

Towards a new scenario of QCD clump formation

based on 2111.05785

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I. Introduction

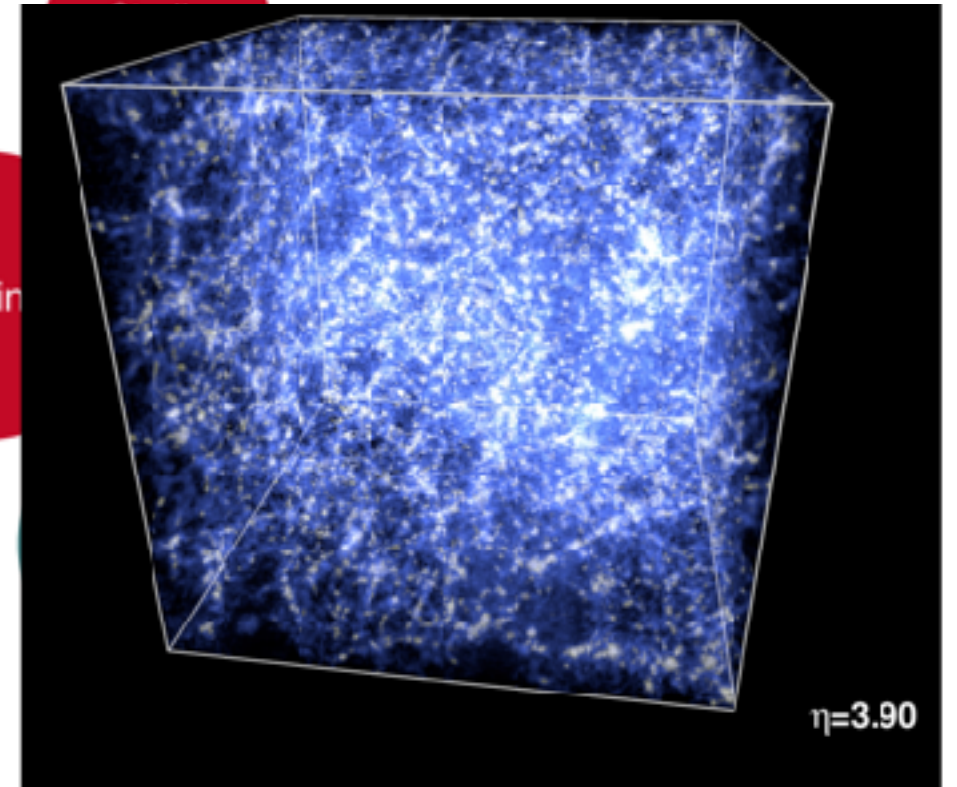
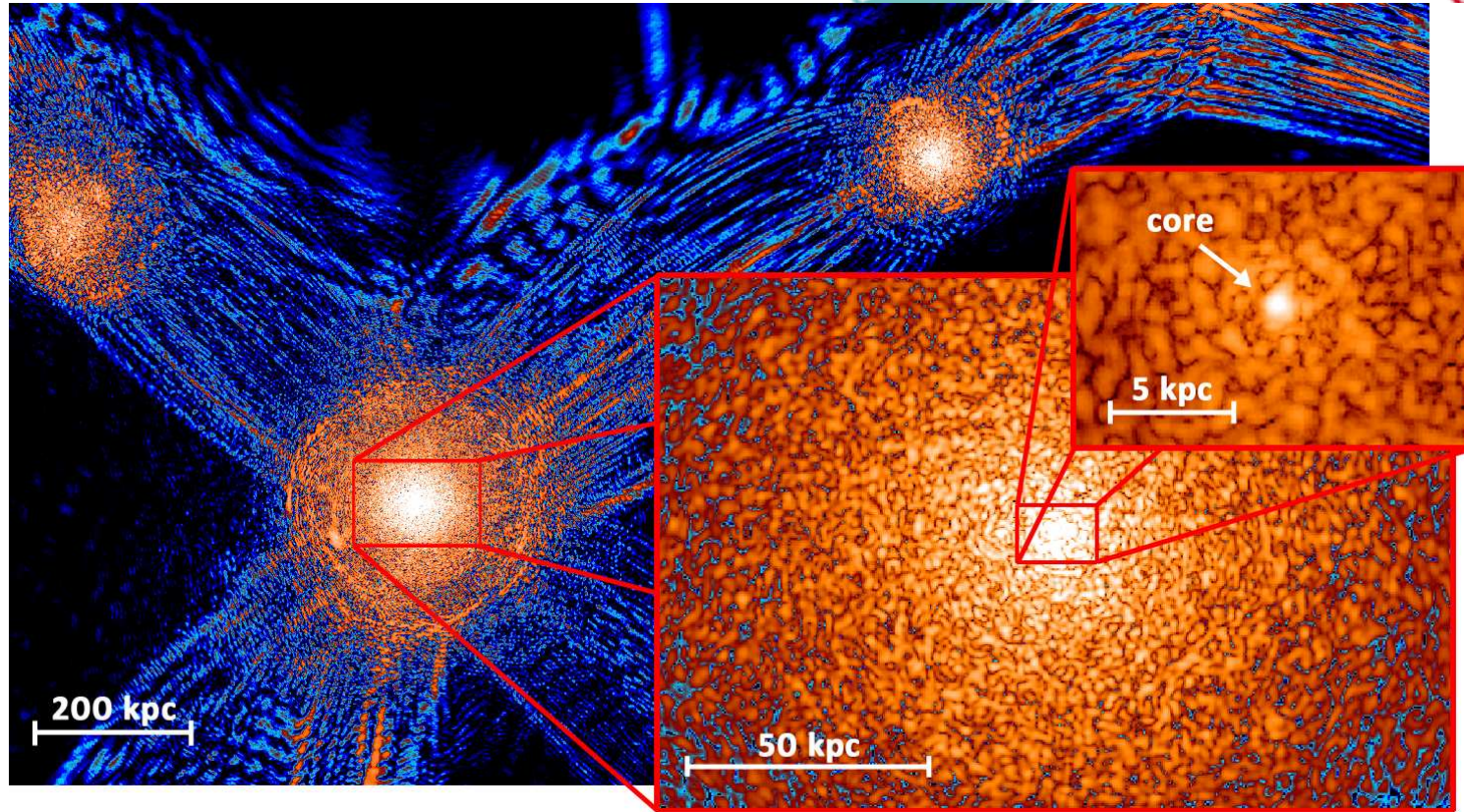


Axion

Axion-like particles

Fuzzy dark matter

Standard-model neutrinos



Weak scale

Little Higgs

Effective

MOND

Emergent gravity

Macroscopic

M

PBH

Primordial black holes

MaCHOs

CDM

WDM



**QCD axion generally predicts
characteristic imprints
on the structure of the Universe**

QCD axion in particle physics

$$\mathcal{L}_{\cancel{CP}} = -\frac{\alpha_s}{8\pi} \theta G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

Measurement of neutron electric dipole moment:

$$|\theta| < 1.3 \times 10^{-10} \quad (\text{strong CP problem})$$

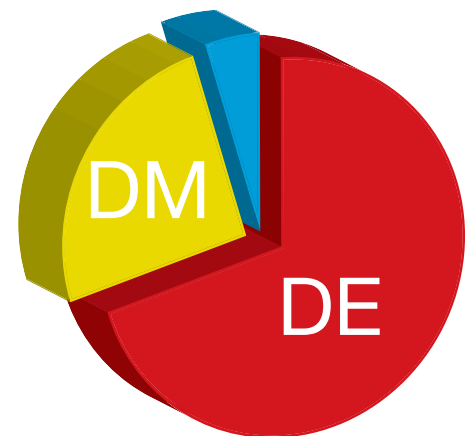


θ : dynamical field = QCD axion

Peccei, Quinn (1977), Weinberg (1978), Wilczek (1978)

QCD axion in cosmology

= dark matter candidate



Preskill, Wise, Wilczek (1983), Abbott, Sikivie (1983), Dine, Fischler (1983)

QCD axion potential

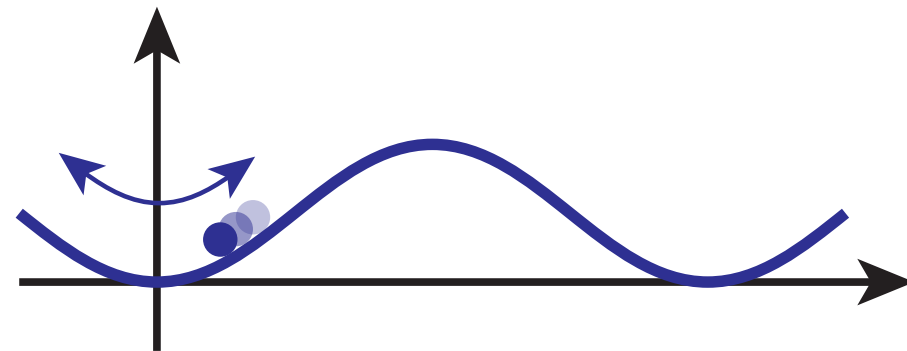
- temperature-dependent axion mass:

$$m_a(T) = \begin{cases} \chi \left(\frac{T_c}{T}\right)^b & T > T_c \\ m_a & T < T_c \end{cases}$$

$$b \simeq 8.16, \quad T_c \simeq 0.15 \text{ GeV} \quad \text{Borsanyi et al 1606.07494}$$

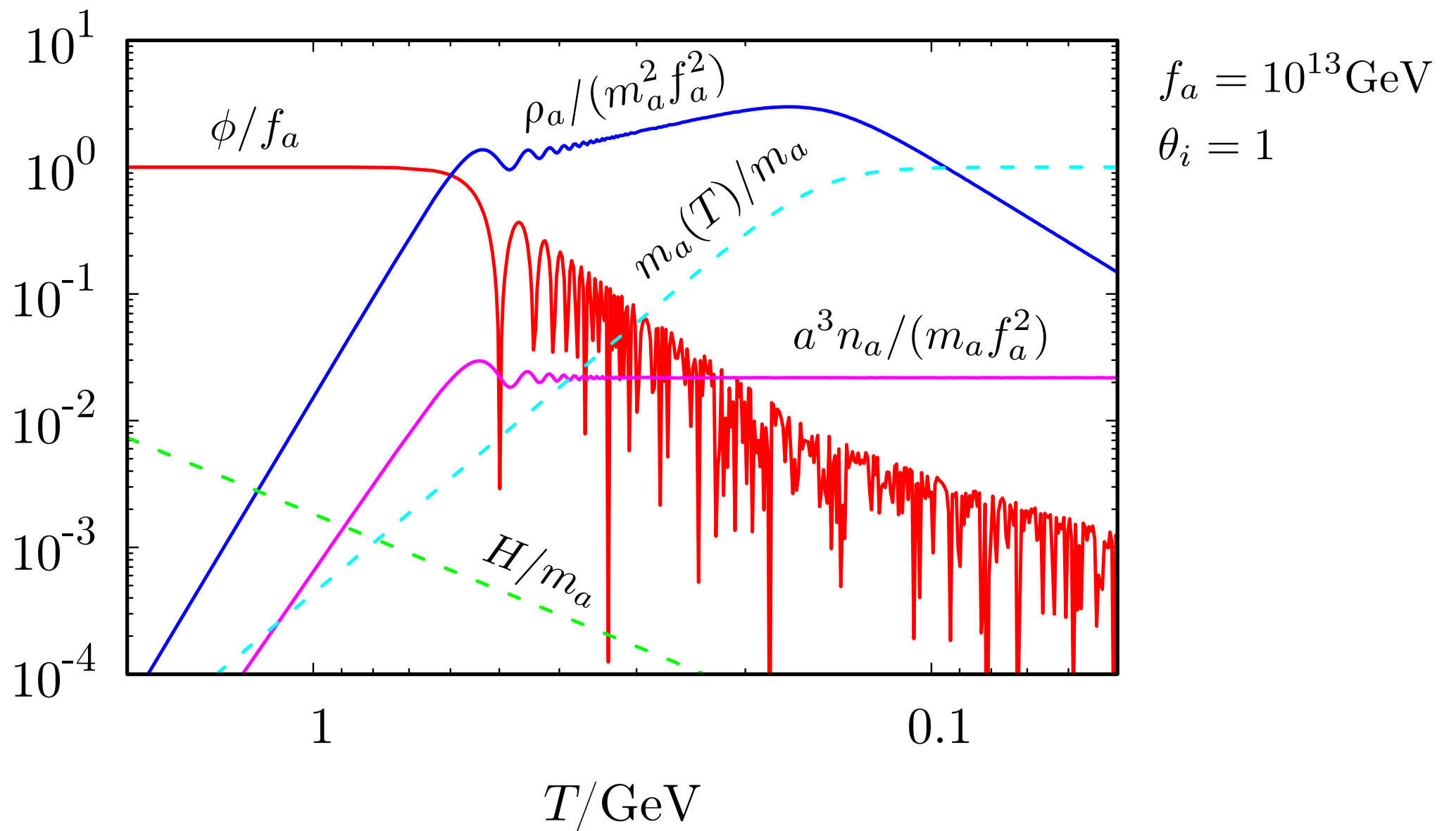
- zero-temperature axion mass: $m_a \simeq 6 \mu\text{eV} \left(\frac{10^{12} \text{ GeV}}{f_a} \right)$

- (typical) axion potential: $V(\phi) = m_a^2(T) f_a^2 \left(1 - \cos \left(\frac{\phi}{f_a} \right) \right)$



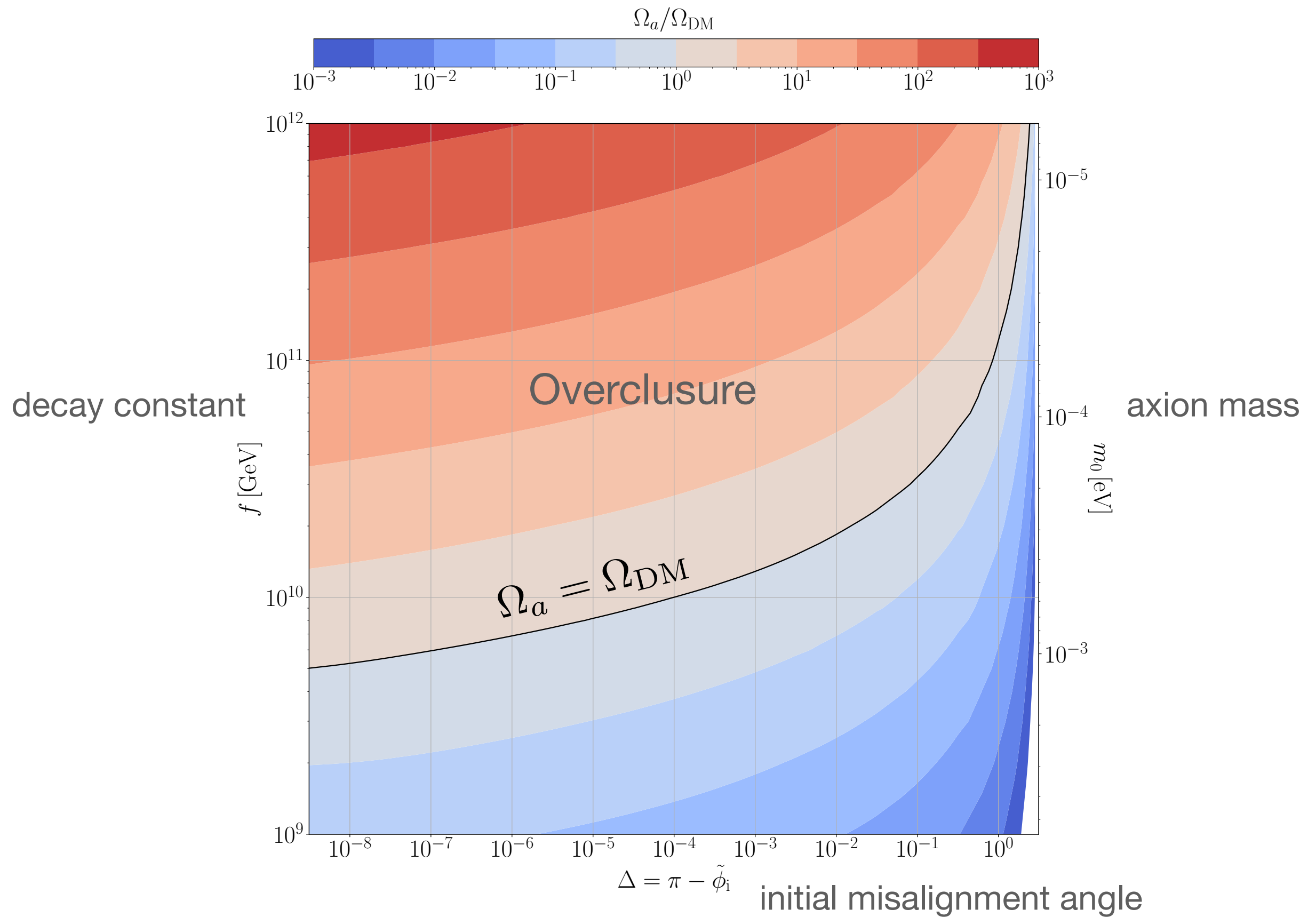
Misalignment production of the QCD axion

$$\ddot{\phi} + 3H\dot{\phi} + V_{\phi} = 0$$

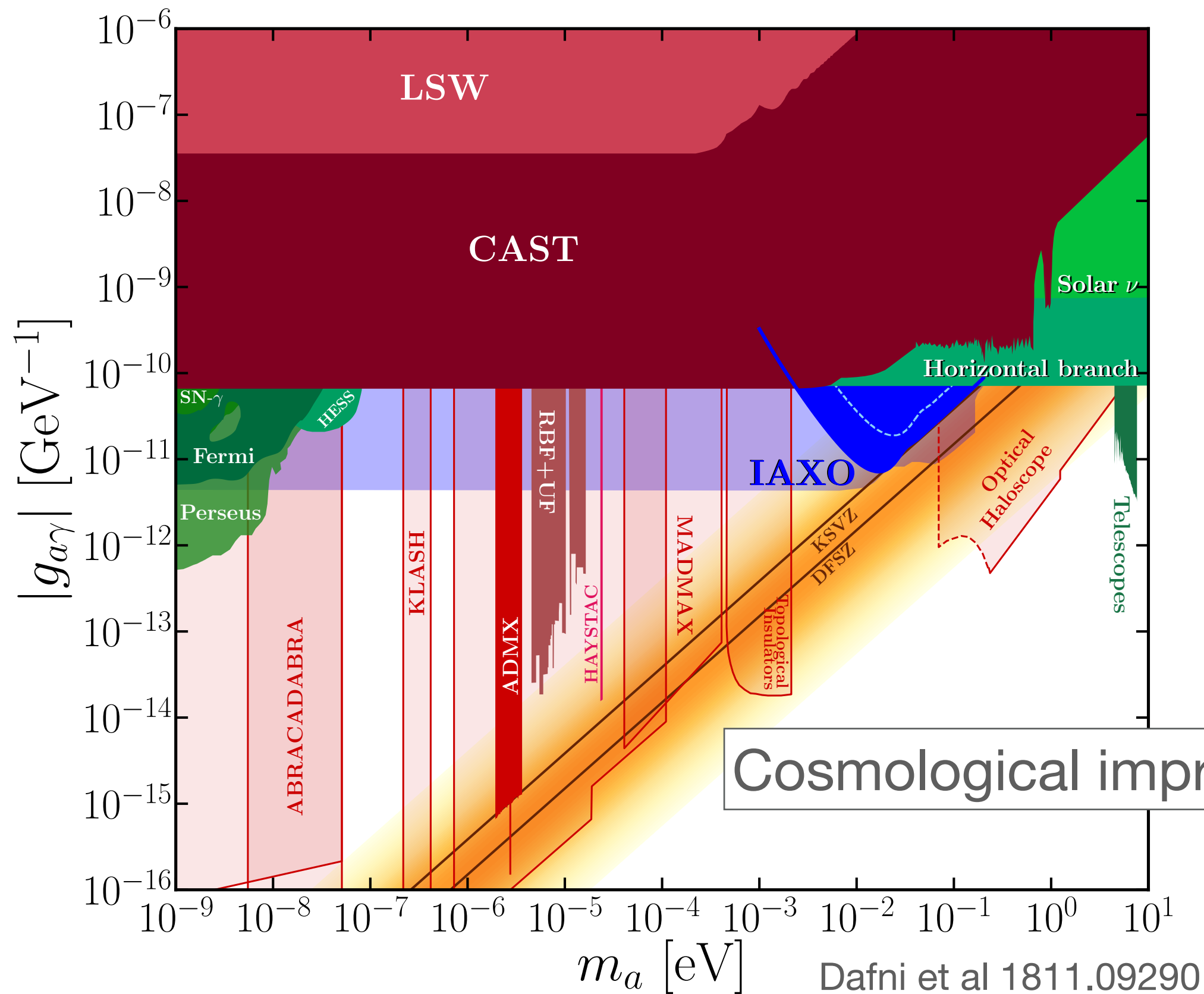


$$T_{\text{osc}} \simeq 1 \text{ GeV} \left(\frac{60}{g_*} \right)^{0.082} \left(\frac{10^{12} \text{ GeV}}{f_a} \right)^{0.16}, \quad \Omega_a h^2 \simeq 0.15 \theta_i^2 \left(\frac{60}{g_*} \right)^{0.42} \left(\frac{f_a}{10^{12} \text{ GeV}} \right)^{1.16} F_{\text{ah}}(\theta_i)$$

