

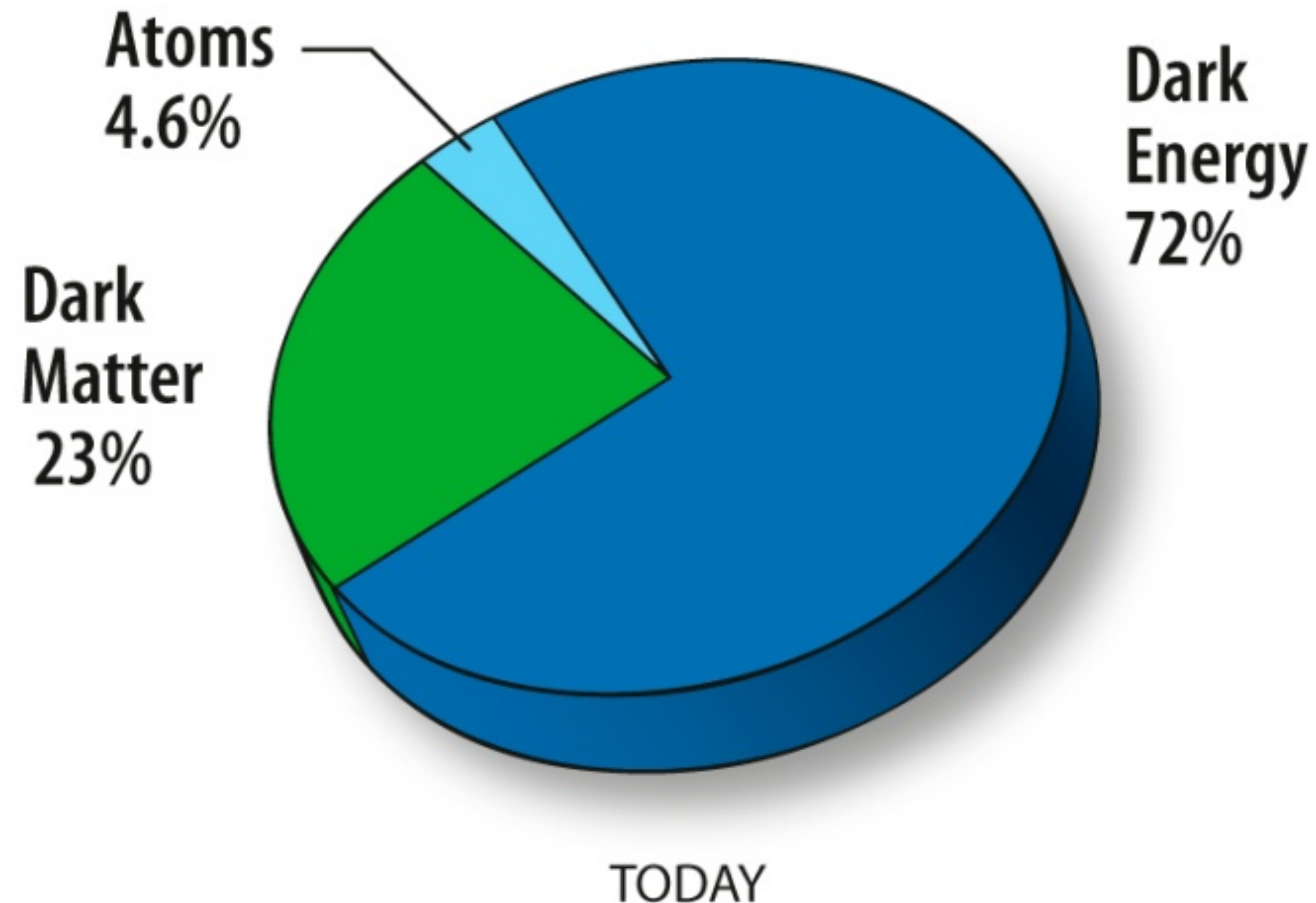
Cosmic Microwave Background as Laboratory for Fundamental Physics

Donghui Jeong
(Penn State Univ. / Korea Institute for Advanced Study)

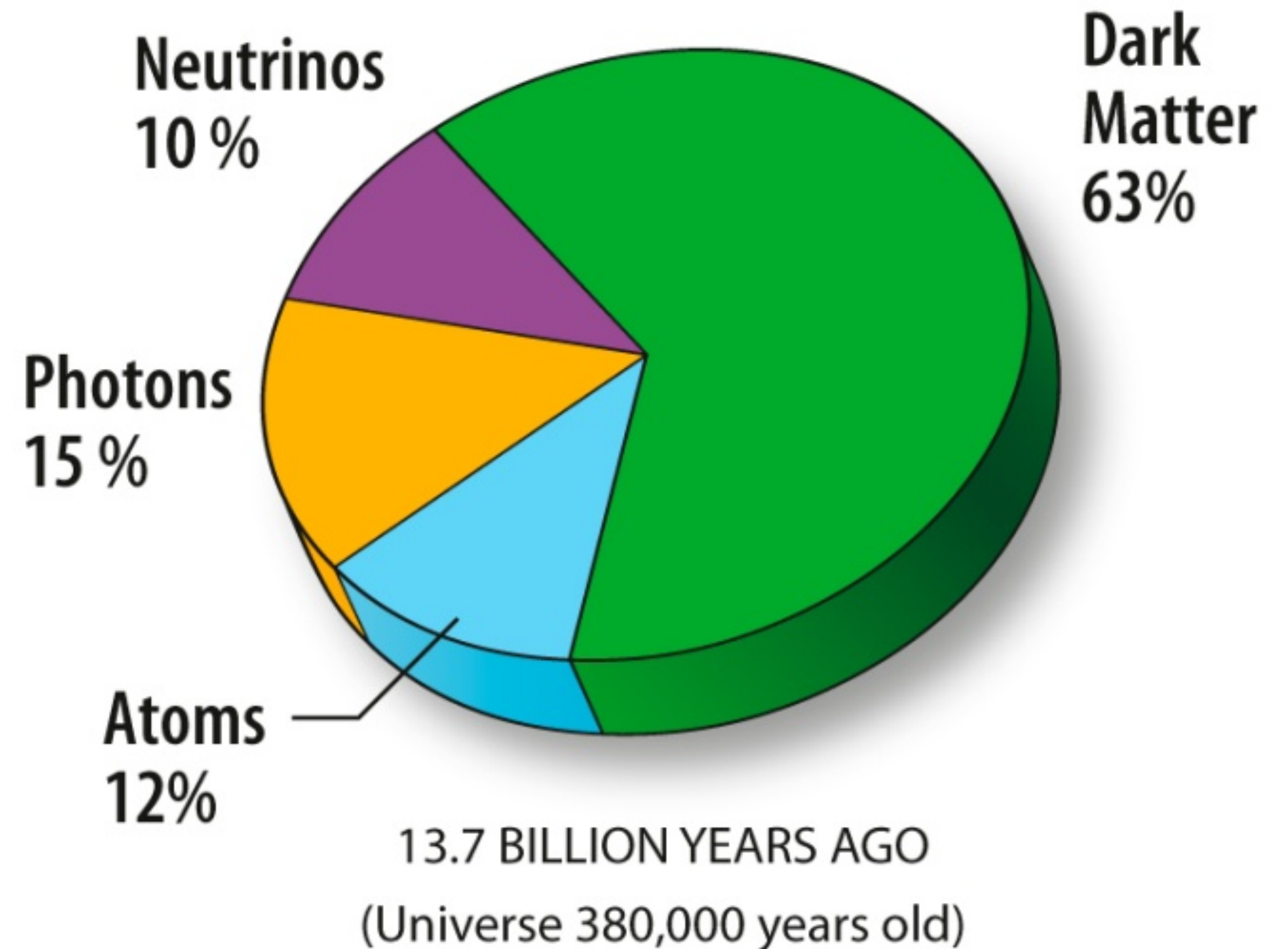
PPC2023 conference
14 June 2023

CMB shapes our physical cosmology

- The Universe is **spatially flat**, and **the expansion** is **accelerating**.



Source: NASA/WMAP science team



Remaining big questions

- ASTRO2010, 2020 decadal review panel questions are all related to the *nature of the building blocks* of the concordance model:
 - **Dark energy:** Why is the Universe accelerating now?
 - **Inflation:** How did the Universe begin?
 - **Dark matter:** What is dark matter?
 - **Neutrinos:** What are the properties of neutrinos?
- *We have been addressing all these questions using the CMB!*

CMB is a relic from hot Big-Bang

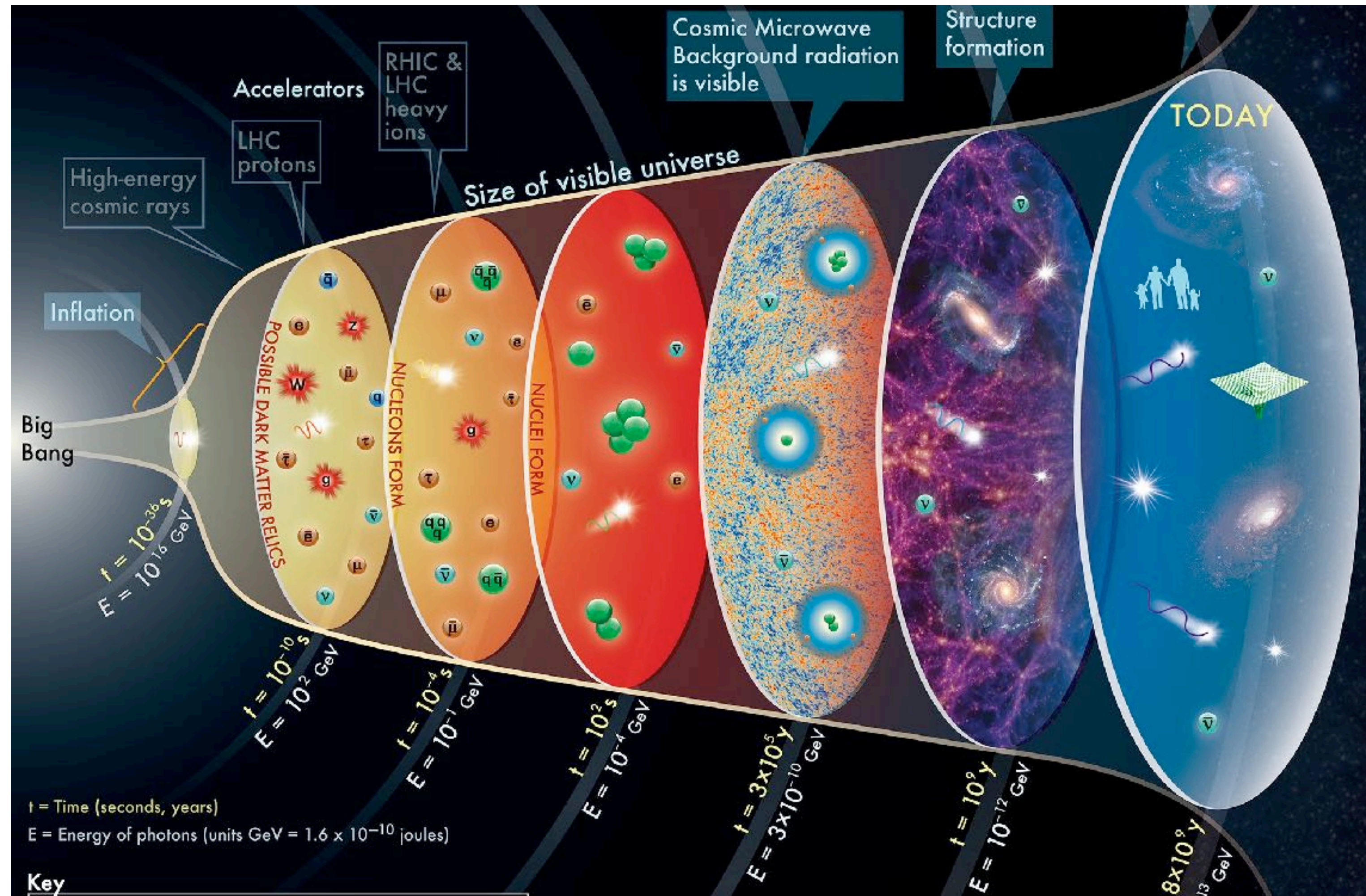


Figure from Particle Data Group, LBNL @ 2015

CMB is a relic from hot Big-Bang

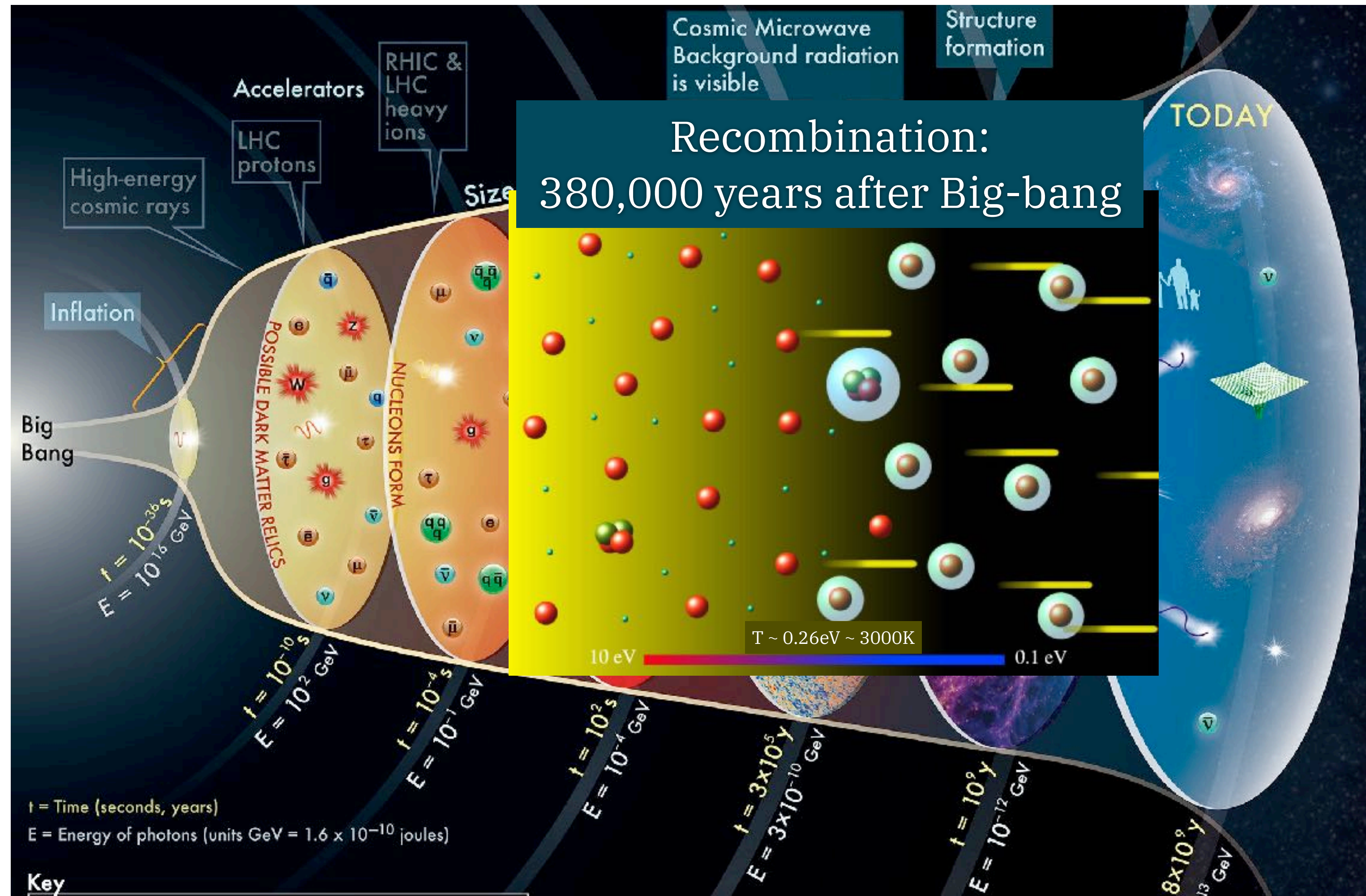
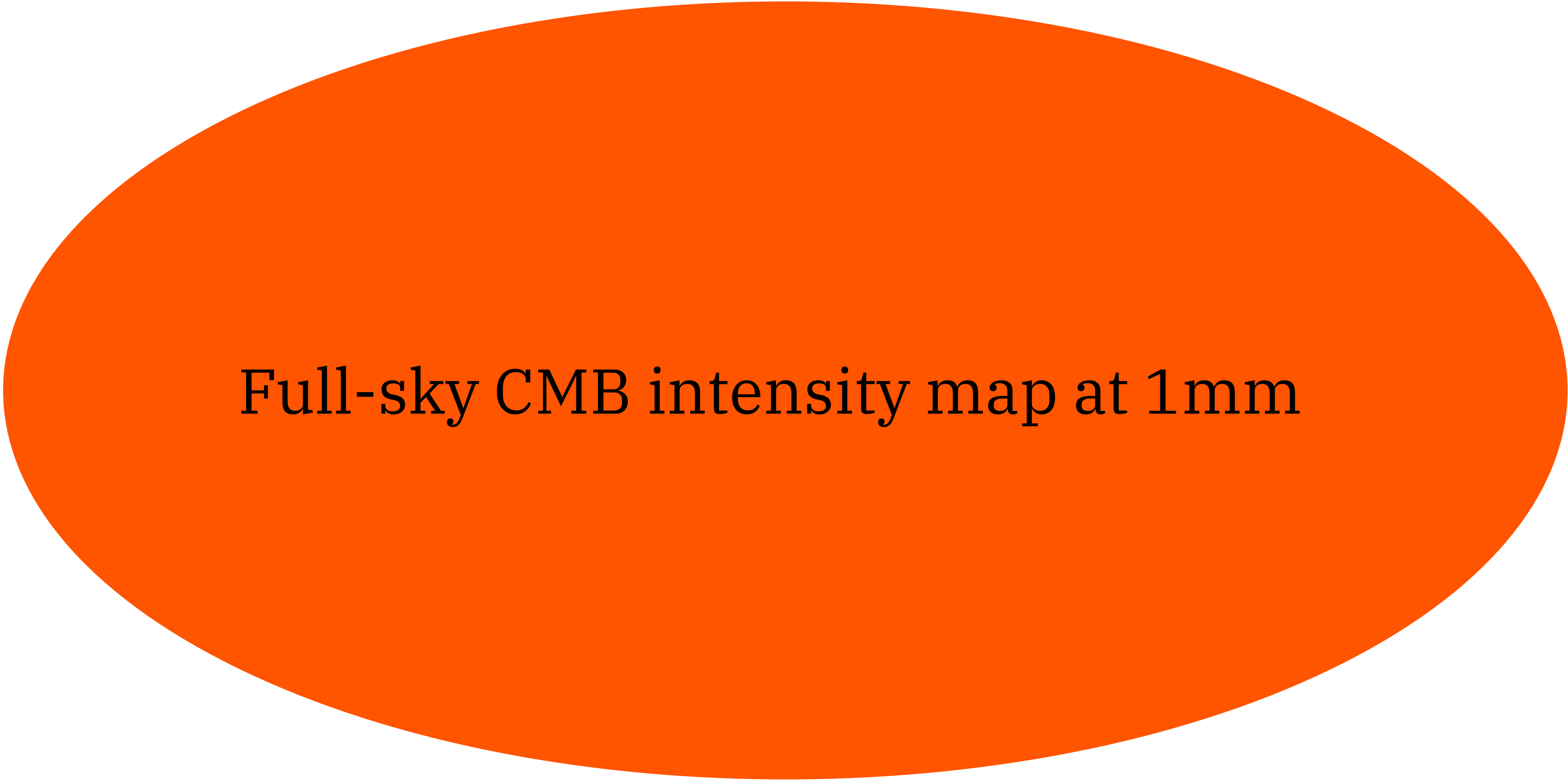


