

# Fission processes in heavy and superheavy elements within the dinuclear system model

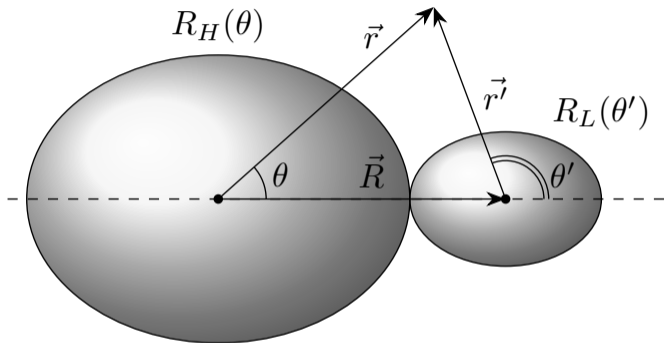
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INPC 2025

Daejeon

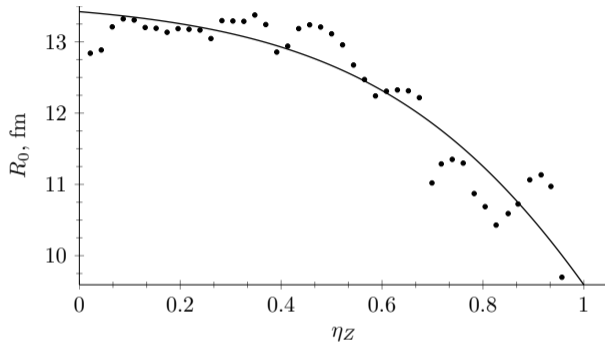
# Dinuclear system (DNS)



Charge asymmetry:

$$\eta_Z = \frac{Z_H - Z_L}{Z_H + Z_L}, \quad Z_{H,L} - \text{charge number}$$

# Dinuclear system (DNS)



## DNS preformation

- Movement in  $\eta Z$  coordinate
- Spectroscopic factor (preformation probability)  $S_L$

## DNS decay

- Movement in  $R$  coordinate
- Penetration probability  $P_L$

The system is described by stationary wave function  $\Psi(\eta_Z)$ :

$$\hat{H}\Psi_n(\eta_Z) = E_n\Psi_n(\eta_Z),$$

где

$$\hat{H} = \hat{T}_{\eta_Z} + U(\eta_Z)$$

Kinetic energy

$$\hat{T}_{\eta_Z} = \frac{\hbar^2}{2} \frac{\partial}{\partial \eta_Z} B_{\eta_Z}^{-1} \frac{\partial}{\partial \eta_Z}$$

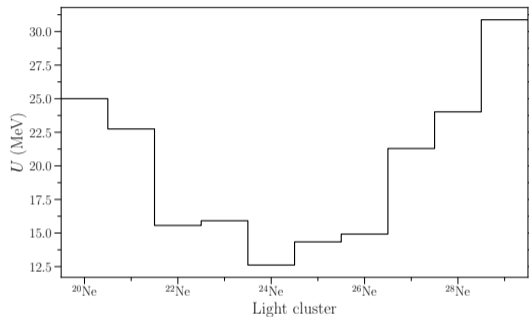
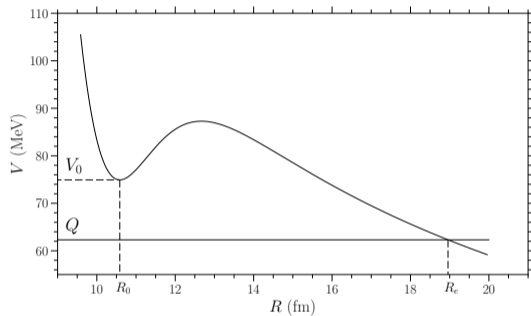
Potential energy

