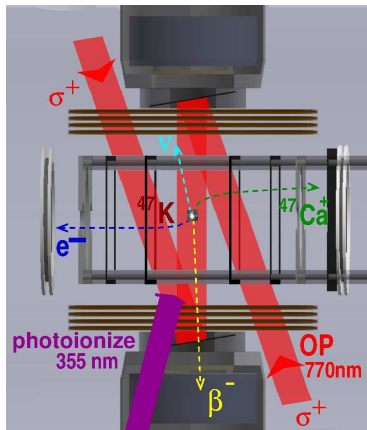




Analog-Antianalog isospin mixing in ^{47}K β^- decay + time-reversal symmetry



- Spin-polarize by direct optical pumping
- Measure asymmetry of decay products wrt initial nuclear spin

- Isobaric analog states and isospin-suppressed β decay
- In ^{47}K isospin-suppressed decay, we measure:
a large Fermi contribution and Coulomb matrix element
a large fraction of predicted analog-antianalog mixing
- Sensitivity to time-reversal breaking \mathcal{T} enhanced in isospin-forbidden β decay ^{47}K



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Supported by NSERC, NRC through TRIUMF, DOE, RBC Foundation

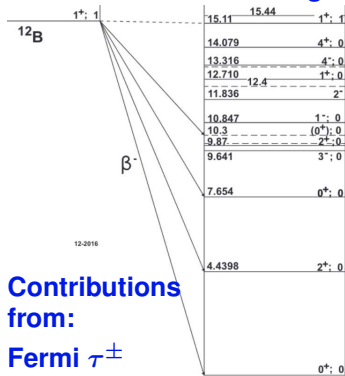
*co-spokesperson

^{47}K β^- decay and Analog- “Anti-analog” isospin mixing

n, tritium β^- decay to their **isobaric mirrors**



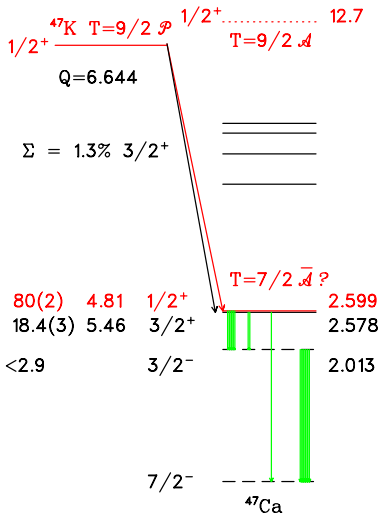
^{12}B β^- decays to ^{12}C
 $E_x=15.11$ **isobaric analog**



Contributions from:

Fermi τ^\pm

Gamow-Teller $\sigma \cdot \tau$



data from J.K. Smith PRC 102 054314 (2020)

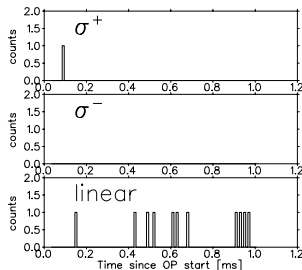
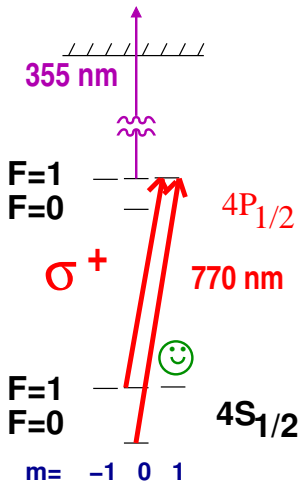
^{47}K decay to its isobaric analog is energetically forbidden, so is purely G-T, unless isospin mixing of analog and “antianalog” configurations lets Fermi contribute \rightarrow nonzero ^{47}Ca asymmetry wrt ^{47}K nuclear spin

Barroso and Blin-Stoyle PL45B 178 (1973):

sensitivity of \mathcal{T} correlations to \mathcal{T} P even N-N isovector interactions is enhanced by $\sim 10^2$, because \mathcal{T} is referenced to Coulomb (not strong) interactions

Optical pumping of $I=1/2$ ^{47}K

We measure by atomic techniques the polarization of the β -decaying nuclei



(tight cuts on timing
wrt pulse laser and
center position exclude
background:
H. Gallop. U. Waterloo)