Axion DM abundance with hilltop initial condition

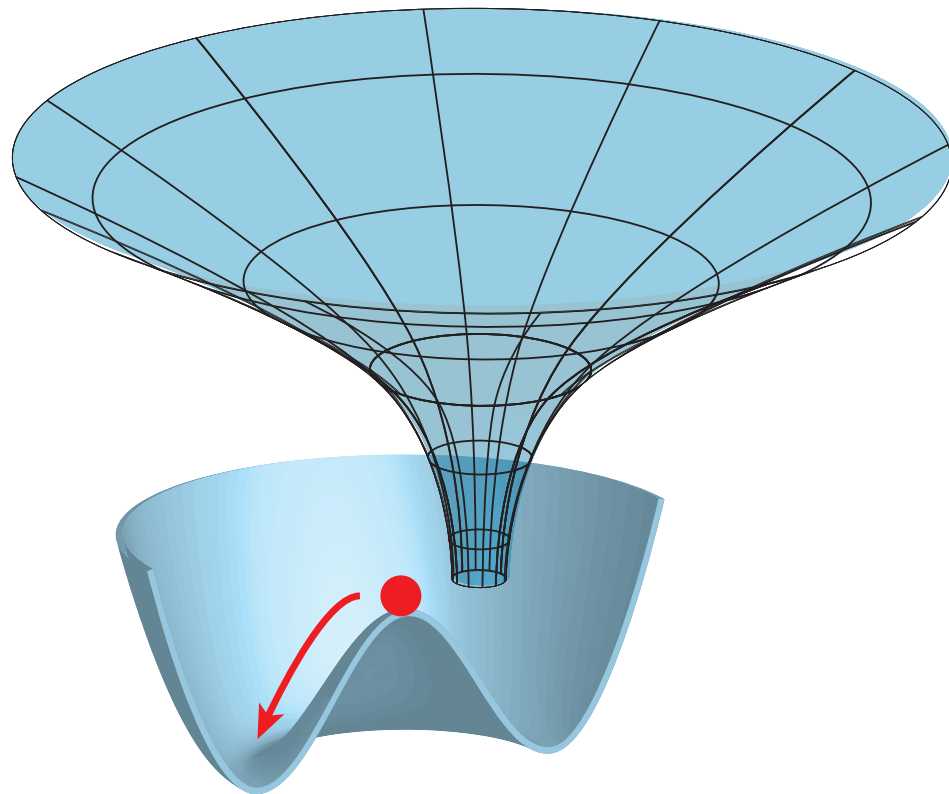


Current status of QCD axion search



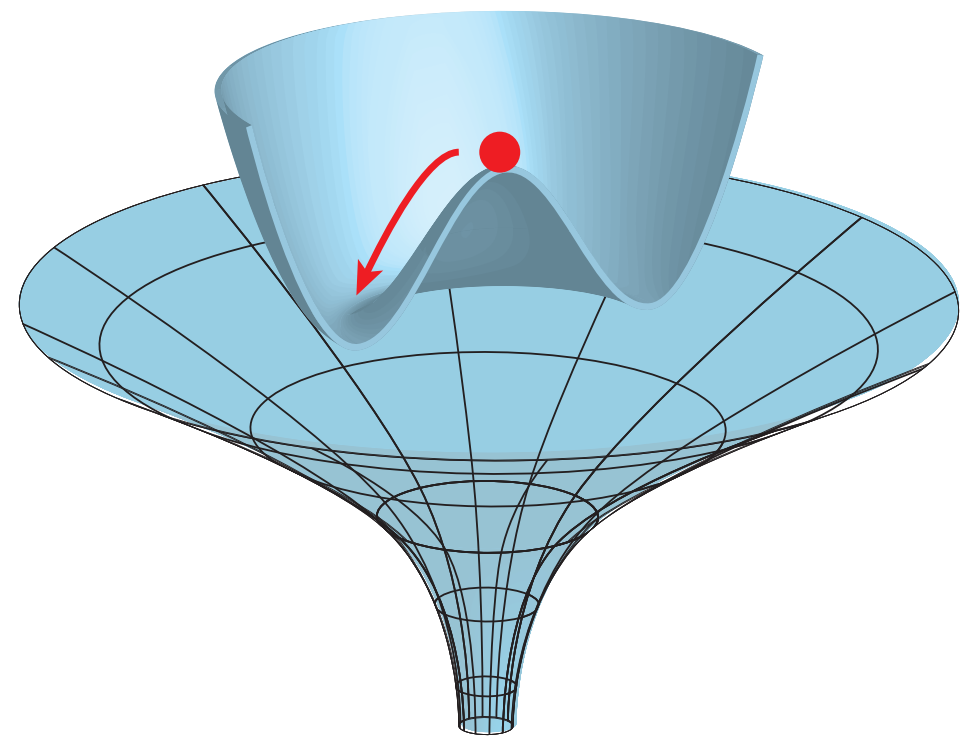
Axion cosmology — two scenarios

Pre-inflationary scenario



- large-scale isocurvature

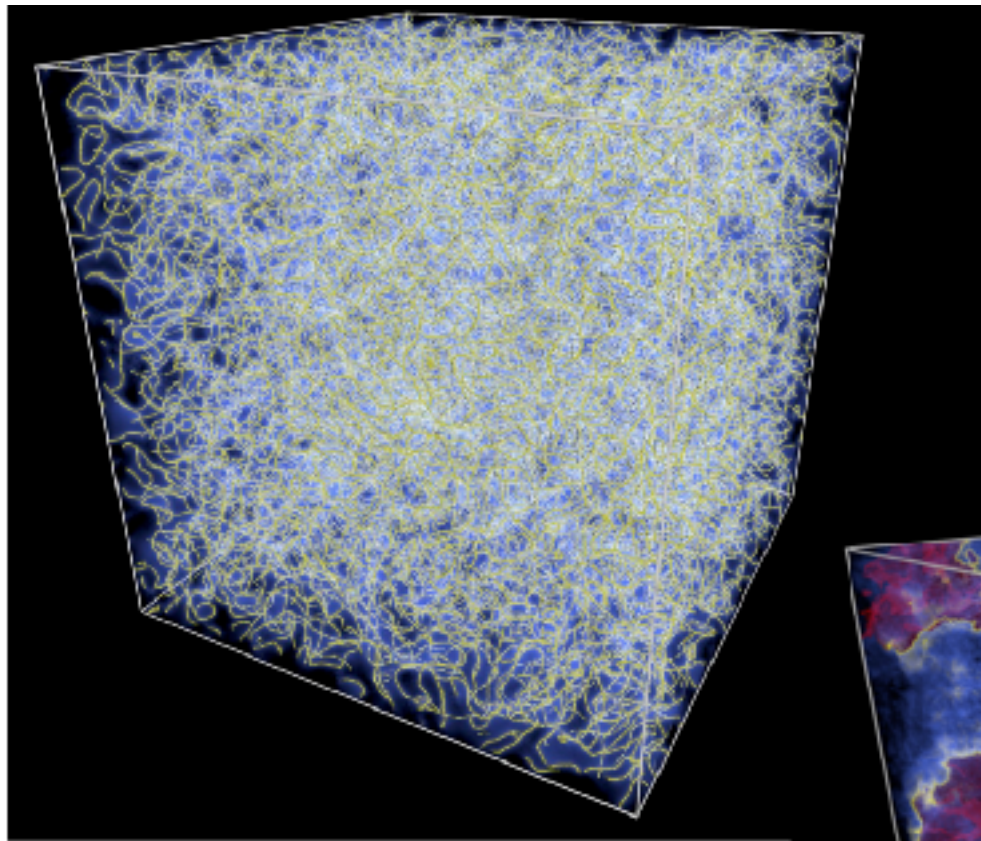
Post-inflationary scenario



- $O(1)$ isocurvature fluctuation
- Topological defect

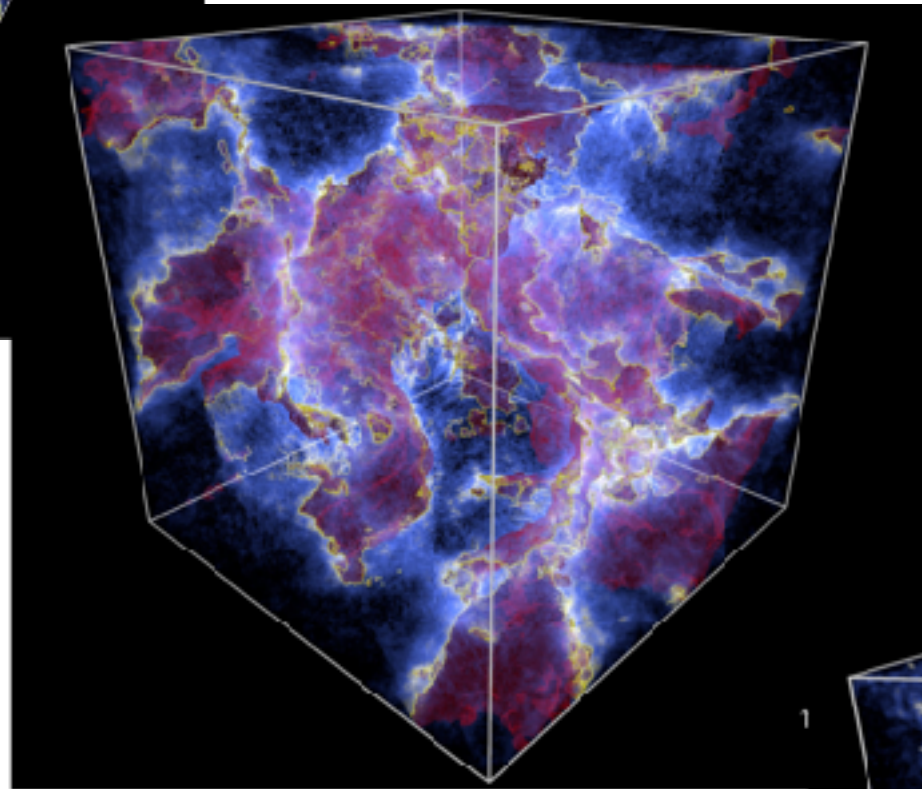
time

Post-inflationary scenario

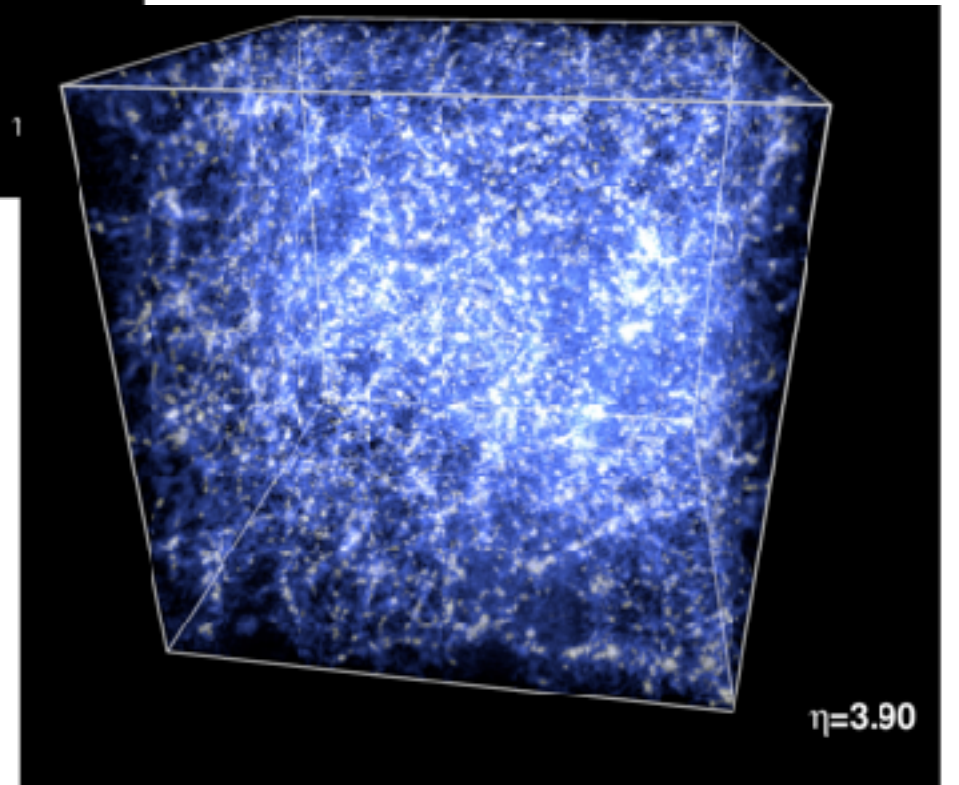


cosmic string

cosmic string & domain wall



axion minicluster



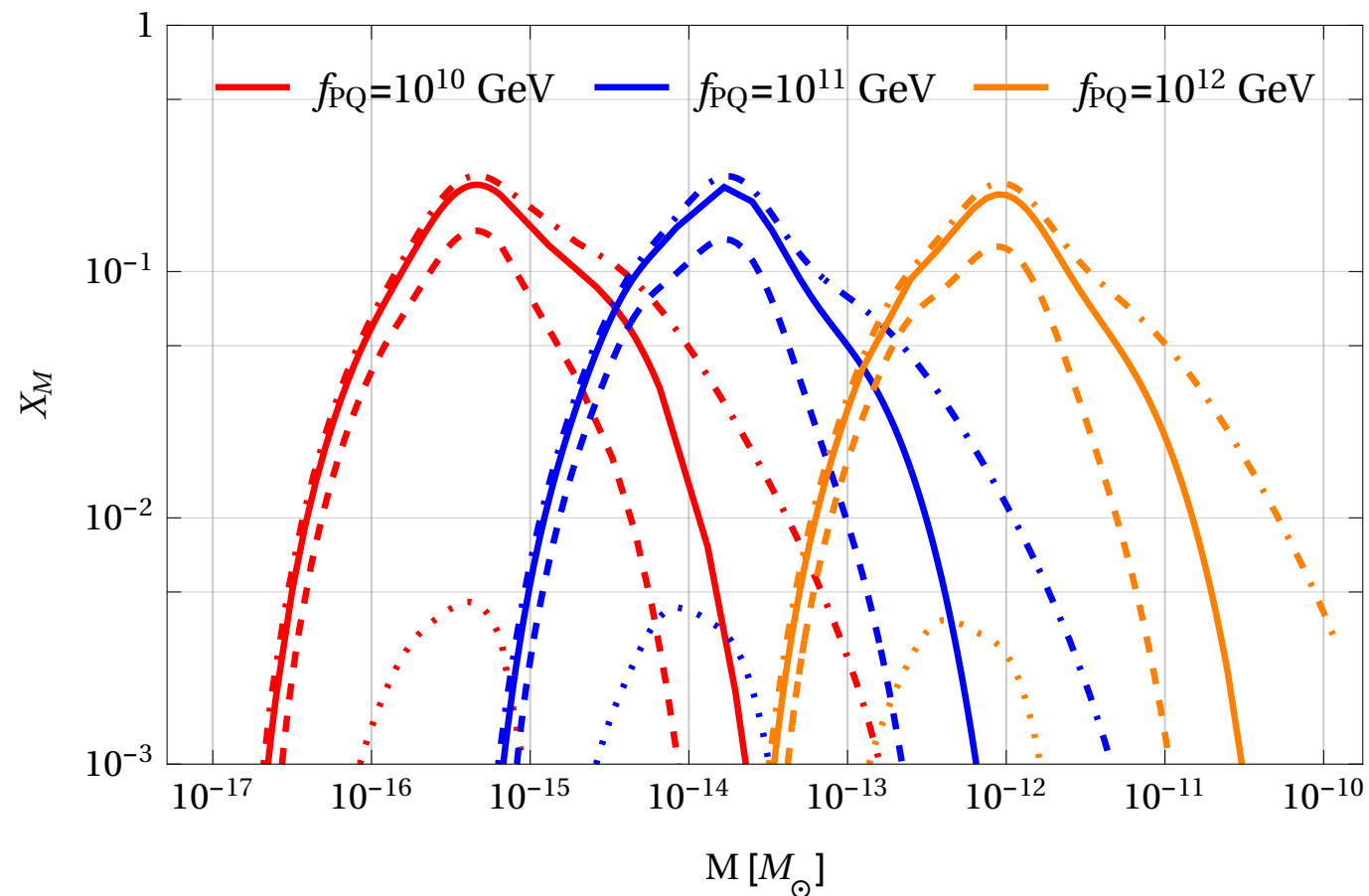
$$\Omega_a = (0.102 \pm 0.02) \times (f_a/10^{11} \text{GeV})^{1.187}$$

$$f_a = (2.27 \pm 0.33) \times 10^{11} \text{GeV}$$

$$(m_a = 25.2 \pm 3.6 \mu\text{eV})$$

Buschmann, Foster, Safdi 1906.00967

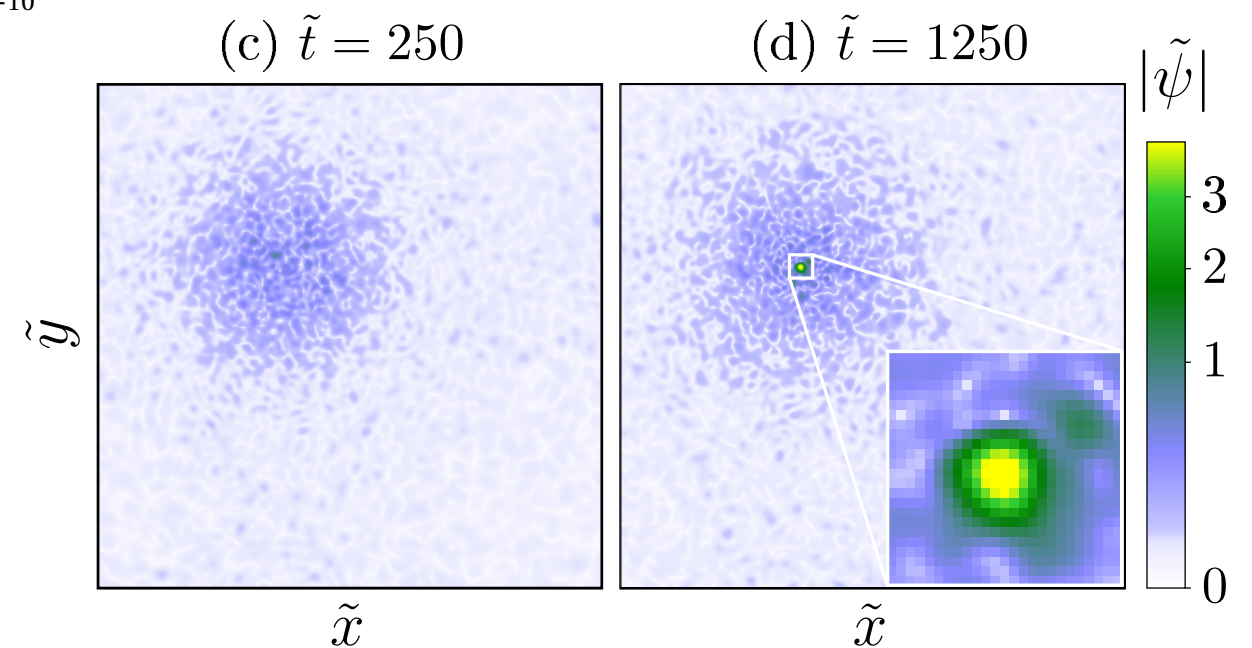
Axion minicluster



Enander, Pargner, Schwetz 1708.04466

Hogan, Rees (1988)
Kolb, Tkachev (1993)
Seidel, Suen (1994)

