -portal

[HML, Seo, 2015]

- Dark meson in kinetic equilibrium with the SM by kinetic mixing between Z' & hypercharge.



$$\mathcal{L}_{\text{mix}} = -\frac{\epsilon}{2 \cos \theta_W} F'_{\mu\nu} F^{\mu\nu}$$

$$\Rightarrow \langle \sigma v \rangle_{\text{kin}} \approx \frac{768 \alpha \alpha_D \epsilon^2}{\pi N_\pi} \frac{m_\pi^2}{m_{Z'}^4} \left(\frac{T_F}{m_\pi} \right).$$

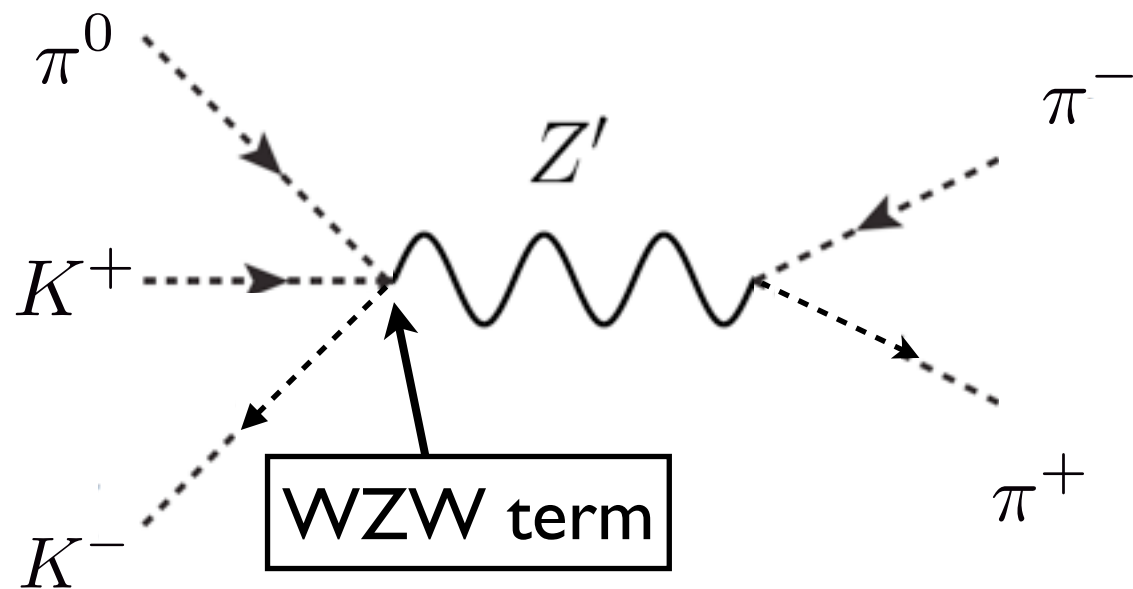
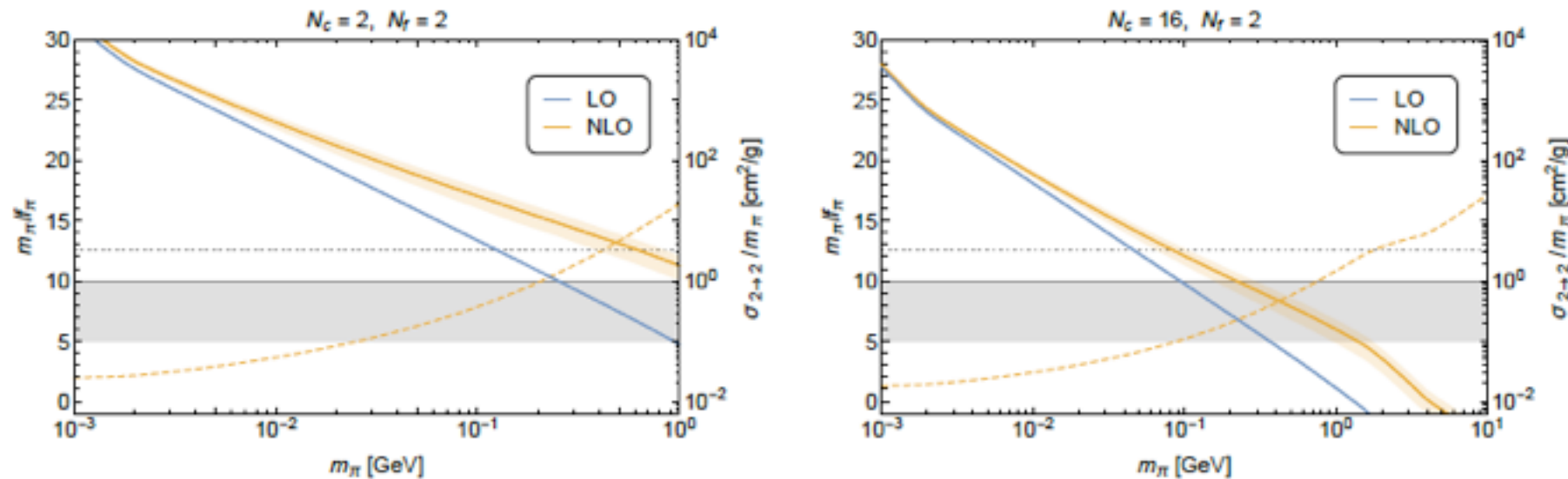
cf. Higgs-portal does not work, because leptons in thermal bath have small Yukawa couplings.

- $\pi \pi \rightarrow \pi Z'$ (AAAV) is forbidden for $m_{Z'} > m_\pi$; suppressed $2 \rightarrow 2$ annihilation via Z' -portal.

$\Rightarrow$ $3 \rightarrow 2$ dominance: SIMP conditions

Meet Unitarity

Too large $2 \rightarrow 2$ self-scattering at NLO. [Hansen et al (2015)]

