

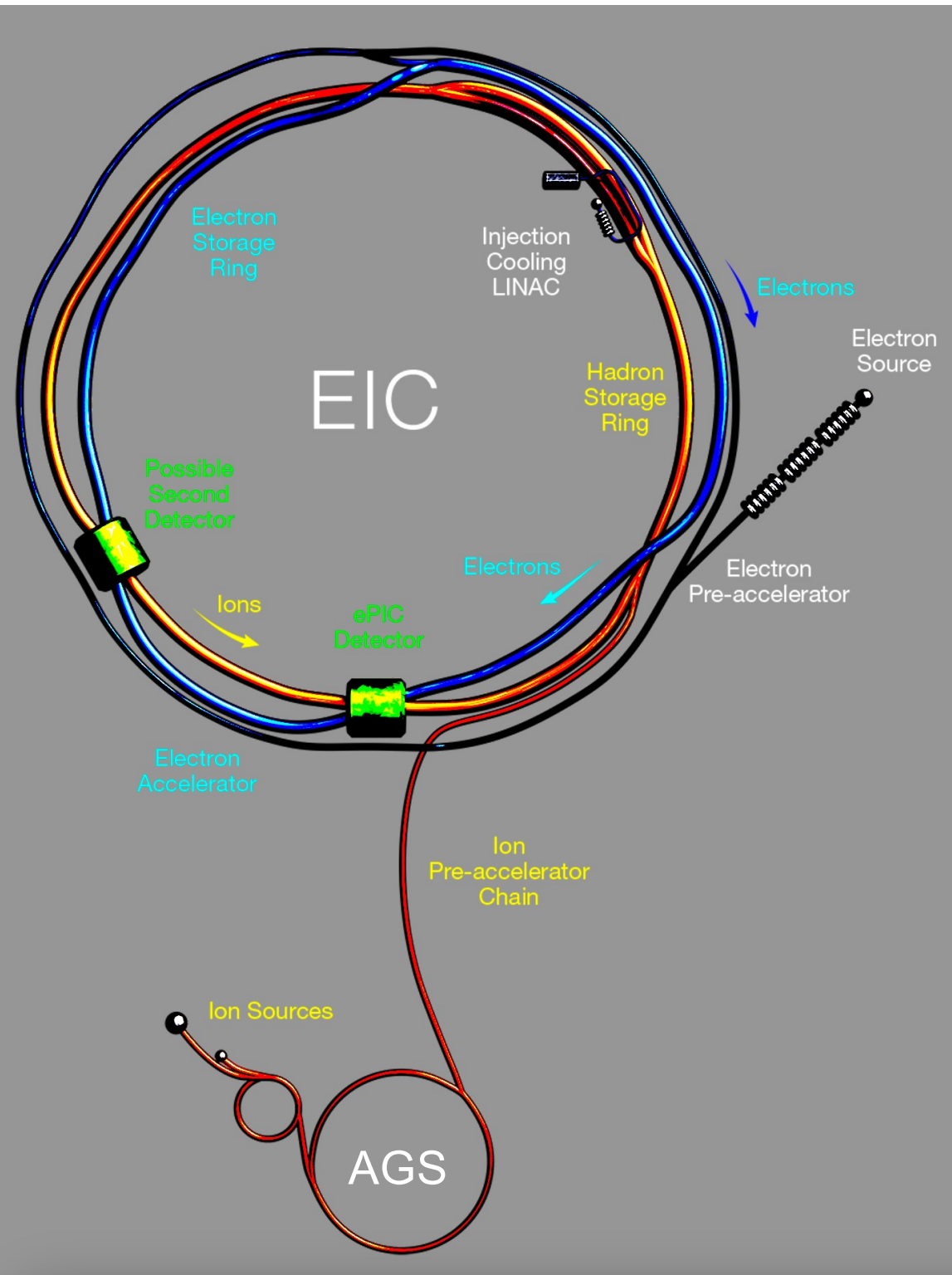
Nuclear Fragmentation at the Future Electron-Ion Collider

