

# A new constraint on millicharged dark matter from galaxy clusters

Toyokazu Sekiguchi (IBS/CTPU)



Based on arXiv: 1603.1959 in collaboration with  
Kenji Kadota (IBS/CTPU) & Hiroyuki Tashiro (Nagoya)



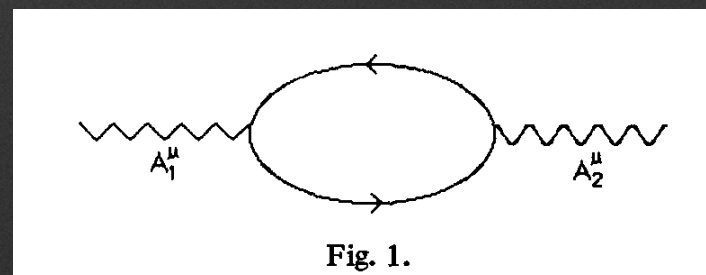
# Millicharge?

## Fractional EM charge

- no evidence of charge quantization of  $U(1)_{\text{EM}}$ 
  - GUT/magnetic monopole is yet to be probed
  - Arbitrarily small fractional charge is possible
- kinetic mixing of multiple  $U(1)$  Holdom (1986)

$$\mathcal{L} \supset \epsilon_{ij} F_i^{\mu\nu} F_{j\mu\nu} \quad (i \neq j)$$

- Allowed from gauge invariance
- Kinetic mixing generally arises from RG





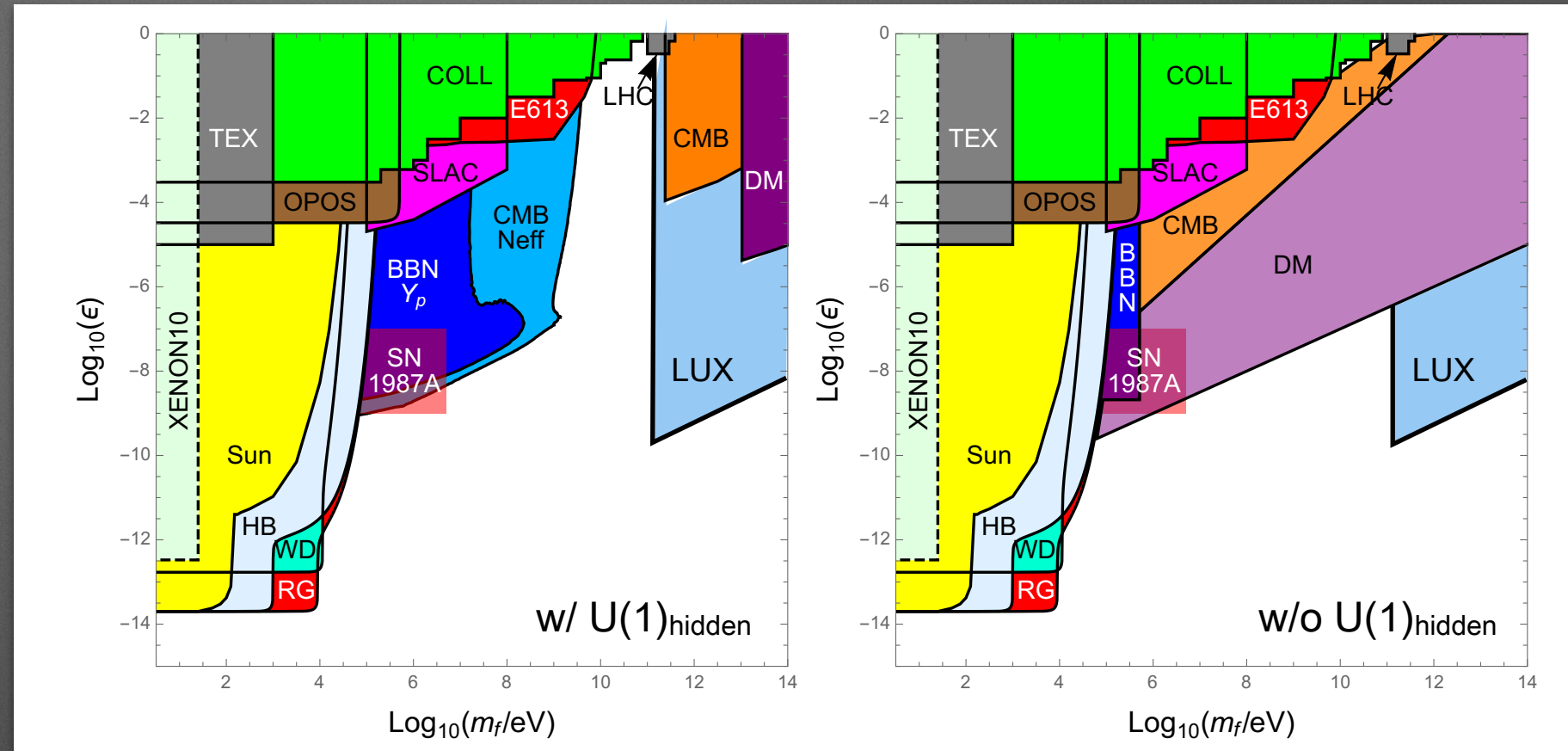
# Millicharged dark matter?

## Dark matter may not be completely dark

- can have a fractional EM charge  $\epsilon = \frac{q}{e} \ll 1$
- subject to various constraints:
  - collider
  - astrophysics (cooling of stars, SNe)
  - cosmology ( $\Omega_{\text{DM}}$ , CMB, BBN, ...)
  - direct DM detection



# Summary of previous constraints



Vinyoles & Vogel (2015)



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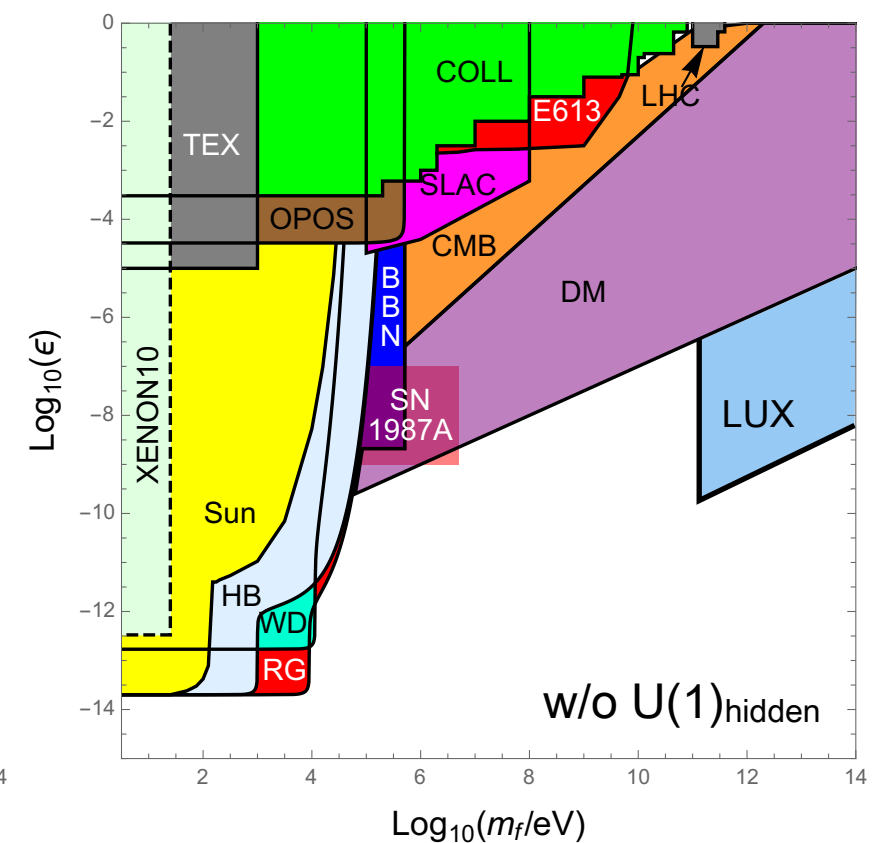
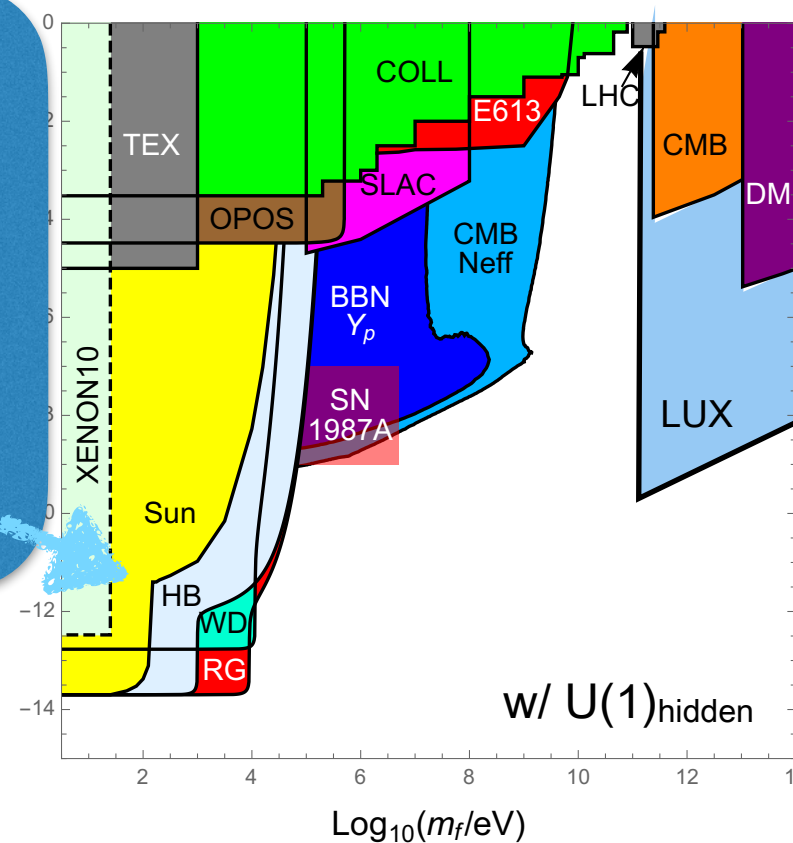
## Astrophysical constraints

Modified stellar evolution with MDM emission  $\gamma^* \rightarrow \chi\bar{\chi}$

Effective only if plasmon mass  $> 2m_{\text{MDM}}$

$$\omega_p^2 = \frac{4\pi\alpha n_e}{m_e},$$

~ 300eV for the Sun;  
10keV for red-giants



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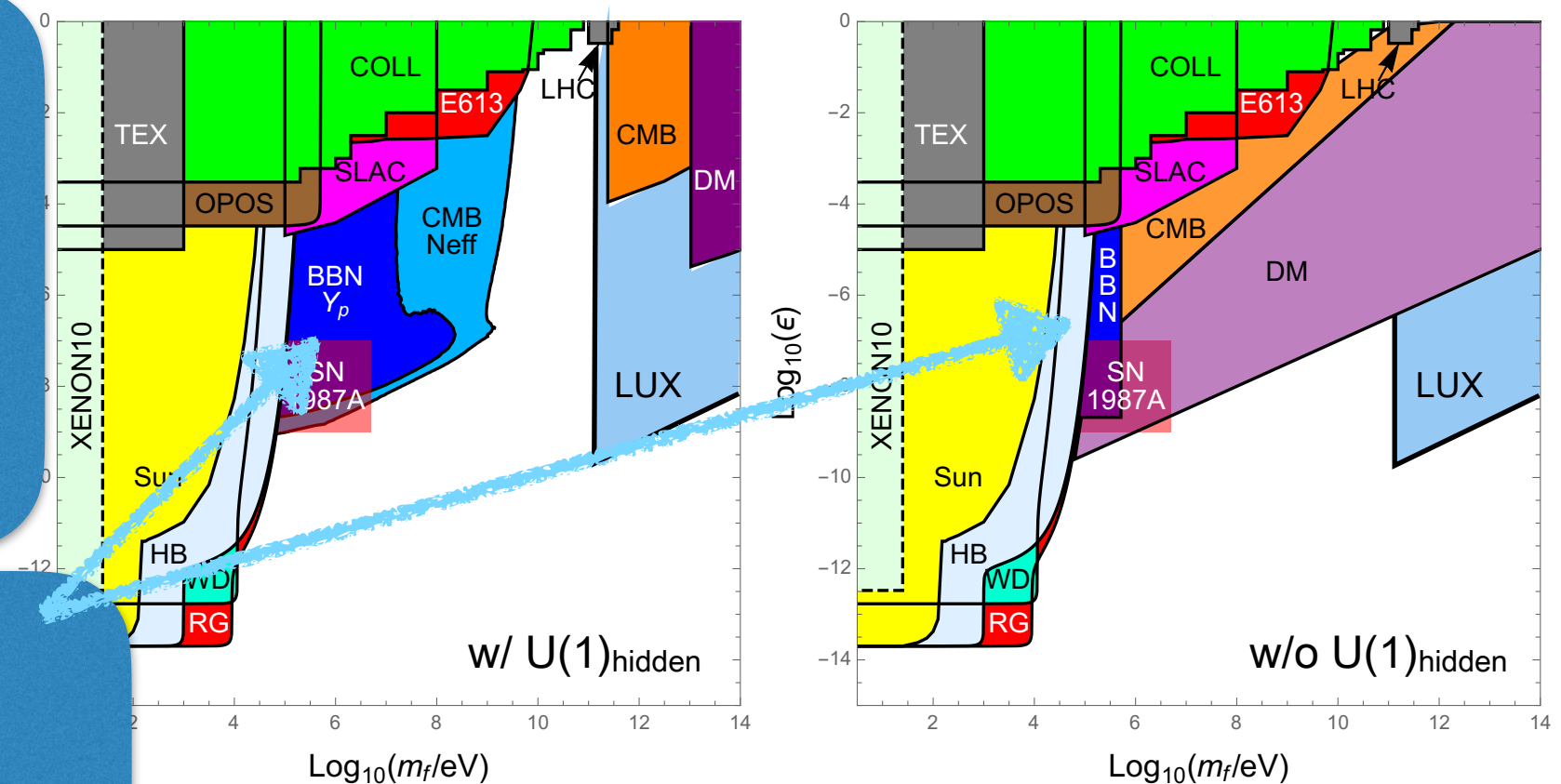
## BBN

For  $m_{\text{DM}} \leq m_e$ ,  $e^+e^-$  annihilate into MDM, while photon is less heated up.

