

Cosmology for sub-GeV Dark Matter

Kenji Kadota

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Based on the work with:

Paolo Gondolo(Utah), Toyokazu Sekiguchi (IBS) , Yi Mao (Paris),
Joe Silk (Oxford, Paris, Johns Hopkins), Hiroyuki Tashiro (Nagoya),
Junji Hisano (Nagoya), Kiyotomo Ichiki (Nagoya)

Cosmology for sub-GeV Dark Matter

Outline

➤ Motivation:

Motivation for sub-GeV DM

Motivation for DM-baryon interactions

- ✓ Halo abundance

- ✓ 21 cm

- ✓ Minimum Protohalo Mass

➤ Concrete example for DM-baryon interactions

Interaction via photon: How "dark" is dark matter?

- ✓ Dipole DM

- ✓ Millicharged DM

We know little about DM

Let's not get biased, and explore beyond the conventional paradigm

➤ Particle physics search for DM:

Dominated by the search for weakly interacting massive particles (WIMPs), $5 \sim 1000$ GeV

Today's talk: interested in less than GeV

➤ Cosmological search (e.g. large scale structure of the Universe) :

Lambda-CDM model : Gravitational interactions, Cold, Non-baryonic

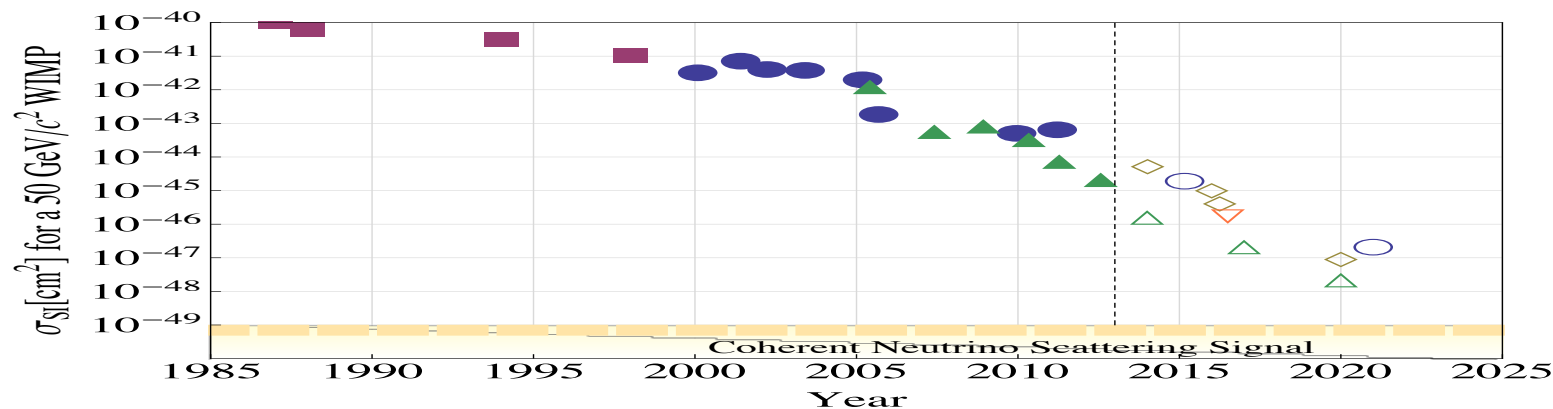
Today's talk: interested in DM-baryon interactions by the light mediator

(e.g. photon: dark matter is not completely "dark")

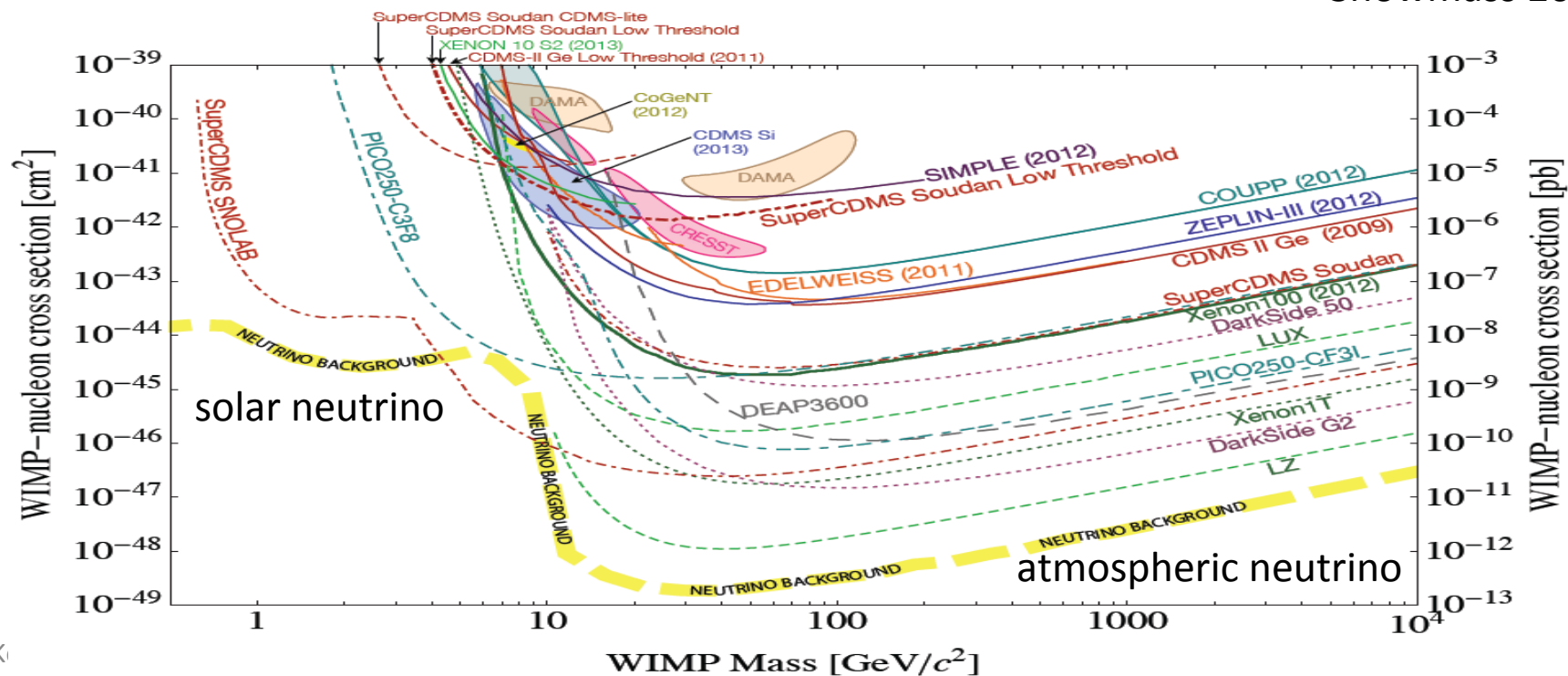
Motivation for sub-GeV

Direct detection experiments

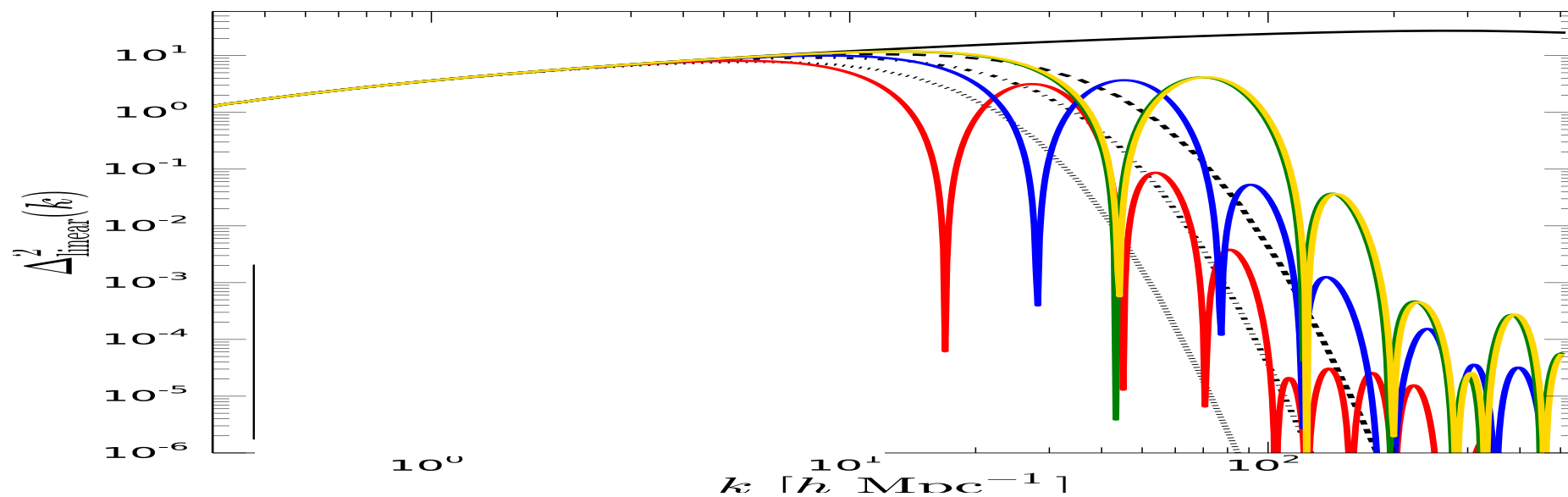
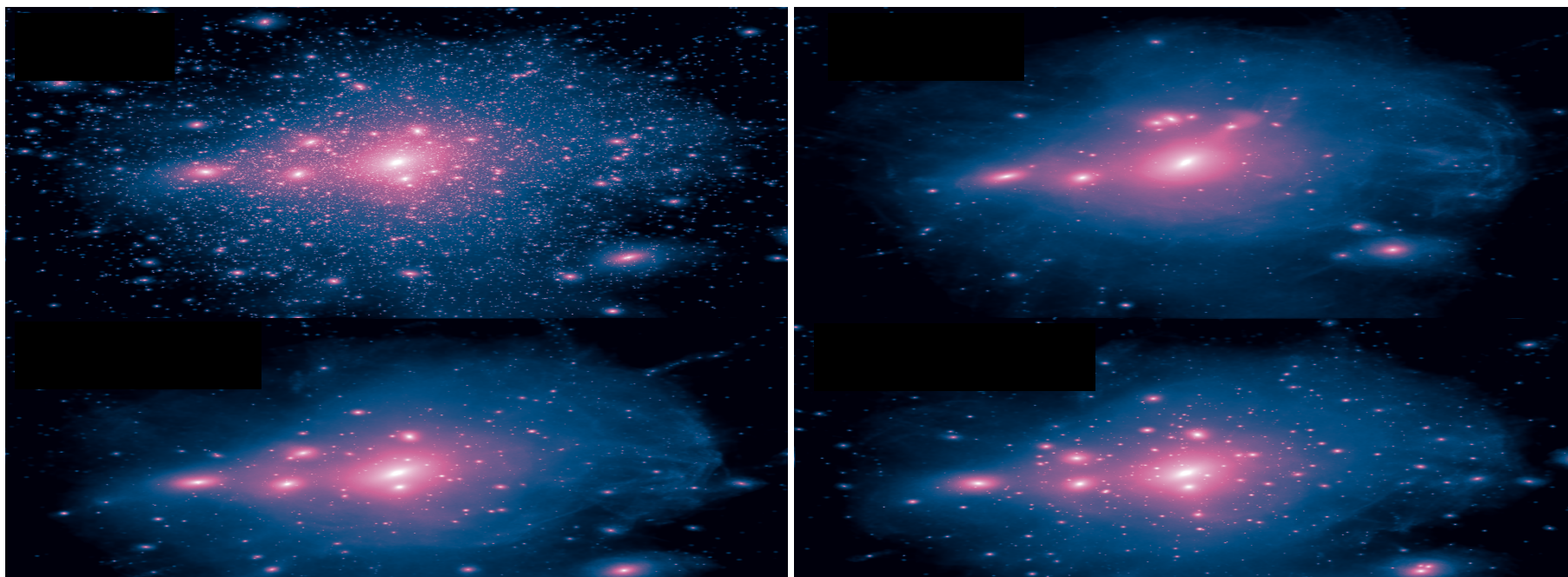
Moore's law for dark matter