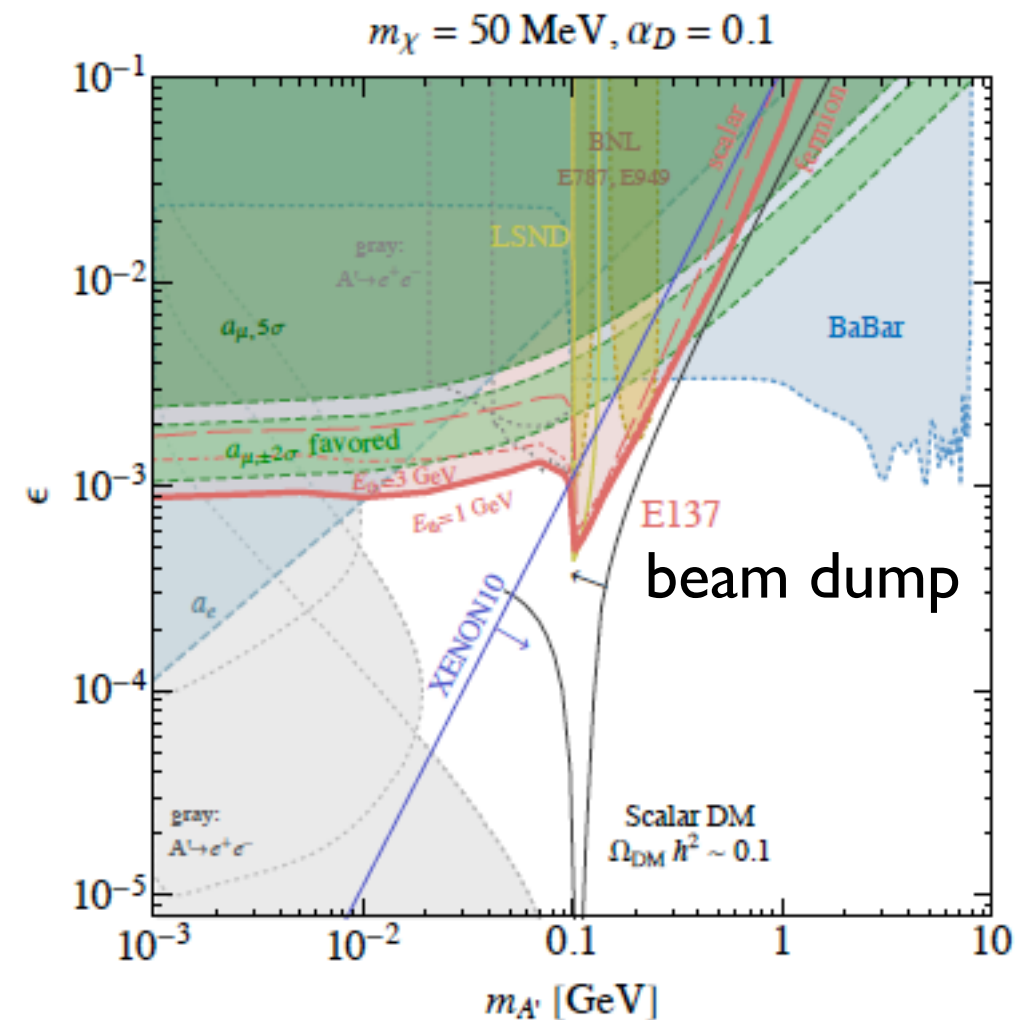
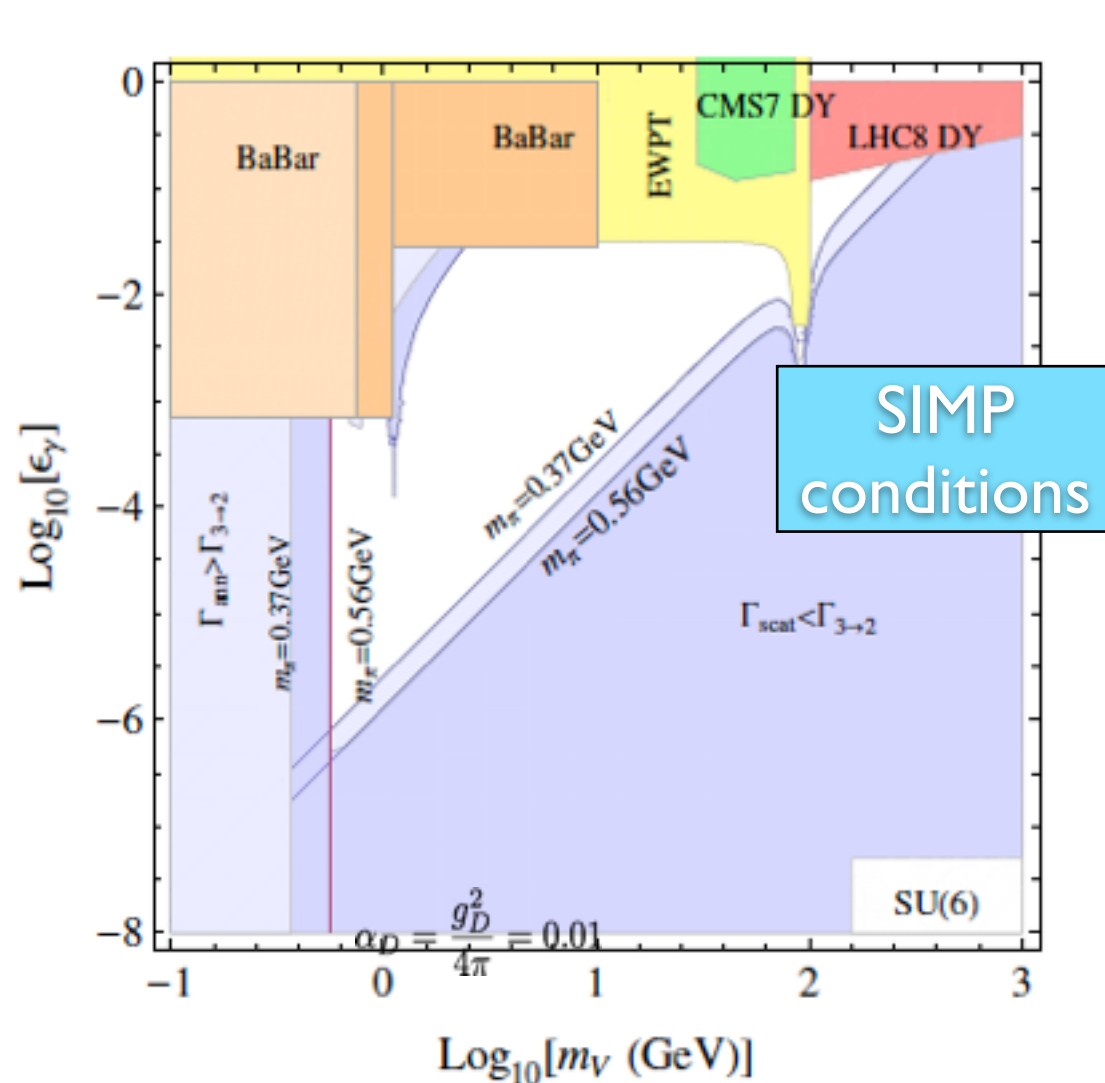


Enhanced $3 \rightarrow 2$ annihilation near Z' resonance with gauged WZW, but there is no enhancement for $2 \rightarrow 2$.

[HML, Seo, In Progress]

$$\langle \sigma v^2 \rangle \sim \frac{\alpha_D^2 N_c^2 m_\pi^5}{F^6} \frac{1}{(9m_\pi^2 - m_{Z'}^2)^2 + \Gamma_{Z'}^2 m_{Z'}^2} \left(\frac{T}{m_\pi} \right)^2$$

Collider searches



[Batell et al, 2014]

$$e^+e^- \rightarrow \gamma Z' \rightarrow \gamma(l^+l^-), \quad e^+e^- \rightarrow \gamma + \text{MET} \quad (\text{BaBar}),$$

$$h \rightarrow ZZ' \quad (\text{CMS 8TeV}), \quad \text{Drell-Yan, dileptons.}$$

- SIMP parameter space can be probed by Z' searches.
- Beam dumps & DM-nucleon scattering lead to similar limits.

