

Constraining the key reaction rates using indirect methods

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Outline

- ☑ Introduction: indirect techniques in nuclear astrophysics
- ☑ The $^{22}\text{Ne}(\alpha, n)$ conundrum
- ☑ Hassle around the triple-alpha reaction
 - 📌 Radiative width of the Hoyle state
 - 📌 Neutrons assisted carbon nucleosynthesis

Indirect methods

- ☑ Indirect method: when the reaction of interest (1) for astrophysics is too difficult or impossible to measure directly, use a different (“easier”) reaction (2) that informs the reaction of interest.
- ☑ Application of a model to go from (2) to (1) is often required.
- ☑ The less model-dependent the technique, the better.

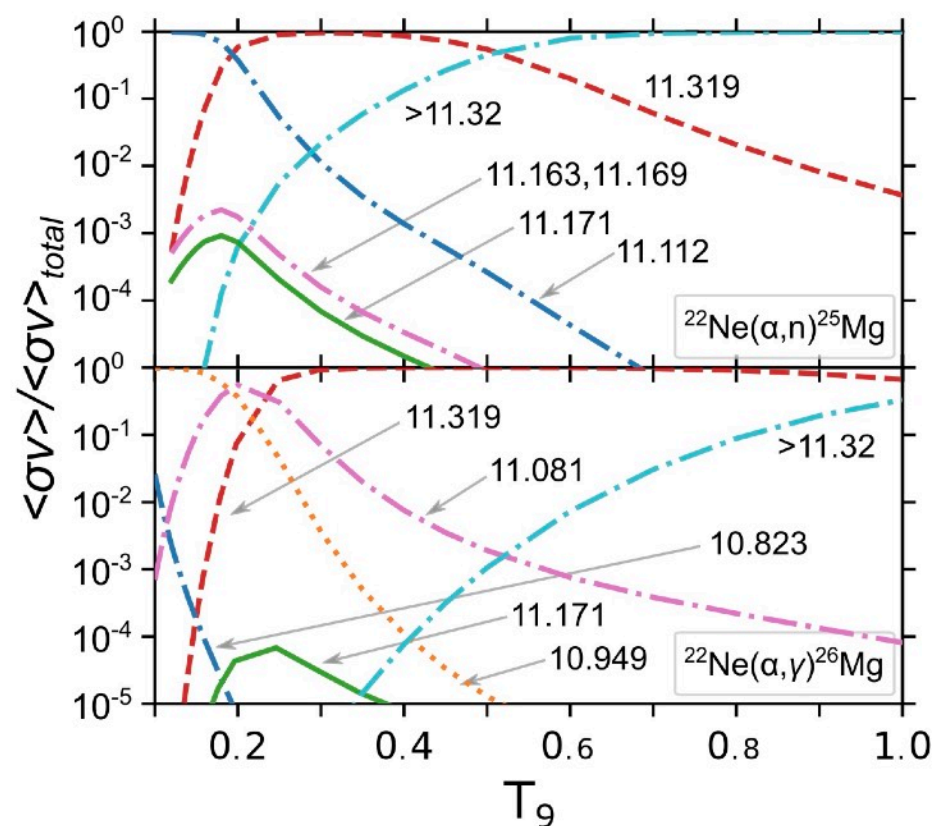
Indirect methods

- ☑ Constraints on (p,γ) , (α,γ) , (n,γ) , pycnonuclear fusion, (α,p) , and many others can be obtained indirectly
- ☑ Incomplete list of indirect methods
 - 📌 Transfer or inelastic scattering reactions
 - 🌐 Spectroscopic factors / **ANCs**
 - 🌐 Trojan Horse Method
 - 🌐 surrogate
 - 🌐 Oslo
 - 🌐 **Branching ratios**
 - 📌 Coulomb dissociation
 - 📌 **Time-reverse reactions**
 - 📌 β -delayed charge particle spectroscopy / β -Oslo

The $^{22}\text{Ne}(\alpha, n)$ conundrum

$^{22}\text{Ne}(\alpha, n)$ - neutron source for s-process

- $^{22}\text{Ne}(\alpha, n)$ is the neutron source for the weak branch of the s-process
- final abundances of some s-process elements depend on this reaction rate (NIC, Section 1.2 and 2)
- One ^{26}Mg resonance dominates the $^{22}\text{Ne}(\alpha, n)$ at $T_9 > 0.2$, the 11.32 MeV



11.32 MeV resonance in ^{26}Mg

$$\omega\gamma_{(\alpha,\gamma)} = 37(4)\mu\text{eV}$$

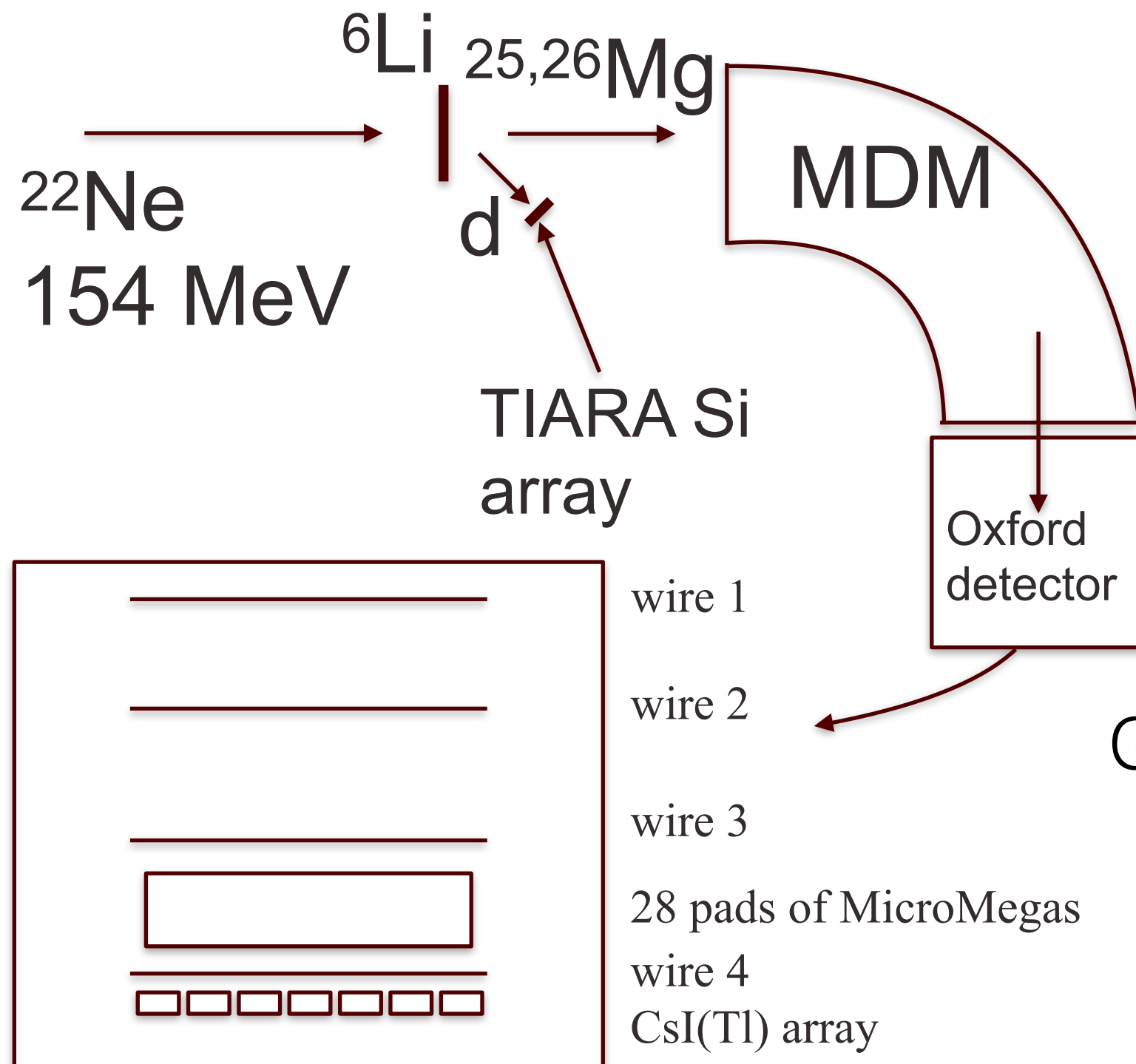
$$\omega\gamma_{(\alpha,\gamma)} \approx (2J + 1) \frac{\Gamma_{\alpha}}{1 + \Gamma_n/\Gamma_{\gamma}}$$

$$\omega\gamma_{(\alpha,n)} \approx (2J + 1) \frac{\Gamma_{\alpha}}{1 + \Gamma_{\gamma}/\Gamma_n}$$

$$\frac{\omega\gamma_{(\alpha,\gamma)}}{\omega\gamma_{(\alpha,n)}} = \frac{\Gamma_{\gamma}}{\Gamma_n}$$

So, one only needs to measure the γ/n BR

BR using ${}^6\text{Li}({}^{22}\text{Ne},d)$



G. Christian



S. Otta

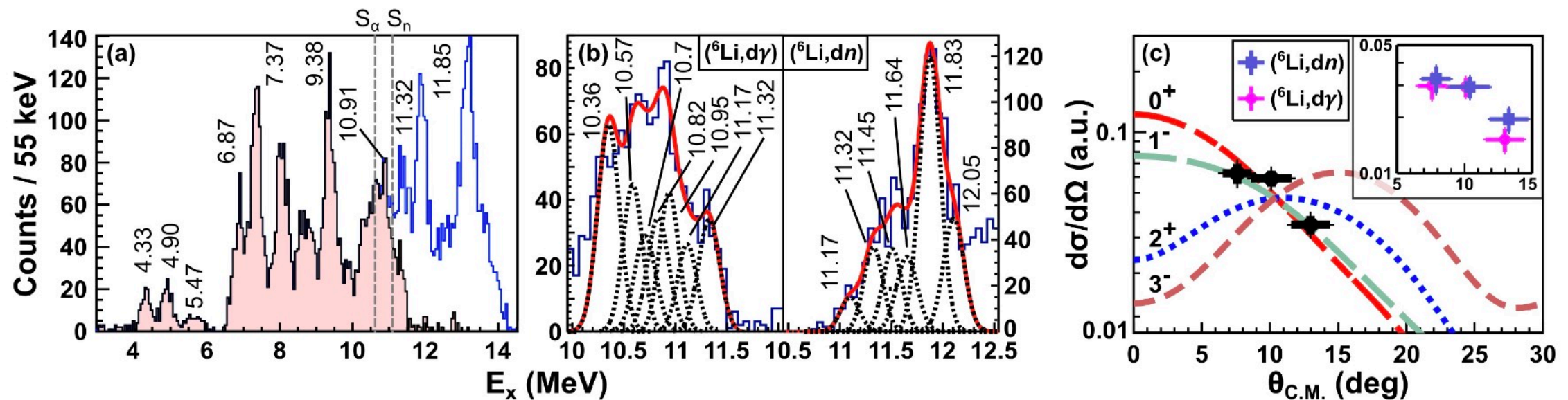
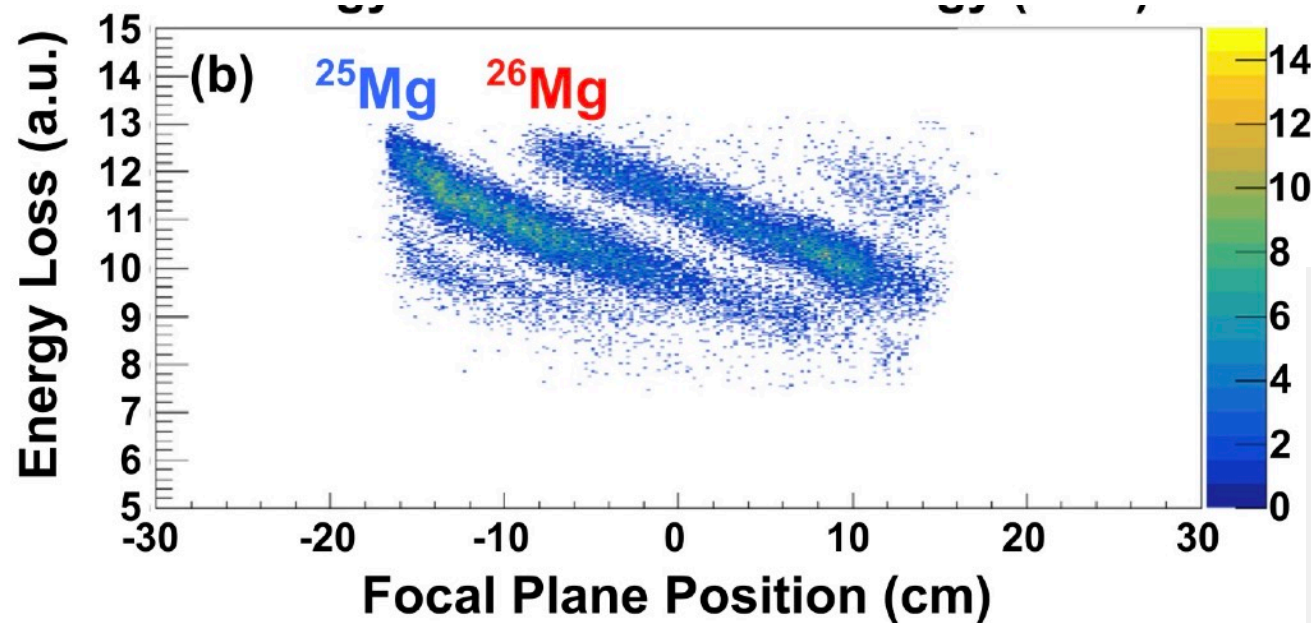
11.32 MeV γ/n BR