[G. Adamian *et al.* Int. J. Mod. Phys. A, 1996]

$$U(R, \eta_Z) = V(R, \eta_Z) - (Q_M - Q_L - Q_H)$$

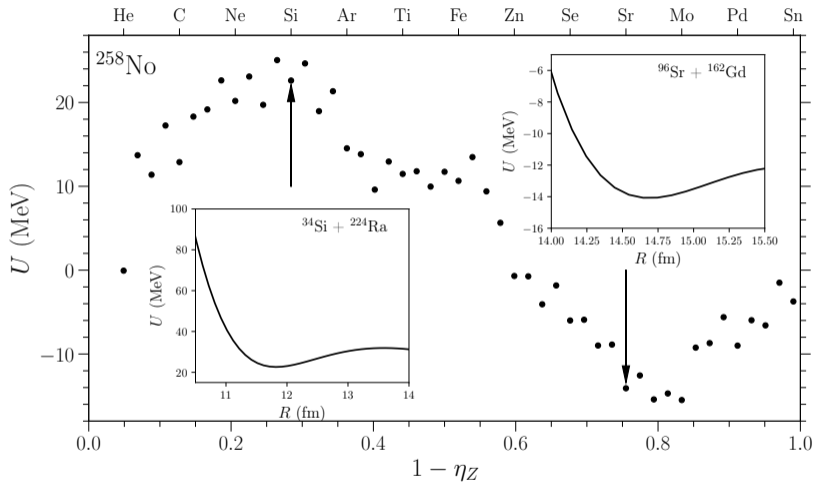
$$V(R, \eta_Z) = V_C(R, \eta_Z) + V_N(R, \eta_Z) + V_r(R, \eta_Z)$$