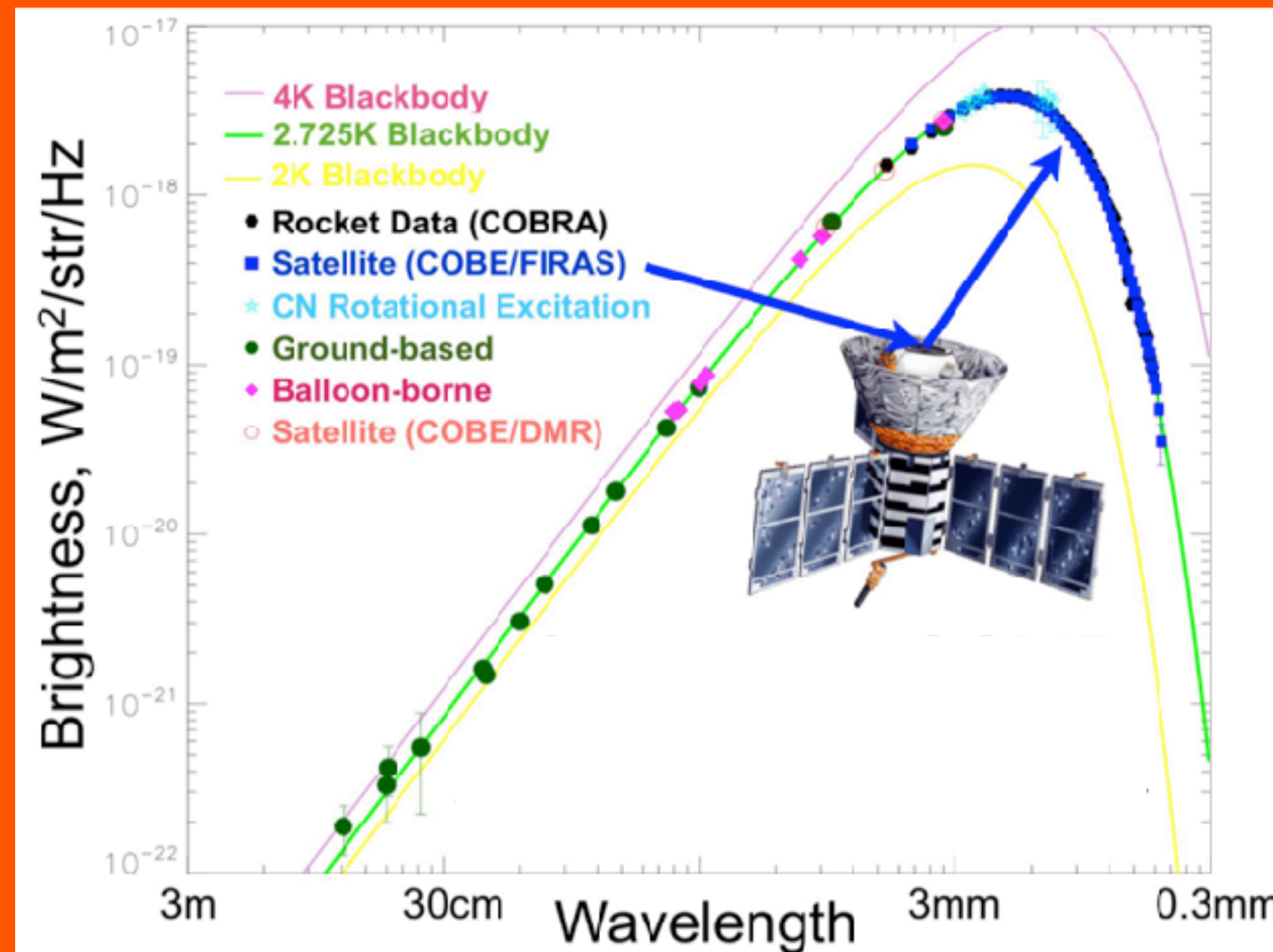
Figure from Particle Data Group, LBNL @ 2015

CMB = isotropic



Full-sky CMB intensity map at 1mm

CMB = isotropic black-body

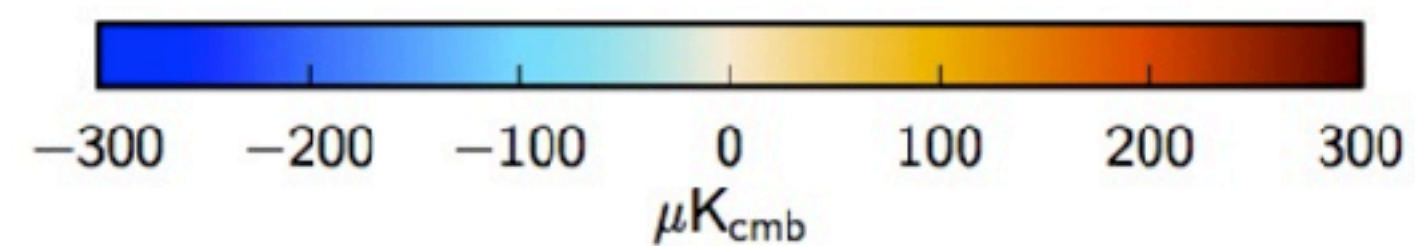
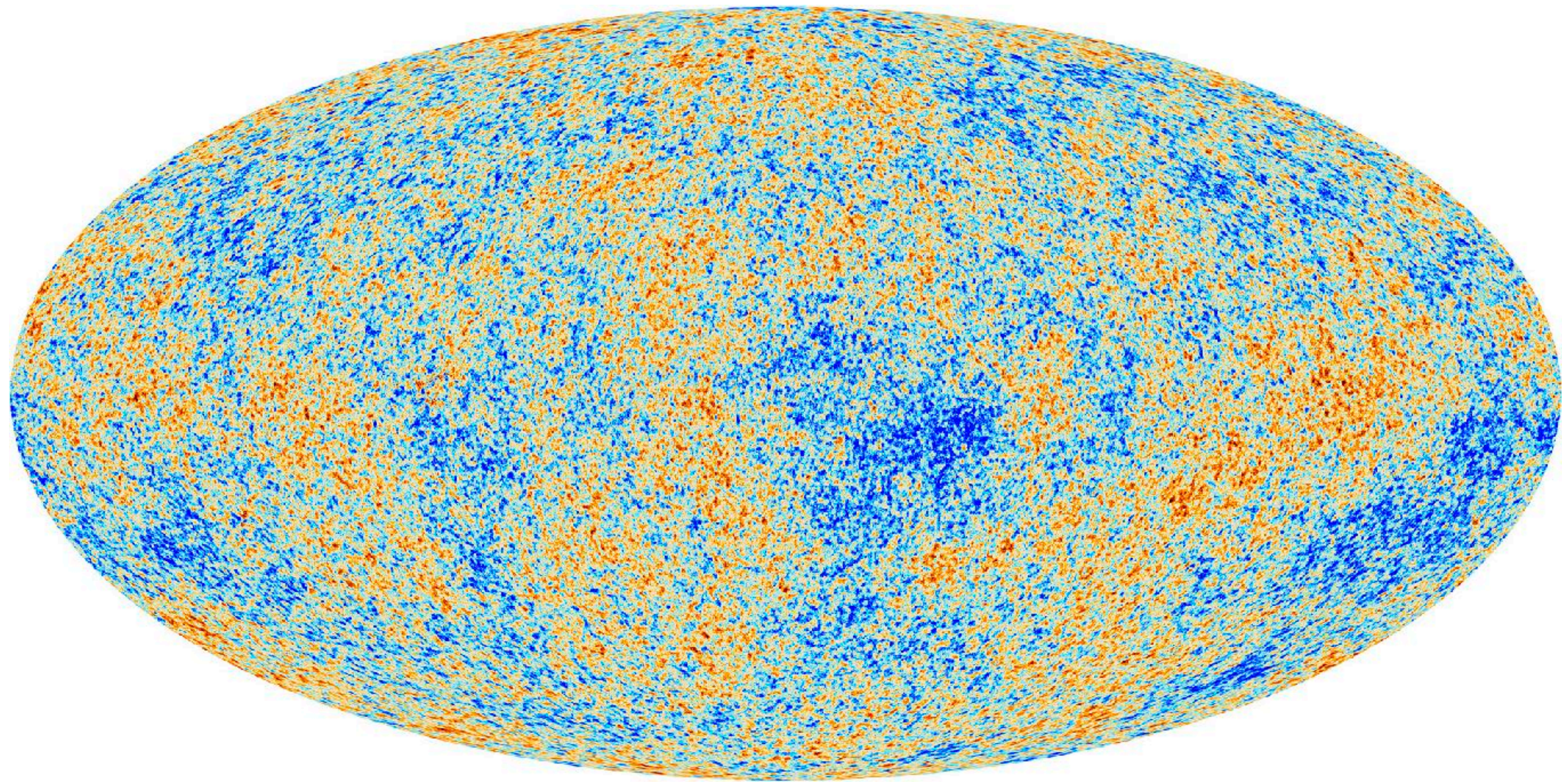


$$T_{\text{CMB}} = 2.7260 \pm 0.0013 \text{ K}$$

(Fixen+2009, COBE/FIRAS)

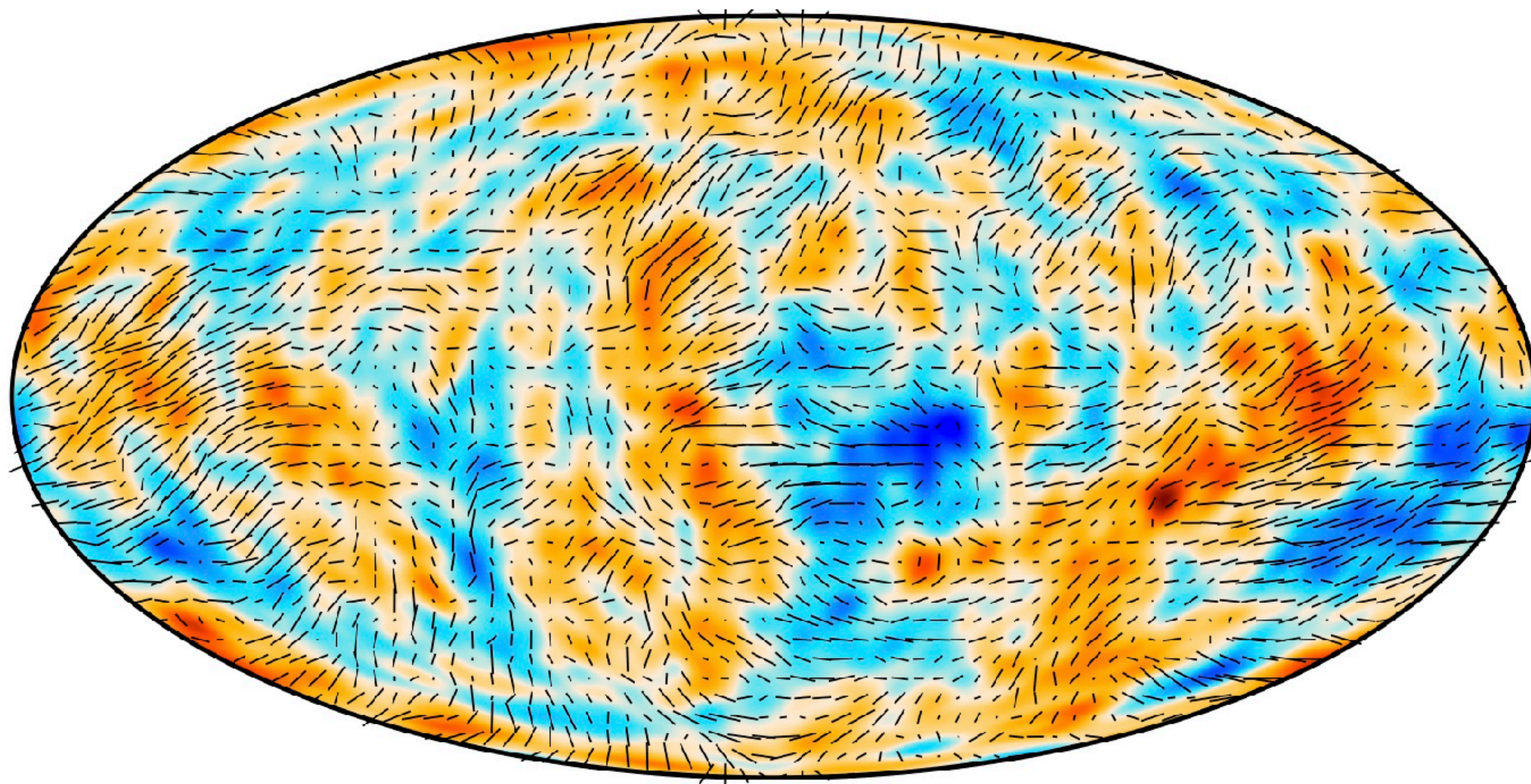
Limits on spectral distortions: $|y| < 1.5 \times 10^{-5}$, $|\mu| < 9 \times 10^{-5}$

CMB is anisotropic



maximum likelihood posterior map
Planck Collaboration

CMB is polarized



| 0.41 μK

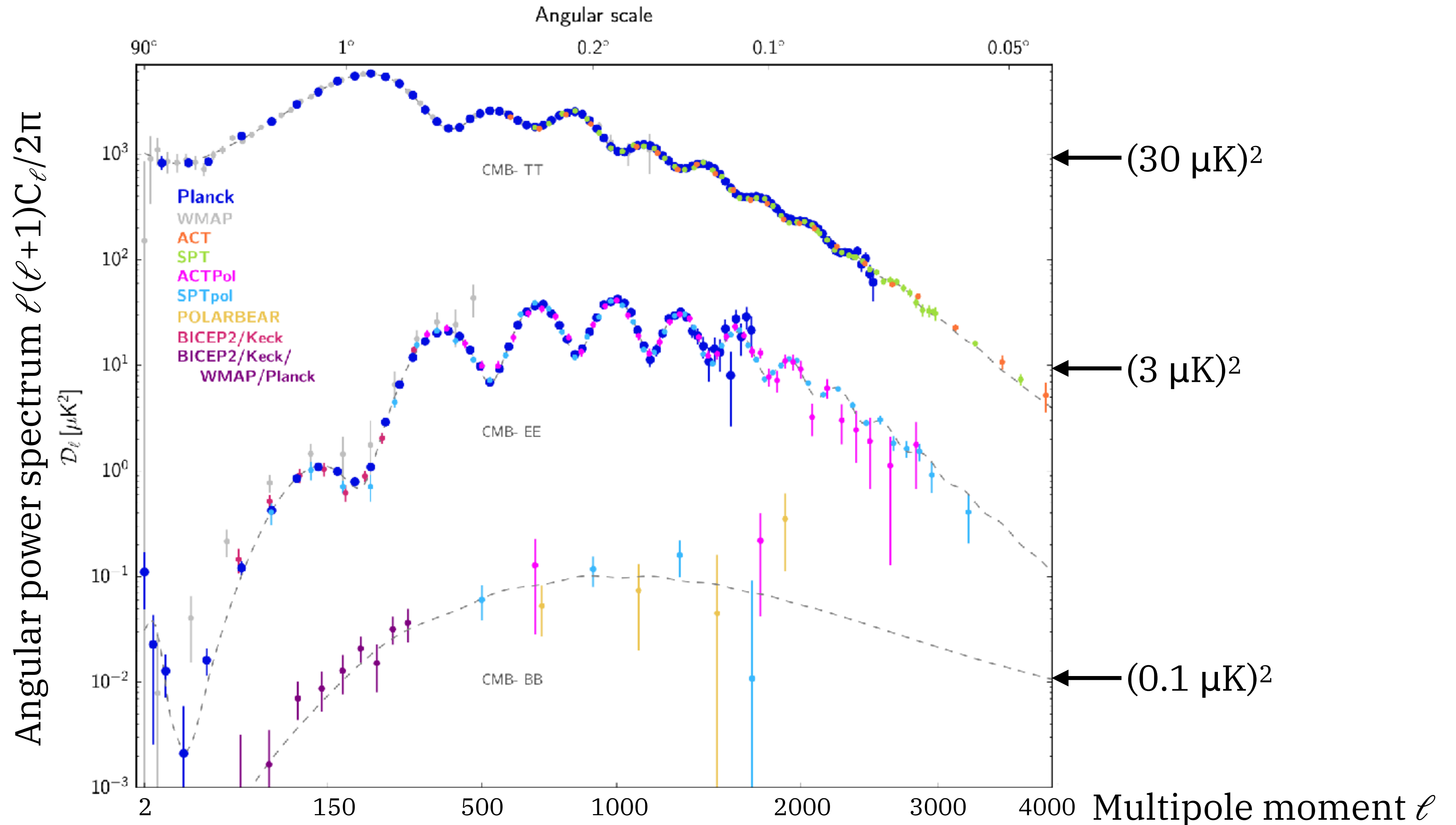
-160



160 μK

Planck map smoothed with 5° filter

Power spectra quantify anisotropies



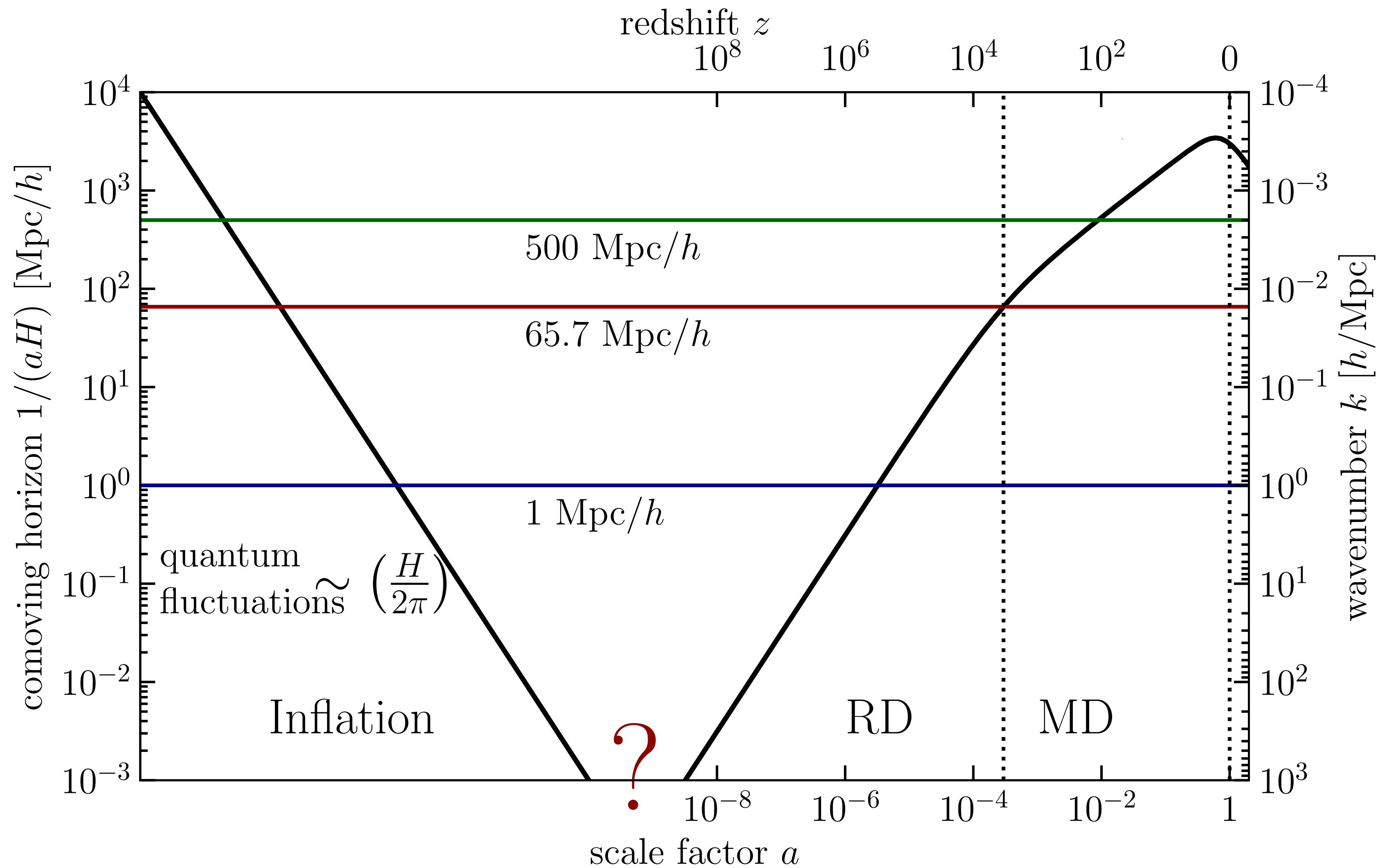
6 parameters fit $\sim 10^6$ multipoles!

Assuming plain Λ CDM model

Parameter	Best-fitting value	68% C.L.	
$\Omega_b h^2$	0.022383	0.02237 ± 0.00015	Baryon density
$\Omega_c h^2$	0.12011	0.1200 ± 0.0012	Cold dark matter density
$100\theta_{MC}$	1.040909	1.04092 ± 0.00031	Acoustic scale
τ	0.0543	0.0544 ± 0.0073	Optical depth
$\ln(10^{10} A_s)$	3.0448	3.044 ± 0.014	Amplitude of primordial power spectrum
n_s	0.96605	0.9649 ± 0.0042	Tilt of primordial power spectrum

Why only six parameters? Let's look into the details!