$$\Gamma_n/\Gamma_\gamma = 1.14(26)$$

$$\omega_{\gamma(\alpha,n)} = 42(11)\mu\text{eV}$$

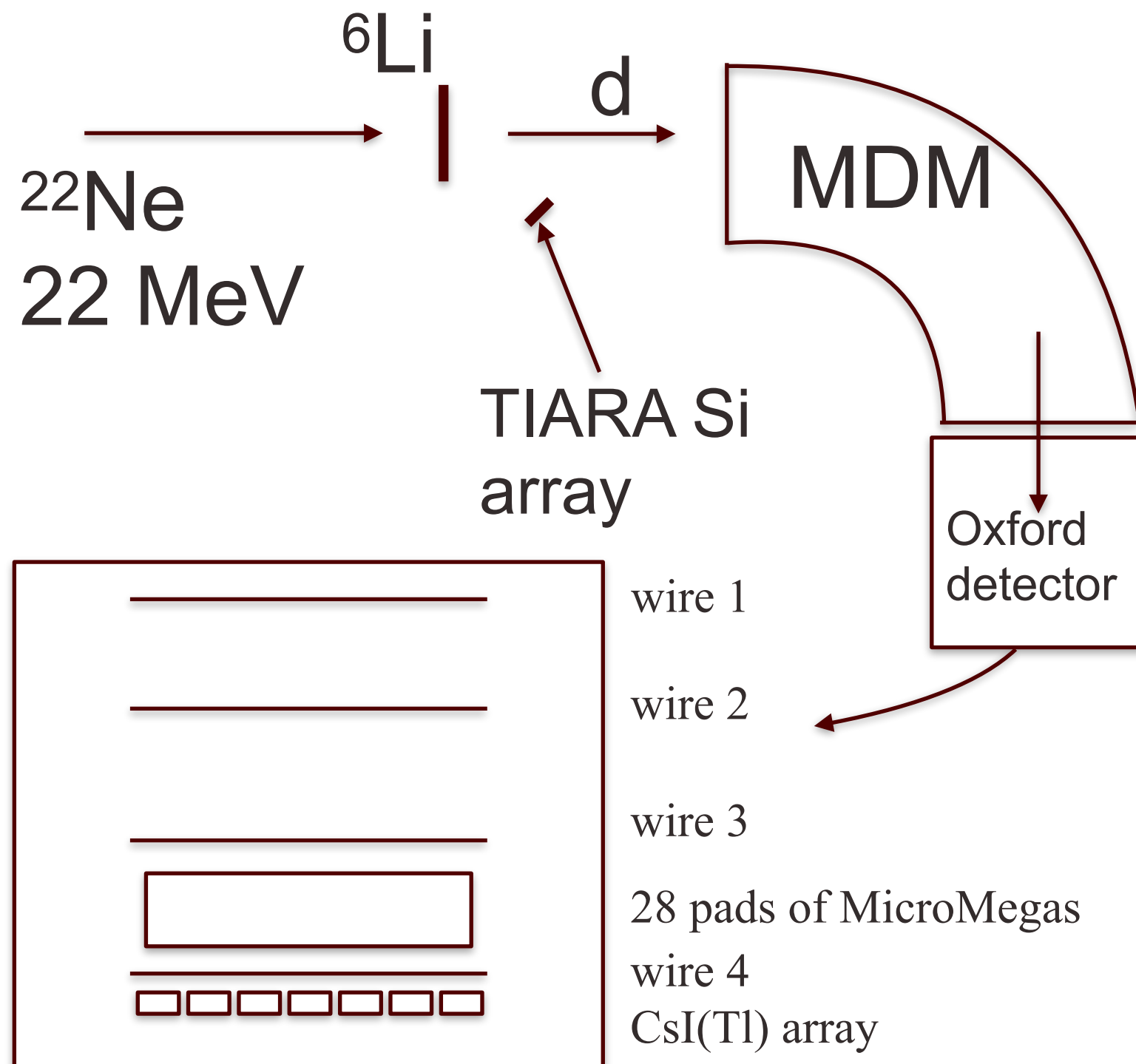
$$\Gamma_\alpha = 79(13)\mu\text{eV}$$

if 0^+



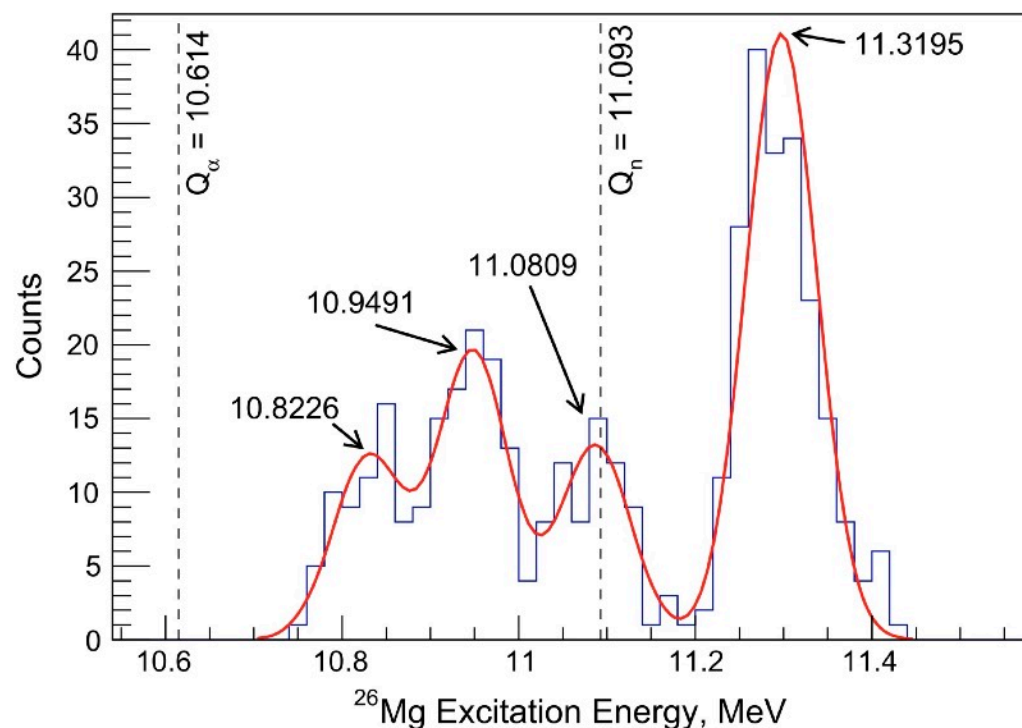
S. Ota, et al., PLB, 802 (2020)

sub-Coulomb ${}^6\text{Li}({}^{22}\text{Ne},d)$



H. Jayatissa

- ☑ Perform (${}^6\text{Li}, d$) α -transfer reaction at sub-Coulomb
- ☑ Extract ANC instead of SF factors
- ☑ Almost independent of the result on optical model parameters of the DWBA calculations, the number of nodes in the cluster wave function or the shape of the form factor
- ☑ The angular distribution is flat.



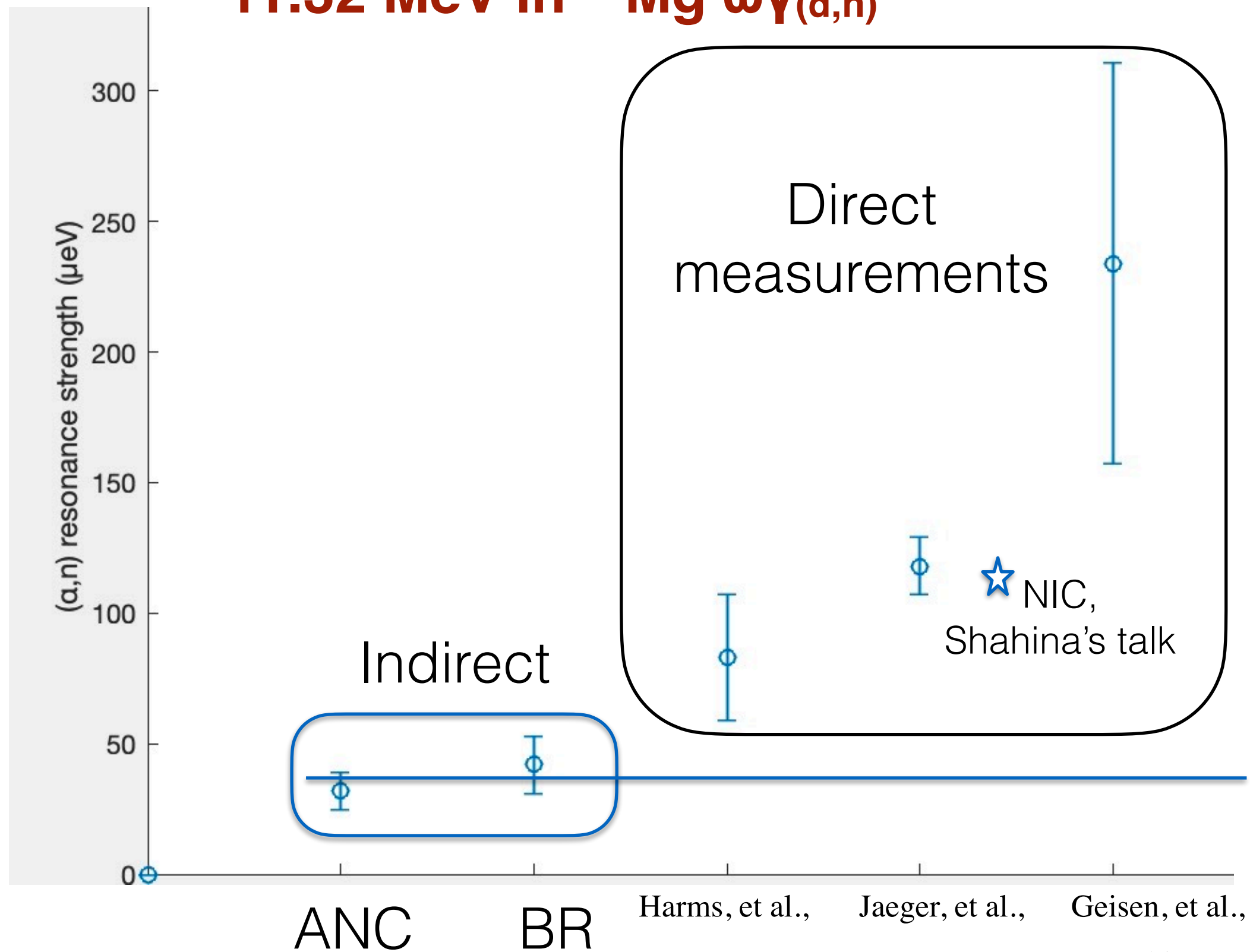
$$C^2 = \frac{2\mu R}{\hbar^2 W_{-\eta, l+1/2}^2(2kR)} \frac{\gamma^2}{1 + \gamma^2 \frac{dS}{dE}}$$

$$\Gamma_\alpha = \frac{2\gamma^2 P}{1 + \gamma^2 \frac{dS}{dE}}$$

$$\Gamma_\alpha = 61(14) \mu\text{eV} \text{ if } 0^+$$

BR gives 79(13) μeV

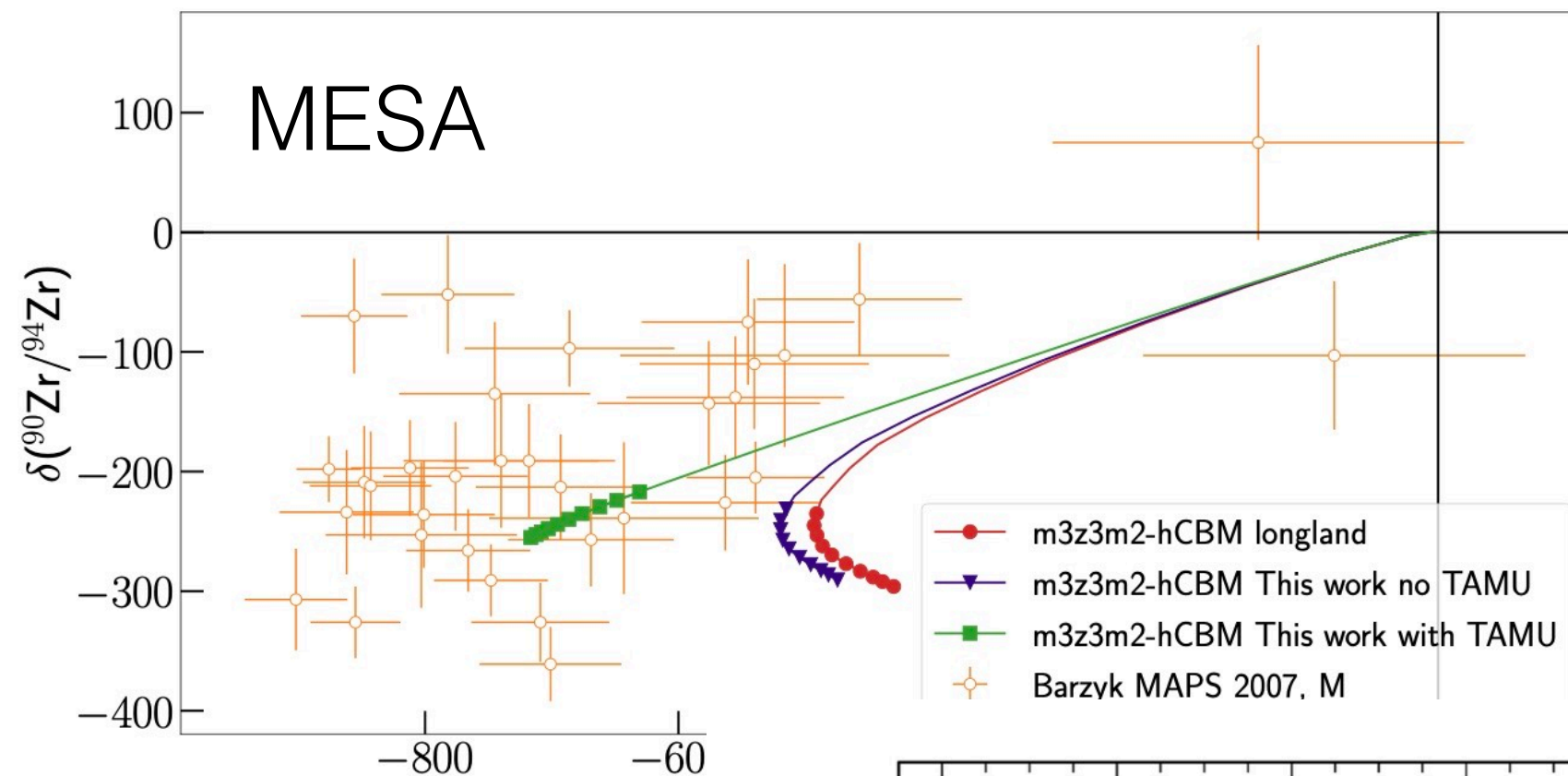
11.32 MeV in ^{26}Mg $\omega\gamma_{(\alpha,n)}$



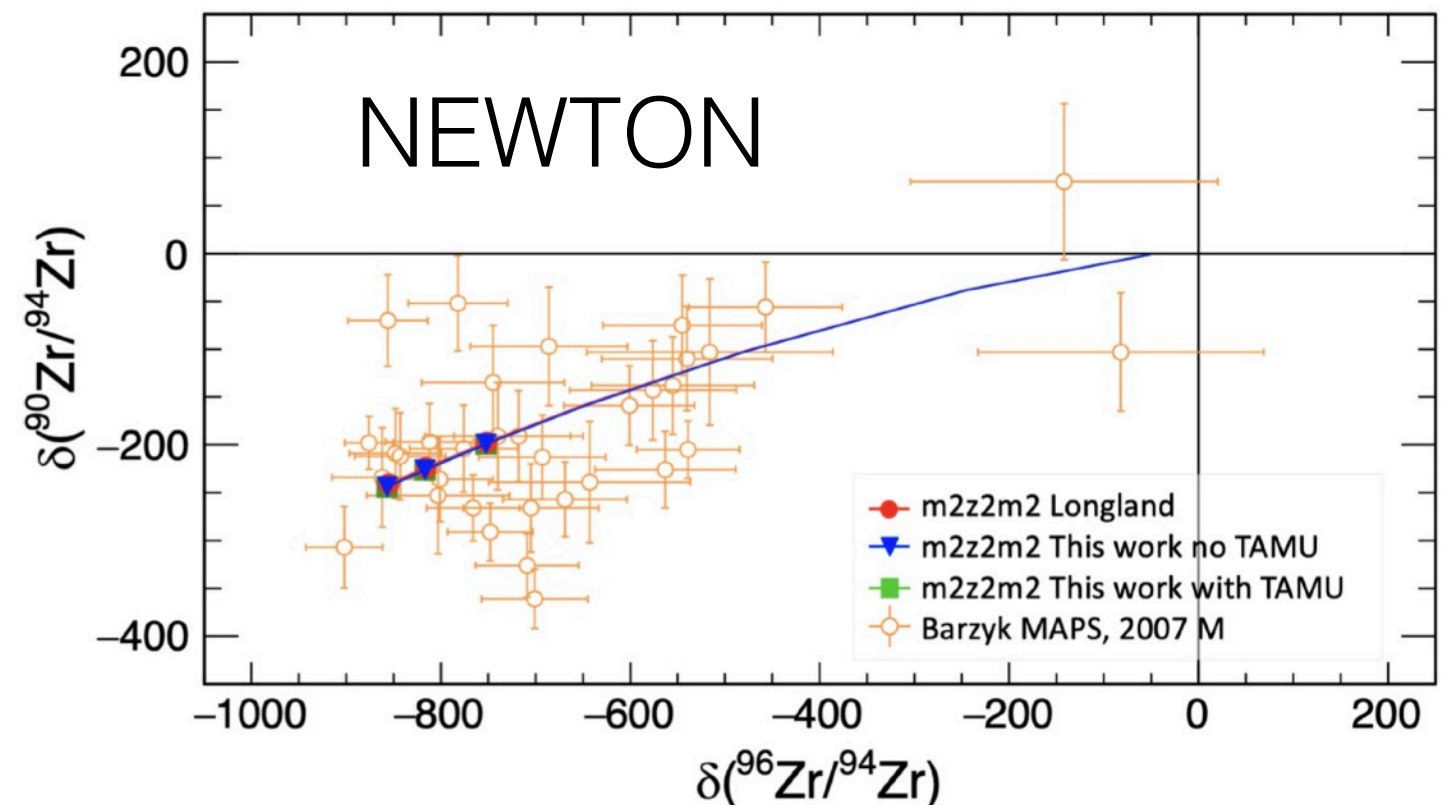
Harms, et al., PRC 43 (1991).
Jaeger, et al., PRL 87 (2001).
Geisen, et al., NPA 561 (1993).