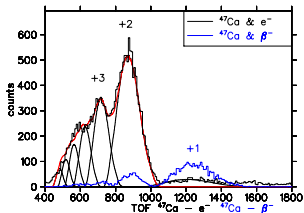
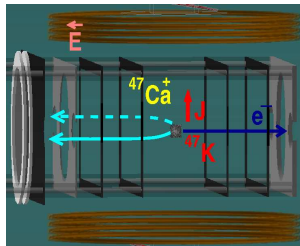
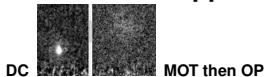
We alternate trap/optical pumping
Apply circularly polarized light along z
quantization axis.

Once we start OP cycle, atoms increase
spin to maximum, then stop absorbing
If light is linearly polarized, atoms keep
absorbing.

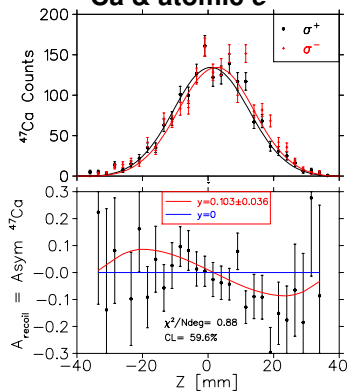
When excited, a pulsed laser has enough
energy/photon to photoionize (a small
fraction) of them.

11 photoions while linearly polarized,
1 photon circularly polarized \rightarrow
nuclear polarization $96 \pm 4\%$

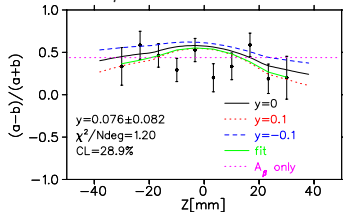
1000 atoms trapped



⁴⁷Ca & atomic e⁻



β^- & ^{47}Ca



Source	A_{recoil}	pseudo A_{β}
A_{recoil} bkg $6 \pm 4\%$	0.014	< 0.002
Polarization 0.96 ± 0.04	0.004	0.023
β^- Branching ratio	0.002	0.022
Weak magnetism	0.0006	0.0003
Fit range in $Z \pm 20$ to 34 mm	0.012	NA
$^{47}\text{Ca}^{+1}$ percent bkg	0.001	NA
$^{47}\text{Ca}^{+N}$ distribution from TOF	< 0.0005	NA
E field	negligible	0.025
Backscatter correction $-0.012 \pm 20\%$	NA	0.0024
Fit statistics	0.037	0.082
Total	0.041	0.091

• Nonzero ^{47}Ca asymmetry wrt spin \Rightarrow

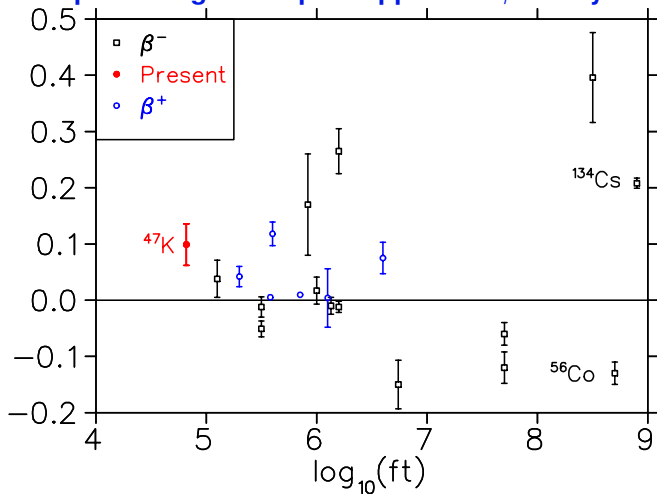
a nonzero M_{Fermi}

$$y = g_V M_F / g_A M_{GT} = 0.098 \pm 0.037$$

$$\langle \bar{A} | V_{\text{Coulomb}} | \mathcal{A} \rangle = 101 \pm 37 \text{ keV}$$



Isospin mixing in isospin-suppressed β decay:



- M_F can remain \sim to M_{GT} as M_{GT} falls two orders but is always smaller

Implications for planned \mathcal{T}

$y = g_V M_F / g_A M_{GT}$ large enough to be favorable for $D\mathcal{T}$ measurement

$$D \hat{\mathbf{J}} \cdot \frac{\vec{p}_\beta}{E_\beta} \times \frac{\vec{p}_\nu}{E_\beta} \xrightarrow{t \rightarrow -t} -D \hat{\mathbf{J}} \cdot \frac{\vec{p}_\beta}{E_\beta} \times \frac{\vec{p}_\nu}{E_\beta}$$

$$D = \sqrt{\frac{J}{J+1}} y / (1 + y^2) \sin(\alpha_V - \alpha_A)$$

In $\mathcal{A} - \bar{\mathcal{A}}$ systems Barroso and Blin-Stoyle

PL45B 178 (1973)

$$\sin \alpha_V = -i \frac{\langle \bar{\mathcal{A}} | V_{\mathcal{T}} | \mathcal{A} \rangle}{\langle \bar{\mathcal{A}} | V_{\text{Coul}} | \mathcal{A} \rangle} \Rightarrow$$

$$D \propto \delta E \frac{\langle \bar{\mathcal{A}} | V_{\mathcal{T}} | \mathcal{A} \rangle}{M_{GT}}$$

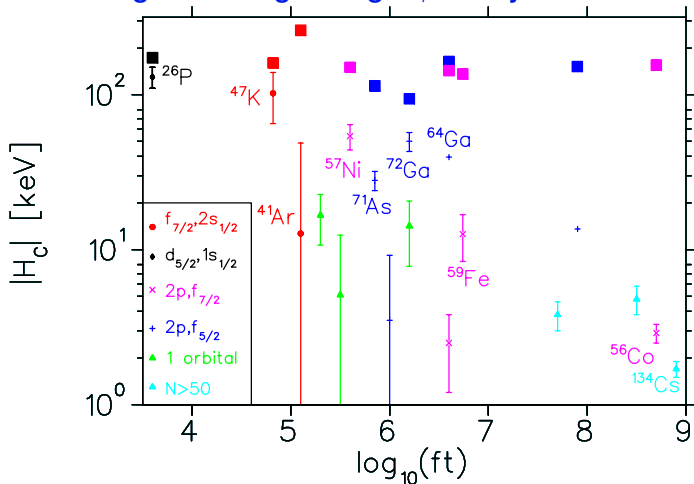
- To get same sensitivity to $\langle \bar{\mathcal{A}} | V_{\mathcal{T}} | \mathcal{A} \rangle$ we need D 30x better in ^{47}K compared to ^{56}Co

$E = -0.01 \pm 0.02$ Calaprice Freedman ... PRC 15 381 (1977) **no worries**

- However, nuclear matrix elements $\langle \bar{\mathcal{A}} | V_{\mathcal{T}} | \mathcal{A} \rangle$ might also fall with M_{GT} i.e. 'complexity' **so may favor ^{47}K**



Analog-antianalog mixing in β decay:



$^{47}\text{K} \beta^-$ decay has:

- Large $H_C = \langle \bar{\mathcal{A}} | V_{\text{Coul}} | \mathcal{A} \rangle = 101 \pm 37 \text{ keV}$
- Large fraction of $\mathcal{A} - \bar{\mathcal{A}}$ mixing prediction Auerbach Loc NPA 1027 122521 (2022)

$\Leftarrow {}^{47}_{20}\text{Ca}^{27}$ has only one $1/2^+$ state, $\bar{\mathcal{A}}$ configuration not fragmented

Schematic model for \mathcal{A} and $\bar{\mathcal{A}} \Rightarrow$

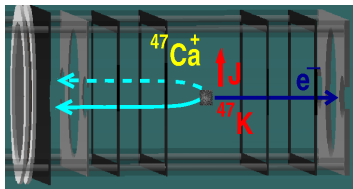
$$H_C = \langle \bar{\mathcal{A}} | V_C | \mathcal{A} \rangle$$

$$= \frac{\sqrt{n_1 n_2}}{2T} (\langle j_1 | V_C | j_1 \rangle - \langle j_2 | V_C | j_2 \rangle)$$

$$\rightarrow 0.35 \frac{\sqrt{n_1 n_2}}{2T} \frac{Z}{A^{2/3}} \text{ MeV, for HO wf's and excess n's occupy 2 major shells}$$