# Driving potential

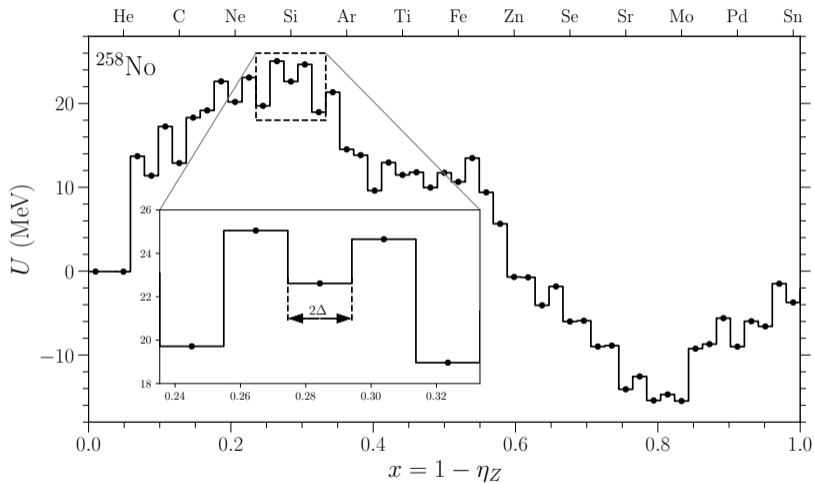


$$a_0 = 0.47 - 0.56 \text{ fm}; \quad r_0 = 1.00 - 1.16 \text{ fm}$$

# Formation of the driving potential

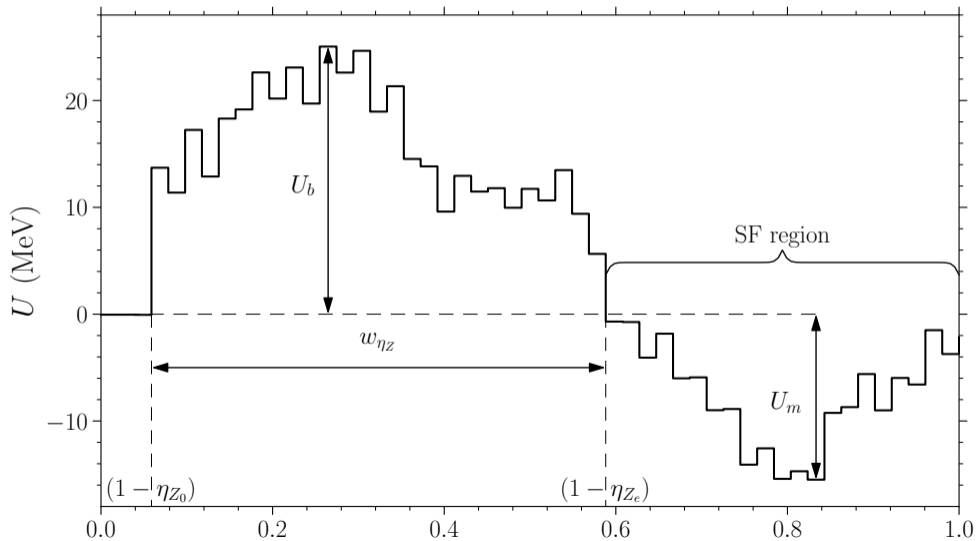


# Formation of the driving potential



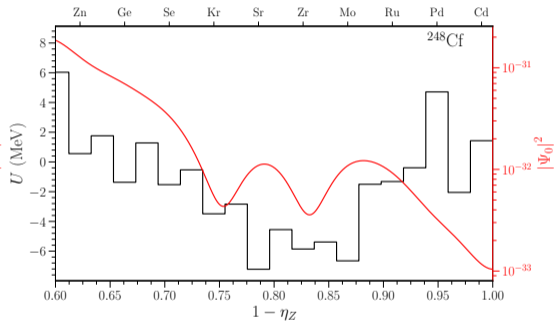
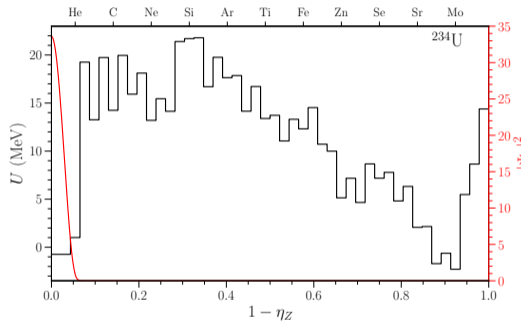
$$\eta_Z \rightarrow x = 1 - \eta_Z; \quad \Delta = 1/Z;$$

# Driving potential characteristics





# Wave function



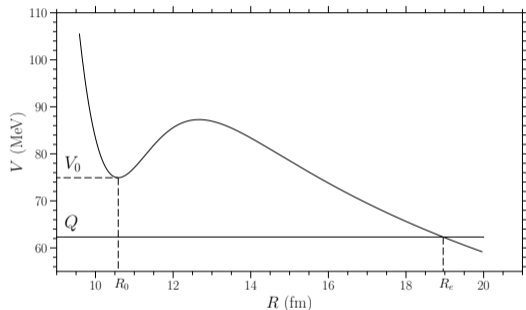
$$S_L = \int_{\eta_Z(Z_l) - \Delta}^{\eta_Z(Z_L) + \Delta} |\Psi(\eta_Z)|^2 d\eta_Z$$

$$\Delta = 1/Z$$

$$\Gamma_L = \frac{\hbar\omega_0}{\pi} S_L P_L, \quad T_{1/2} = \frac{\hbar \ln 2}{\Gamma_L}$$

$$T_{1/2} = \frac{\pi \ln 2}{\omega_0 S_L P_L}$$

$$P_L = \left( 1 + \exp \left[ \frac{2}{\hbar} \int_{R_0}^{R_{Jl}} \sqrt{2\mu(V(R, \eta_Z) - Q)} dR \right] \right)^{-1}$$



## Spectroscopic factor for SF

The SF decay width is

$$\Gamma_{SF} = \sum_L \Gamma_L = \frac{\hbar\omega_0}{\pi} \sum_L S_L P_L$$

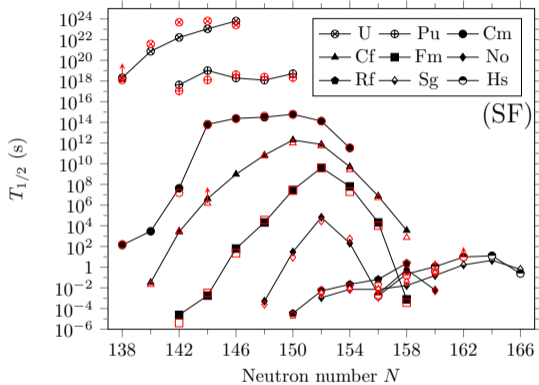
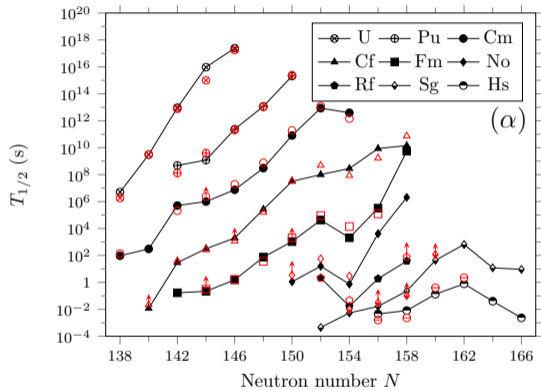
For SF region  $P_L = 1$ , so:

$$\Gamma_{SF} = \frac{\hbar\omega_0}{\pi} \sum_L S_L = \frac{\hbar\omega_0}{\pi} S_{SF},$$