✓ higher  $N_{\text{eff}}$  ←  $U(1)'$  can contribute

✓ higher  $n_b/n_\gamma$  at BBN

→ Earlier neutron freeze-out increases  $Y_p$



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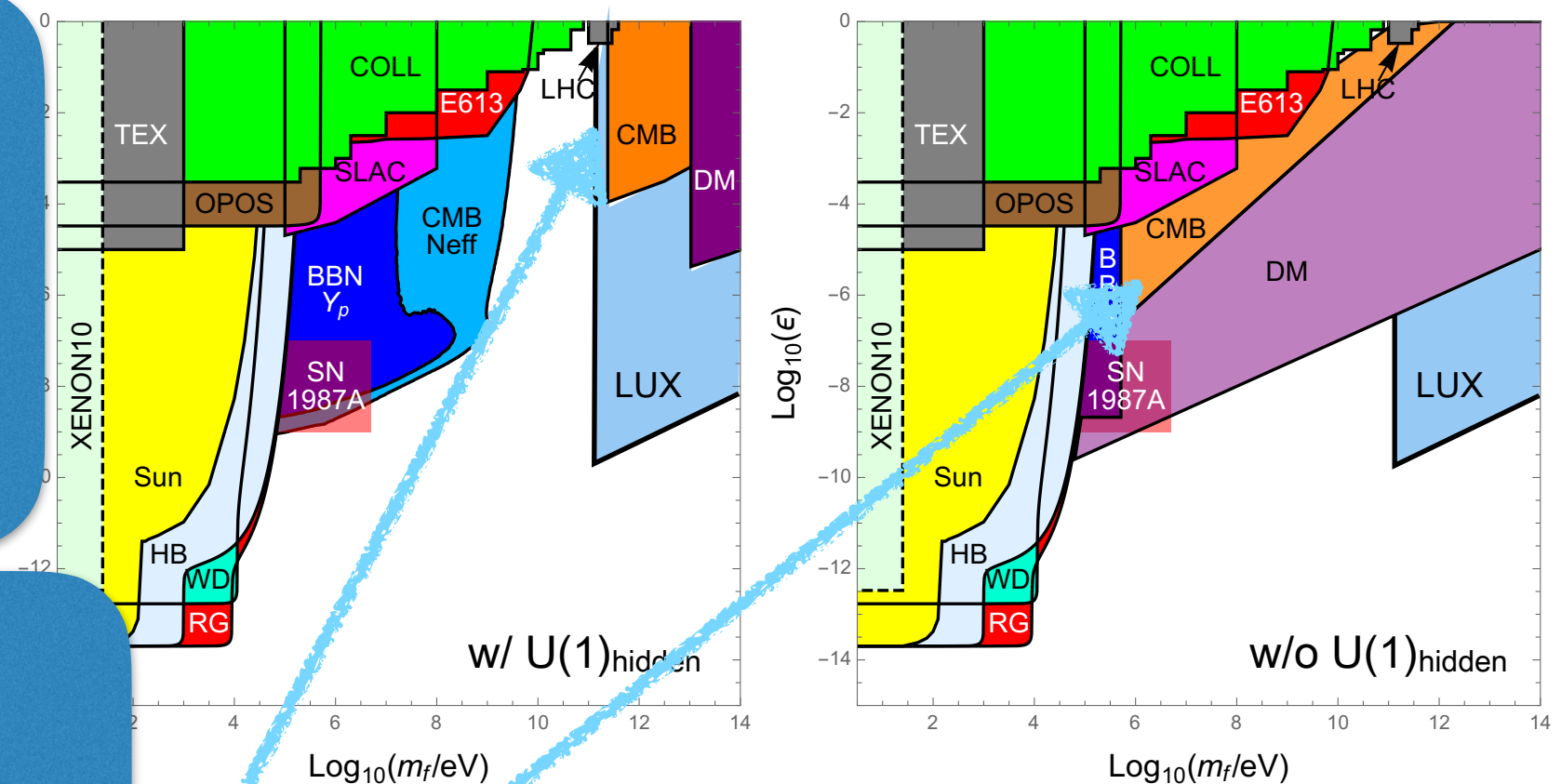
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## CMB

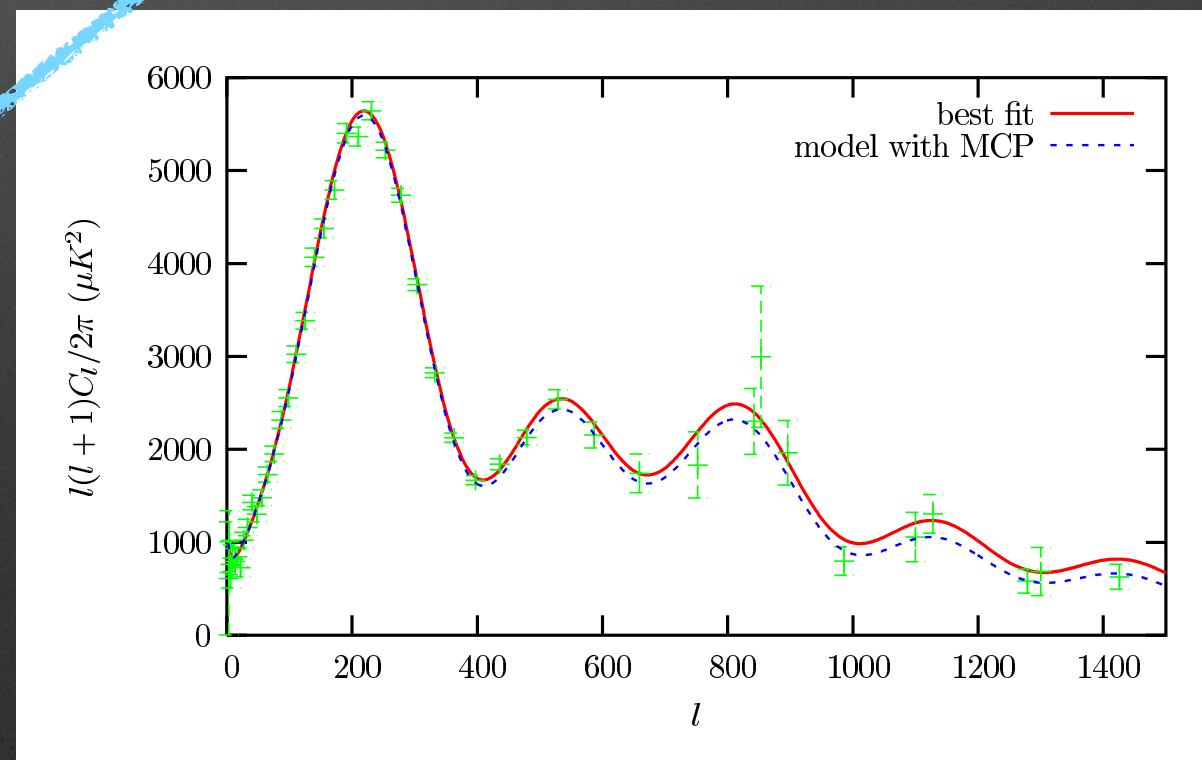
MDM can kinetically couple to  $e^-$  via Coulomb scattering

➔ Acoustic oscillation is modified  
 (or enhanced diffusion damping  
 fixed  $\Omega_b + \Omega_{\text{mdm}}$ )

MDM should decouple before recombination



Vinyoles & Vogel (2015)



Dubovskya, Gorbunova & Rubtsov (2003)



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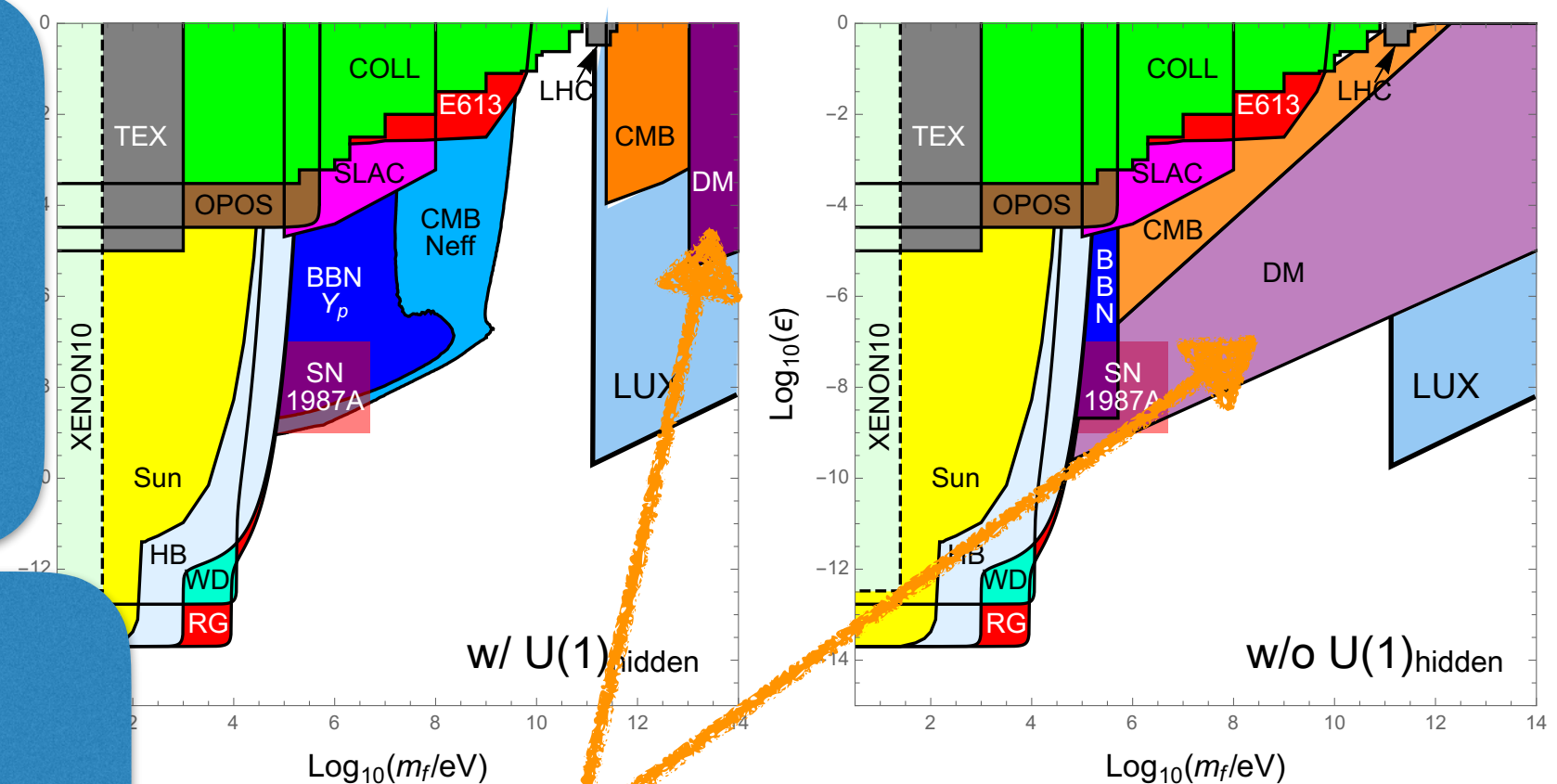
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## Thermal relic abundance

main process:  $\chi\bar{\chi} \leftrightarrow f\bar{f}$

- w/o  $U(1)'$ : overclose when thermalized
- w/  $U(1)'$ : MDM annihilates into  $U(1)'$



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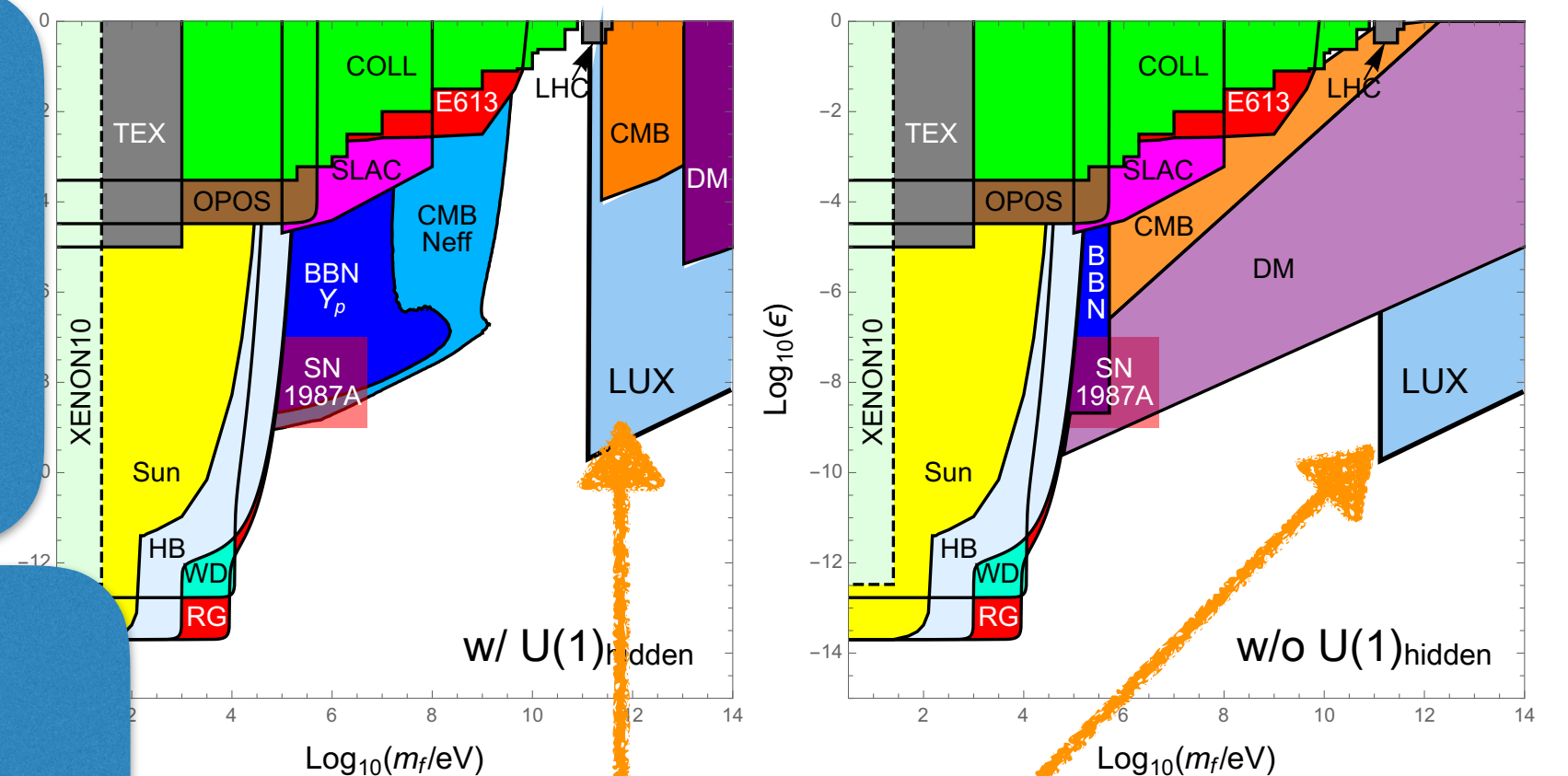
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## Direct detection

cross section wrt recoil energy

$$\frac{d\sigma_T}{dE_R}(v, q^2) = 8\pi m_T \frac{\alpha^2 \epsilon^2}{v^2 q^4} Z_T^2 F_T^2(q^2)$$