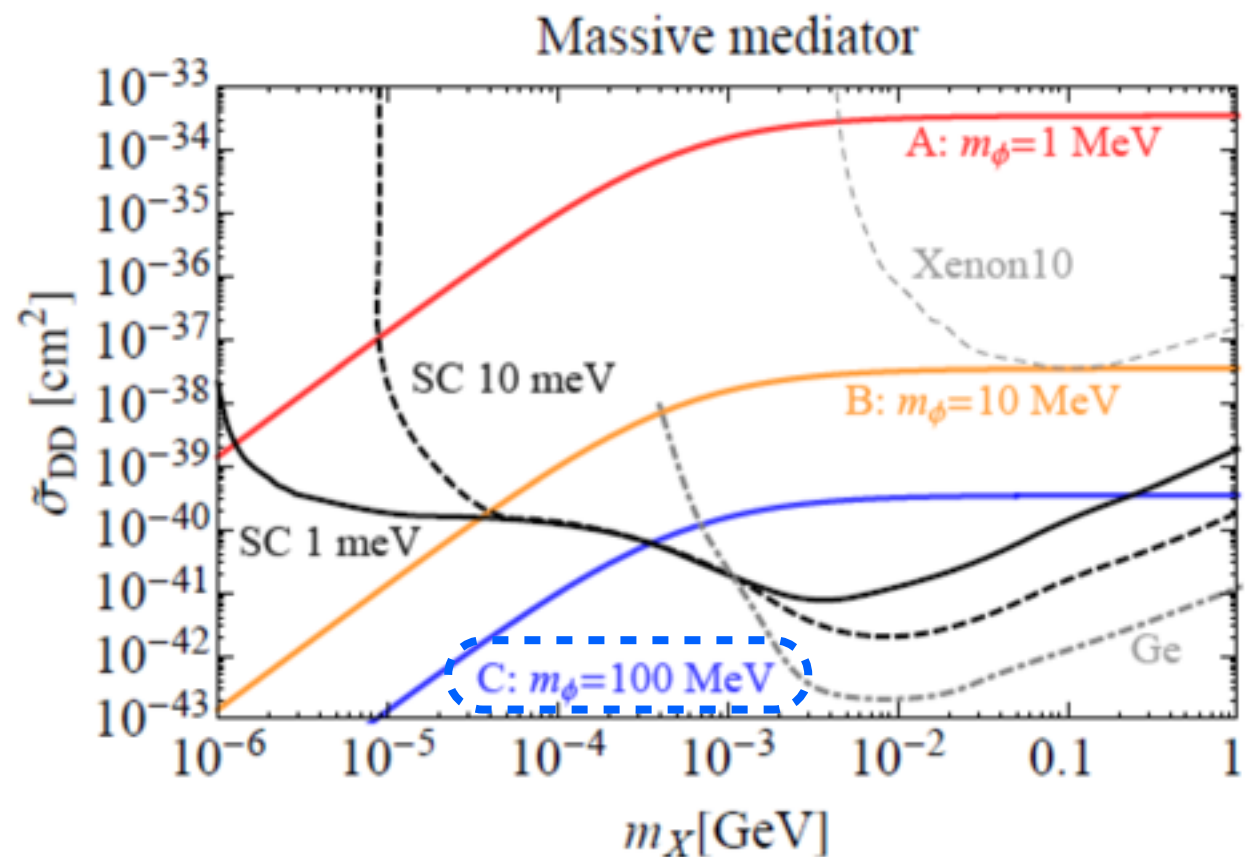
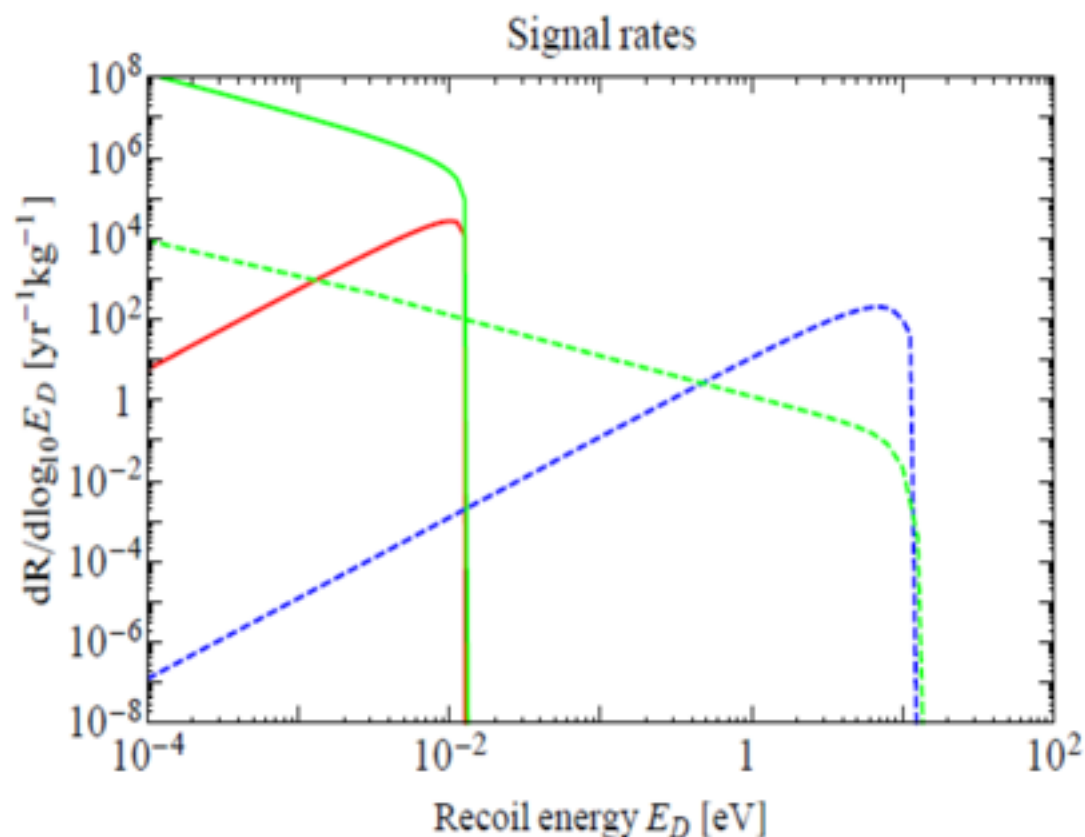
Direct detection

- SIMP dark mesons scatters off electrons, with small threshold for recoil energy: $\left(E = \frac{q^2}{2m_e} \lesssim 20 \text{ eV}\right)$

$$\sigma_{\text{DD}} = \frac{\varepsilon^2 e^2 g_D^2 \mu^2}{\pi m_{Z'}^4} \quad (q = \mu v_{\text{DM}}, \mu = m_e m_\chi / (m_e + m_\chi))$$

Superconducting detectors: scattering with free electrons in a metal (Al) $\rightarrow$ sensitive to meV recoil energy.

[Hochberg et al (2015)]

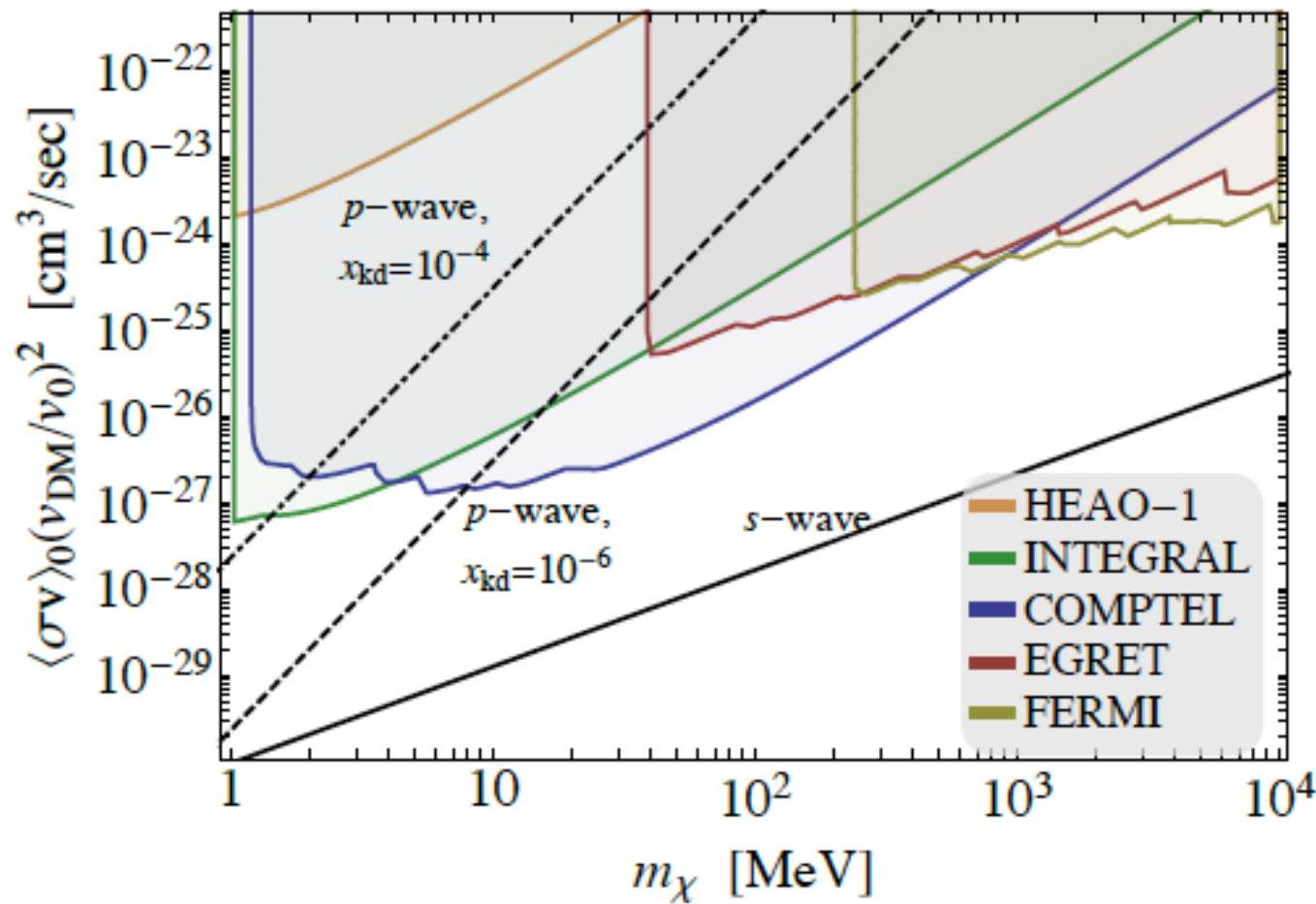


Blue: $(m_\phi, m_X, \alpha_X, g_e) = (100 \text{ MeV}, 100 \text{ MeV}, 0.1, 3 \times 10^{-5})$