Zr isotopic ratios from premolar SiC grains



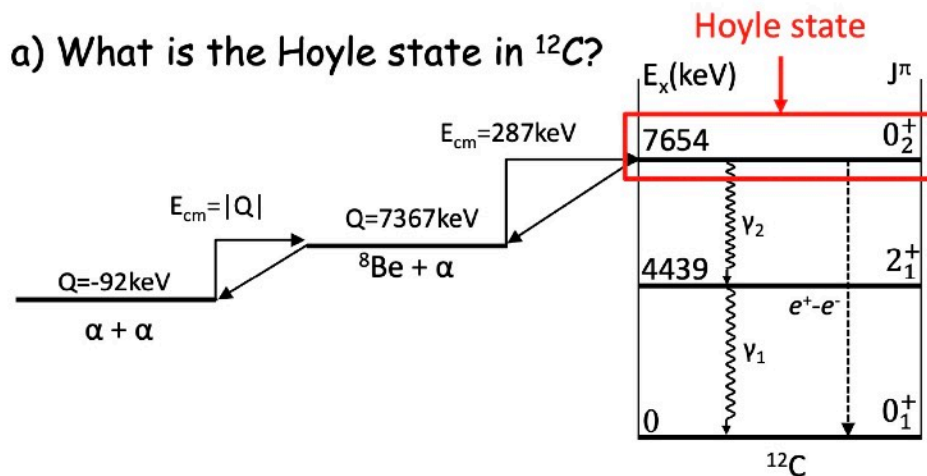
P. Adsley, et al.,
PRC 103, 015805 (2021)



Radiative width of the Hoyle state

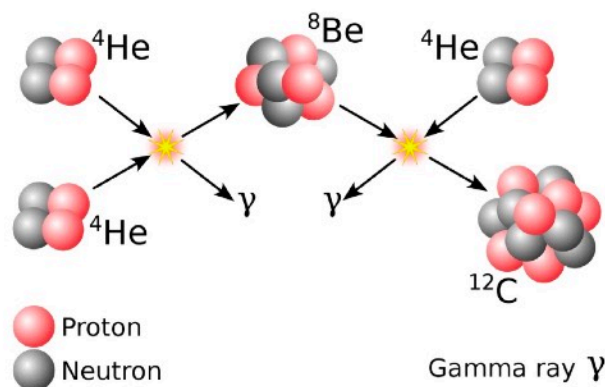
Radiative width of the Hoyle state

a) What is the Hoyle state in ^{12}C ?



b) Nuclear physics:

- ^{12}C is produced via $2\alpha \rightleftharpoons {}^8\text{Be}(\alpha, \gamma){}^{12}\text{C}$ (3α -process) in star formation.
- ${}^8\text{Be}$ is known to be unbound to 2α -decay with a lifetime of about 10^{-16}s .
- $\alpha + {}^8\text{Be} \rightleftharpoons {}^{12}\text{C}$ equilibrium (Γ_α) is broken by the small leakage (1 in 2500 cases) to the ^{12}C ground state facilitated by the radiative branches; either two γ -decay (Γ_γ) or e^+e^- pair production (Γ_π).



c) Astrophysics:

- The reaction rate of 3α -process $\langle \sigma v \rangle \propto \omega \gamma \exp\left(-\frac{E_R}{hT}\right)$.
- The resonance strength $\omega \gamma = \frac{\Gamma_\alpha \Gamma_{\text{rad}}}{\Gamma_\alpha + \Gamma_{\text{rad}}} = \frac{\Gamma_{\text{rad}}}{1 + \Gamma_{\text{rad}}/\Gamma_\alpha} \approx \Gamma_{\text{rad}} = \Gamma_\gamma + \Gamma_\pi$ ($\Gamma_{\text{rad}} \ll \Gamma_\alpha$)

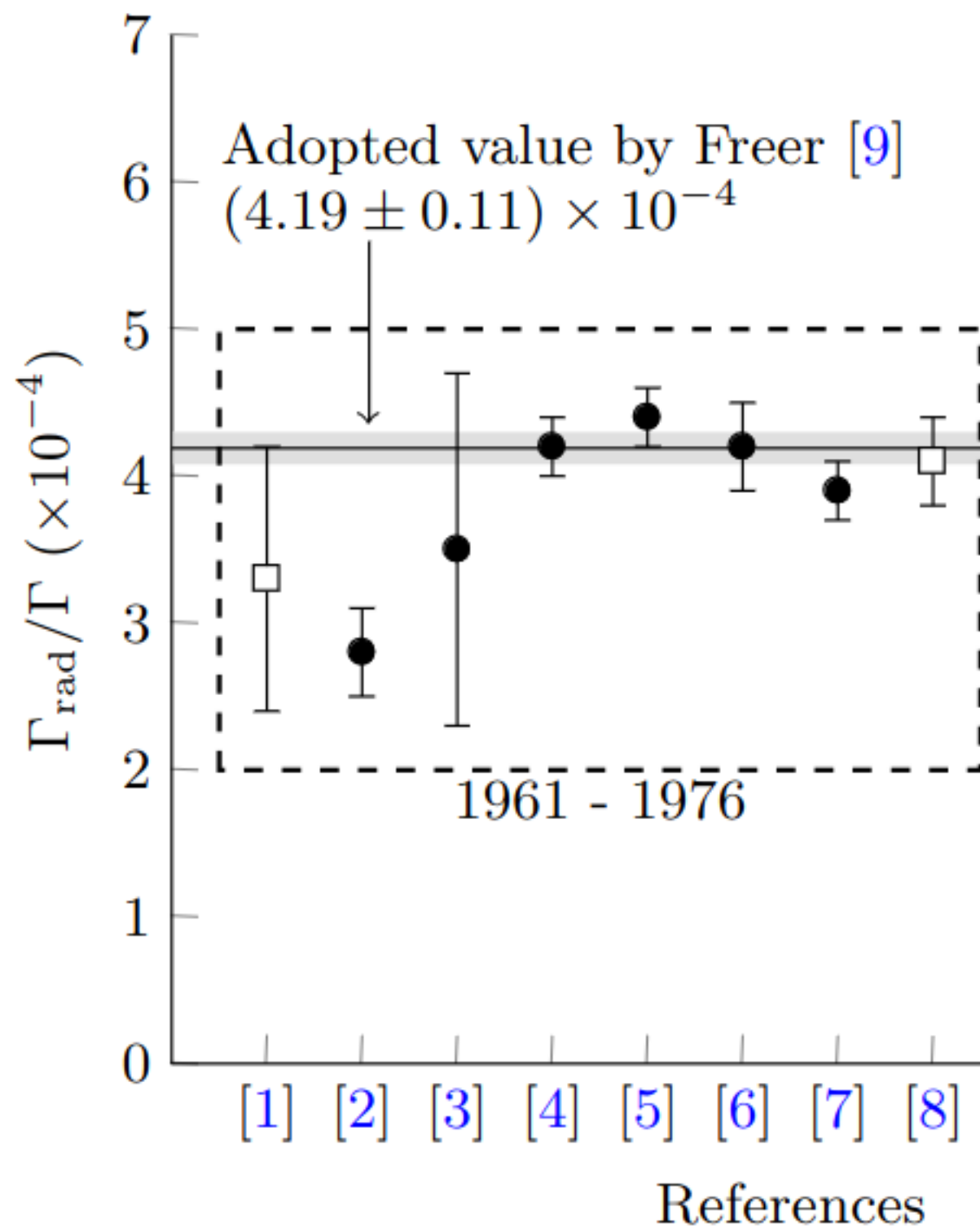
Experimental determination:

$$\Gamma_{\text{rad}} = \frac{\Gamma_{\text{rad}}}{\Gamma} \times \frac{\Gamma}{\Gamma_\pi(E0)} \times \Gamma_\pi(E0)$$

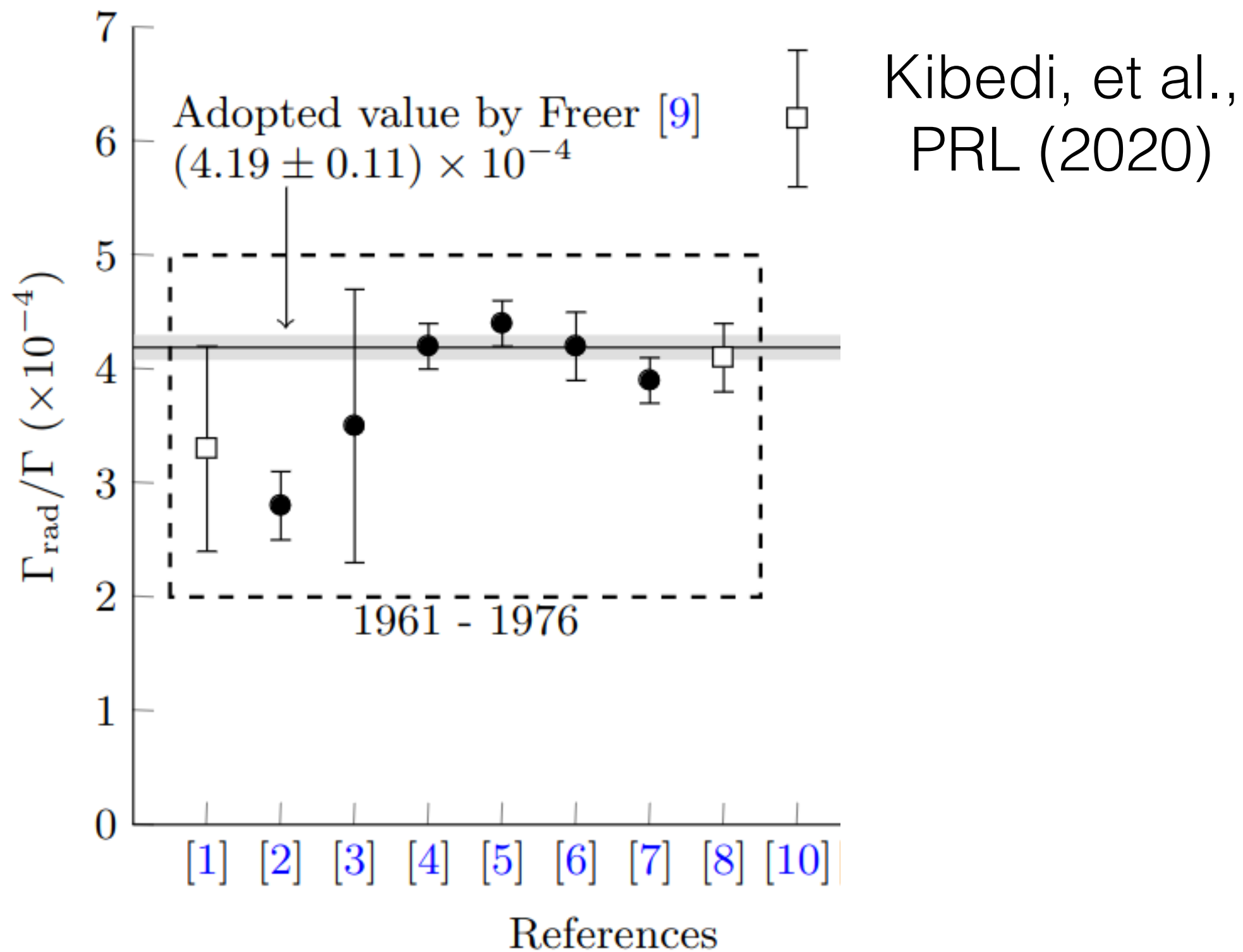
	Adopted [1]
$\Gamma_{\text{rad}}/\Gamma$	$4.19(11) \times 10^{-4}$
$\Gamma_\pi(E0)/\Gamma$	$6.7(6) \times 10^{-6}$
$\Gamma_\pi(E0)$	$62.3(2)\mu\text{eV}$
Γ_{rad}	$3.8 \times 10^{-3} \text{ eV}$

[1] M. Freer, et al., Prog. Part. Nucl. Phys. 78, 1 (2014).

$\Gamma_{\text{rad}} / \Gamma$ branching ratio for the Hoyle

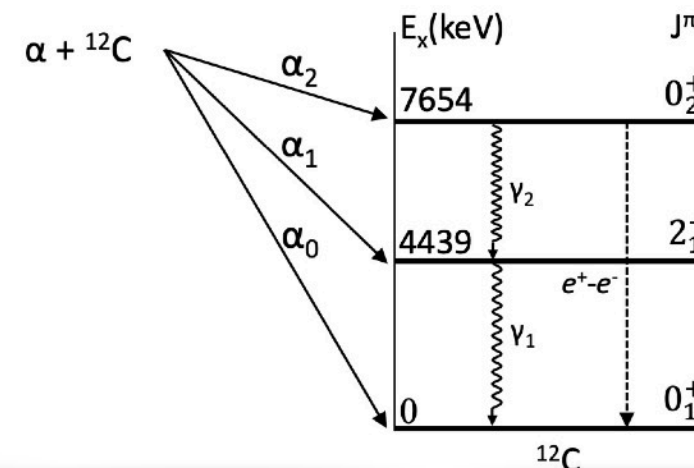
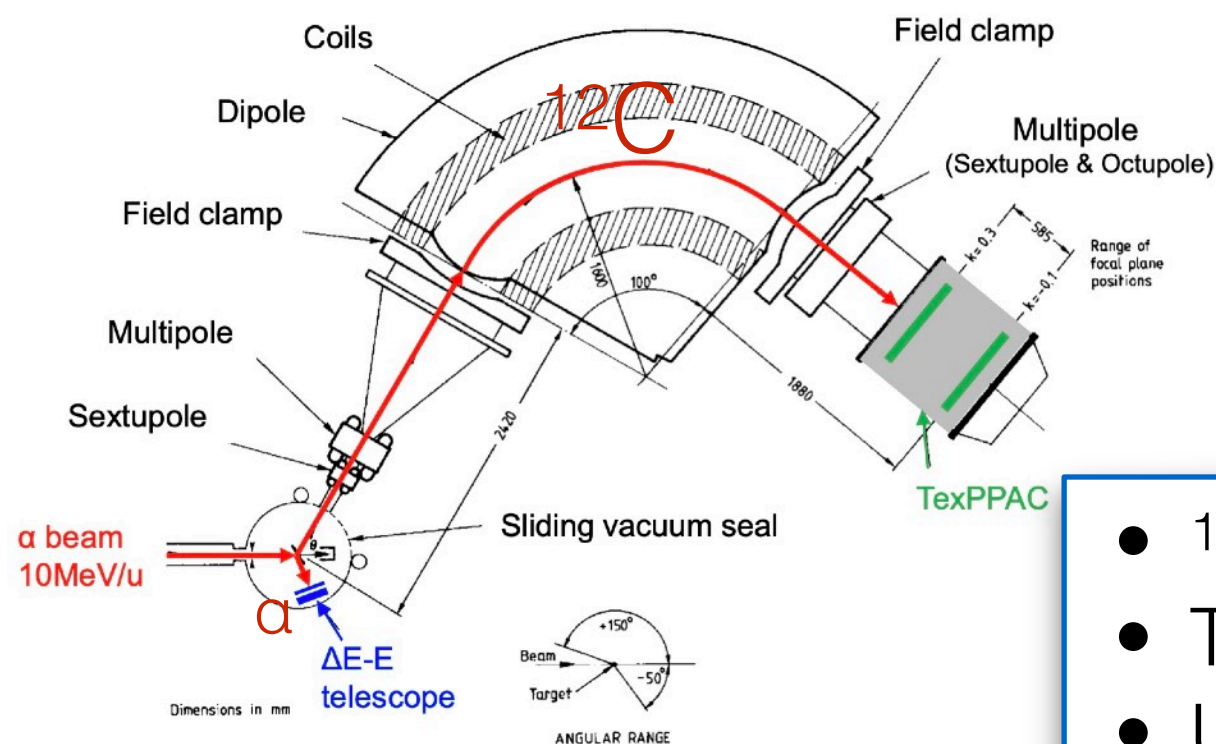


$\Gamma_{\text{rad}} / \Gamma$ branching ratio for the Hoyle



Hoyle $\Gamma_{\text{rad}} / \Gamma$ BR experiment

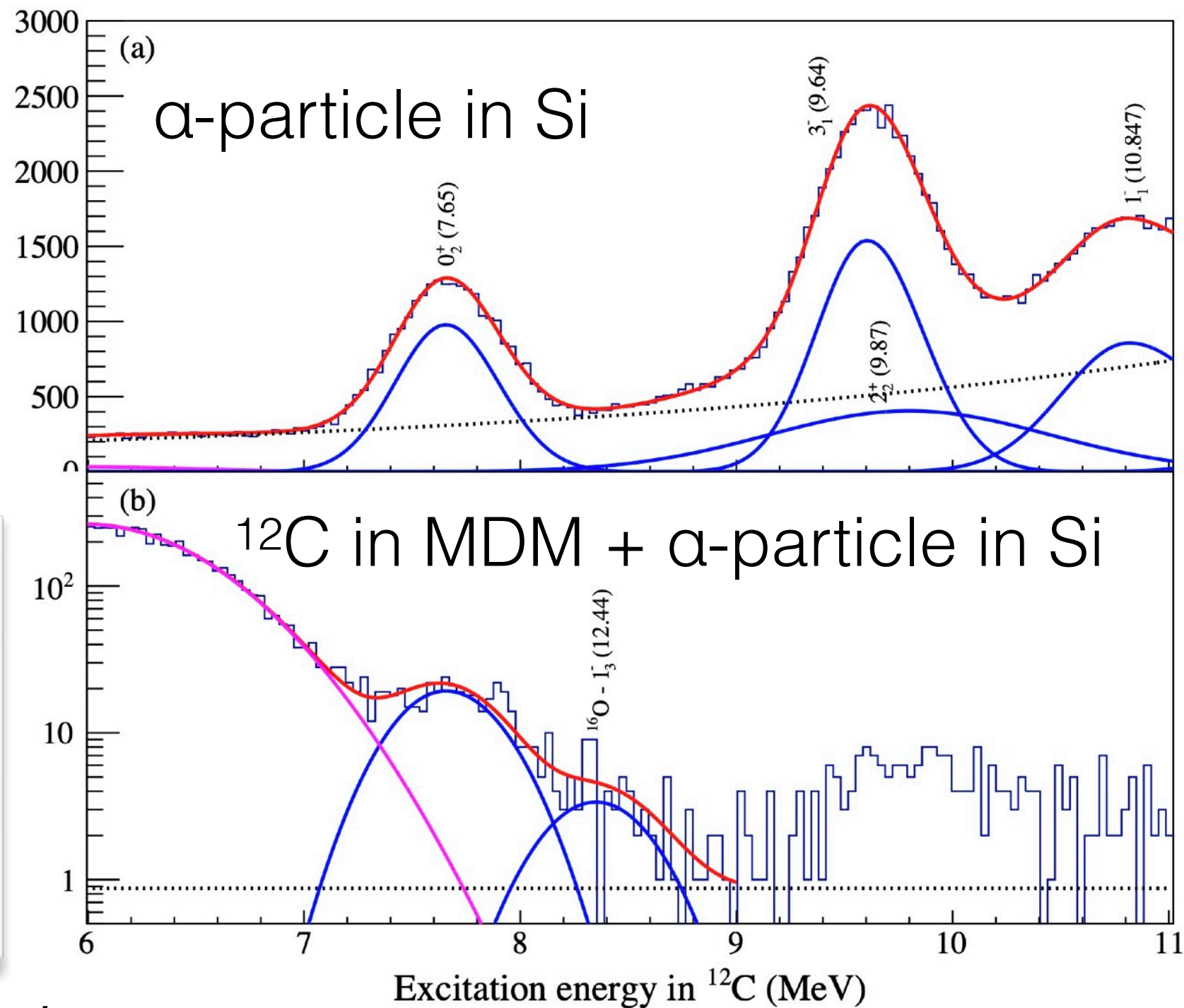
- Populate Hoyle using $^{12}\text{C}(\alpha, \alpha')^{12}\text{C}(\text{Hoyle})$ reaction
- Use Si to count the Hoyles populated
- Use MDM spectrometer to count surviving ^{12}C