Axion star

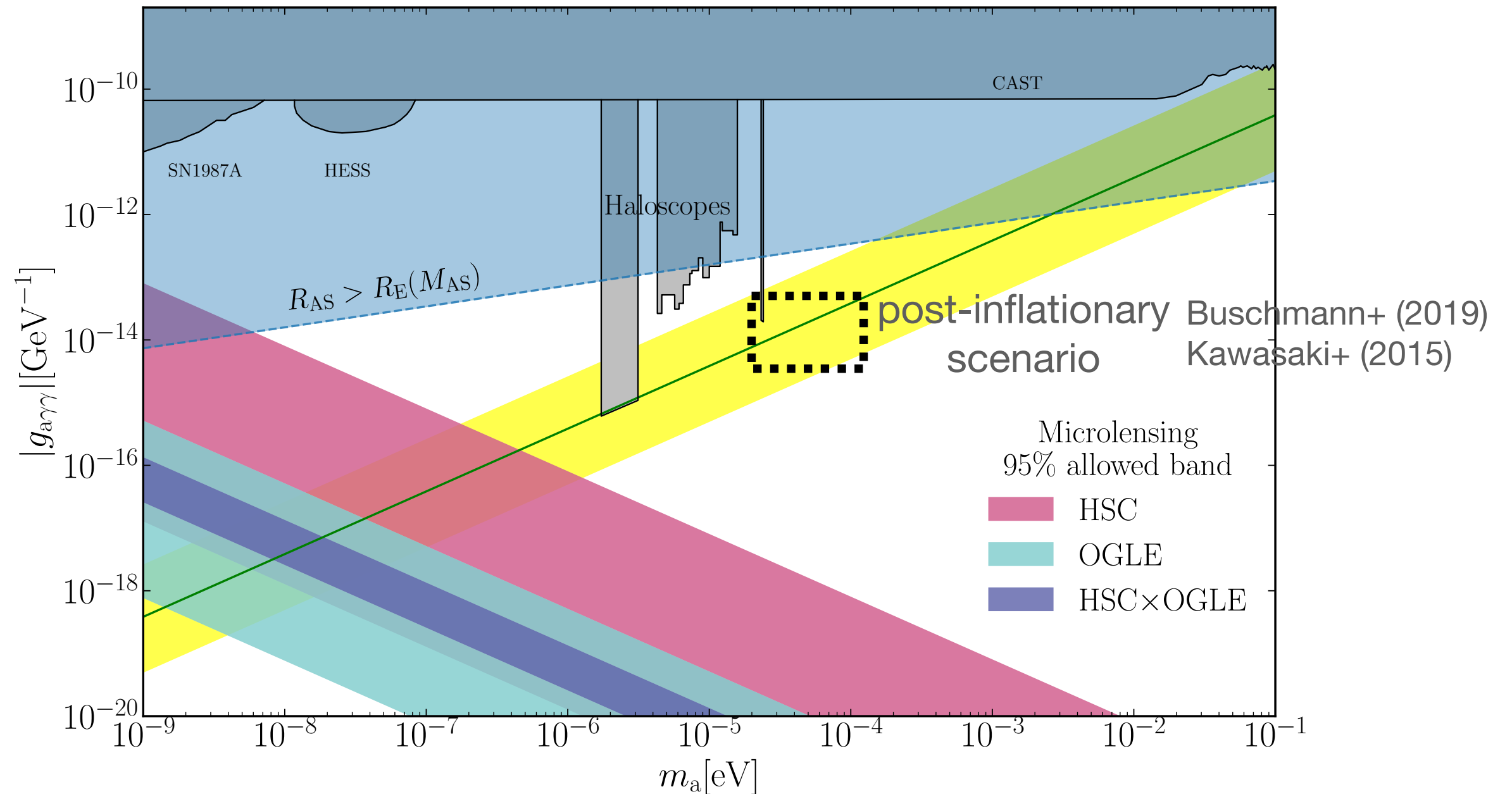


Levkov, Panin, Tkachev 1804.05857

see also Schiappacasse, Hertzberg 1704.04729

HSC & OGLE microlensing events as evidence of QCD axion star

Sugiyama, Takada, Kusenko 2108.03063



see also Fujikura, Hertzberg, Schiappacasse, Yamaguchi 2109.04787
(constraints from EROS-2 & HSC)

II. Axion fluctuation & clustering

Possible amplification of QCD axion fluctuation

- $O(1)$ isocurvature fluctuation (post-inflationary)
 - cosmic string/domain wall decay (post-inflationary)
-

- resonant (tachyonic) instability from self-interaction

Arvanitaki et al 1909.11665; Fukunaga, NK, Urakawa 2004.08929

- resonant (tachyonic) gauge field production

Agrawal, Marques-Tavares, Xue 1708.05008; NK, Sekiguchi, Takahashi 1711.06590

- adiabatic (curvature & temperature) fluctuation

Arvanitaki et al 1909.11665; Sikivie, Xue 2110.13157; NK, Kogai, Urakawa 2111.05785

(pre-inflationary scenario)

Strategy

Axion field evolution in curved spacetime:

$$\frac{1}{\sqrt{-g}} \partial_\mu (\sqrt{-g} g^{\mu\nu} \partial_\nu \phi) + \frac{\partial V(\phi, T)}{\partial \phi} = 0$$

$$V(\phi, T) = m_a^2(T) f_a^2 \left[1 - \cos \left(\frac{\phi}{f_a} \right) \right]$$

Perturbing metric & temperature (energy-momentum tensor):

$$g_{\mu\nu} = \bar{g}_{\mu\nu} + \delta g_{\mu\nu}, \quad T \rightarrow T + \delta T \quad (\rho \rightarrow \rho + \delta\rho)$$



* linear perturbation

Evolution of axion fluctuation sourced by adiabatic fluctuations
(metric/temperature fluctuations)

Metric perturbation with Conformal Newtonian gauge:

$$ds^2 = -a^2(1 - 2\Phi)d\tau^2 + a^2(1 + 2\Psi)d\mathbf{x}^2$$

.....

Perturbed (linearized) Einstein equations:

$$-3\mathcal{H}^2\Phi - 3\mathcal{H}\Psi' + \nabla^2\Psi = -4\pi Ga^2\delta\rho$$

$$\partial_i(\mathcal{H}\Phi + \Psi') = 4\pi Ga^2(\rho + p)\partial_i v$$

$$-\mathcal{H}(\Phi' + 2\Psi) + \mathcal{H}^2\Phi - \frac{1}{3}\nabla^2(\Phi - \Psi) - \Psi'' - \frac{2a''}{a} = 4\pi Ga^2\delta p$$

.....

Energy-momentum conservation: $T^\mu_{\nu;\mu} = 0$

$$\delta' + (1 + w)\nabla^2 v + 3(c_s^2 - w)\mathcal{H}\delta + 3(1 + w)\Psi' = 0$$

$$\mathcal{H}(1 - 3c_s^2)\partial_i v + \partial_i v' + \frac{c_s^2}{1 + w}\partial_i \delta - \partial_i \Phi = 0$$

Radiation-dominated Universe & no anisotropic stress

$$(c_s^2 = w = 1/3)$$

$$(\Psi = \Phi)$$



$$\delta_r'' - \frac{1}{3}\nabla^2\delta_r + 4\Phi'' + \frac{4}{3}\nabla^2\Phi = 0$$

$$\Phi'' + 4\mathcal{H}\Phi' - \frac{1}{3}\nabla^2\Phi = 0$$

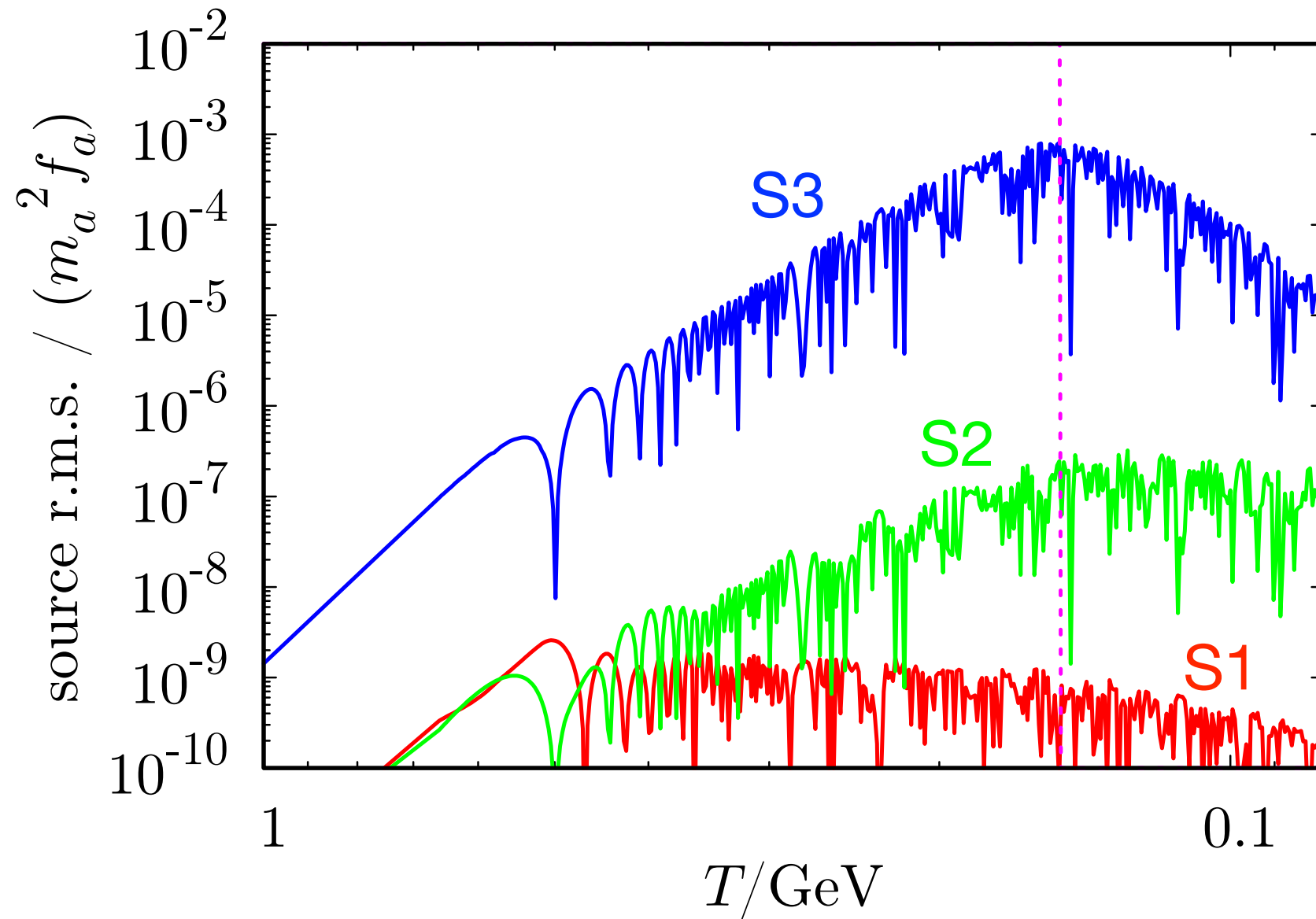
.....

Axion field evolution:

$$\phi'' + 2\mathcal{H}\phi' - (1 - 4\Phi)\nabla^2\phi + a^2V_\phi + \underbrace{4\Phi'\phi' - 2a^2\Phi V_\phi + a^2V_{\phi T}\delta T}_{\text{source terms}} = 0$$

source terms

Source for axion fluctuation

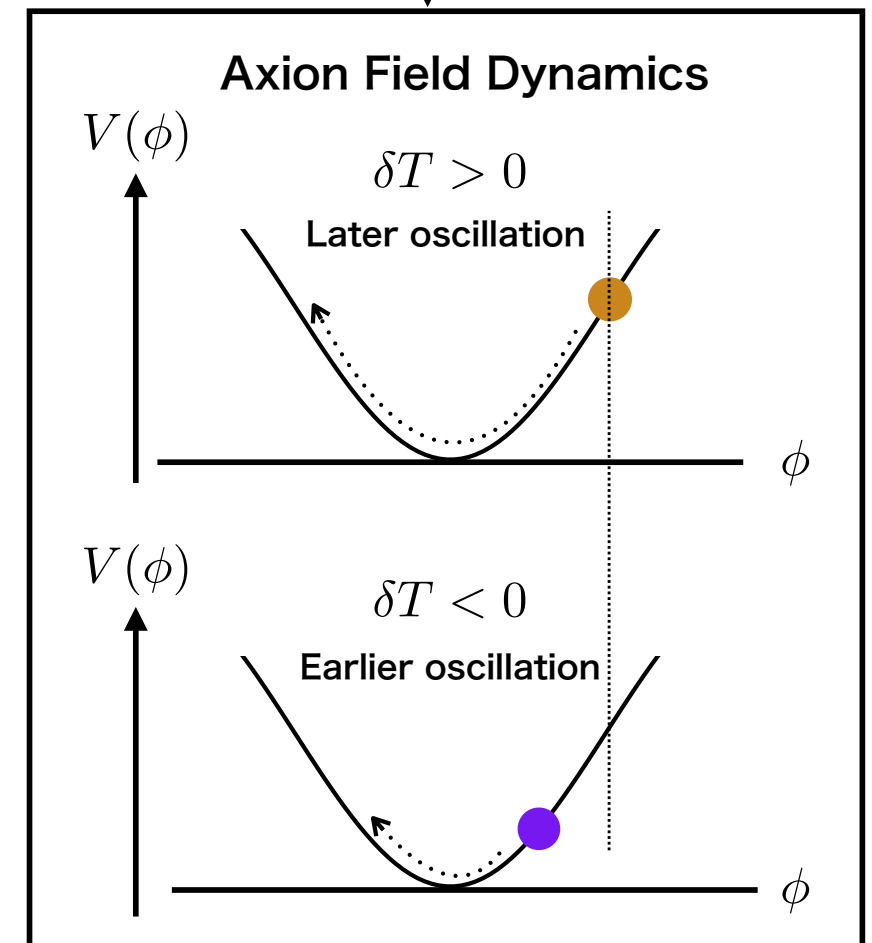
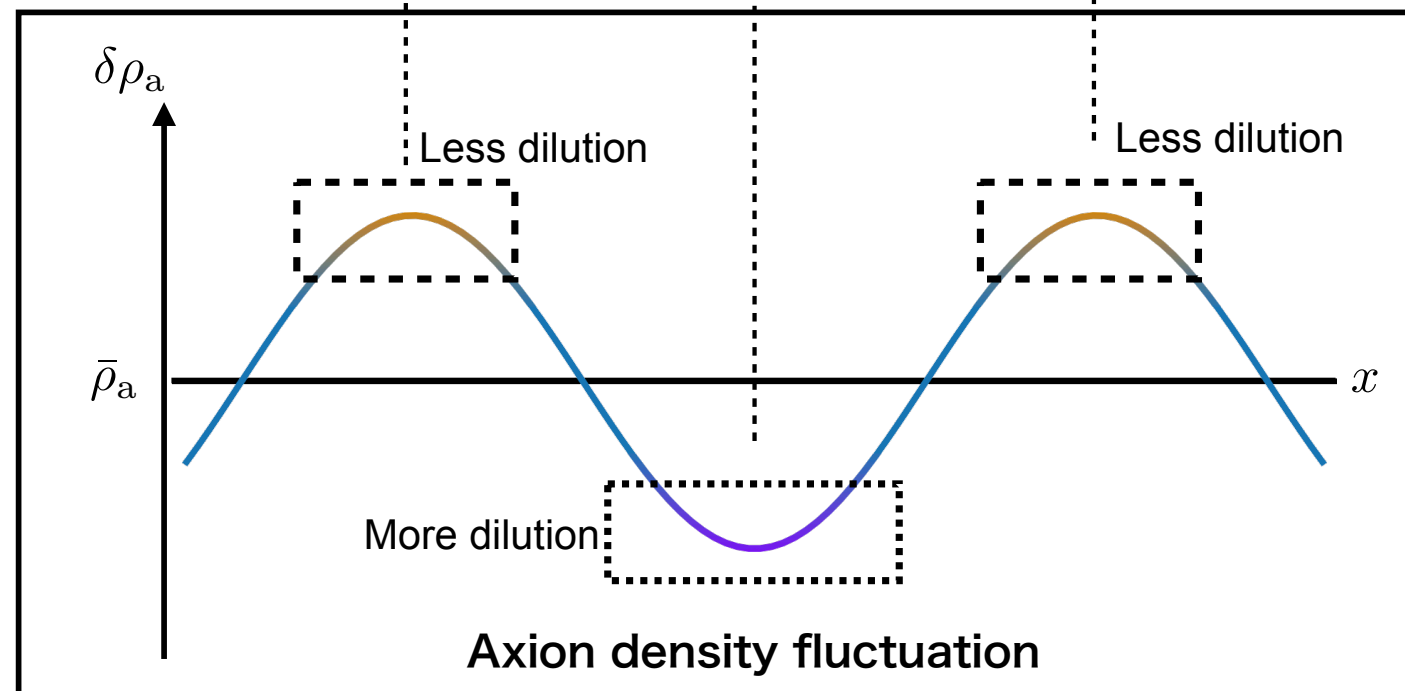
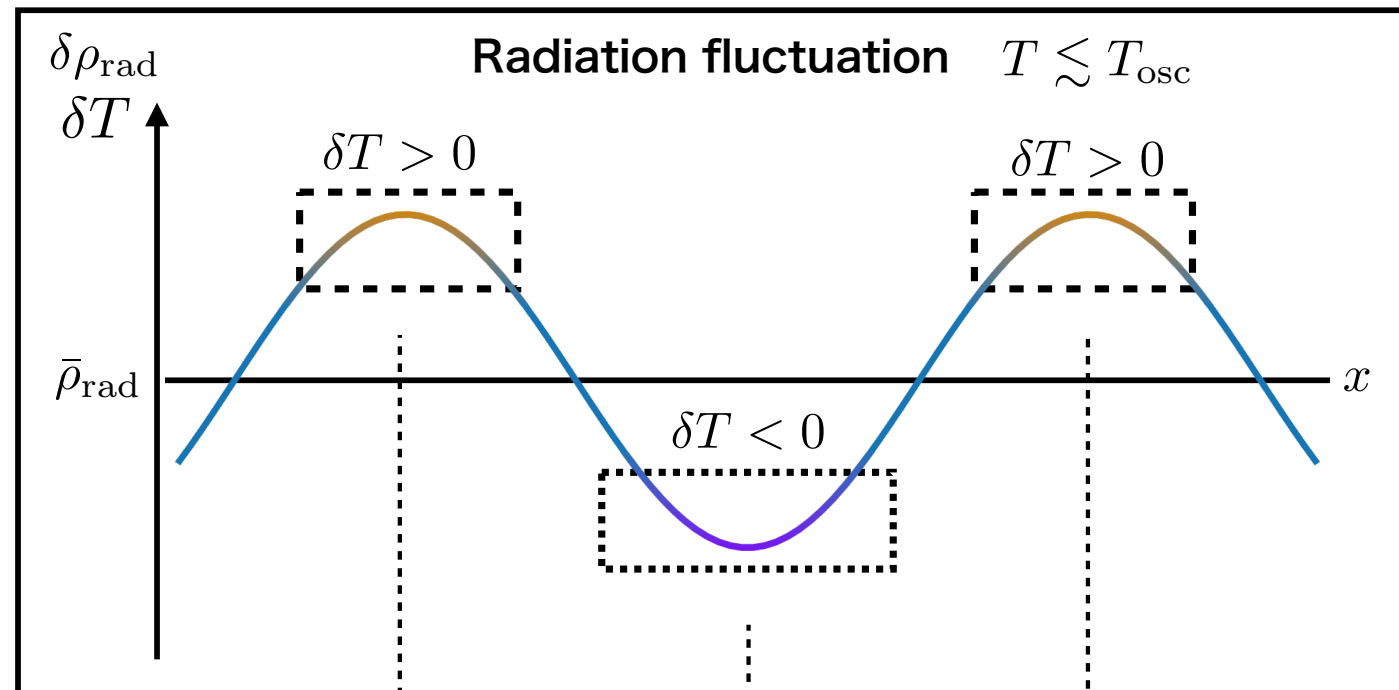