Snowmass 2013



Motivation for DM-baryon interactions, beyond Λ CDM



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IBS-SNU workshop

(Vogelsberger et al (2016))

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$$(1+z) \frac{dT_d}{dz} = 2T_d + \frac{2m_d}{m_d + m_H} \frac{K_b}{H} (T_d - T_b),$$

$$(1+z) \frac{dT_b}{dz} = 2T_b + \frac{2\mu_b}{m_e} \frac{K_\gamma}{H} (T_b - T_\gamma) + \frac{2\mu_b}{m_d + m_H} \frac{\rho_d}{\rho_b} \frac{K_b}{H} (T_b - T_d)$$

Momentum transfer rate

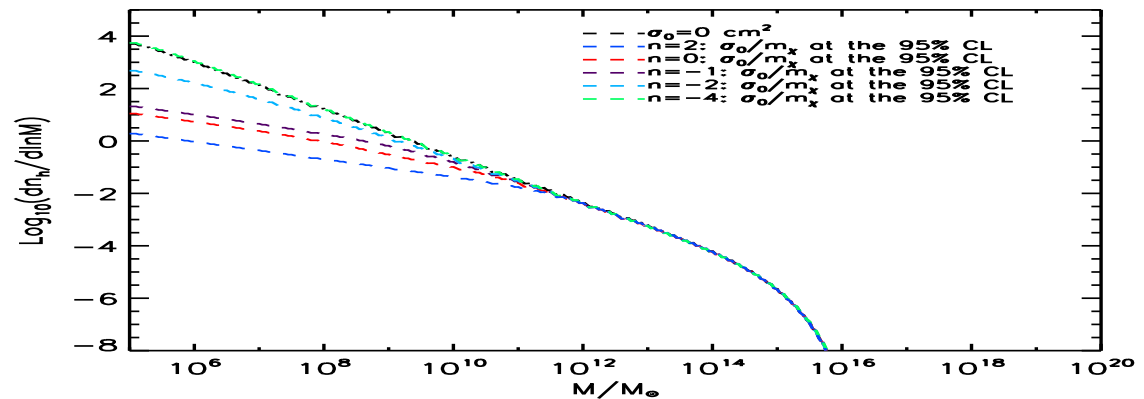
$$K_\gamma = \frac{4\rho_\gamma}{3\rho_b} n_e \sigma_T \quad (\text{Compton collision rate})$$

$$K_b = \frac{c_n \rho_b \sigma_0}{m_H + m_d} \left(\frac{T_b}{m_H} + \frac{T_d}{m_d} \right)^{\frac{n+1}{2}}, \quad \sigma(v) = \sigma_0 v^n$$

✧ Planck+SDSS

(Dvorkin, Blum and Kamionkowski (2013))

n	$\sigma / m_{DM} v$ (95%CL, cm ² /g)
-4	1.7×10^{-17}
-2	6.2×10^{-10}
-1	1.4×10^{-6}
0	3.3×10^{-3}
+2	9.5×10^3



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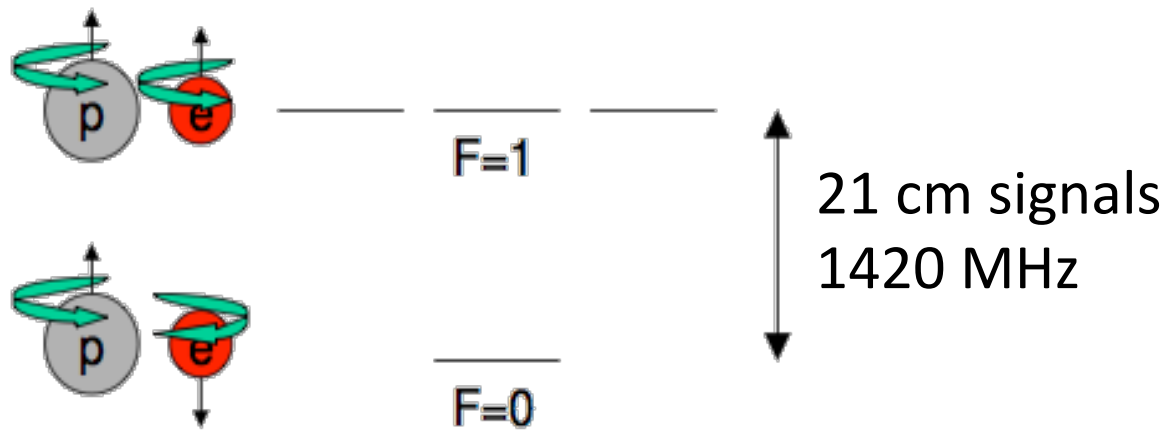
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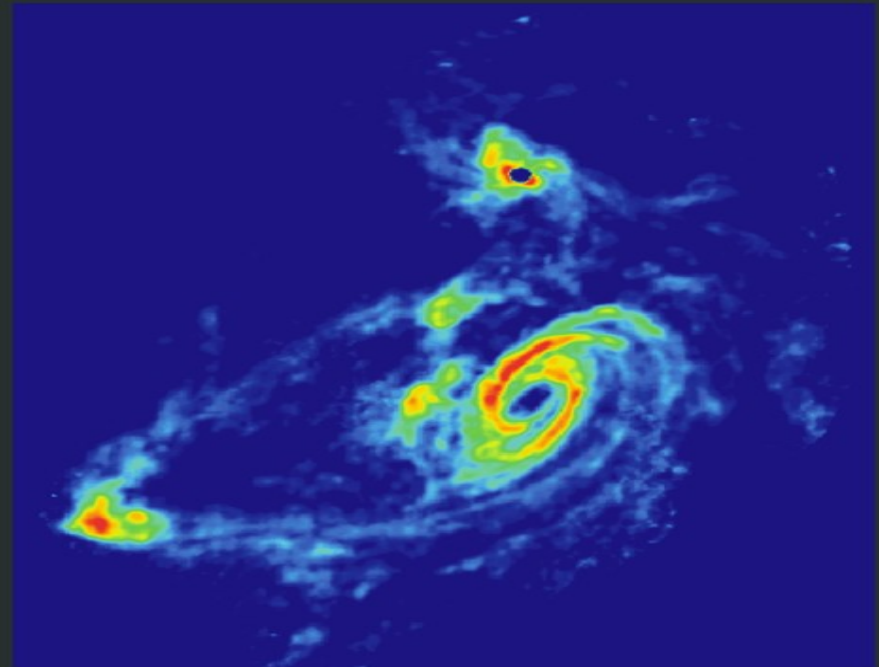
TIDAL INTERACTIONS IN M81 GROUP