➔ Equivalent to  $F_T$  with  $1/q^4$  in short-range interaction

spin-independent ➔ best constraint from LUX



# Circumventing direct detection

Chuzhoy & Kolb (2009)

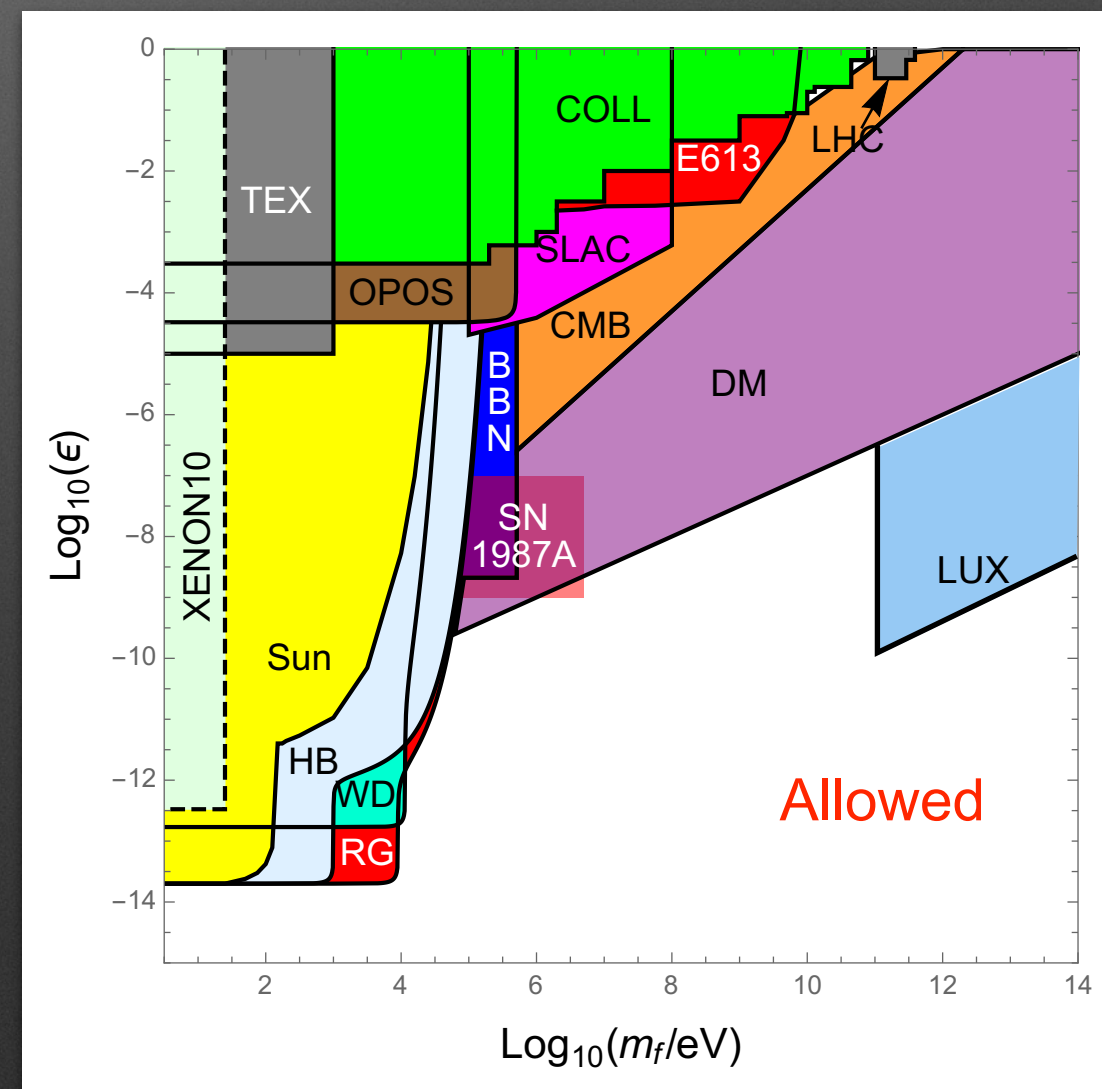
## Charged DM may be absent in Milky Way

- MDM is accelerated by past supernova explosions (Fermi acceleration). MDM cannot lose energy efficiently and be expelled from Milky Way.

$$\tau_{\text{rel},p} \approx 300 \text{ years} \left( \frac{e}{q_X} \right)^2 \left( \frac{m_X}{m_p} \right) \left( \frac{v_X}{100 \text{ km s}^{-1}} \right)^3 \times \left( \frac{n_p}{10^{-2} \text{ cm}^{-3}} \right)^{-1},$$

- DM from Milky Way halo cannot reach galaxy due to Galactic magnetic fields mostly parallel to Galactic plane (thickness~100pc).

$$R_g = 10^{-9} \text{ pc} \left( \frac{m_X}{m_p} \right) \left( \frac{e}{q_X} \right) \left( \frac{v_X}{300 \text{ km s}^{-1}} \right) \left( \frac{B}{1 \mu\text{G}} \right)^{-1}$$





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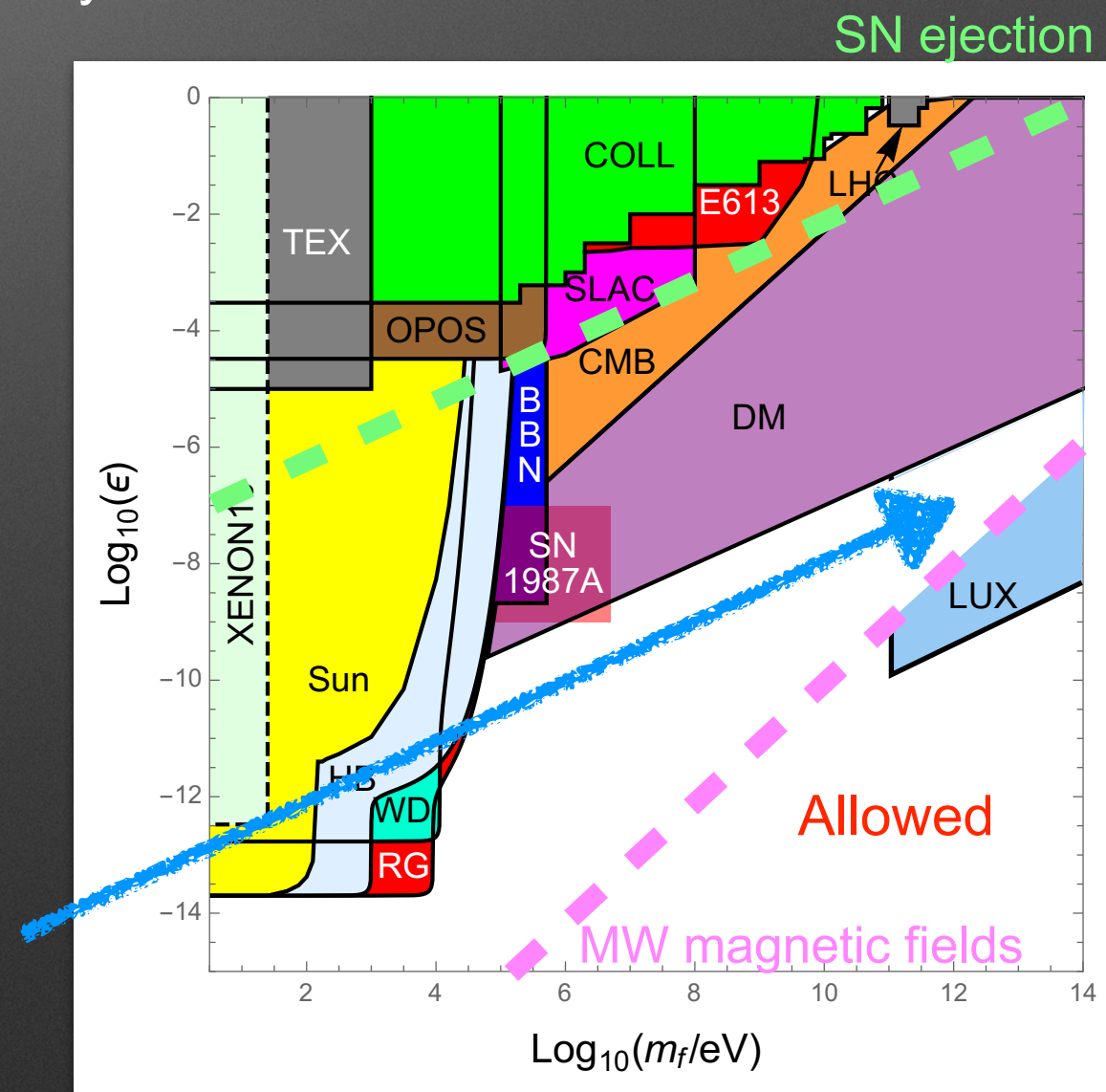
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These arguments open up a window of MDM.

$$10^{-11} \frac{m_{\text{DM}}}{\text{GeV}} \lesssim \epsilon \lesssim 3 \times 10^{-3} \left( \frac{m_{\text{DM}}}{\text{GeV}} \right)^{1/2}$$

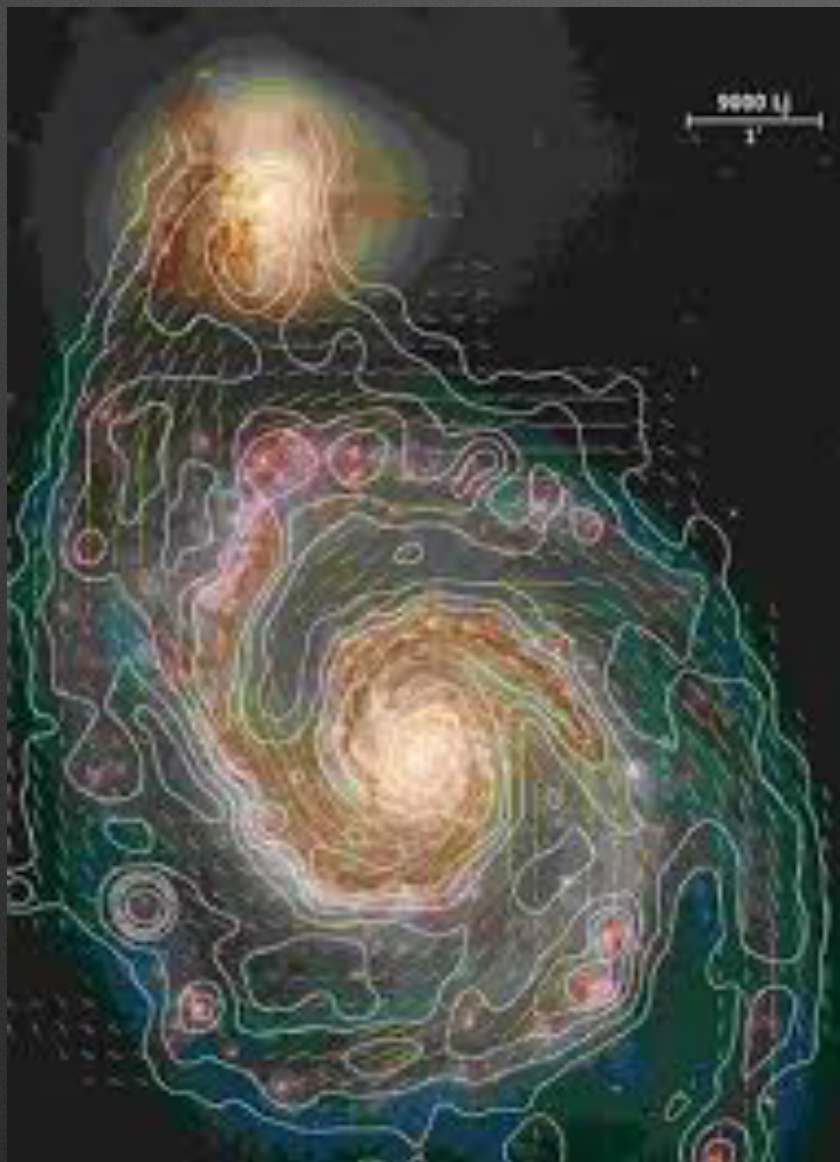




# Galaxy to galaxy clusters?

K. Kadota, TS & H. Tashiro (2016)

If motion of MDM is modified at galaxy scales, what will happen at larger scales like galaxy clusters?