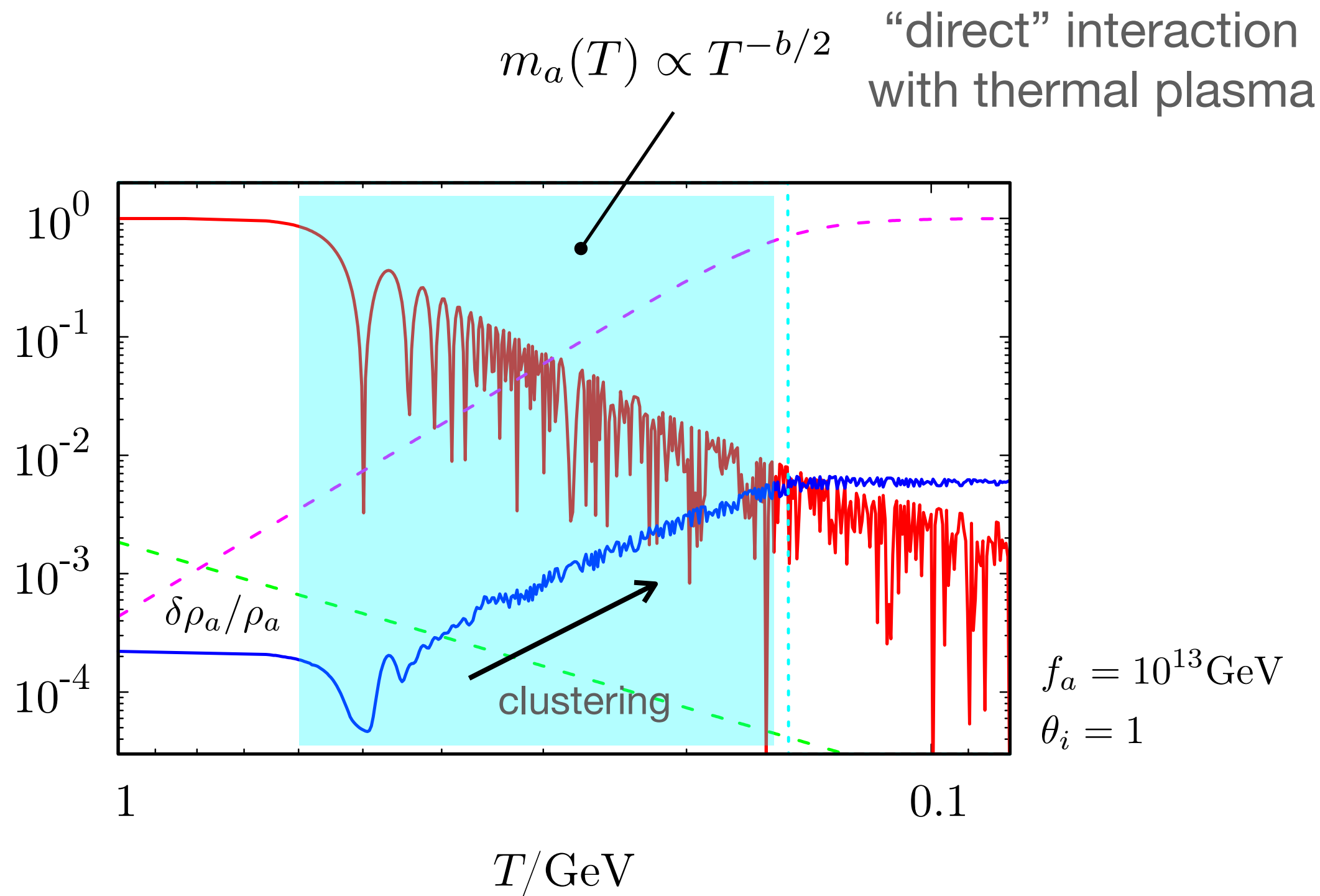
$$\phi'' + 2\mathcal{H}\phi' - (1 - 4\Phi)\nabla^2\phi + a^2 V_\phi + \underbrace{4\Phi'\phi'}_{\text{S1}} - \underbrace{2a^2\Phi V_\phi}_{\text{S2}} + \underbrace{a^2 V_{\phi T}\delta T}_{\text{S3}} = 0$$

S1 S2 S3
 “indirect” “direct”

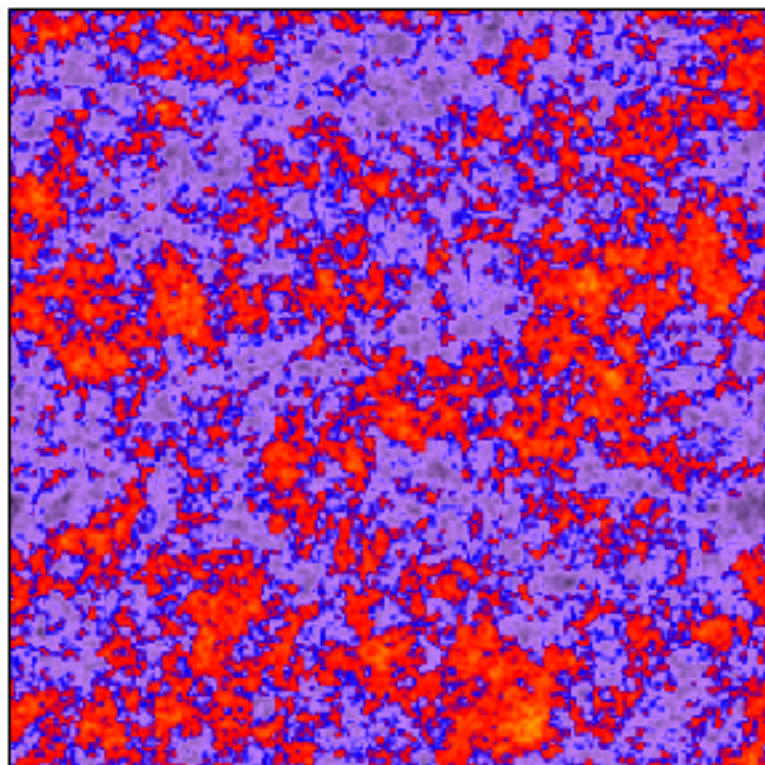
Clustering of axion due to the temperature fluctuation

NK, Kogai, Urakawa 2111.05785

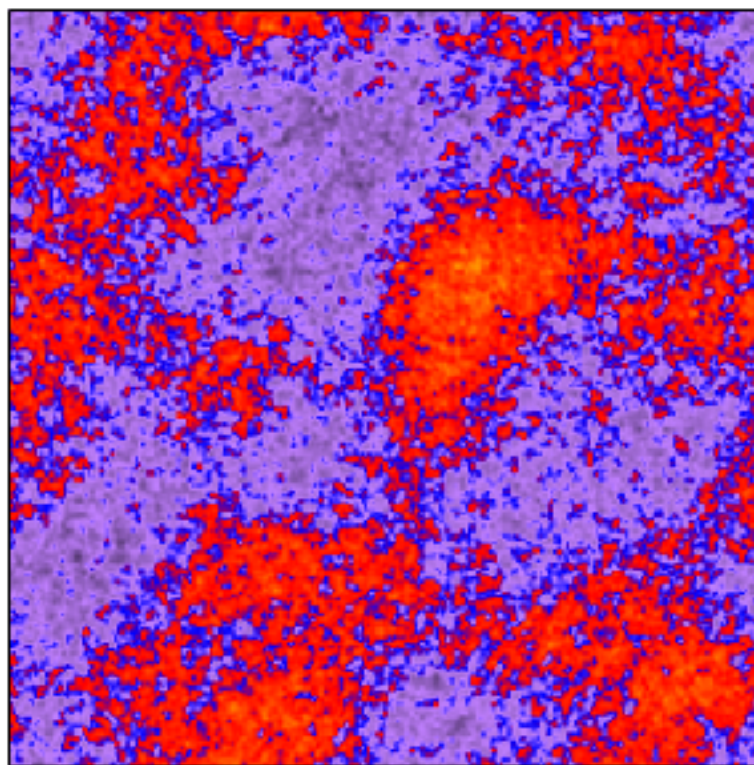




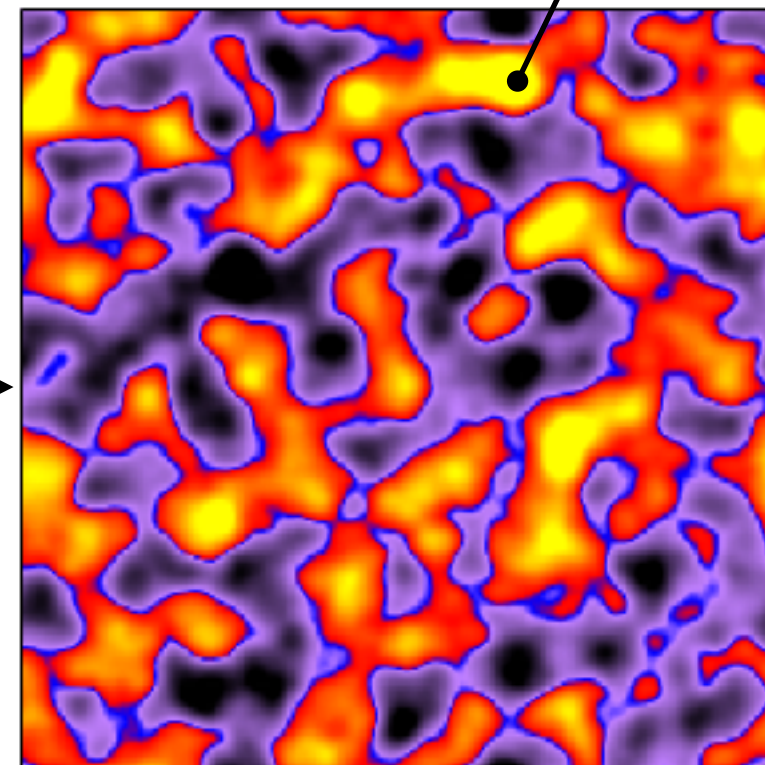
axion density contrast



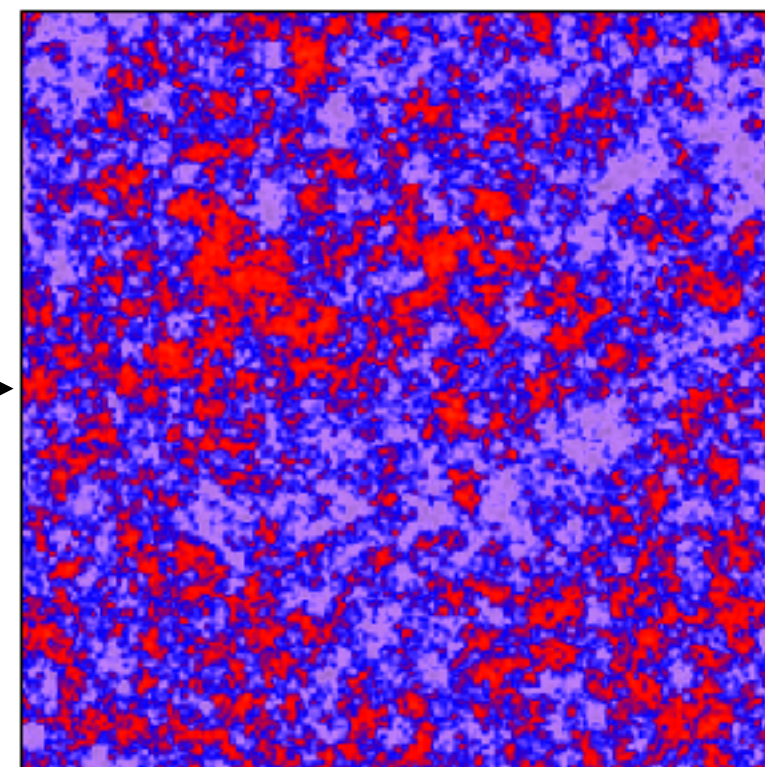
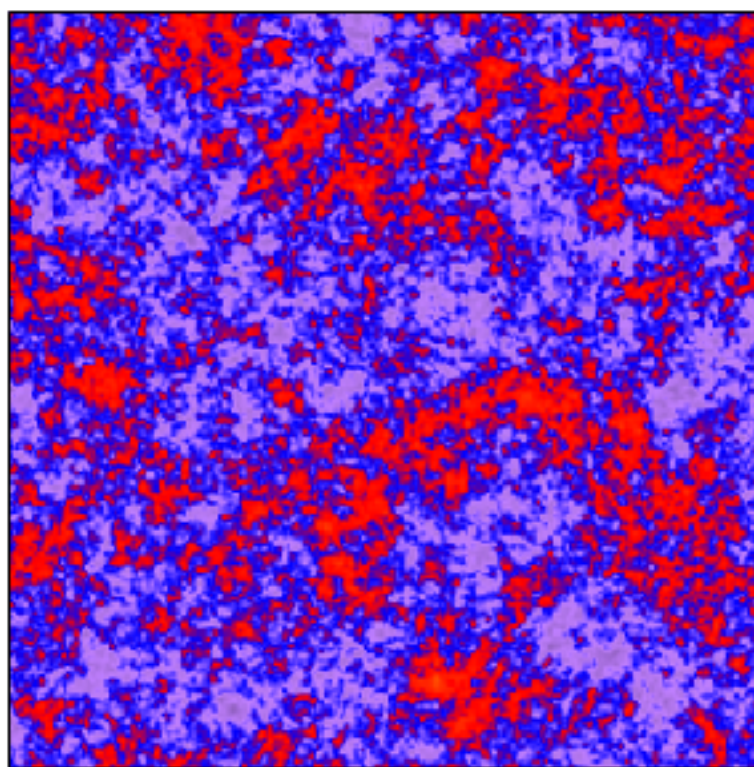
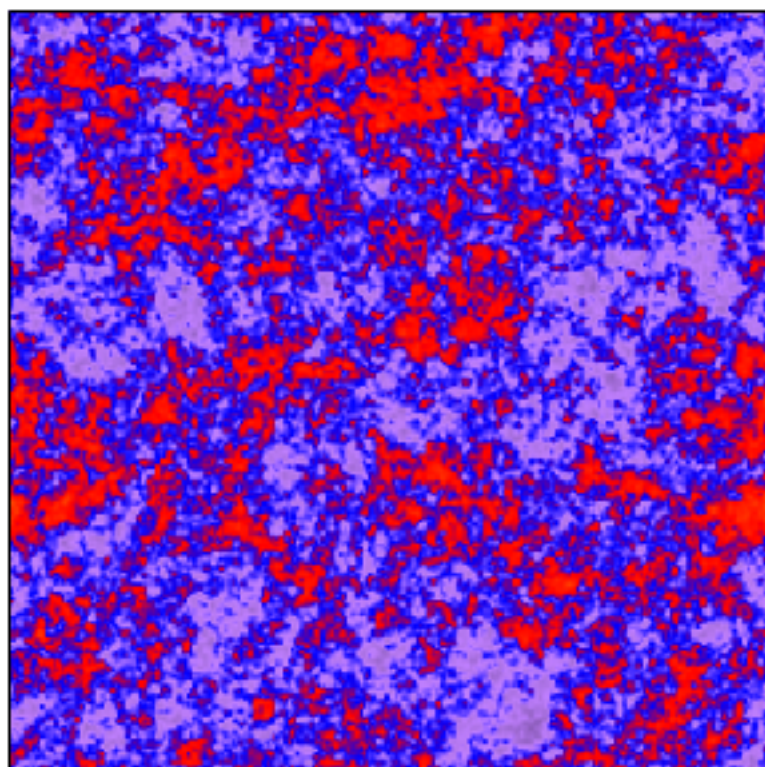
clustering occurs ...



x10 larger than δ_r



radiation density contrast



III. Linear analysis

Evolution of Fourier mode

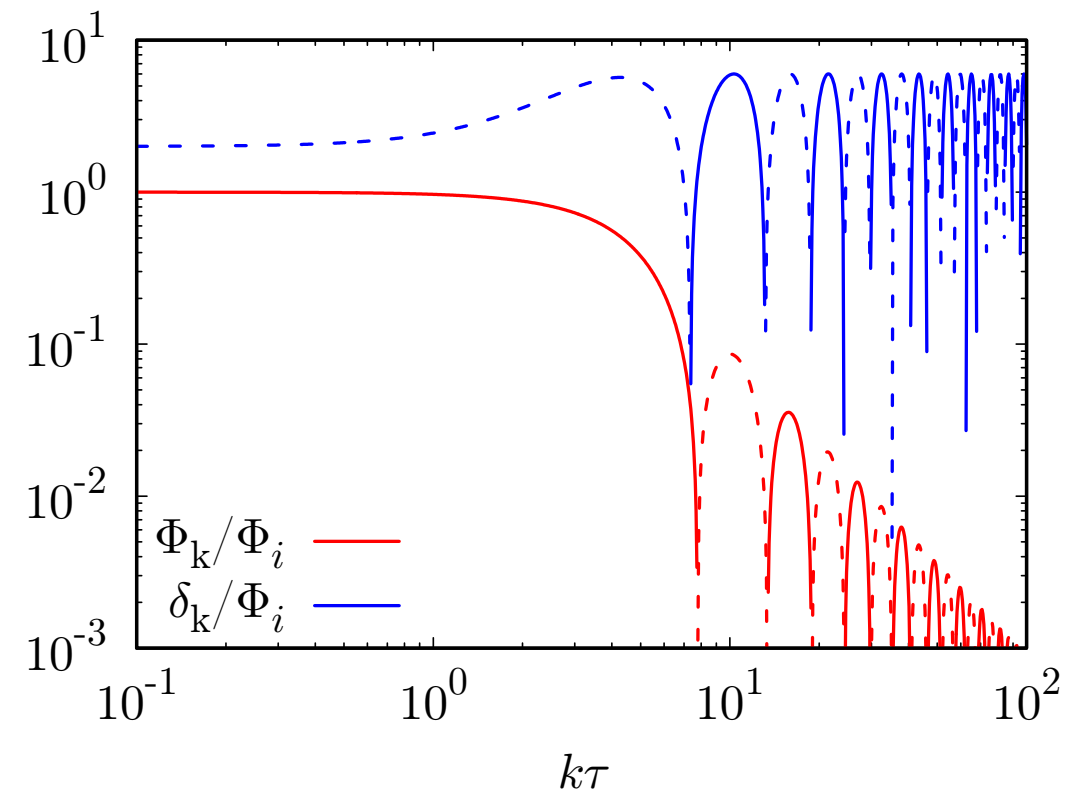
$$\delta\phi_{\mathbf{k}}'' + 2\mathcal{H}\delta\phi_{\mathbf{k}}' + 4\phi'\Phi_{\mathbf{k}}' + k^2\delta\phi_{\mathbf{k}} + a^2(V_{\phi\phi}\delta\phi_{\mathbf{k}} - 2V_{\phi}\Phi_{\mathbf{k}} + V_{\phi T}\delta T_{\mathbf{k}}) = 0$$

- radiation density fluctuation & scalar metric perturbation

$$\delta_{\mathbf{k}} = \frac{36\Phi_i}{(k\tau)^2} \left(\left(1 - \frac{(k\tau)^2}{3} \right) \frac{\sqrt{3}}{k\tau} \sin\left(\frac{k\tau}{\sqrt{3}}\right) - \left(1 - \frac{(k\tau)^2}{6} \right) \cos\left(\frac{k\tau}{\sqrt{3}}\right) \right) \left(\rightarrow \delta T_{\mathbf{k}} = \frac{T}{4}\delta_{\mathbf{k}} \right)$$

$$\Phi_{\mathbf{k}} = \frac{9\Phi_i}{(k\tau)^2} \left(\frac{\sqrt{3}}{k\tau} \sin\left(\frac{k\tau}{\sqrt{3}}\right) - \cos\left(\frac{k\tau}{\sqrt{3}}\right) \right)$$

(radiation dominated Universe)