Stellar Light Distribution



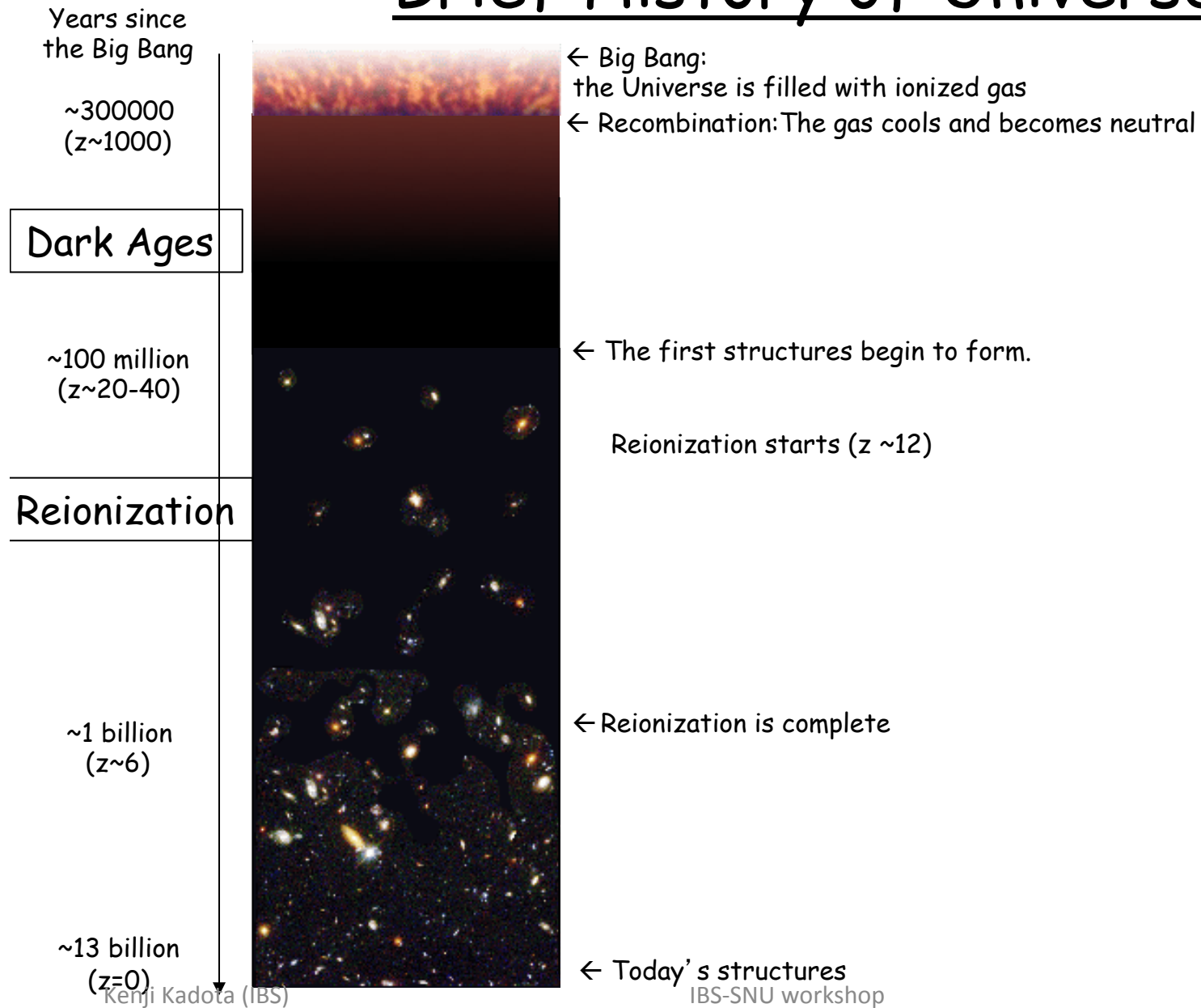
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21 cm HI Distribution



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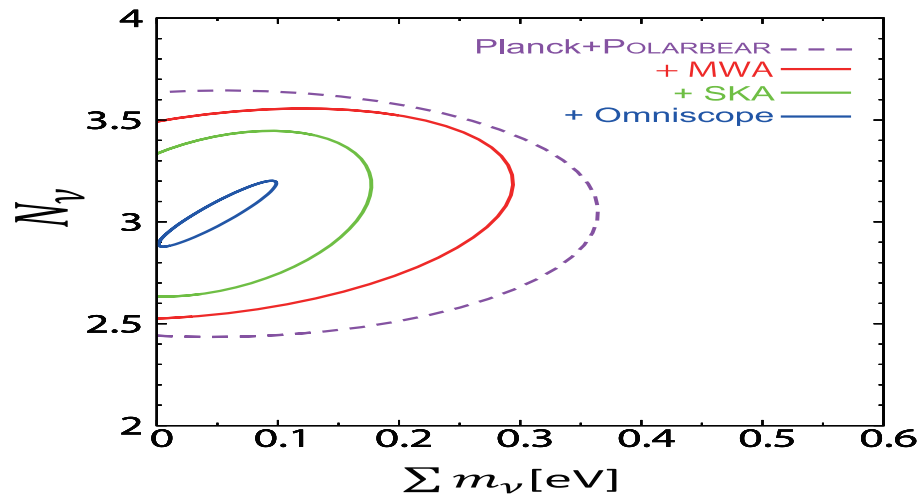
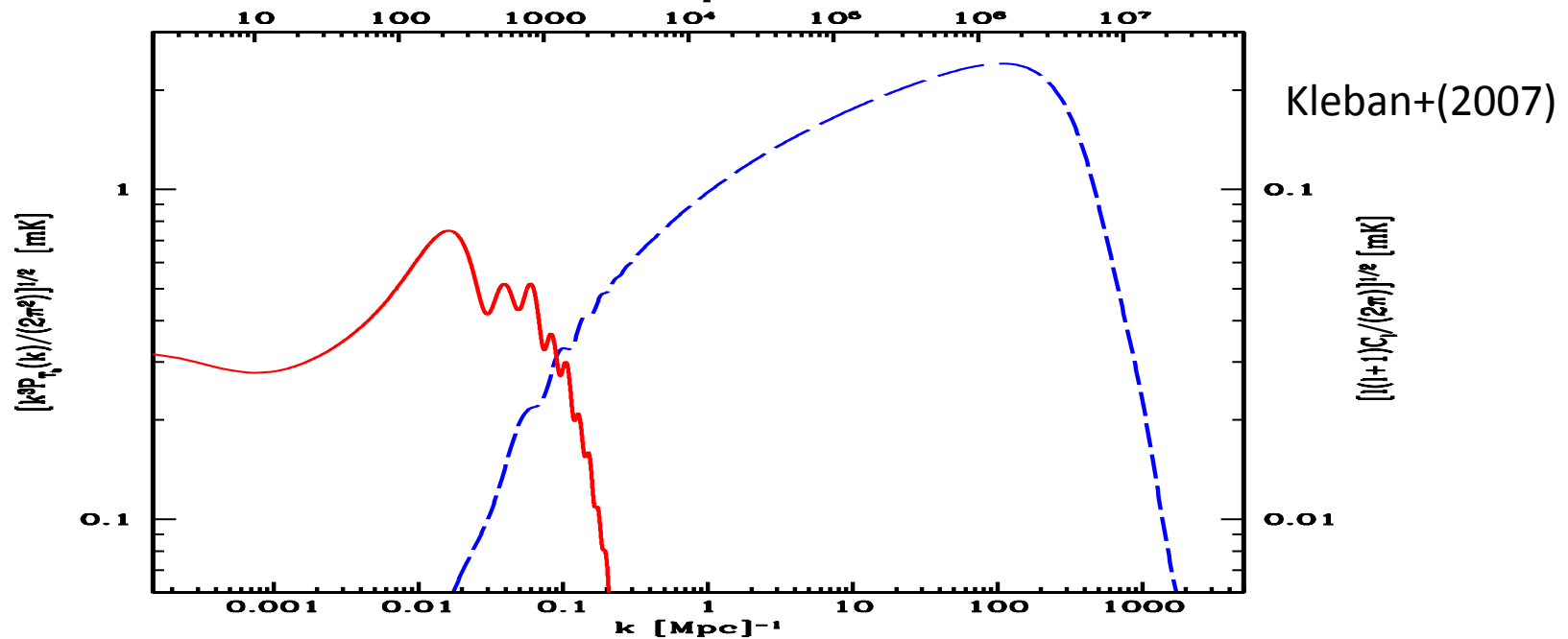
Brief History of Universe



What can we do with 21cm?