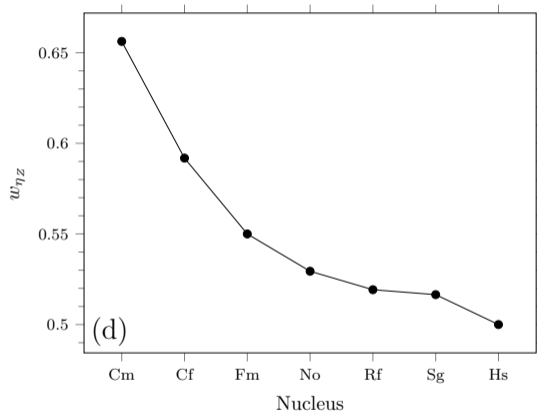
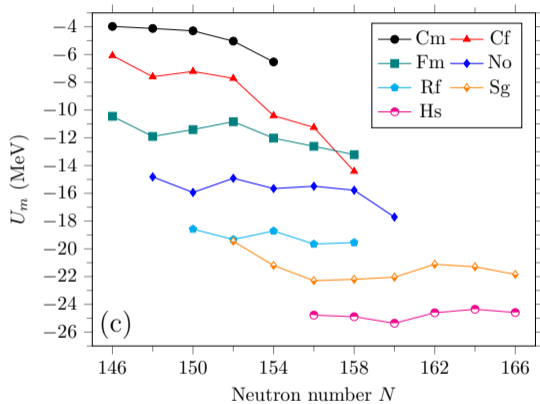
and the spectroscopic factor  $S_{SF}$  for SF:

$$S_{SF} = \sum_L S_L,$$

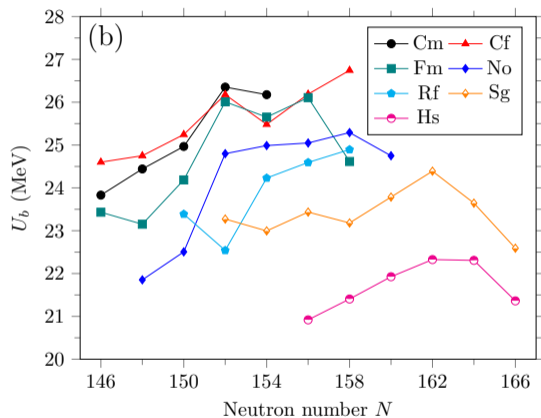
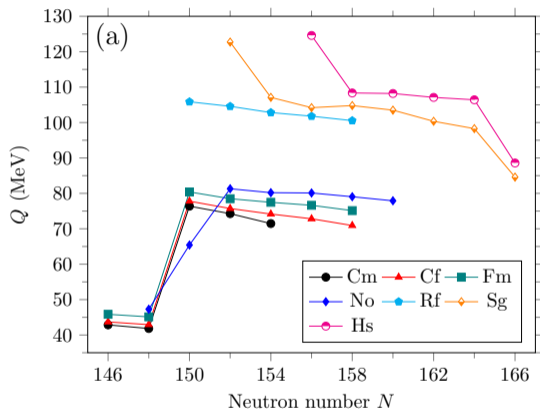
# Even-even nuclei half-lives



# Driving potential characteristics

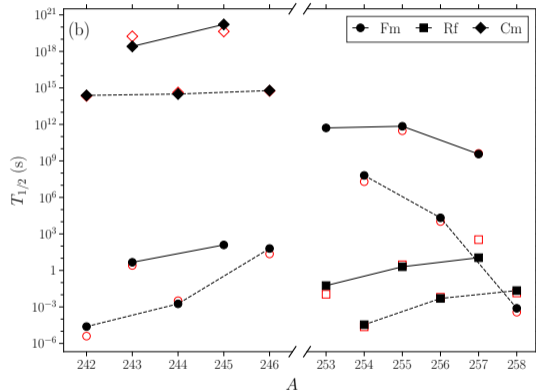
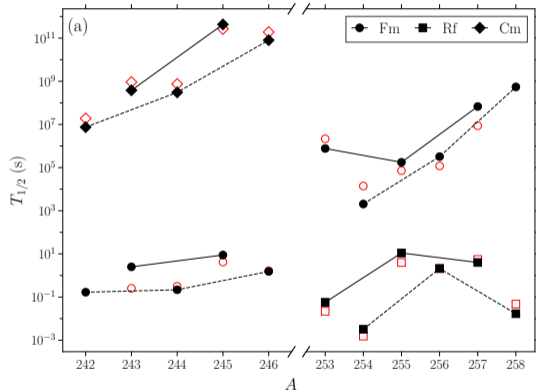