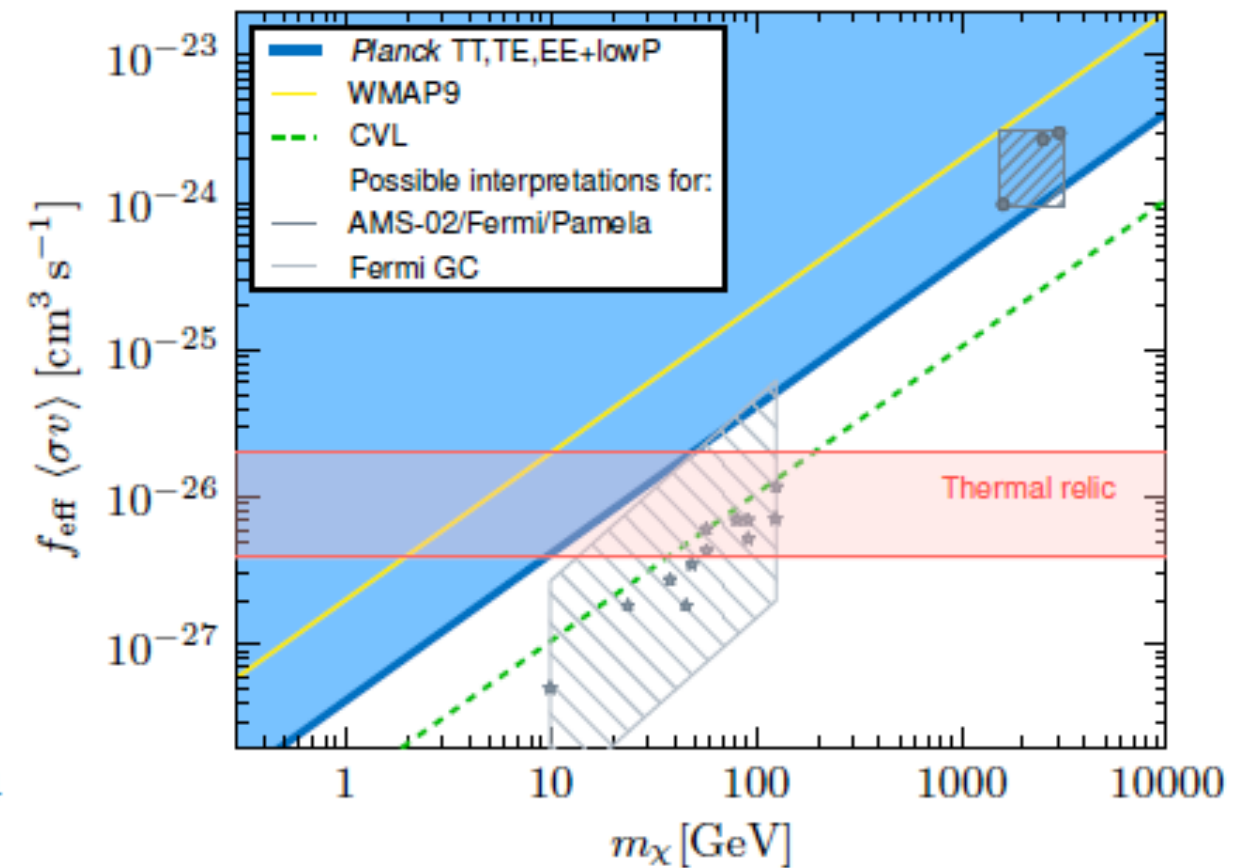
Indirect detection

Galactic Center

$\chi\chi \rightarrow e^+e^-$



CMB



[Essig et al, 2013]

X-ray/gamma-ray & CMB can constrain sub-GeV DM.

No bound on $2 \rightarrow 2$ ann for scalar DM (p-wave suppressed).

$$\langle\sigma v_{\text{rel}}\rangle_{l+l^-} = \left(1.2 \times 10^{-27} \text{cm}^3/\text{s}\right) \left(\frac{\varepsilon_2}{10^{-6}}\right)^2 \left(\frac{100 \text{MeV}}{m_\pi}\right)^2, \quad \varepsilon_2(T) = \varepsilon_2(T_F) \sqrt{T/T_F}$$

SIMP with discrete symmetries

DM stability

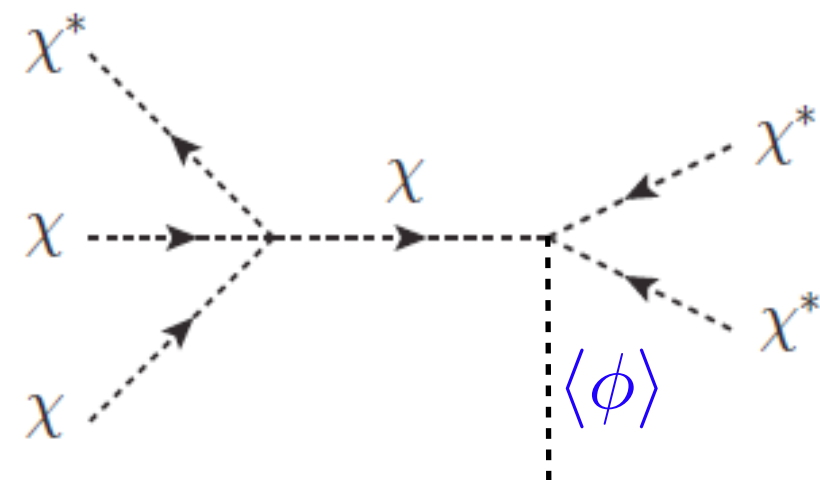
[S.-M.Choi, HML, 2015]

- Fundamental stable particle for SIMP?
- Z_3 is the minimal discrete symmetry consistent with SIMP, which is a remnant of a local $U(1)$.
- Built-in Z' gauge boson communicates with the SM via the kinetic mixing.