- ^{12}C energy very low ~ 1.2 MeV/u
- TexPPACs - new focal plane det.
- Used ^{12}C 5+ charge state
- ^{12}C charged state fractions were accurately measured

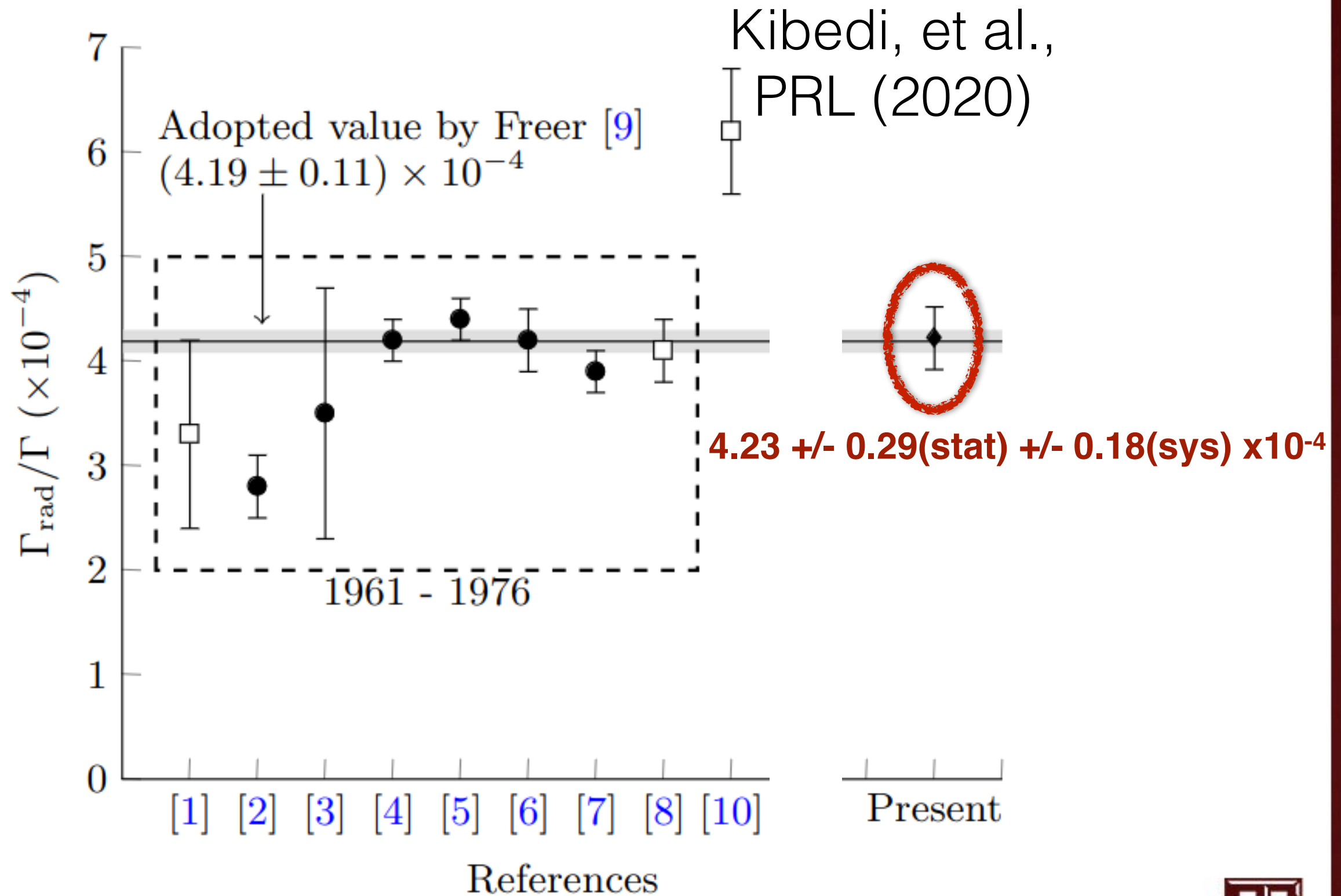
Used highly enriched ^{12}C target ($<0.1\%$ ^{13}C)

Hoyle $\Gamma_{\text{rad}} / \Gamma$ BR results

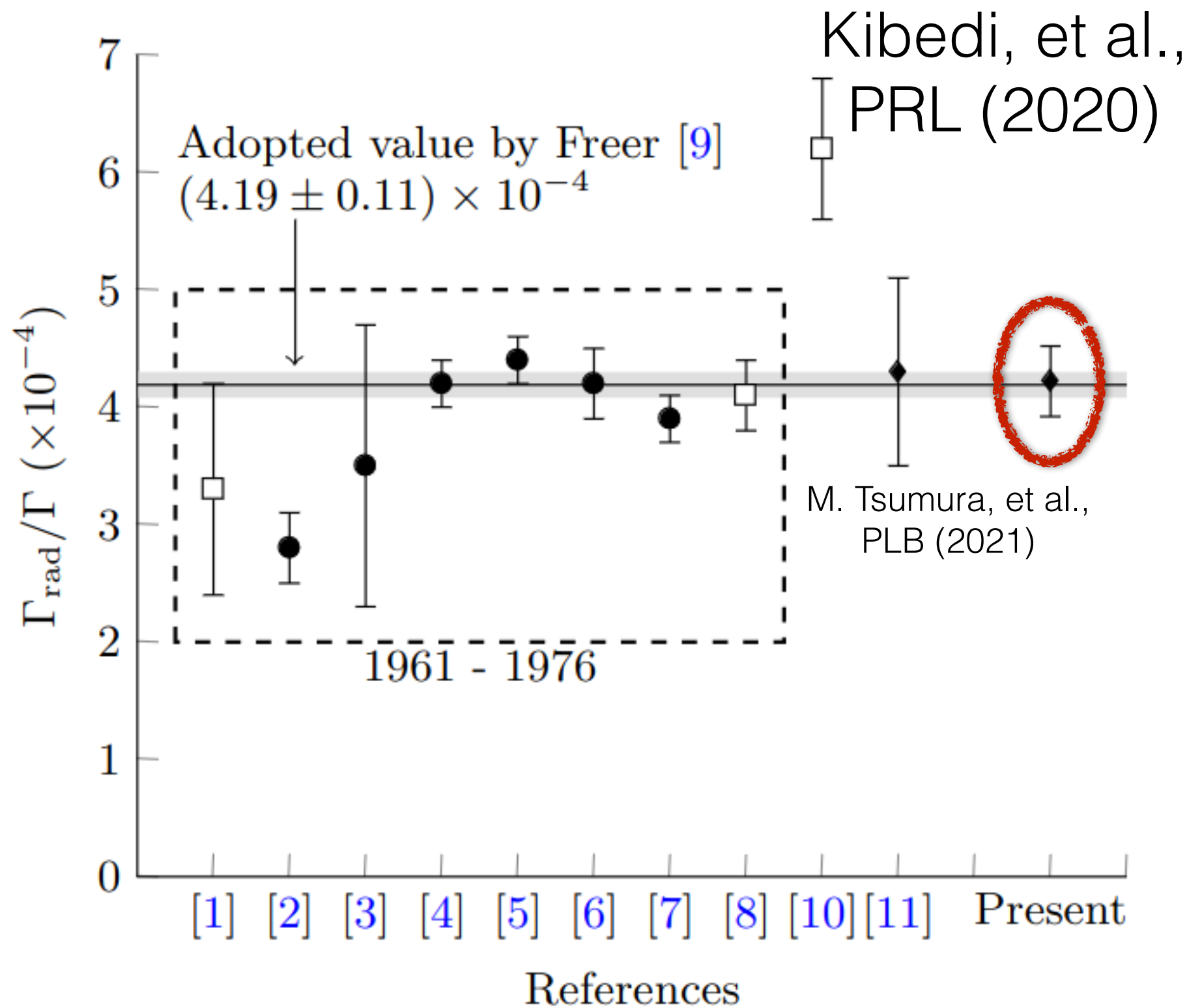


Zifeng Luo
TAMU graduate student

$\Gamma_{\text{rad}} / \Gamma$ branching ratio for the Hoyle



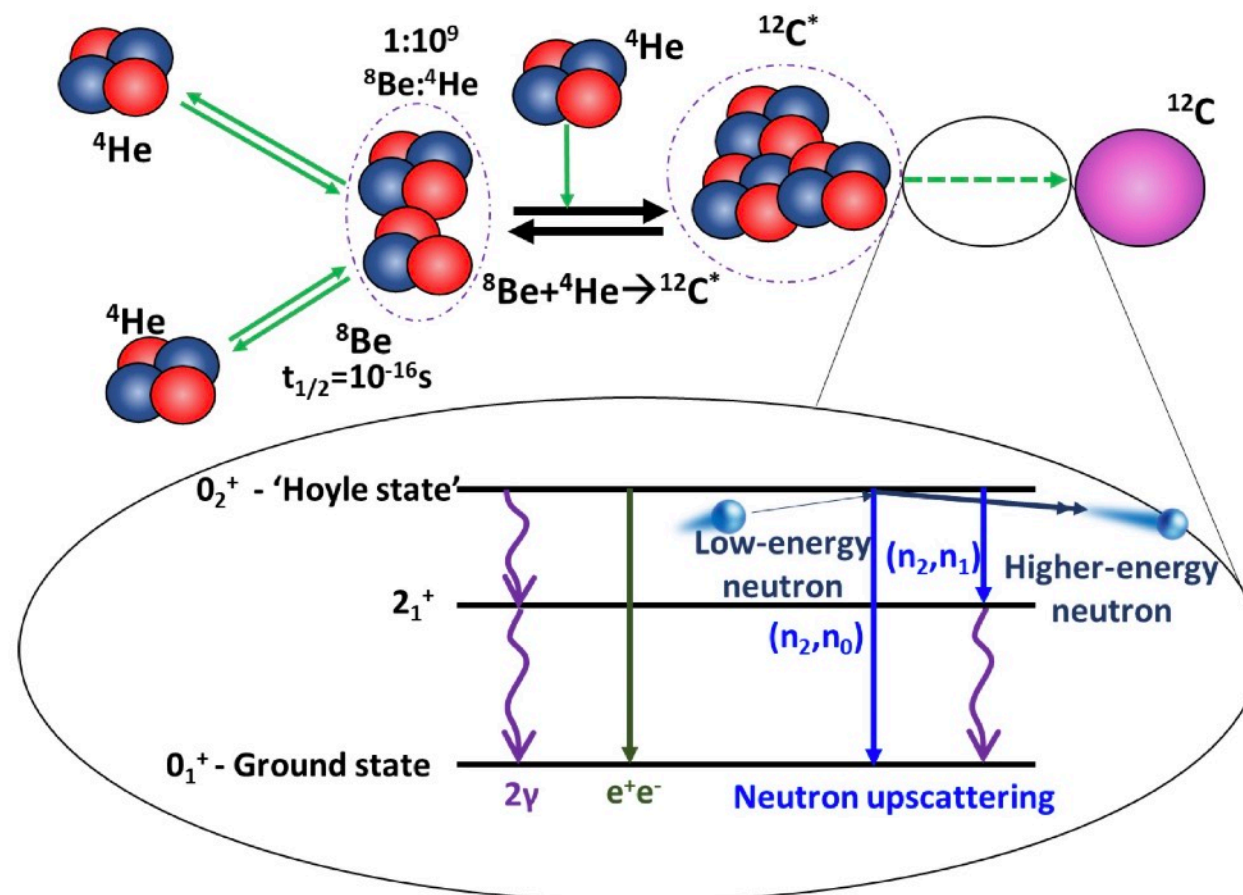
$\Gamma_{\text{rad}} / \Gamma$ branching ratio for the Hoyle



The role of neutrons in carbon nucleosynthesis

Triple-alpha reaction and neutron upscattering

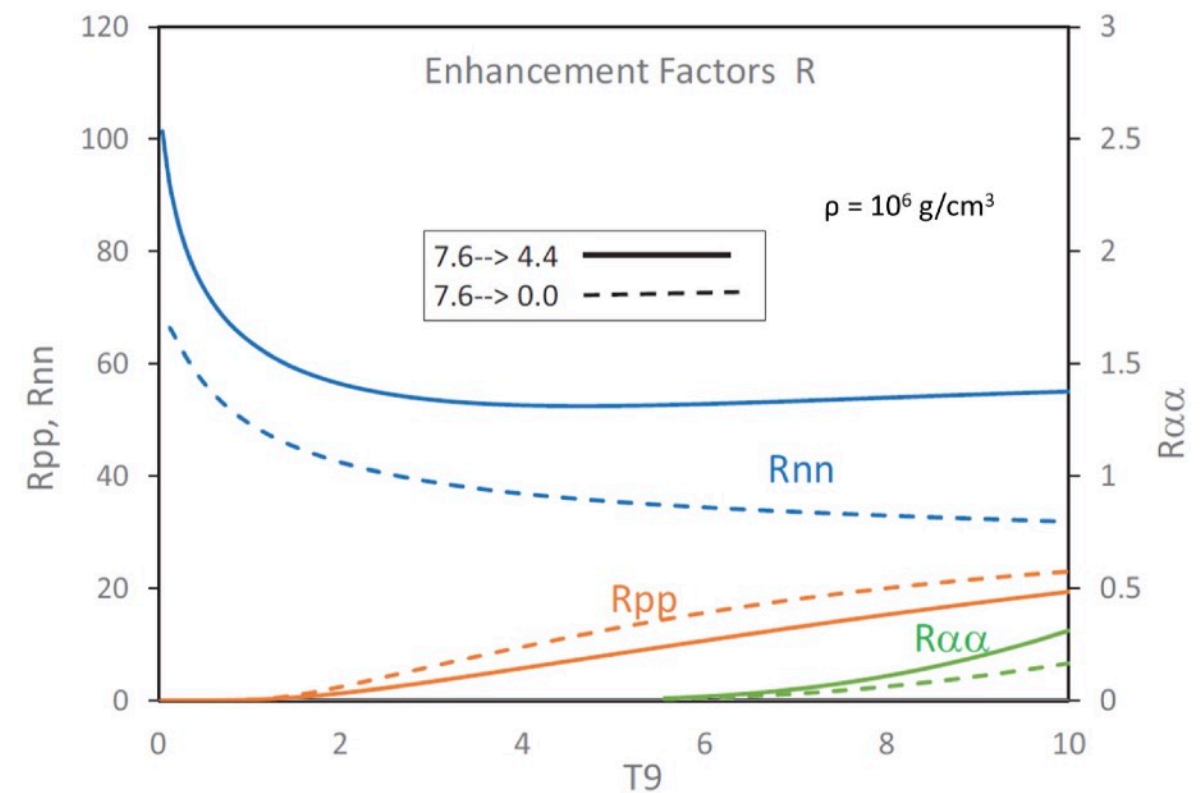
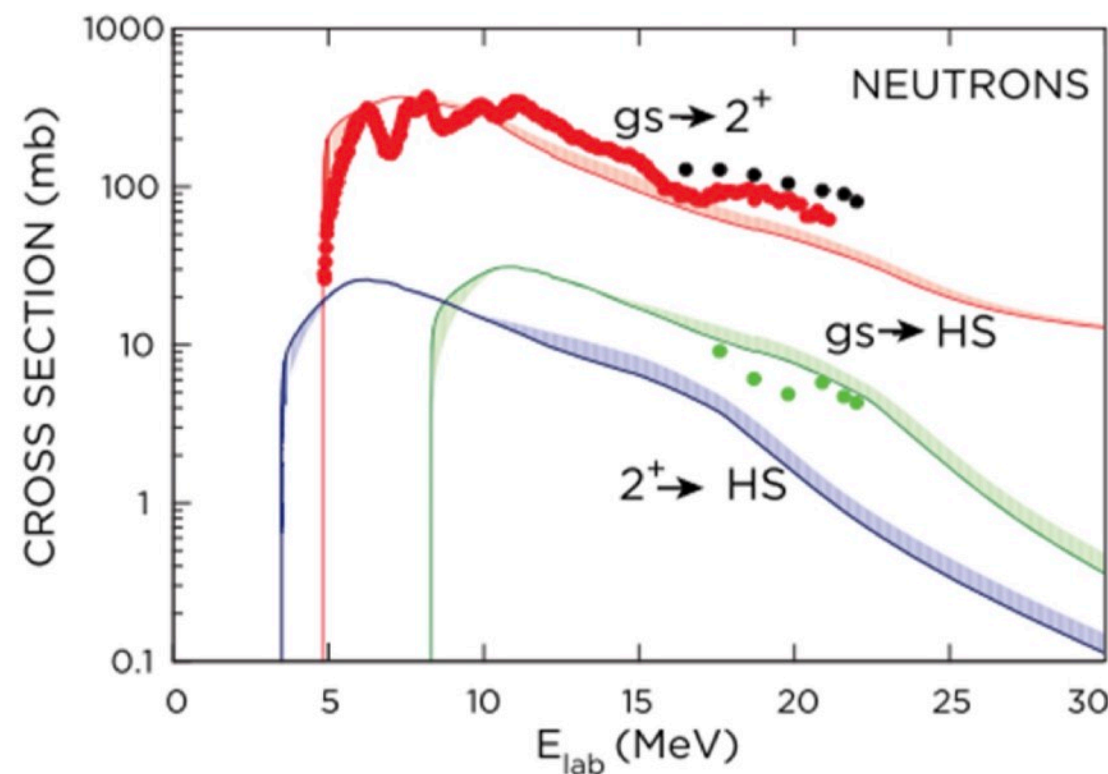
- three alphas produce Hoyle state in ^{12}C (through $^8\text{Be}(\text{g.s.})$)
- Hoyle state can be de-excited by:
 - gamma cascade
 - electron-positron pair
 - neutrons + Hoyle scattering
 - protons + Hoyle scattering
- OR **decay back to 3 α**