# Driving potential characteristics

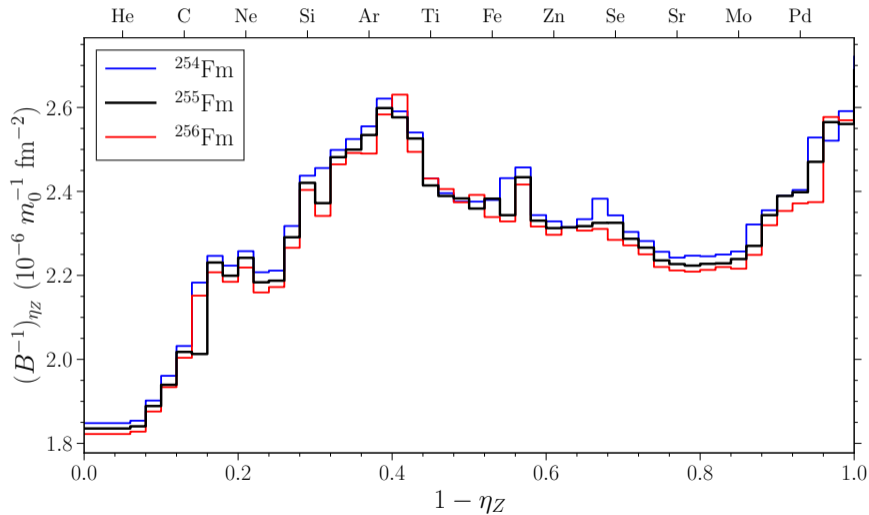


$$Q = (Q_M - Q_L - Q_H), \text{ for } \eta_Z \text{ at } U_b$$

# Even-odd nuclei half-lives

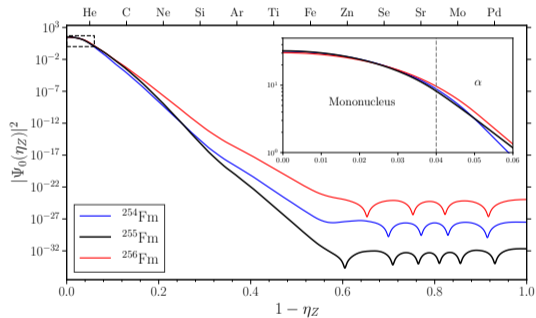
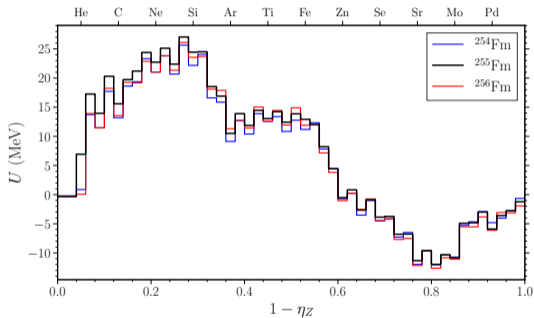


# HF origins. Inertia parameter influence





# Driving potential influence



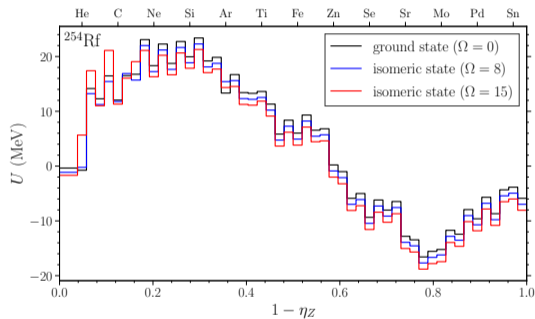
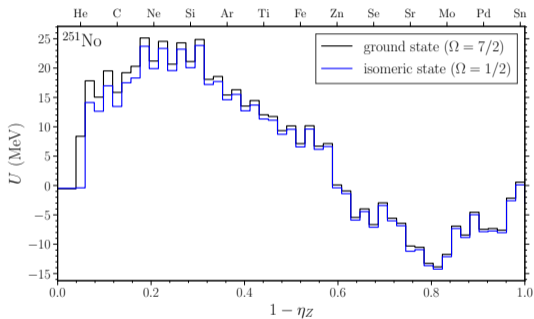
# Rotational part influence