	ϕ	χ
$U(1)_V$	+3	+1

Table 1: $U(1)_V$ charges.

$$\langle \phi \rangle = \frac{1}{\sqrt{2}} v' \Rightarrow U(1)_V \rightarrow Z_3.$$



Z₃ Model

- χ : Dark Matter, H : Dark Higgs, V : Dark photon.

$$\mathcal{L} = -\frac{1}{4}V_{\mu\nu}V^{\mu\nu} - \frac{1}{2}\sin\xi V_{\mu\nu}B^{\mu\nu} + |D_\mu\phi|^2 + |D_\mu\chi|^2 + |D_\mu H|^2 - V(\phi, \chi, H)$$

$$D_\mu\chi = (\partial_\mu - iq_\chi g_D V_\mu)\chi$$

$$V(\phi, \chi, H) = V_{\text{DM}} + V_{\text{SM}} \text{ with}$$

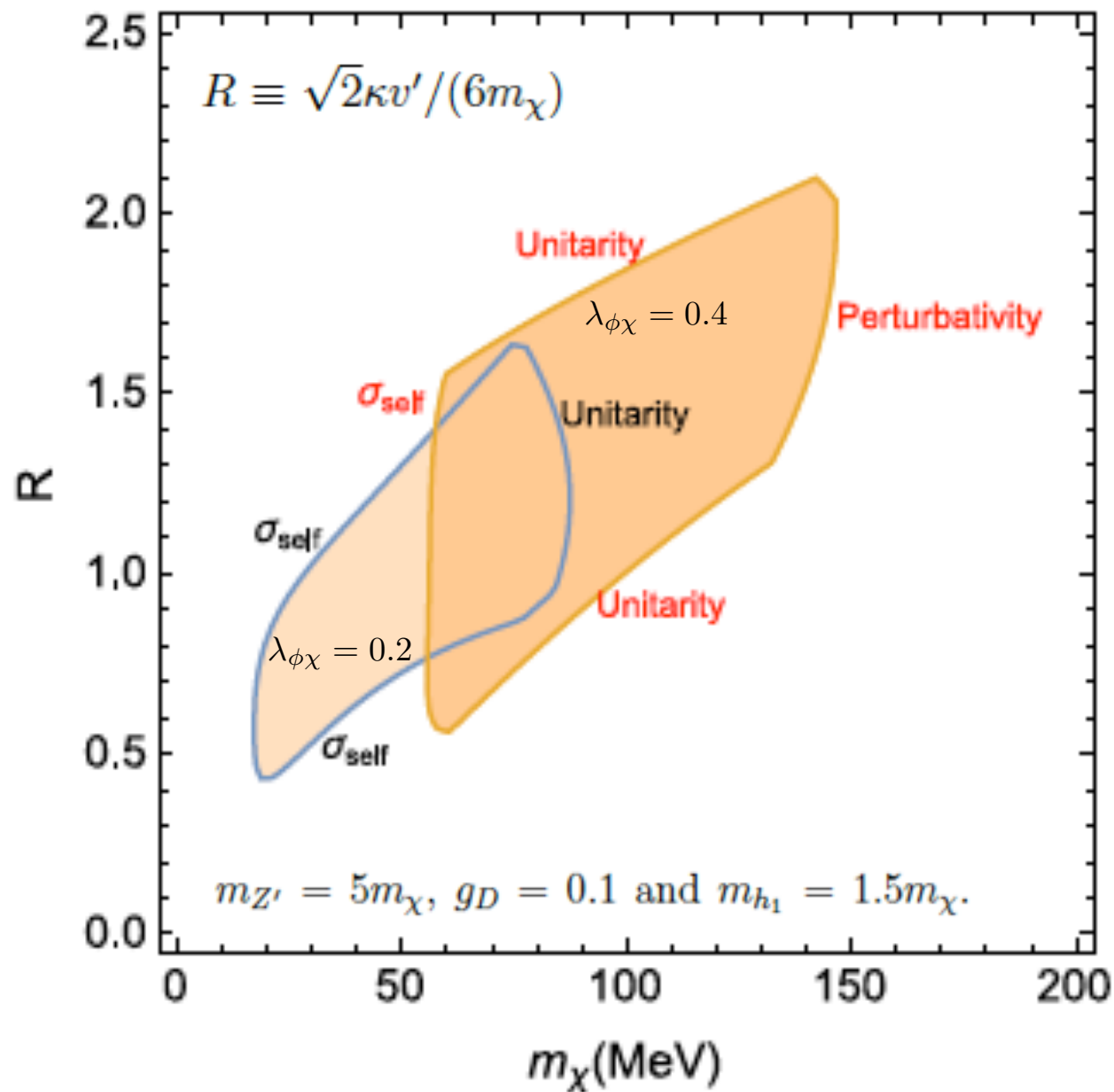
$$V_{\text{DM}} = -m_\phi^2|\phi|^2 + m_\chi^2|\chi|^2 + \lambda_\phi|\phi|^4 + \lambda_\chi|\chi|^4 + \lambda_{\phi\chi}|\phi|^2|\chi|^2 \\ + \left(\frac{\sqrt{2}}{3!}\kappa\phi^\dagger\chi^3 + \text{h.c.}\right) + \lambda_{\phi H}|\phi|^2|H|^2 + \lambda_{\chi H}|\chi|^2|H|^2,$$

$$V_{\text{SM}} = -m_H^2|H|^2 + \lambda_H|H|^4.$$

cubic coupling for broken U(1)

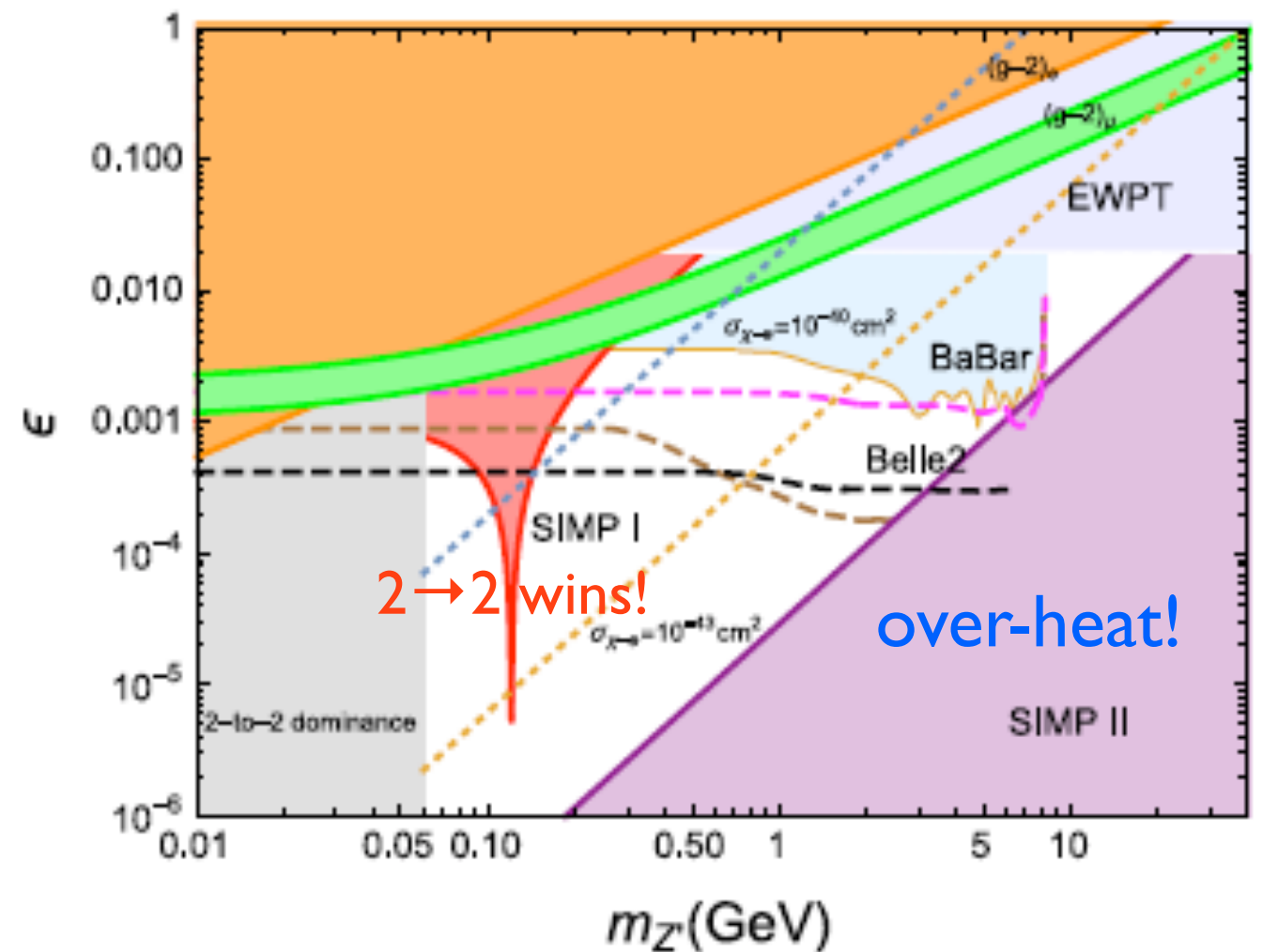
SIMP parameter space

$\sigma_{\text{self}}/m_\chi < 1 \text{ cm}^2/\text{g}$, perturbativity



Bullet cluster bound,
perturbativity imposed.