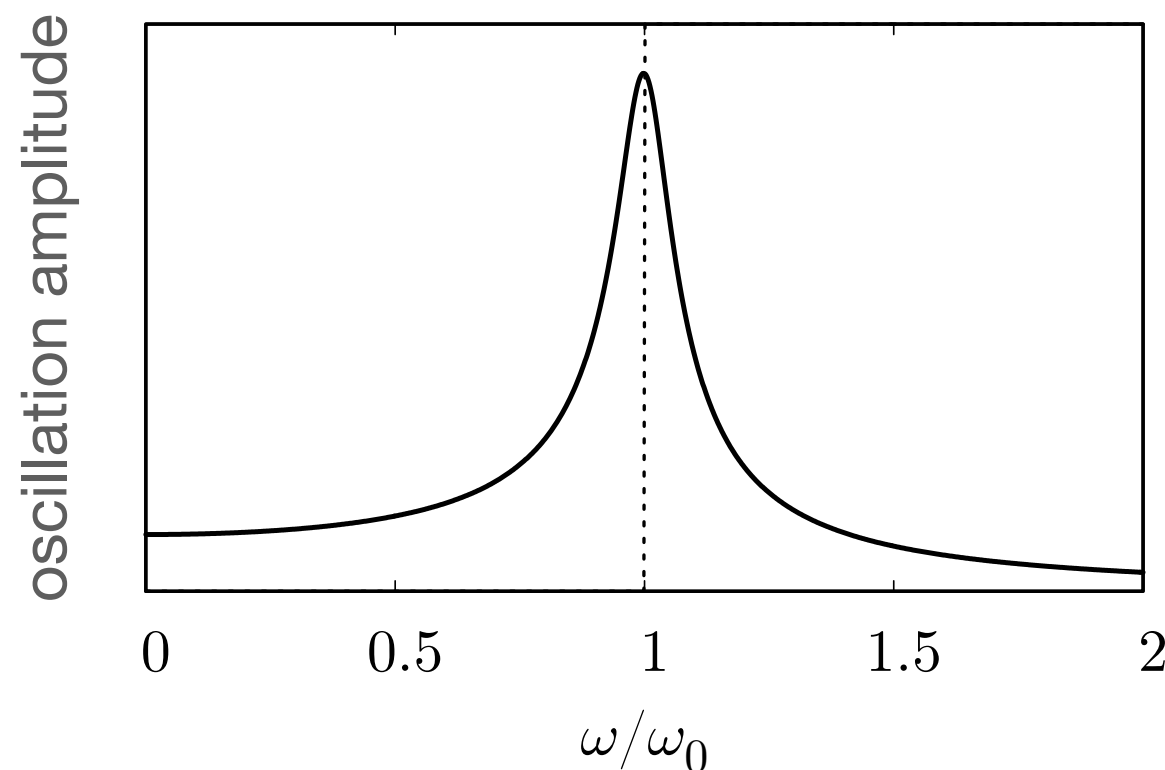


$$\text{EoM: } \delta\phi_{\mathbf{k}}'' + 2\mathcal{H}\delta\phi_{\mathbf{k}}' + (k^2 + a^2 m^2(T))\delta\phi_{\mathbf{k}} = -a^2 V_{\phi T} \delta T_{\mathbf{k}}$$

$\updownarrow$ analogy

Forced oscillation model: $\ddot{x} + 2\gamma\dot{x} + \omega_0^2 x = F_0 \sin(\omega t + \delta)$

$\longrightarrow x(t) = \frac{F_0}{\sqrt{(\omega^2 - \omega_0^2)^2 + (2\gamma\omega)^2}} \sin(\omega t + \delta)$
(particular solution)



$$\text{EoM: } \delta\phi_{\mathbf{k}}'' + 2\mathcal{H}\delta\phi_{\mathbf{k}}' + (k^2 + a^2 m^2(T))\delta\phi_{\mathbf{k}} = -a^2 V_{\phi T} \delta T_{\mathbf{k}}$$



... analogy with forced-oscillation system ...

$$\delta\phi_{\mathbf{k}} \rightarrow x \quad (\text{position})$$

$$\mathcal{H} \rightarrow \gamma \quad (\text{damping term})$$

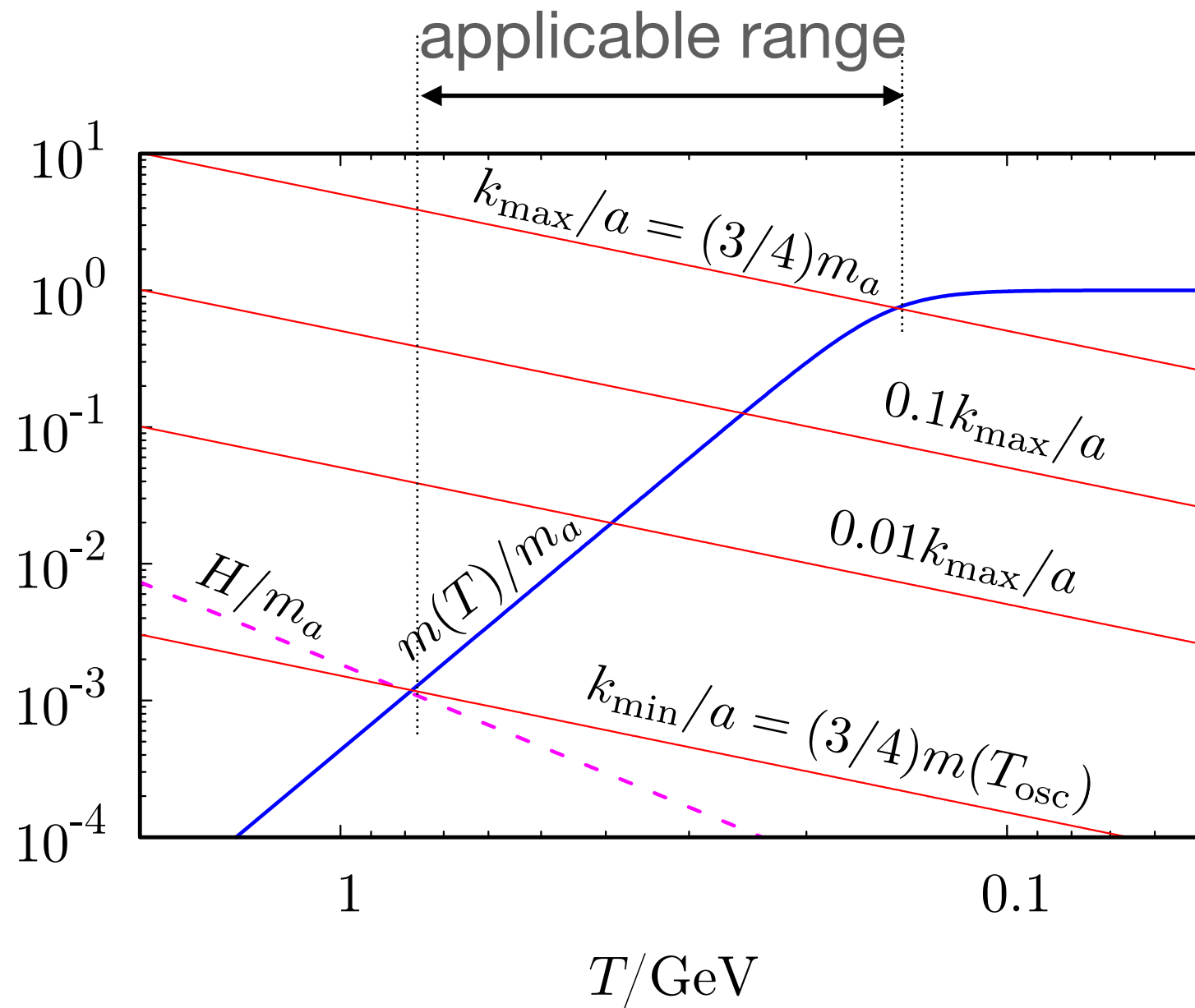
$$k^2 + a^2 m^2(T) \rightarrow \omega_0^2 \quad (\text{eigen frequency})$$

$$\text{r.h.s} = \underbrace{ba^2 m^2(T) \phi_0 \delta T_{\mathbf{k}} / T}_{\text{(driving force)}} \rightarrow F_0 \sin(\omega t - \delta)$$

$$\propto \cos \left[\left(\frac{am(T)}{2} \pm k \right) \tau + \alpha \right]$$

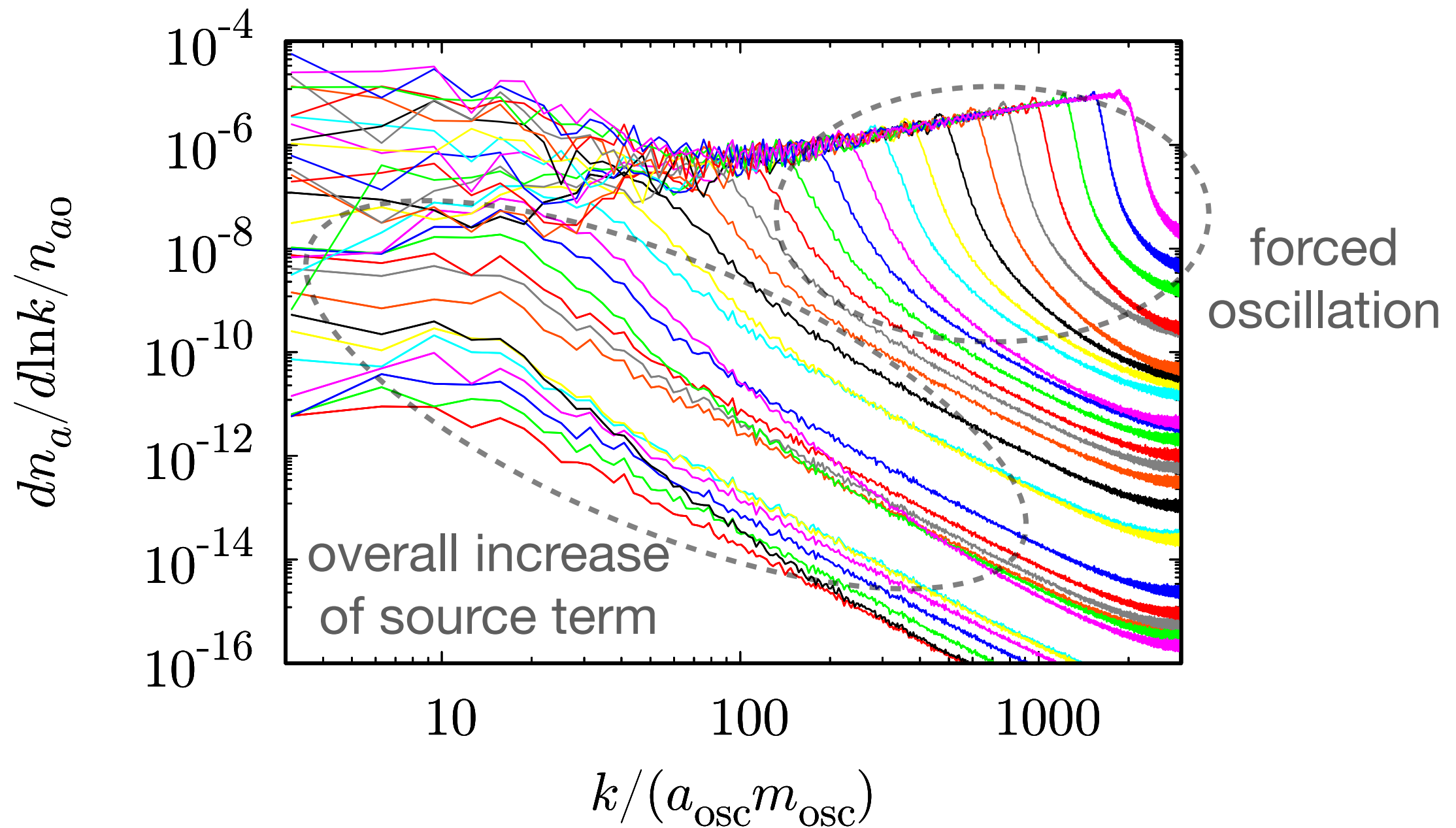
resonance condition : $\omega = \omega_0 \rightarrow \frac{k}{a} = \frac{3}{4}m(T)$

resonance condition : $\frac{k}{a} = \frac{3}{4}m(T)$

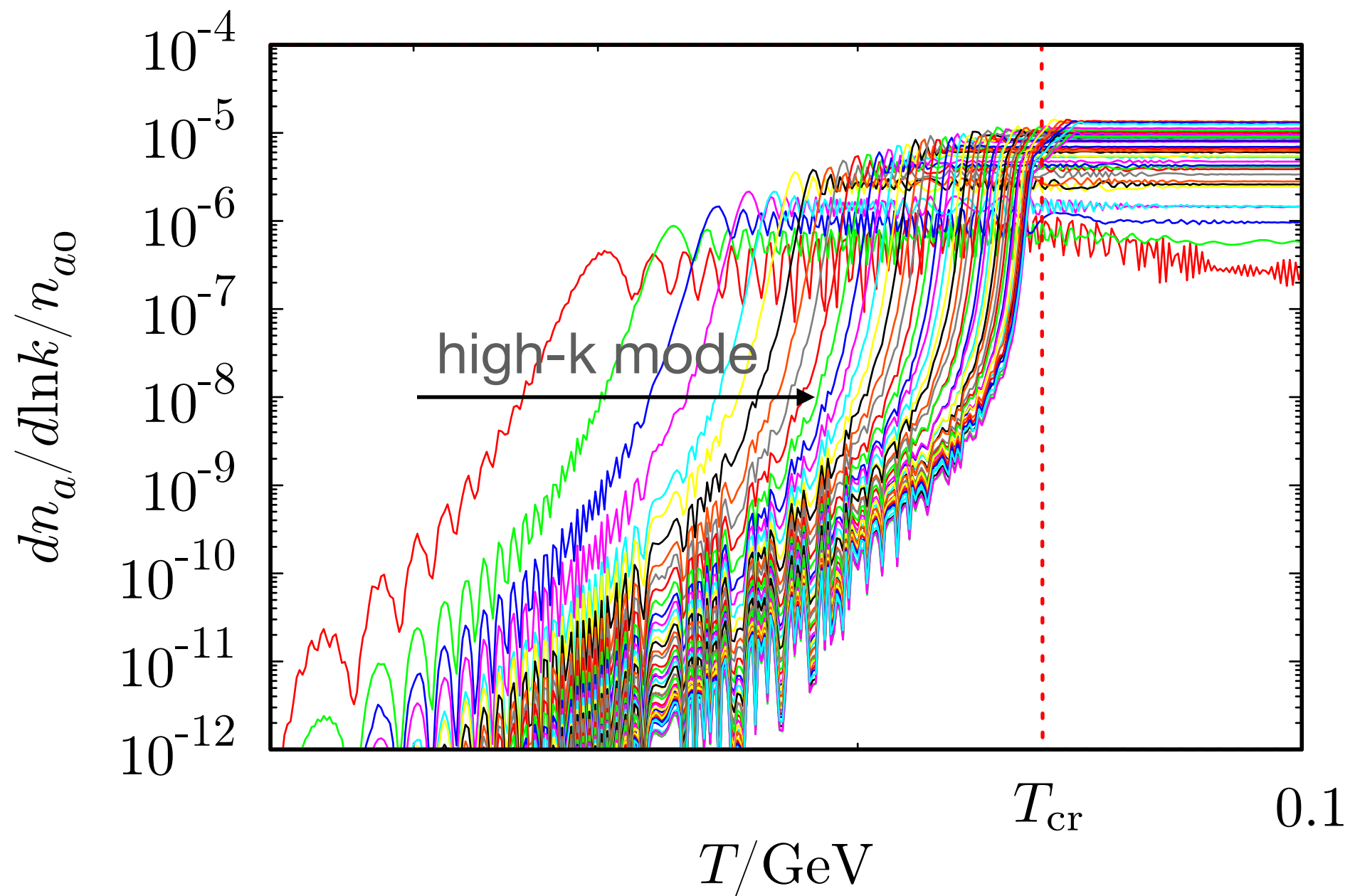


Resonance condition is met from low-k to high-k modes

Time evolution of the spectrum (number density)