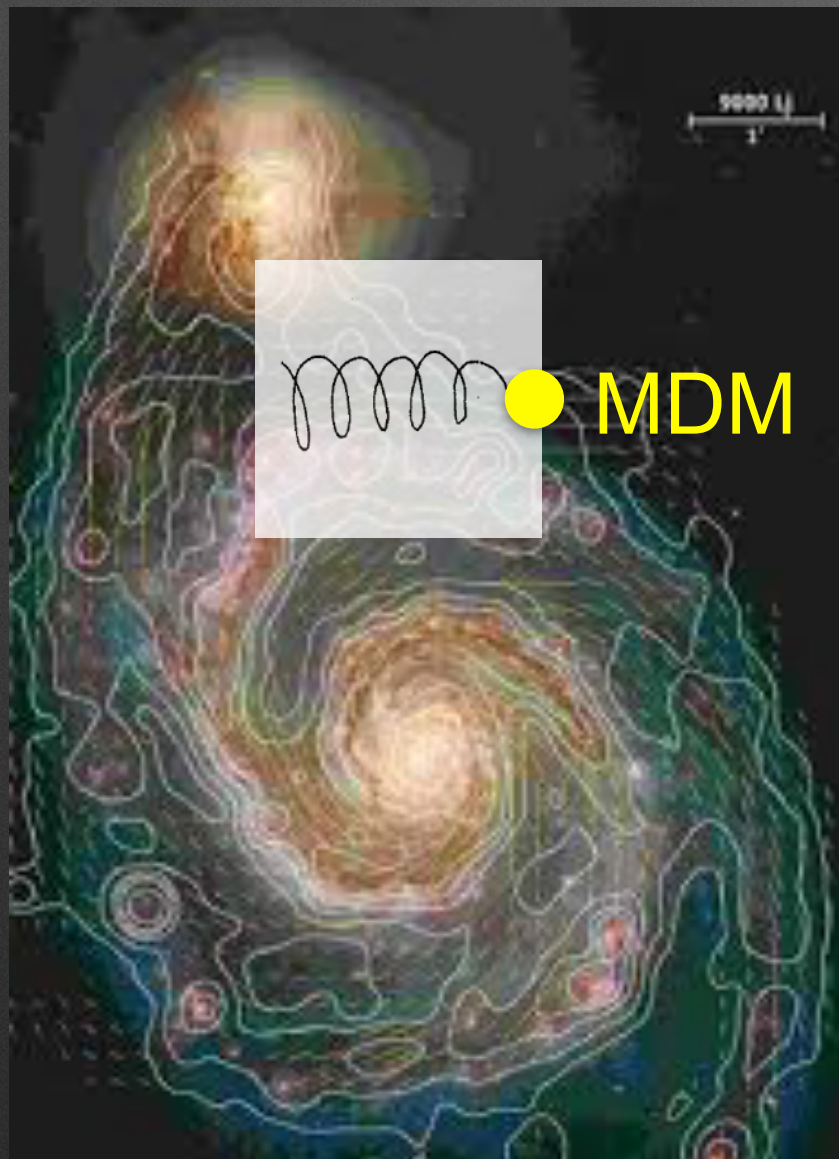




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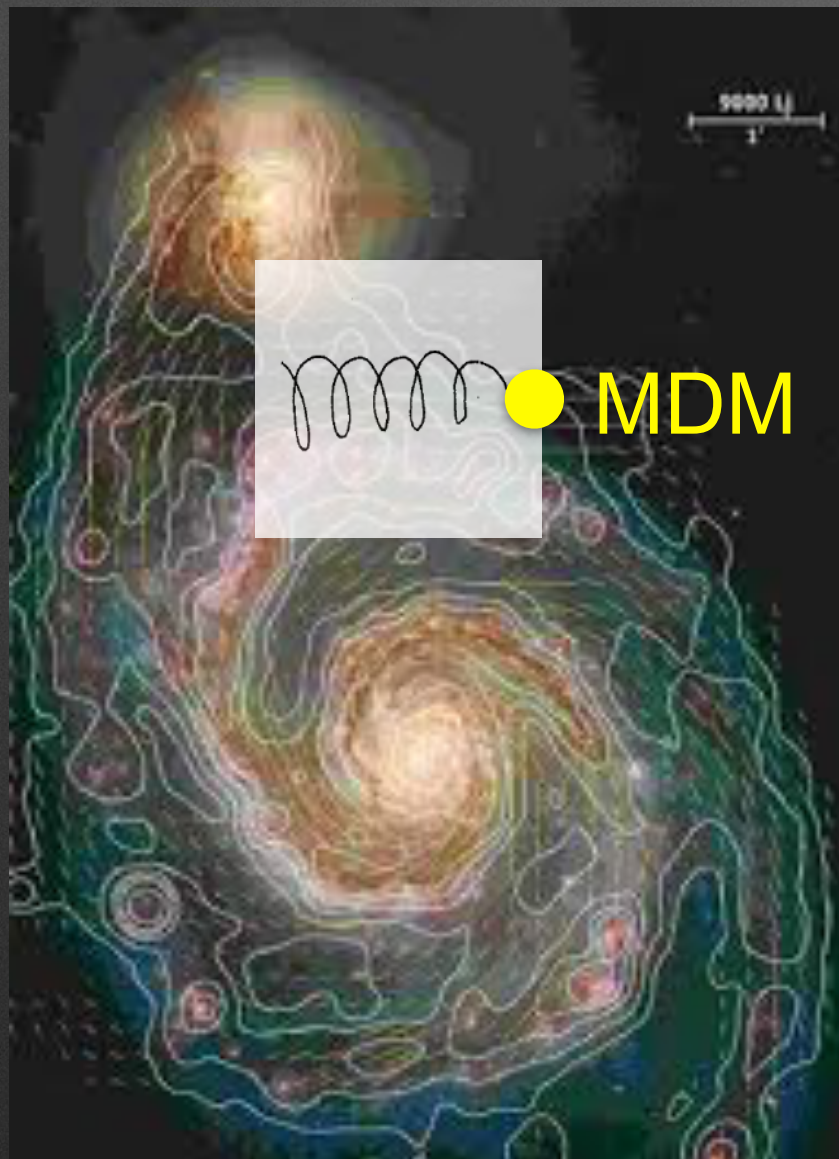




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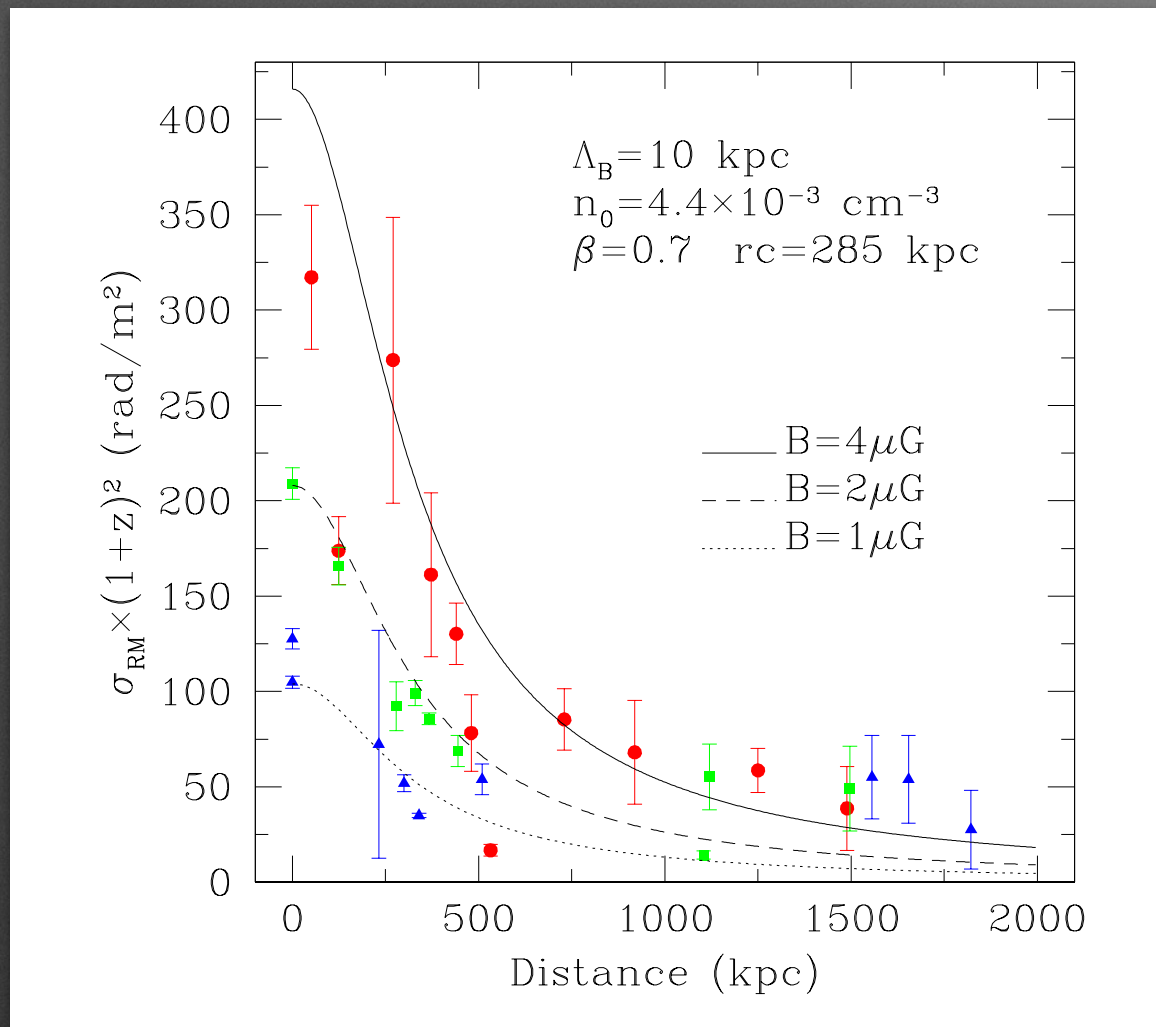
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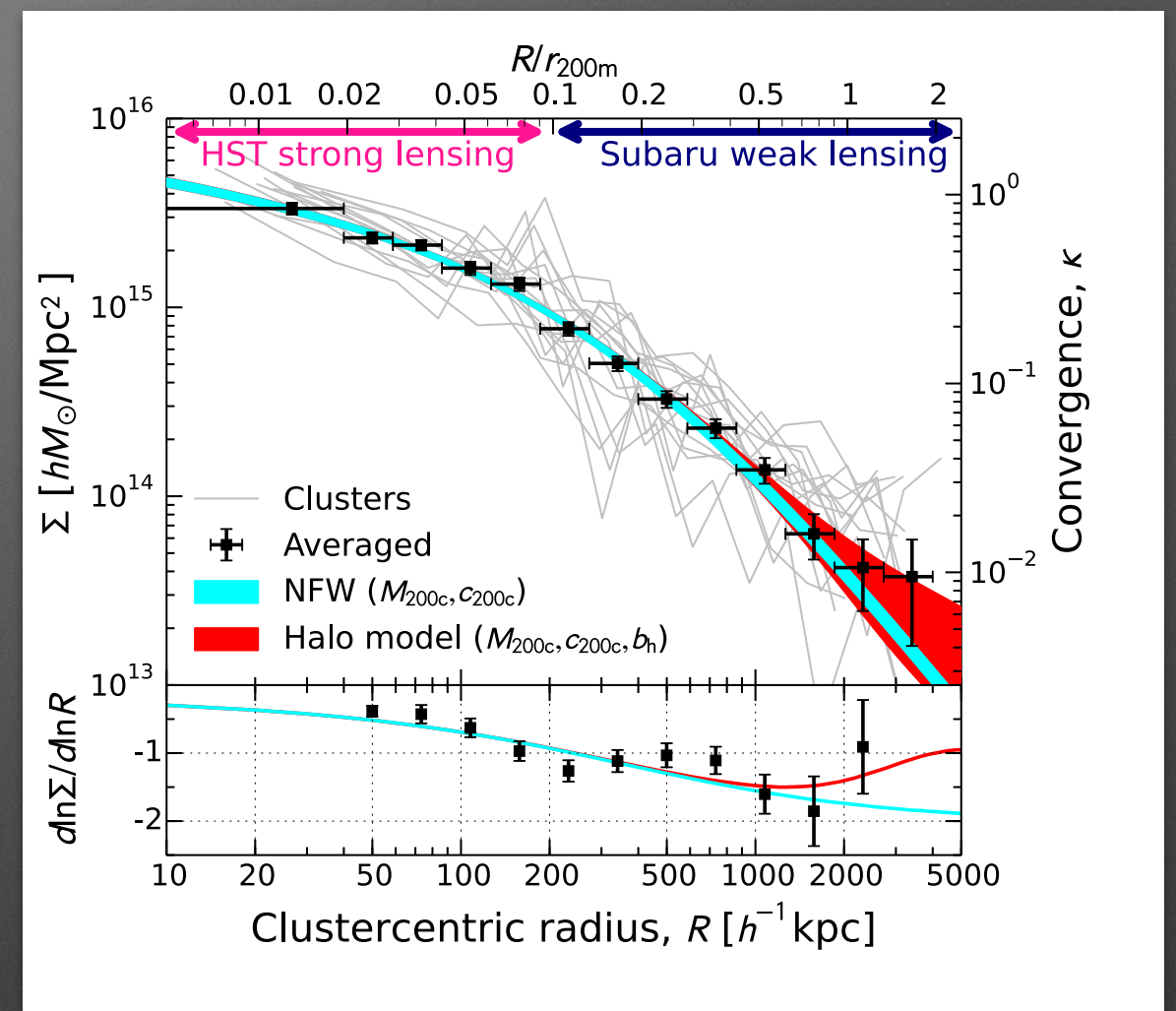


# Two facts about galaxy clusters



Govoni+ (2010)

- ✓ Magnetic fields exist also in galaxy clusters
- $B = \text{a few } \mu\text{G}$  (Faraday rotation measure)



Umetsu+ (2015)

- ✓ Observed density distribution is consistent with CDM predictions
- steep profile Navarro Frenk White (1996)