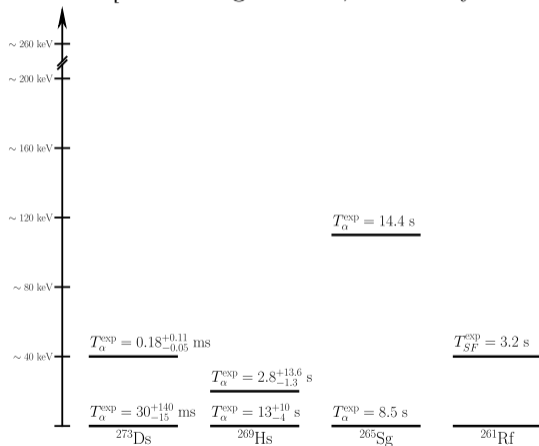
	$\Omega$	$S_\alpha$	$S_\alpha^{\Omega=0}$	$T_{1/2}, \text{ s}$	$T_{1/2}^{\Omega=0}, \text{ s}$	$T_{1/2}^{\text{est}}, \text{ s}$
$^{243}\text{Cm}$	5/2	0.0526	0.0707	$2.57 \times 10^{18}$	$1.02 \times 10^{14}$	$2.75 \times 10^{14}$
$^{245}\text{Cm}$	7/2	0.0428	0.0947	$1.65 \times 10^{20}$	$7.34 \times 10^{14}$	$4.35 \times 10^{14}$
$^{243}\text{Fm}$	7/2	0.0712	0.0904	3.51	$3.14 \times 10^{-4}$	$2.08 \times 10^{-4}$
$^{255}\text{Fm}$	7/2	0.0527	0.0816	$3.01 \times 10^{11}$	$1.62 \times 10^6$	$1.16 \times 10^6$
$^{257}\text{Fm}$	9/2	0.0481	0.0888	$4.13 \times 10^9$	1.19	4.02
$^{255}\text{Rf}$	9/2	0.0691	0.0930	2.00	$2.95 \times 10^{-3}$	$4.14 \times 10^{-4}$
$^{257}\text{Rf}$	1/2	0.0893	0.0918	$1.11 \times 10^1$	$3.99 \times 10^{-2}$	$1.05 \times 10^{-2}$

$$T_{1/2} = F \cdot T_{1/2}(\Omega = 0), F = \exp \left[ \frac{c \cdot \Omega(\Omega + 1)}{\sqrt{(B^{-1})_{\eta Z \alpha}}} \right], c = 0.086 \text{ MeV}^{-1/2} \text{ s}^{-1}$$

Nucleus	$\Omega$	$T_{1/2}(\Omega = 0)$ (s)	$F$	$T_{1/2}^{\text{fit}}$ (s)	$T_{1/2}^{\text{exp}}$ (s)
$^{243}\text{Cm}$	5/2	$1.02 \times 10^{14}$	$3.47 \times 10^3$	$3.54 \times 10^{17}$	$2.57 \times 10^{18}$
$^{243}\text{Fm}$	7/2	$3.14 \times 10^{-4}$	$1.20 \times 10^4$	3.77	4.64
$^{245}\text{Cm}$	7/2	$7.34 \times 10^{14}$	$2.63 \times 10^6$	$1.93 \times 10^{21}$	$1.65 \times 10^{20}$
$^{255}\text{Fm}$	7/2	$1.62 \times 10^6$	$7.72 \times 10^5$	$1.25 \times 10^{12}$	$7.04 \times 10^{11}$
$^{255}\text{Rf}$	9/2	$2.95 \times 10^{-3}$	$3.17 \times 10^4$	$9.38 \times 10^1$	2.00
$^{257}\text{Fm}$	9/2	1.19	$3.33 \times 10^8$	$3.96 \times 10^8$	$3.64 \times 10^9$
$^{257}\text{Rf}$	1/2	$2.02 \times 10^{-2}$	1.59	$3.21 \times 10^{-2}$	$1.15 \times 10^1$