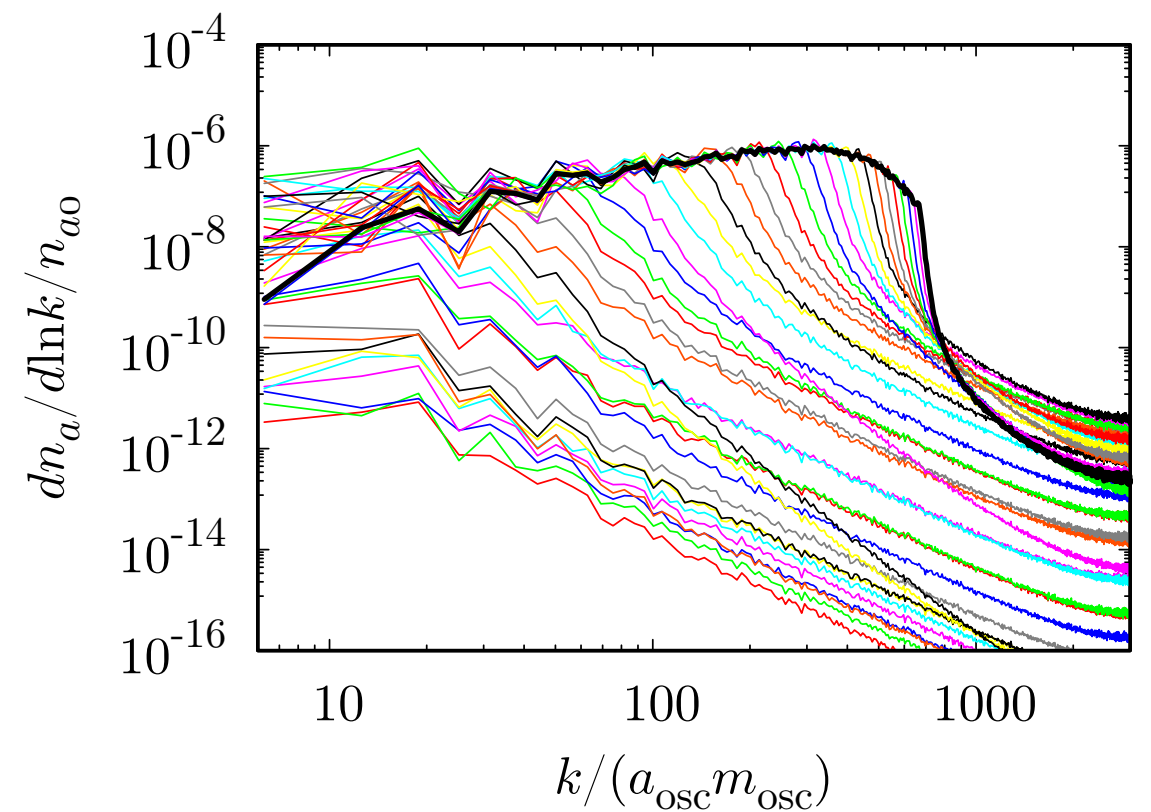
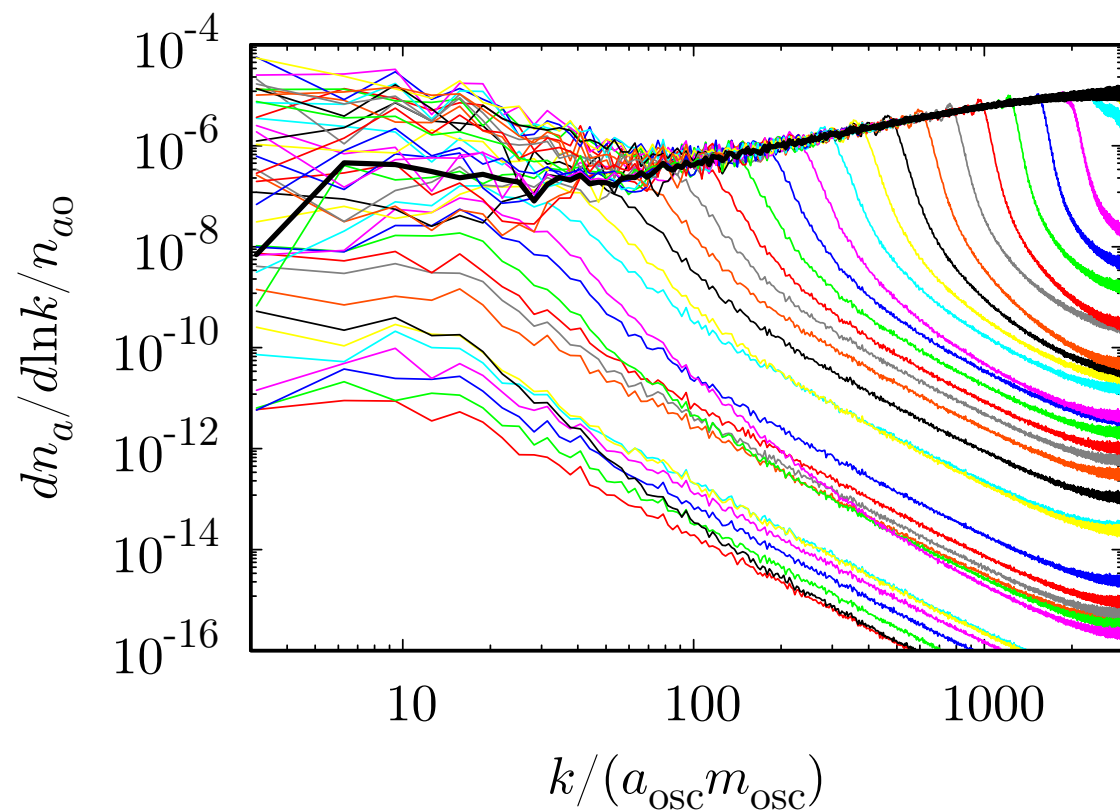
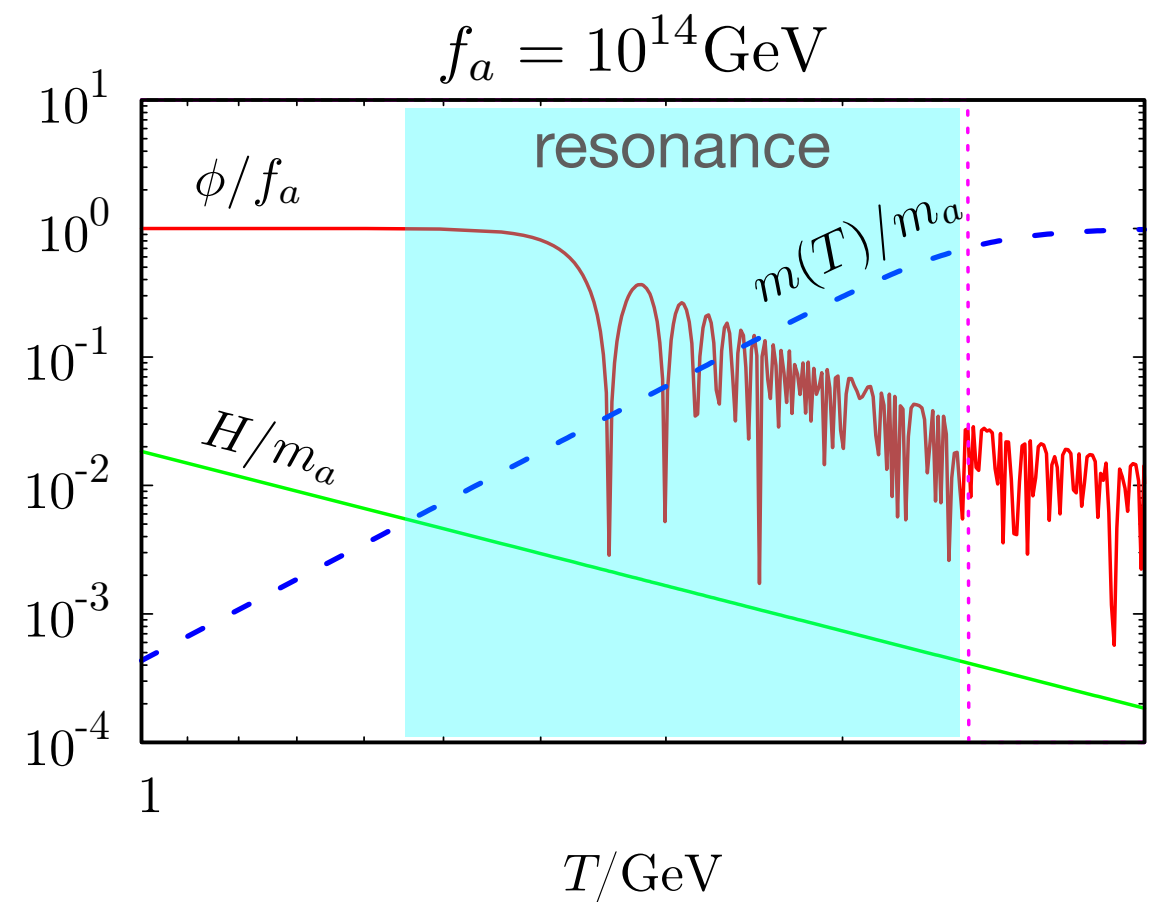
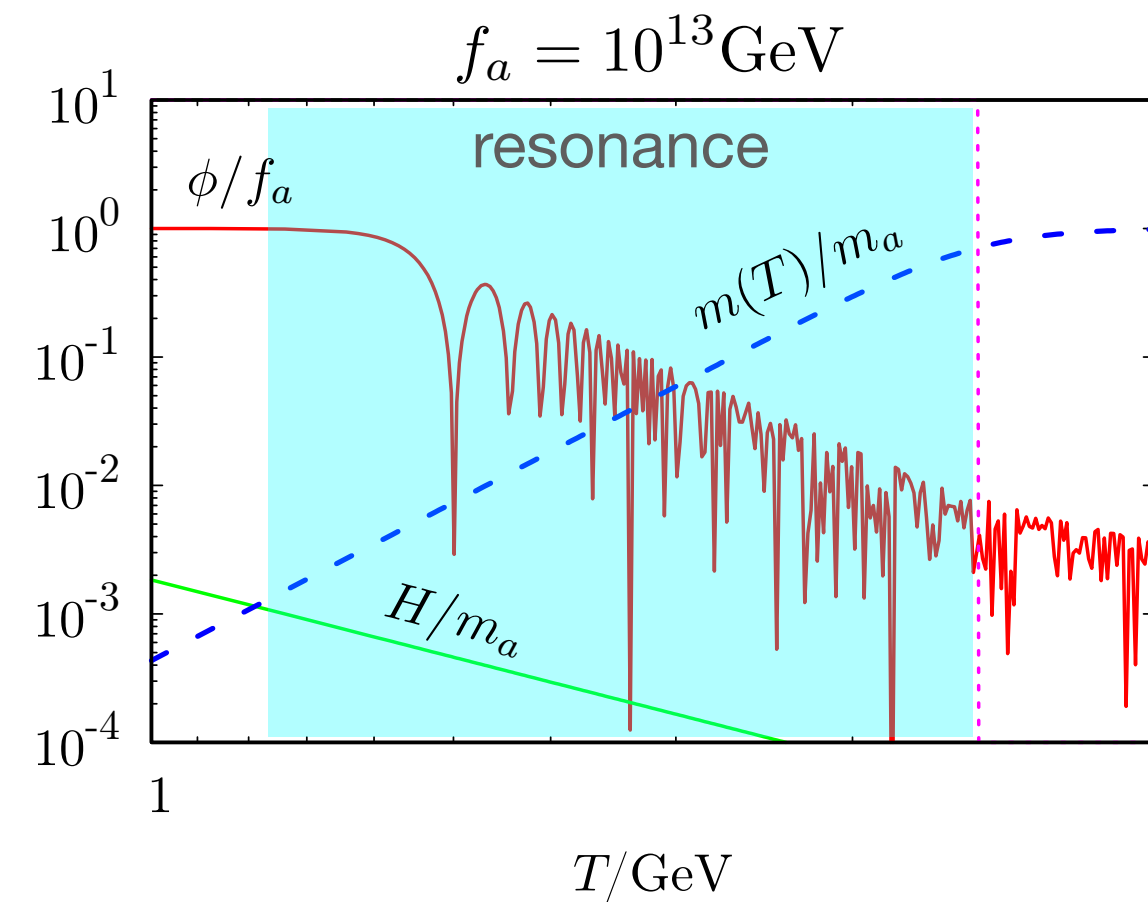


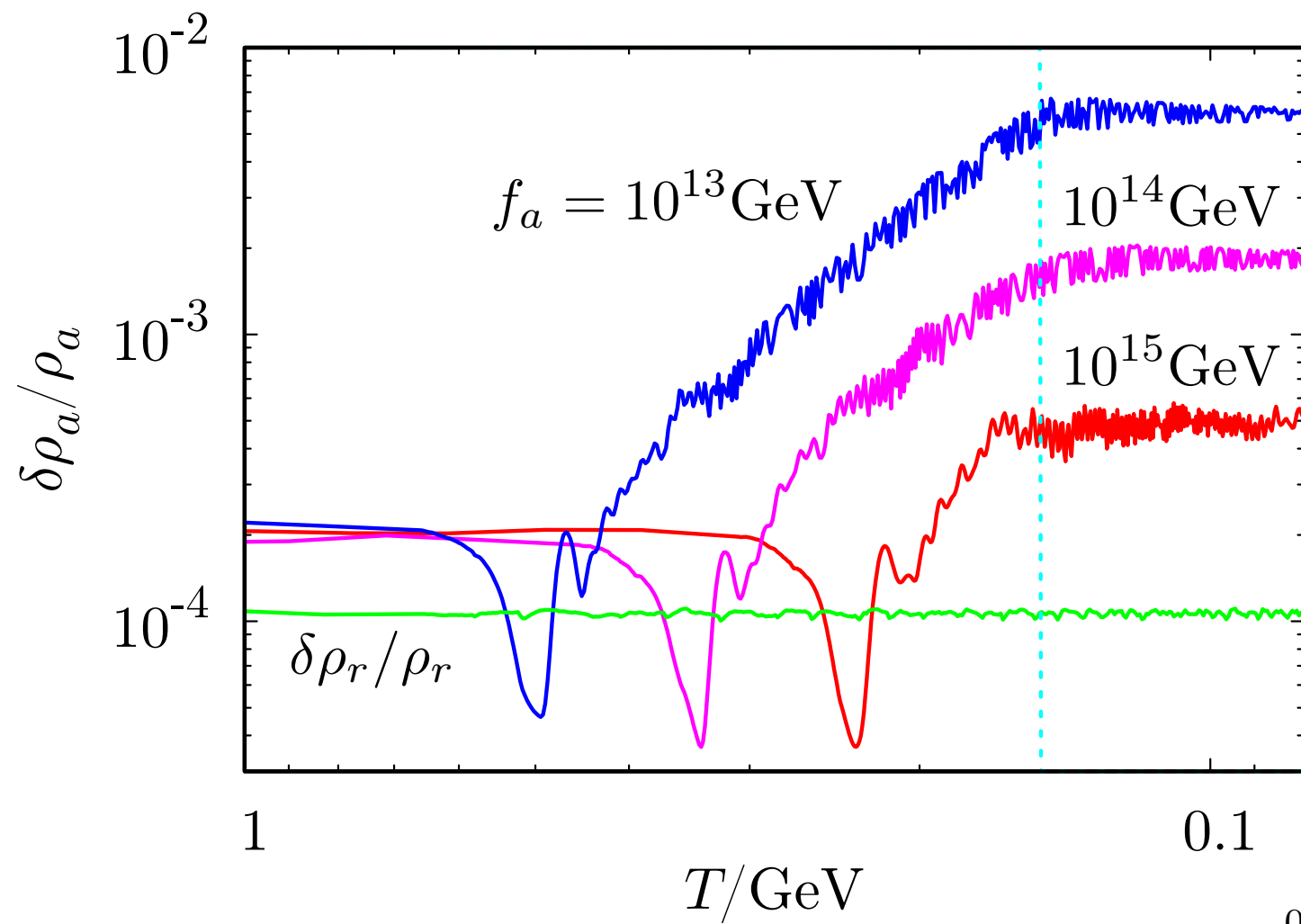
Time evolution of mode functions



Amplification ends at $T=T_{\text{cr}}$

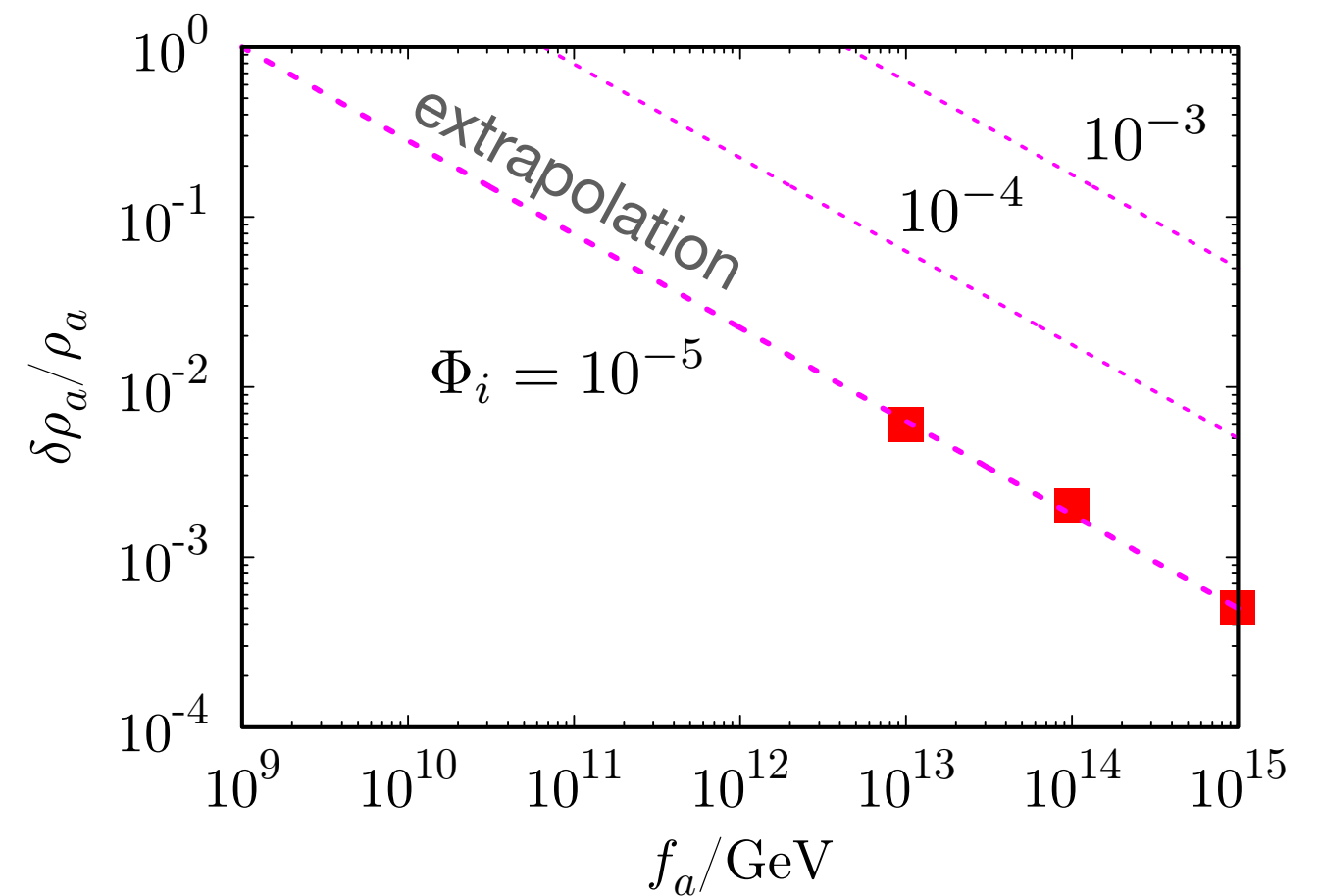
Dependence on the decay constant



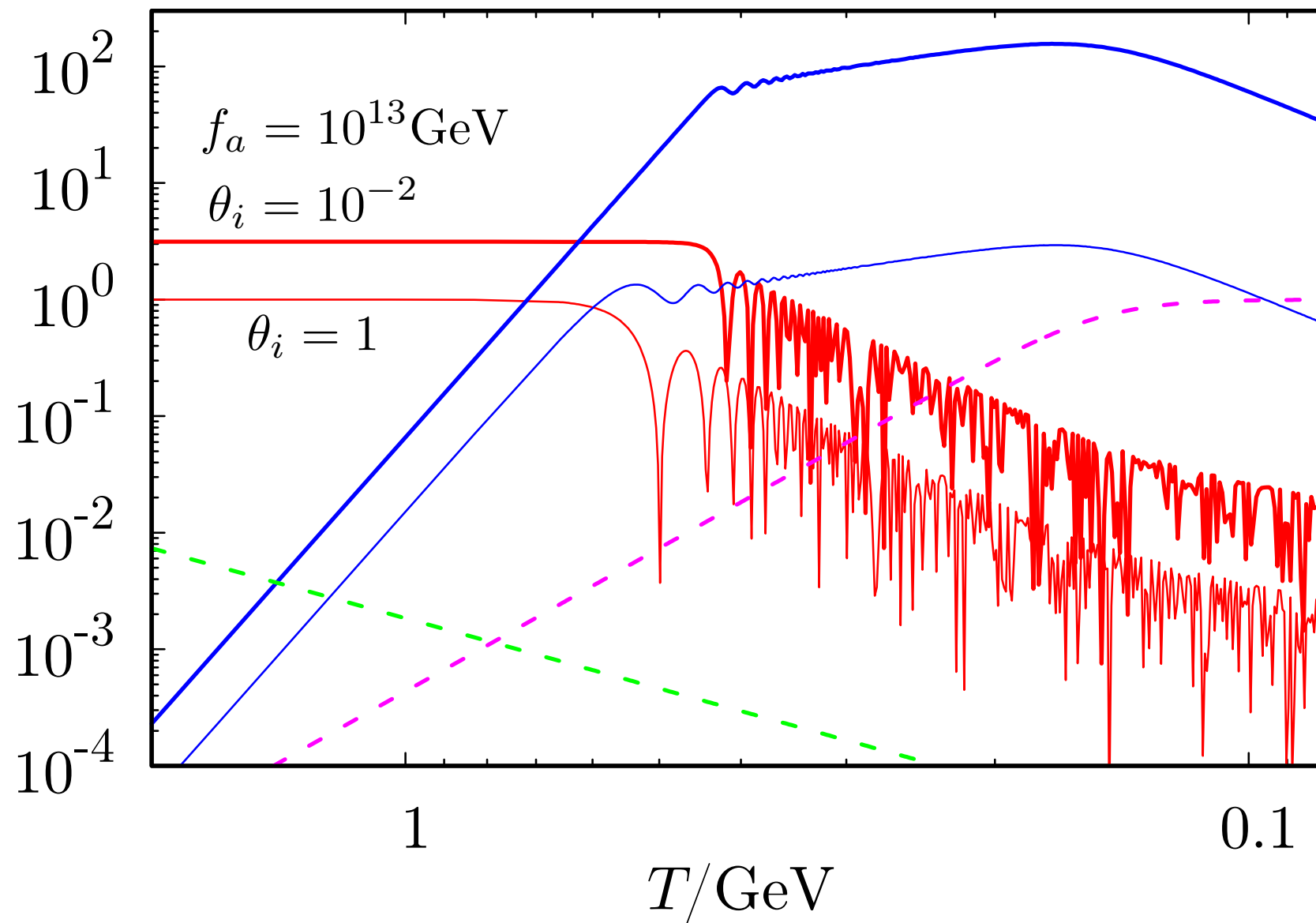
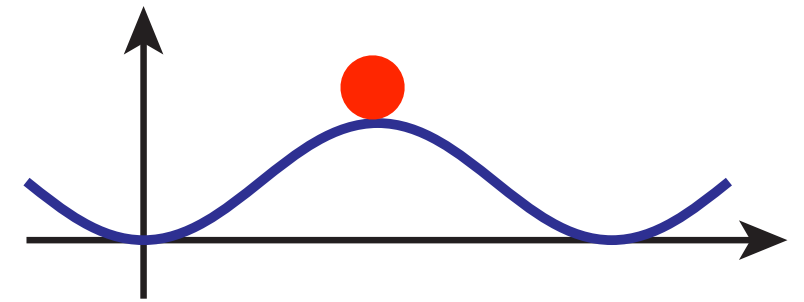