$m_\chi = 60 \text{ MeV}$, $g_D = 0.3$



BaBar γ +MET; Belle2
projection; EWPT; g-2;
XENON10; (similar limits
from beam dump)

Z₅ model

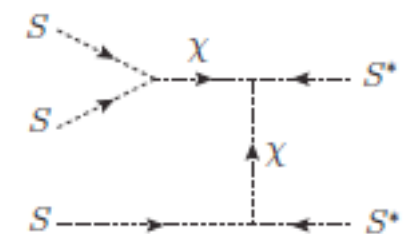
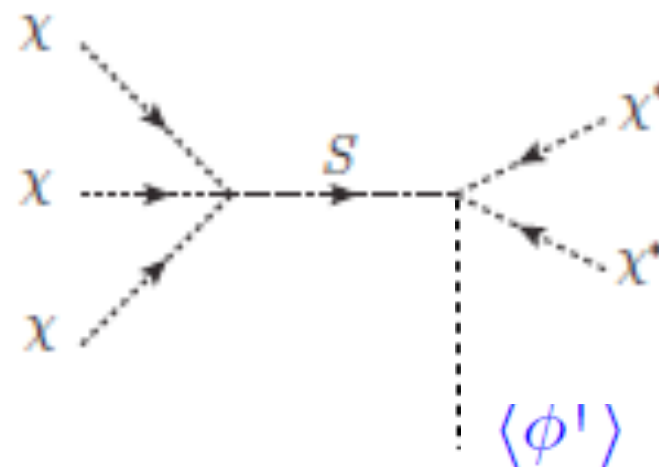
[S.M.Choi, HML, 2016]

Z₅ is a natural symmetry for 5-point interaction, which requires an extra heavy field.

	ϕ	χ	S
$U(1)_V$	+5	+1	+3

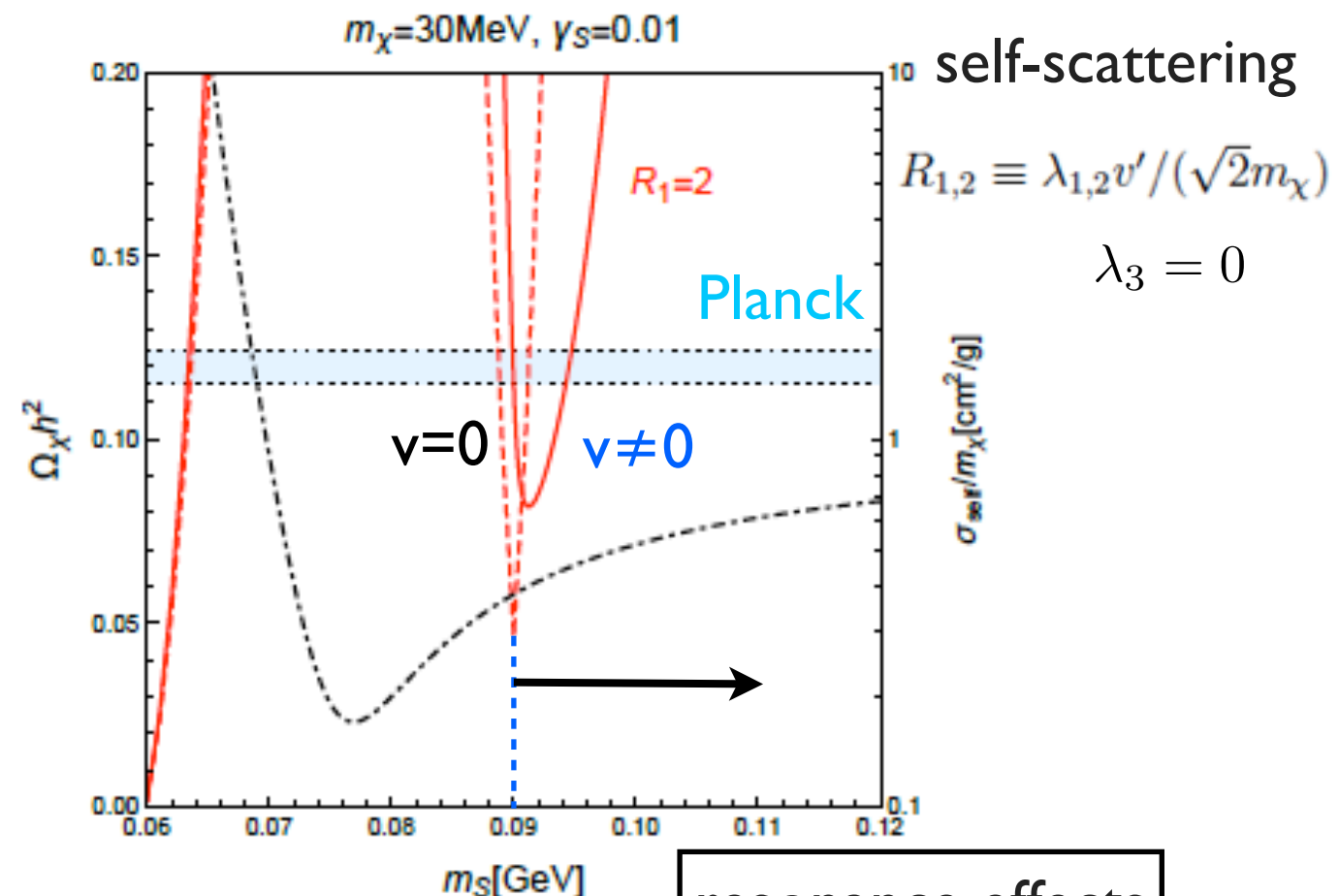
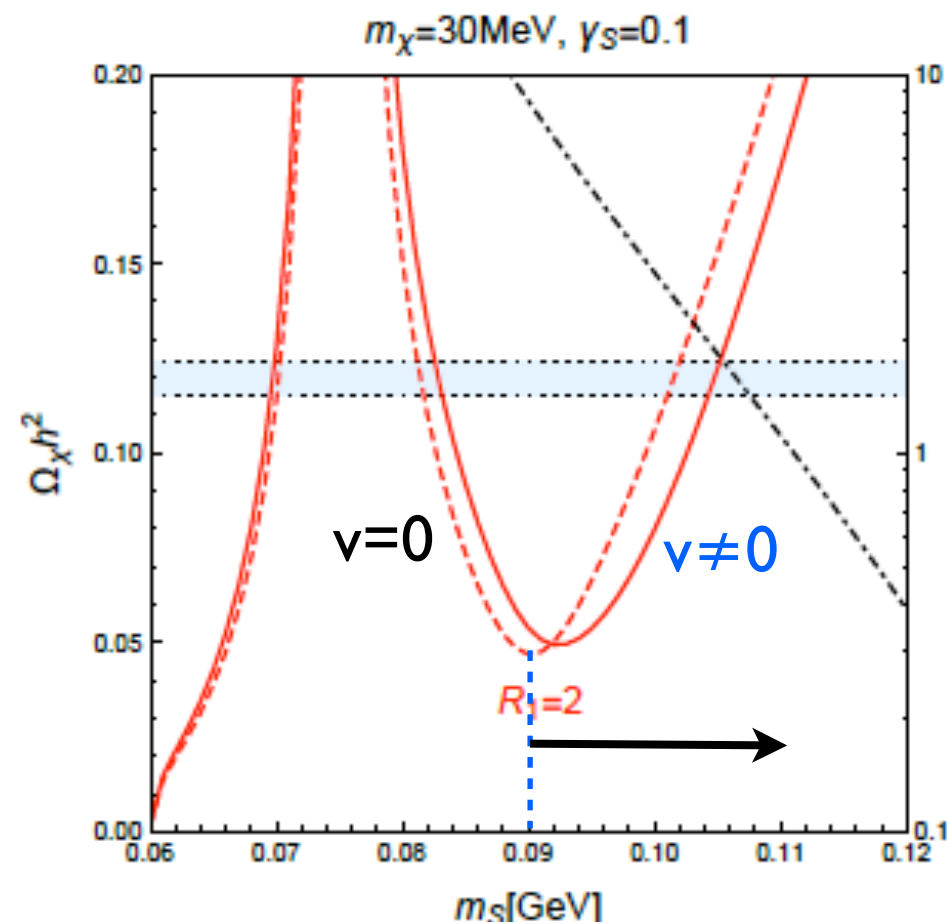
Table 1: $U(1)_V$ charges.

$$\mathcal{L}_{\text{int}} \supset \frac{1}{\sqrt{2}}\lambda_1\phi^\dagger S^2\chi^\dagger + \frac{1}{\sqrt{2}}\lambda_2\phi^\dagger S\chi^2 + \frac{1}{6}\lambda_3 S^\dagger\chi^3 + \text{h.c.}$$



- $3 \rightarrow 2$ annihilation can be enhanced near resonance.
- Z' again makes SIMP DM in kinetic equilibrium.

