

# Halo-independent bounds on Inelastic Dark Matter

Arpan Kar

CQUeST, Sogang University  
Seoul, Korea

Based on: *JCAP 11 (2023) 077* & *JCAP 03 (2023) 011*

in collaboration with: *S. Scopel and S. Kang*

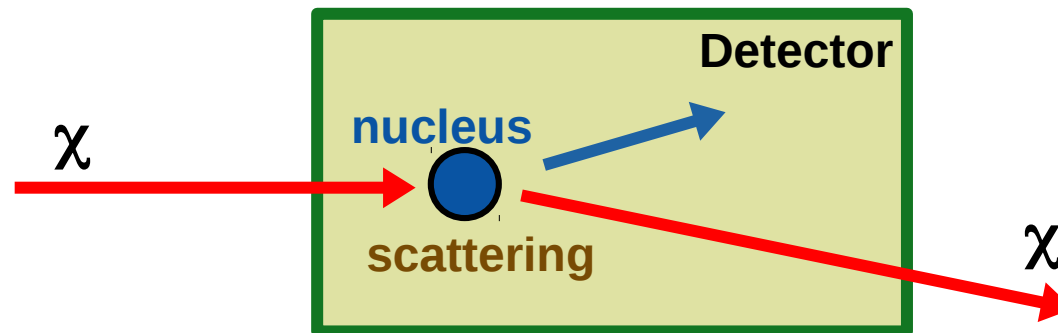
*The 4th Workshop on New Physics Opportunities at Neutrino Facilities  
(NPN 2024)*

*Institute for Basic Science (IBS)*

*Jun 3 - 5, 2024*

# WIMP dark matter searches

- Cold Dark Matter (CDM): provides  $\sim 25\%$  of the energy density of the Universe; evidences are only through gravitational effects
- Weakly Interacting Massive Particles (WIMPs): one of the most popular candidates for CDM [mass in GeV – TeV range]
- **Direct Detection (DD)**: A popular technique to search for WIMPs
  - mainly based on scatterings of local WIMPs off nuclear targets in terrestrial detectors and the observation of the corresponding nuclear recoil signal



- Non-detection of any new signal in DD experiments
  - ⇒ upper-limit on the WIMP-nucleon coupling that drives the WIMP-nucleus scattering

# *Uncertainties in the signal prediction*

- Two classes of major uncertainties in the signal prediction:
  - Nature of the WIMP-nucleus interaction
  - WIMP speed distribution in the local halo that determines the incoming WIMP flux
  
- WIMP-nucleus interaction:  
common choice: **standard spin-independent (SI)** or **spin-dependent (SD)** interaction
  
- WIMP speed distribution in the local halo:  
common choice: a Maxwell-Boltzmann speed distribution w.r.t. the Galactic reference frame  
(and boosted to the Lab frame)  
**Standard Halo Model (SHM)**

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## WIMP speed distribution: Halo-independent approach

$f(u)$   $\Rightarrow$  WIMP speed distribution in the local halo

$$\int_0^{u_{max}} f(u) du = 1$$

$u$  = WIMP speed in the halo (w.r.t. Solar frame)

$u_{max}$  = Galactic escape speed (w.r.t. Solar frame)  
 $\approx 800$  km/s

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- MB distribution (based on Isothermal Model) provides a zero-order approximation to  $f(u)$
- Numerical simulations of Galaxy formation can only tell us about the statistical average properties of halos
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- Growing number of observed dwarf galaxies suggests that our halo is not perfectly thermalized

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- **Halo-independent approach:**
  - **Constraint on the WIMP interaction independent of the WIMP speed distribution in the halo**

$f(u)$   $\iff$  any possible WIMP speed distribution

## Halo-independent approach using Direct Detection

- Direct Detection (DD) experiments are sensitive only for a WIMP speed  $u > u_{th}$

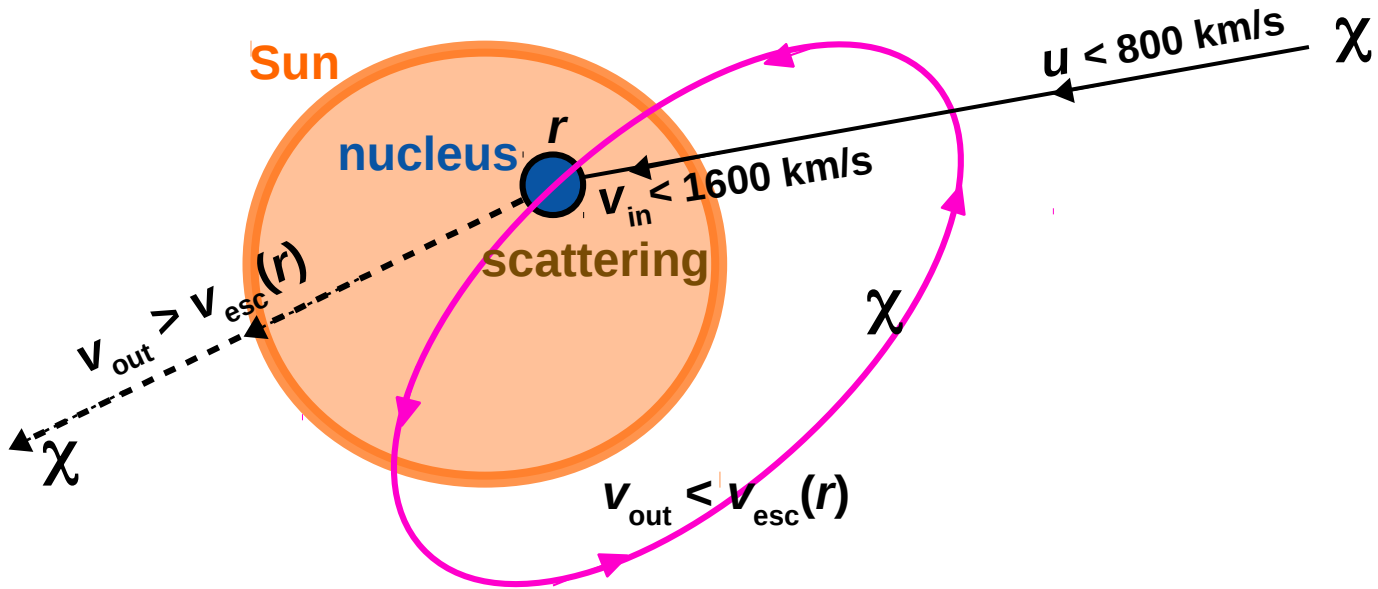
$$u_{th} = \sqrt{\frac{m_N}{2\mu_{\chi N}^2} E_{th}} \quad (\mu_{\chi N} = \text{WIMP-nucleus reduced mass})$$

- For a  $f(u)$  concentrated below  $u_{th}$  the DD sensitivity is zero
- A halo-independent approach is not possible using only DD



# Capture of WIMPs in the Sun and the Neutrino Signal

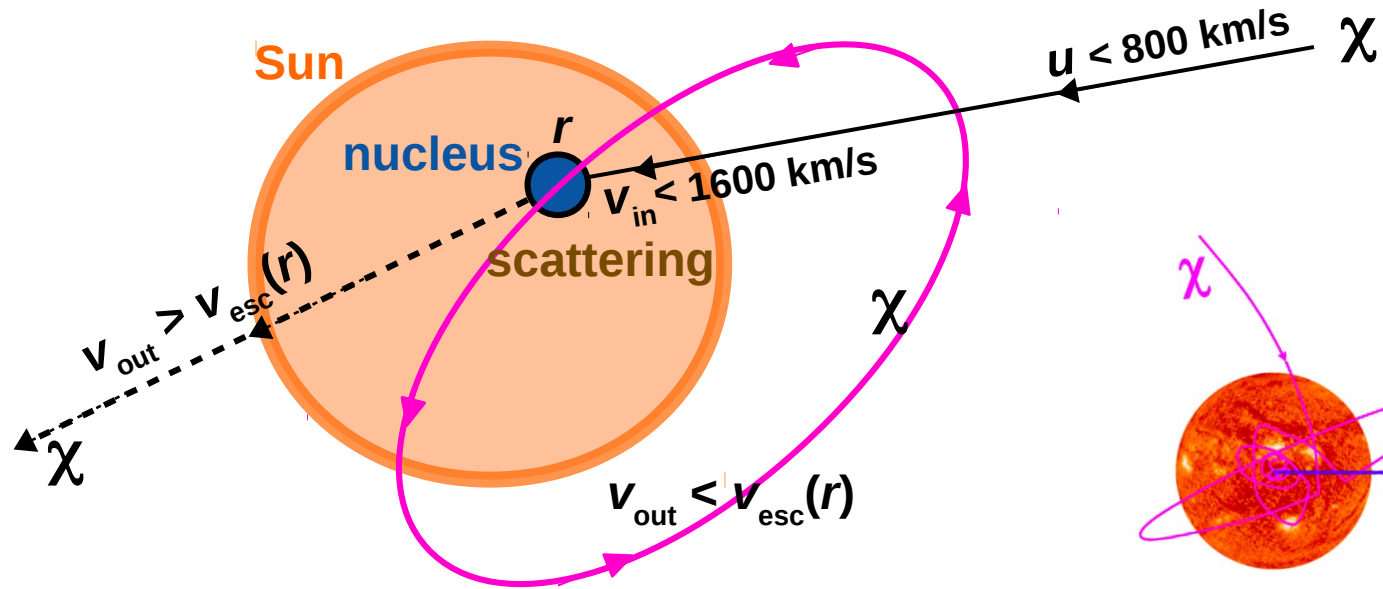
- Capture of WIMPs in the Sun is favoured for low (or even vanishing) speeds



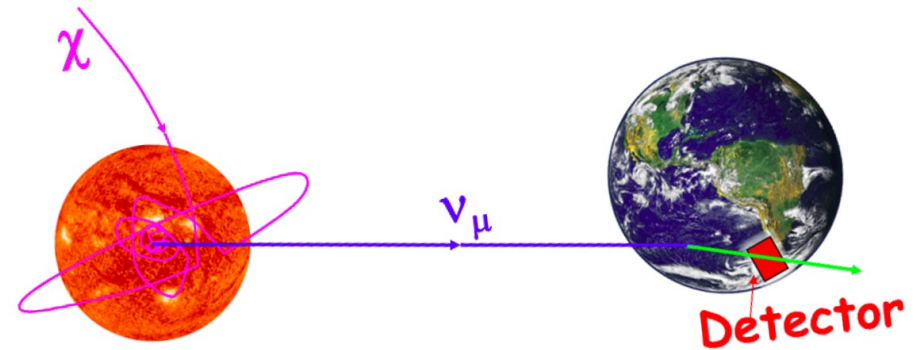
$v_{esc}(r)$  = escape speed inside the Sun  
= [620 , 1400] km/s  
(from solar surface to center)

# Capture of WIMPs in the Sun and the Neutrino Signal

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see also Talk by Carsten Rott