<— enhancement of axion density contrast

$\Phi_i \sim 10^{-3}$
 $\rightarrow \text{O}(1)$ density fluctuation



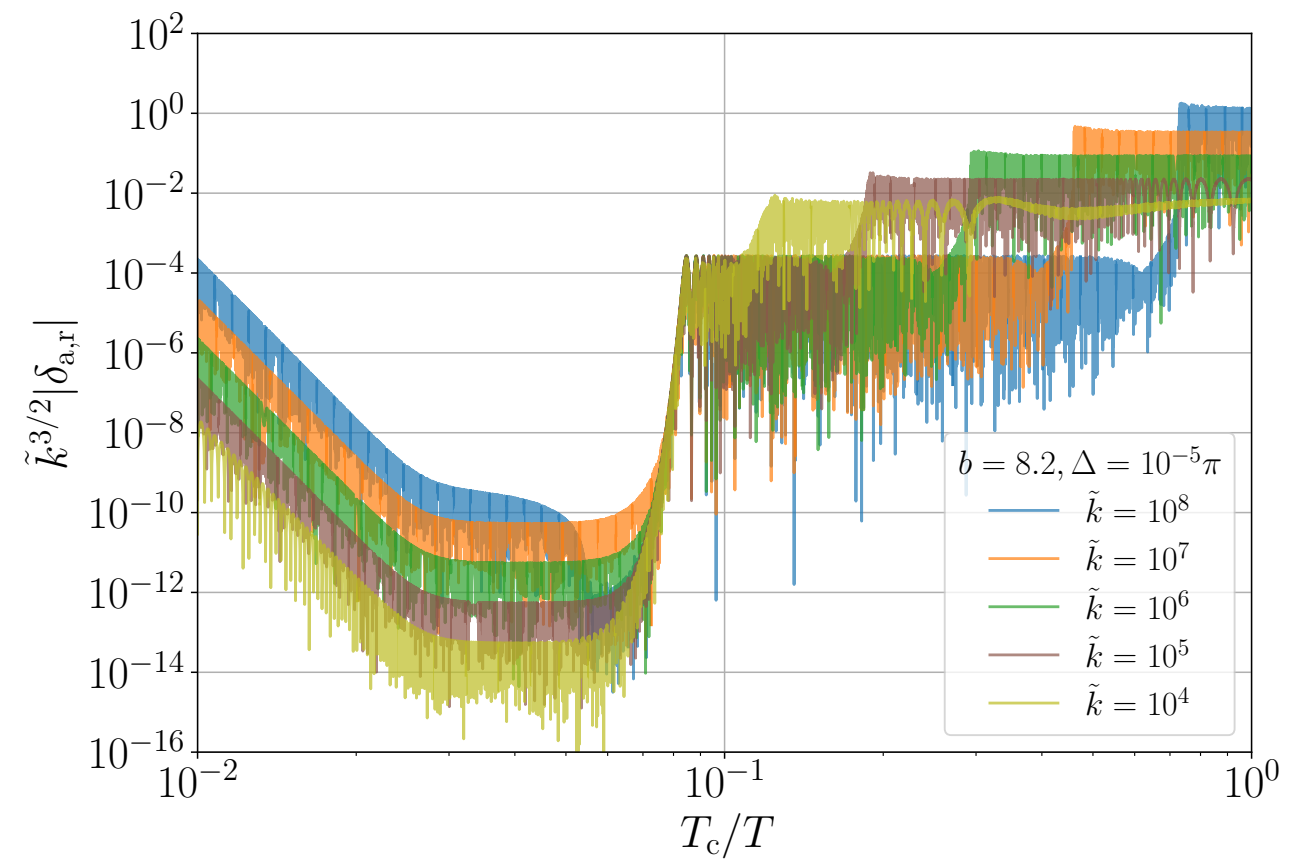
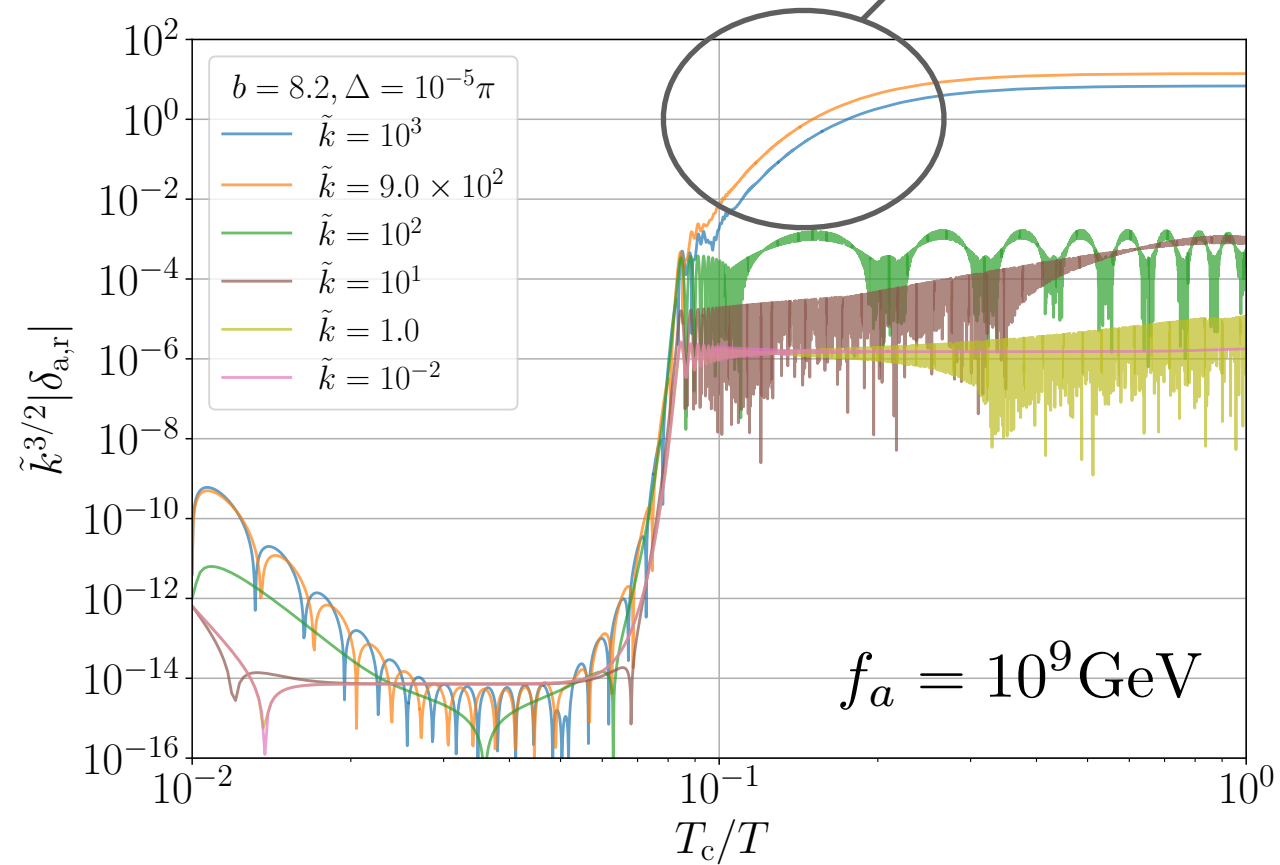
Fine-tuned initial misalignment (hilltop)



- delayed onset of oscillation $\rightarrow$ less Hubble friction
- more efficient self-interaction $\rightarrow$ resonance instability

resonant instability due to self-interaction

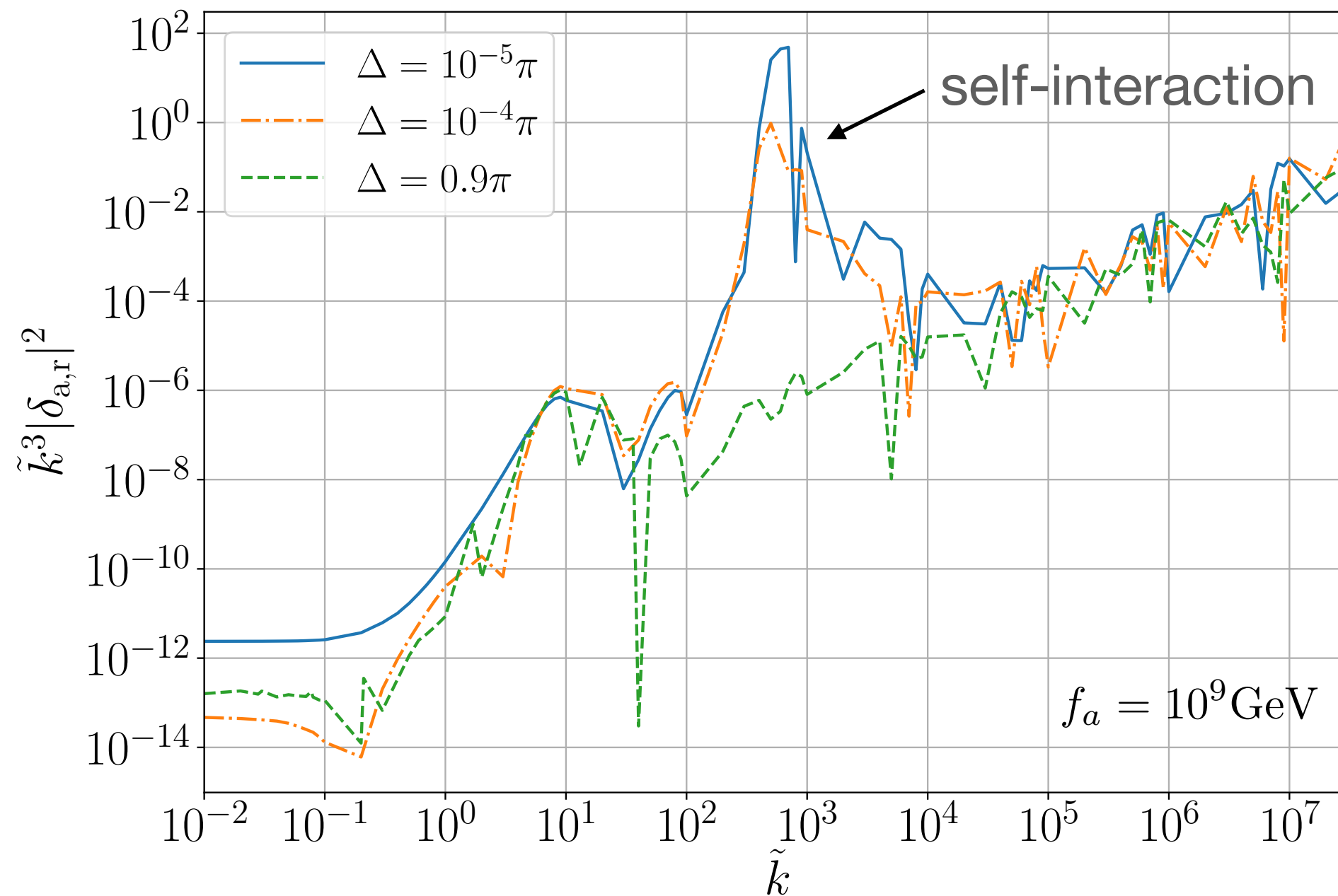
→ O(1) density fluctuation



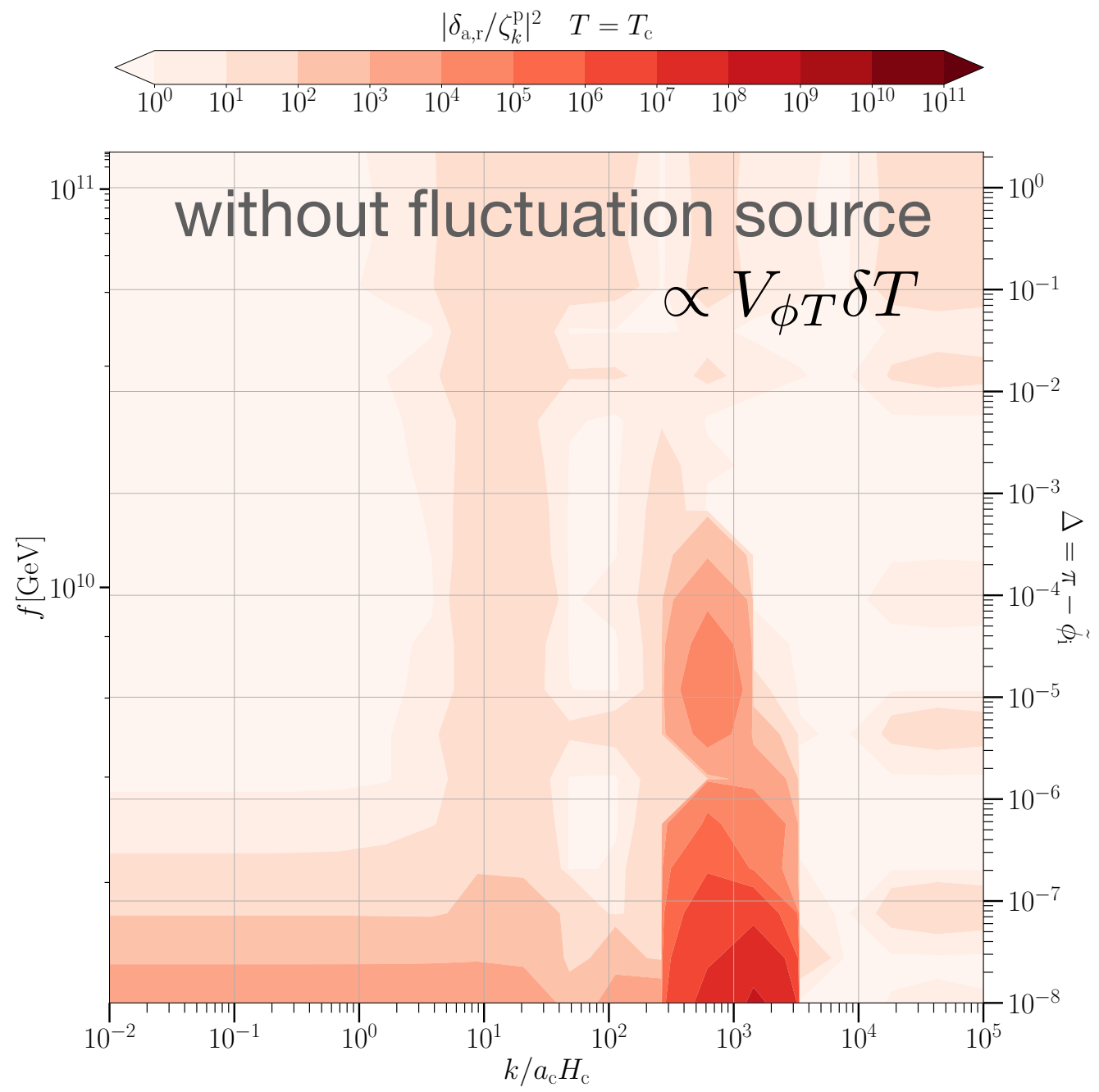
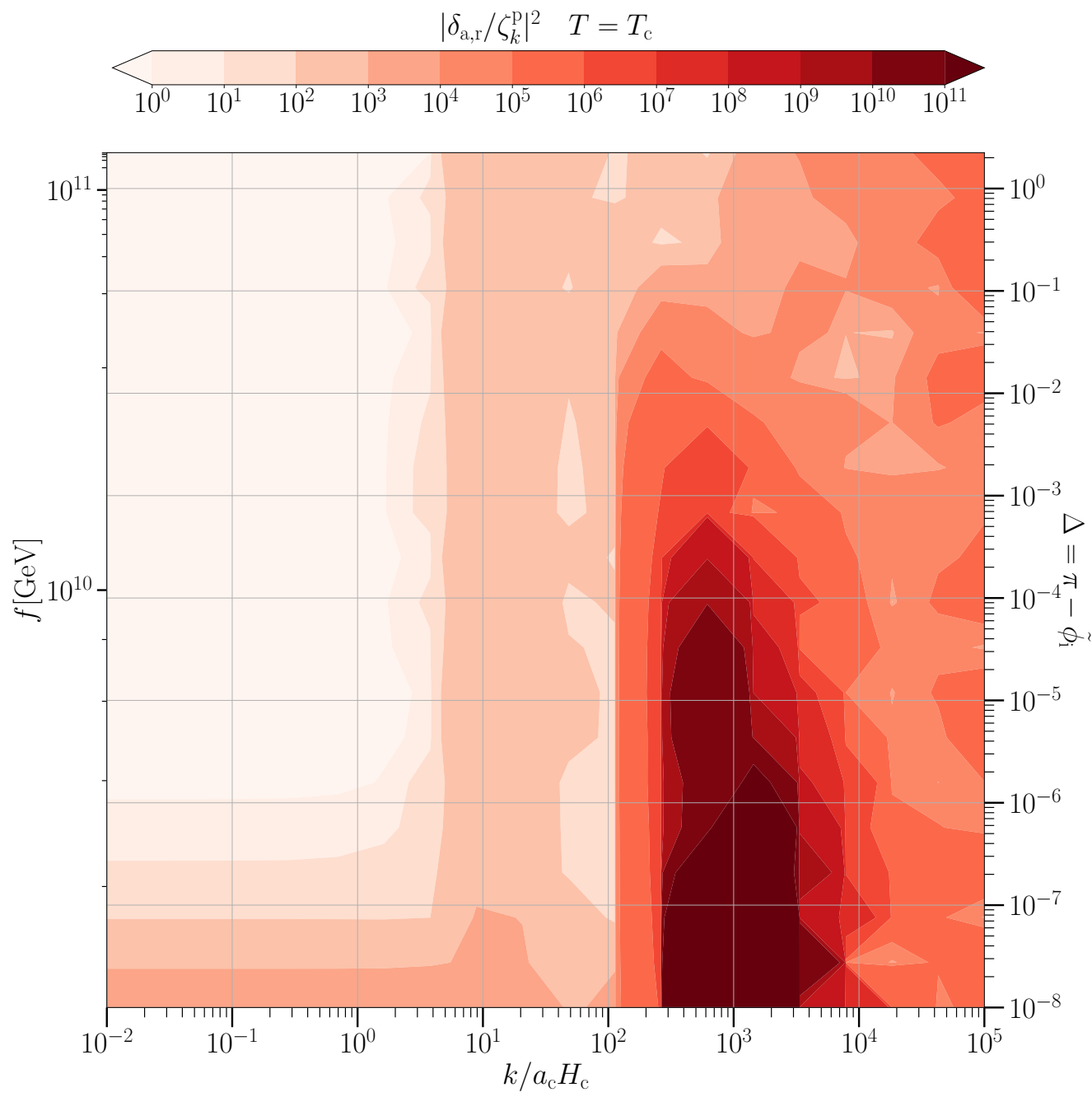
$$\Delta = \pi - \theta_i, \quad \tilde{k} = \frac{k}{a(T_c)H(T_c)}$$