Inflationary perturbation theory



Story of CMB anisotropies I

- It is seeded by the quantum fluctuation generated during inflation, stretched outside *the horizon*. We call this ζ .

$$\mathcal{P}_\zeta(k) = A_s \left(\frac{k}{k_0} \right)^{n_s - 1}$$

$n_s=1$: scale-invariant power spectrum

6 parameters fit $\sim 10^6$ multipoles!

Assuming plain Λ CDM model

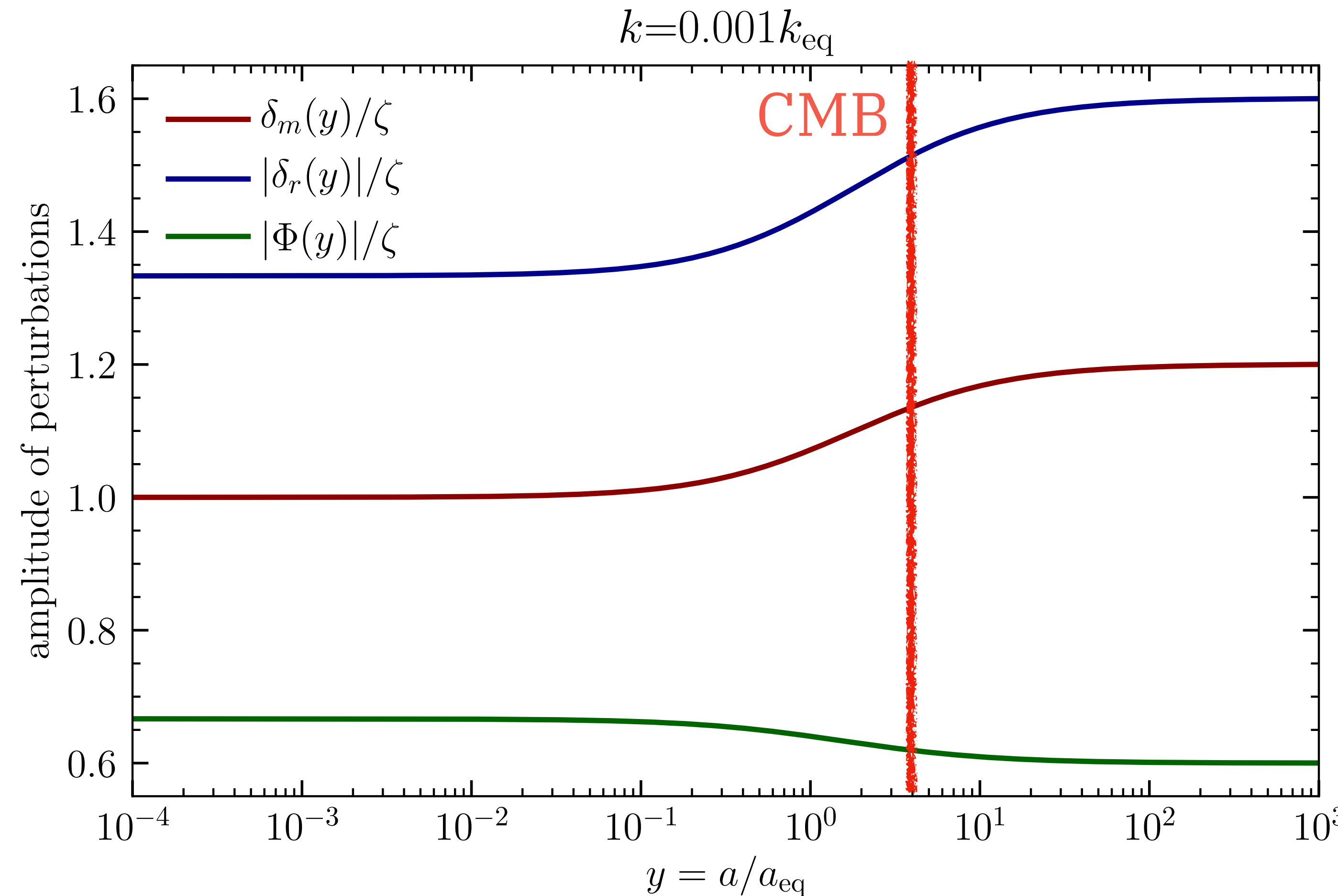
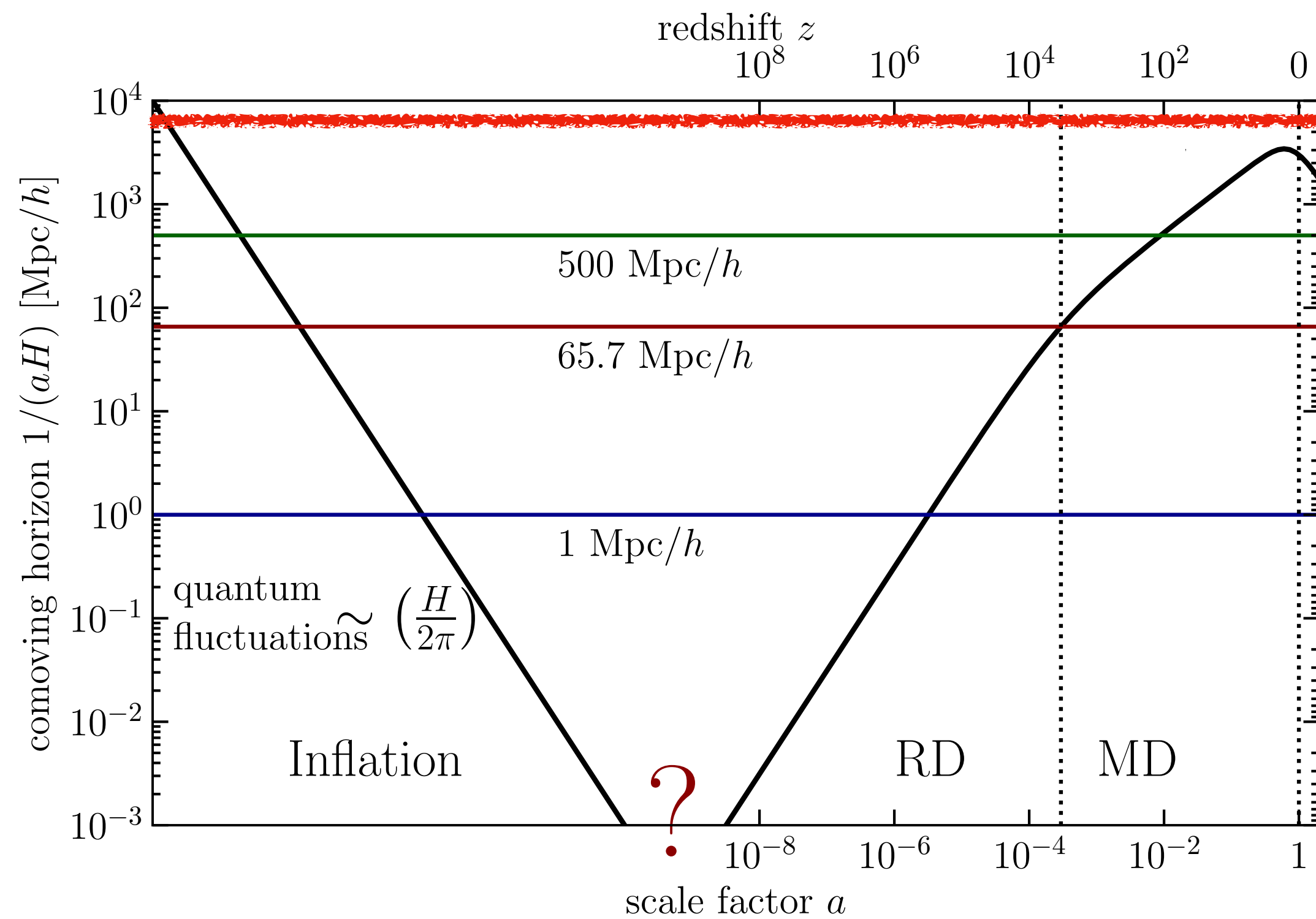
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Story of CMB anisotropies II

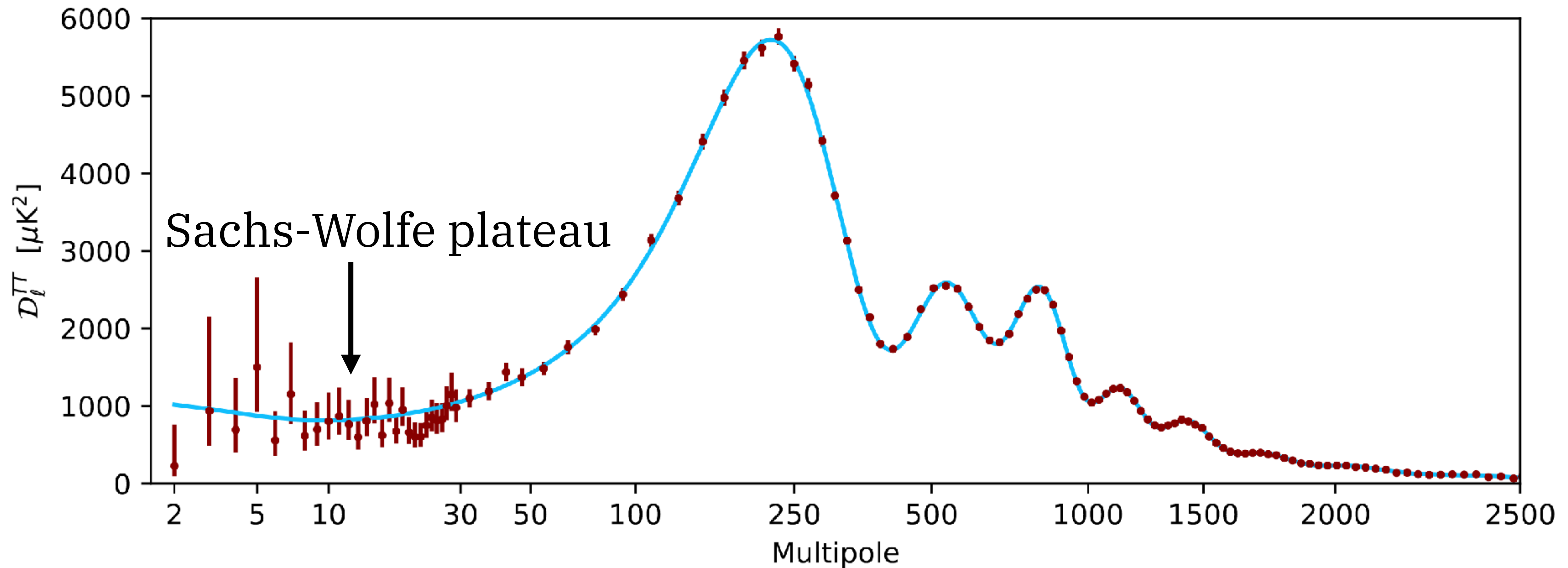
- It is seeded by the quantum fluctuation generated during inflation, stretched outside *the horizon*. We call this ζ .
- For the large-scale modes that are still outside of the horizon at the CMB decoupling time, anisotropies are determined by competition between the photon perturbation and gravitational potential (Sachs-Wolfe effect, mind the sign!)

$$\left(\frac{\delta T}{T}\right)_{\text{obs}} = -\frac{1}{5}\zeta$$

Linear evolution @ super-horizon



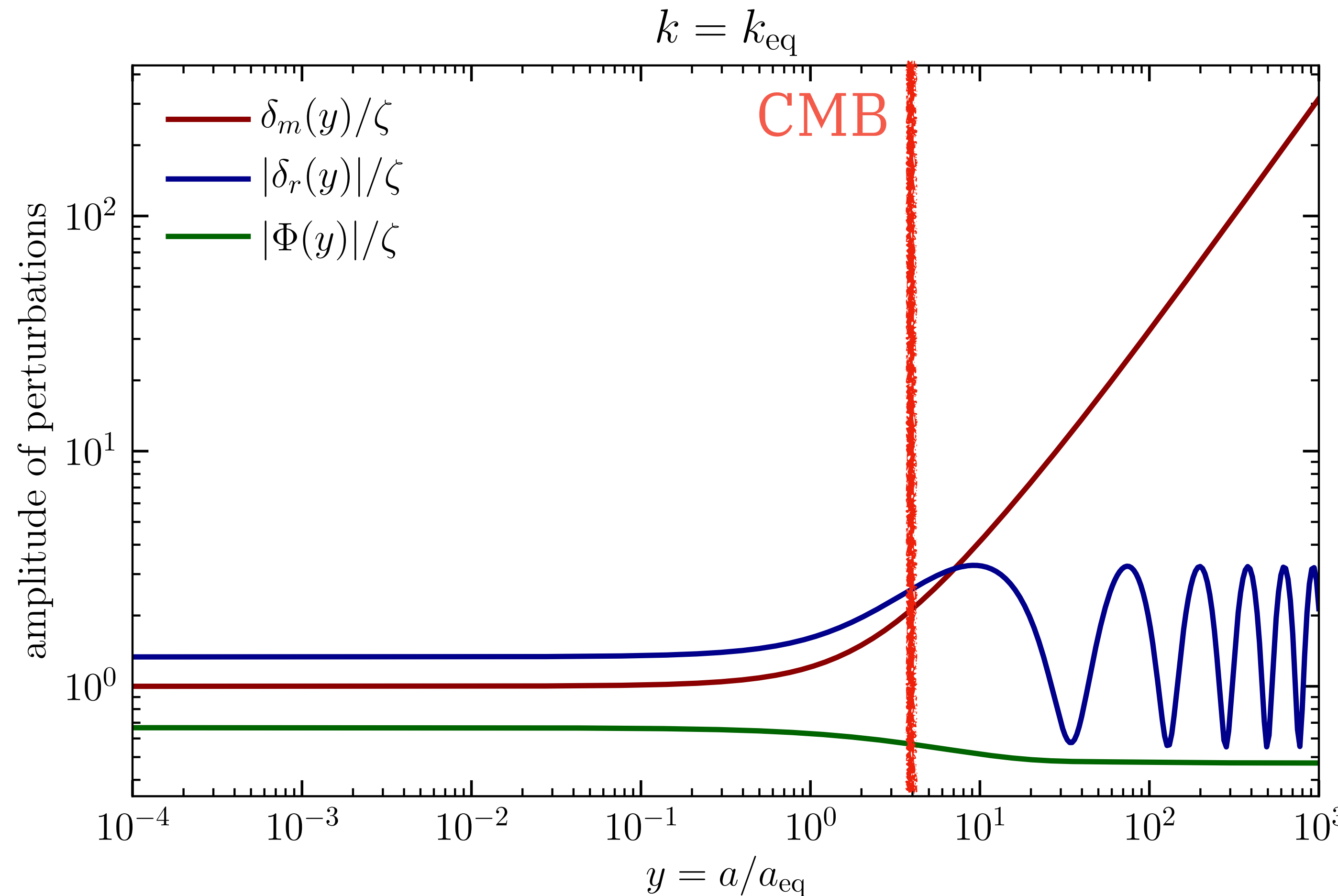
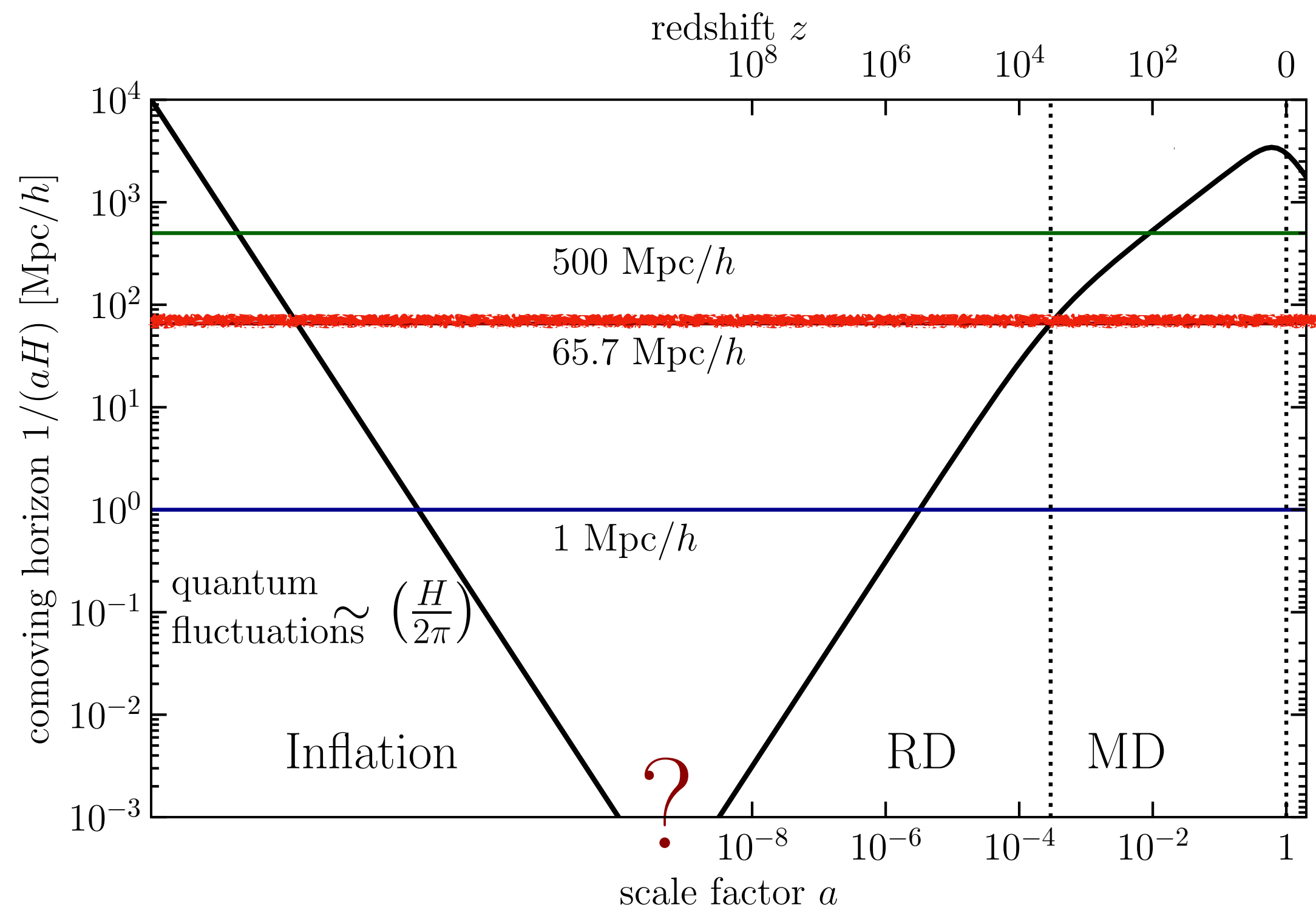
Temperature power spectrum