Enhancement of the Triple Alpha Rate in a Hot Dense MediumMary Beard,^{1,2,*} Sam M. Austin,^{2,†} and Richard Cyburt^{2,‡}¹Department of Physics, University of Notre Dame, Notre Dame, Indiana 46556, USA²Joint Institute for Nuclear Astrophysics, National Superconducting Cyclotron Laboratory, Michigan State University, 640 South Shaw Lane, East Lansing, Michigan 48824-1321, USA

(Received 10 March 2017; revised manuscript received 3 July 2017; published 15 September 2017)

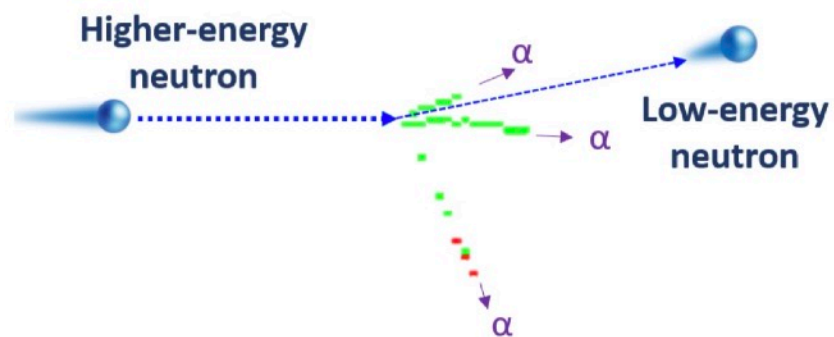
[M. Beard et al. Phys. Rev. Lett. 119, 112701]



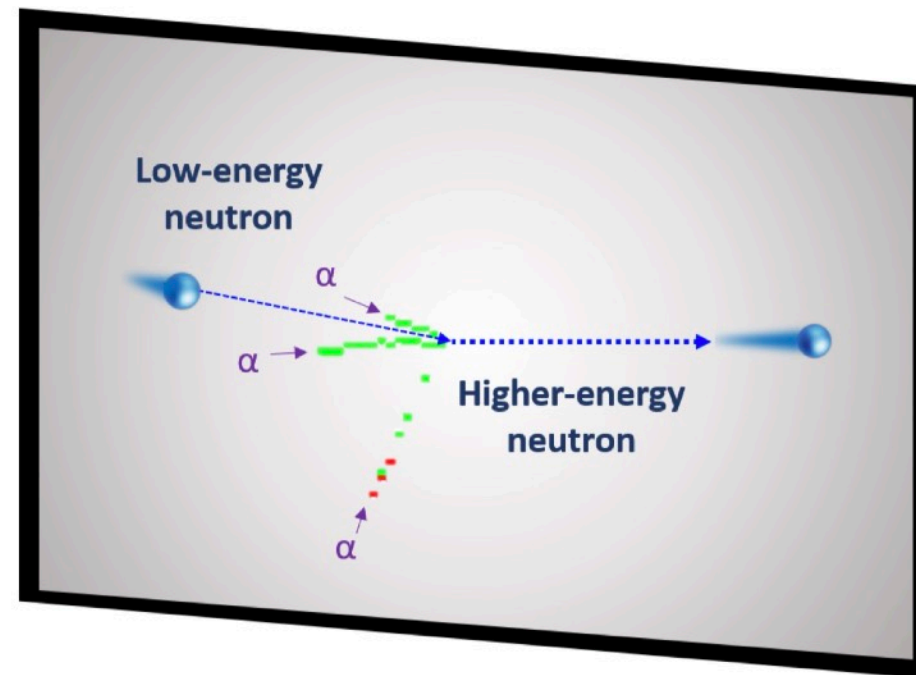
Using Hauser Feshbach XS predictions. High-density environment, large neutron enhancements at low temperature (≈ 0.2 GK (T_9))

Measuring time-reversed reaction

Experimental case



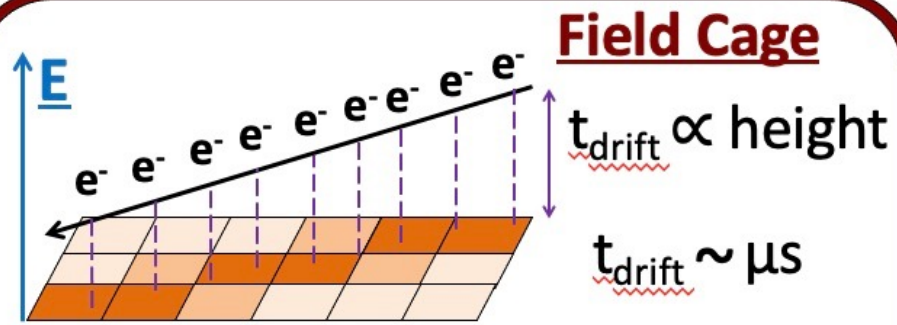
Time-reversed astrophysical case



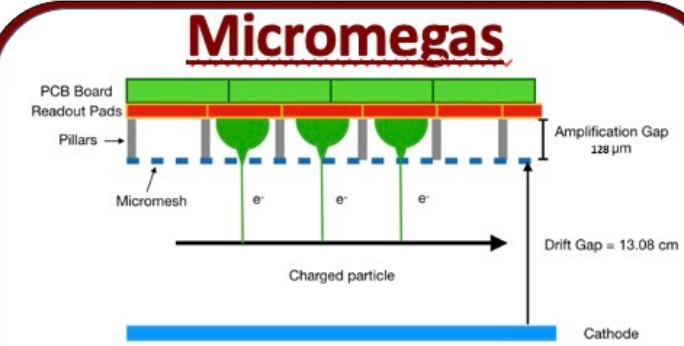
Time-reversal symmetry

Quantum mechanically we can relate a reaction and the time reverse of that reaction using "detailed balance"

TexAT TPC: Texas Active Target Time Projection Chamber

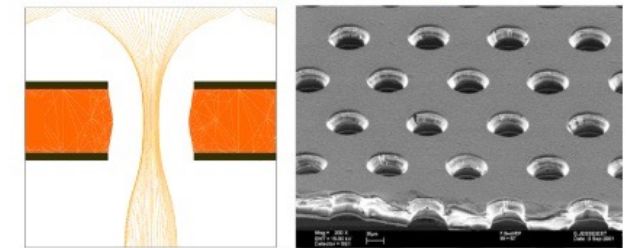


Provides electric field ~ 1 kV over 13 cm to drift electrons to the Micromegas. Drift time gives the height the electron was created at.



Micromegas (MM) provide gain factor of ~ 100 and segmented readout of 1024 channels.

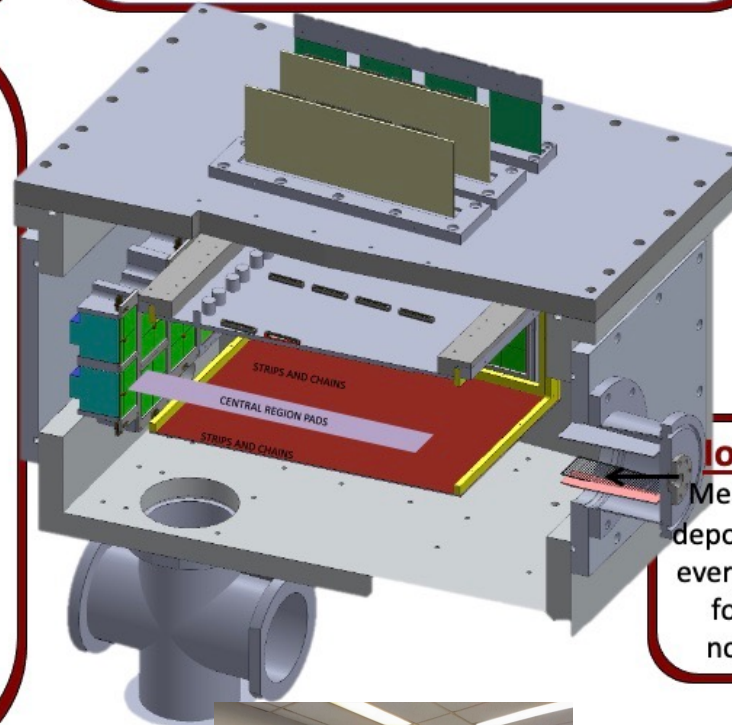
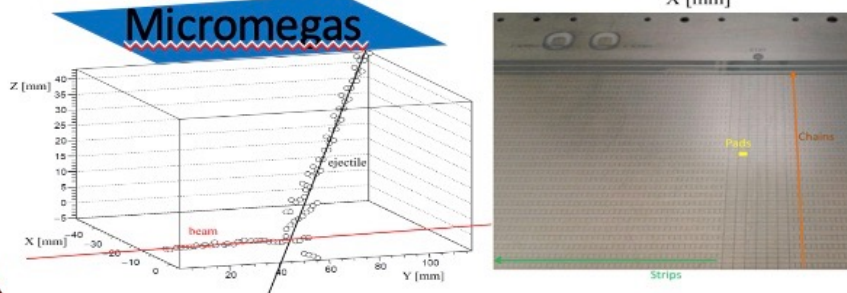
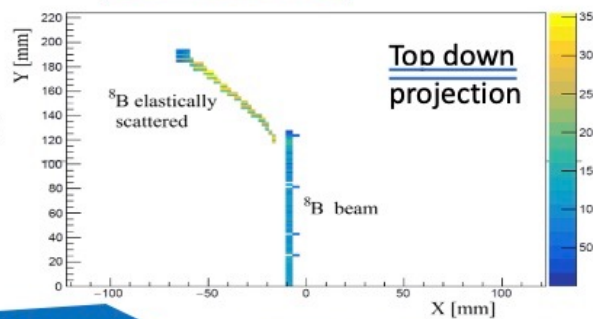
(TH)GEMs



Choice between 50 μm (thin) and 1.5 mm thickness (thick). Provides additional gain factor of ~ 10 -100.

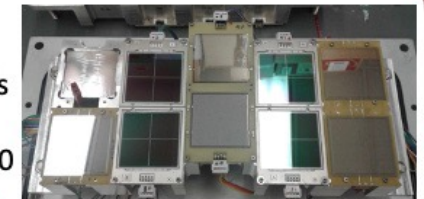
3D tracks

Readout segmentation of 1.75 x 3.5 mm (in central region) gives 3D track of the event.



Si + CsI(Tl) wall

Good energy resolution measurement of light recoils that escape TPC.
 Telescope of 500,600 or 1000 μm Si + 40-mm-thick CsI.

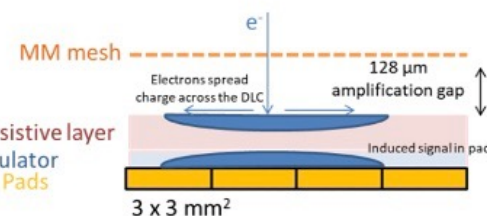


Ion Counter

Measures energy deposited in gas for every incoming ion for beam ID + normalization.

Future upgrade: TeBAT

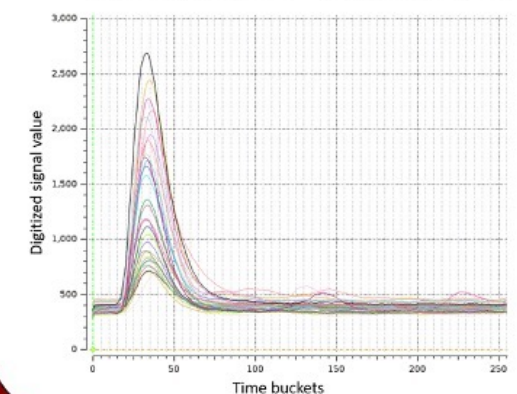
- New DLC charge-spreading MM technology
- Position resolution from 1.5 mm $\rightarrow$ 0.2 mm
- 1024 channels $\rightarrow$ 7056 channels



E. Koshchiv

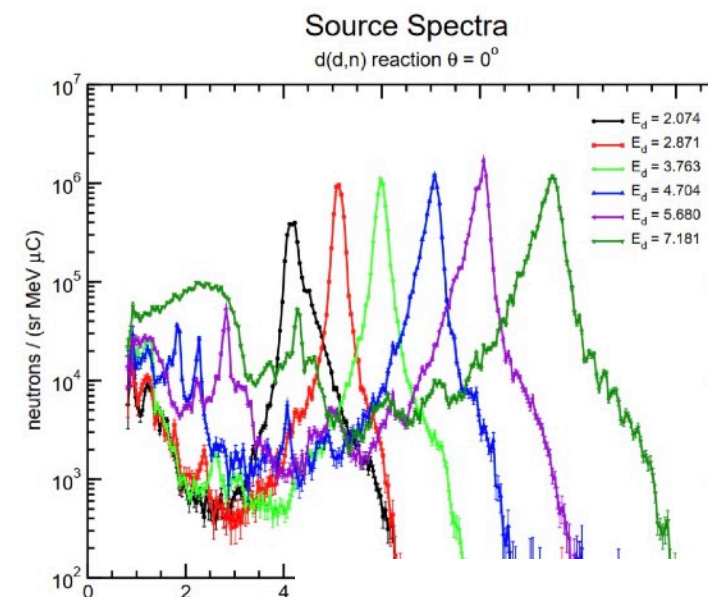
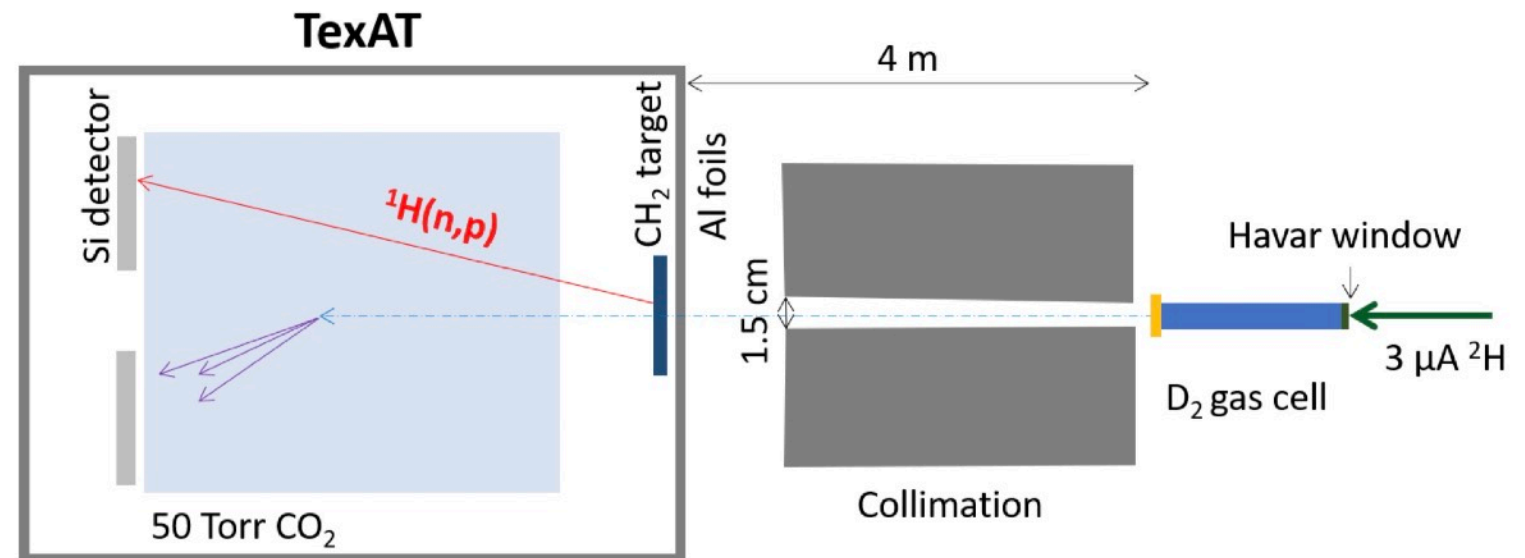
GET – General Electronics for TPCs