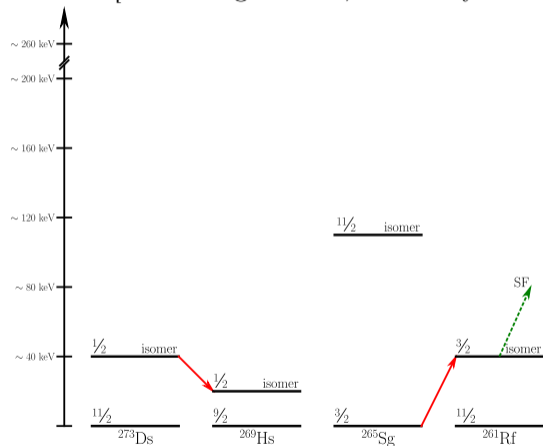
# Isomers decay



[Yu. Ts. Oganessian, V. K. Utyonkov *et al.* Phys. Rev C 109, 054307 (2024)]

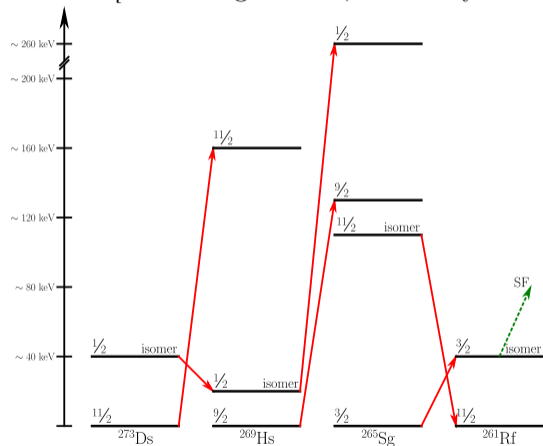
# Decay chains $^{273,275}\text{Ds}$

[Yu. Ts. Oganessian, V. K. Utyonkov *et al.* Phys. Rev C 109, 054307 (2024)]



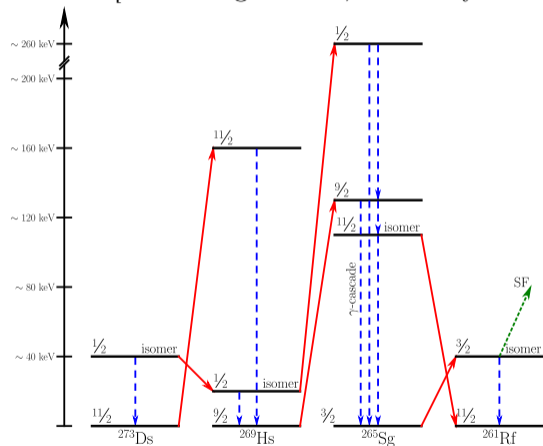
# Decay chains $^{273,275}\text{Ds}$

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# Decay chains $^{273,275}\text{Ds}$

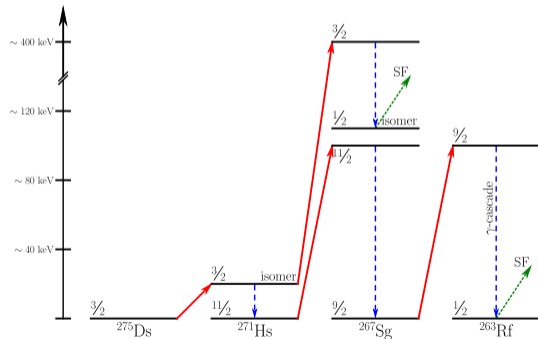
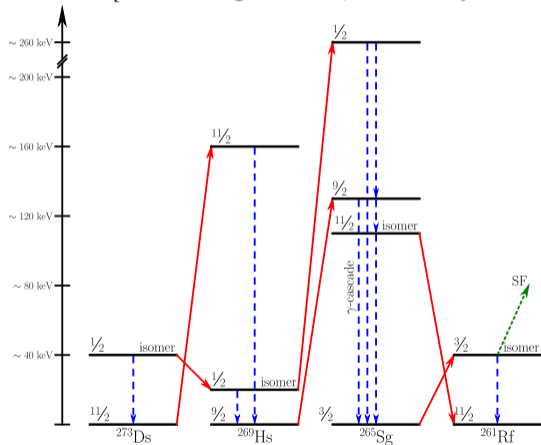
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Thank you for your attention