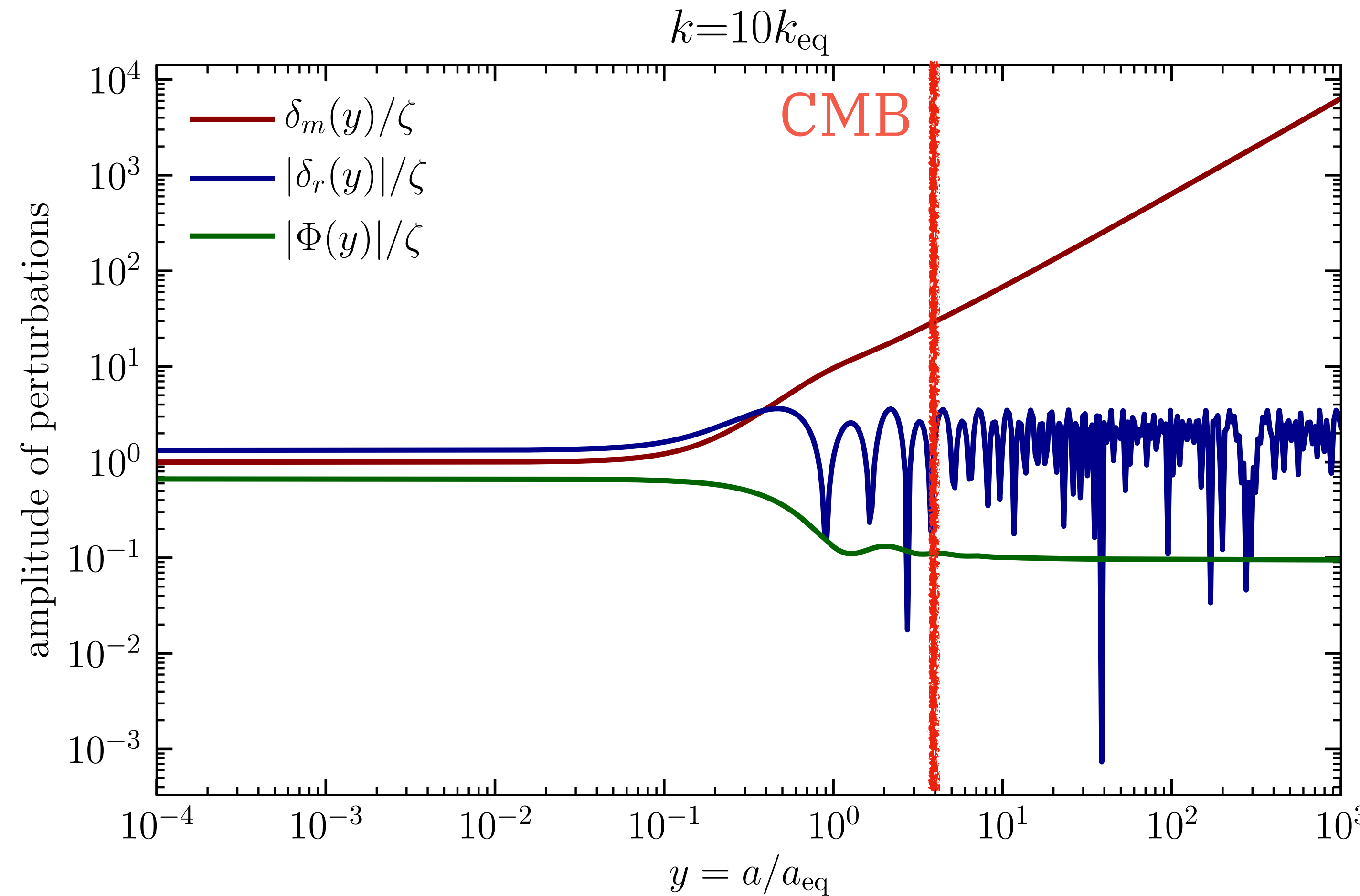
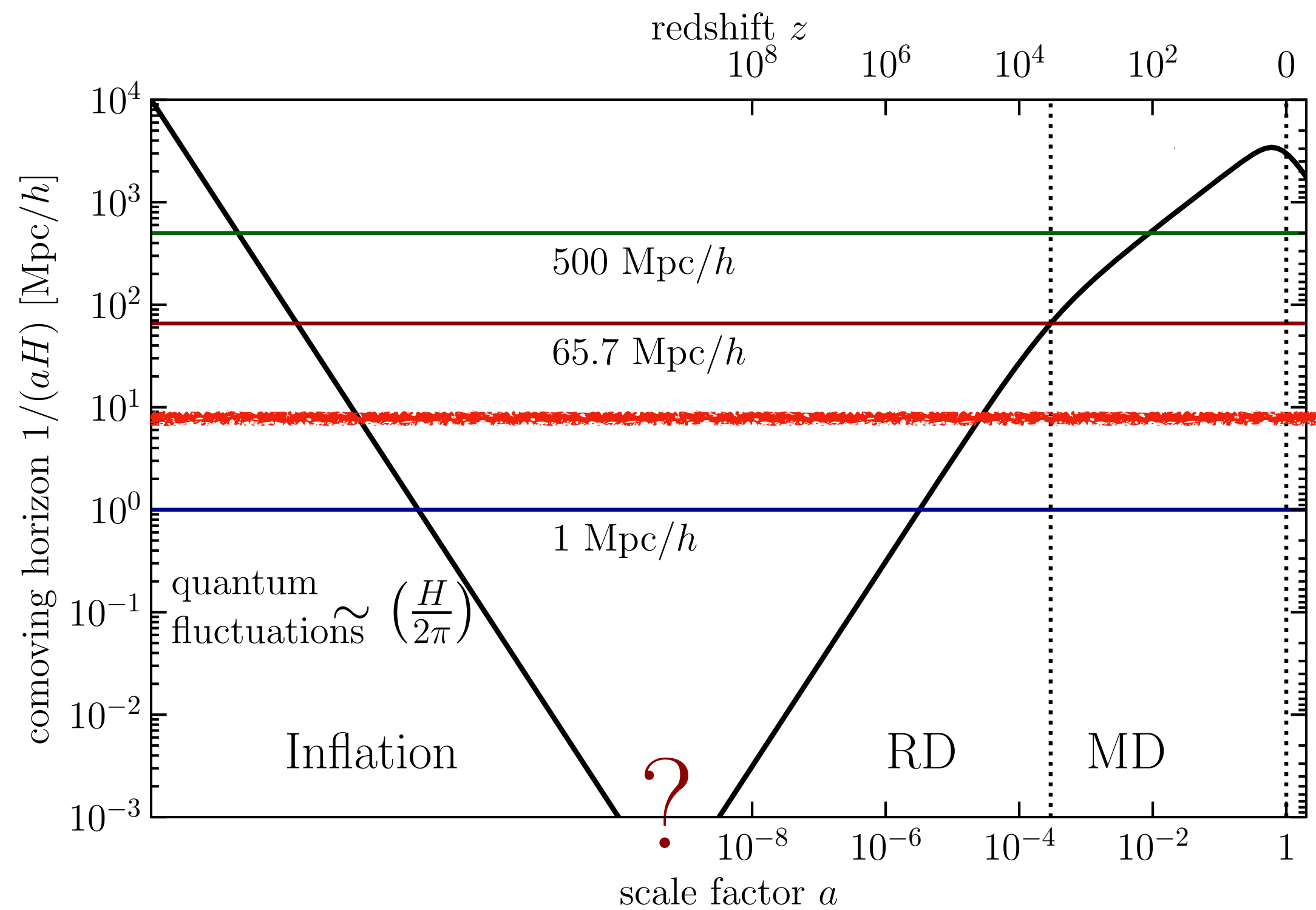
Story of CMB anisotropies II

- For the small-scale modes that were inside the horizon, tightly coupled baryon-photon plasma evolves as the pressure wave in the external gravitational field provided by dark matter perturbations: *Acoustic oscillation*

Linear evolution @ k_{eq}



Linear evolution @ $10 k_{\text{eq}}$



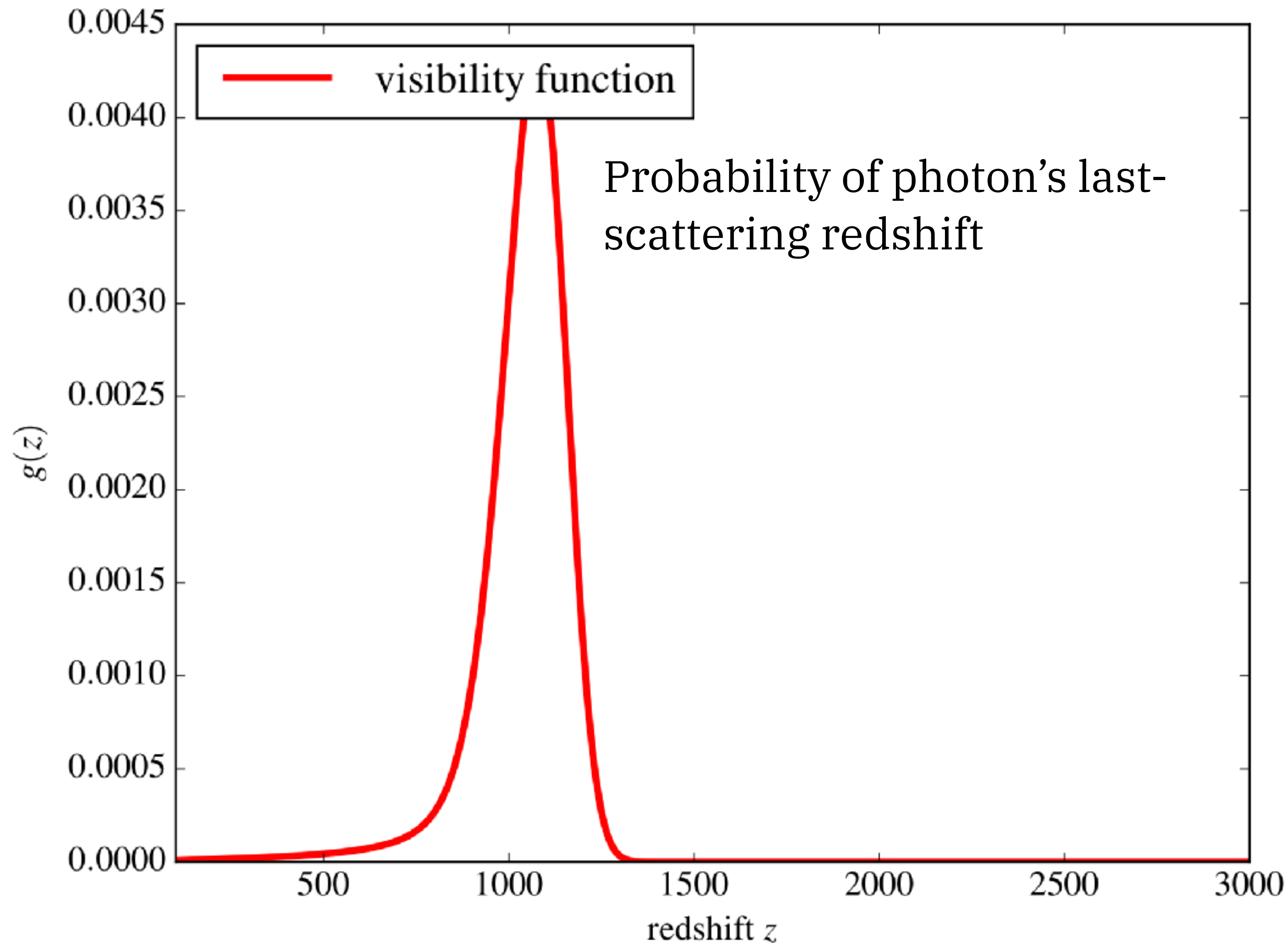
Story of CMB anisotropies III

- The comoving sound horizon of the pressure wave is modified from the usual $1/\sqrt{3}$ (photon fluid) because of the *extra inertia*

$$r_s = \int_0^{t_{\text{dec}}} c_s(t) \frac{dt}{a(t)} \quad c_s = \frac{1}{\sqrt{3(1 + 3\bar{\rho}_b/4\bar{\rho}_\gamma)}}$$

- Expansion rate determined by Friedman: $3H^2 = 8\pi G (\bar{\rho}_r + \bar{\rho}_m)$
- The amplitude of the gravitational potential is determined by the cold dark matter density : $\bar{\rho}_c$

Story of CMB anisotropies IV



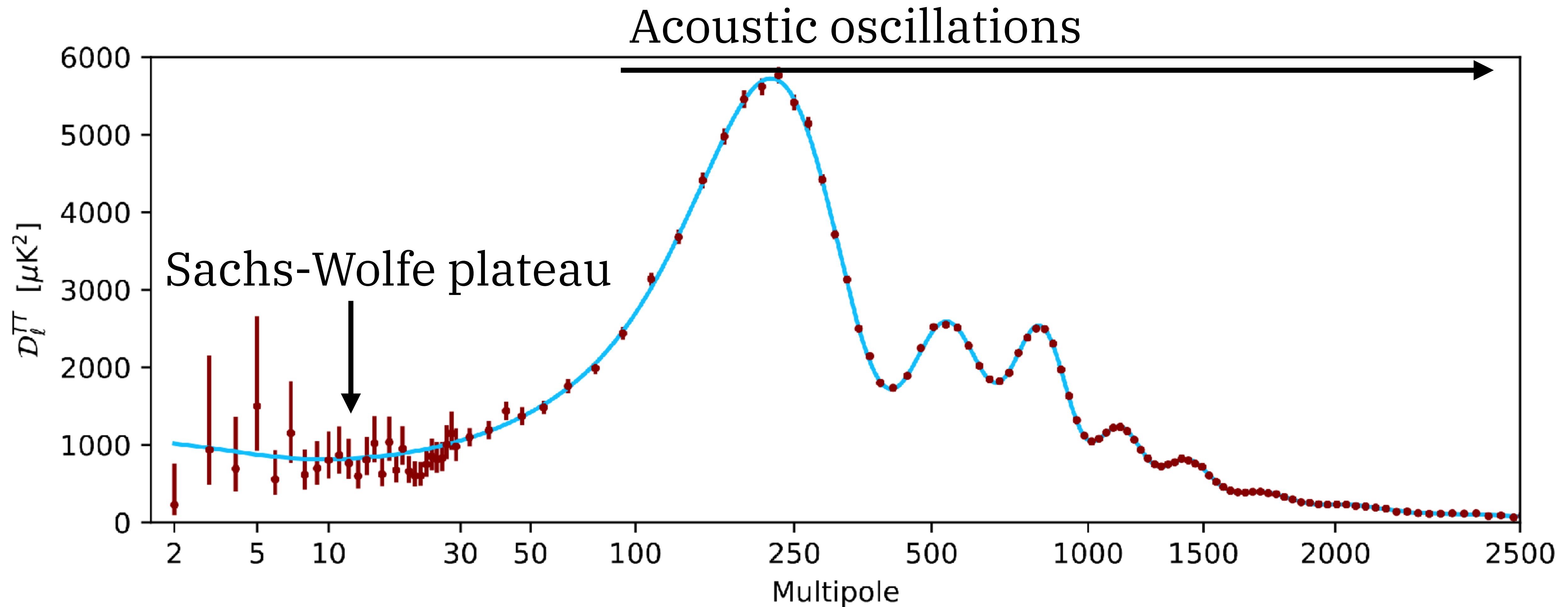
- Of course, the decoupling epoch (t_{dec}) also depends on
 - **baryon density:**
how many hydrogen to break
 - **matter density:**
how fast the photons loose energy by cosmological redshift

6 parameters fit $\sim 10^6$ multipoles!

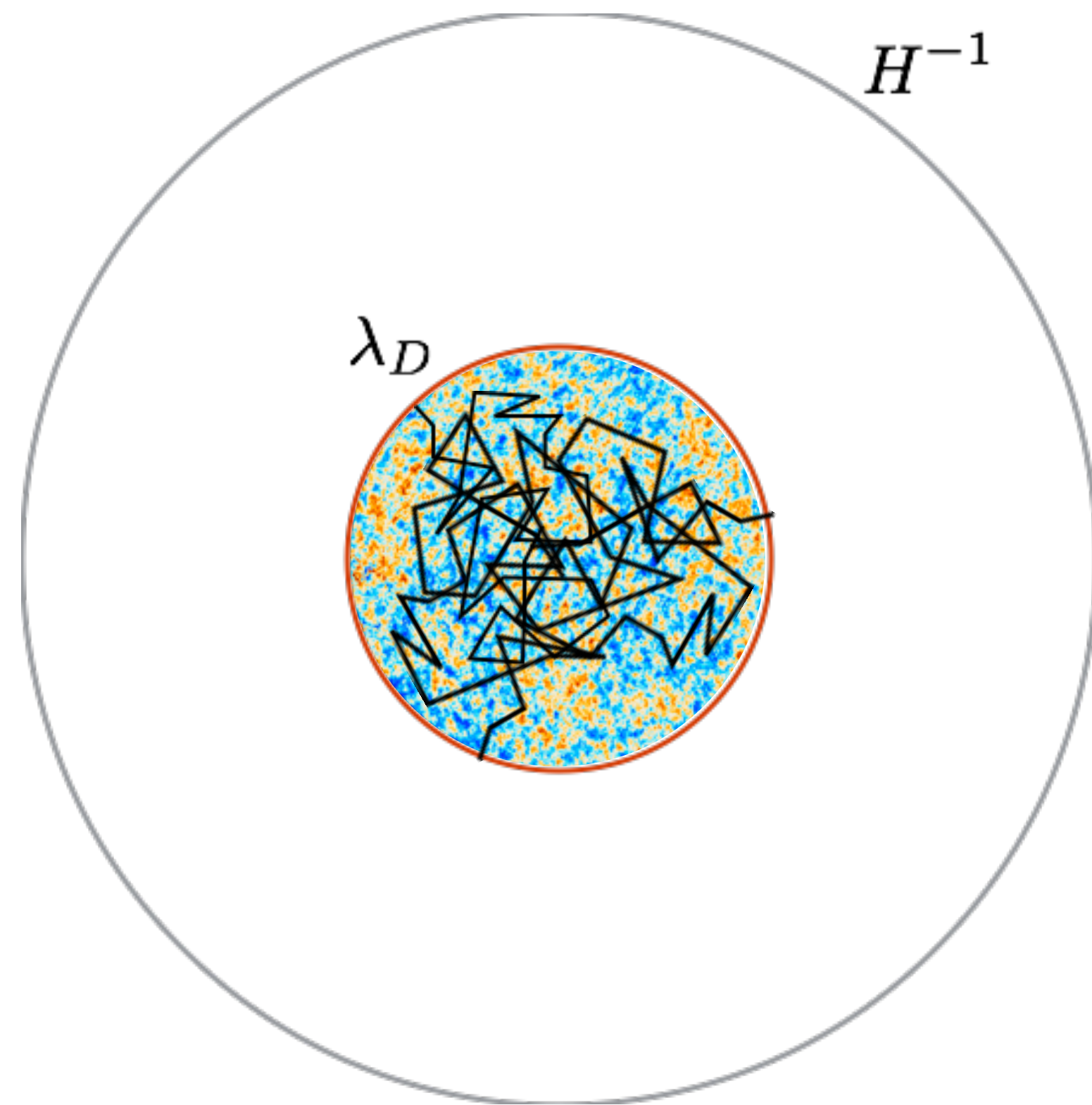
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Temperature power spectrum