High precision on small-scale power spectrum

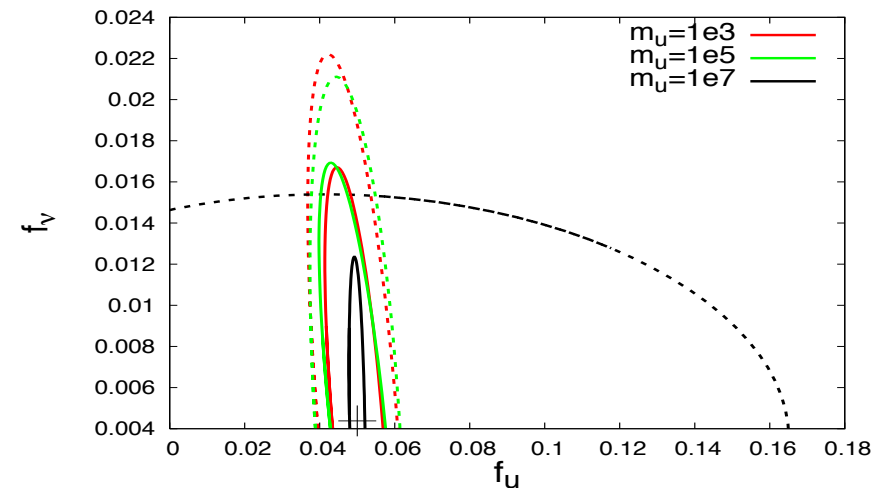
$$\Delta P / P \sim 1 / \sqrt{N}$$



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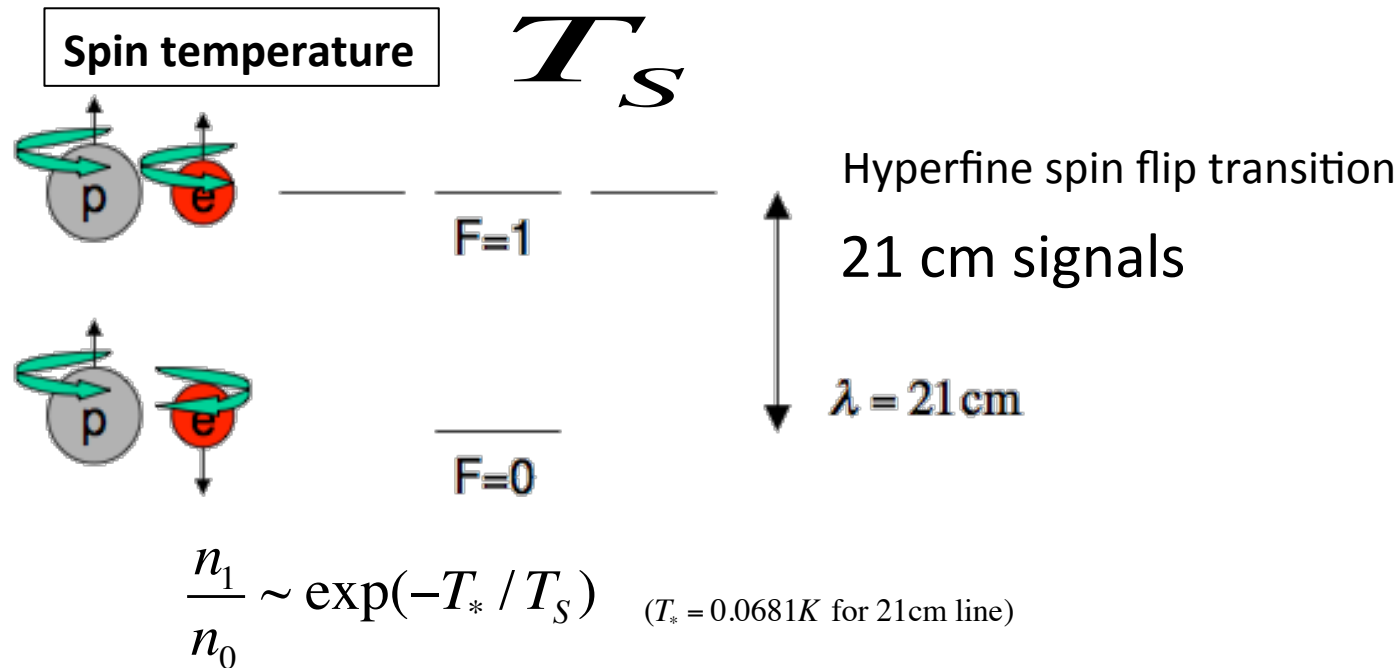
Oyama+(2013)

IBS-SNU workshop



KK, Mao, Ichiki, Silk (2014)

What can we measure through 21cm signals?



The occupation number of each level (equivalently spin temperature) can be altered by

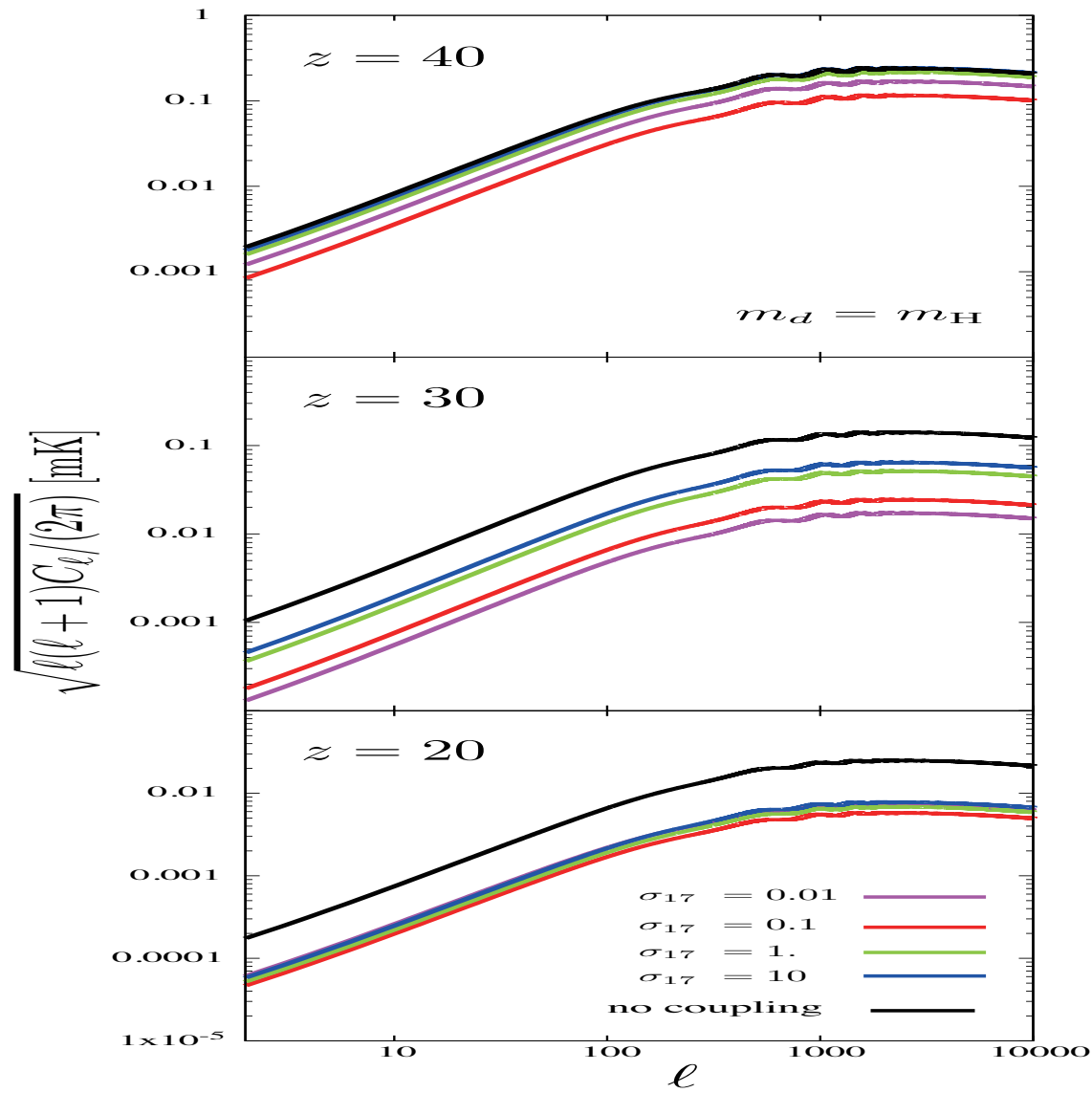
- a) the absorption/stimulated emission from/to CMB photons
- b) collision with other gas particles (other hydrogen atoms, protons and electrons).

T_s is the weighted average of CMB temperature and gas temperature (Field (1958)):

$$T_s = \frac{T_{CMB} + y_c T_k}{1 + y_c}$$

If collision is efficient, coupling coefficient y_c gets big and $T_s \rightarrow T_k$
If y_c or T_k gets small, $T_s \rightarrow T_{CMB}$.

21 cm signals



Tashiro, KK, Silk (2014)

$$C_\ell \sim (\delta T_b)^2, \delta T_b \sim 26 \text{ mK} \left(1 - \frac{T_\gamma}{T_s} \right) \left(\frac{1+z}{10} \right)$$

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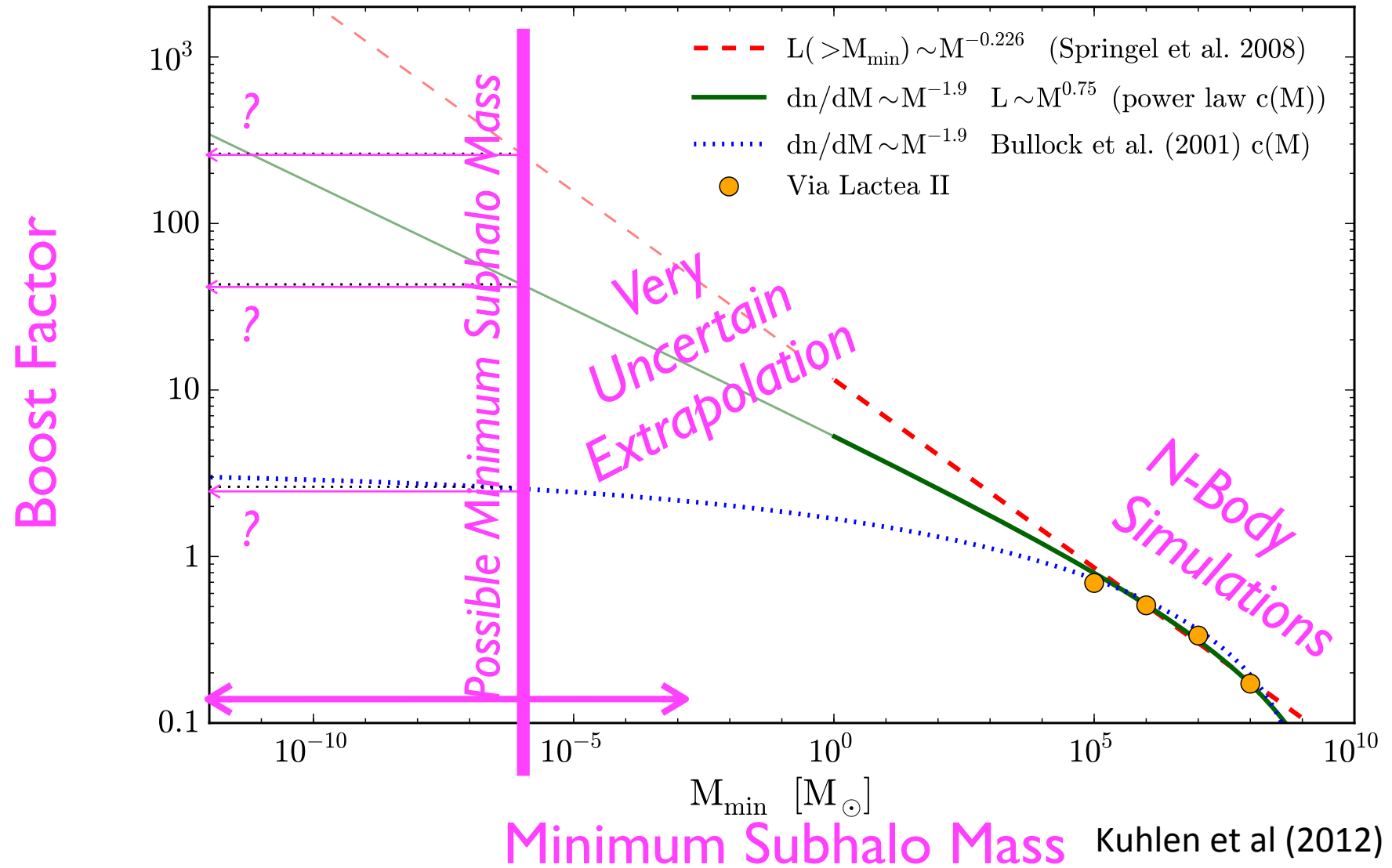
What is the size of the smallest gravitationally bound objects (protohalo)?