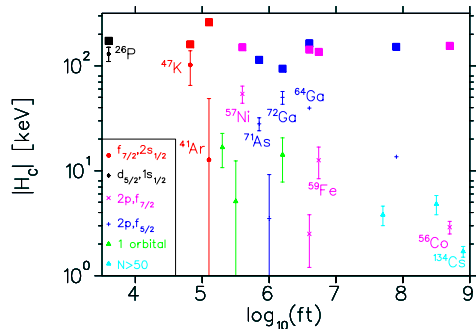
H_C for many β decays is a small fraction of the prediction: attributed to fragmentation of $\bar{\mathcal{A}}$ configuration among several eigenstates

Auerbach, Loc NPA 1027 122521 (2022)



Analog-Antianalog isospin mixing in ^{47}K β^- decay and \mathcal{T}
Measuring *isospin* in $^{47}\text{K}^{28}$ decay determines sensitivity to
parity-even *isospin* \mathcal{T} N-N interactions via future $D\vec{I} \cdot \vec{v}_\beta \times \vec{v}_\nu$

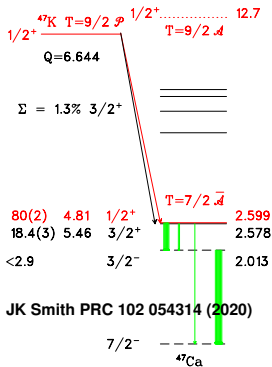
B. Kootte et al. Phys Rev C 109 L052501 2024



$I=1/2^+$ ^{47}K β^- decay has large:

- $H_C = \langle \bar{\mathcal{A}} | V_{\text{Coul}} | \mathcal{A} \rangle = 101 \pm 37 \text{ keV}$
- fraction of $\mathcal{A} - \bar{\mathcal{A}}$ mixing

prediction Auerbach, Loc NPA 1027 122521 (2022)



$^{47}_{20}\text{Ca}^{27}$'s single $1/2^+$ state contains most of the $\bar{\mathcal{A}}$ config

$y = g_V M_F / g_A M_{GT} = 0.098 \pm 0.037$
large enough to be favorable for
 D , enhanced by $\sim 10^2$ in
isospin-suppressed β decay

Barroso and Blin-Stoyle PL45B 178 (1973)

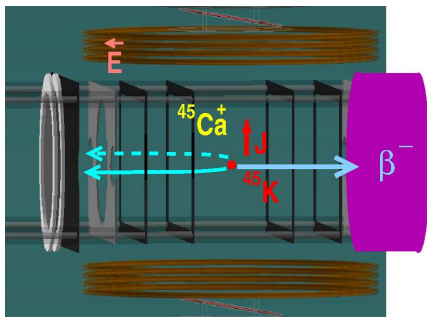
calculate reasonably large ^{134}Cs

\mathcal{T} matrix elements:

^{47}Ca 's $1/2^+$ simple structure

should make calculating \mathcal{T}
nuclear matrix elements of $\hat{r} \cdot \vec{p}$
practical

$D \vec{l} \cdot \vec{v}_\beta \times \vec{v}_\nu$ in atom trap: Features, Systematics



- Collect recoils going into 4 pi with electric field of 1 kV/cm
- Full reconstruction of recoil and beta momenta
- Point source: we know where it is (by sampling photoionization) and it doesn't move when we flip the polarization

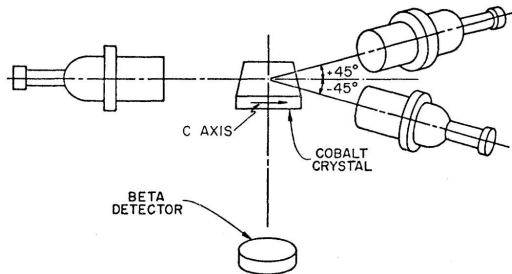
D Uncertainties / 100 scaling from Melconian PLB 649 270 (2007)