Silk damping and Diffusion scale



mean free path: $\lambda_{\text{mfp}} \simeq \frac{1}{\sigma_{e\gamma} n_e}$

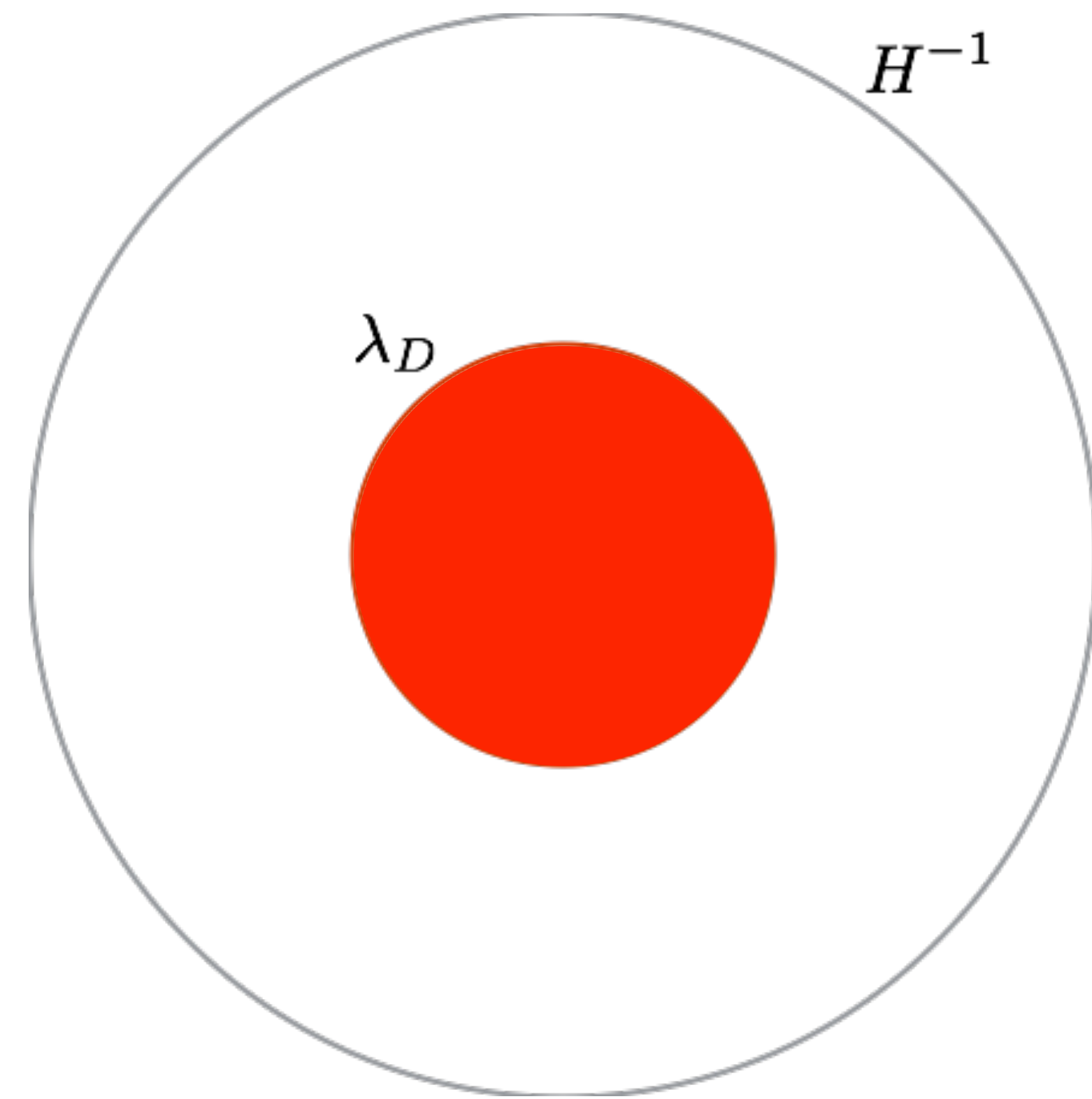
of scatters: $N \simeq \sigma_{e\gamma} n_e H^{-1}$

diffusion scale (r.m.s. of random walk):

$$\lambda_D \simeq \lambda_{\text{mfp}} \sqrt{N} \simeq \frac{1}{\sqrt{\sigma_{e\gamma} n_e H}}$$

temperature anisotropies
at $\sim 0.0001''$ scale, *at early time*

Silk damping and Diffusion scale



temperature anisotropies
at $\sim 1''$ scale, *observed*

mean free path: $\lambda_{\text{mfp}} \simeq \frac{1}{\sigma_{e\gamma} n_e}$

of scatters: $N \simeq \sigma_{e\gamma} n_e H^{-1}$

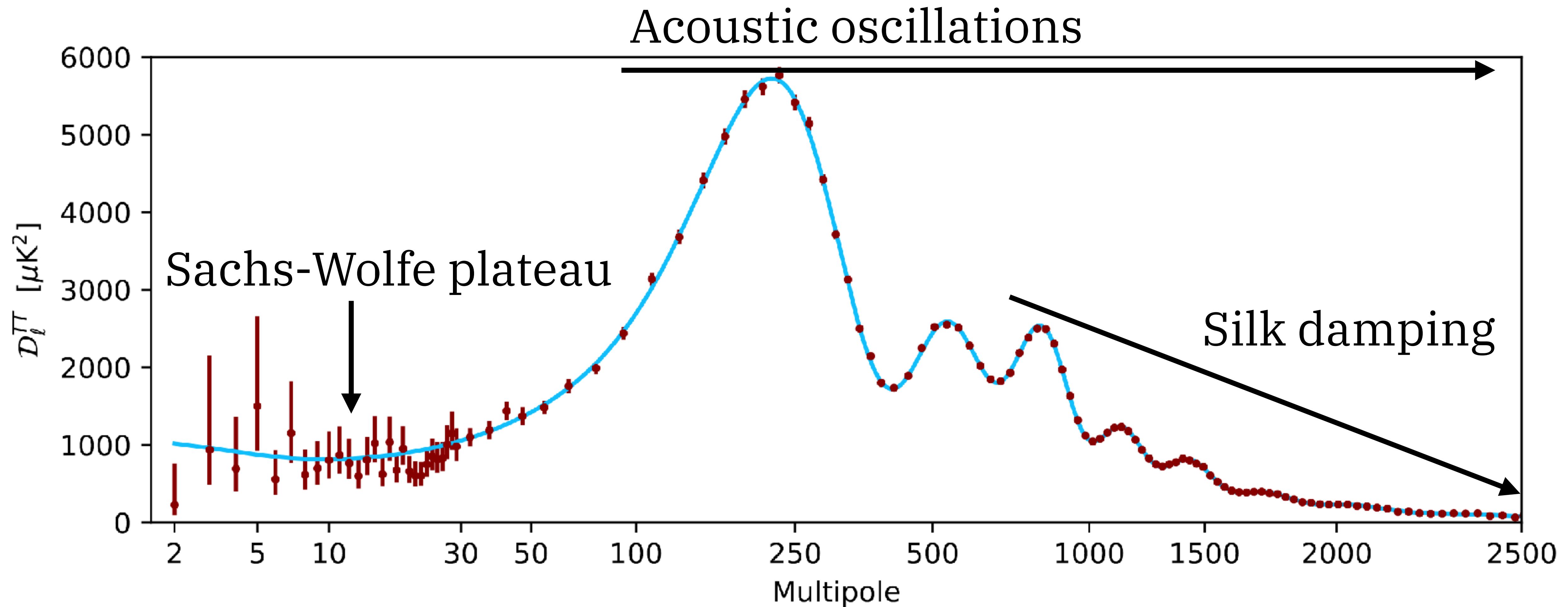
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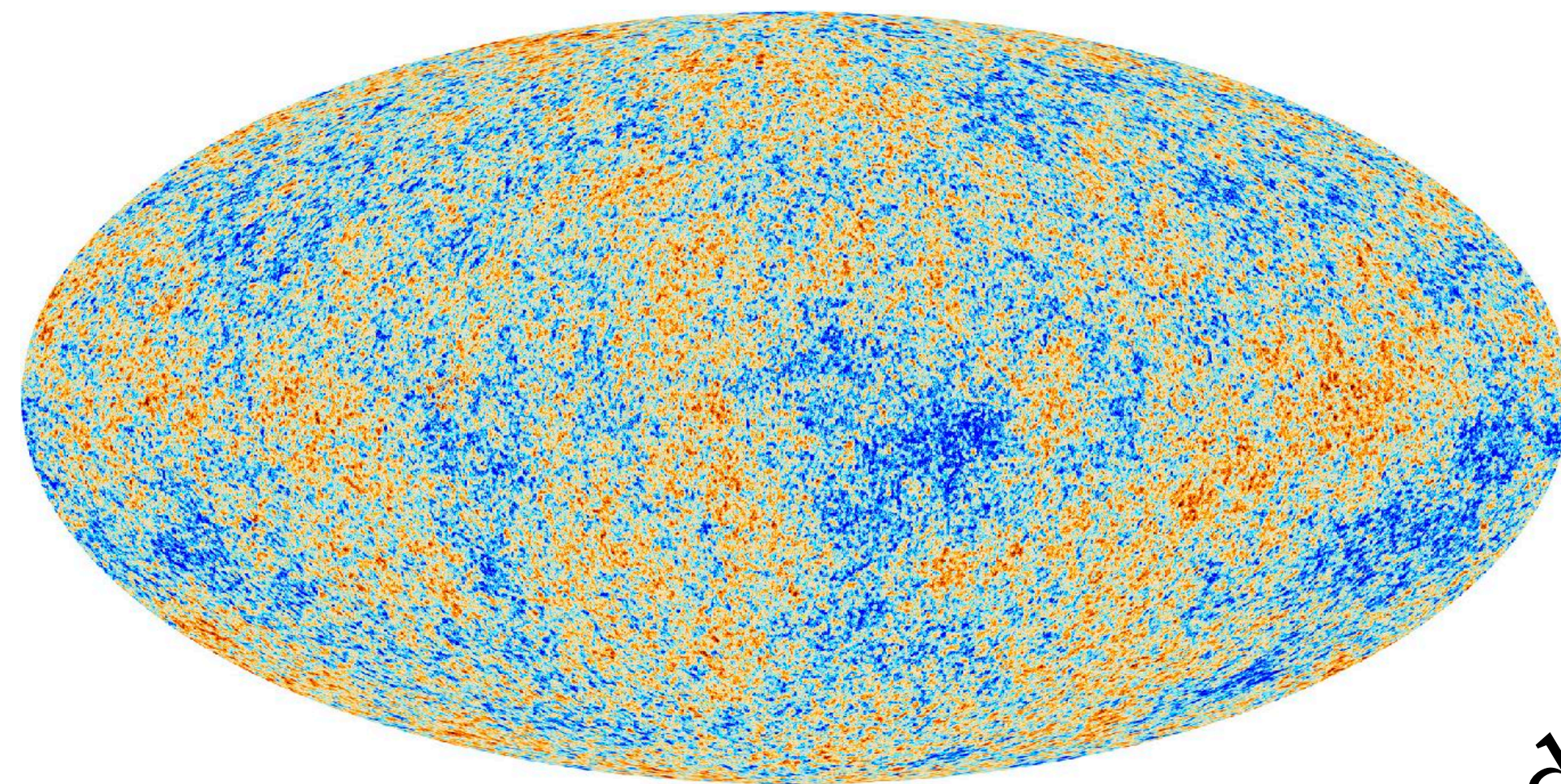
Diffusion = temperature equalizer

Diffusion length scale $\sim$ **10 Mpc**!!

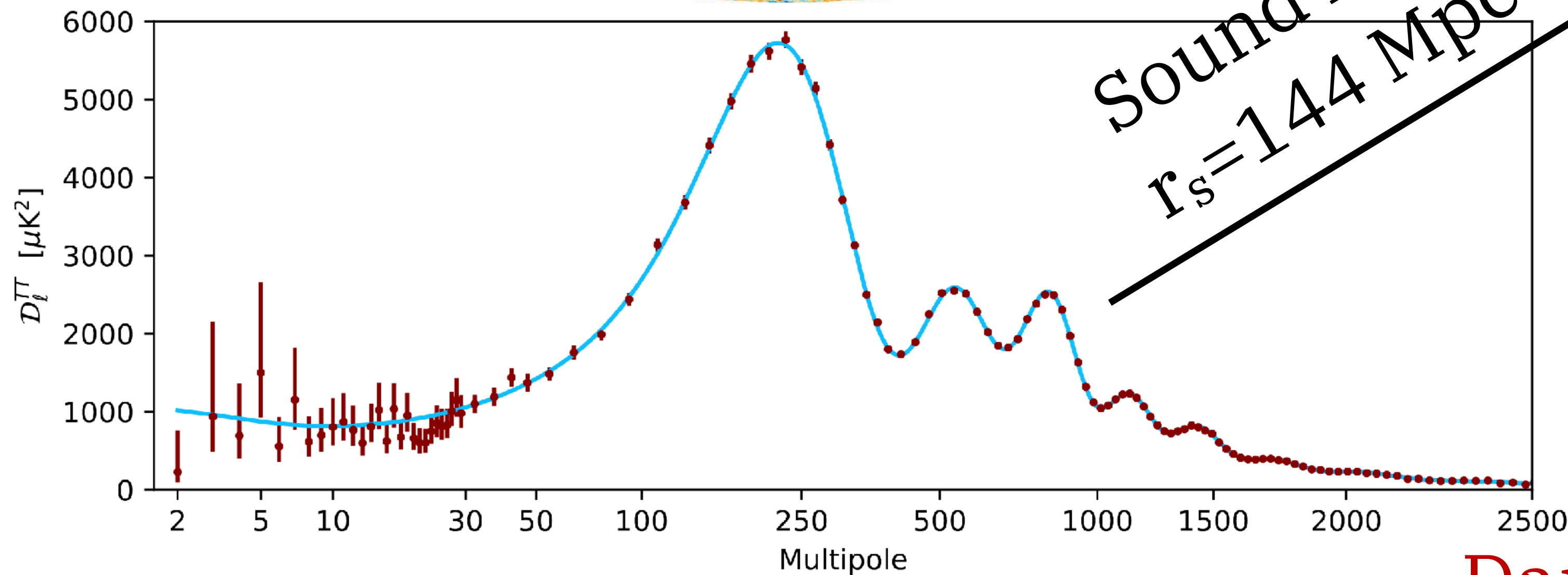
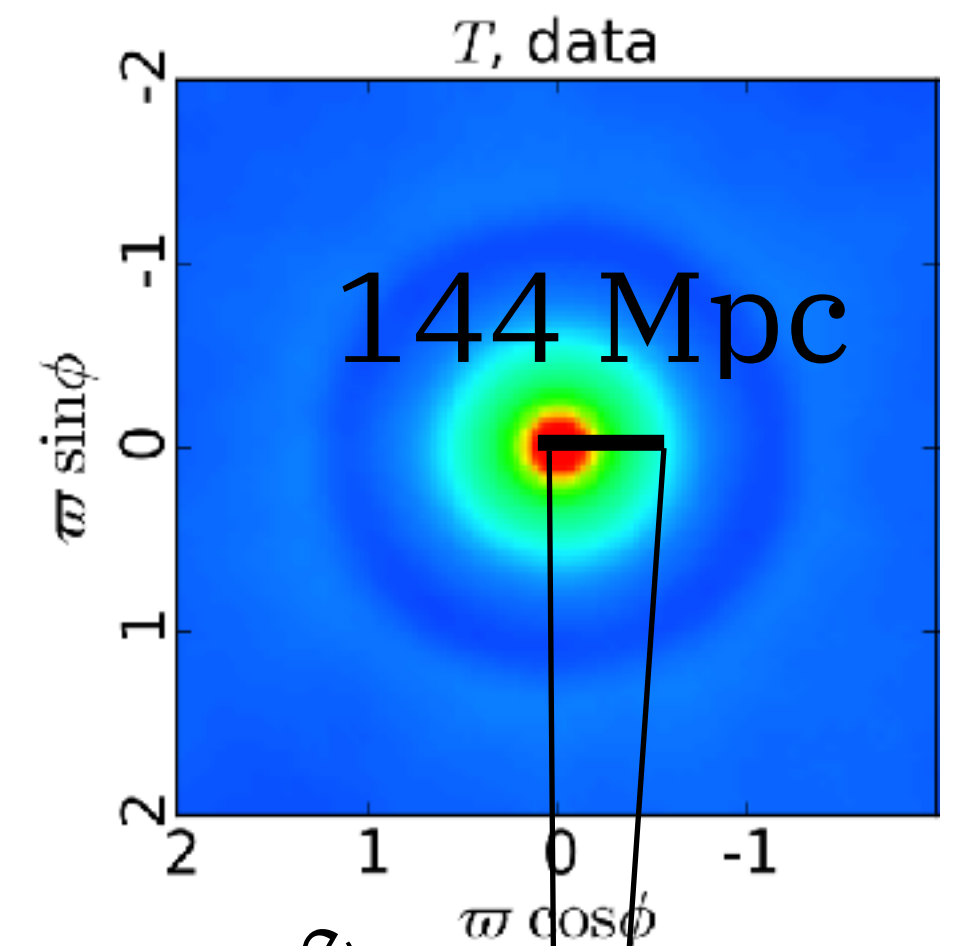
Temperature power spectrum



Sound horizon and acoustic scale



Stacking



Sound horizon
 $r_s = 144 \text{ Mpc}$

angular diameter distance

θ_{MC}

Observer

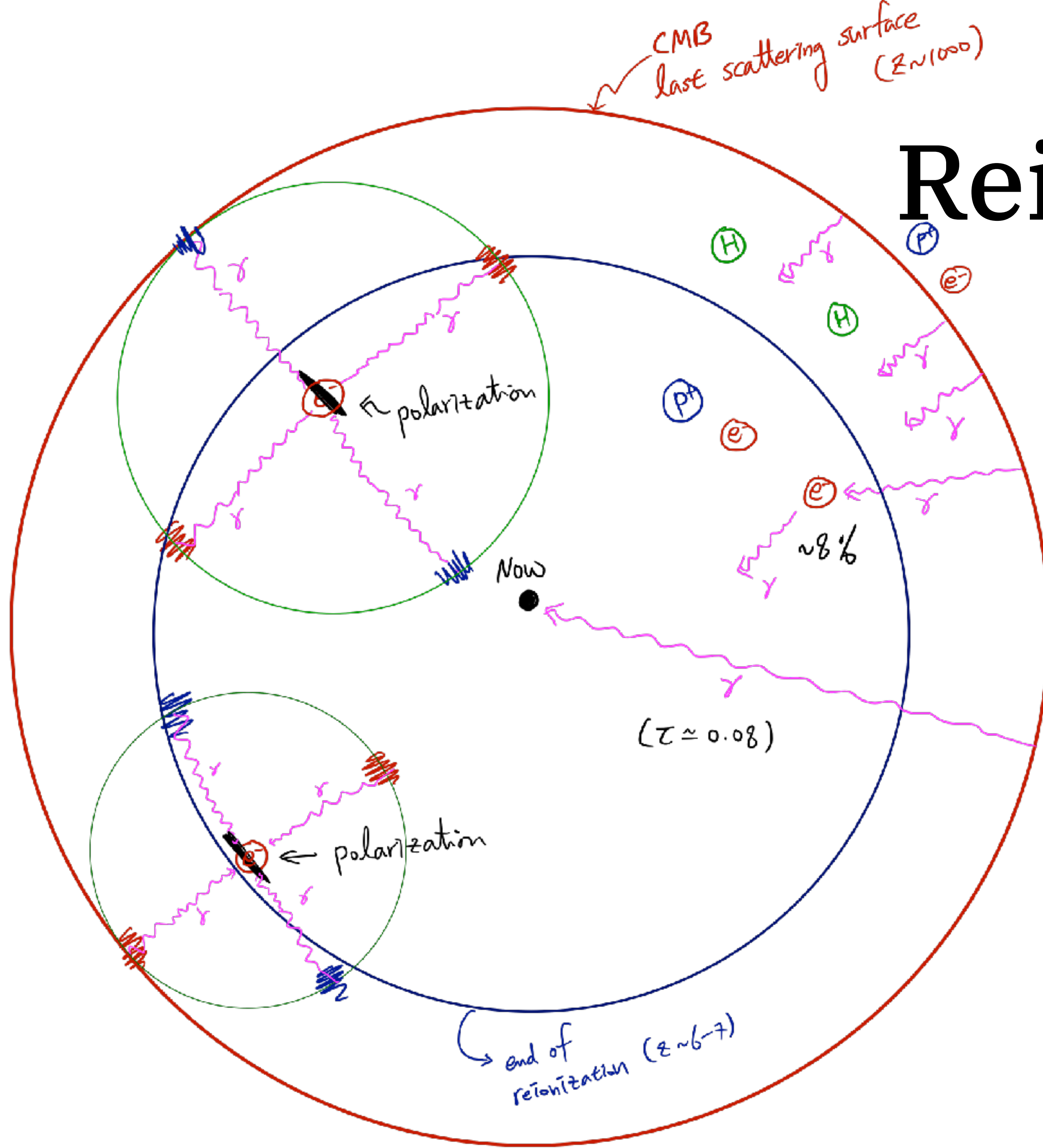
Dark energy, H_0 !

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Reionization and CMB



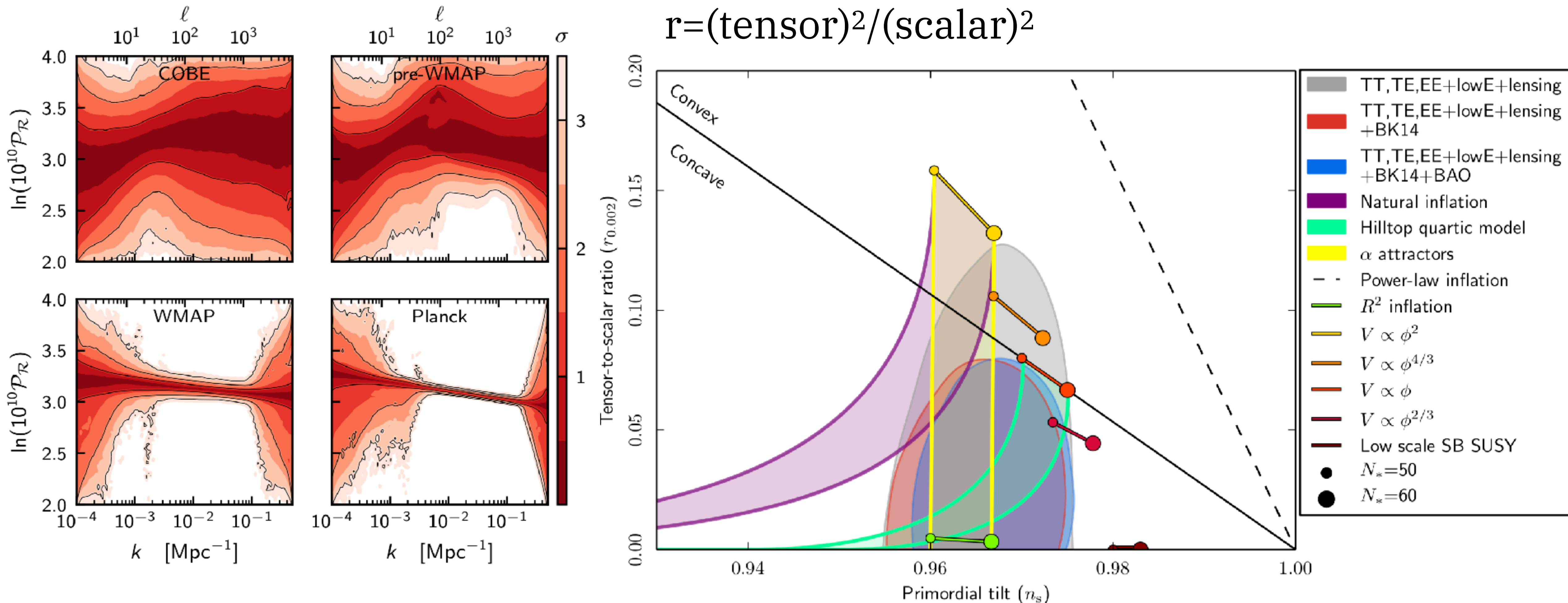
- Reionization Optical depth ~ 0.05 (Planck), 0.08 (WMAP): $5\sim 8\%$ of CMB re-scatter
- Three effects:
 - Damping the temperature anisotropies on small scales
 - Polarization on large scales.
 - kSZ from reionization patches

6 parameters fit $\sim 10^6$ multipoles!