Resultant spectrum

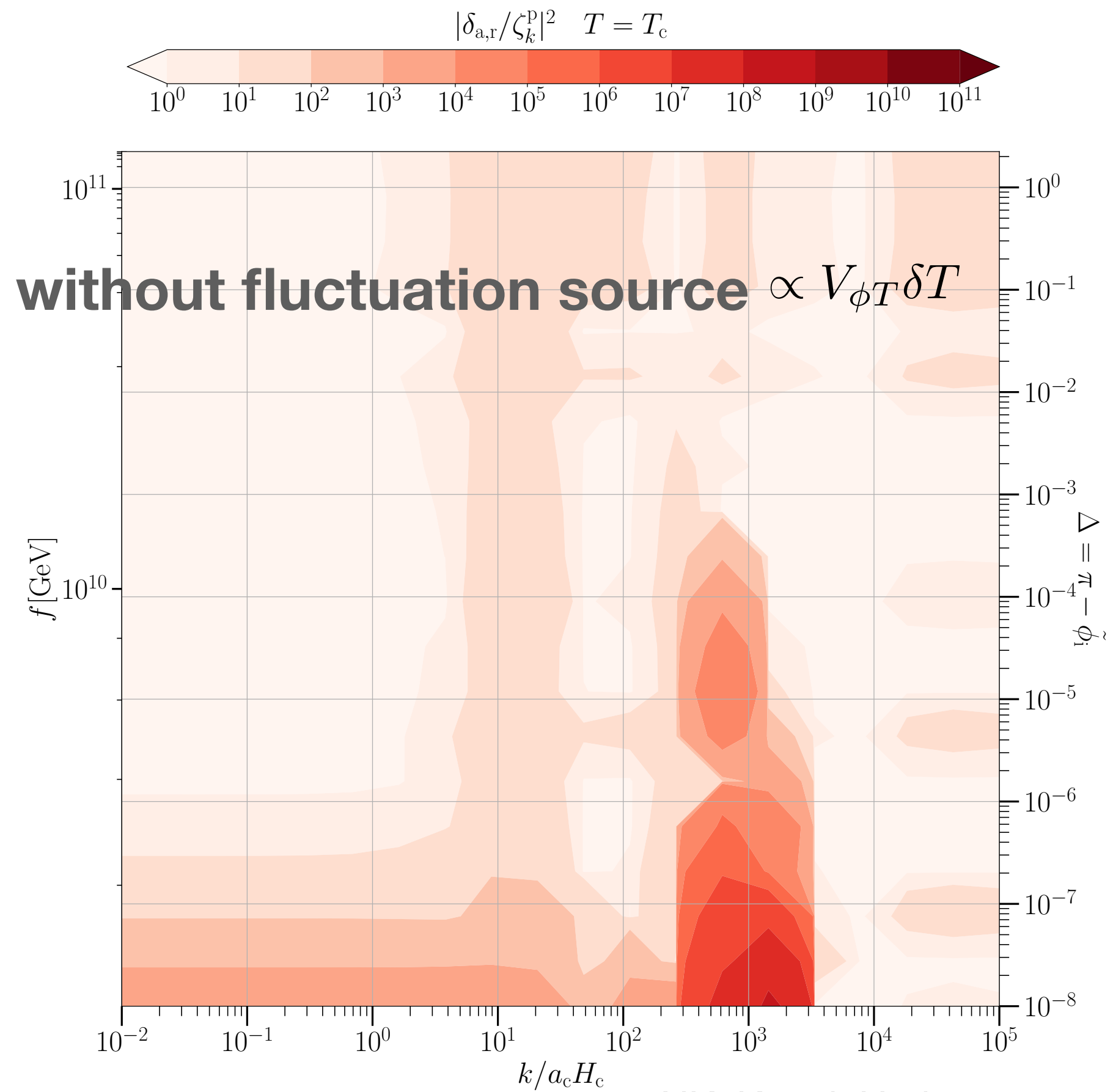
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$$\Delta = \pi - \theta_i, \quad \tilde{k} = \frac{k}{a(T_c)H(T_c)}$$



NK, Kogai, Urakawa 2111.05785



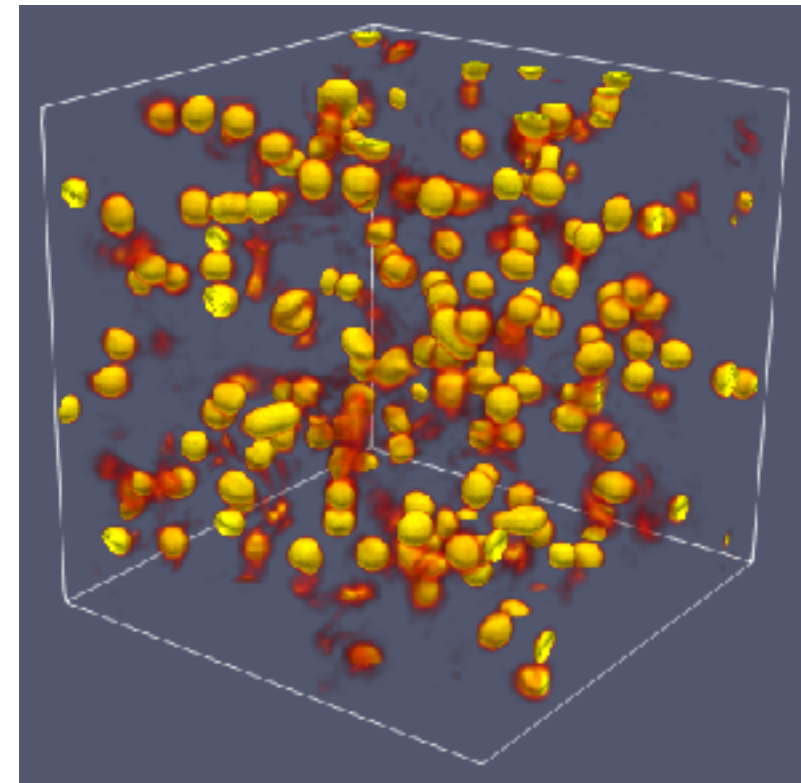
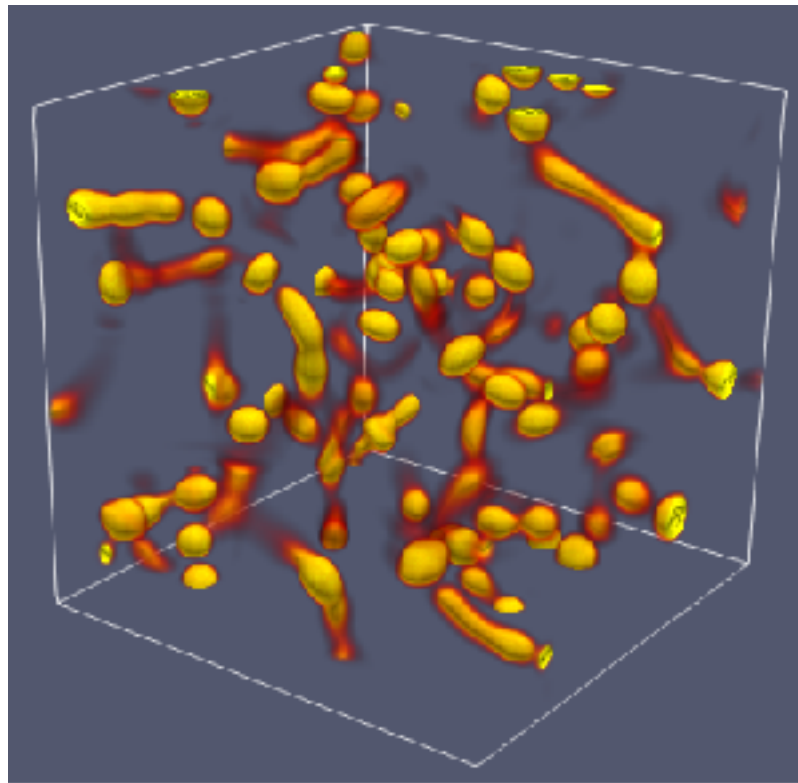
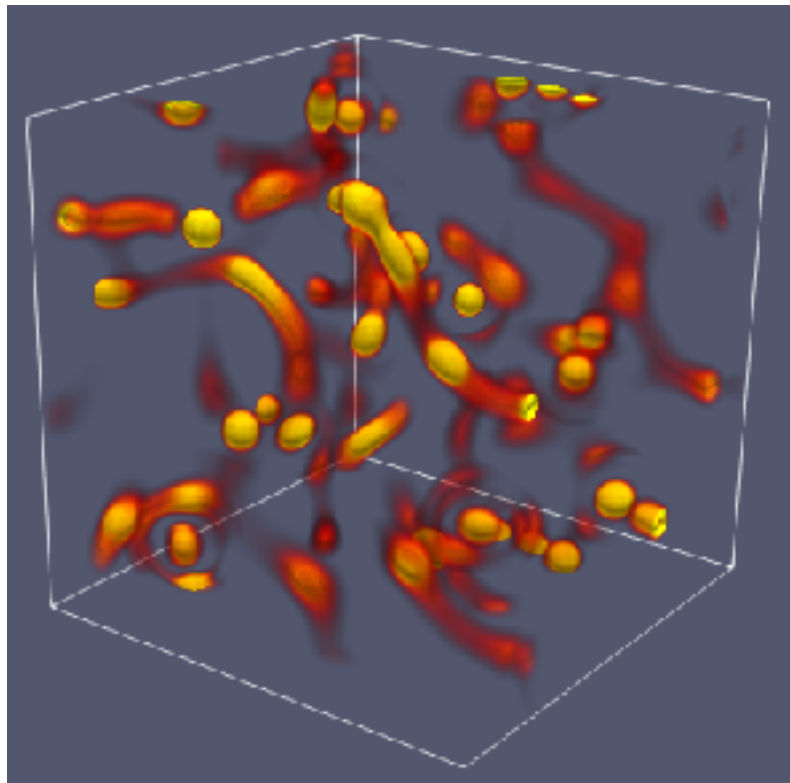
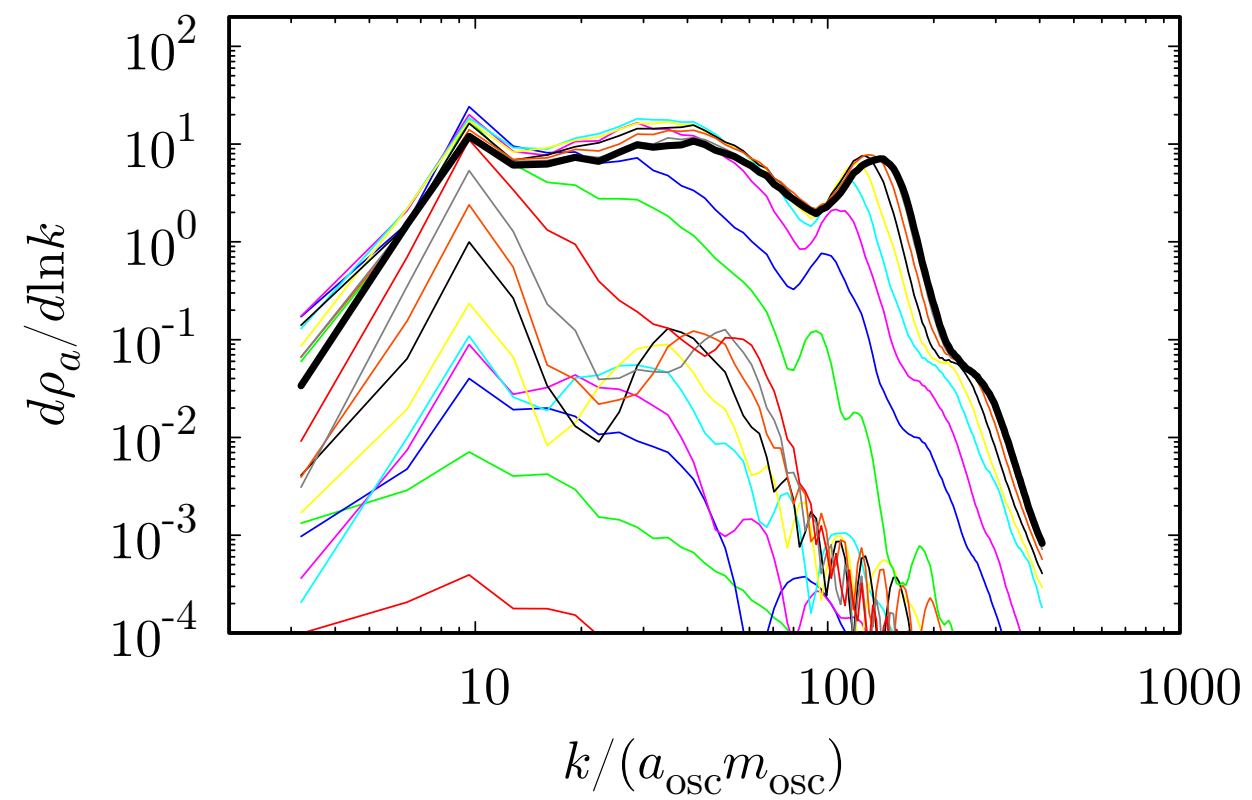
$O(1)$ fluctuation



nonlinear analysis

- nonlinear power spectrum
- oscillon formation / decay

Nonlinear simulation (preliminary)



Summary

- Microlensing can be a powerful tool for QCD axion search
 - > possibility to search cosmological imprints of QCD axion

Q. Any path for axion clump formation in pre-inflationary scenario?

- Adiabatic fluctuations can enhance the axion fluctuations
in general / model-independent way

(through the direct interaction with thermal plasma)

& it can (probably) modify the mass function of axion minicluster

- nonlinear analysis is necessary (in progress)

Initial fluctuation and gauge issue

gauge-invariant curvature perturbation: $-\zeta = -\Psi + \frac{H}{\dot{\rho}}\delta\rho$

gauge-invariant scalar field fluctuation: $\delta\phi_I = \delta\phi - \frac{\dot{\phi}}{\dot{\rho}}\delta\rho$
(isocurvature fluctuation)

- Newtonian gauge
- superhorizon scale
- radiation dominant
- no anisotropic stress



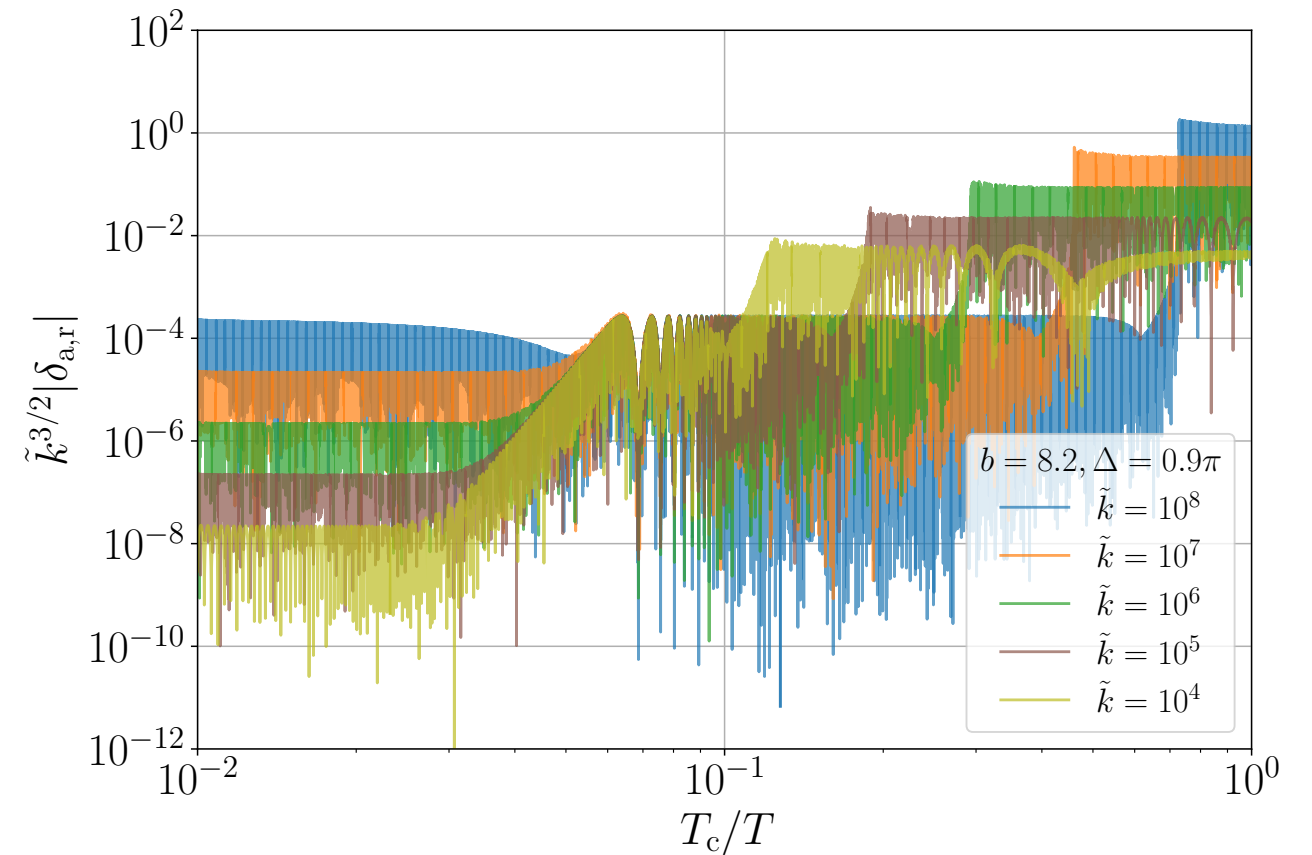
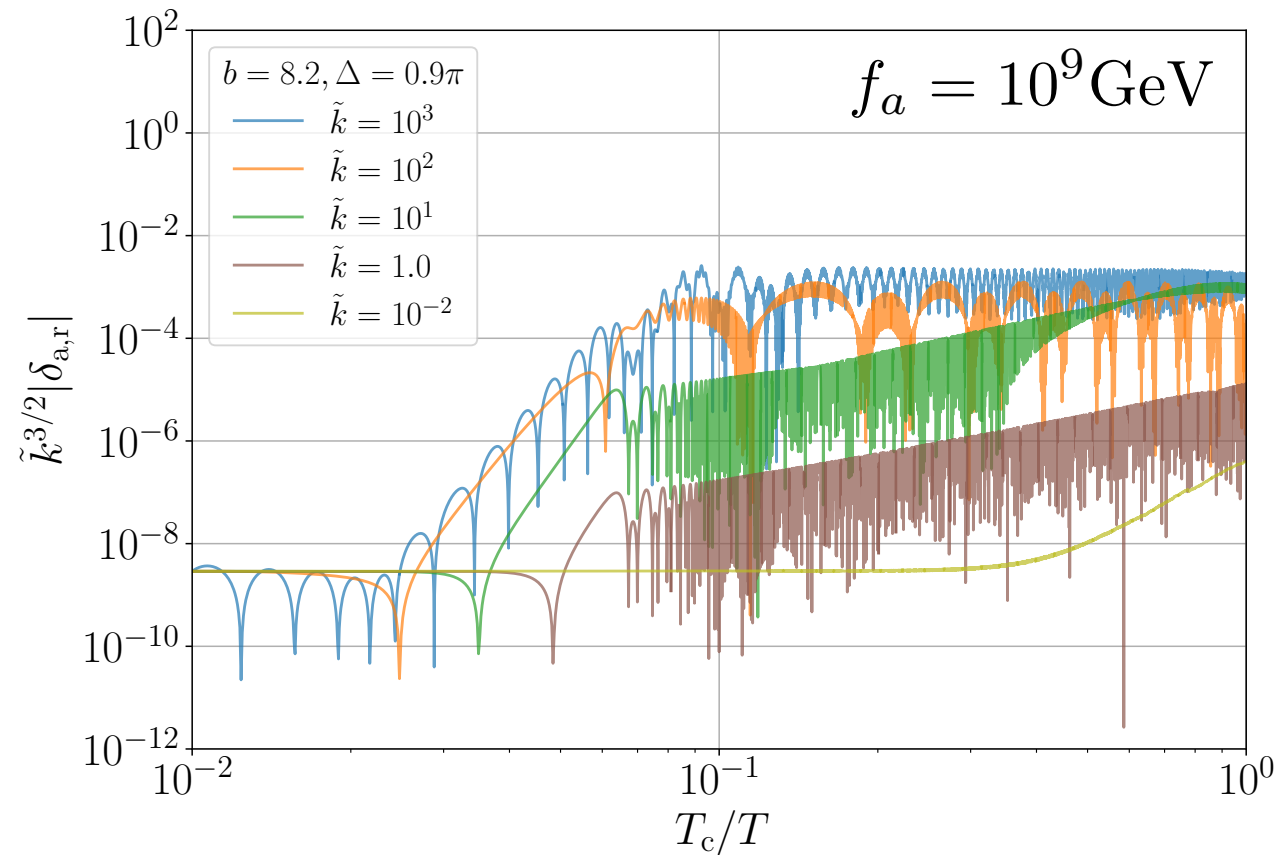
$$\zeta \simeq \frac{3}{2}\Phi$$
$$\delta\phi \simeq \delta\phi_I - \frac{\dot{\phi}}{2H}\Phi$$

fluctuation at the onset of the oscillation: $\delta\phi \sim \delta\phi_I - f_a\theta_i\Phi$

$$(\dot{\phi} \sim m_a(T)f_a\theta_i, \quad H \sim m_a(T))$$

1. clustering due to the temperature fluctuation
(soon after the onset of oscillation)

2. resonant enhancement due to the oscillating source
(radiation density wave)



$$\Delta = \pi - \theta_i, \quad \tilde{k} = \frac{k}{a(T_c)H(T_c)}$$