	B_ν	Improvements	Projected
Cloud position σ^\pm	1.3	$\pm 500 \mu\text{m} \rightarrow \pm 20 \mu\text{m}$	0.05
Cloud size/Temp	0.3	" "	0.03
MCP Position cal	1.0	DLA+ mask	≤ 0.1
\hat{x} -OP alignment	0.25	Geometry is \perp	≤ 0.02
E field	0.2		≤ 0.1

- Any stray polarization along wrong axis is deadly, a lowest-order fake D : Measure with singles asymmetry for recoils and β 's

^{56}Co \mathcal{T} experiment

Asymmetry of the 45° γ detectors with nuclear alignment



“Test of time-reversal invariance in the beta decay of ^{56}Co ”

Calaprice, Freedman, (Princeton);
Osgood, Thomlinson (BNL)

PRC 15 381 (1977)

$$E_1 = -0.01 \pm 0.02$$

$\log(ft) = 8.7$, yet known allowed:
 E_β spectrum, no β - γ correlation)

$$y = -0.13 \pm 0.02 \text{ PRC 26 287R (1982)}$$

Markey, Boehm (RIP Felix 2021)

$$V_{\text{Coul}} = 2.9 \text{ keV}, V_{\mathcal{T}} = 54 \pm 110 \text{ eV}$$

(J.L. Mortara Ph.D. thesis 1999 UCB

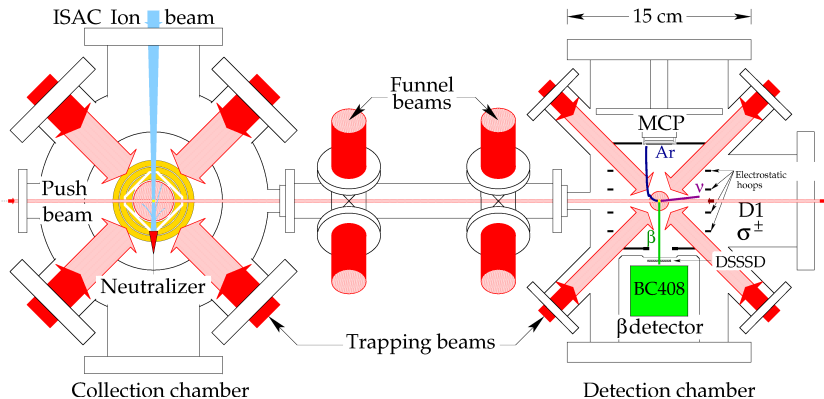
$$E_1 = -0.001 \pm 0.006$$

$$\Rightarrow V_{\mathcal{T}} = 5 \pm 33 \text{ eV}$$

We believe we can measure D in $^{47,45}\text{K}$
much more accurately than E in ^{56}Co ,
but we must find a case with $|M_{GT}|$,
 V_{Coul} , and \mathcal{T} N-N matrix elements to
allow complementary or better
sensitivity to $V_{\mathcal{T}}$

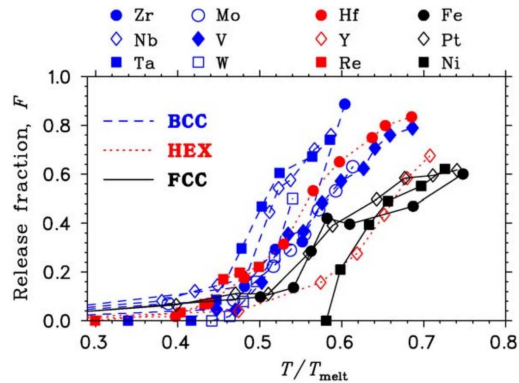
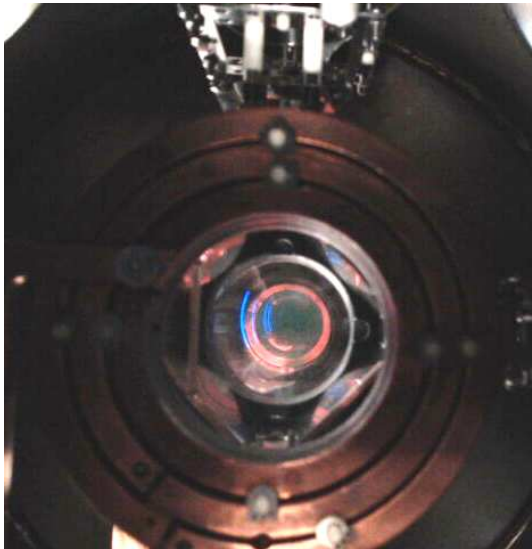
TRINAT plan view