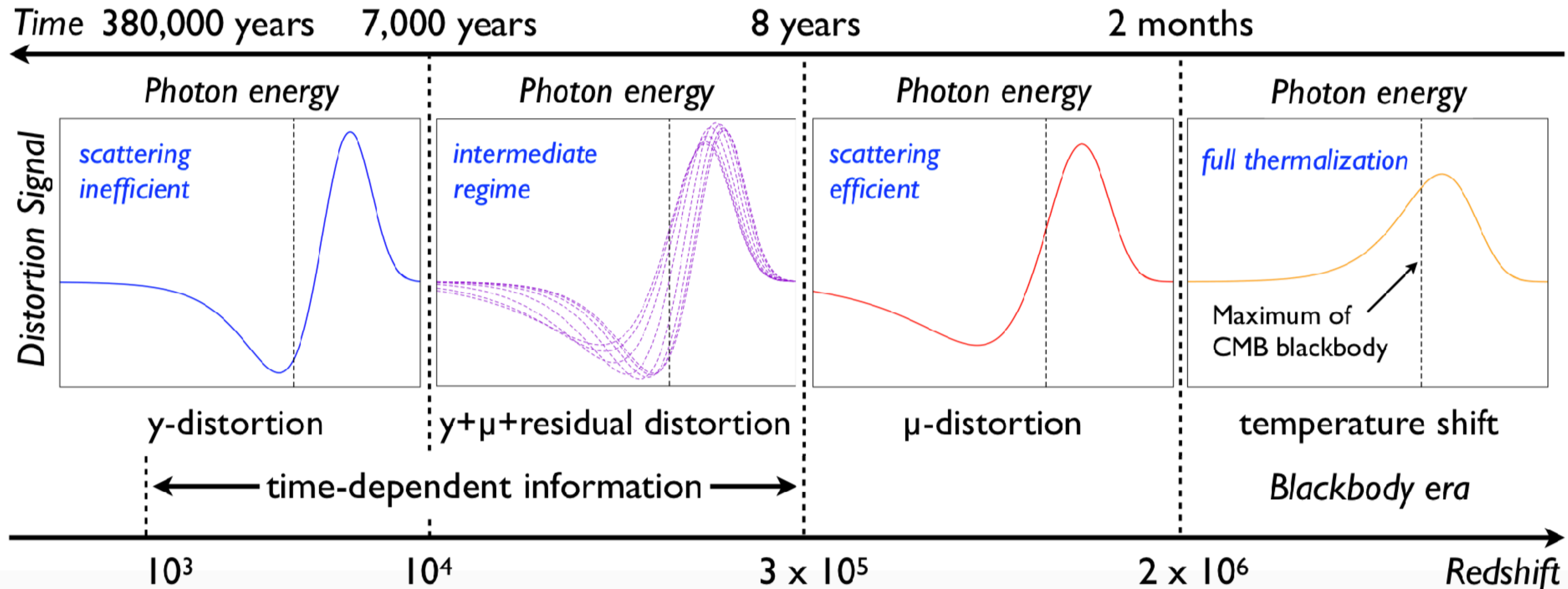
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Undo evolution to constrain the *I.C.*

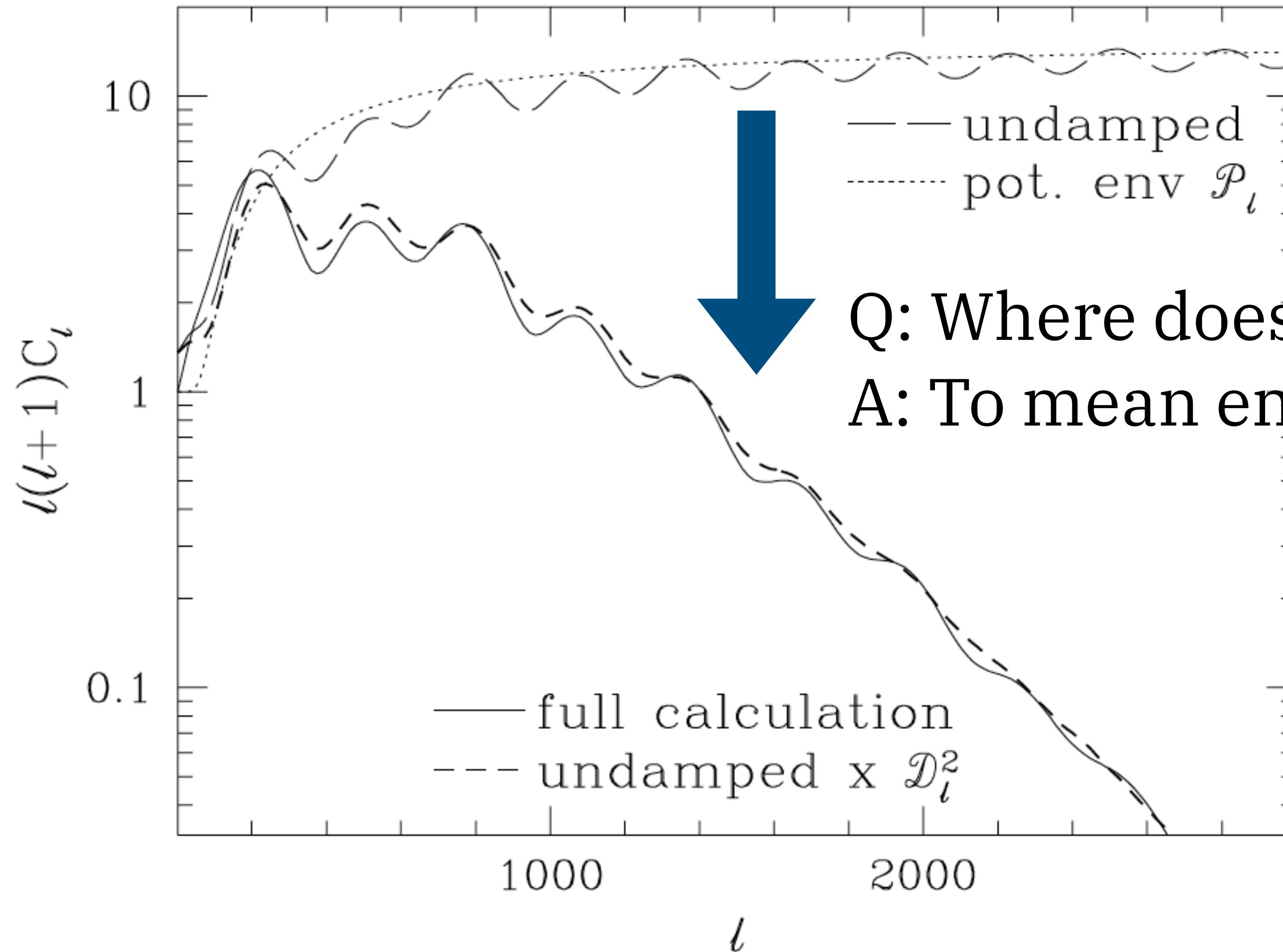


CMB spectrum and energy injection



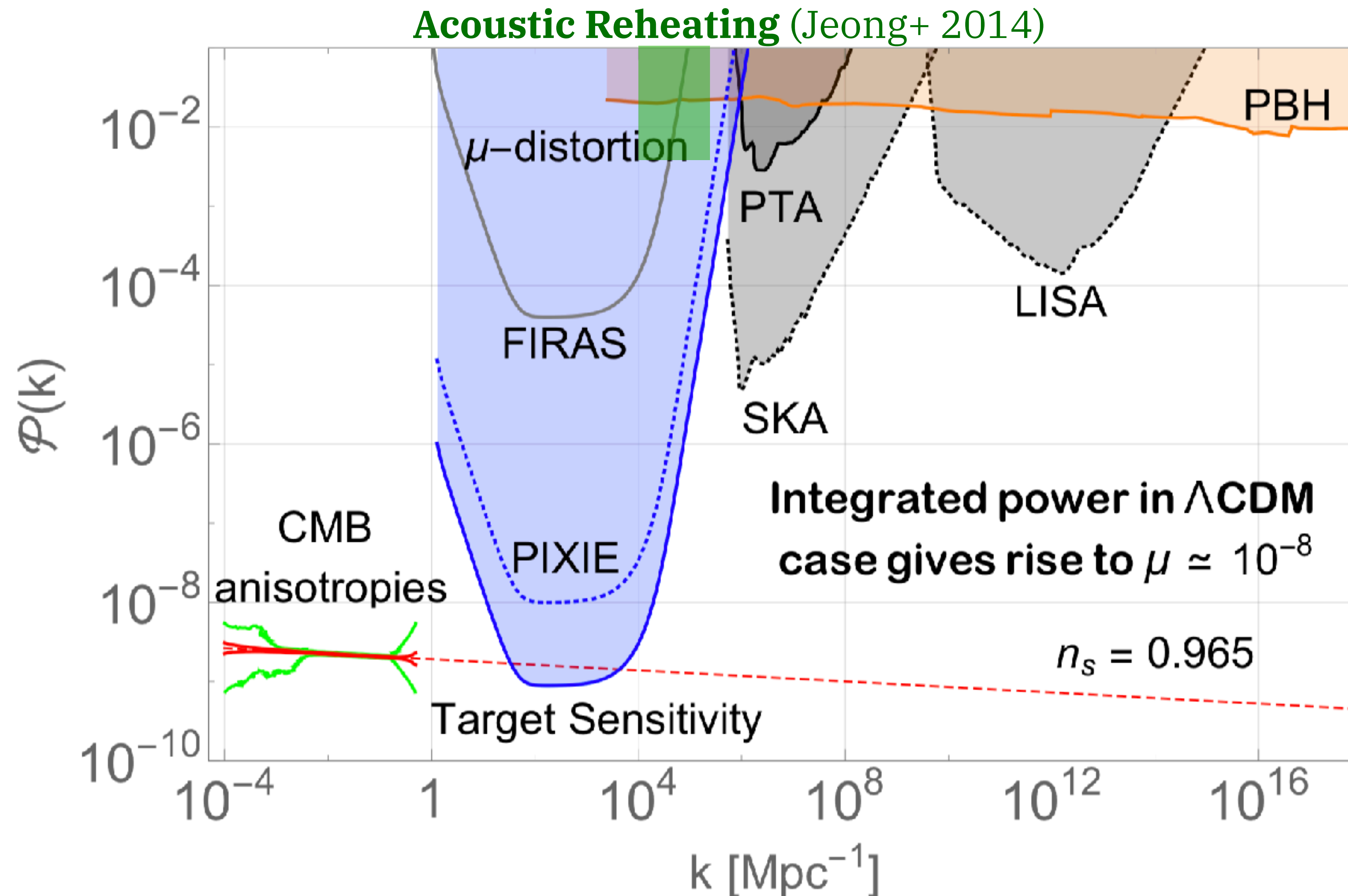
Silk damping to heat up the spectrum

Hu & White 1997



Q: Where does the acoustic energy go?
A: To mean energy spectrum

μ -distortion can probe small-scales



Primordial GW (PGW)

- de Sitter spacetime generates stochastic gravitational waves with amplitude of (here, $m_{\text{pl}} = \sqrt{G_N}$):

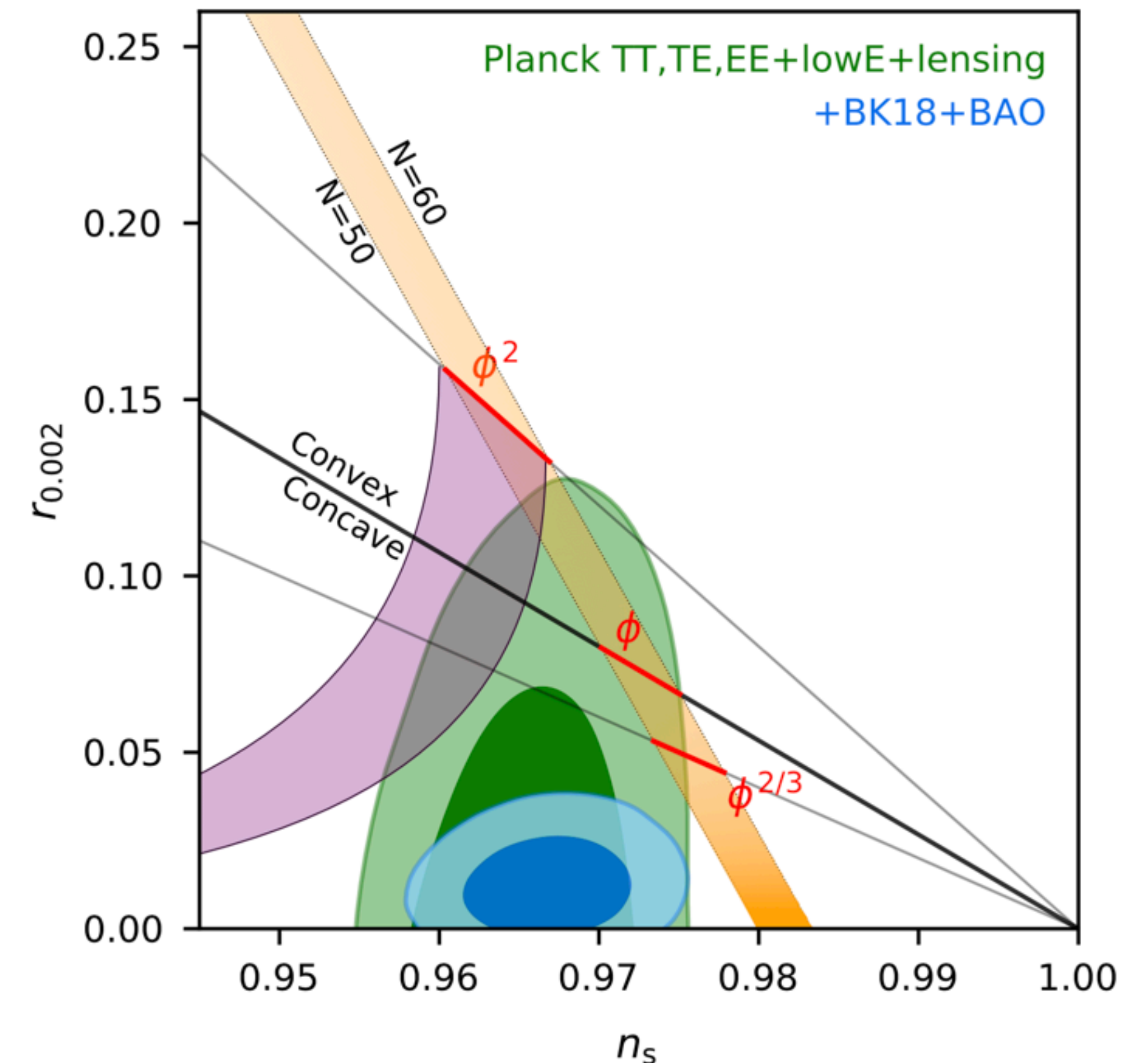
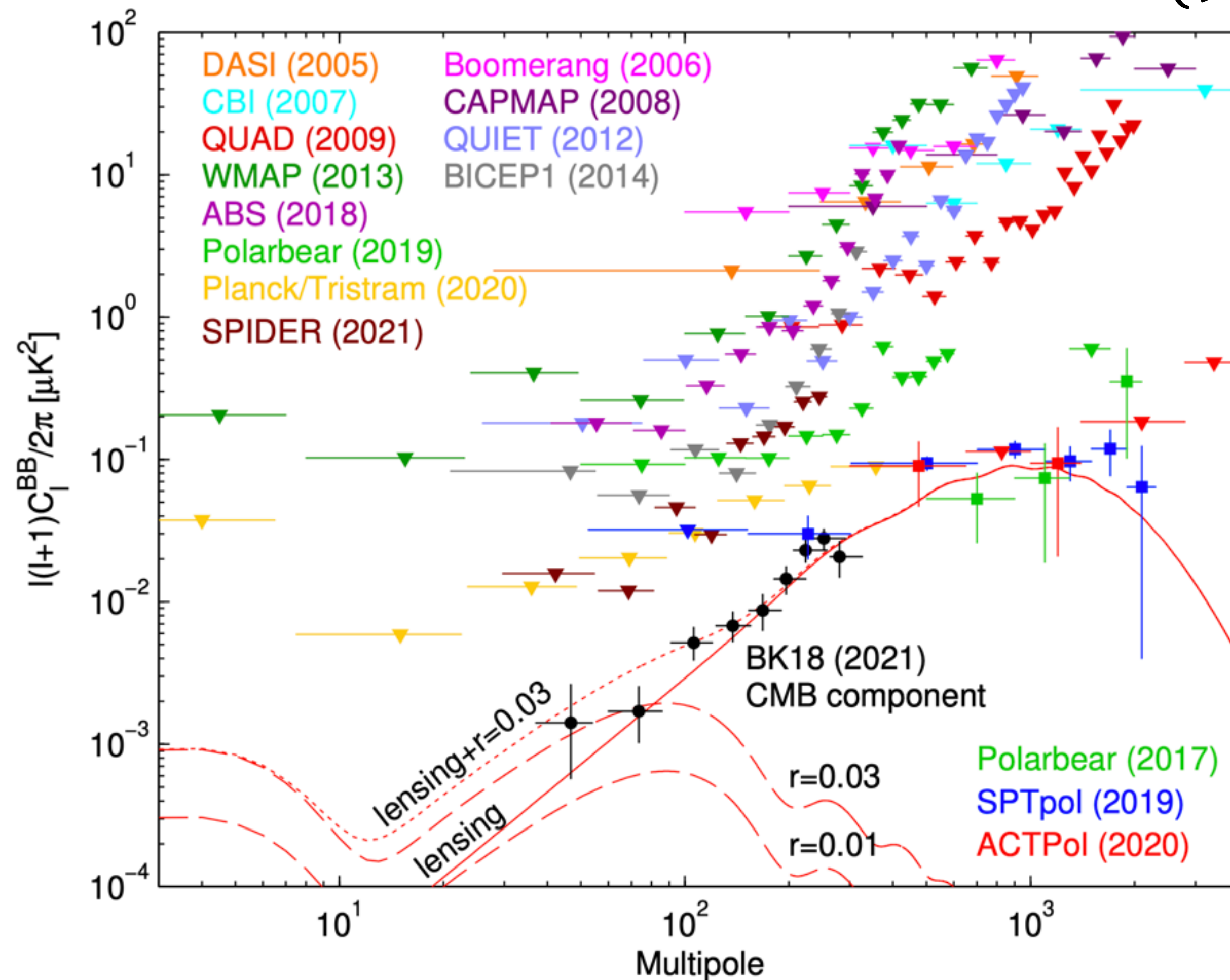
$$\Delta_h^2(k) = \frac{k^3 P_T(k)}{2\pi^2} = \frac{64\pi}{m_{\text{pl}}^2} \left(\frac{H}{2\pi} \right)^2 \Big|_{k=aH}$$

+ Friedmann equation: $3H^2 \sim 8\pi G\rho$

- ***PGW = energy scale*** of inflation: $E \sim (r/0.01)^{1/4} 10^{16} \text{GeV!}$
- ***PGW = expansion rate*** during inflation: *the proof of inflation!*