- Dark matter kinetic decoupling

- Analogous to:

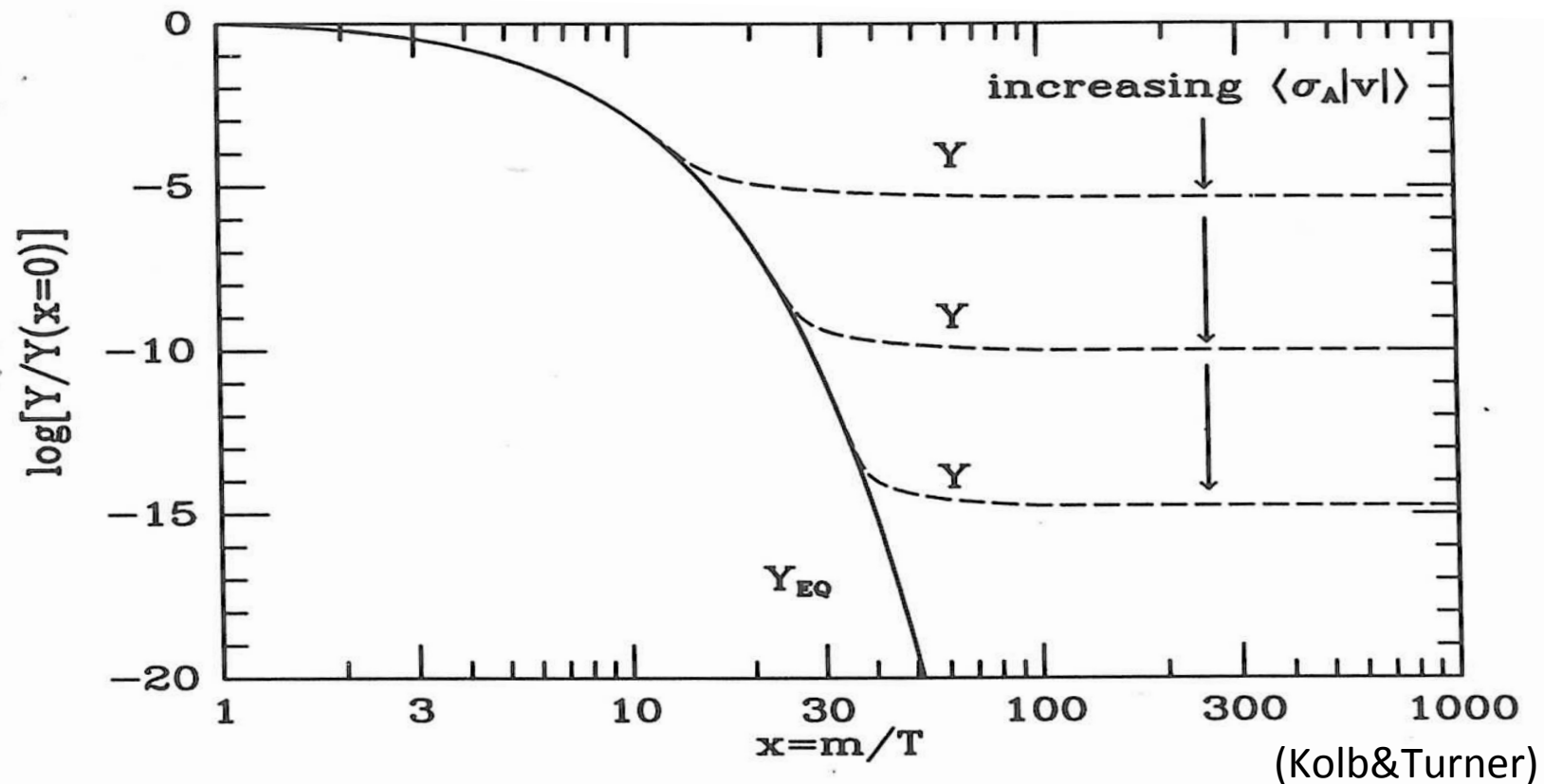
Physics of baryon decoupling

probing the nature of Universe via BAO and CMB



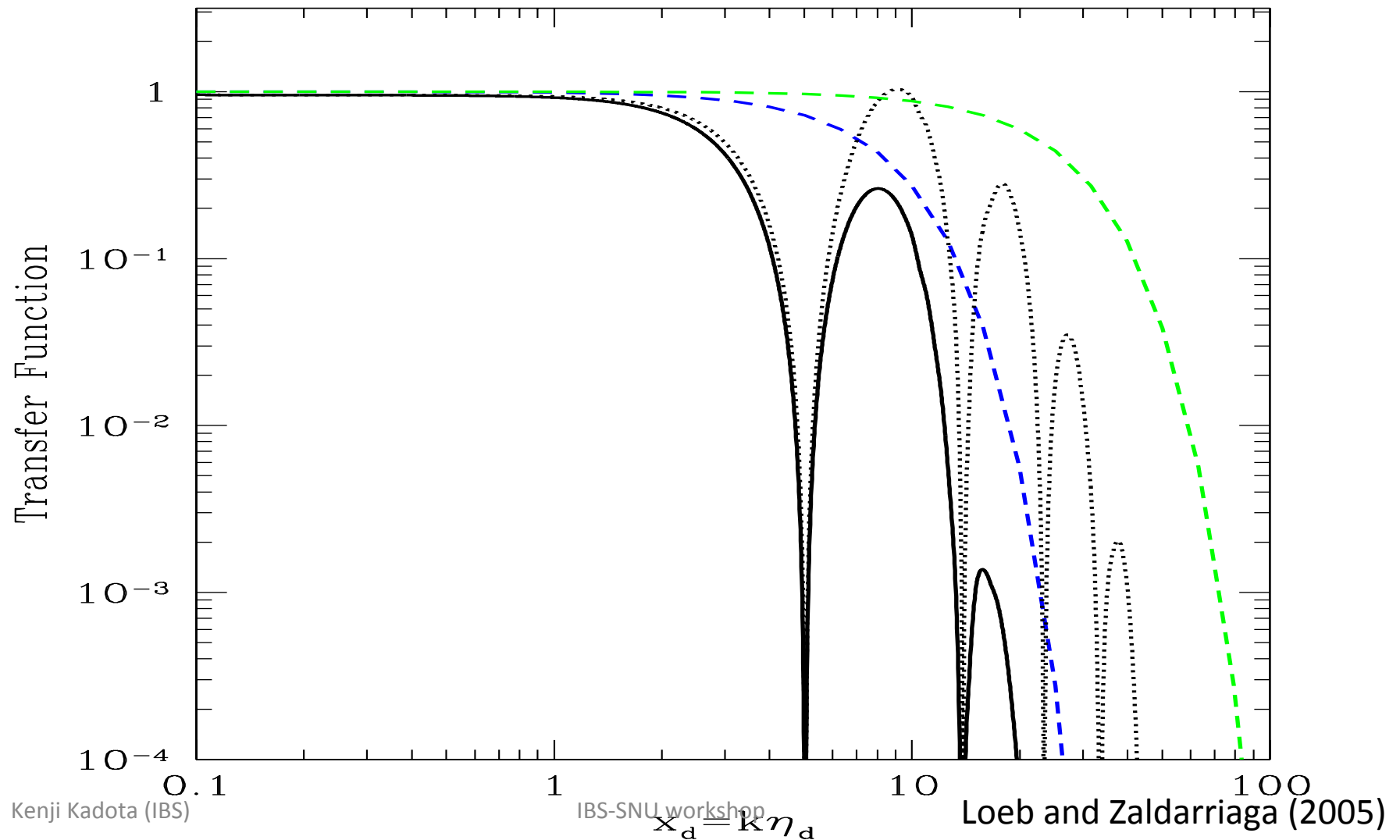
Taken from P. Gondolo's talk

Chemical decoupling and kinetic decoupling



- Chemical decoupling:
Annihilation $<$ Hubble expansion, $T \sim m_\chi/20$
- Kinetic decoupling:
Elastic scattering $<$ Hubble expansion, $T \sim m_\chi/2000$