- 1024 TPC channels + 1024 for Si/CsI/spare
- 10-100 MHz waveform digitizer
 - 512 time buckets
- On chip shaping + amplification
- Internal/external trigger schemes

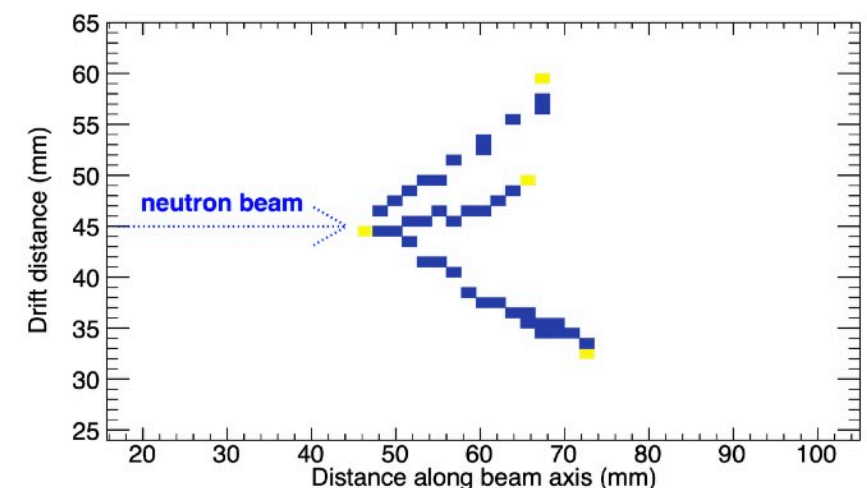


TPCs and neutron beams

- Edwards Accelerator Lab - Ohio University
- Deuteron beam from accelerator: $\approx 10^{13}$ pps
- Neutron beam from $d(d, n)$ reaction - scanning from 7.2-10.0 MeV
- 5×10^3 neutrons/s:
 $\sigma(E_n) \approx 200$ keV
- Normalization is a big issue! Use $^1\text{H}(n, p)$

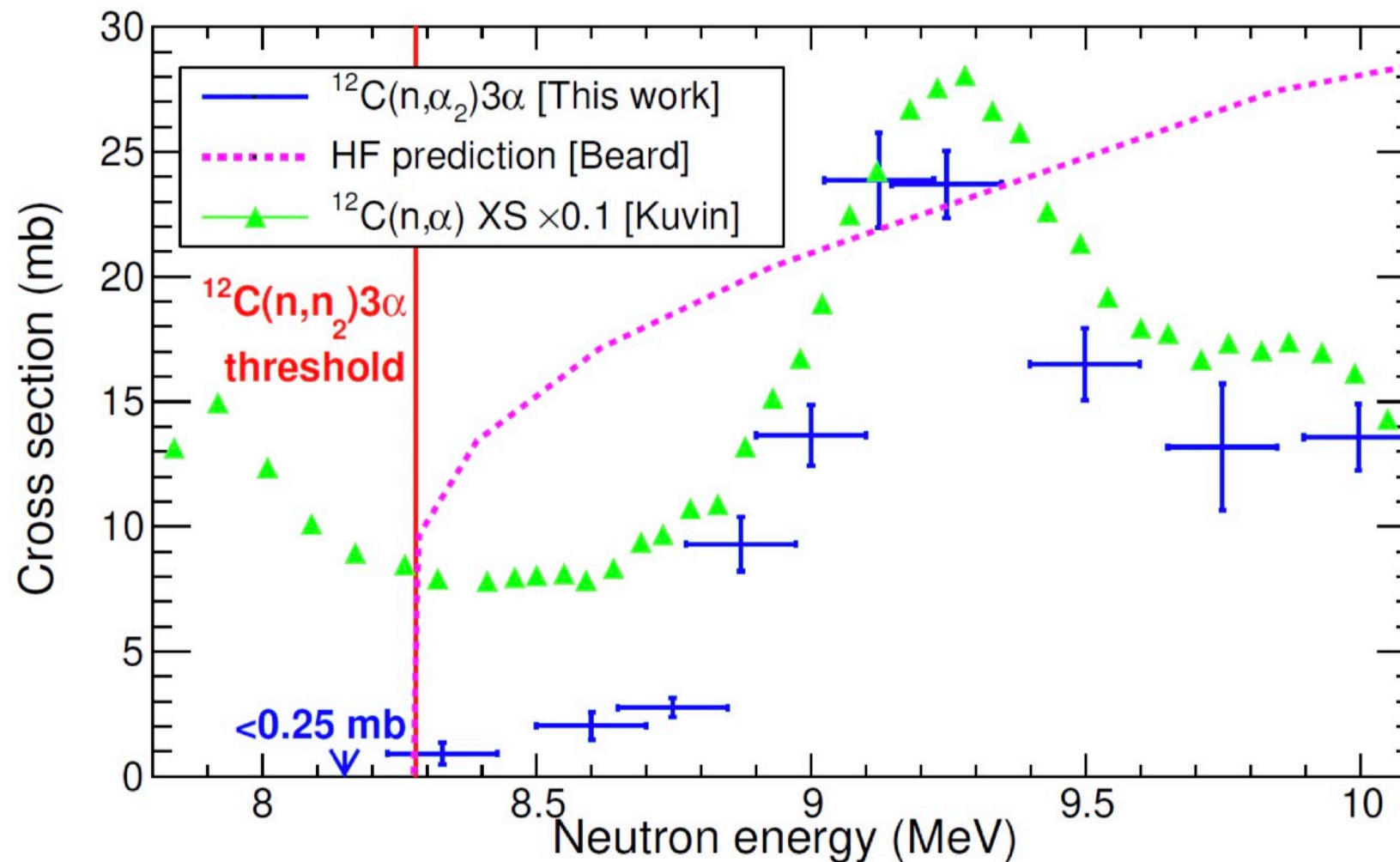


J. Bishop
C. Parker
S. (Tony) Ahn
E. Koshchiy

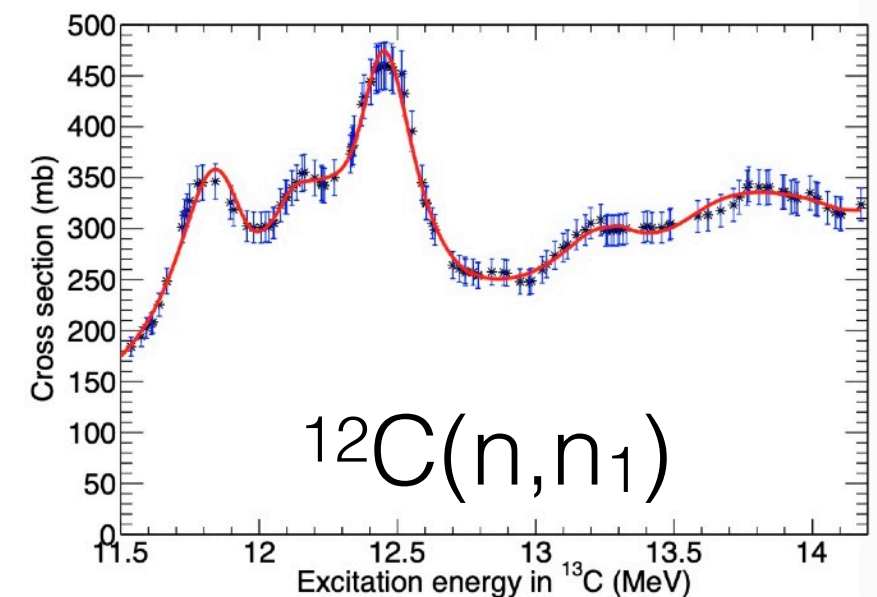
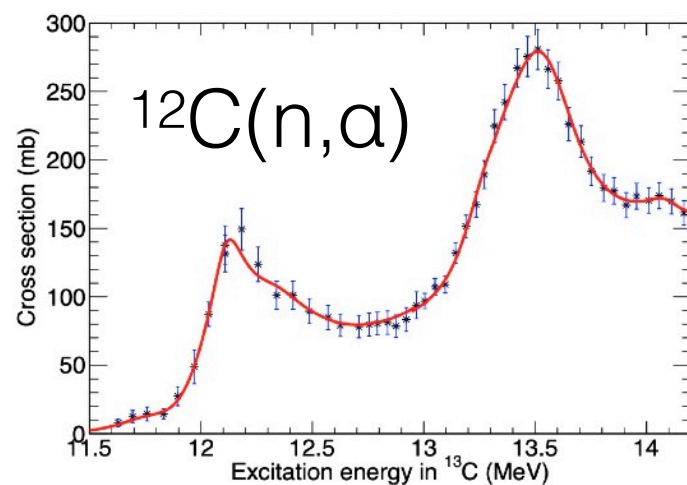
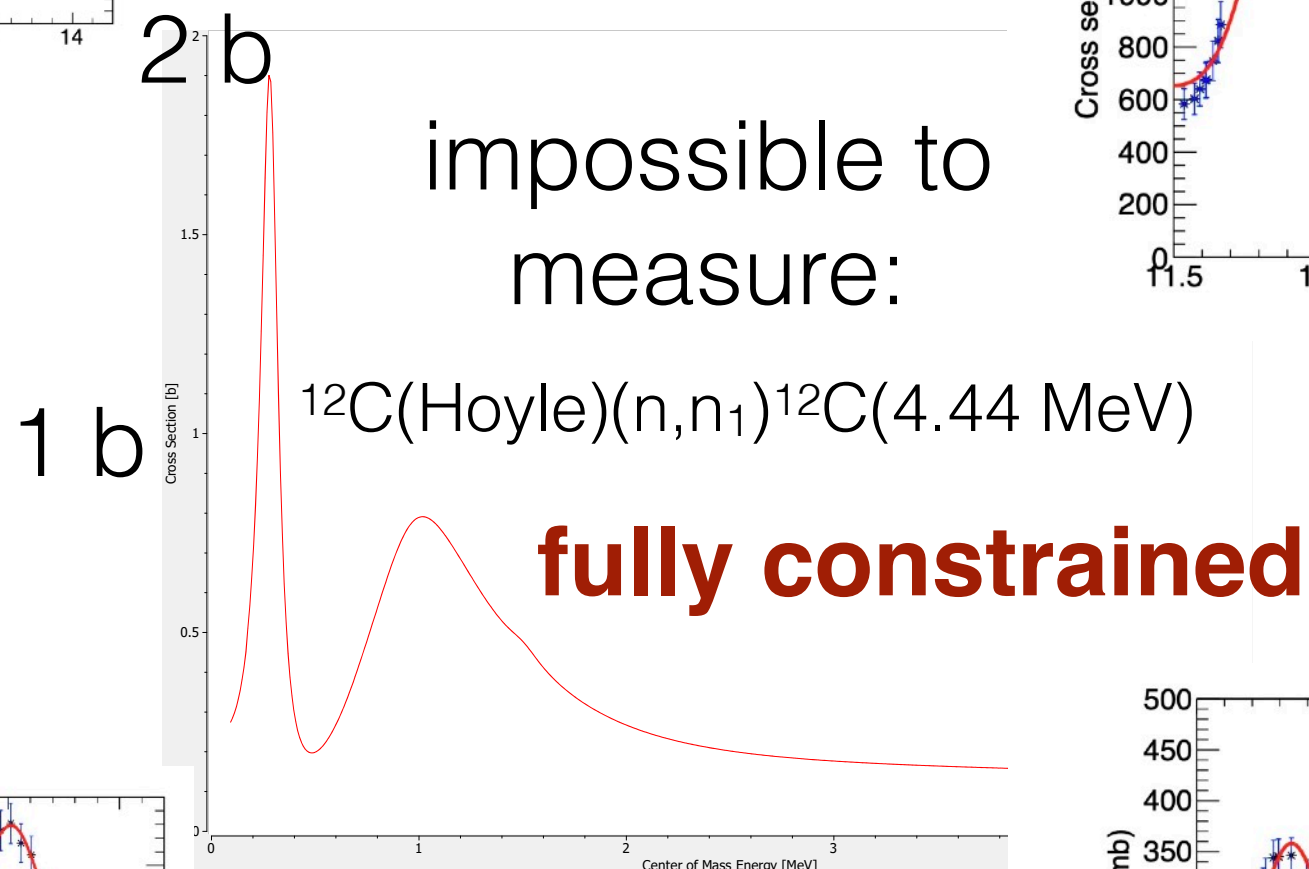
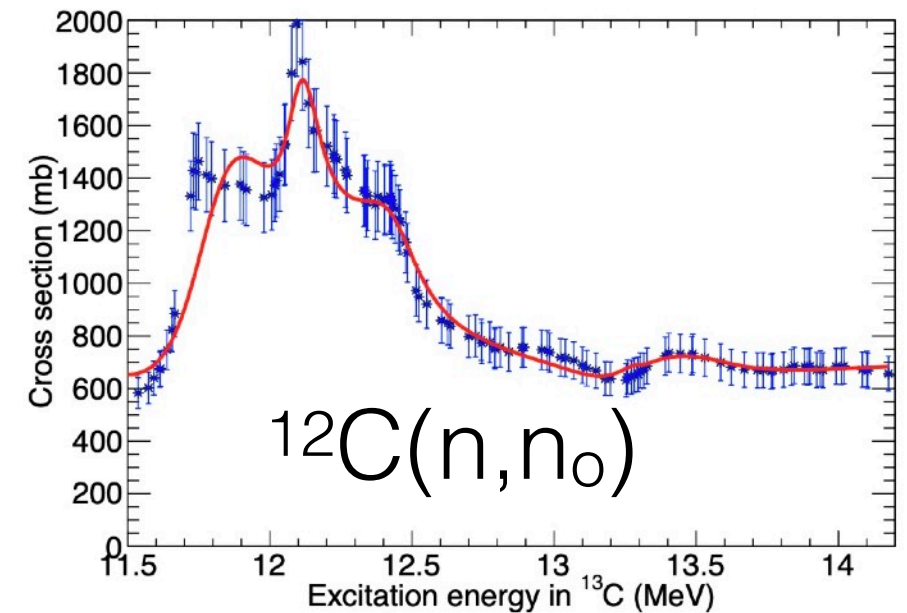
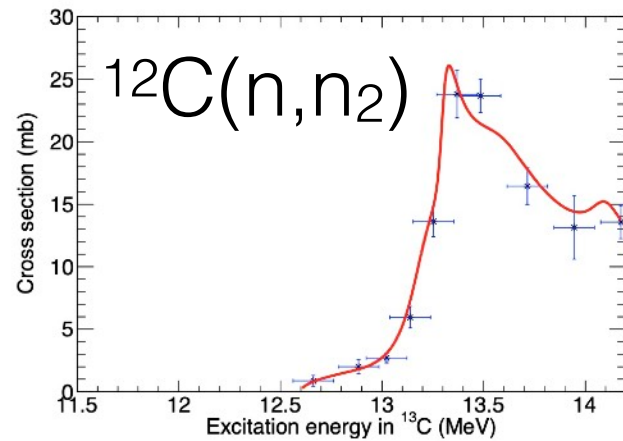


$^{12}\text{C}(n,n_2)\text{Hoyle}$ reaction XS

Reconstruct three α -particles to make Hoyle state, count the events and neutrons!
 $^{12}\text{C}(n, \alpha_{1,2})^9\text{Be}^*$ contribution is removed