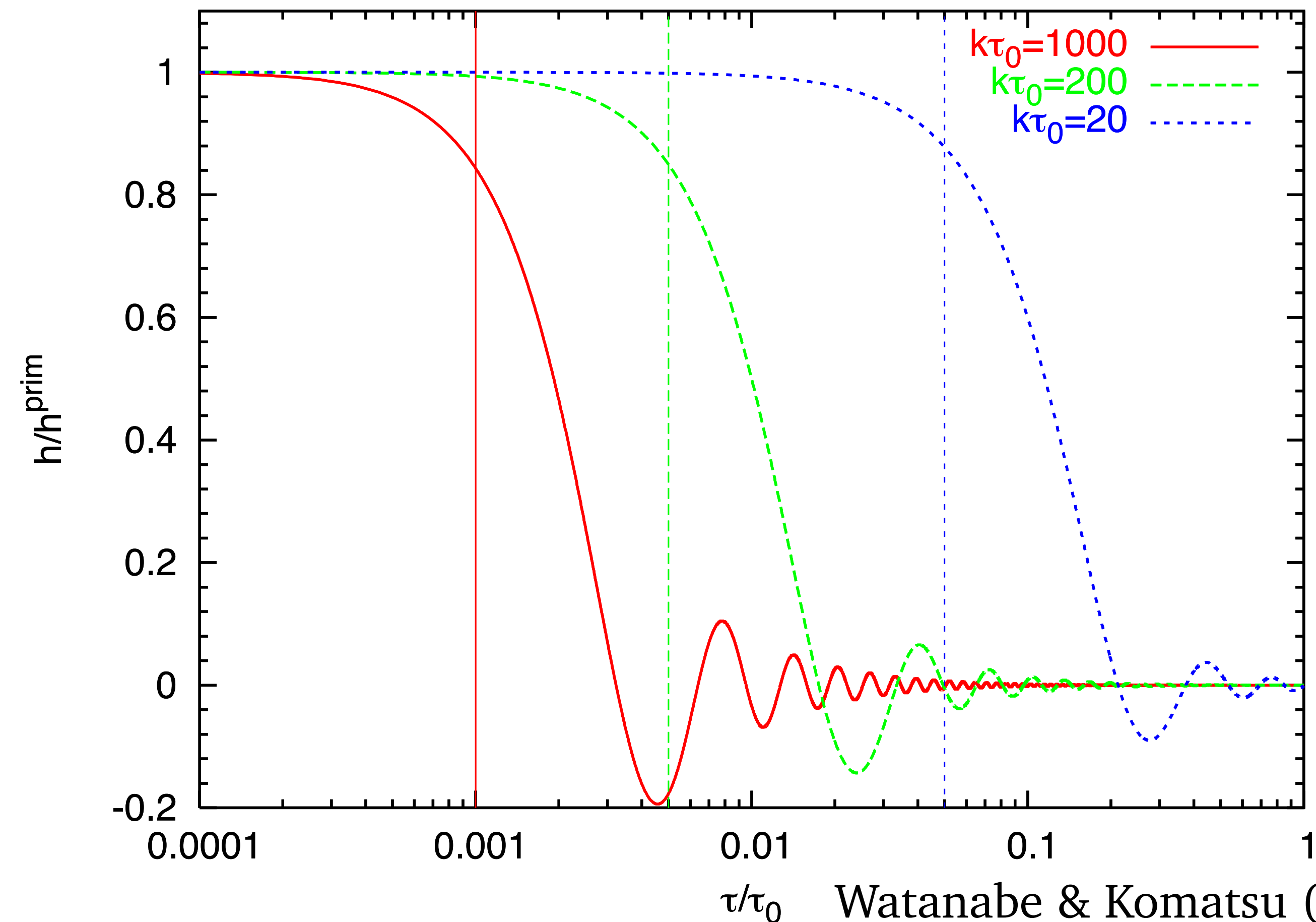
B-mode polarization, status

$r < 0.036$ (95% C.L.)



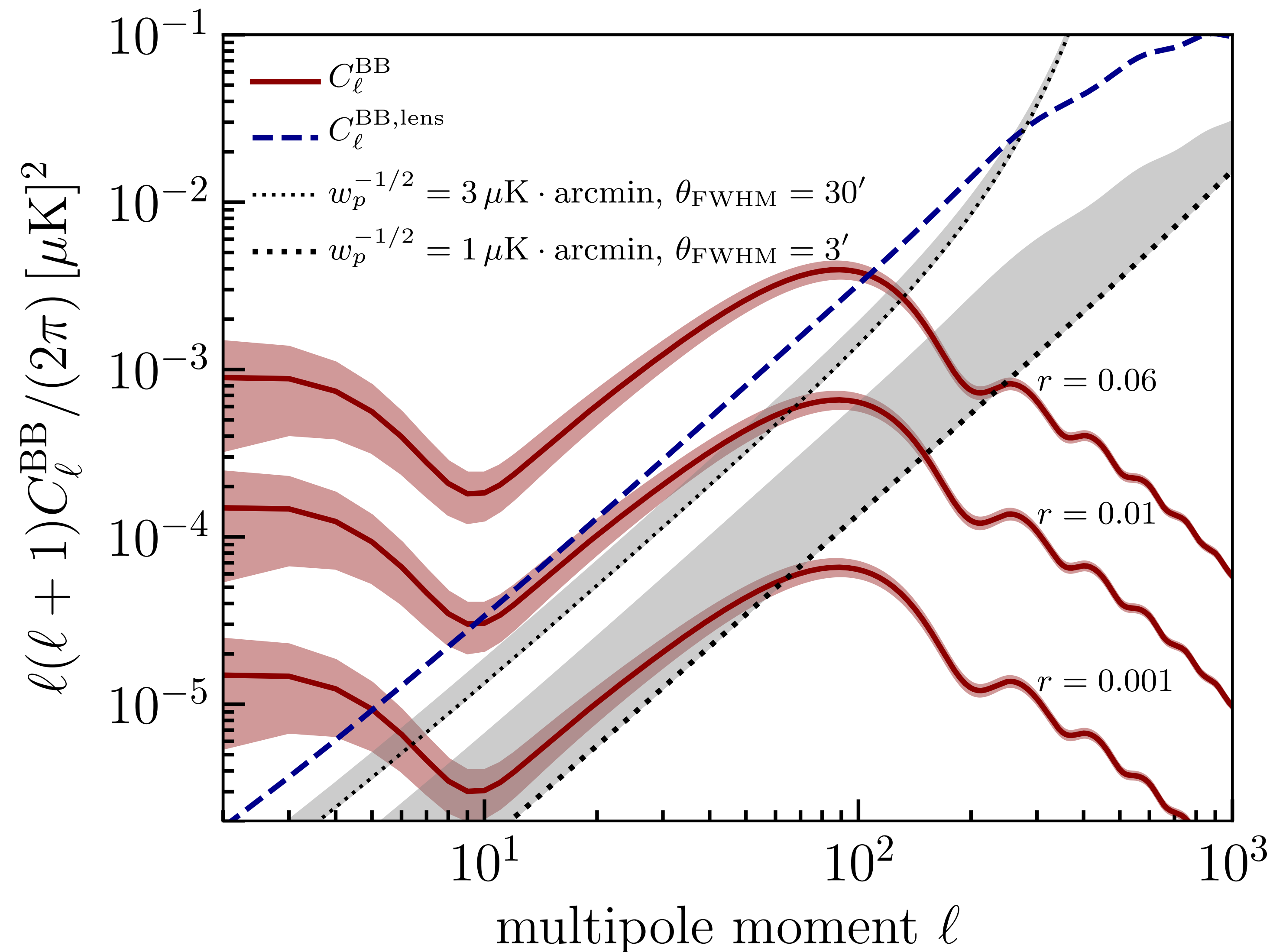
Evolution of PGW w/o sources

$$-\square h_{ij} = h_p''(\mathbf{k}) + 2\mathcal{H}h_p'(\mathbf{k}) + k^2 h_p(\mathbf{k}) = 0$$

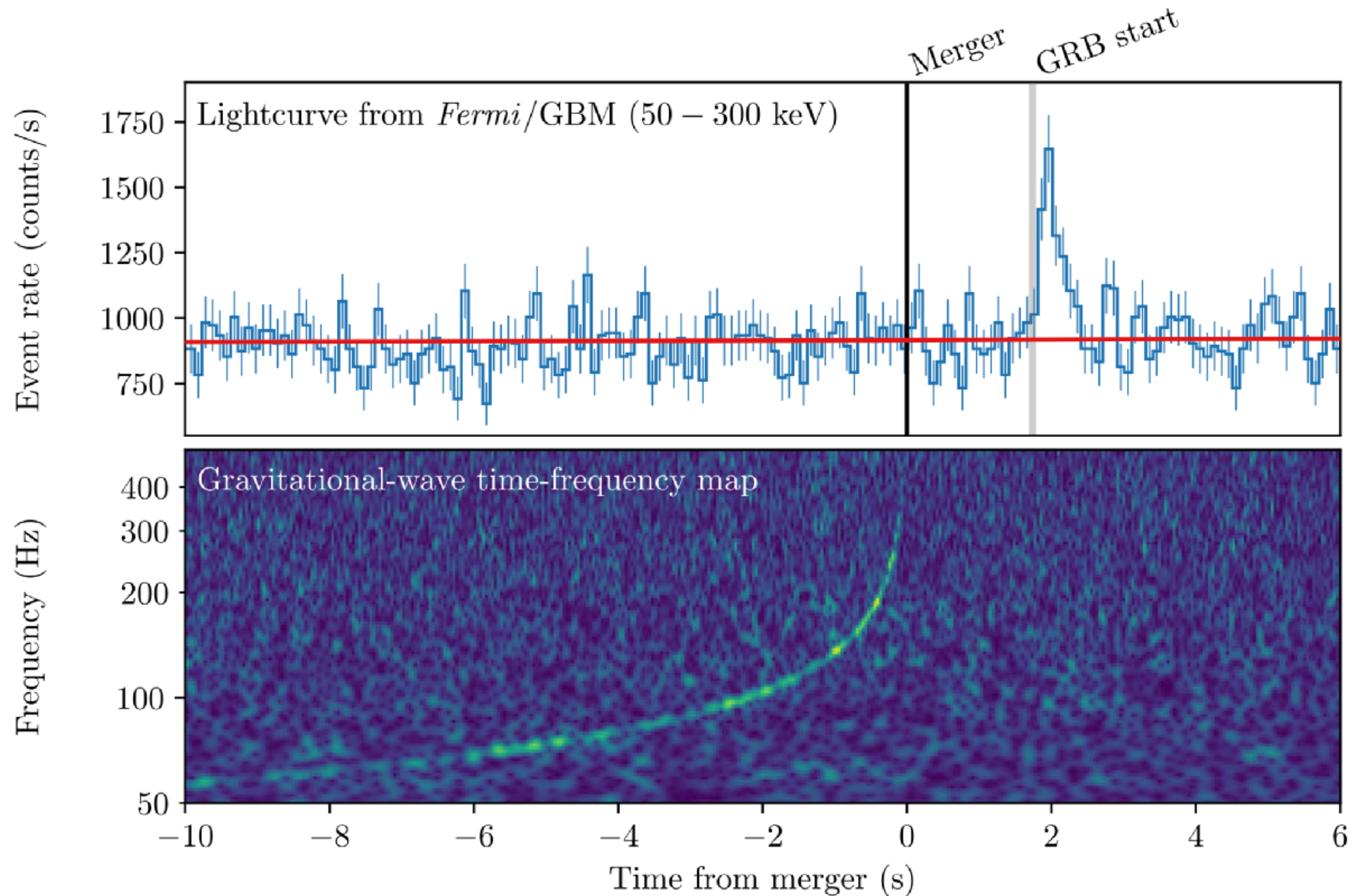


- **PGW** stays constant outside of horizon, but **decays** once the mode enters the horizon.
- *cf.* **scalar perturbations grow** inside of horizon.

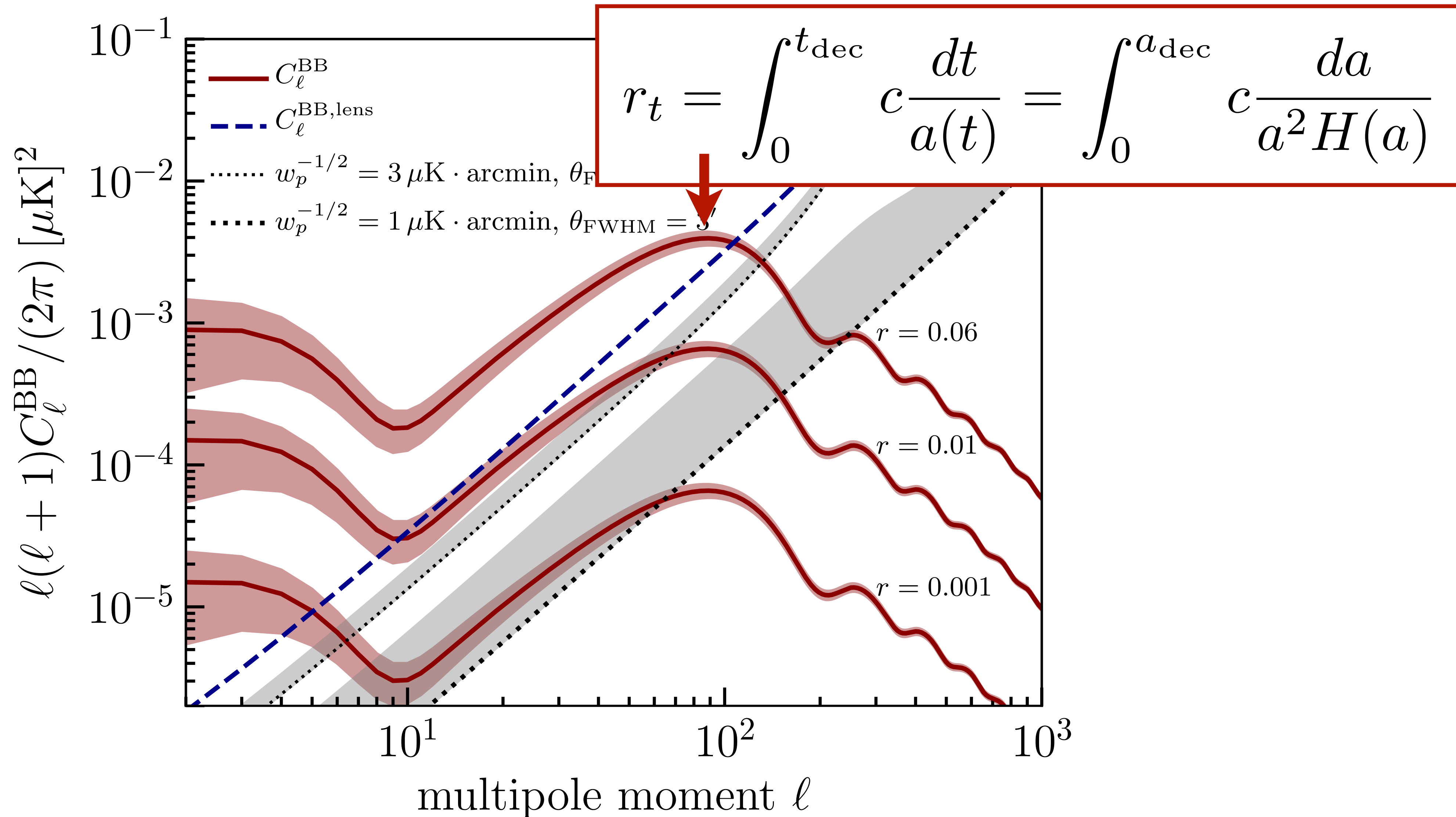
B-mode power spectrum



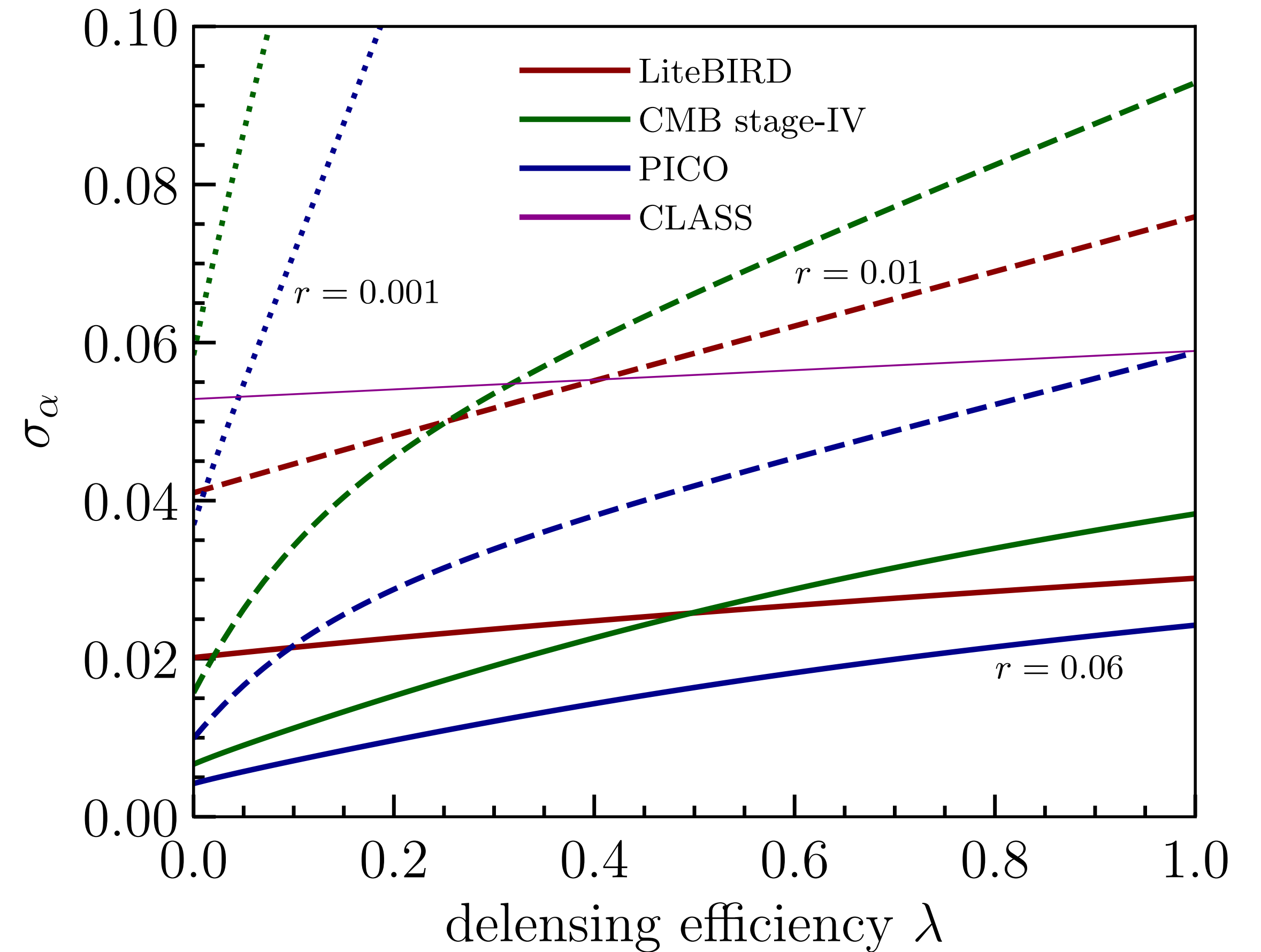
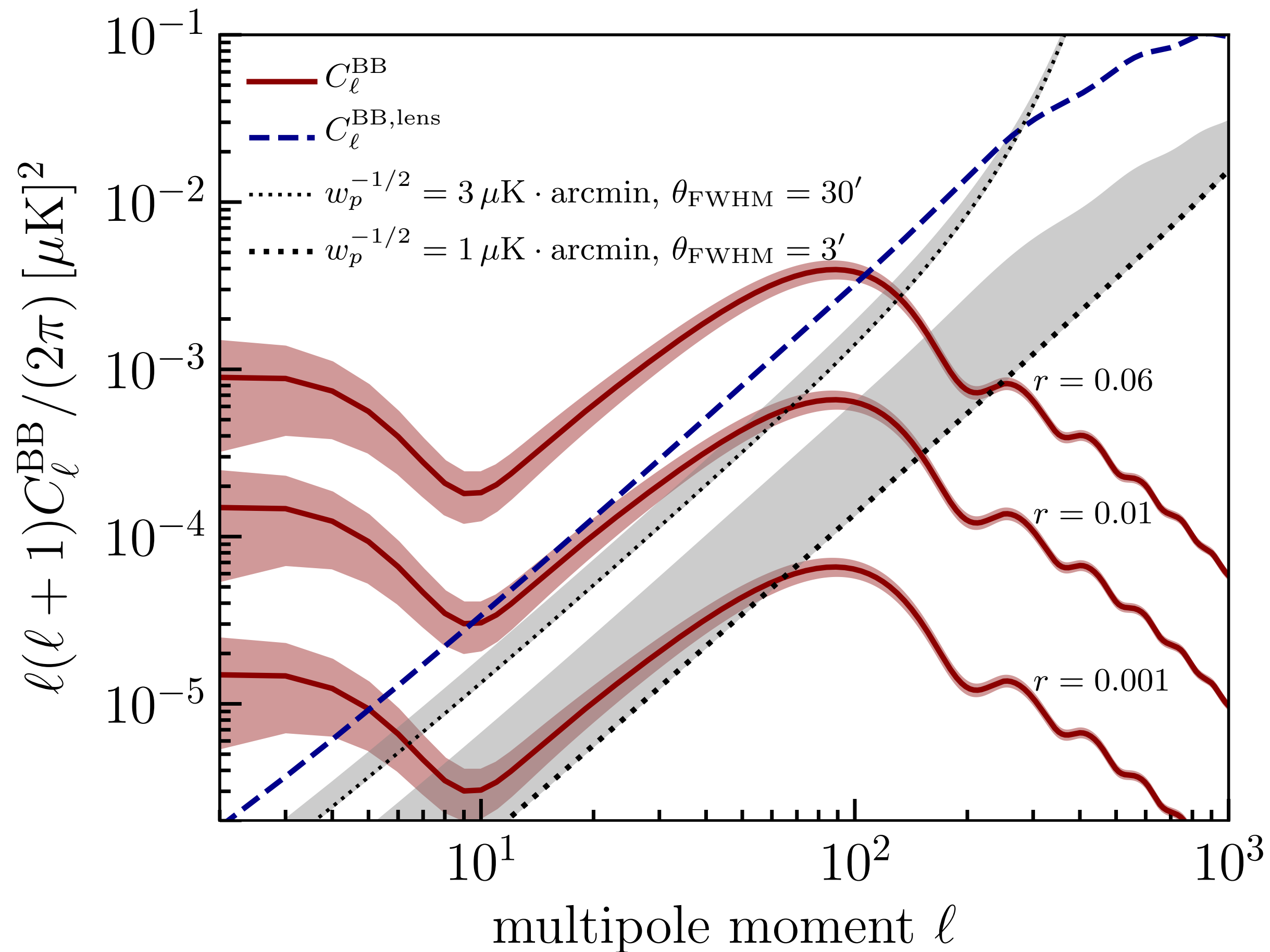
GW170817 and GRB 170817A



Turn-over scale r_t



We can measure r_t , if $r > 0.001$!