# A constraint from galaxy clusters

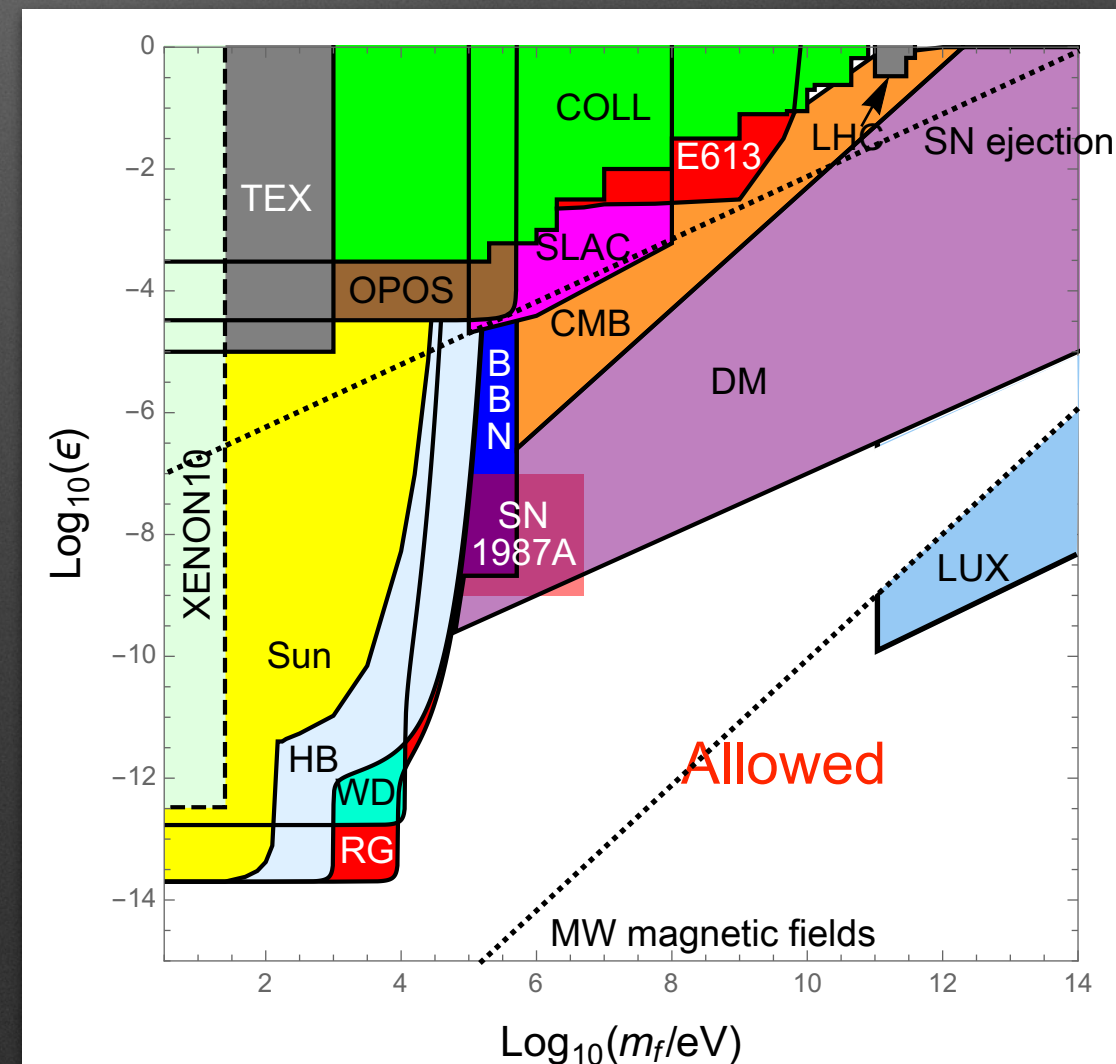
## Lorentz force should be subdominant

- Otherwise DM distribution in clusters should differ from CDM predictions.

$$\rightarrow qBv \lesssim \frac{GM_{\text{halo}}m_{\text{DM}}}{R_{\text{halo}}}$$

- For typical galaxy clusters:

$$\left. \begin{array}{l} R_{\text{halo}} \simeq 1\text{Mpc} \\ M_{\text{halo}} \simeq 10^{14}M_{\odot} \\ B \simeq 1\mu\text{G} \end{array} \right\} \rightarrow v \simeq 10^4\text{km/sec}$$





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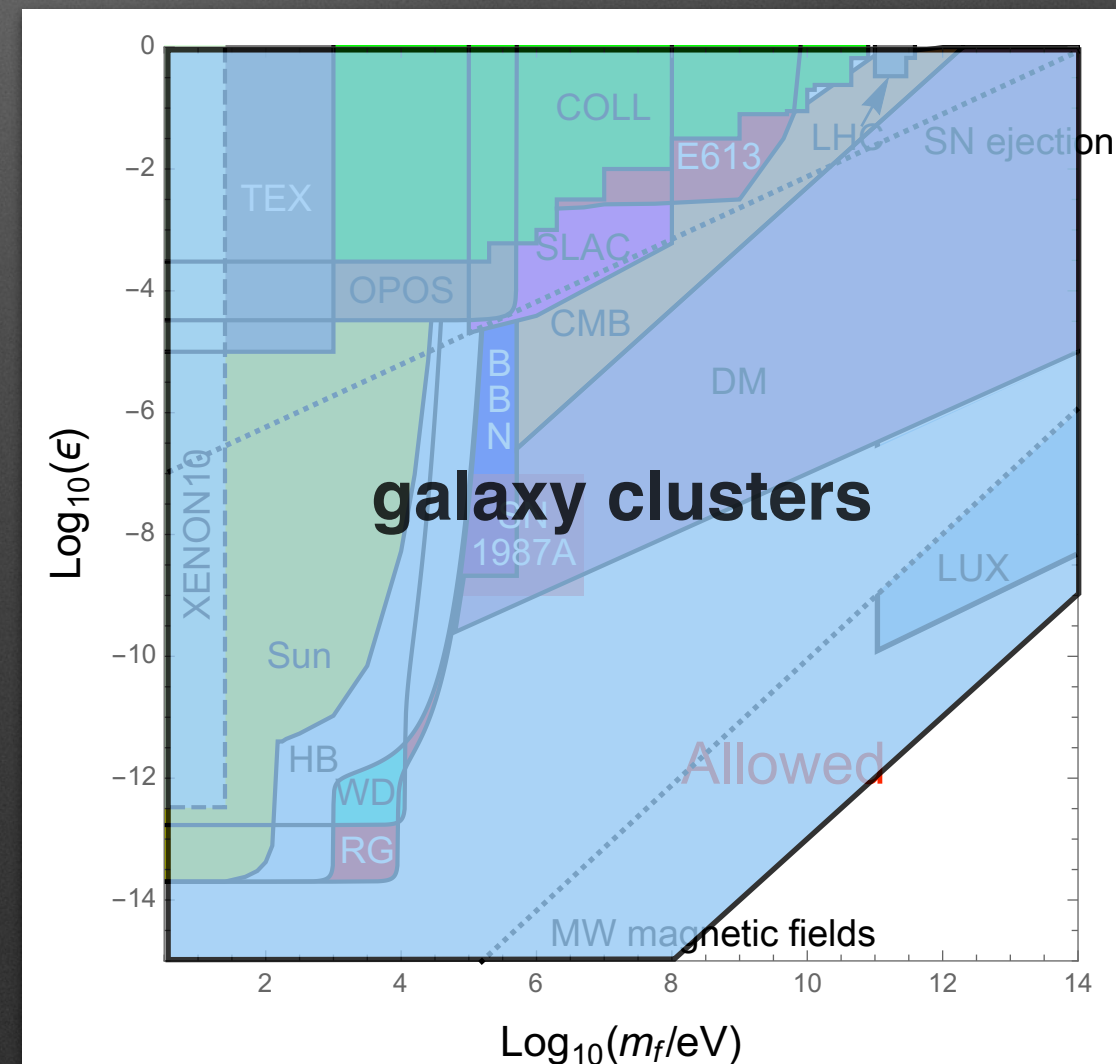
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$$\epsilon \lesssim 10^{-14} \frac{m_{\text{DM}}}{\text{GeV}}$$

- Tighter than any of previous constraints **as long as DM is 100% MDM**
- Independent of existence of  $U(1)_{\text{hidden}}$  and DM asymmetry





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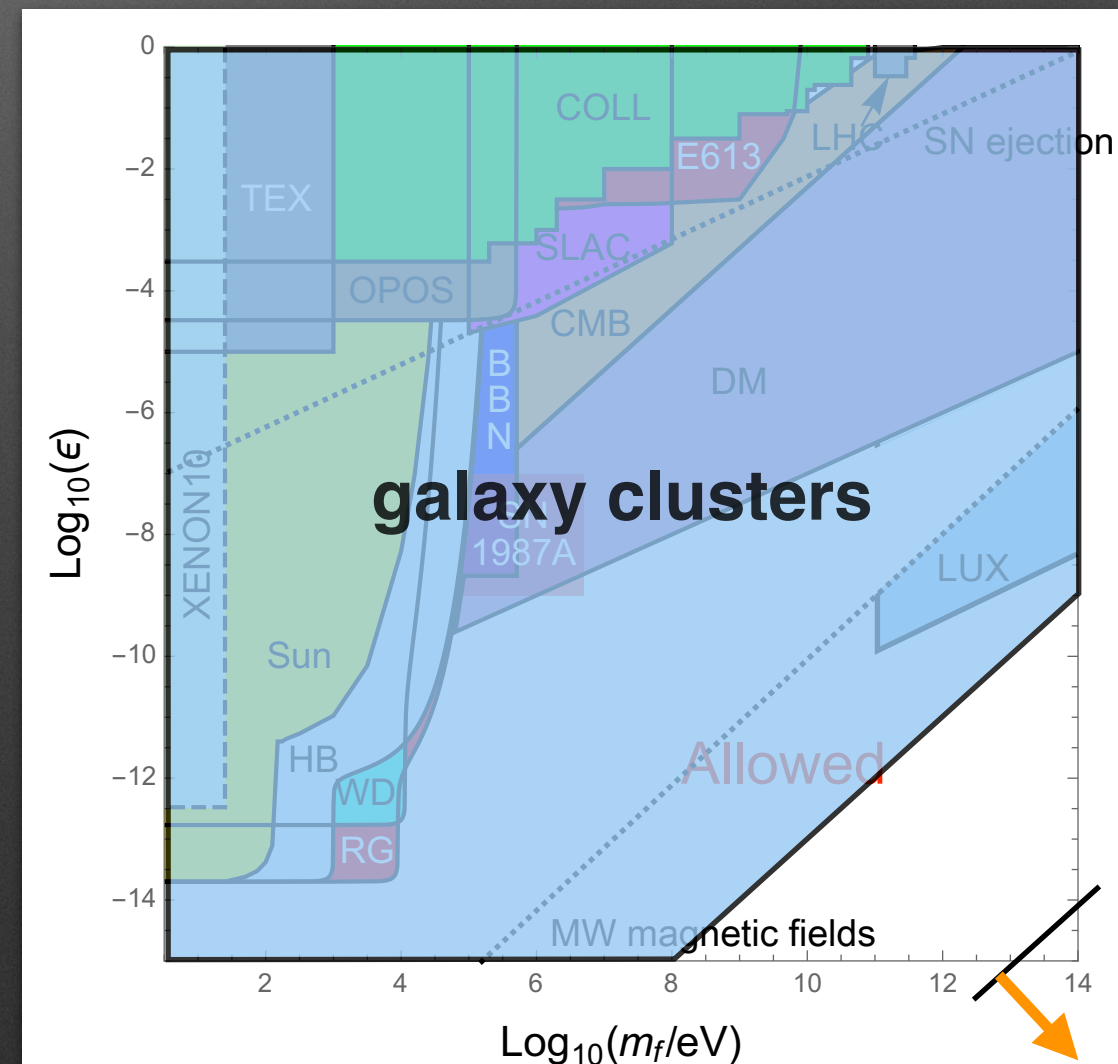
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EM weaker than gravity



# Back-reaction?

## Impact of MDM on dynamics of magnetic fields

- Momentum transfer equation (assuming local homogeneity)

$$m_x \frac{\partial}{\partial t} (n_x \vec{u}_x) = q_x e n_x \left[ \vec{E} + \frac{1}{c} \vec{u}_x \times B \right] + n_x \sum_y \mu_{xy} \gamma_{xy} (\vec{u}_x - \vec{u}_y)$$

- Generalized Ohm's law

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- By integrated this into Maxwell eqs., evolution eq. of magnetic fields is obtained



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(collision-less at leading order in  $\epsilon$ )

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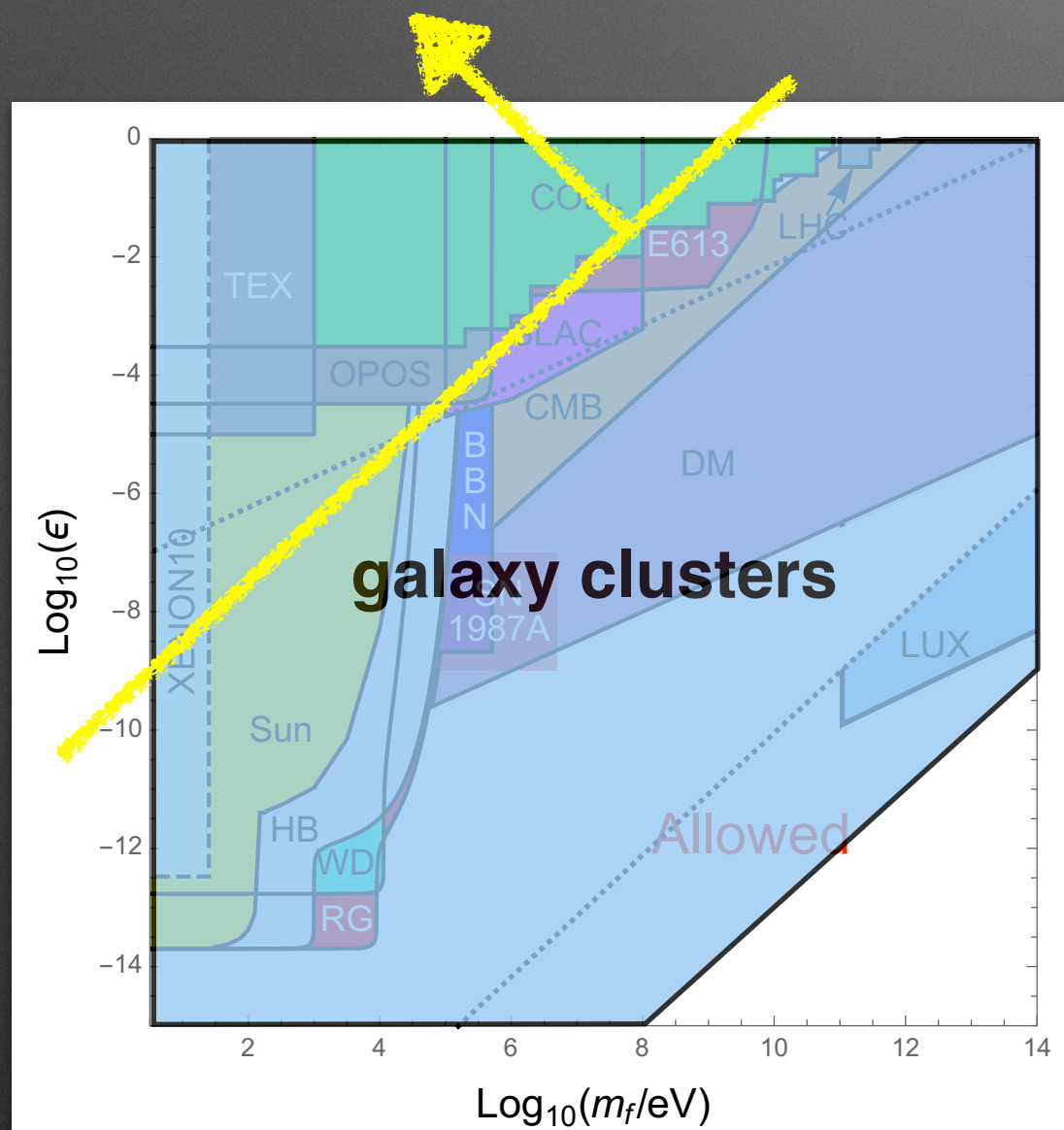
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- MDM contribution is subdominant for  $\epsilon/m_{\text{DM}} [\text{GeV}] < 1$ .
- Magnetic fields are frozen into baryonic gas.