## WIMP annihilation in the Sun

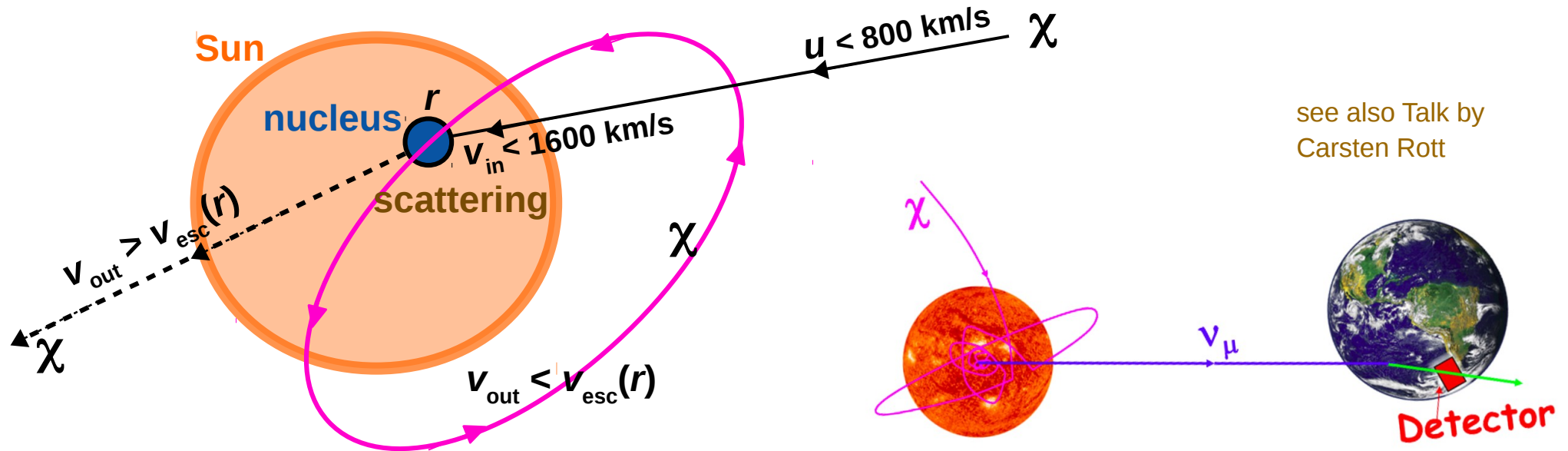
$$\chi\chi \rightarrow b\bar{b}, \tau^+\tau^-, W^+W^-, \dots$$

$$\Rightarrow \nu(\bar{\nu})$$

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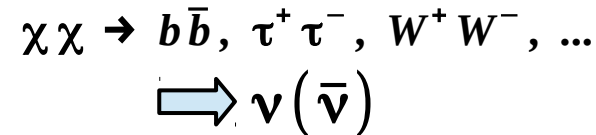
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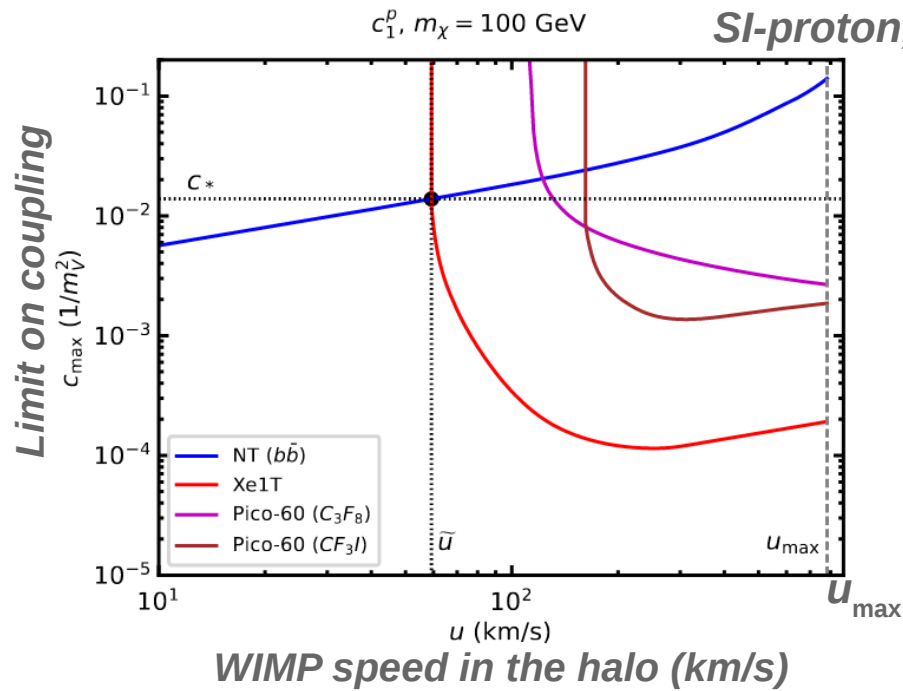
**WIMP annihilation in the Sun**



- **A possible solution to the Halo-independent approach:  
 Direct detection (DD) “+” Neutrino Telescope (NT)**

[F. Ferrer, A. Ibarra, S. Wild; (JCAP 09 (2015) 052]

# Halo-independent approach



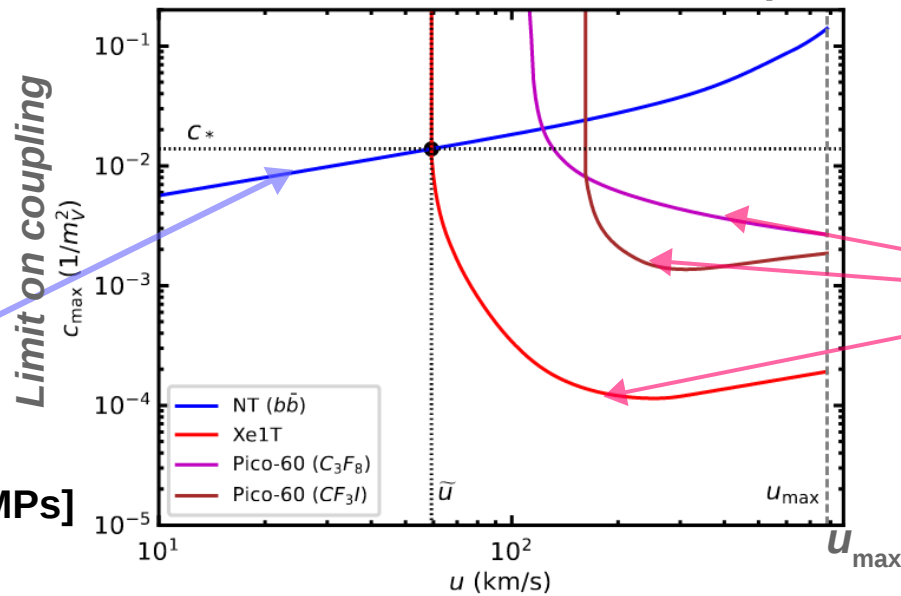
[S. Kang, AK, S. Scopel,  
(JCAP 03 (2023) 011)]

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 $\approx 800 \text{ km/s}$

# Halo-independent approach

$c_1^p, m_\chi = 100 \text{ GeV}$

SI-proton,  $m_\chi = 100 \text{ GeV}$



[S. Kang, AK, S. Scopel, (JCAP 03 (2023) 011)]

**Direct detection (DD)**

**[sensitive to high speed WIMPs]**

**Neutrino Telescope (NT)**

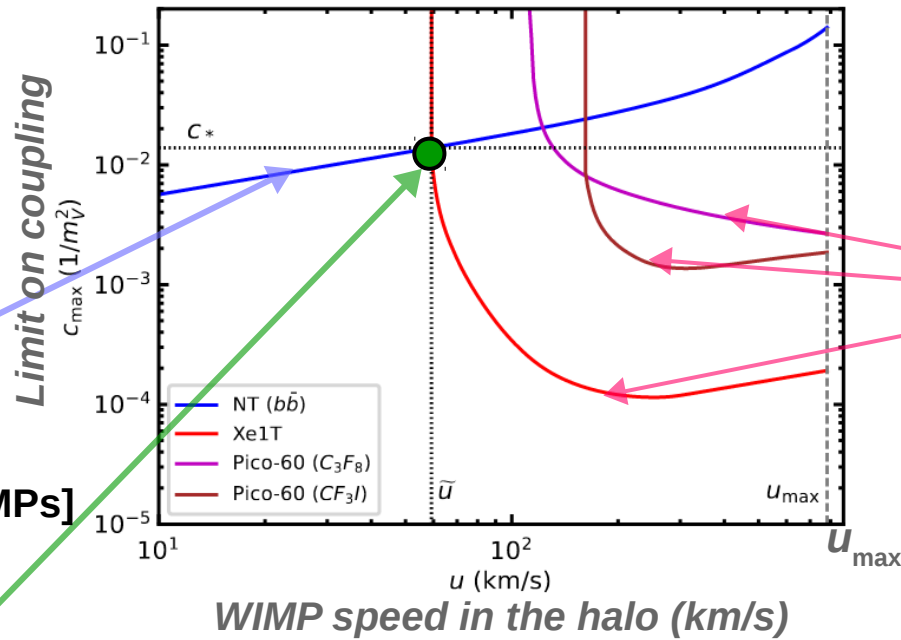
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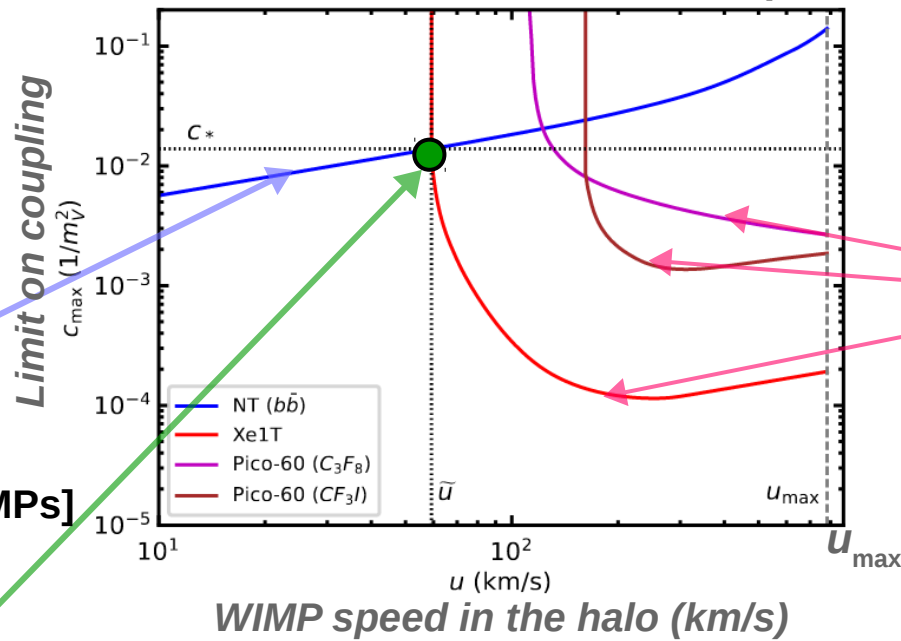
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Halo-independent limit is determined by the weakest point of the experimental sensitivity

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- A finite Halo-independent bound requires Experimental sensitivity covering the full WIMP speed range  $[0, u_{\max}]$