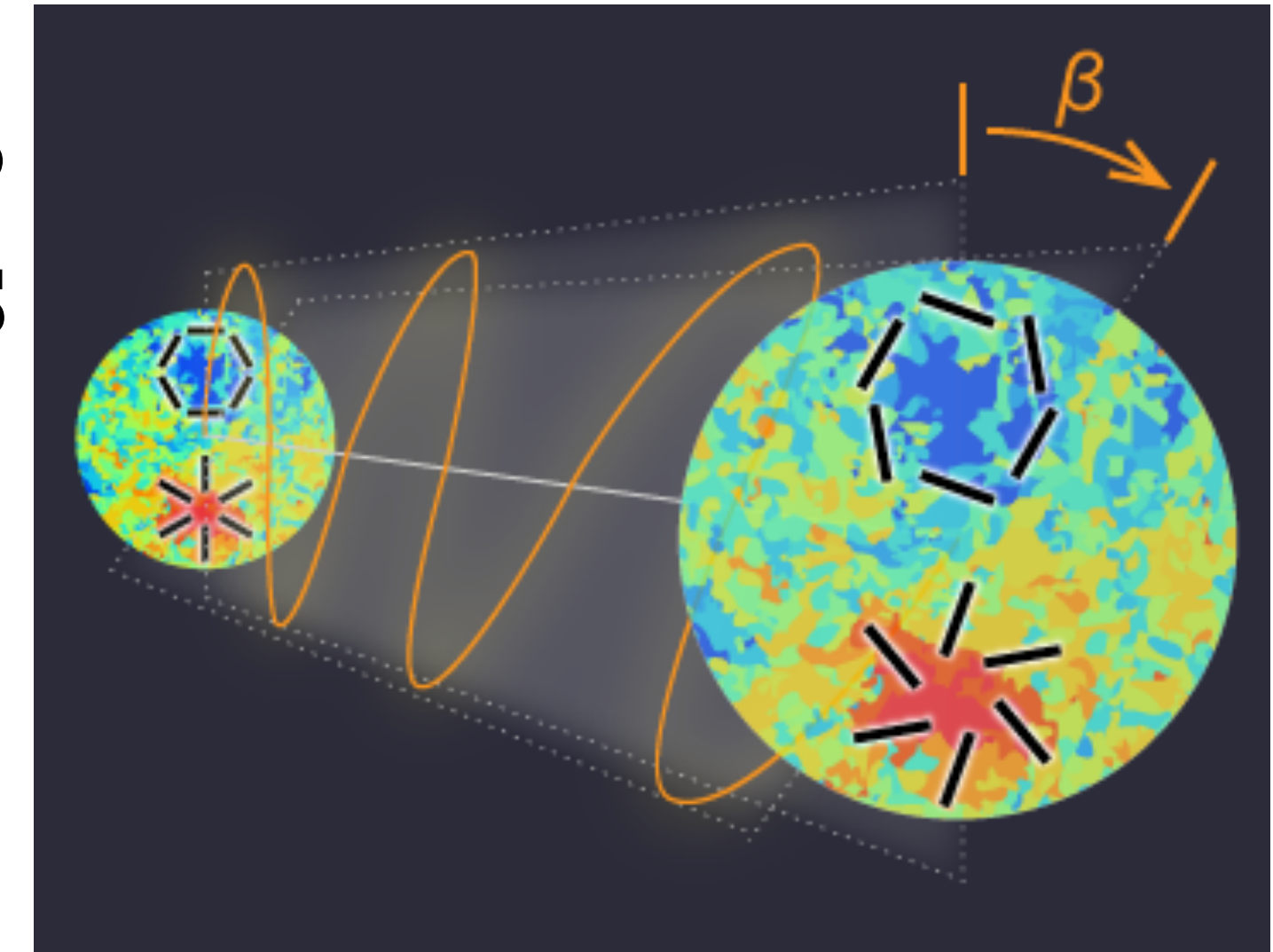


The Cosmic Birefringence

E $\leftrightarrow$ B conversion by rotation of the linear polarization plane

- The intrinsic EE, BB, and EB power spectra 13.8 billion years ago would yield the observed EB as

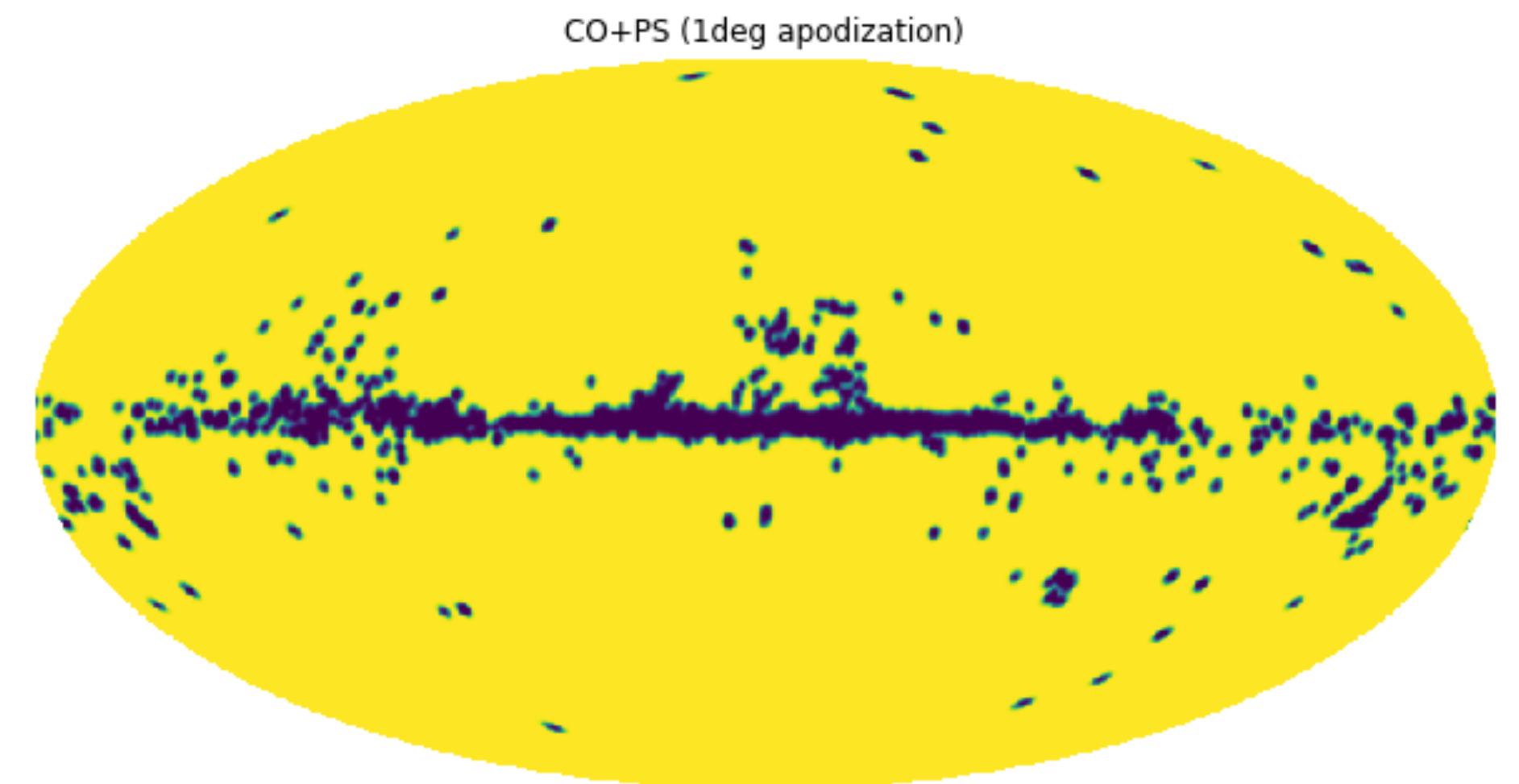
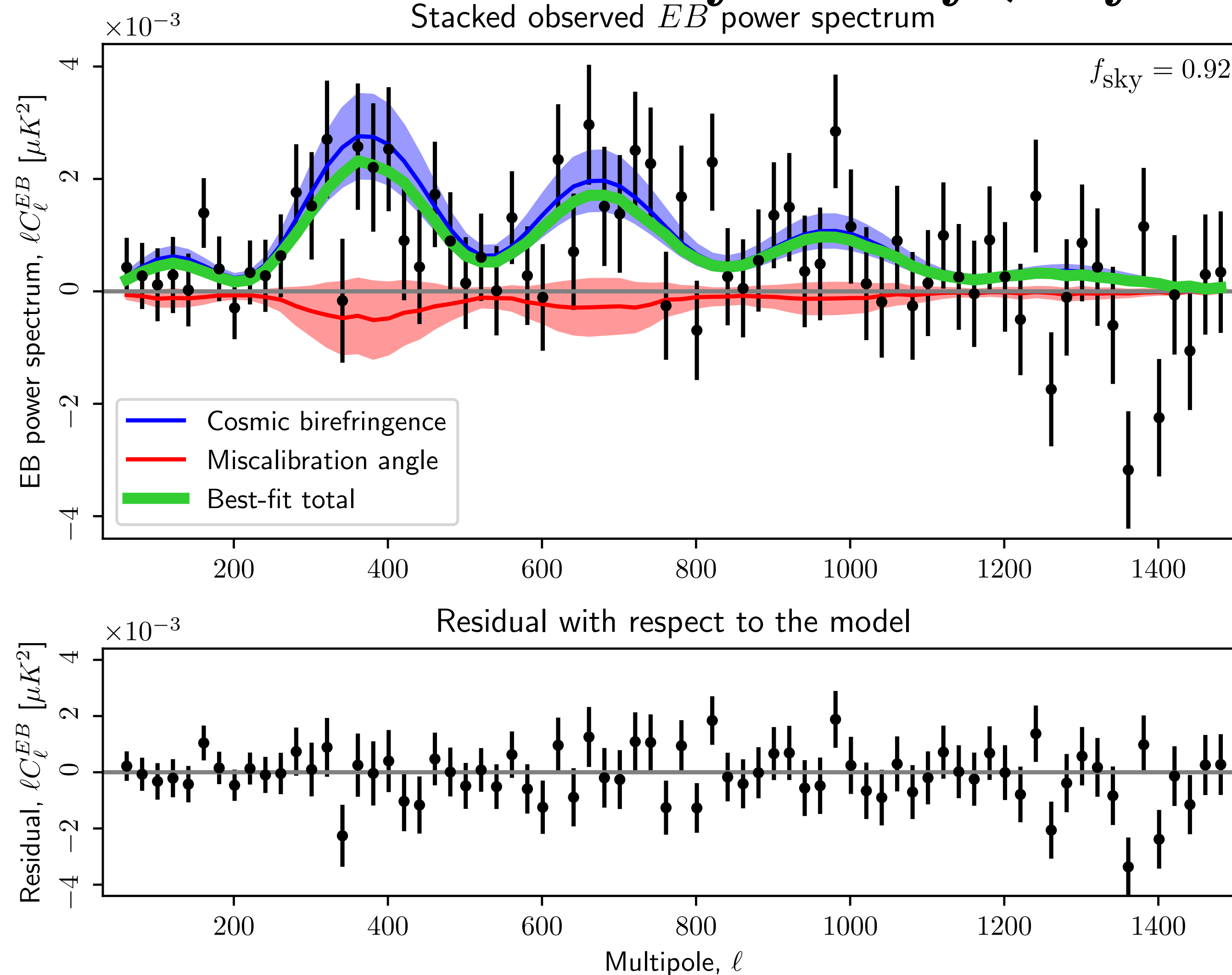
$$C_{\ell}^{EB,\text{obs}} = \frac{1}{2} (C_{\ell}^{EE} - C_{\ell}^{BB}) \sin(4\beta) + C_{\ell}^{EB} \cos(4\beta)$$



- One would find β by fitting $C_{\ell}^{EE,\text{CMB}} - C_{\ell}^{BB,\text{CMB}}$ to the observed $C_{\ell}^{EB,\text{obs}}$ using the best-fitting CMB model, and assuming the intrinsic EB to vanish, $C_{\ell}^{EB}=0$.

Cosmic Birefringence in WMAP+Planck

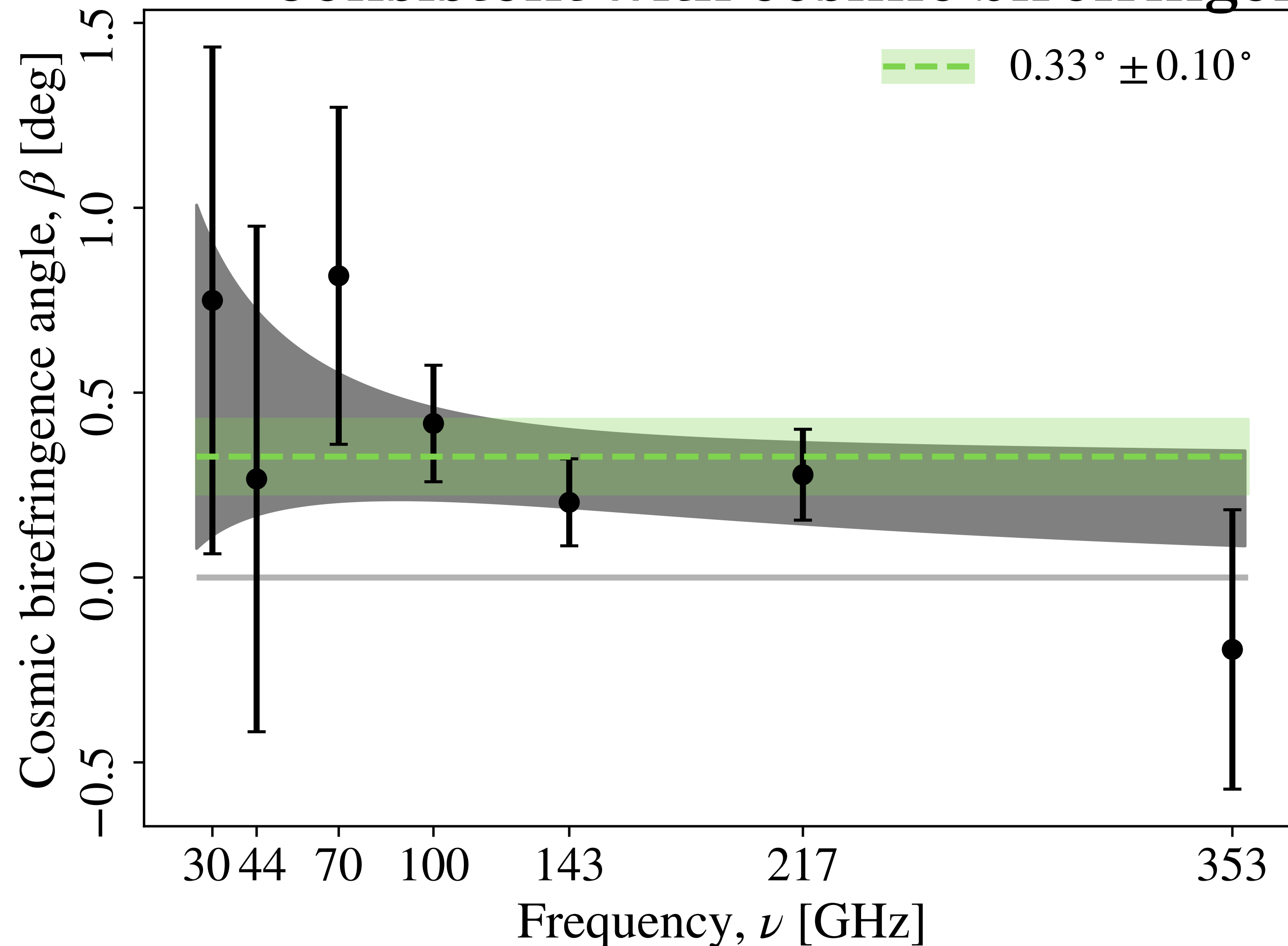
Nearly full sky ($f_{\text{sky}} = 92\%$) analysis



- Mis-calibration angles** make only small contributions thanks to the cancellation.
- $\beta = 0.34 \pm 0.09$ deg **3.6 σ !!**
- $\chi^2 = 65.3$ for DOF=72

No strong frequency dependence

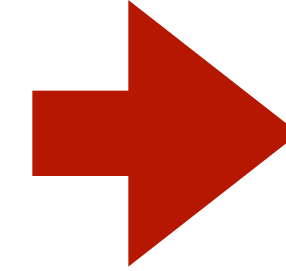
Consistent with cosmic birefringence due to $\mathcal{L} \ni \theta F \tilde{F}$



- No evidence for frequency dependence:
- For $\beta \sim (\nu/150\text{GHz})^n$,
 $\mathbf{n} = -0.20^{+0.41}_{-0.39}$ (68% CL)
- Faraday rotation ($n=-2$) is disfavored.

Kinetic coupling with Dark-U(1)?

$$\mathcal{L} = -\frac{1}{4}\hat{F}^{\mu\nu}\hat{F}_{\mu\nu} - \frac{1}{4}\hat{F}_X^{\mu\nu}\hat{F}_{X\mu\nu} - \frac{\varepsilon}{2}\hat{F}_{\mu\nu}\hat{F}_X^{\mu\nu}$$



$$\beta_\nu \propto \varepsilon \sqrt{\frac{I_{D\gamma}}{I_{\text{CMB}}}} \sin \beta_{D\gamma}$$

- The frequency dependence is weak as long as $T_{\text{dark-U(1)}} \lesssim T_{\text{CMB}}$.
- Dark recombination preceded the baryonic recombination:
 - Unless we have a strong coupling to correlate the polarization of dark U(1) at dark recombination to the CMB's linear polarization, the relative linear polarization is *random*.
 - The random angle removed the average birefringence signal.
 - Leading contribution = Spectral distortion and $\langle \text{EEBB} \rangle$ trispectrum.

Summary & Conclusion

- With WMAP and Planck, the CMB has been providing most accurate measurement of cosmological parameters.
- The CMB is still a valuable source of clues for puzzles that we are facing now. Three examples:
 - Amplitude of small-scale power spectrum from spectral distortion
 - B-mode polarization turn-over for testing early dark energy models
 - EB cross correlation for possible parity breaking signatures