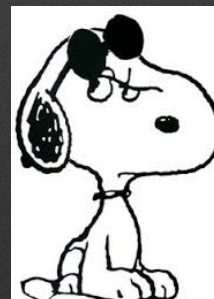
# Back-reaction?

Back-reaction needs to be taken into account



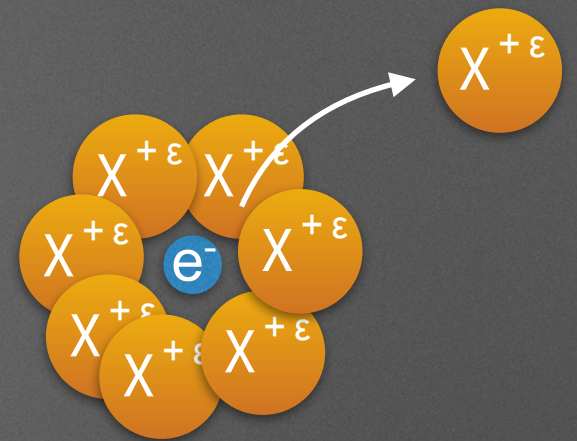
- Excluded by other constraints.
- It's unlikely that observed density profile can be realized in such a strongly coupled regime.

Probably back-reaction does not spoil our constraint.





# Neutralization?



If DM is neutralized in clusters, our constraints is inapplicable

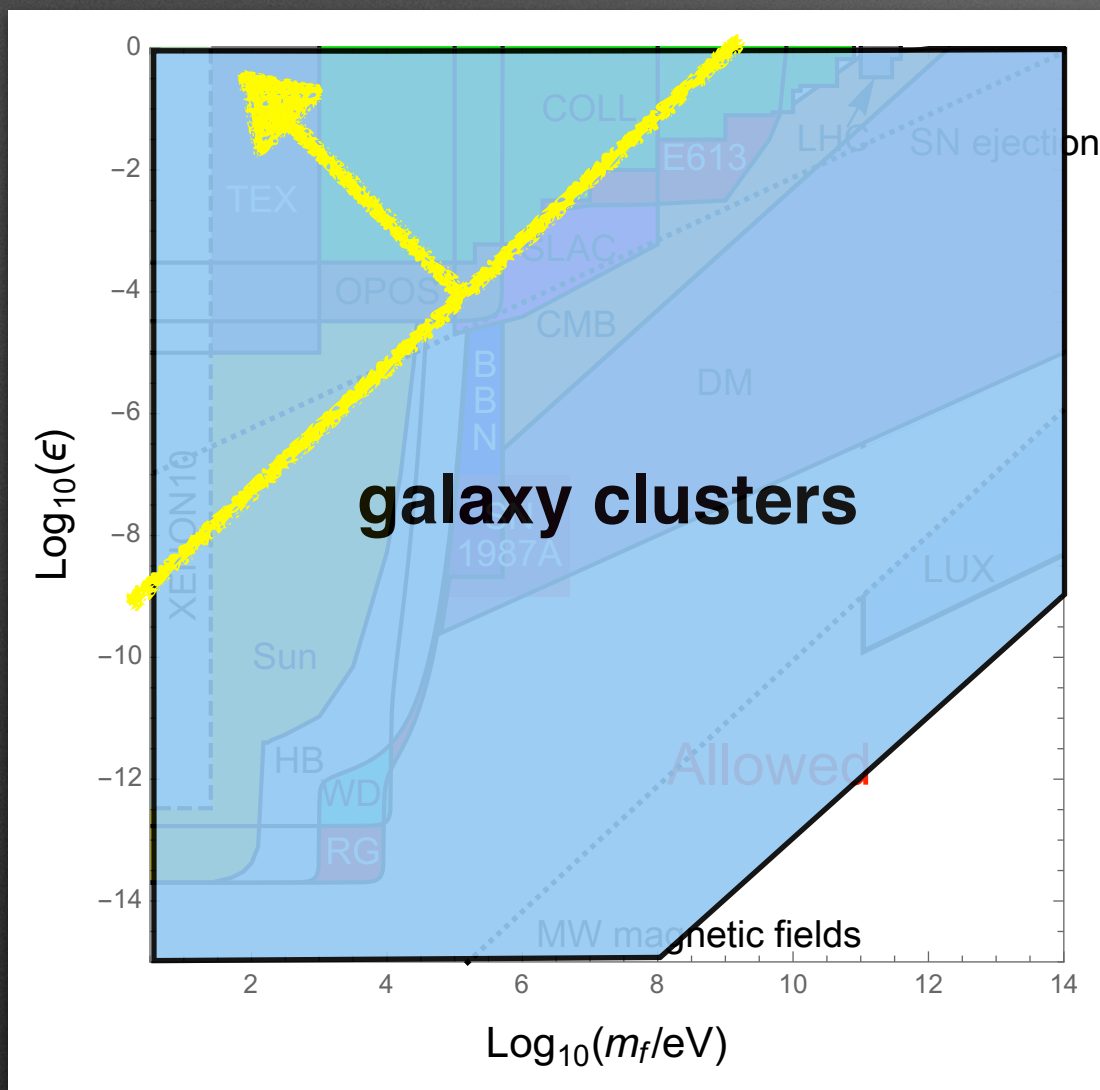
- Ionization energy: independent of DM asymmetry

$$E_{\text{ion}} \sim O(10) \epsilon^4 (m/\text{GeV}) \text{ keV}$$

- **Symmetric DM:** DM (charge  $\epsilon$ ) recombines with anti-DM ( $-\epsilon$ )
- **Asymmetric DM:**  $O(1/\epsilon)$  DMs recombine with  $e^-/p^+$

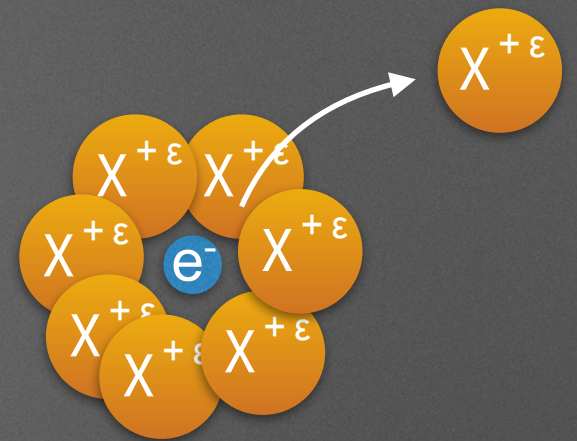
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backreaction





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backreaction

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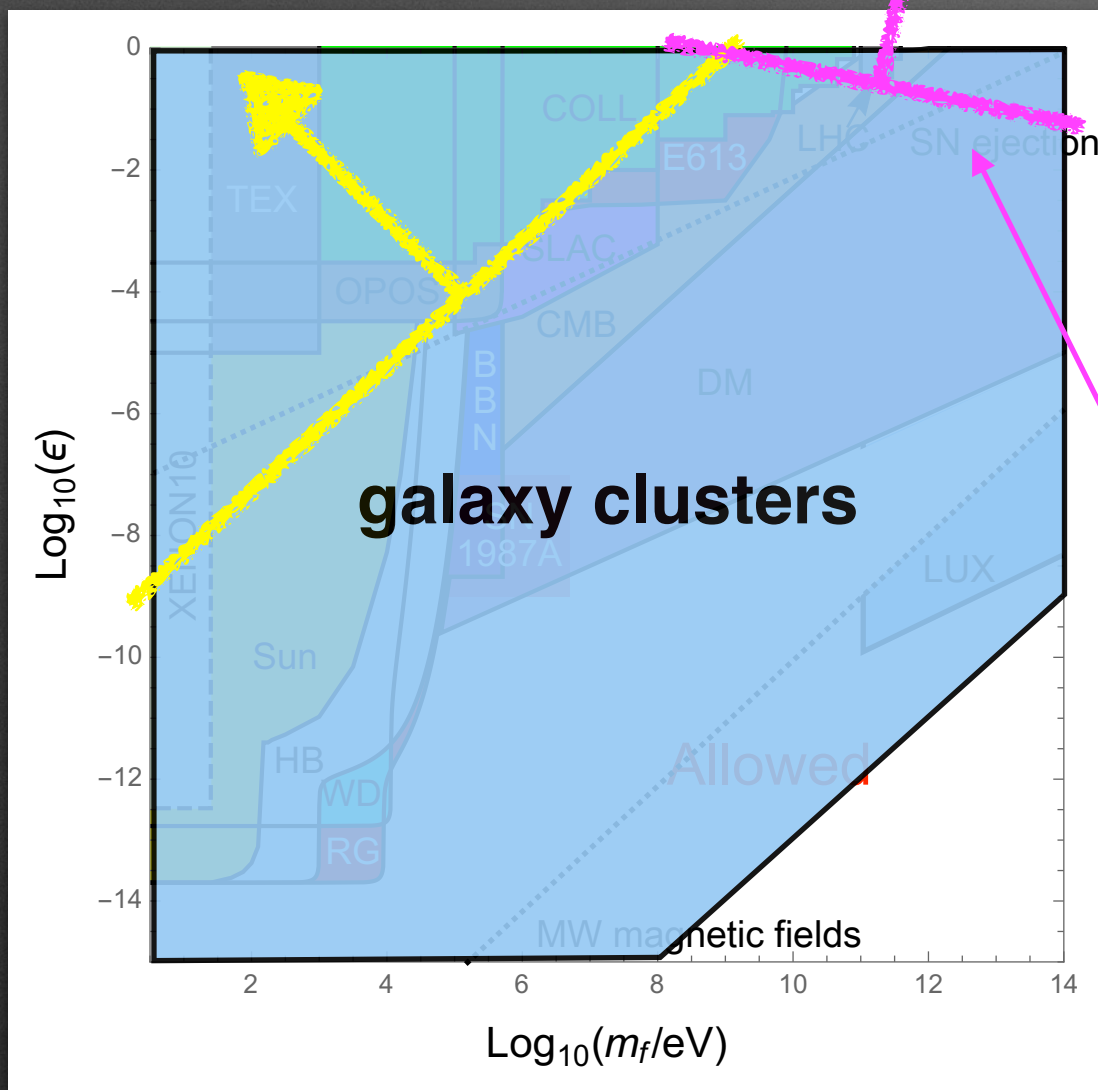
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Possibility for DM to be neutralized

- However, such a region is covered by other constraints.
- Whether neutralization can be really achieved within  $t_{\text{age}}$  is model-dependent.

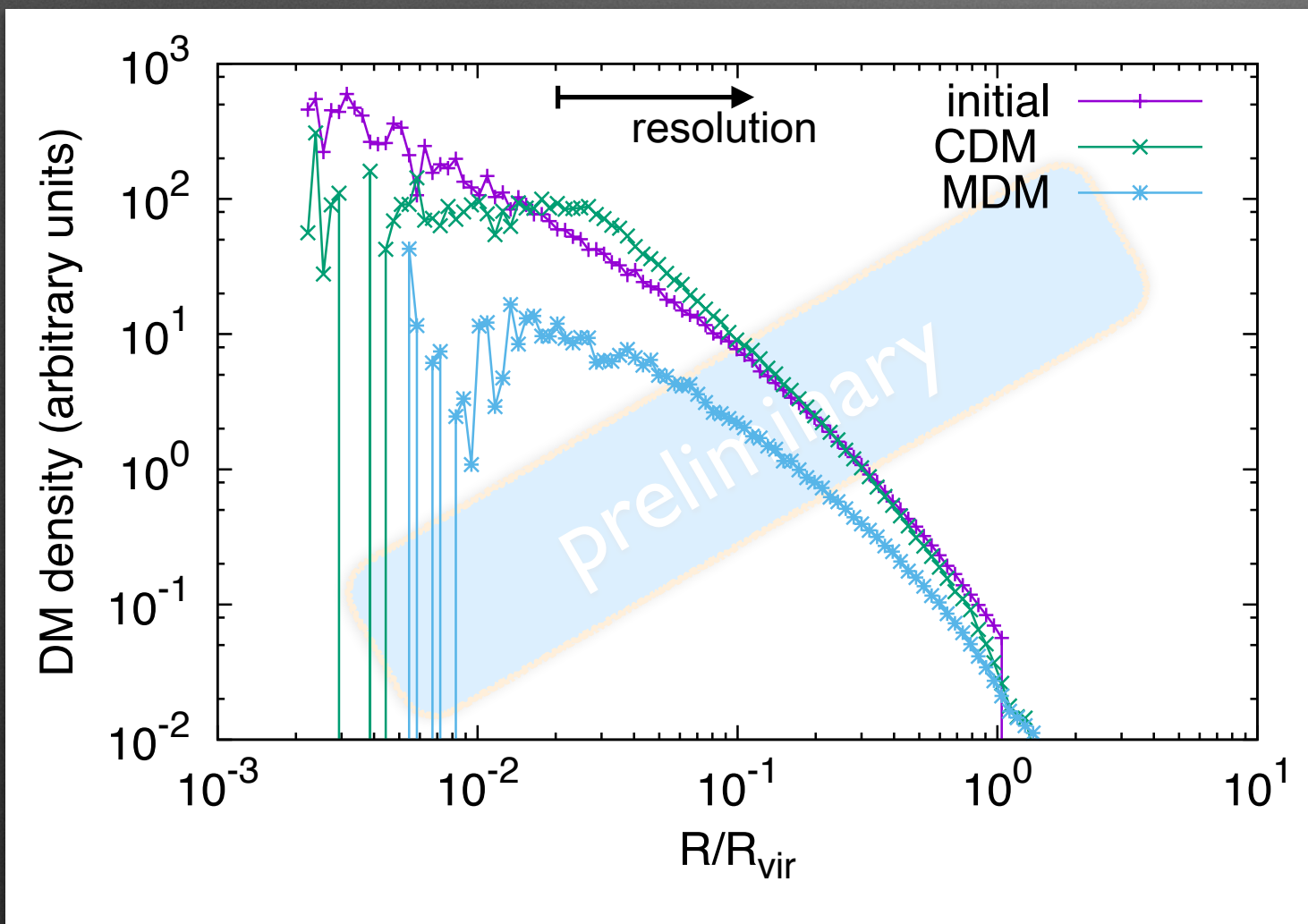




# Simulation

Hasegawa, Ichiki, Kadota, TS & Tashiro, in progress

## 3-dim N-body simulation of DM single halo in MDM model



- Halo size: a Coma-like cluster  
 $M_{\text{halo}} = 10^{15} M_{\text{sun}}$ ,  $R_{\text{halo}} = 2.8 \text{ Mpc}$
- Magnetic fields (fixed configuration):  
 $B = 1 \mu\text{G}$ ,  $\lambda_{\text{coherence}} = 50 \text{ kpc}$  (coarser than reality)
- Initial profile: NFW
- Number of particles:  $\sim 2 \times 10^5$
- Simulation time:  $t_{\text{age}} \sim 10 t_{\text{freefall}}$
- **MDM charge/mass ratio**

$$\frac{\epsilon}{m[\text{GeV}]} = 10^{-13}$$

- Modification of profile is apparent. Smoother profile in MDM.
- In CDM, NFW is quasi-stable. Yet not rigorously examined; scrutiny check is underway.