SIMP Resonance



resonance effects
important!

$$(\sigma v^2)_\chi \equiv \frac{c_\chi}{m_\chi^5} \frac{\gamma_S^2}{(\epsilon_S - v_{\text{rel}}^2/4)^2 + \gamma_S^2}$$

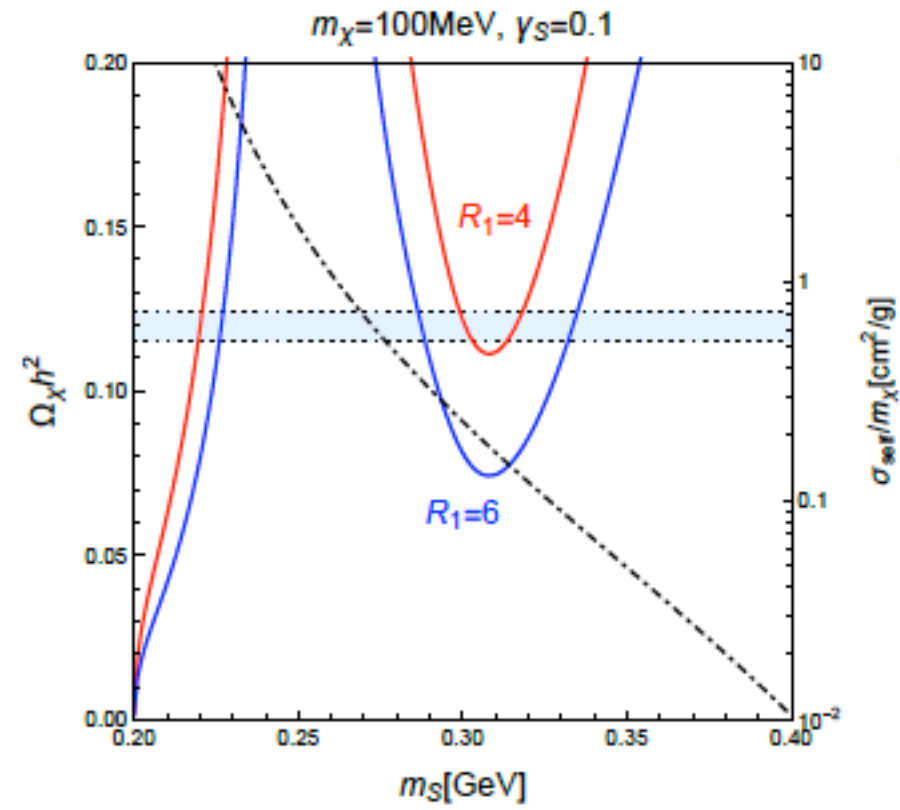
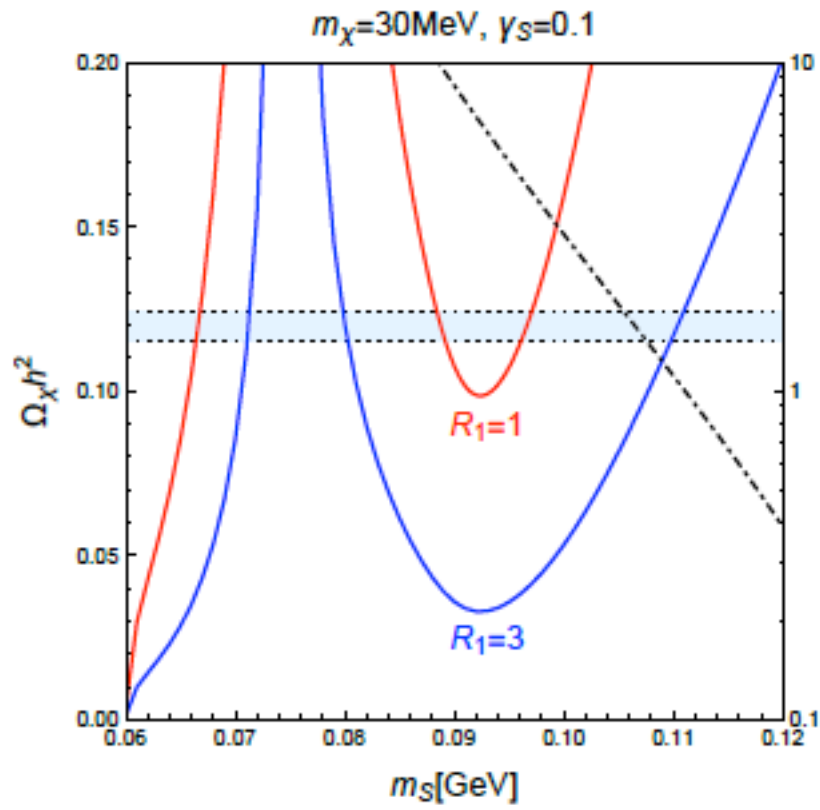
$$\gamma_S \equiv m_S \Gamma_S / (9m_\chi^2), \quad \epsilon_S \equiv (m_S^2 - 9m_\chi^2) / (9m_\chi^2)$$

narrow width: $\gamma_S \ll 1$ $\rightarrow$

$$\langle (\sigma v^2)_\chi \rangle \approx \frac{2c_\chi}{m_\chi^5} x^{3/2} \sqrt{\pi} \gamma_S \epsilon_S^{1/2} e^{-x\epsilon_S} \theta(\epsilon_S)$$