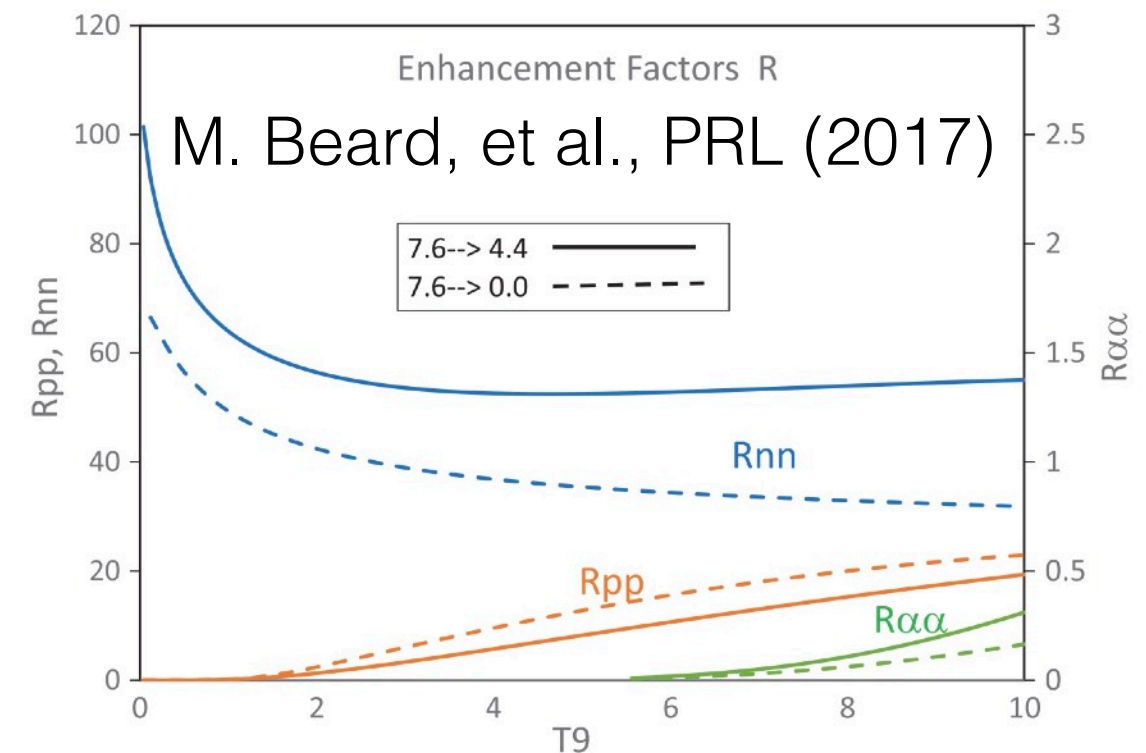
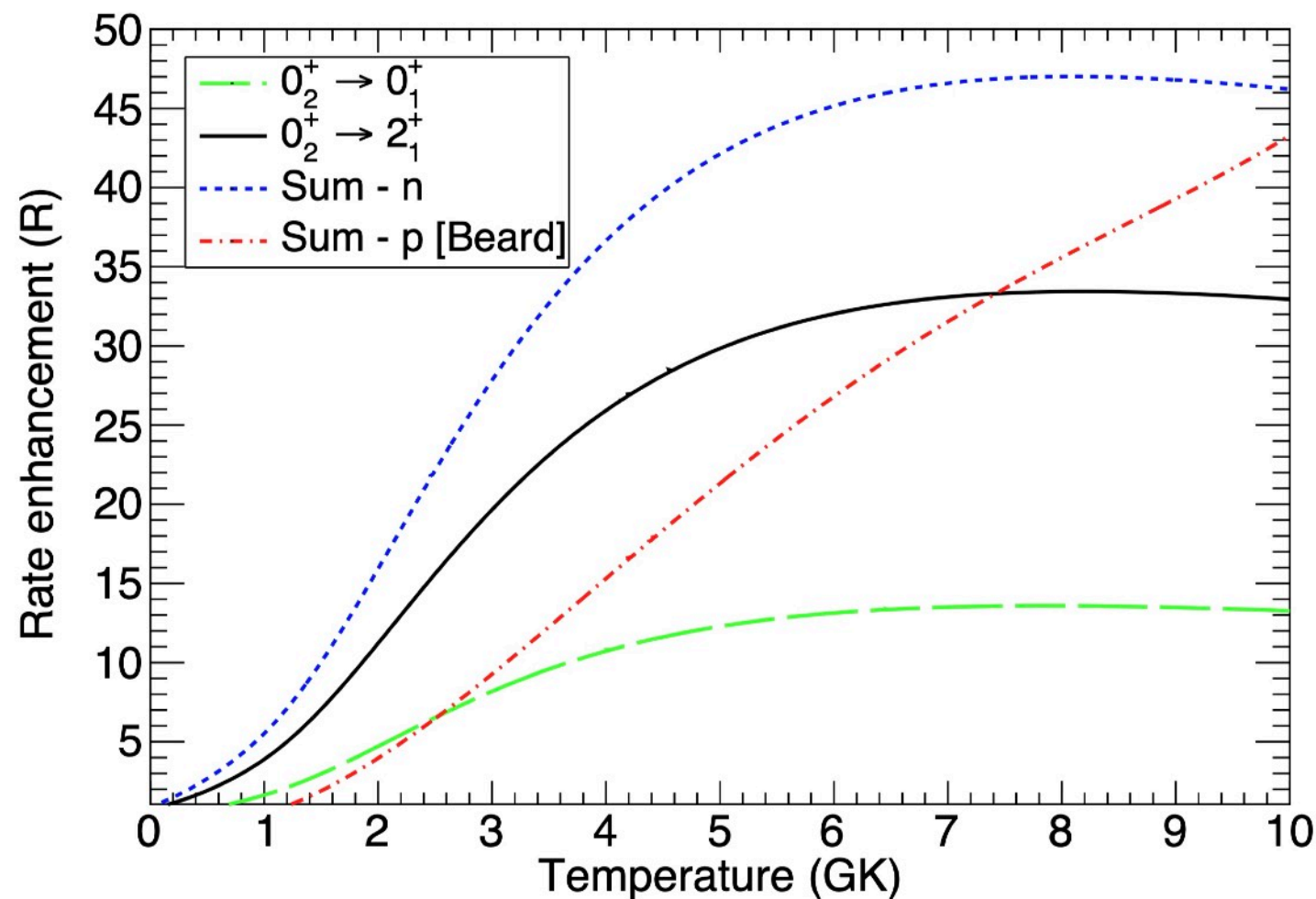


R-matrix analysis



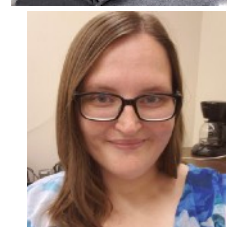
Neutron-upscattering enhancement of the triple-alpha process

J. Bishop , C. E. Parker, G. V. Rogachev, S. Ahn, E. Koshchiy, K. Brandenburg, C. R. Brune, R. J. Charity, J. Derkin, N. Dronchi, G. Hamad, Y. Jones-Alberty, Tz. Kokalova, T. N. Massey, Z. Meisel, E. V. Ohstrom, S. N. Paneru, E. C. Pollacco, M. Saxena, N. Singh, R. Smith, L. G. Sobotka, D. Soltesz, S. K. Subedi, A. V. Voinov, J. Warren & C. Wheldon [— Show fewer authors](#)



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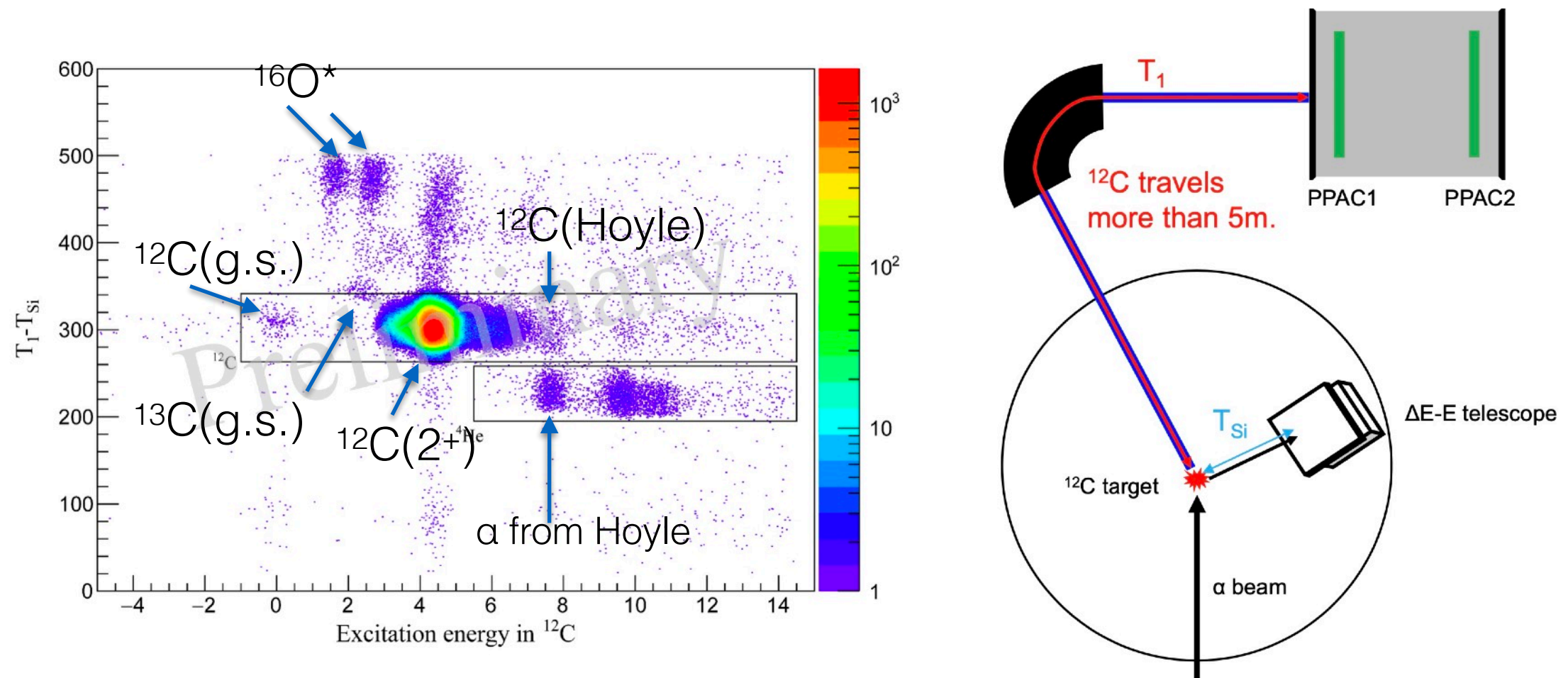


Summary

- ☑ Indirect methods are essential in nuclear astrophysics
- ☑ Major discrepancy between direct and indirect methods for the $^{22}\text{Ne}(\alpha, n)$ reaction
- ☑ The radiative width of the Hoyle state is well constrained - no problem there.
- ☑ Neutron upscattering on Hoyle is well-constrained now and is not as important in carbon nucleosynthesis as was suggested previously.



Hoyle $\Gamma_{\text{rad}} / \Gamma$ BR experiment



Zifeng Luo
TAMU graduate student

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Article | [Published: 02 December 2020](#)

Enhanced triple- α reaction reduces proton-rich nucleosynthesis in supernovae

[Shilun Jin](#), [Luke F. Roberts](#) , [Sam M. Austin](#) & [Hendrik Schatz](#)

[Nature](#) **588**, 57–60 (2020) | [Cite this article](#)

4334 Accesses | **9** Citations | **127** Altmetric | [Metrics](#)

Abstract



TPCs and neutron beams

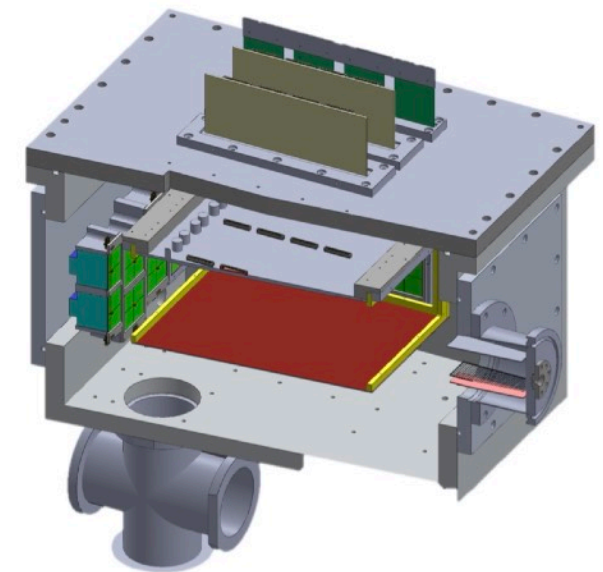
TPCs can be well-suited to many different types of neutron-induced measurements

Active-target (gas IS the target and readout medium)

TPC filled with CO₂ looking to measure:

- $^{12}\text{C}(n, n_2)3\alpha$ - inelastic neutron scattering to the Hoyle state
- $^{12/16}\text{C}/\text{O}(n, \alpha)$ - hugely important reactions for nuclear data measured parasitically

Can be measured with the TexAT with 50 Torr CO₂ gas. Represents a great opportunity for future measurements with low-energy recoil products - can be well resolved using low pressure TPC.



TexAT “Hoyle” Publications

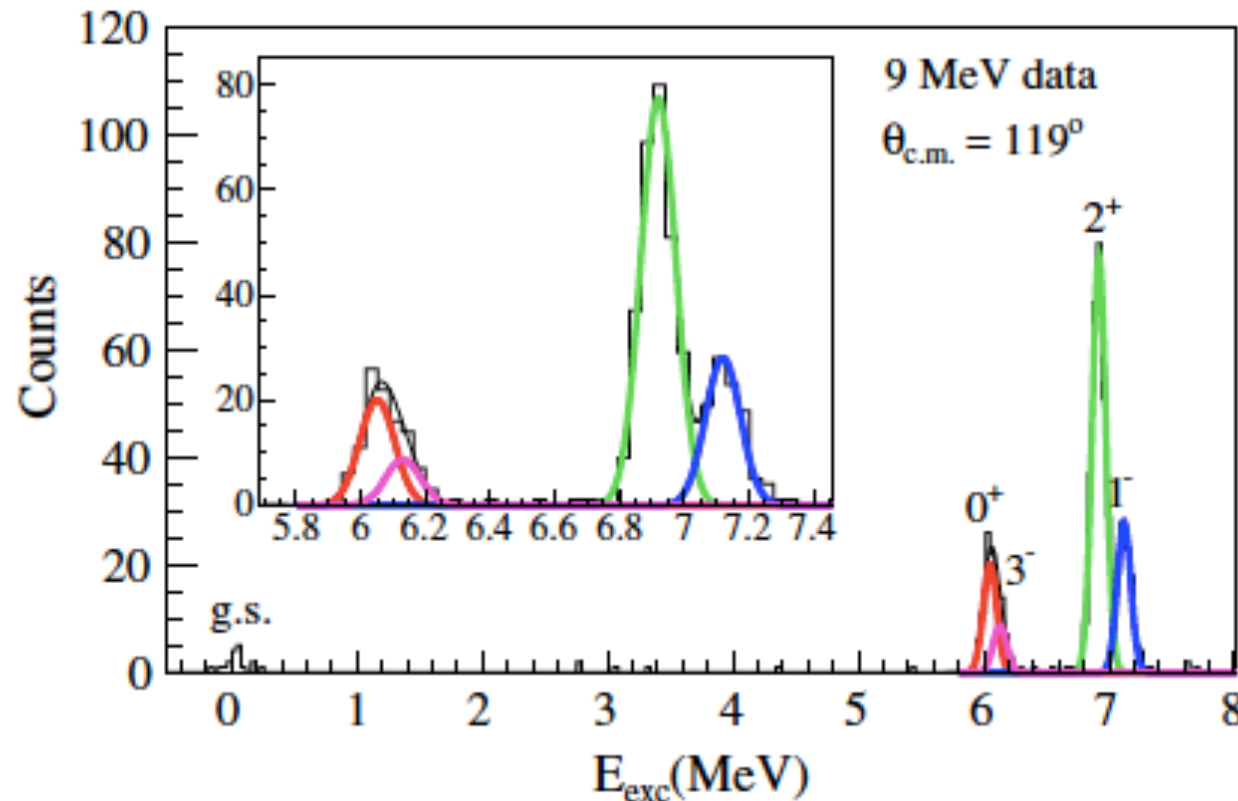
- ☑ J. Bishop, et al., NIM A964 (2020) 163773.
- ☑ J. Bishop, et al., PRC 102 (2020) 041303.
- ☑ J. Bishop, et al., PRC Letter 103 (2021) L051303.
- ☑ J. Bishop, et al., Nature Communication 13 (2022)