# Summary

We have discussed constraints on millicharged dark matter

- MDM is possible for GUT nor magnetic monopole are not confirmed. In models with dark  $U(1)$ , MDM can be achieved via kinetic mixing.
- We proposed **a new constraint on MDM from magnetic fields in galaxy clusters**. For density profile of DM halo to be consistent with CDM prediction & observations, Lorentz force should not dominate gravitational one. Our constraint assumes DM is pure MDM.
- Our constraint is tighter than any of previous constraints regardless of presence of  $U(1)_{\text{hidden}}$  or DM asymmetry. Backreaction & neutralization are irrelevant. Numerical simulation is in progress.



Thank you for your attention!



# Astrophysical constraints

Holdom (1986); Davidson, Hannestad, Raffelt (2000), ...

## Modified stellar evolution

- Produced via plasmon decay  $\gamma^* \rightarrow \chi \bar{\chi}$

If MDM mass  $< \omega_p/2$ , production is efficient

- plasmon mass:

$$\omega_p^2 = \frac{4\pi\alpha n_e}{m_e},$$

~ 300eV for the Sun; 10keV for red-giants

- decay rate:

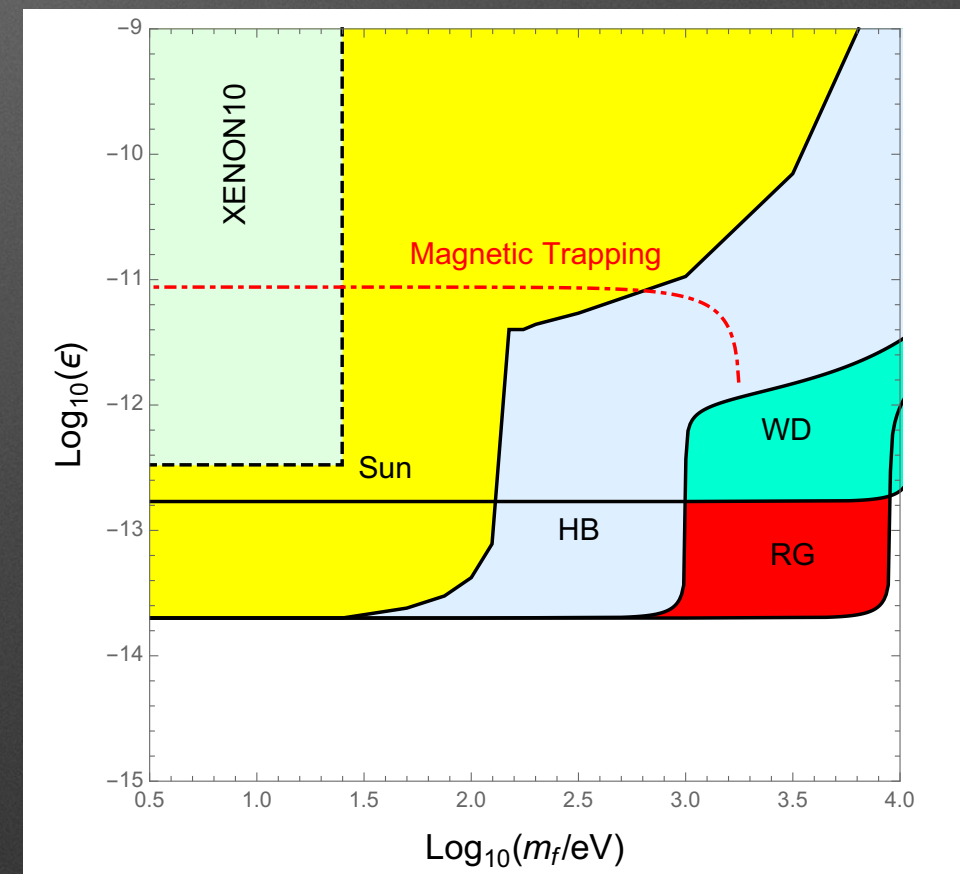
$$\Gamma_{\gamma^*} = \frac{\alpha}{3} \frac{Z}{\omega} (\omega_p^2 + 2m_f^2) \sqrt{1 - \frac{4m_f^2}{\omega_p^2}}$$

- MDM escapes if (cyclotron radius) > (stellar radius)

⇒ MDM channel should be subdominant:

$$\epsilon \leq 2 \times 10^{-14} \quad \text{for MDM mass} < 10\text{keV}.$$

cf. white dwarfs are less constraining because MDM escapes only from surface.



Vinyoles & Vogel (2015)



# Relic MDM abundance

## Thermal production

- main processes  $\chi\bar{\chi} \leftrightarrow f\bar{f}$  cf.  $2\gamma$  suppressed

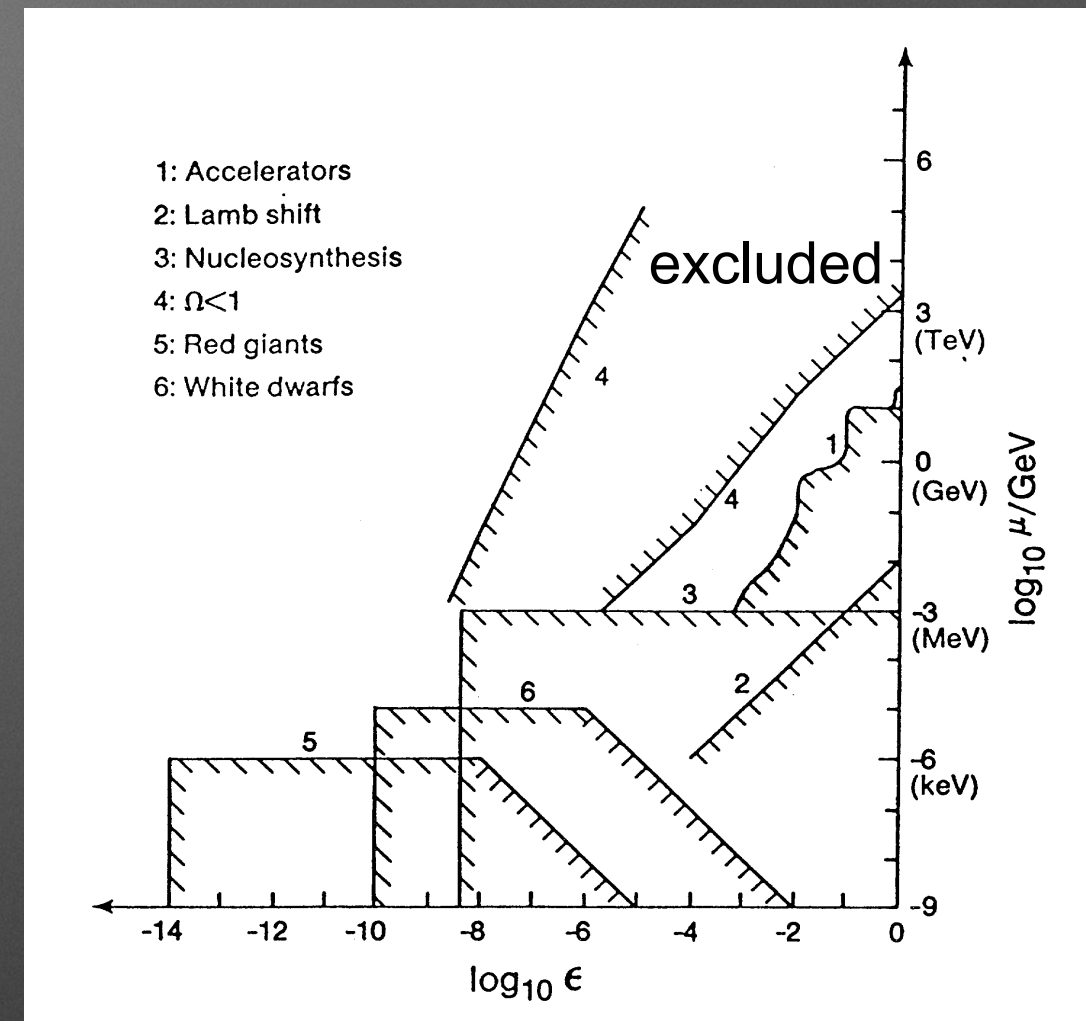
$$(\sigma_{\text{an}} v_{\text{rel}})_{f\bar{f}} = \frac{\pi\alpha_{\text{em}}^2\epsilon^2}{m_X^2} q_f^2 N_c \sqrt{1 - \frac{m_f^2}{m_X^2}} \left(1 + \frac{m_f^2}{2m_X^2}\right)$$

- Relic abundance (equilibrium assumed)

$$\Omega_{\text{MDM}} h^2 \simeq 0.1 \times \left(\frac{m}{\text{GeV}}\right)^2 \left(\frac{\epsilon}{10^{-3}}\right)^{-2}$$

- MDM is fully thermalized only if

$$\epsilon > 10^{-7} \left(\frac{m}{\text{GeV}}\right)^{1/2}.$$



Davidson, Campbell & Bailey (1991)

Thermal relics with observed  $\Omega_m \sim 0.24$  is incompatible with e.g, CMB.  
In principle, symmetric MDM should be produced non-thermally.

Caveat: if  $U(1)_{\text{hidden}}$  exists, MDM can annihilate into hidden photons and relic abundance can be suppressed significantly.



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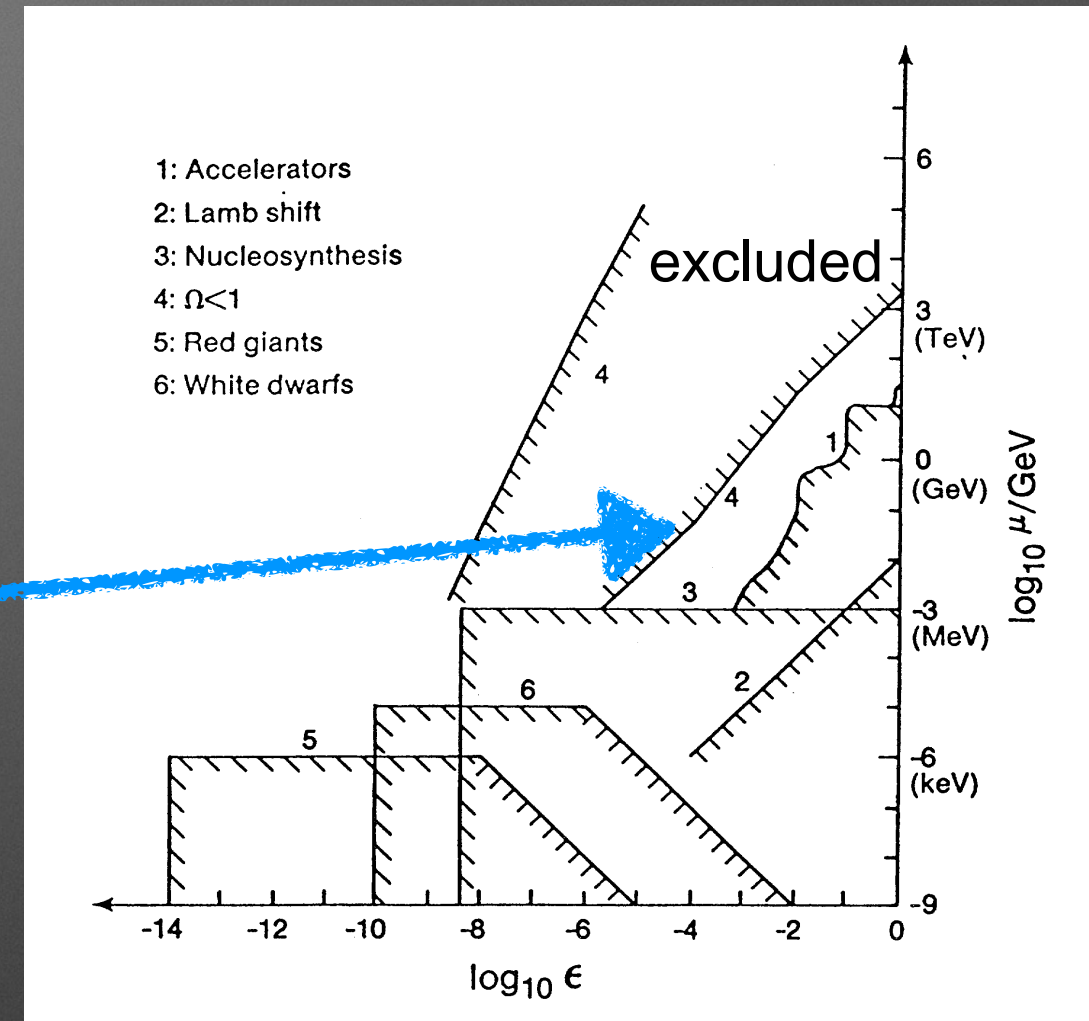
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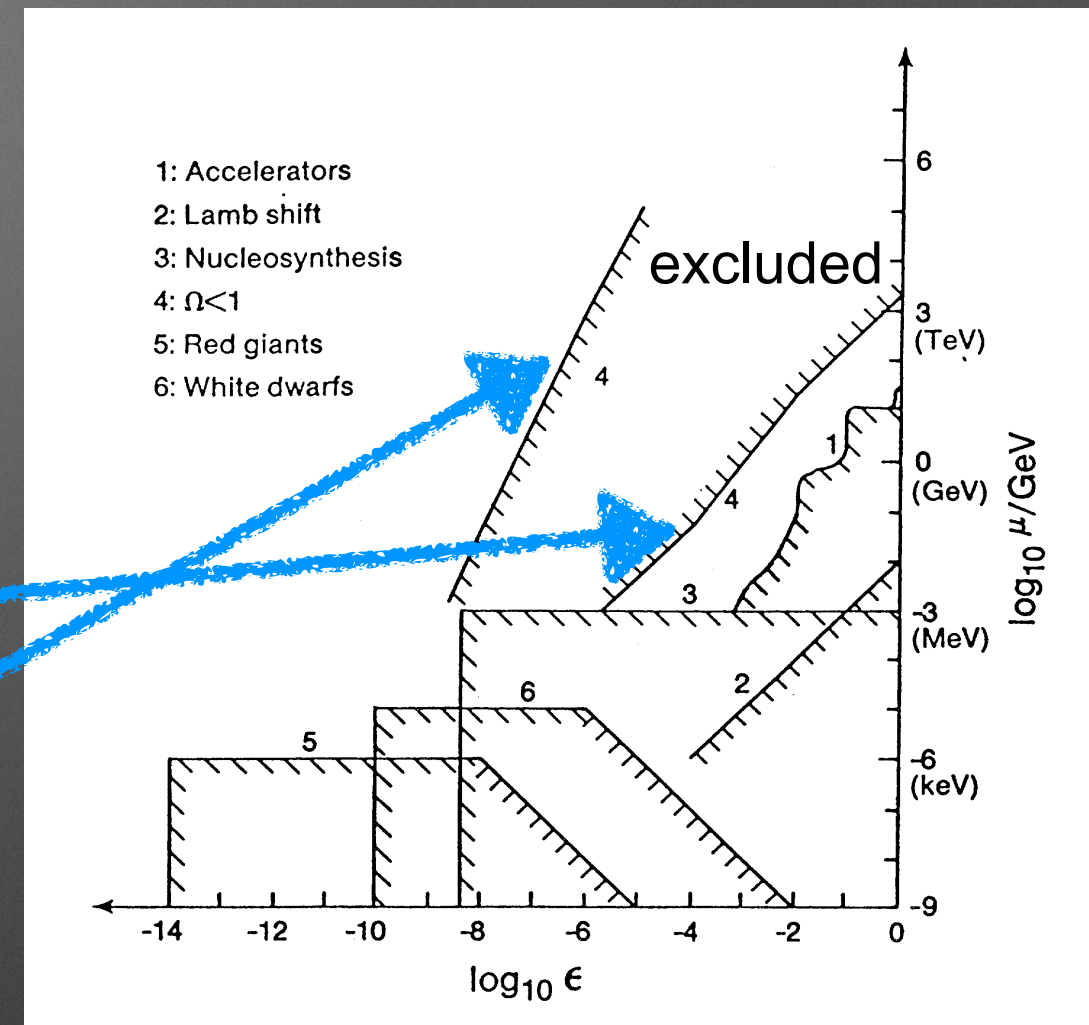
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# Structure formation & CMB

