# The proper conflict-free $k$-coloring problem and the odd $k$-coloring problem are NP-complete on bipartite graphs 

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#### Abstract

A proper coloring of a graph is proper conflict-free if every non-isolated vertex $v$ has a neighbor whose color is unique in the neighborhood of $v$. A proper coloring of a graph is odd if for every non-isolated vertex $v$, there is a color appearing an odd number of times in the neighborhood of $v$. For an integer $k$, the PCF $k$-Coloring problem asks whether an input graph admits a proper conflict-free $k$ coloring and the Odd $k$-Coloring asks whether an input graph admits an odd $k$-coloring. We show that for every integer $k \geq 3$, both problems are NP-complete, even if the input graph is bipartite. Furthermore, we show that the PCF 4-Coloring problem is NP-complete when the input graph is planar.


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