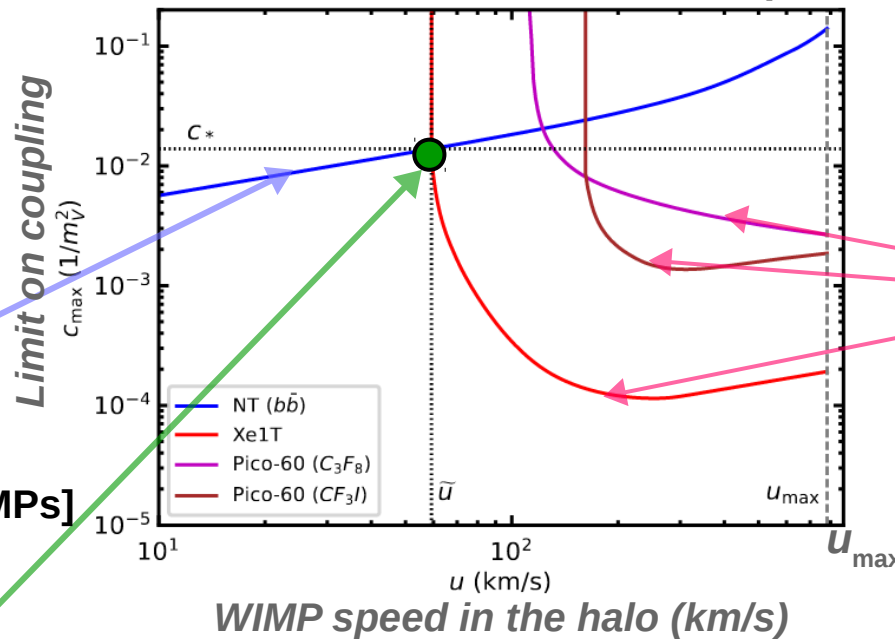


Neutrino Telescope (NT) observations should be combined with Direct Detection (DD)

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Neutrino Telescope (NT)

[sensitive to low speed WIMPs]

Halo-independent limit is determined by the weakest point of the experimental sensitivity

DD : XENON, PICO

NT : IceCube, Super-K [ $\chi\chi \rightarrow b\bar{b}$ ]

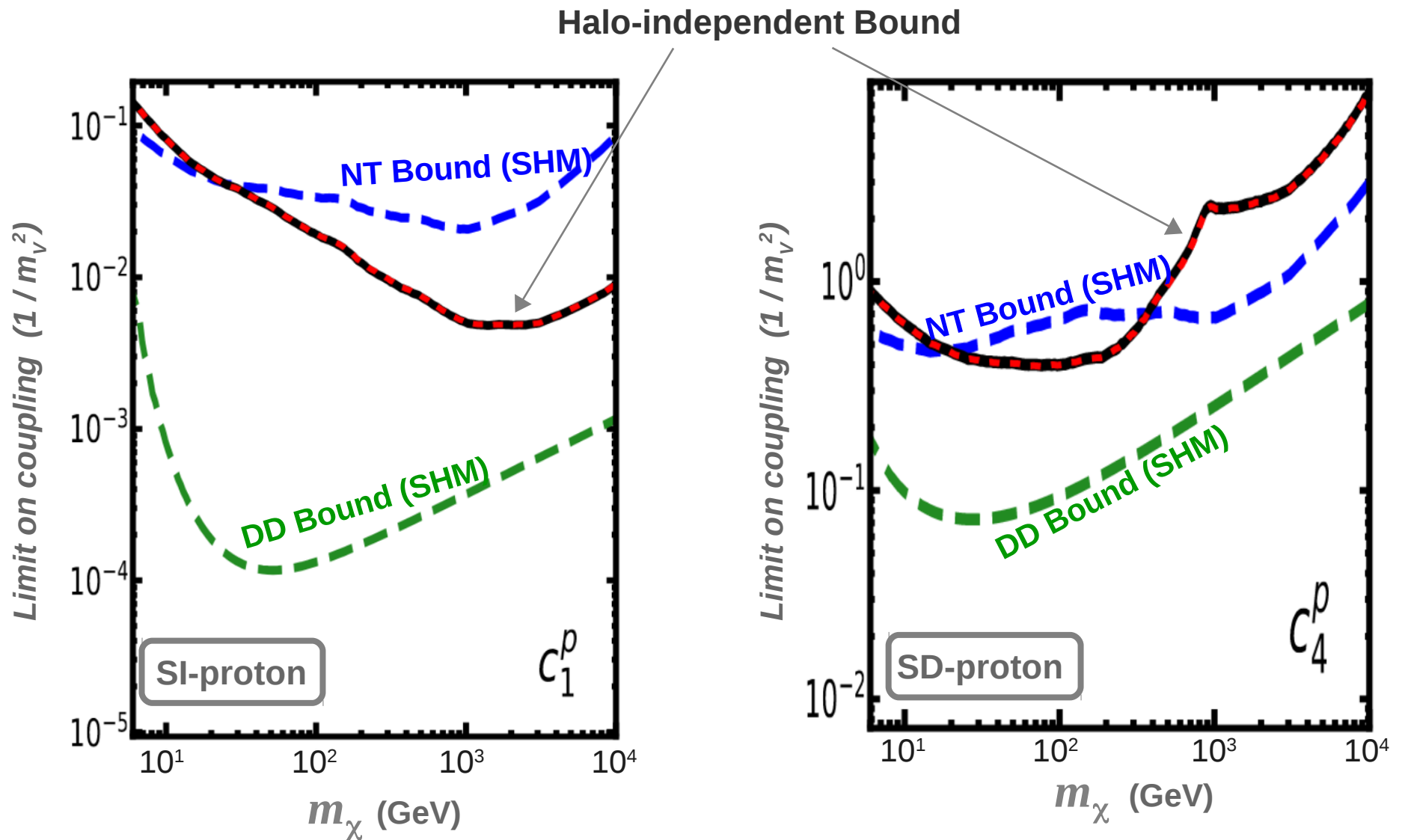
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# Halo-independent bounds on WIMP-nucleon couplings

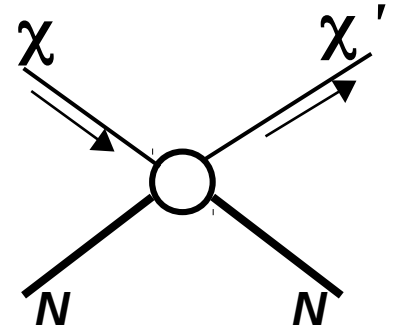


[S. Kang, AK, S. Scopel, (JCAP 03 (2023) 011)]

**What is the situation for Inelastic WIMP dark matter scenario?**

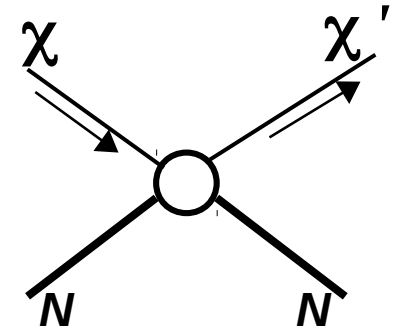
## Inelastic Dark Matter (IDM)

- WIMP DM  $\chi$  scatters off a Nucleus  $N$  by making a transition to a slightly heavier state  $\chi'$
- $m_{\chi'} - m_{\chi} = \delta > 0$



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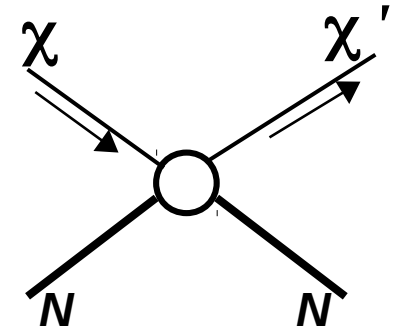
$$\frac{1}{2} \mu_{\chi N} v_{\text{in}}^2 > \delta, \quad [\mu_{\chi N} \equiv \text{reduced mass} = \frac{m_{\chi} m_N}{m_{\chi} + m_N}]$$

$$\Rightarrow v_{\text{in}} > \sqrt{\frac{2\delta}{\mu_{\chi N}}} = v_{N*}$$

**Condition for Inelastic Scattering**

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- For Direct Detection (DD) :  $\underbrace{\text{max. } [v_{\text{in}}] \approx 800 \text{ km/s}}_{\text{Galactic escape speed}} \Rightarrow \text{max. } [\delta] \text{ that can be probed} \approx 200 \text{ keV}$

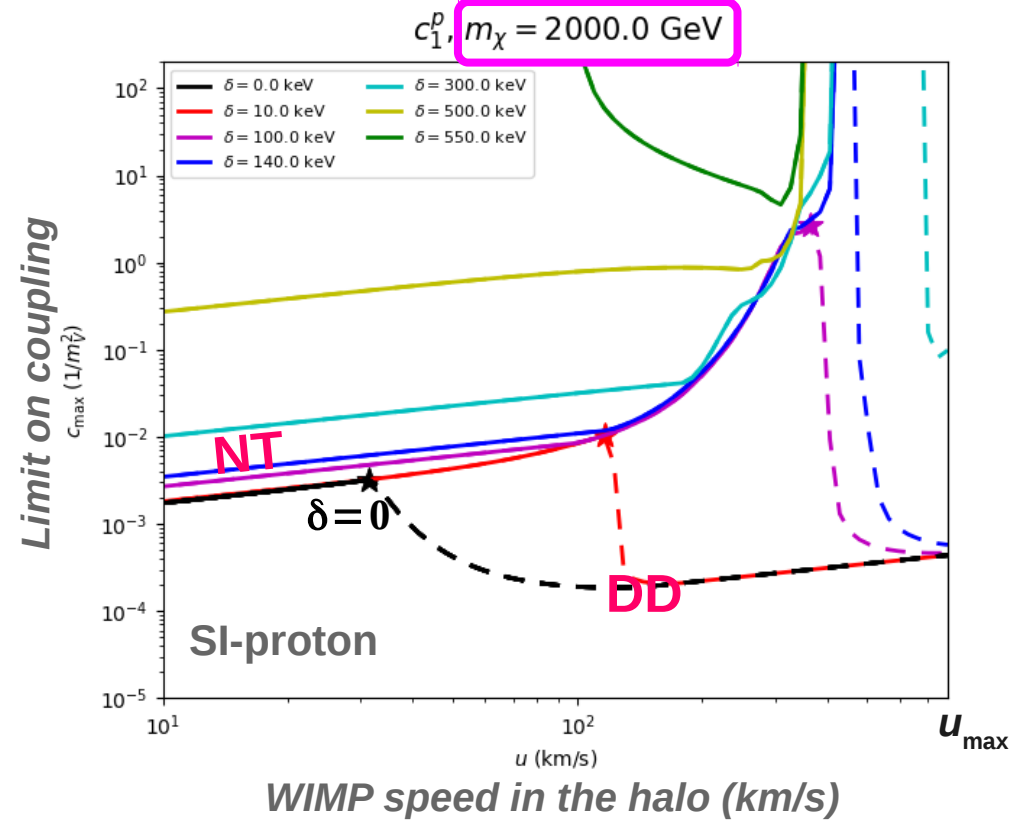
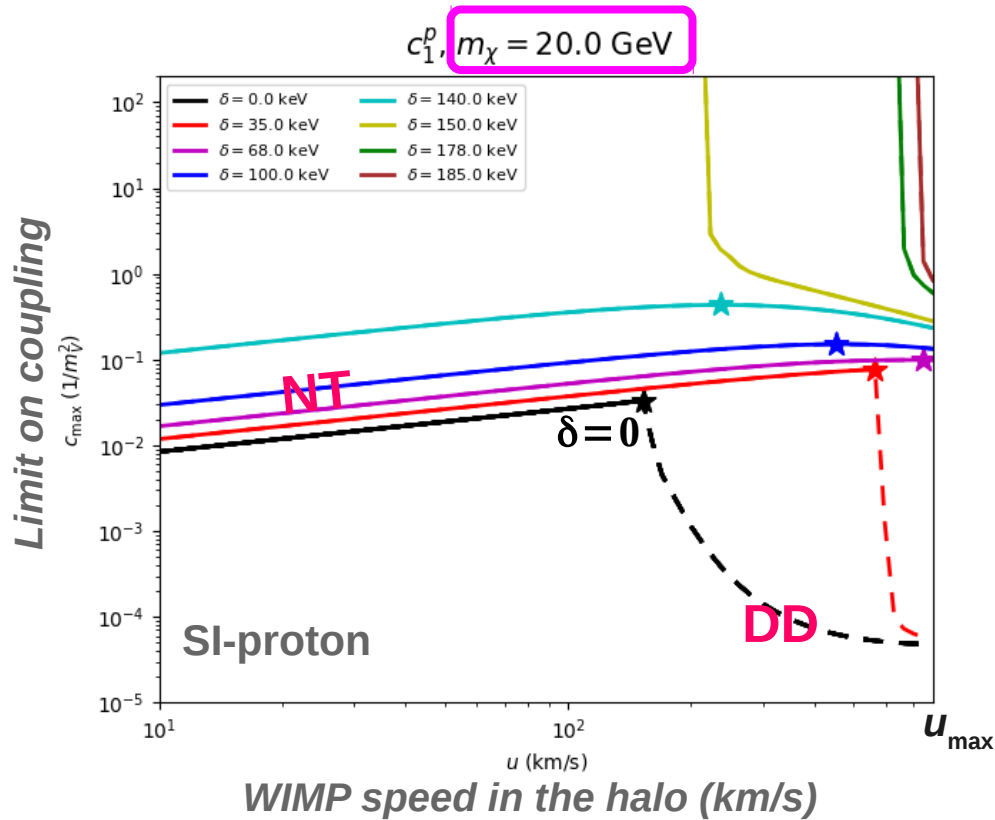
- For Capture in the Sun :  $\underbrace{\text{max. } [v_{\text{in}}] \approx 1600 \text{ km/s}}_{\text{due to Solar gravity}} \Rightarrow \text{max. } [\delta] \text{ that can be probed using a Neutrino Telescope} \approx 600 \text{ keV}$