- Isotope/Isomer selective
- Avoid untrapped atom background with 2nd trap
- 75% transfer
- 0.7 mm cloud for $\beta\text{-Ar}^+ \rightarrow \nu$ momentum

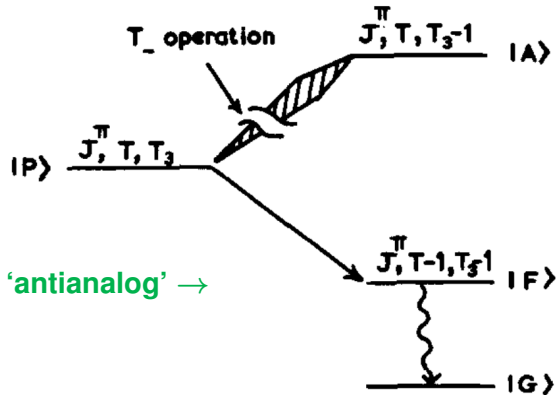


- Spin-polarized $99.1 \pm 0.1\%$

Neutralizer and Collection trap



\mathcal{T} in isospin-hindered β^- decay Barroso and Blin-Stoyle, PL 45B 178 (1973)



Any \mathcal{T} decay experiment should answer:

- Does interaction between outgoing particles mimic \mathcal{T} ? (We hope we can reach the $D < 10^{-3}$ level of such false \mathcal{T})
- Have null EDM's ruled you out? (Not if we reach $D < 10^{-2}$)

$$D \hat{\mathbf{J}} \cdot \frac{\vec{p}_\beta}{E_\beta} \times \frac{\vec{p}_\nu}{E_\beta} \xrightarrow{t \rightarrow -t} -D \hat{\mathbf{J}} \cdot \frac{\vec{p}_\beta}{E_\beta} \times \frac{\vec{p}_\nu}{E_\beta}$$

$$D = \sqrt{\frac{J}{J+1}} y / (1 + y^2) \sin(\alpha_V - \alpha_A)$$

$$\text{with } y = \frac{|M_F|}{|M_{GT}|}$$

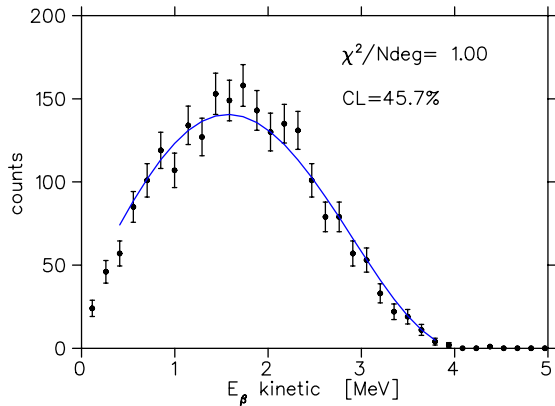
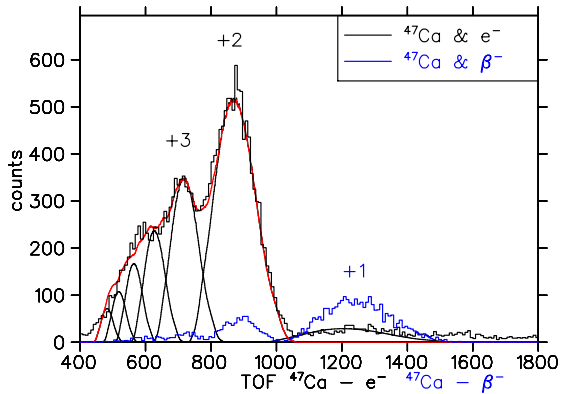
$$\text{In this system, } \sin \alpha_V = -i \frac{\langle F | V_{\mathcal{T}} | A \rangle}{\langle F | V_{\text{Coul}} | A \rangle}$$