2151

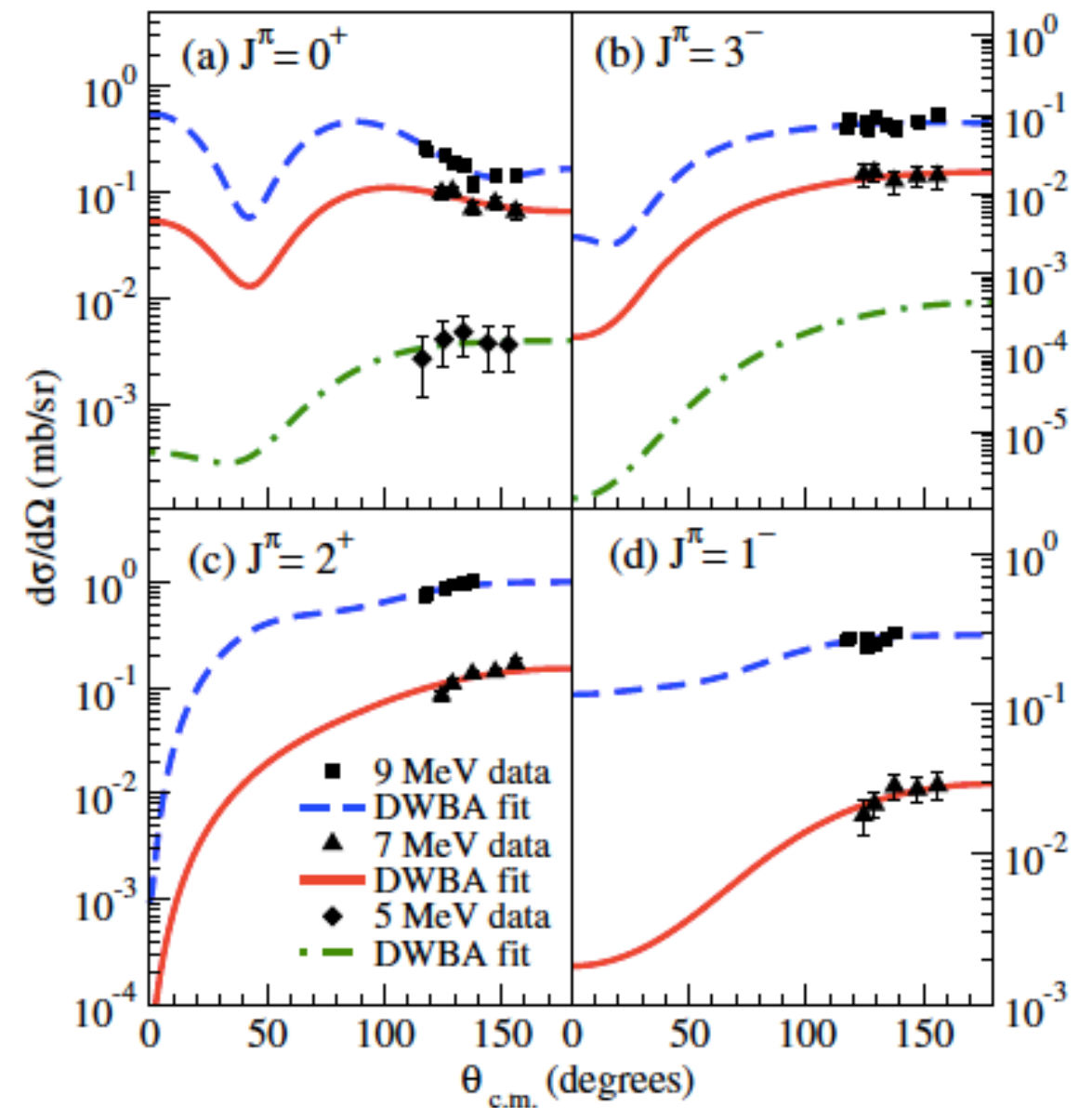


ANCs for $^{12}\text{C}(\alpha,\gamma)$ reaction

- ✓ Spectrum of deuterons from sub-Coulomb $^6\text{Li}(^{12}\text{C},d)$ reaction. The total energy of the ^{12}C beam is 9 MeV.



- ✓ Angular distributions



M.L. Avila, GVR, E. Koshchiy, et al., Phys. Rev. Lett. **114**, 071101 (2015).

ANCs for $^{12}\text{C}(\alpha,\gamma)$ reaction

- ☑ ANC of all sub-threshold states in ^{16}O

$(C_{\alpha-^{12}\text{C}}^{^{16}\text{O}(0+)})^2 (10^6 \text{ fm}^{-1})$	$(C_{\alpha-^{12}\text{C}}^{^{16}\text{O}(3-)})^2 (10^4 \text{ fm}^{-1})$	$(C_{\alpha-^{12}\text{C}}^{^{16}\text{O}(2+)})^2 (10^{10} \text{ fm}^{-1})$	$(C_{\alpha-^{12}\text{C}}^{^{16}\text{O}(1-)})^2 (10^{28} \text{ fm}^{-1})$	Ref.
...	...	2.07 ± 0.80	4.00 ± 1.38	[1]
...	...	1.29 ± 0.23	4.33 ± 0.84	[2]
...	...	$1.96^{+1.41}_{-1.27}$	3.48 ± 2.0	[3]
2.43 ± 0.30	1.93 ± 0.25	1.48 ± 0.16	4.39 ± 0.59	This work

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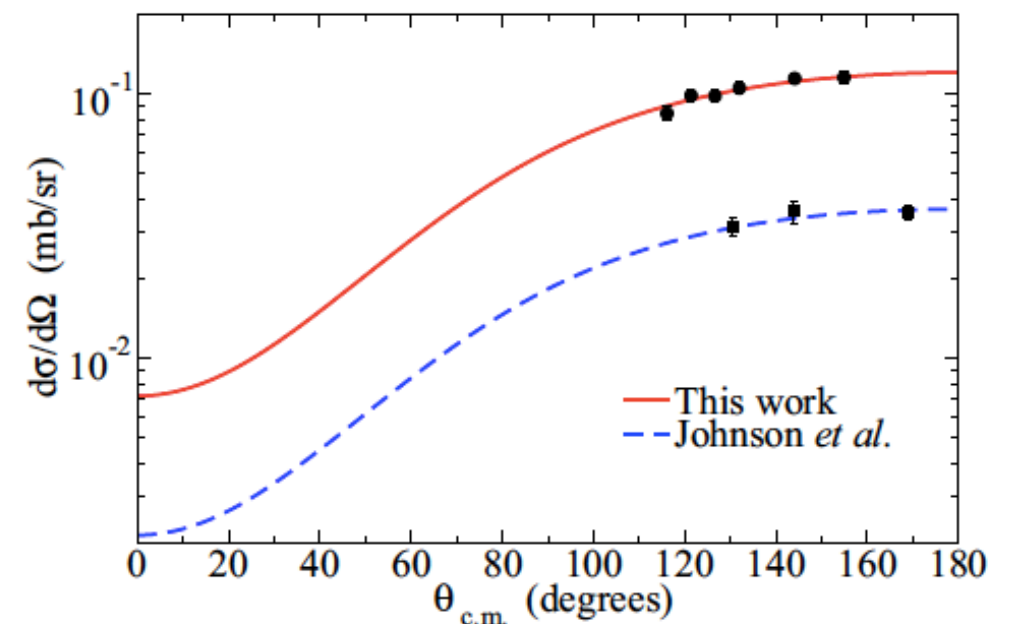
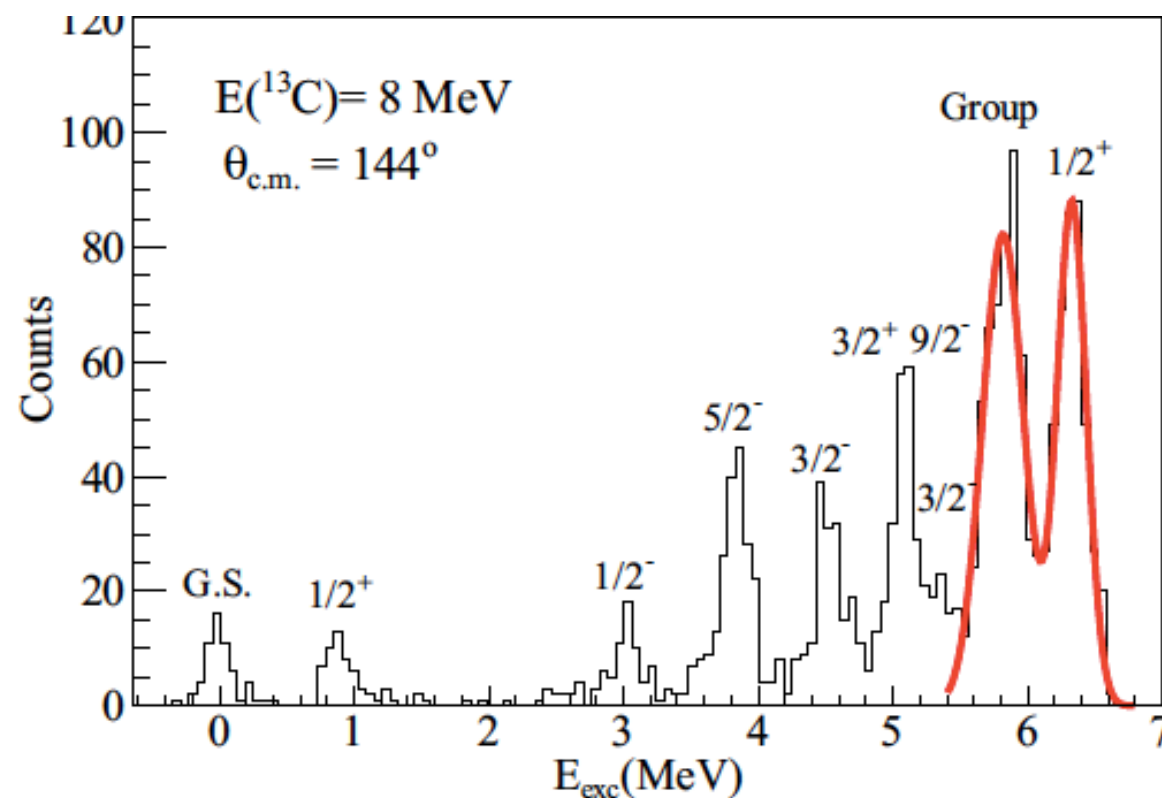
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The ${}^6\text{Li}({}^{13}\text{C},d)$ reaction at sub-Coulomb energy

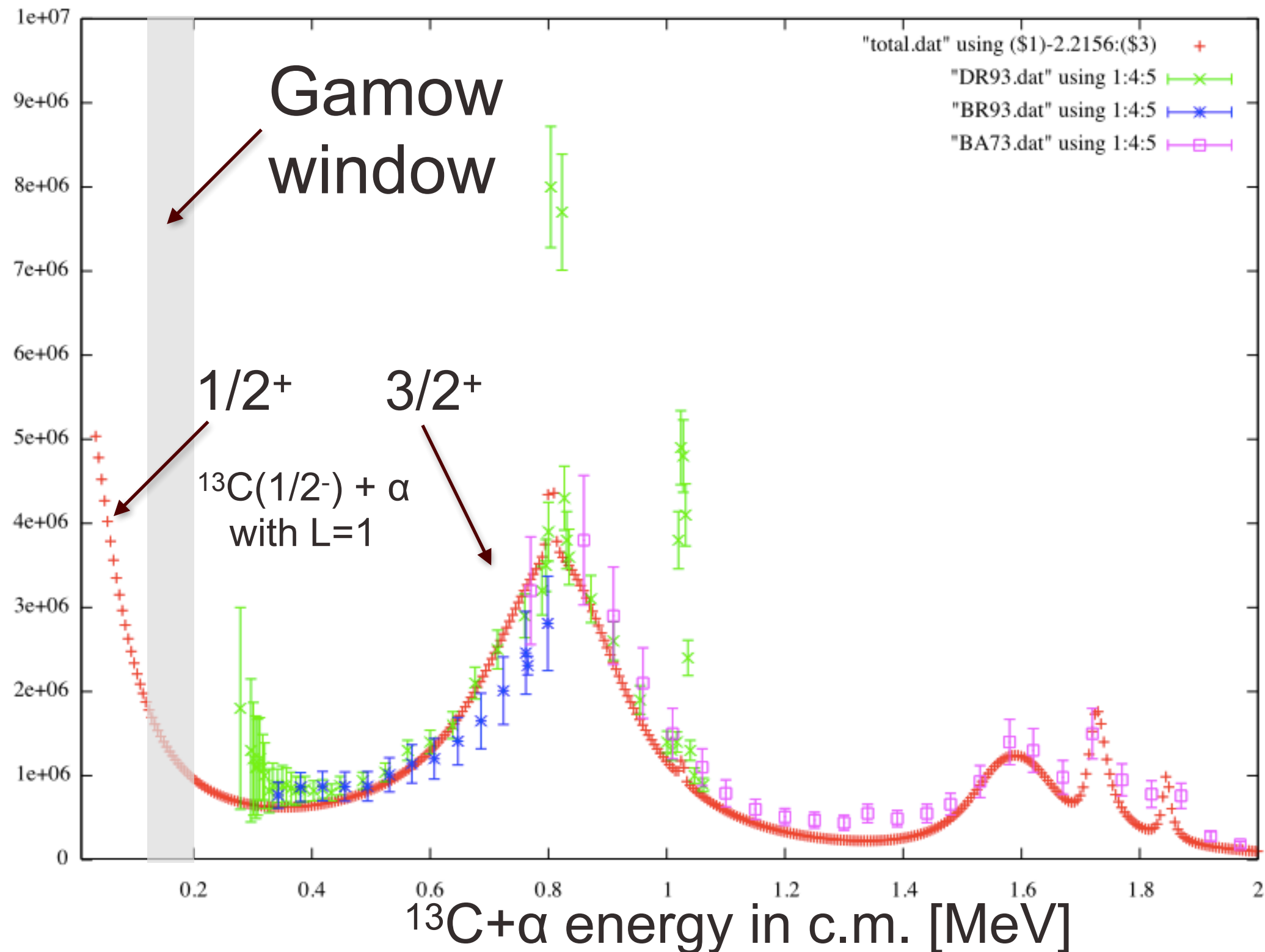
✓ Spectrum of deuterons from ${}^6\text{Li}({}^{13}\text{C},d)$ reaction. Total energy of the ${}^{13}\text{C}$ beam is 8 MeV.

✓ Angular distribution

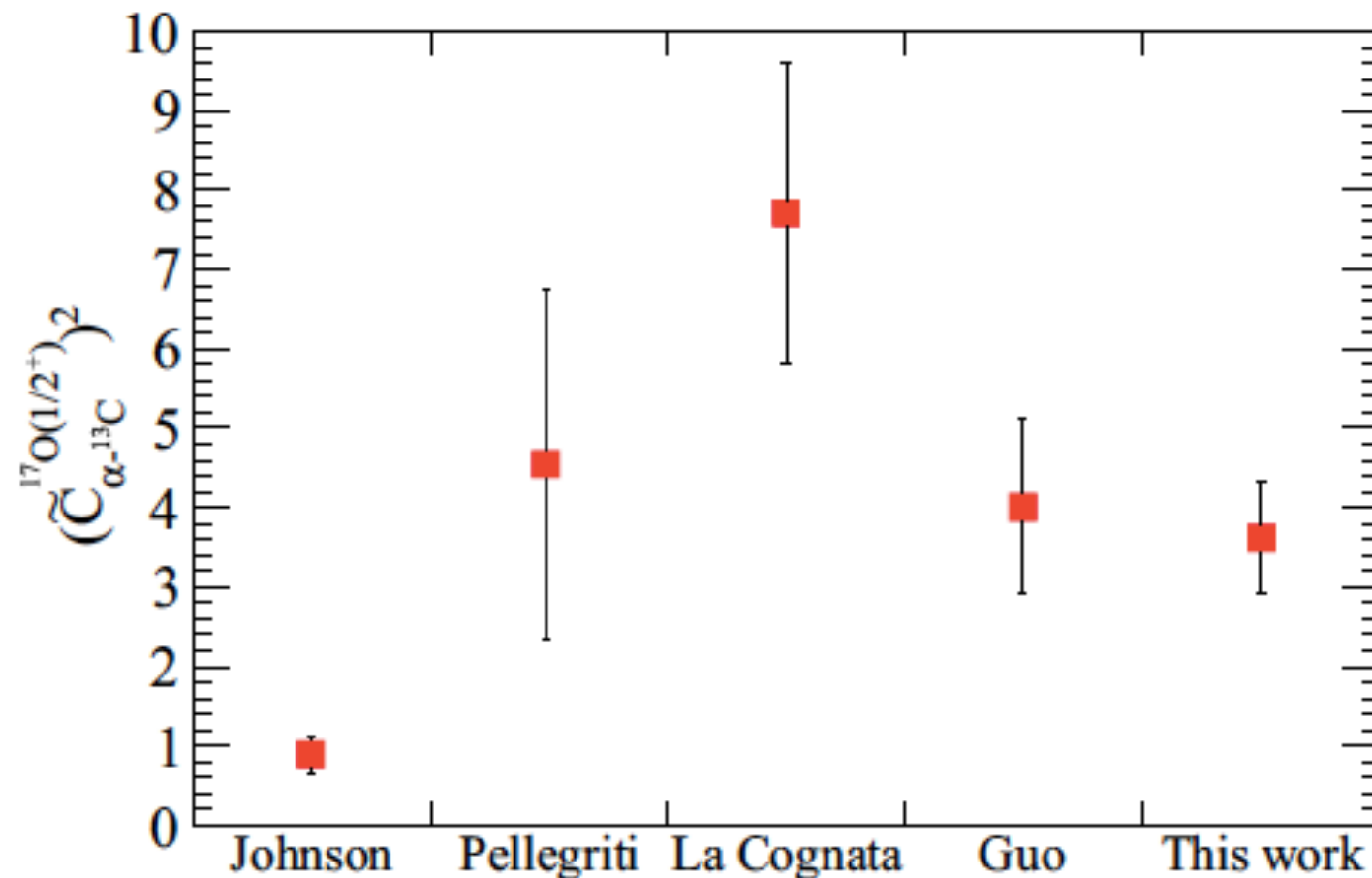


The s-factor for the $^{13}\text{C}(\alpha, n)$

s-factor [eV b]



α - ANC for the $1/2^+$ state at 6.356 MeV in ^{17}O .



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