$$v_{\text{in}} = \sqrt{u^2 + v_{\text{esc}}(r)^2}$$

$$v_{\text{esc}}(r) = [620, 1400] \text{ km/s} \\ \text{(from solar surface to center)}$$

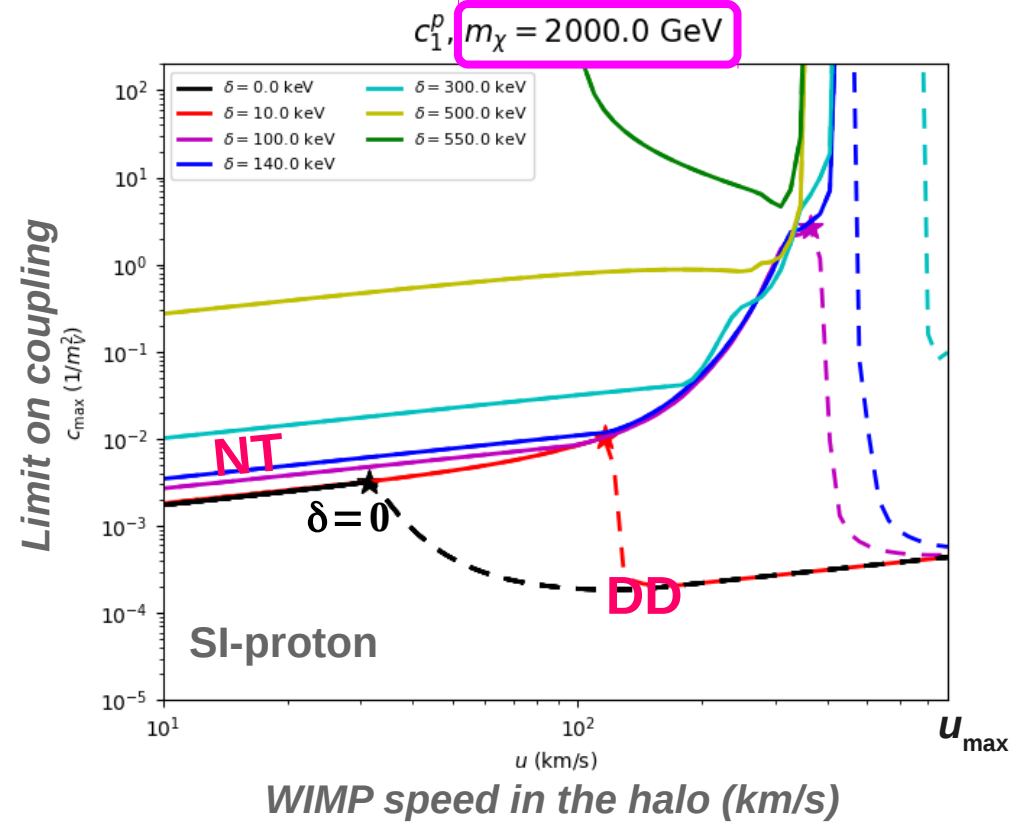
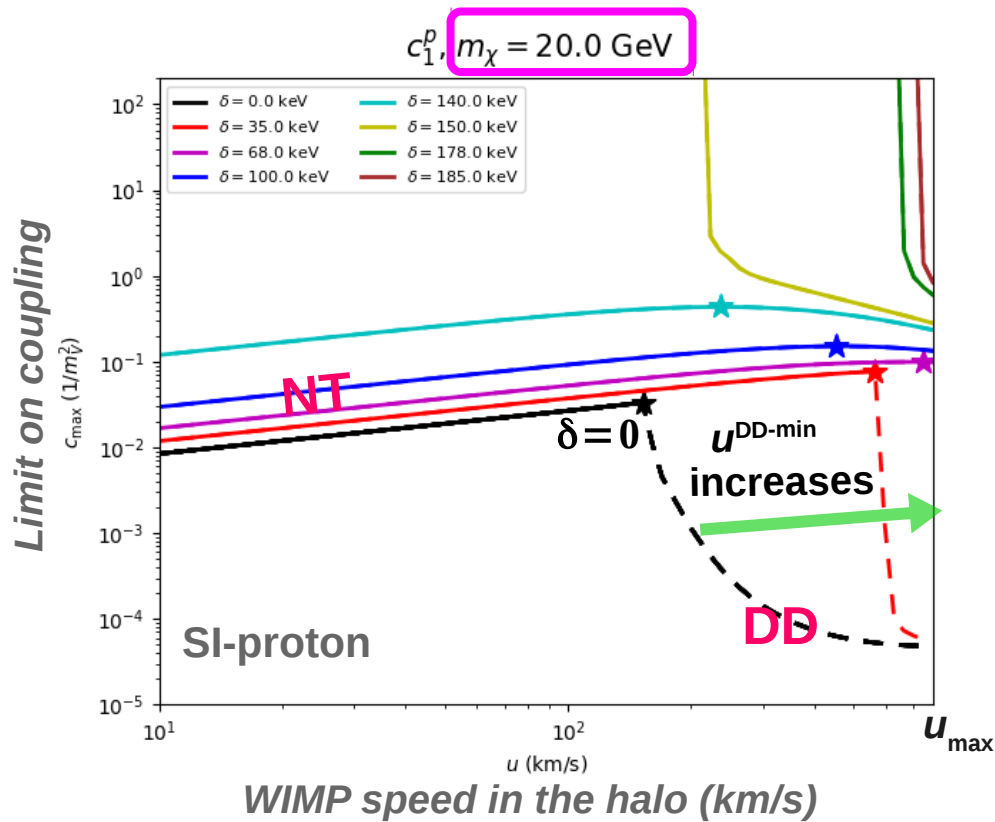
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NT : continues curves  
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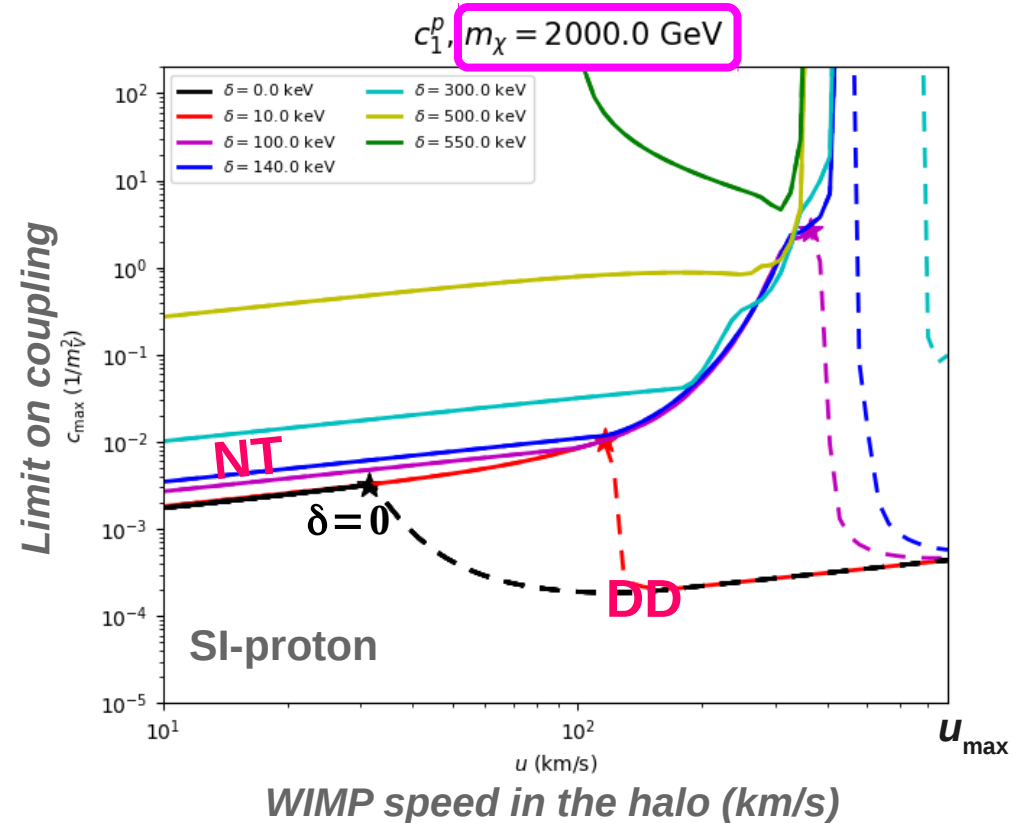
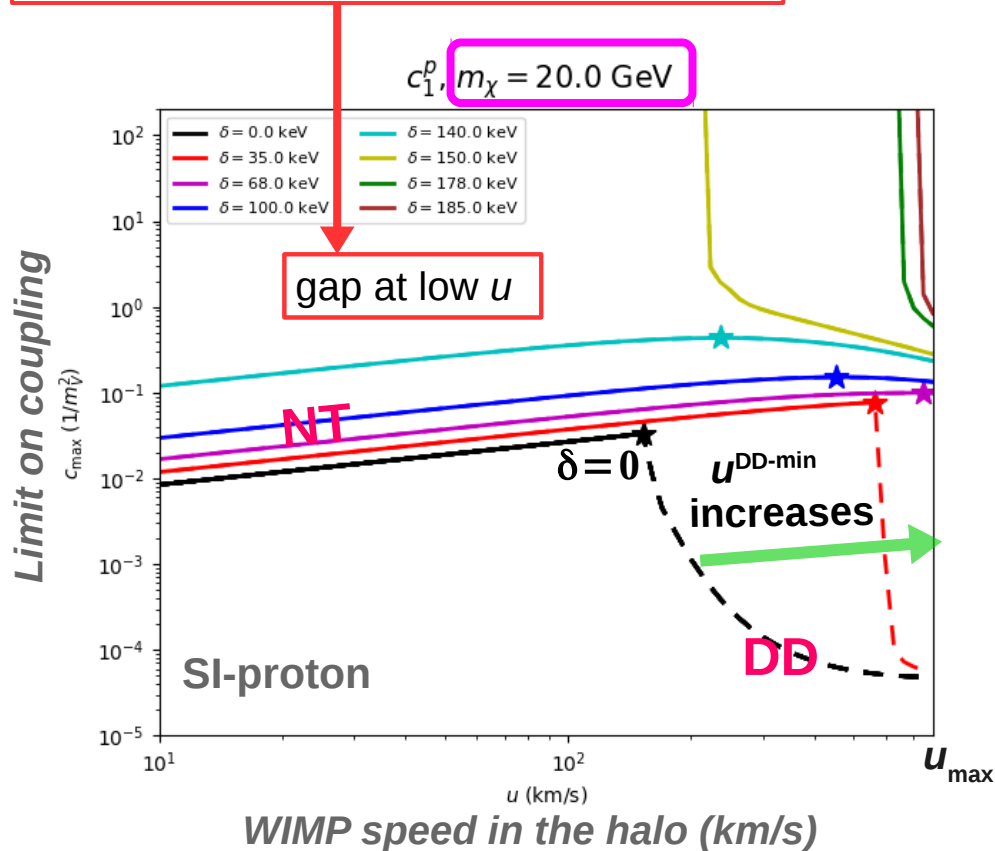
$u^{\text{DD-min}}$  : minimum WIMP speed required to produce a DD signal