So for \mathcal{T} physics mixing antianalog $|F\rangle$ with analog $|A\rangle$, then $V_{\mathcal{T}}$ is only competing with V_{Coul} , not V_{strong} ,

enhancing α_V by $\sim 10^2$ or 10^3 😊

- Has your experiment been done better? (Our goal is 3x better than Calaprice et al. ^{56}Co , and complementary to NOPTREX neutron scattering resonances for parity-even isospin-breaking interactions)

TOF and β spectra



⁴⁷K recoil order estimates still in progress

⁴⁷₁₉K²⁸ $\mu = 1.9 \mu_{\text{nucleon}} \Rightarrow$ thought to be 71% $2s_{1/2}$ Choudhary, Kumar, Srivasta, Suzuki PRC 103 064325 (2021)

Assuming $1/2^+ \rightarrow 1/2^+$ transition is $2s_{1/2} \rightarrow 2s_{1/2}$ (no orbital l contributions):

- Weak magnetism $b_W \sim$ the nucleon value
- 1st-class induced tensor $d_I \sim 0$

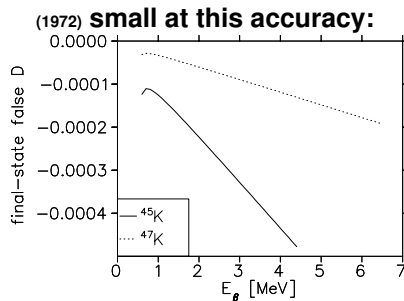
For our M_F/M_{GT} measurement,

$A_{\text{recoil}}, A_\beta$ changed by ≤ 0.01

Finite-size correction cancels most of this
in A_{recoil}

Recoil-order effects small at present level
of accuracy \rightarrow statistics-limited
measurement

Future D final-state effects Holstein PRC 5 1529



Note: ⁵⁶Co final-state $E_1=0.0002$ Calaprice 1977

• **P even N-N isovector/tensor \mathcal{T} :
complementary to \mathcal{T} neutron resonance
experiments**

Barroso and Blin-Stoyle

using Herczeg NP 75 655 (1966):

$$V_{t.v.} = G_{t.v.} \frac{1}{2} [f(r) \hat{r} \cdot \mathbf{p} + \text{h.c.}]$$

$$\times [1 + a \sigma^{(1)} \cdot \sigma^{(2)})(\tau_3^{(1)} + \tau_3^{(2)})$$

$$+ (b + c \sigma^{(1)} \cdot \sigma^{(2)}) \tau_3^{(1)} \tau_3^{(2)}]$$

NOPTREX: P -even \mathcal{T} neutron resonance experiments are ongoing (in addition to \mathcal{P} ones), with planned sensitivity to matrix elements \sim eV.

We hope to be complementary on isovector P -even \mathcal{T} by reaching similar sensitivity.

**Samart Schat Schindler Phillips PRC
2016: Isoscalar and isotensor P even \mathcal{T}
 π -N suppressed by $1/N_C$; isovector a_1
contributes, not ρ and h_1**

**D produced by most \mathcal{T} interactions
would make a large neutron EDM $\Rightarrow D$
less than 10^{-4} (Ng and Tulin PRD 85
033001 (2012).**

**Isotensor \mathcal{T} interaction would make D
but not $T=1/2$ neutron EDM, but tricky
microscopically without making
isovector \mathcal{T} .**

**Barroso and Blin-Stoyle $10^2 \mathcal{A} - \bar{\mathcal{A}}$
enhancement \Rightarrow our goal of $D < 10^{-3}$
in ^{47}K evades Ng-Tulin bound.**