## Coupling with baryon via Coulomb scattering

$$\frac{d\sigma_{Xb}}{d\Omega_*} = \frac{\alpha_{\text{em}}^2 \epsilon^2}{4\mu_b^2 v_{\text{rel}}^4 \sin^4(\theta_*/2)}$$

cf. Compton scattering is further suppressed by  $\epsilon^2$ .

### - Acoustic oscillation is modified

- When MDM and baryon tightly couple, they collectively act as heavy baryon.
- Given fixed  $\Omega_b + \Omega_{\text{mdm}}$ , Silk damping is enhanced.

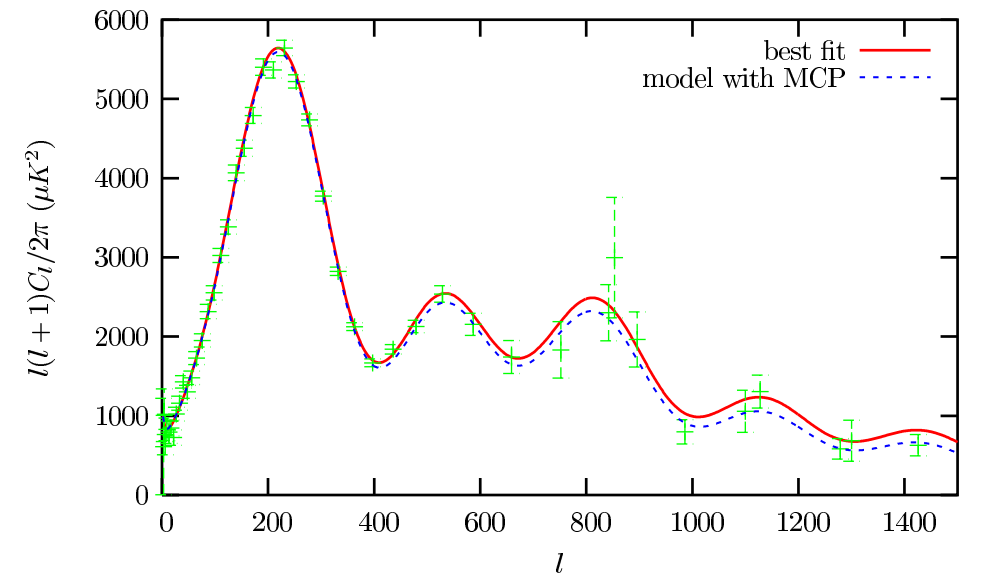


Figure 3: Two different CMB anisotropy spectra compared with extended WMAP dataset. Solid line represents the best fit model without millicharged particles,  $\Omega_b h_0^2 = 0.022$ . Dashed line corresponds to model with  $\Omega_b h_0^2 = 0.014$ ,  $\Omega_{\text{mcp}} h_0^2 = 0.007$ .

Dubovskya, Gorbunova & Rubtsov (2003)

### - MDM should have kinetically decoupled from baryon before recombination

$$\epsilon \lesssim 2.24 \times 10^{-4} \left( \frac{M}{1 \text{ TeV}} \right)^{1/2} \Rightarrow \text{thermal relic MDM is excluded}$$

Caveat: if  $U(1)_{\text{hidden}}$  exists, MDM acoustic-oscillates at late-times (kinetic recoupling), which leads to tighter constraints from matter power spectrum. [Kamada+ \(2013\)](#)



# Structure formation & CMB

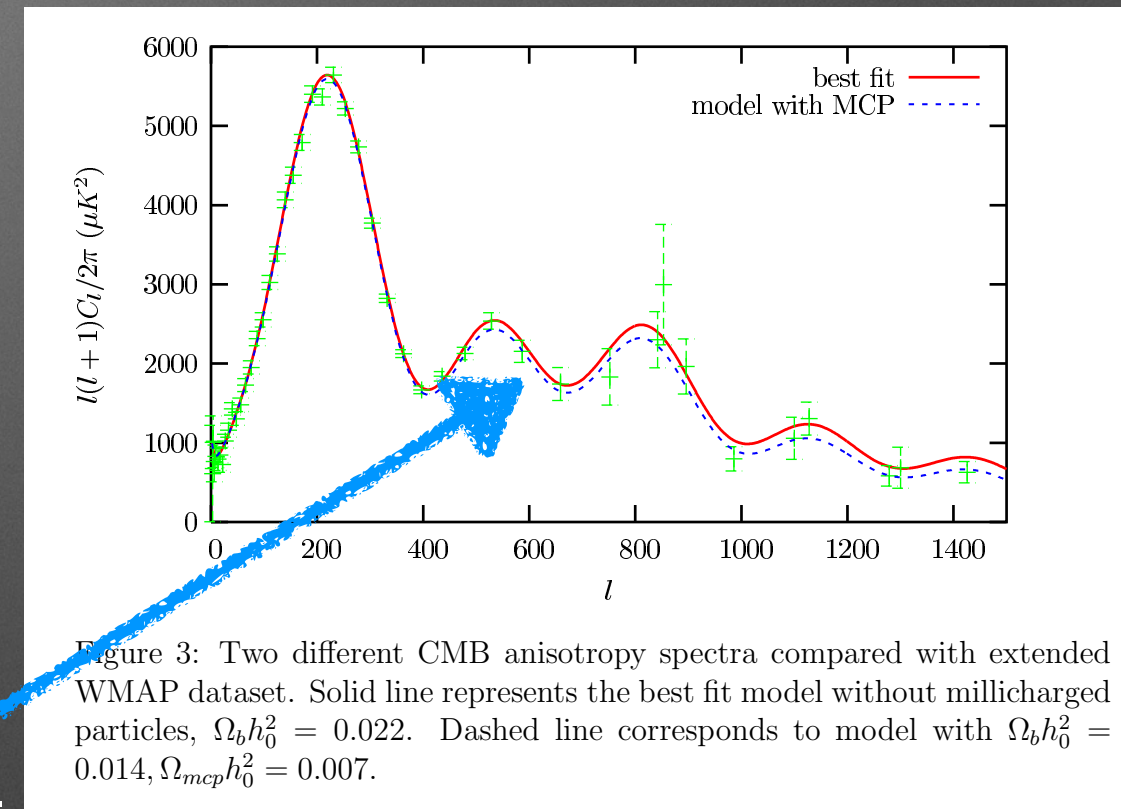
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# BBN constraints

## Effects on BBN

- Relevant only when  $m_{\text{DM}} \leq m_e$
- $e^+e^-$  annihilate also into MDM. Meanwhile photon is less heated up.

✓ higher  $N_{\text{eff}}$      $\Delta N_{\text{eff}} \simeq 6.9 \left( \frac{\epsilon}{10^{-8}} \right)^2$

If  $U(1)_{\text{hidden}}$  exist,  $N_{\text{eff}}$  is increased further

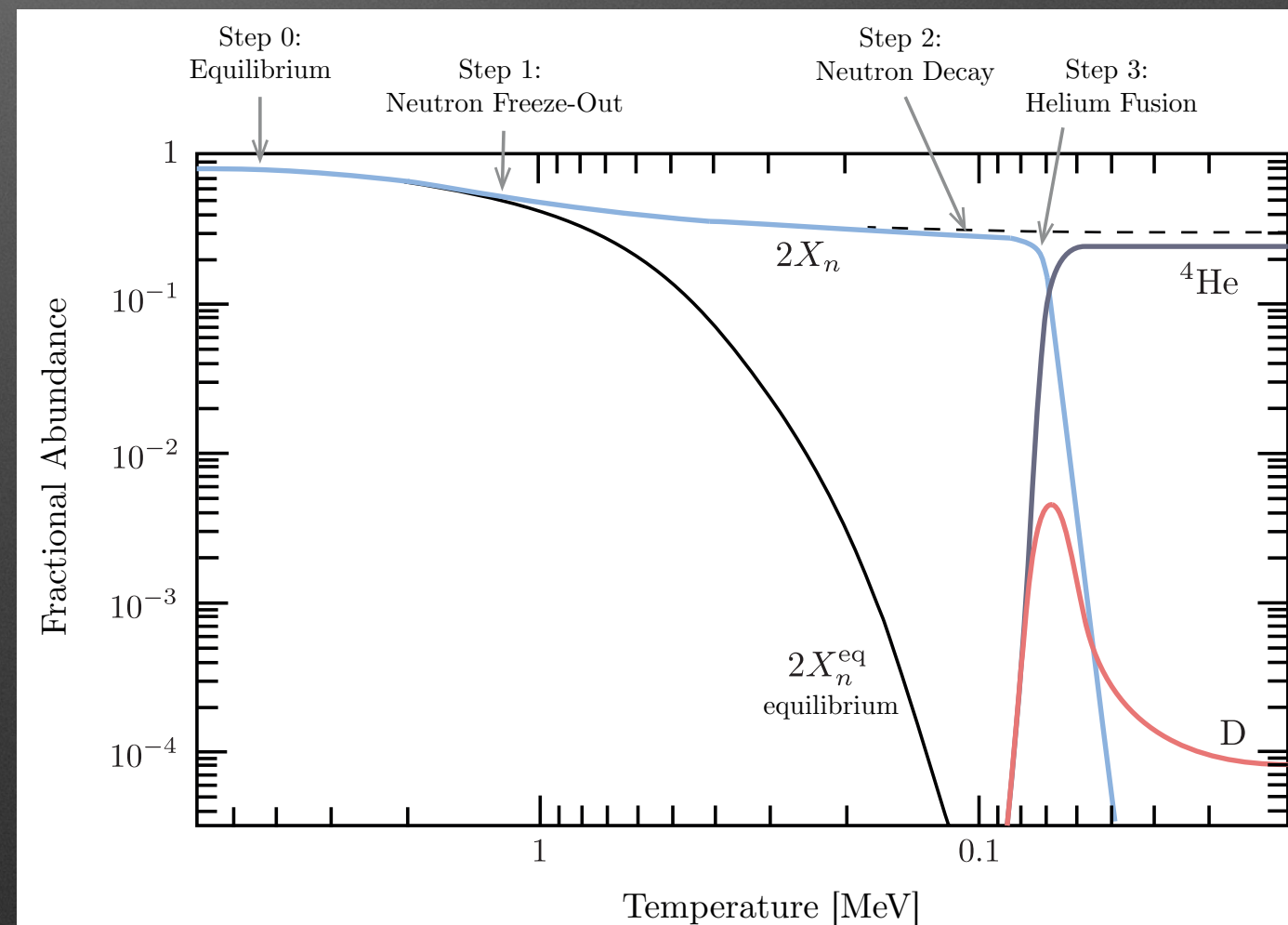
✓ higher  $n_B/n_\gamma$

(MDM also annihilates after BBN  
but well before recombination)

- Earlier freeze-out of neutrons & onset of BBN enhance  $^4\text{He}$  abundance.

$$\epsilon < 2.1 \times 10^{-9}.$$

(for  $m_{\text{DM}} \leq m_e$ )



(c) D. Baumann



# Direct detection

## Coulomb scattering of nuclei with MDM

- Nucleonic matrix element

$$\mathcal{M}_N = \frac{16\pi\alpha}{q^2} \epsilon Q_N m_\chi m_N \quad \Leftarrow \text{spin-independent scattering}$$

- Non-relativistic diff. cross-section wrt. recoil energy  $E_R = q^2/2m_T$

$$\frac{d\sigma_T}{dE_R}(v, q^2) = 8\pi m_T \frac{\alpha^2 \epsilon^2}{v^2 q^4} Z_T^2 F_T^2(q^2)$$

$F_T$ : the form factor (i.e. charge distribution in nuclei)  
 $m_T$ : mass of target nucleus

➡ Equivalent to exotic form factor with  $1/q^2$  in short-range interaction

- Current tightest constraint comes from LUX.

$$\epsilon \lesssim 7.6 \times 10^{-10} \left( \frac{M}{1 \text{ TeV}} \right)^{1/2}$$