Smallest dark matter halo size:
 Max (Free streaming scale, Horizon size)



letters to nature

polating the subhalo mass function to the smallest scale, the total number of substructure haloes $N(M > 10^{-6} M_{\odot})$ and the expected number density of subhaloes at the scale $n(R_{\odot}) \approx 500 \text{ pc}^{-3}$, assuming that they trace the mass. An extrapolation is made to much smaller masses than previously, the substructure within haloes collapsing at scales $\sim 10^7 M_{\odot}$ fits the extrapolation from large scales²³, even though they form from regions of the CDM spectra with effective index $n \approx -2.95$. Can these structures survive the strong disruptive gravitational forces from the Galaxy? The tidal radius is simply the inner Lagrange

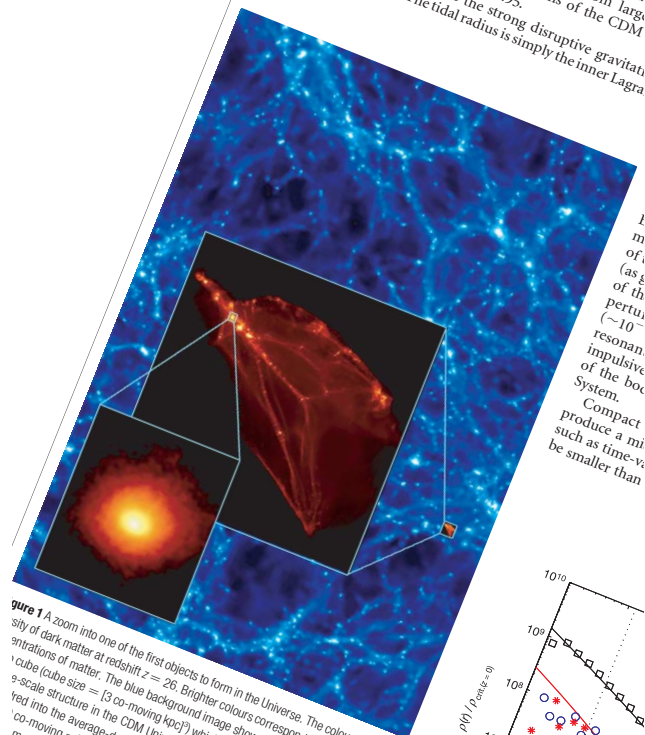


Figure 1 A zoom into one of the first objects to form in the Universe. The colours show the density of dark matter at redshift $z = 26$. Brighter colours correspond to regions of higher concentrations of matter. The blue background image shows the small-scale structure in a cube (cube size = 3 co-moving kpc) which has a filamentary topology similar to the large-scale structure in the CDM Universe. The first red image zooms by a factor of 10 into the average-density high-resolution region. This region was initially a co-moving pc^3 resolved with 64 million particles with a gravitational softening of 0.024 pc . A close-up of one of the individual dark-matter haloes in this region. The first Earth-mass halo has a central cusp-like density profile and is smooth. The index of the power spectrum is very steep on these scales. The haloes can collapse before merging into a larger system, rather than being disrupted by the Galaxy. The tidal radius is simply the inner Lagrange

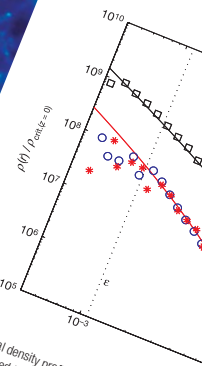


Figure 2 Radial density profiles of three typical mini-haloes. The density is plotted in physical units and we show low-resolution galaxy-cluster simulations²⁰, that is, $\rho(r)$ versus r in pc . We use the mean dark-matter profile of the $10^7 M_{\odot}$ halo as a comparison. The dashed line shows the profile of a $10^6 M_{\odot}$ halo, and the dotted line shows the profile of a $10^5 M_{\odot}$ halo. The solid line shows the profile of a $10^4 M_{\odot}$ halo. The index of the power spectrum is very steep on these scales. The haloes can collapse before merging into a larger system, rather than being disrupted by the Galaxy. The tidal radius is simply the inner Lagrange

Earth-mass dark-matter haloes as the first structures in the early Universe

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The Universe was nearly smooth and homogeneous before a redshift of $z = 100$, about 20 million years after the Big Bang. After this epoch, the tiny fluctuations imprinted upon the matter distribution during the initial expansion began to collapse because of gravity. The properties of these fluctuations depend on the unknown nature of dark matter²⁻⁴, the determination of which is one of the biggest challenges in present-day science⁵⁻⁷. Here we report supercomputer simulations of the concordance cosmological model, which assumes neutralino dark matter (at present the preferred candidate), and find that the first objects to form are numerous Earth-mass dark-matter haloes about as large as the Solar System. They are stable against gravitational disruption, even within the central regions of the Milky Way. We expect over 10^{15} to survive within the Galactic halo, with one passing through the Solar System every few thousand years. The nearest structures should be among the brightest sources of γ -rays (from particle-particle annihilation).

The cosmological parameters of our Universe and initial conditions for structure formation have recently been measured via a combination of observations, including the cosmic microwave background (CMB)⁸, distant supernovae^{9,10} and the large-scale distribution of galaxies¹¹. Cosmologists now face the outstanding problem of understanding the origin of structure in the Universe from its strange mix of particles and vacuum energy^{12,13}.

Most of the mass of the Universe must be made up of a kind of non-baryonic particle¹⁴ that remains undetected in laboratory experiments. The leading candidate for this 'dark matter' is the neutralino, the lightest supersymmetric particle, which is predicted to solve several key problems in the standard model for particle physics⁵. This cold dark matter (CDM) candidate is not completely collisionless. It can collide with baryons, thus revealing its presence in laboratory detectors, although the cross-section for this interaction is extremely small. In a cubic-metre detector containing $\sim 10^{30}$ baryon particles, only a few collisions per day are expected from the $\sim 10^{15}$ dark-matter particles that flow through the experiment as the Earth moves through the Galaxy. The neutralino is its own anti-particle, and can self-annihilate, creating a shower of new particles including γ -rays⁵. The annihilation rate increases as the density squared; the central regions of the Galaxy and its satellites will therefore give the strongest signal¹⁵⁻¹⁸. However, the expected rate is very low—the flux of photons on Earth is the same as we would receive from a single candle placed on Pluto. Numerous experiments using these effects are under way that may detect the neutralino within the next decade⁷. Furthermore, in the next few years the Large Hadron Collider (LHC) at CERN will confirm or

density patch of the Universe that is nested within a hierarchy of larger and lower resolution grids of particles.

The fluctuations are imposed on the particles using accurate calculations of the linear theory power spectrum for a SUSY model with a particle mass $m_{\nu} = 100 \text{ GeV}$. This includes collisional damping, free streaming and the transfer of fluctuations through the matter-radiation era of the Universe²⁻⁴. The resulting power spectrum is close to a power law of $P(k) \propto k^n$ with $n = -3$, with an exponential cut-off at $0.6 \text{ co-moving parsecs}$, which corresponds to a mass scale of $10^{-6} M_{\odot}$, where M_{\odot} is the mass of the Sun. The cut-off scale depends on the neutralino mass and decoupling energy. From accelerator searches we know that $m_{\nu} > 37 \text{ GeV}$ and that the cosmic matter density sets an upper limit at 500 GeV . The damping scale for the allowed neutralino models differ from the model we used by less than a factor of three in mass²⁻⁴ and structure formation is therefore very similar in all SUSY-CDM scenarios. A less popular CDM candidate is the axion, which has a much smaller damping scale of $10^{-13} M_{\odot}$. For comparison we simulated the high-resolution region with an axion CDM fluctuation spectrum on the resolved scales. Both models produce equal halo abundances above $5 \times 10^{-6} M_{\odot}$, but the axion model also forms bound structures down to the smallest resolved scales; see Fig. 3. Here we concentrate on the properties of the first structures to form in the SUSY-CDM model.

We evolve the initial particle distribution using a parallel multi-stepping tree code, starting at a redshift of $z = 350$ when the fluctuations are still linear. The high-resolution region forms the first nonlinear structures at $z = 60$ and the entire region quickly becomes distorted by the complex tidal field from the surrounding overdensities. By a redshift of $z = 26$, the high-resolution region begins to merge into the lower-resolution surroundings and we do not analyse the region further—however, this is sufficiently late that about 5% of the mass in the region has collapsed into bound dense structures (haloes); see Fig. 1.