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for larger  $\delta$ 's, low  $u$ 's are not enough to satisfy  $\mathbf{v}_{in}^2 = u^2 + v_{esc}(r)^2 \geq \frac{2\delta}{\mu_{\chi T}}$

**Condition for IDM scattering in the Sun**

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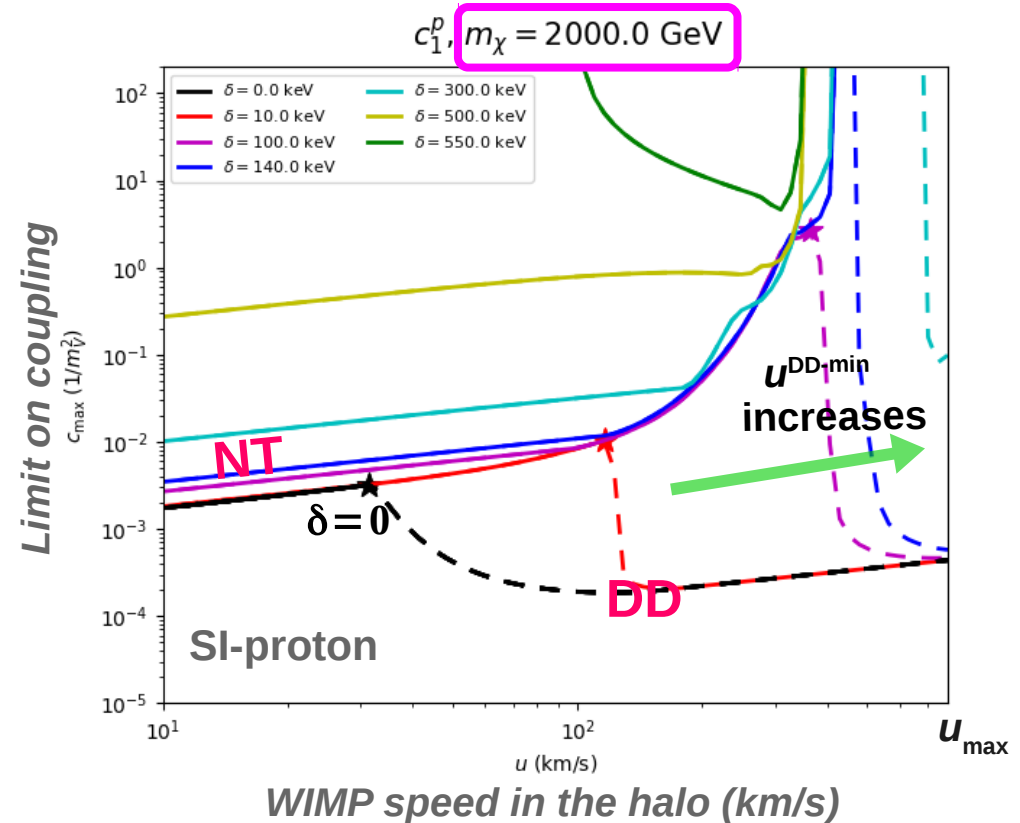
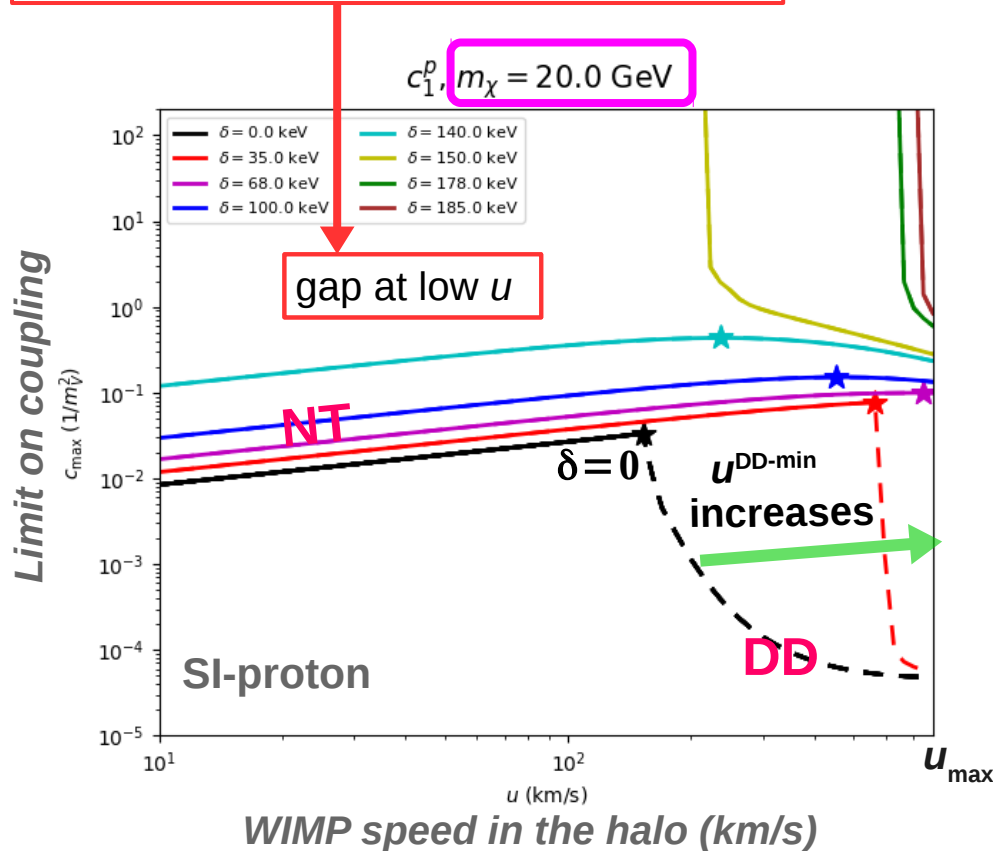


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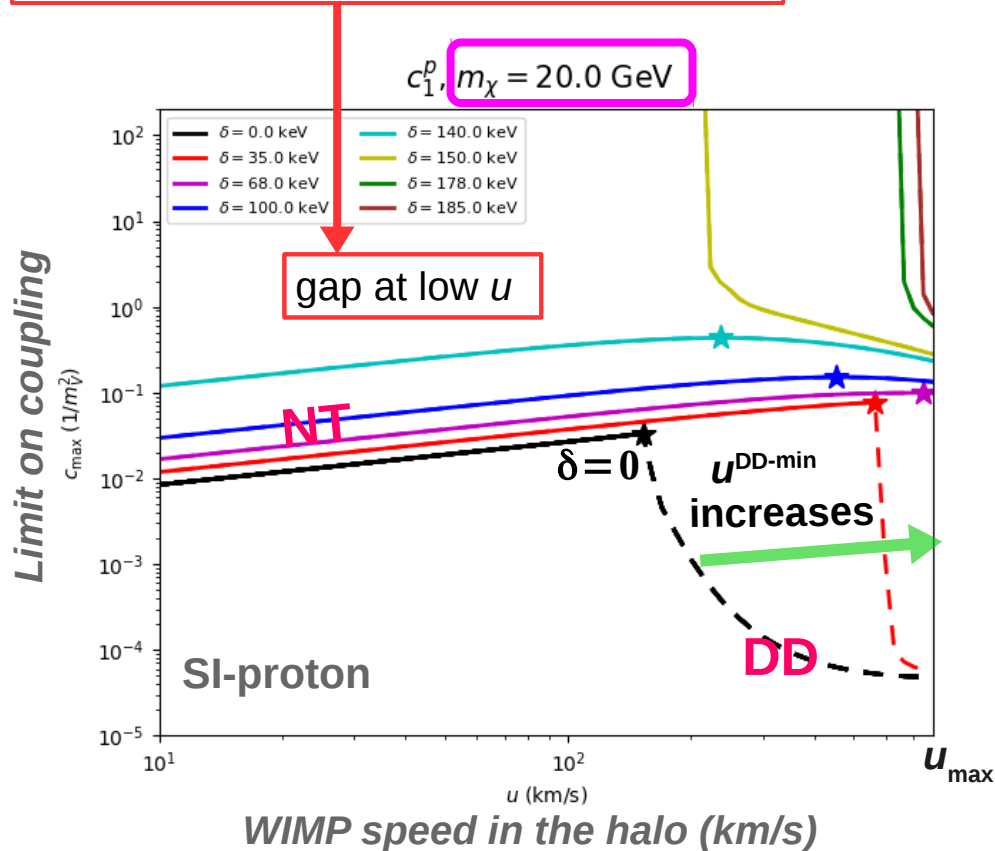