H_{Coul} from isospin-forbidden β -decay

- [17] L. G. Mann, D. C. Camp, J. A. Miskel, and R. J. Nagle, New measurements of β -circularly-polarized γ angular-correlation asymmetry parameters in allowed β decay, *Phys. Rev.* **139**, AB2 (1965).
- [18] J. Atkinson, L. Mann, K. Tirsell, and S. Bloom, Coulomb matrix elements from β - γ (cp) correlation measurements in ^{57}Ni and ^{65}Ni , *Nuclear Physics A* **114**, 143 (1968).
- [19] H. Behrens, Messung des asymmetrie-koeffizienten der $\beta - \gamma$ -zirkularpolarisationskorrelation an erlaubten β -übergängen, *Z. Physik* **201**, 153 (1967).
- [20] J. Markey and F. Boehm, Fermi—gamow-teller interference in ^{56}Co decay, *Phys. Rev. C* **26**, 287 (1982).
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- [22] N. Severijns, D. Vénos, P. Schuurmans, T. Phalet, M. Honusek, D. Srnka, B. Vereecke, S. Versyck, D. Zákoucký, U. Köster, M. Beck, B. Delauré, V. Golovko, and I. Kraev, Isospin mixing in the $t = 5/2$ ground state of ^{71}As , *Phys. Rev. C* **71**, 064310 (2005).
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- [24] J. J. Liu, X. X. Xu, L. J. Sun, C. X. Yuan, K. Kaneko, Y. Sun, P. F. Liang, H. Y. Wu, G. Z. Shi, C. J. Lin, J. Lee, S. M. Wang, C. Qi, J. G. Li, H. H. Li, L. Xayavong, Z. H. Li, P. J. Li, Y. Y. Yang, H. Jian, Y. F. Gao, R. Fan, S. X. Zha, F. C. Dai, H. F. Zhu, J. H. Li, Z. F. Chang, S. L. Qin, Z. Z. Zhang, B. S. Cai, R. F. Chen, J. S. Wang, D. X. Wang, K. Wang, F. F. Duan, Y. H. Lam, P. Ma, Z. H. Gao, Q. Hu, Z. Bai, J. B. Ma, J. G. Wang, C. G. Wu, D. W. Luo, Y. Jiang, Y. Liu, D. S. Hou, R. Li, N. R. Ma, W. H. Ma, G. M. Yu, D. Patel, S. Y. Jin, Y. F. Wang, Y. C. Yu, L. Y. Hu, X. Wang, H. L. Zang, K. L. Wang, B. Ding, Q. Q. Zhao, L. Yang, P. W. Wen, F. Yang, H. M. Jia, G. L. Zhang, M. Pan, X. Y. Wang, H. H. Sun, H. S. Xu, X. H. Zhou, Y. H. Zhang, Z. G. Hu, M. Wang, M. L. Liu, H. J. Ong, and W. Q. Yang (RIBLL Collaboration), Observation of a strongly isospin-mixed doublet in ^{26}Si via β -delayed two-proton decay of ^{26}P , *Phys. Rev. Lett.* **129**, 242502 (2022).
- [25] S. D. Bloom, Isotopic-spin conservation in allowed β -transitions and coulomb matrix elements, *Il Nuovo Cimento* **32**, 1023 (1964).

The analog is:

$$|A\rangle = \frac{1}{\sqrt{2T}} \left[\sqrt{n_1} |j_1^{n_1-1}(n) j_1(p) j_2^{n_2}(n)\rangle \right. \\ \left. + \sqrt{n_2} |j_1^{n_1}(n) j_2^{n_2-1}(n) j_2(p)\rangle \right]$$

The anti-analog $|\bar{A}\rangle$ is then:

$$|\bar{A}\rangle = \frac{1}{\sqrt{2T}} \left[\sqrt{n_2} |j_1^{n_1-1}(n) j_1(p) j_2^{n_2}(n)\rangle \right. \\ \left. - \sqrt{n_1} |j_1^{n_1}(n) j_2^{n_2-1}(n) j_2(p)\rangle \right].$$

Schematic model for \mathcal{A} and $\bar{\mathcal{A}} \Rightarrow$

$$H_C = \langle \bar{\mathcal{A}} | V_C | \mathcal{A} \rangle \\ = \frac{\sqrt{n_1 n_2}}{2T} (\langle j_1 | V_C | j_1 \rangle - \langle j_2 | V_C | j_2 \rangle) \\ \rightarrow 0.35 \frac{\sqrt{n_1 n_2}}{2T} \frac{Z}{A^{2/3}} \text{MeV},$$

for HO wf's and excess n's occupy 2 major shells

H_C for many β decays is a small fraction of the prediction: attributed to fragmentation of $\bar{\mathcal{A}}$ configuration among several eigenstates

Auerbach, Loc NPA 1027 122521 (2022)