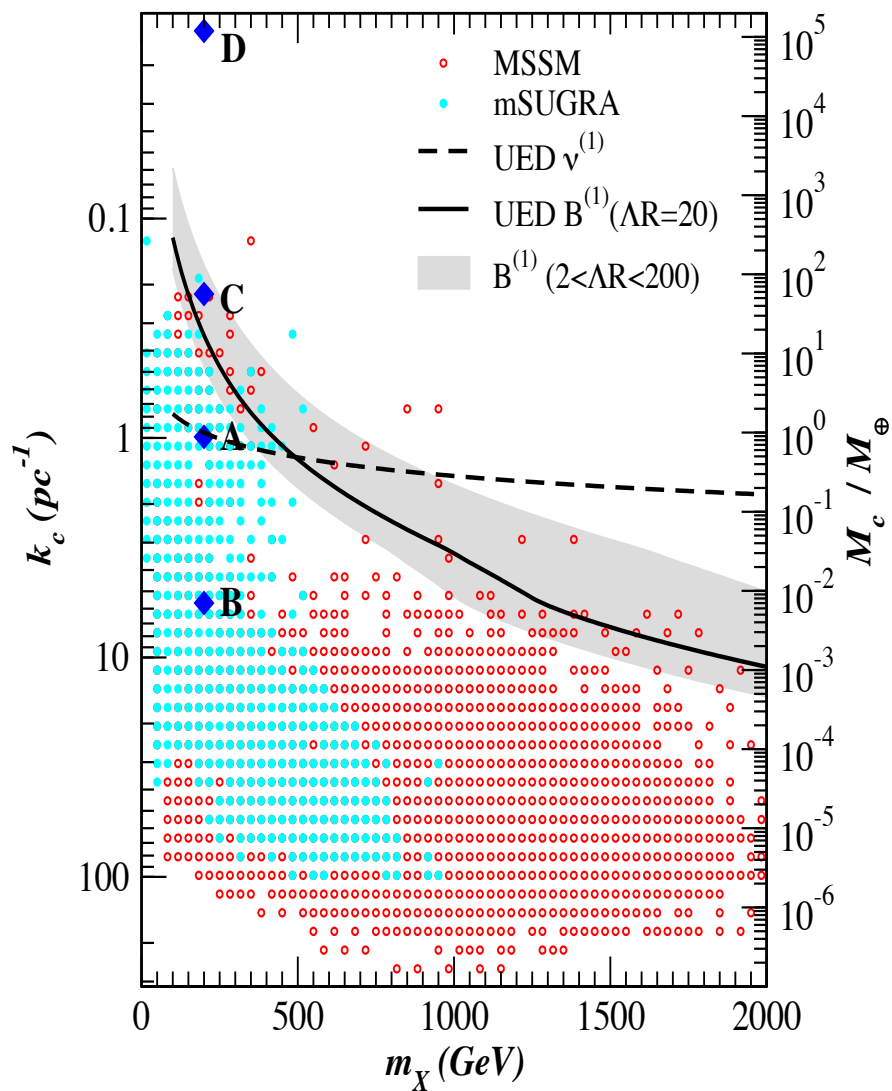
The first dark-matter haloes to collapse and virialize are smooth triaxial objects of mass $10^{-6} M_{\odot}$ and half-mass radii of 10^{-2} pc . Figure 2 shows the density profiles of three representative haloes at $z = 26$ that are well fitted by single power-law density profiles $\rho(r) \propto r^{-\gamma}$ with slopes γ in the range from 1.5 to 2, similar to galactic haloes shortly after their formation²⁰. We note that the densities at the virial radius are about an order of magnitude higher than the density at $0.01 r_{\text{virial}}$ in a galactic halo today, which makes the survival of many of these haloes as galactic substructure possible. The central resolved densities reach 10^9 times the mean background density at 1% of their virial radii. Unlike galactic and cluster-mass CDM haloes, they do not contain substructure because no smaller-mass haloes have collapsed in the hierarchy.

Figure 3 shows the mass function of haloes. We use a 'friends of friends' algorithm with a linking length set to identify the dense central regions of collapsed haloes, then for each halo centre we recursively search for the radius r_{200} that is at an overdensity of 200 times the cosmic mean density. The resulting halo mass function is steep: $\text{dn}(M)/\text{d log } M \propto M^{-1}$. For comparison we plot an extrapolation of the halo mass function found on much larger scales $> 10^7 M_{\odot}$ (ref. 21), which fits surprisingly well up to the cut-off scale of $10^{-6} M_{\odot}$, below which we find no more structures.

At these epochs the baryons are kept sufficiently warm by the CMB that they are unable to cool and form visible objects such as stars or planets within such tiny systems¹³. The dark haloes may be

Profumo et al (2006)

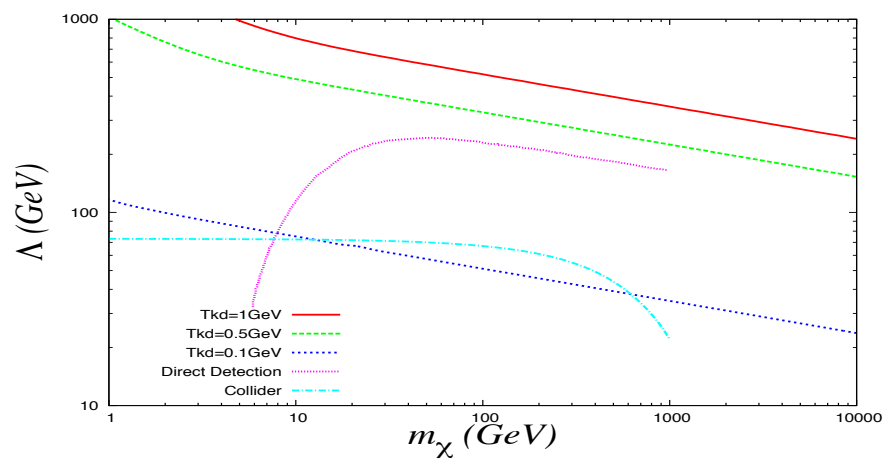
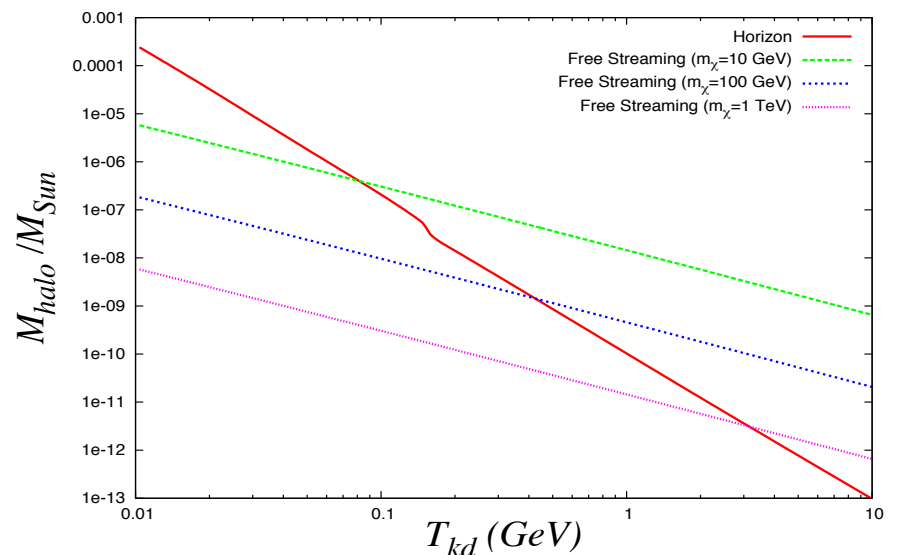
$$M_{halo} : 10^{-6} M_{sun} \sim 100 M_{sun}$$



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P. Gondolo, J. Hisano, KK (2012)

$$\text{Maximum: } M_{halo} \sim 10^{-6} M_{sun}$$



(a) Scalar effective operator

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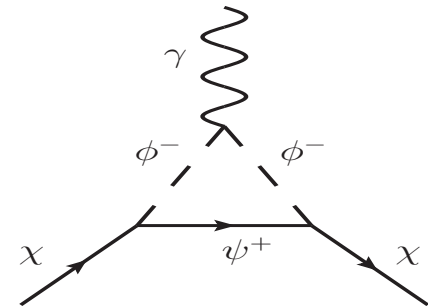
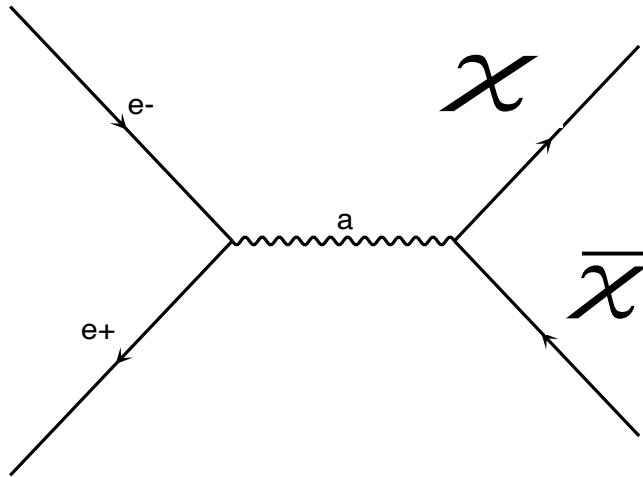
Dipole DM

Pospelov et al (2000), Sigurson et al(2004), Barger et al (2012), Heo and Kim (2012),Graham (2012) Nobile et al (2013),..