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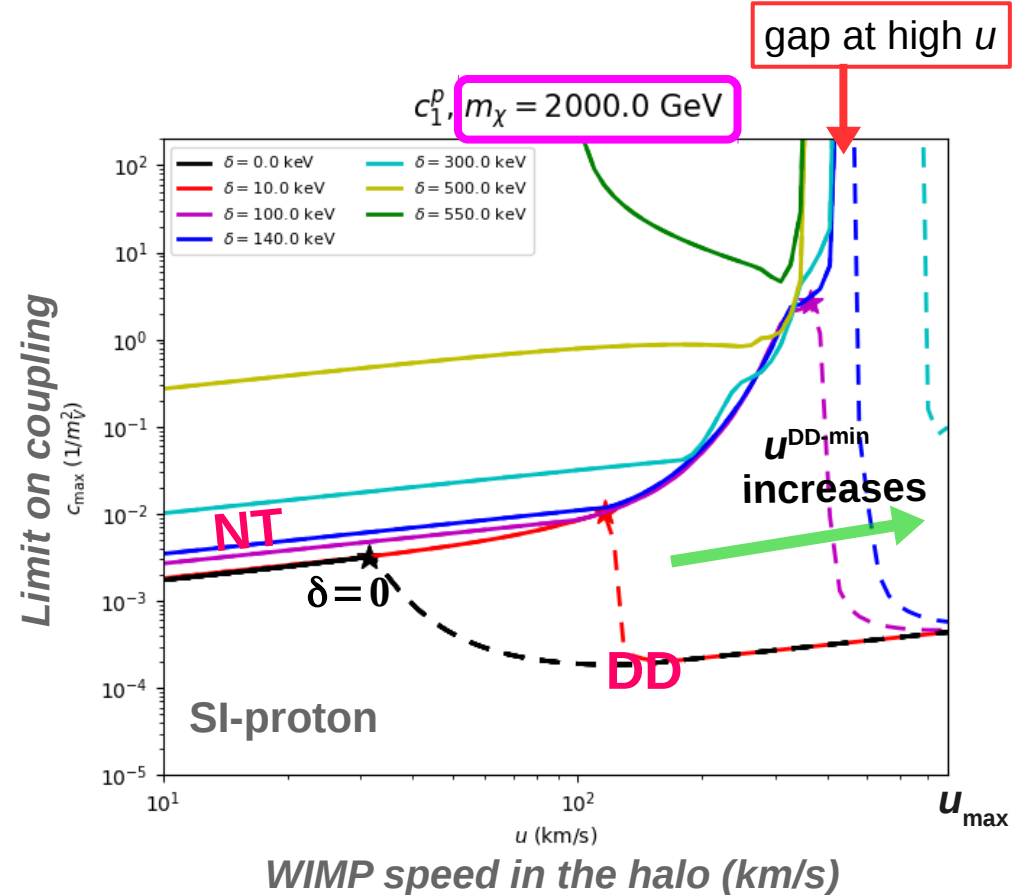
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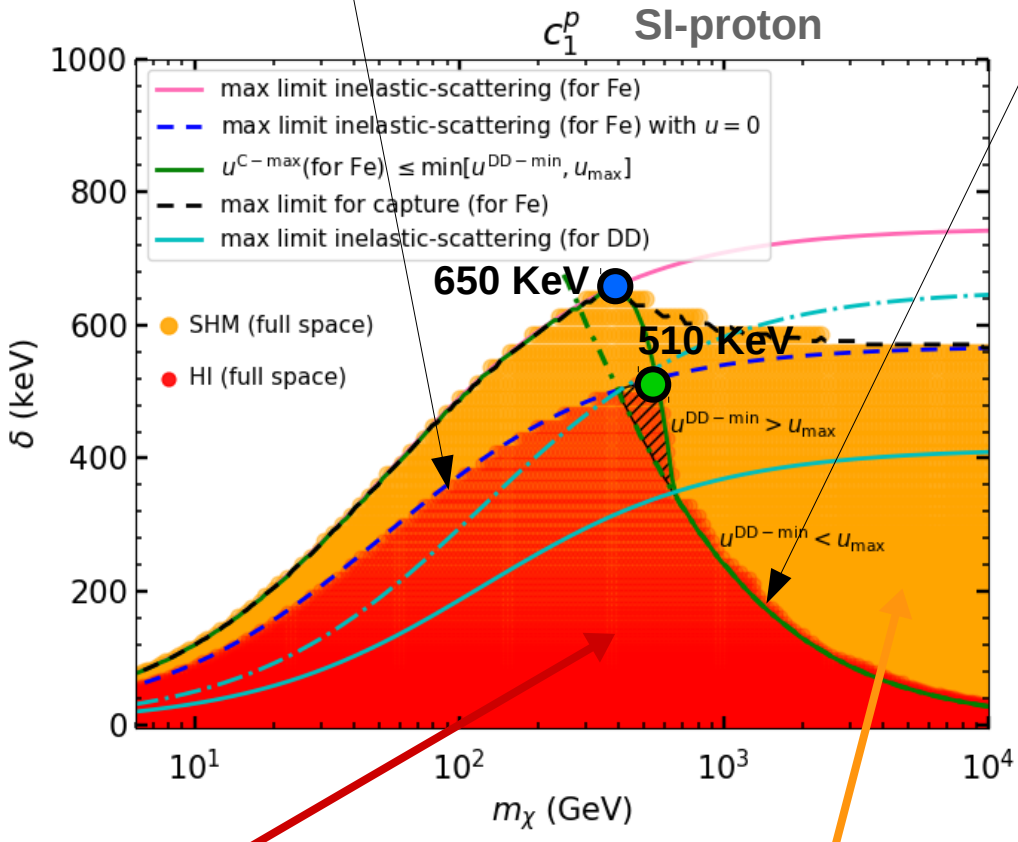
$u^{DD-min}$  : minimum WIMP speed required to produce a DD signal

$u^{C-max}$  : maximum WIMP speed beyond which the WIMP can not be captured in the Sun

# IDM: parameter space in Halo-independent approach

~~Condition for IDM scattering in the Sun~~

$$u^{C-\max} < u^{DD-\min}$$



Halo-independent method

Standard Halo Model (SHM)

[S. Kang, AK, S. Scopel, (JCAP 11 (2023) 077)]

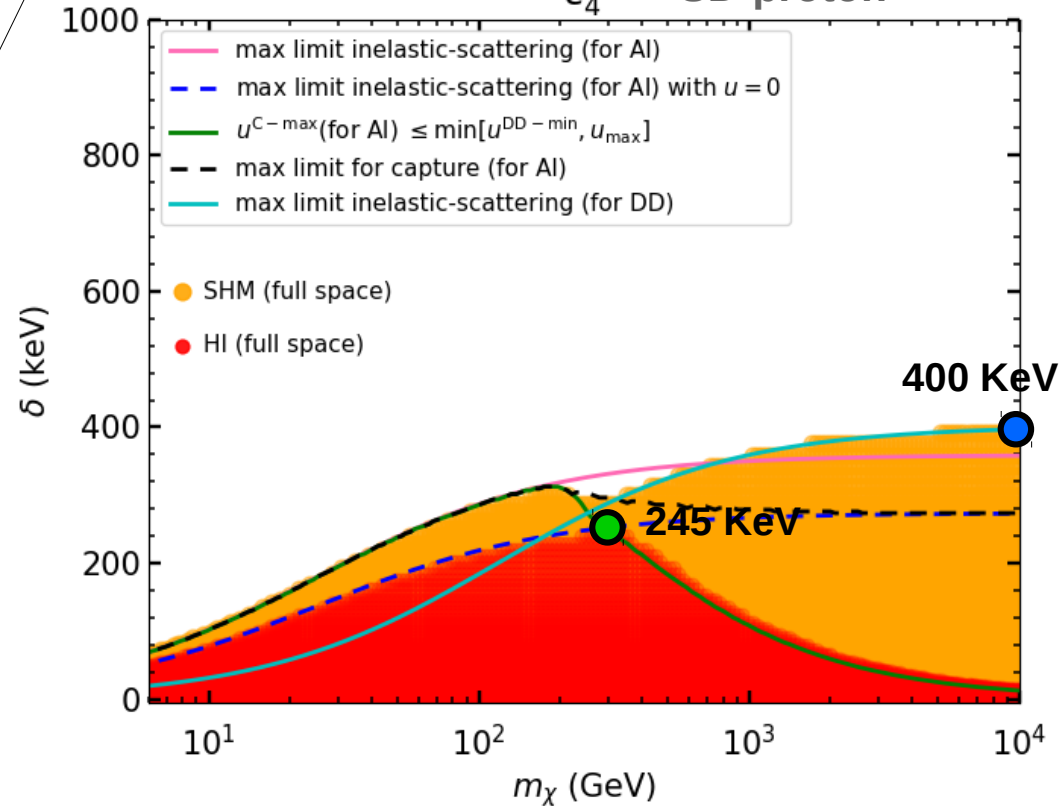
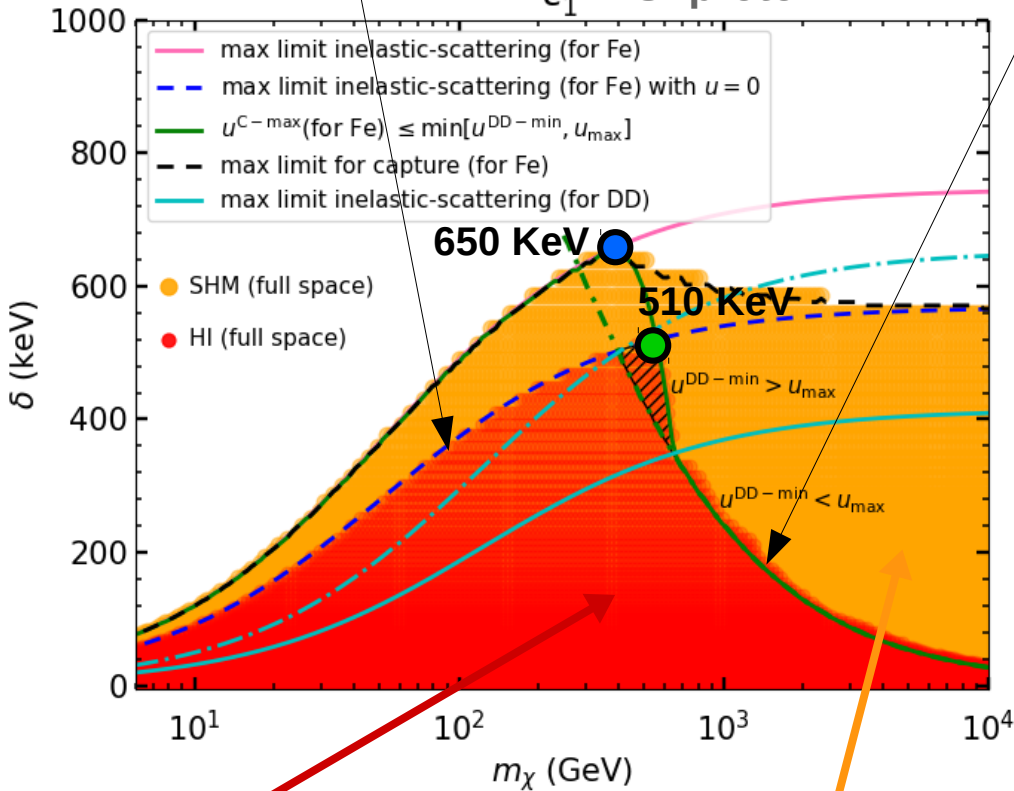
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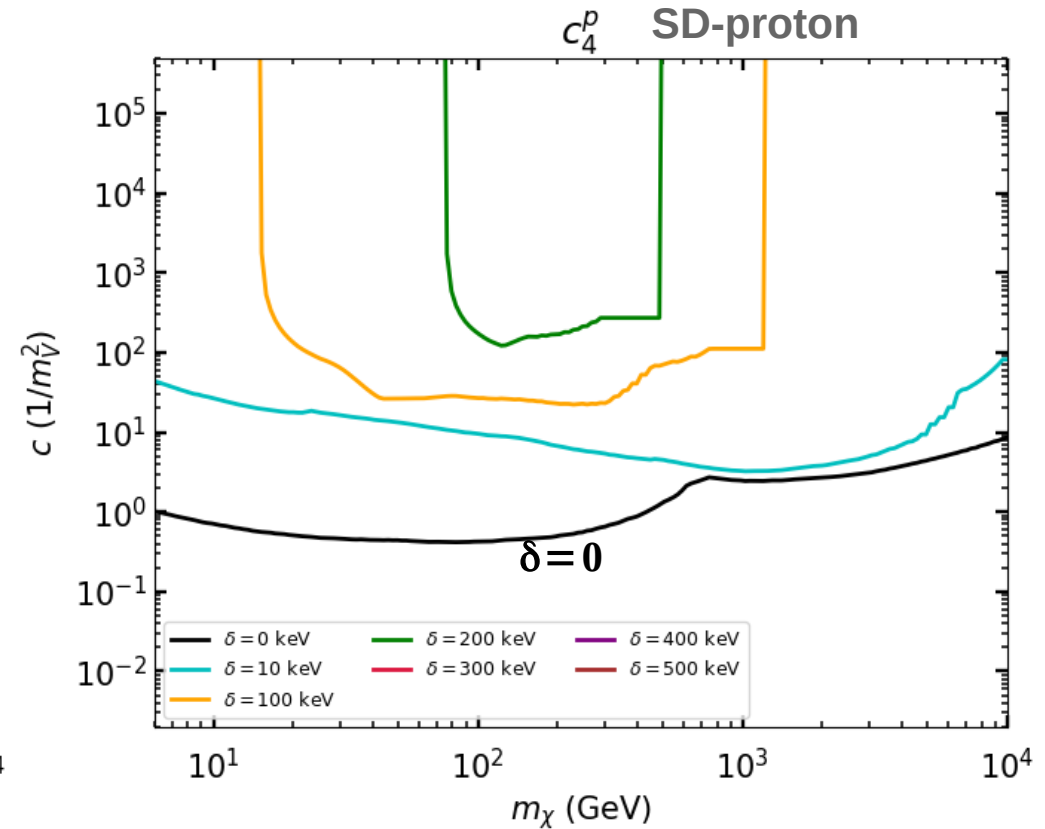
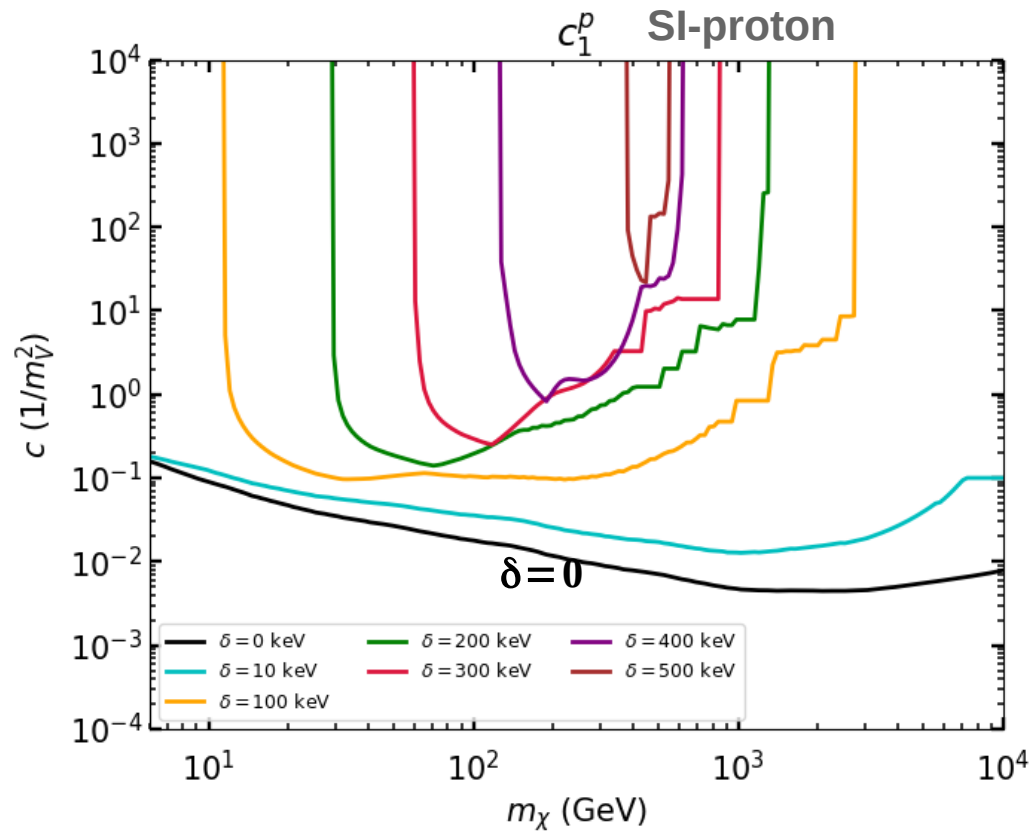