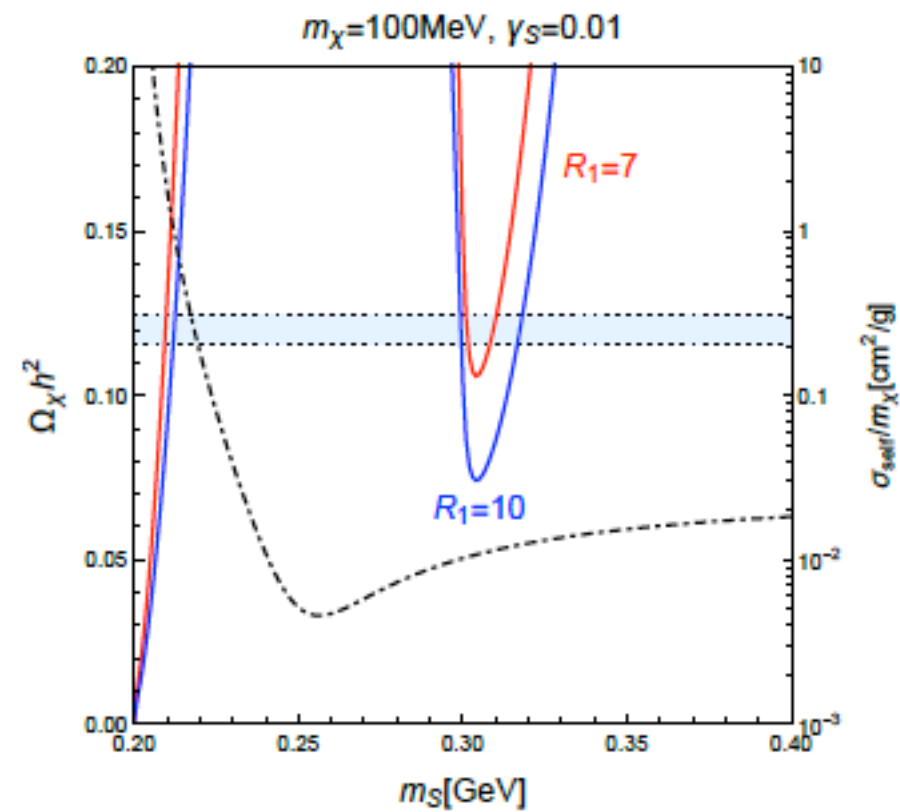
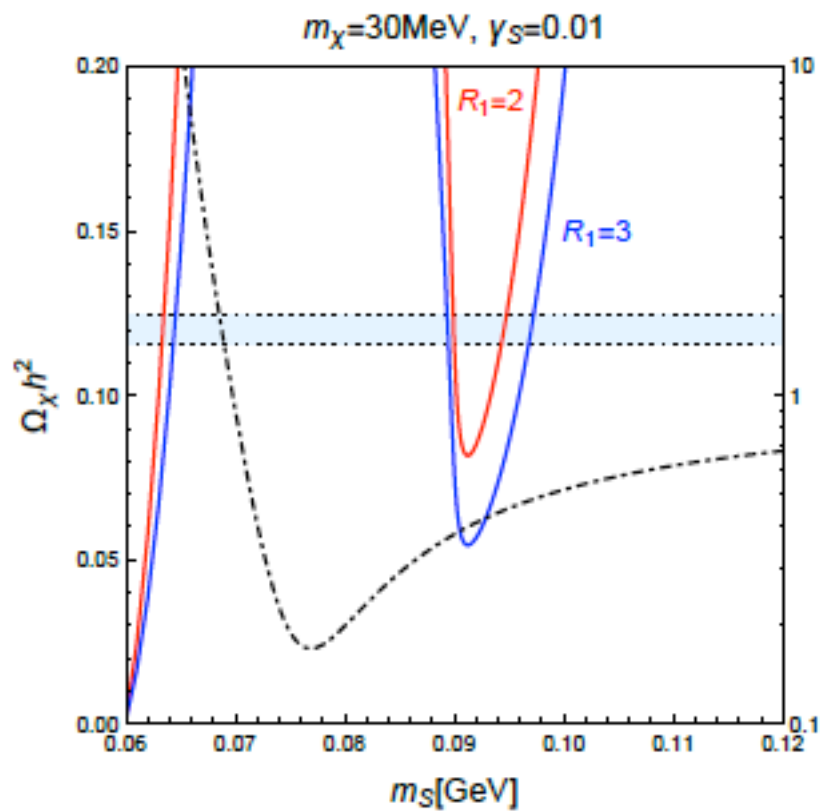
Resonance-enhanced due to
nonzero velocity above threshold.

$\Rightarrow$ Allows for small coupling!



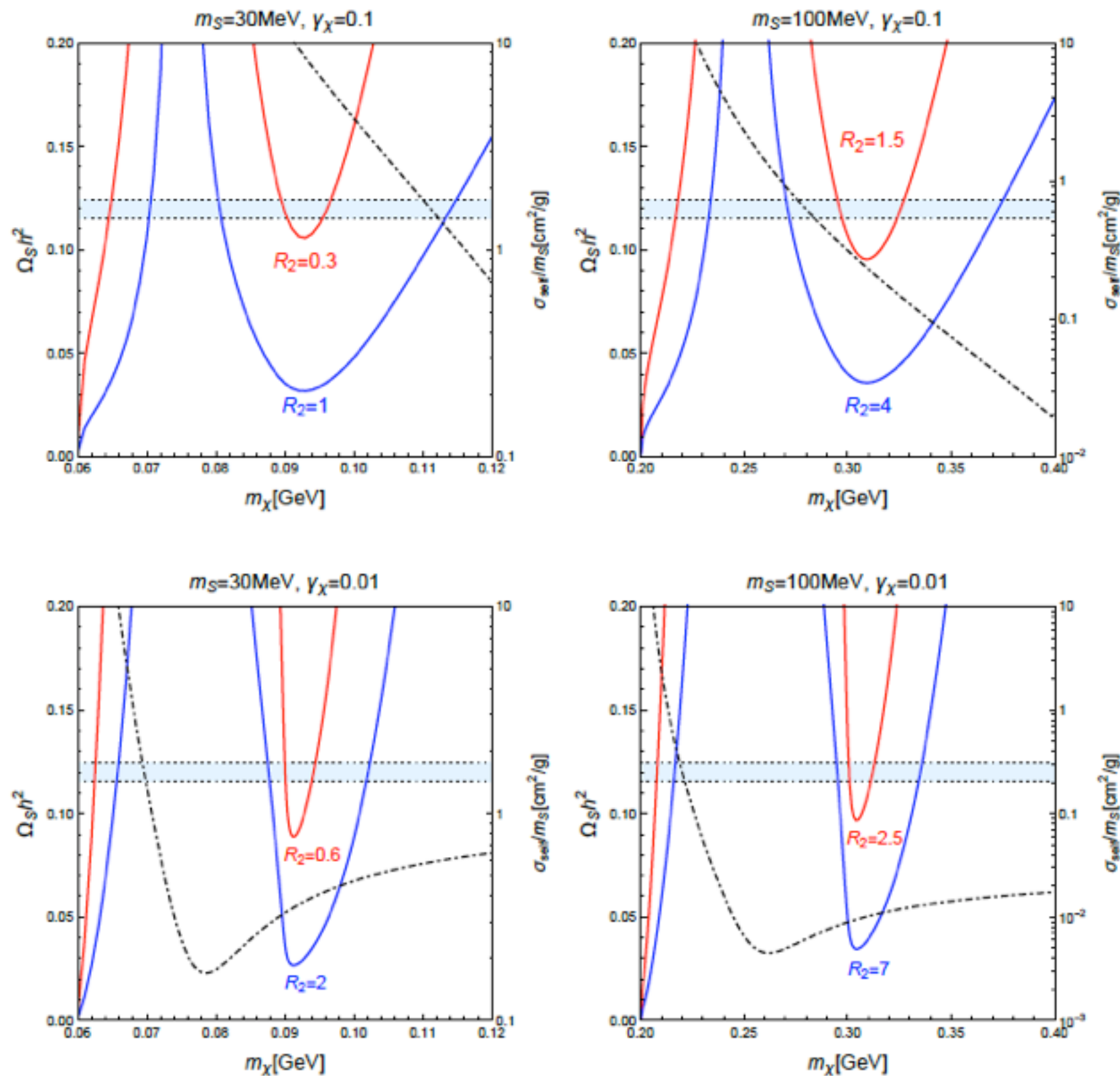
$$R_{1,2} \equiv \lambda_{1,2} v' / (\sqrt{2} m_\chi)$$

$$\lambda_3 = 0$$



self-scattering: $m_V = 500 \text{ MeV}, g_D = 0.1$ and $\lambda_S = 1$

S SIMP case



$$R_{1,2} \equiv \lambda_{1,2} v' / (\sqrt{2} m_\chi)$$

self-scattering: $m_V = 500 \text{ MeV}$, $g_D = 0.1$ and $\lambda_S = 1$

Conclusions

- SIMP is a new thermal dark matter with sub-GeV mass, which would require different strategies for direct detection.
- Generalized WZW term with vector-like dark $U(1)$ makes dark mesons consistent SIMP.
- SIMP with discrete symmetries has built-in mechanisms for stabilization and kinetic equilibrium.
- Bounds on self-interaction bounds can be avoided near resonance for $3 \rightarrow 2$ annihilation.
- SIMP dark matter is testable via self-interactions, mediator particle, and DM elastic scattering, etc.