- DM with a dipole moment:

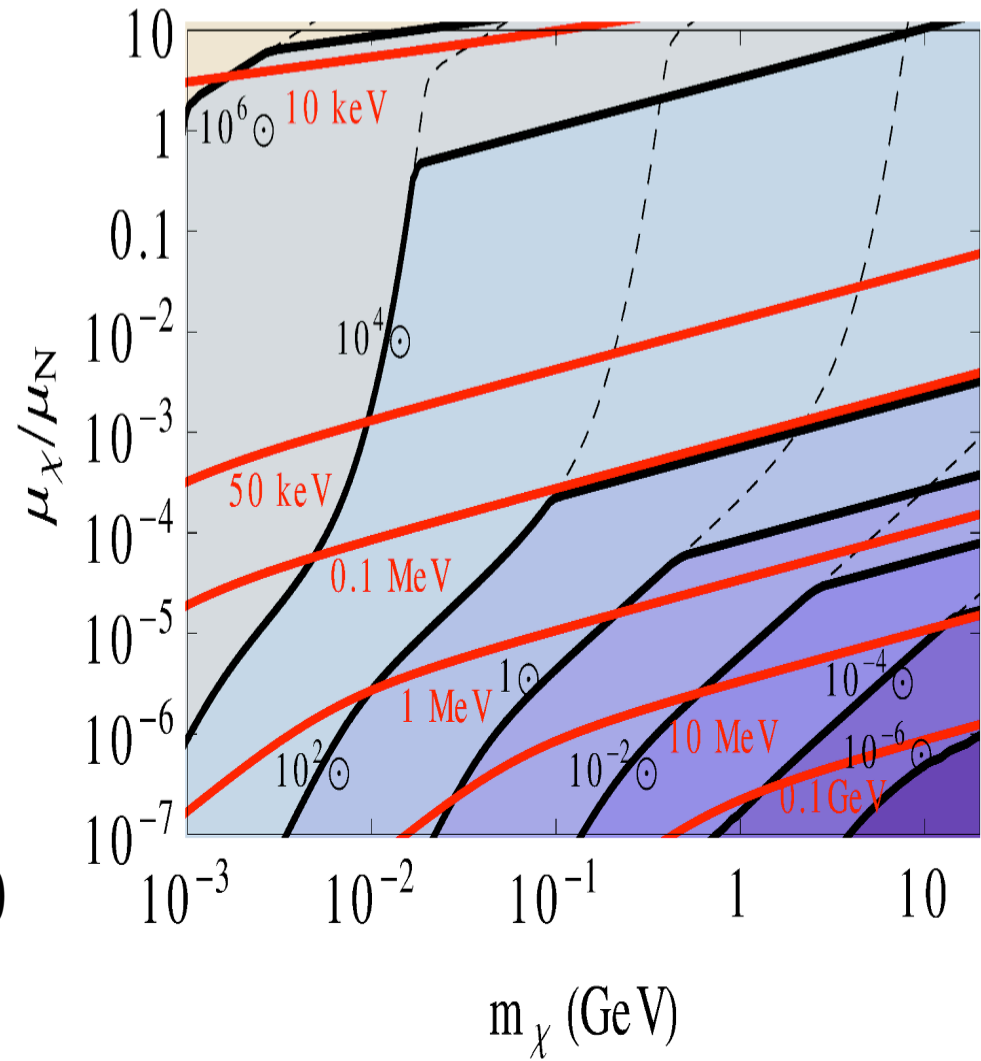
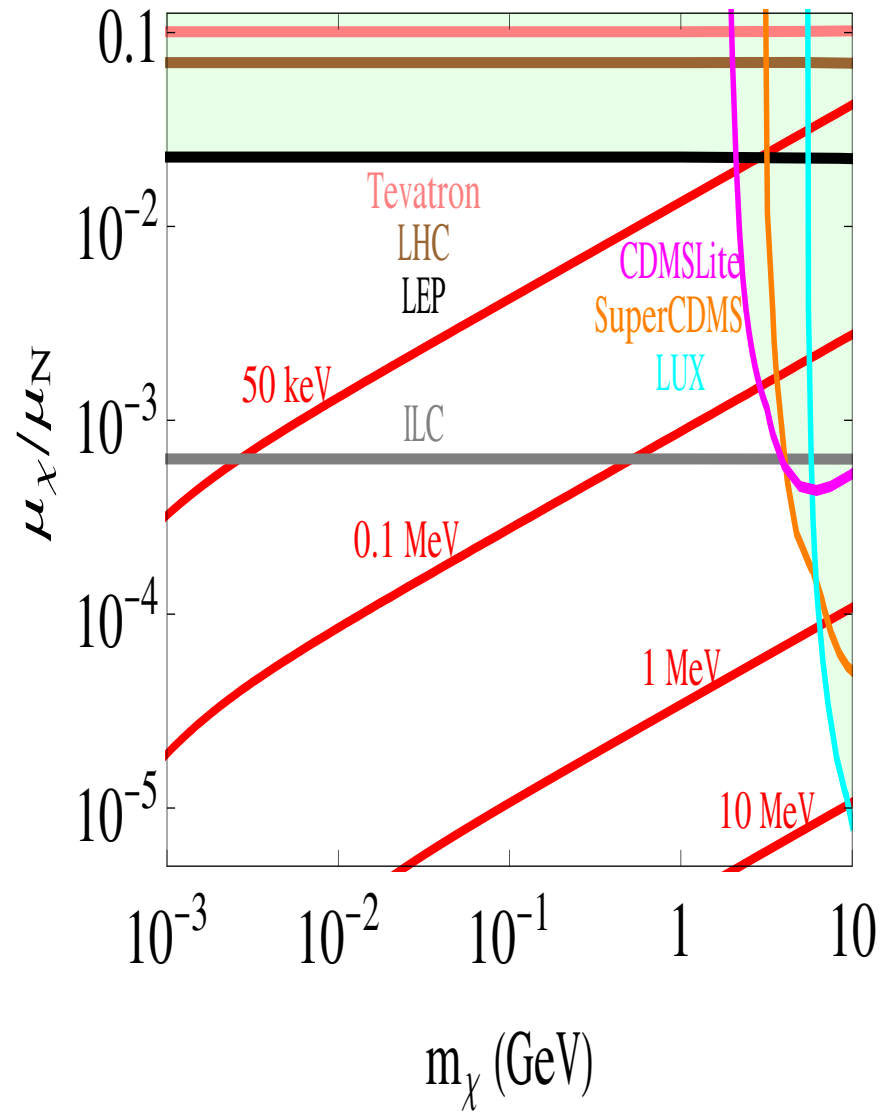
The lowest dimensional coupling between DM fermions and the SM gauge bosons

$$L_{MDM} = -\frac{i}{2} \mu \bar{\chi} \sigma^{\mu\nu} \chi F_{\mu\nu} \quad \mu \equiv \frac{1}{\Lambda}$$



$$\mu \sim \frac{eg^2}{M}$$

P. Gondolo and KK(2016)



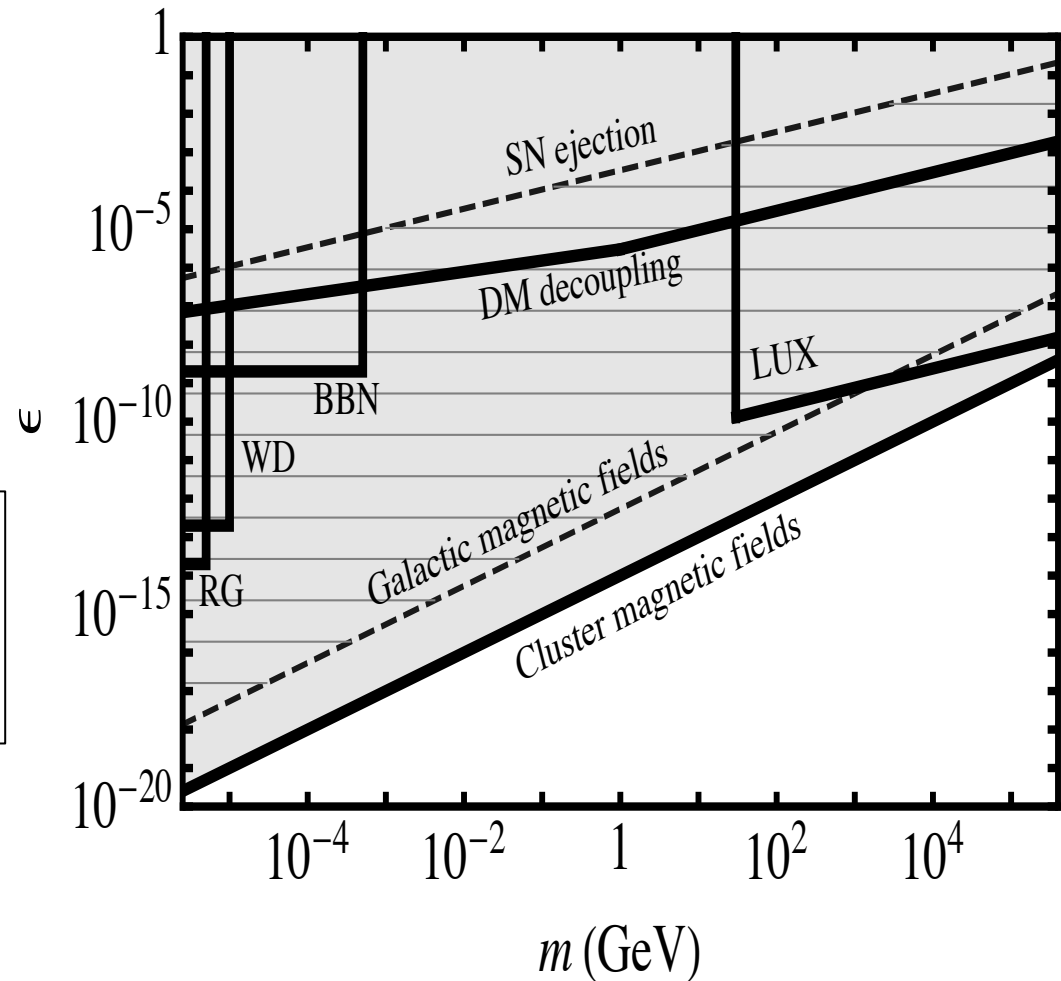
Millicharged DM: DM charge ϵe

Davidson et al (2000), Dubovsky et al (2004), Chuzhoy et al (2008), McDermott et al (2011), Izaguirre et al (2015), ...

(KK, Sekiguchi & Tashiro (2016))

" The SU(2) x U(1) unification theory
is not particularly beautiful. ...
The problem is the U(1) charge..."
- Howard Georgi

" One would be surprised if nature had
made no use of it (magnetic monopole)"
- Paul Dirac



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Summary: Be open-minded. Multiple DM probes can be complementary

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