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# IDM: Halo-independent bound on WIMP-nucleon coupling



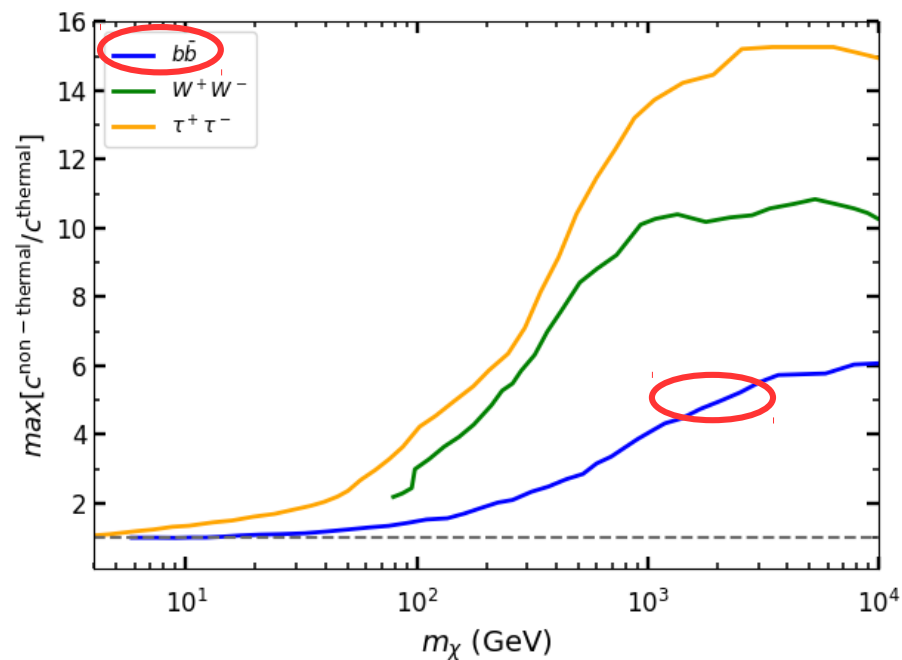
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# IDM: issue of thermalization

Relaxation of the Neutrino Telescope bounds on the coupling when the assumption of thermalization of the WIMPs with the solar plasma is not made

$$\left. \vphantom{\frac{c^{\text{non-thermal}}}{c^{\text{thermal}}}} \right\} \frac{c^{\text{non-thermal}}}{c^{\text{thermal}}}$$

$$\max. \left[ \frac{c^{\text{non-thermal}}}{c^{\text{thermal}}} \right]$$



$$\frac{c^{\text{non-thermal}}}{c^{\text{thermal}}} \simeq \left( \frac{V_\odot}{2\langle\sigma v\rangle t_\odot^2 \Gamma_{\text{exp}}} \right)^{1/4}$$

[S. Kang, AK, S. Scopel, (JCAP 11 (2023) 077)]

# Summary

- We discuss **halo-independent bounds** (bounds independent of the WIMP speed distribution in the halo) on the **Inelastic Dark Matter (IDM)** scenario  $\chi + N \rightarrow \chi' + N$   $m_{\chi'} - m_{\chi} = \delta > 0$
- A finite halo-independent bound requires experimental sensitivity over the full WIMP speed range
  - ➡ combine **Direct detection (DD)** & **Neutrino Telescope (NT)** [ **complementary** ]  
(searches for the signal from WIMPs captured in the Sun)
- For  $\delta$  larger than some value (depending on  $m_{\chi}$ ) the complementarity between DD & NT is lost (the full WIMP speed range cannot be probed anymore)
  - ➡ A halo-independent bound is Not possible anymore for such larger  $\delta$ 's
  - ➡ In such cases a specific model for the WIMP speed distribution in the halo (e.g., the SHM) is required to obtain a constraint on the WIMP-nucleon coupling
- When the assumption of thermalization of IDM in the Sun is relaxed the effect on the bounds is relatively mild

Thank  
you 

**Backup slides**



## IDM: Direct Detection (DD) signal

$$R_{\text{DD}} = M \tau_{\text{exp}} \underbrace{\left( \frac{\rho_{\odot}}{m_{\chi}} \right)}_{\text{local DM density}} \int du f(u) u \sum_T N_T \Theta(u^2 - v_{T*}^2) \int_{E_{\text{min}}(u)}^{E_{\text{max}}(u)} dE \zeta_T \frac{d\sigma_T}{dE}$$

scattering cross-section

$T = \text{Target Nucleus in DD}$

$$E_{\text{min,max}}(u) = \frac{\mu_{\chi T}^2 u^2}{2m_T} \left( 1 \mp \sqrt{1 - \frac{2\delta}{\mu_{\chi T} u^2}} \right)^2 \quad v_{T*} = \sqrt{\frac{2\delta}{\mu_{\chi T}}}$$

### • Kinematic conditions:

1) Incoming WIMP speed  $u \geq v_{T*} = \sqrt{\frac{2\delta}{\mu_{\chi T}}}$  [condition for IDM scattering]

2)  $E_{\text{max}} \geq \text{max.} [E_{\text{min}}, E_{\text{th}}]$   $E_{\text{th}}$ : threshold energy of the DD experiment

$$\Rightarrow u \geq u^{\text{DD-min}} = \text{max.} \left[ \sqrt{\frac{2\delta}{\mu_{\chi T}}}, \frac{1}{\sqrt{2m_T E_{\text{th}}}} \left( \frac{m_T E_{\text{th}}}{\mu_{\chi T}} + \delta \right) \right]$$

- For a finite  $\delta$ , the minimum WIMP speed to produce a DD signal increases

# IDM: Capture in the Sun

$$\Gamma_{\odot} = \frac{C_{\odot}}{2} \tanh^2(t_{\odot}/\tau_{\odot})$$

Annihilation rate of WIMPs captured in the Sun that produces the neutrino flux

$C_{\odot}$  : Capture rate       $t_{\odot}$  : Solar age       $\tau_{\odot} = (C_{\odot}C_A)^{-\frac{1}{2}}$  : equilibration time for Capture & Annihilation

$$C_{\odot} = \underbrace{\left(\frac{\rho_{\odot}}{m_{\chi}}\right)}_{\text{local DM density}} \int du \frac{f(u)}{u} \int_0^{R_{\odot}} dr 4\pi r^2 w^2 \sum_T \Theta(w^2 - v_{T*}^2) \Omega_T$$

$T$  = Target Nucleus in Sun

with  $\Omega_T = \eta_T(r) \Theta(E_{\max} - E_{\text{cap}}) \int_{\max[E_{\min}, E_{\text{cap}}]}^{E_{\max}} dE \frac{d\sigma_T}{dE}$  scattering cross-section

$$w(u, r) = \sqrt{u^2 + v_{\text{esc}}(r)^2} = v_{\text{in}} \quad (\text{incoming WIMP speed inside Sun})$$

$u$  = WIMP speed in the Halo  
 $v_{\text{esc}}(r)$  = solar escape speed

$$E_{\min, \max}(w) = \frac{1}{2} m_{\chi} w^2 \left[ 1 - \frac{\mu_{\chi T}^2}{m_T^2} \left( 1 \pm \frac{m_T}{m_{\chi}} \sqrt{1 - \frac{v_{T*}^2}{w^2}} \right)^2 \right] - \delta$$

$$v_{T*} = \sqrt{\frac{2\delta}{\mu_{\chi T}}}$$

$$E \geq E_{\text{cap}}(u) = \frac{1}{2} m_{\chi} u^2 - \delta. \quad \text{minimum energy to be deposited by the WIMP so that } \mathbf{v}_{\text{out}} < \mathbf{v}_{\text{esc}}(\mathbf{r}) \text{ and the WIMP is captured}$$

# IDM: Capture in the Sun

$$w(u, r) = \sqrt{u^2 + v_{\text{esc}}(r)^2} = \mathbf{v}_{\text{in}} \quad (\text{incoming WIMP speed inside Sun})$$

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 $v_{\text{esc}}(r)$  = solar escape speed

$$E_{\text{min,max}}(w) = \frac{1}{2} m_{\chi} w^2 \left[ 1 - \frac{\mu_{\chi T}^2}{m_T^2} \left( 1 \pm \frac{m_T}{m_{\chi}} \sqrt{1 - \frac{v_{T*}^2}{w^2}} \right)^2 \right] - \delta$$

$$v_{T*} = \sqrt{\frac{2\delta}{\mu_{\chi T}}}$$

$$E \geq E_{\text{cap}}(u) = \frac{1}{2} m_{\chi} u^2 - \delta$$

minimum energy to be deposited by the WIMP  
 so that  $\mathbf{v}_{\text{out}} < \mathbf{v}_{\text{esc}}(r)$  and the WIMP is captured

## • Kinematic conditions:

### 1) [Condition for IDM scattering]

$$\text{Incoming WIMP speed } w(u, r) = \sqrt{u^2 + v_{\text{esc}}(r)^2} \geq \mathbf{v}_{T*} = \sqrt{\frac{2\delta}{\mu_{\chi T}}}$$

$$\Rightarrow u^2 + v_{\text{esc}}(r)^2 \geq \frac{2\delta}{\mu_{\chi T}}$$

$v_{\text{esc}}(r) = [620, 1400]$  km/s  
 (from solar surface to center)

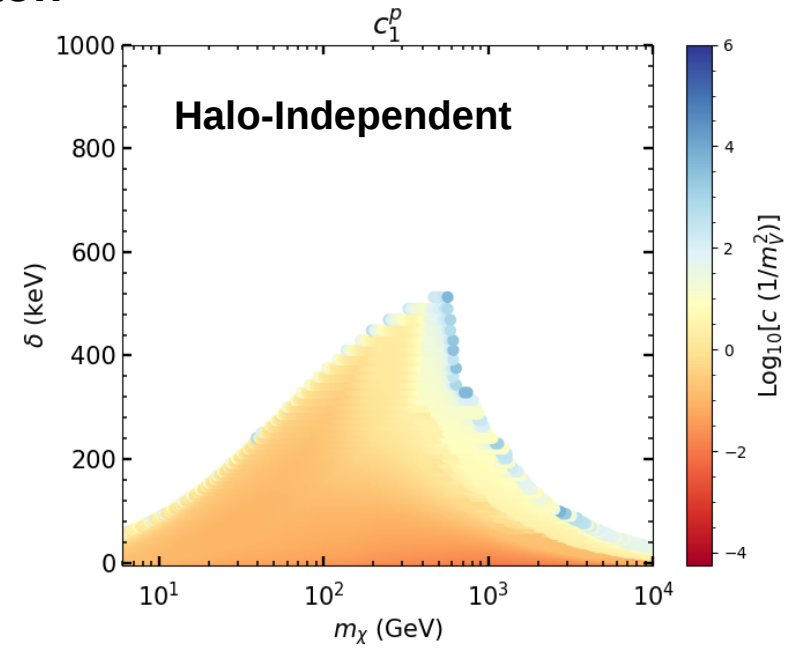
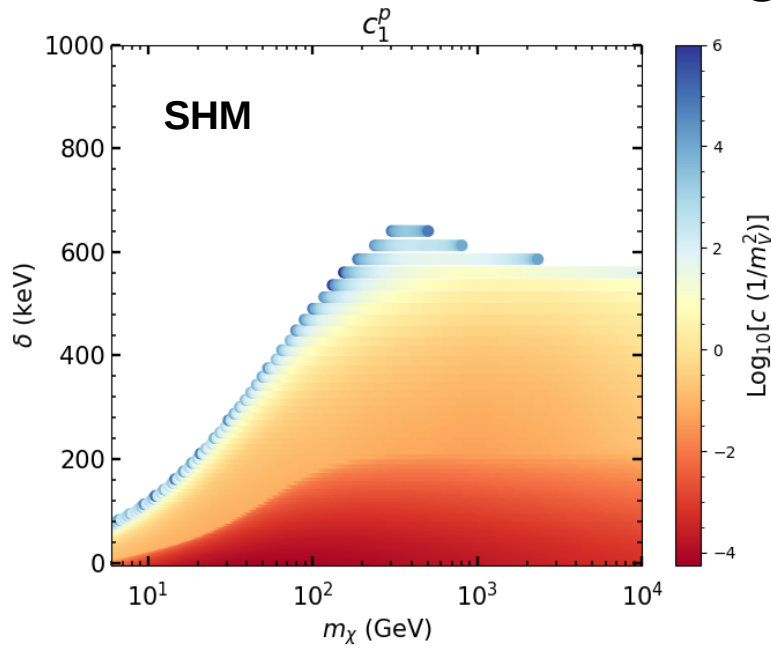
**→ If  $\frac{2\delta}{\mu_{\chi T}} \geq v_{\text{esc}}(r)^2$  IDM scattering for  $u \rightarrow 0$  is Not possible, needs a larger  $u$**

$$2) E_{\text{max}} \geq E_{\text{cap}}$$

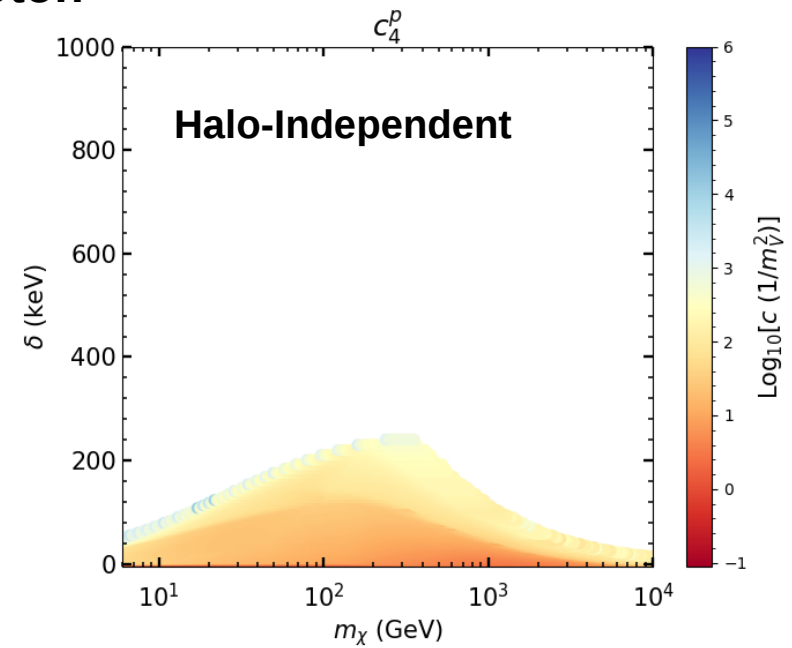
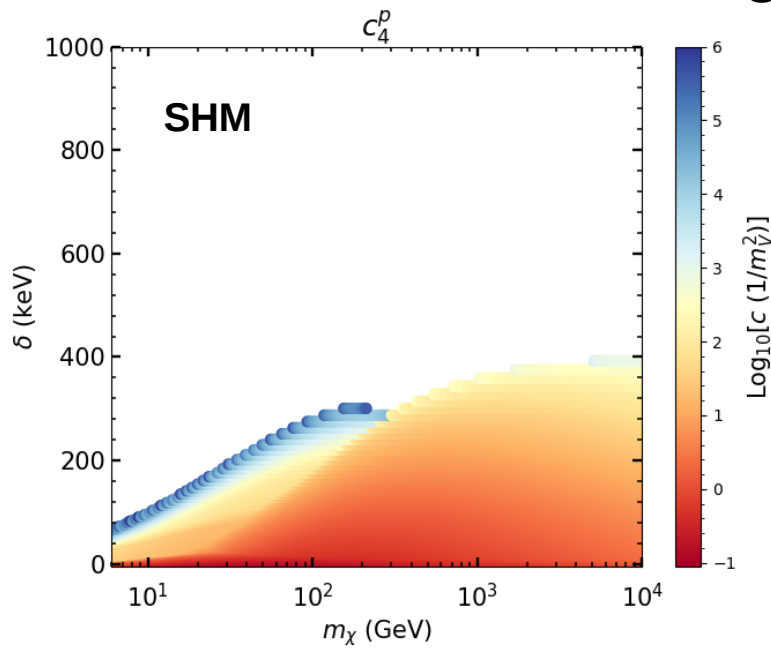
$$\Rightarrow u \leq \mathbf{u}^{\text{C-max}}(r, m_{\chi}, m_T, \delta)$$

If the WIMP speed  $u$  crosses the maximum limit  $\mathbf{u}^{\text{C-max}}$ , it is Not captured by the Sun

## SI-proton



## SD-proton



## IDM: issue of thermalization

$$\Gamma_{\odot} = \frac{C_{\odot}}{2} \tanh^2(t_{\odot}/\tau_{\odot}) = \frac{C_{\odot}}{2} \tanh^2(t_{\odot} \sqrt{C_{\odot} C_A})$$

$$\tau_{\odot} = (C_{\odot} C_A)^{-\frac{1}{2}} \quad \text{equilibration time for Capture \& Annihilation}$$

$C_{\odot}$  : WIMP Capture rate in the Sun

Annihilation coefficient : 
$$C_A = \frac{\langle \sigma v \rangle 4\pi \int_0^{R_{\odot}} r^2 n_{\chi}^2(r) dr}{\left[ 4\pi \int_0^{R_{\odot}} r^2 n_{\chi}(r) dr \right]^2}$$

$$\langle \sigma v \rangle = 3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$$

$$n_{\chi}(r) = n_0 e^{-m_{\chi} \phi(r)/T_c} \simeq n_0 e^{-r^2/r_{\chi}^2}$$

$$\phi(r) = \int_0^r \frac{GM(r)}{r^2} dr$$

$$r_{\chi}^2 = \frac{3k_B T_c}{2\pi G \rho_c m_{\chi}}$$

$$T_c \simeq 1.55 \times 10^7 \text{ }^{\circ}\text{K}$$

$$C_A = \langle \sigma v \rangle \frac{V_2}{V_1^2}$$

$$V_n = 4\pi \int_0^{r_{\odot}} r^2 e^{-nr^2/r_{\chi}^2} dr$$

$$C_A^{\min} = \frac{\langle \sigma v \rangle}{V_{\odot}} \quad \Longrightarrow \quad \Gamma_{\odot}^{\min}$$

(for  $n_{\chi}(r) = n_0$ )