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EAST TEXAS A&M
— UNIVERSITY —

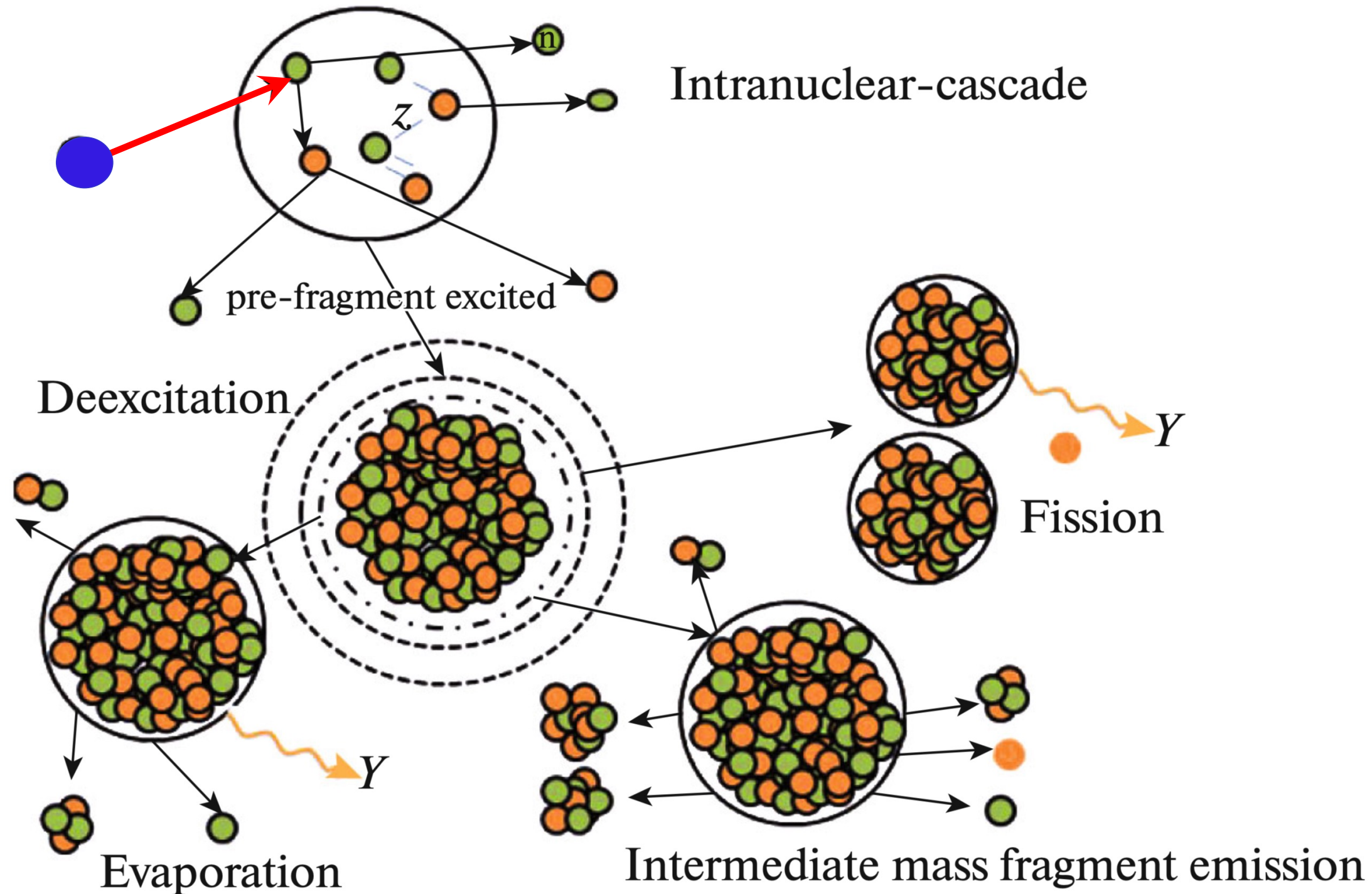
Electron Ion Collider (EIC)



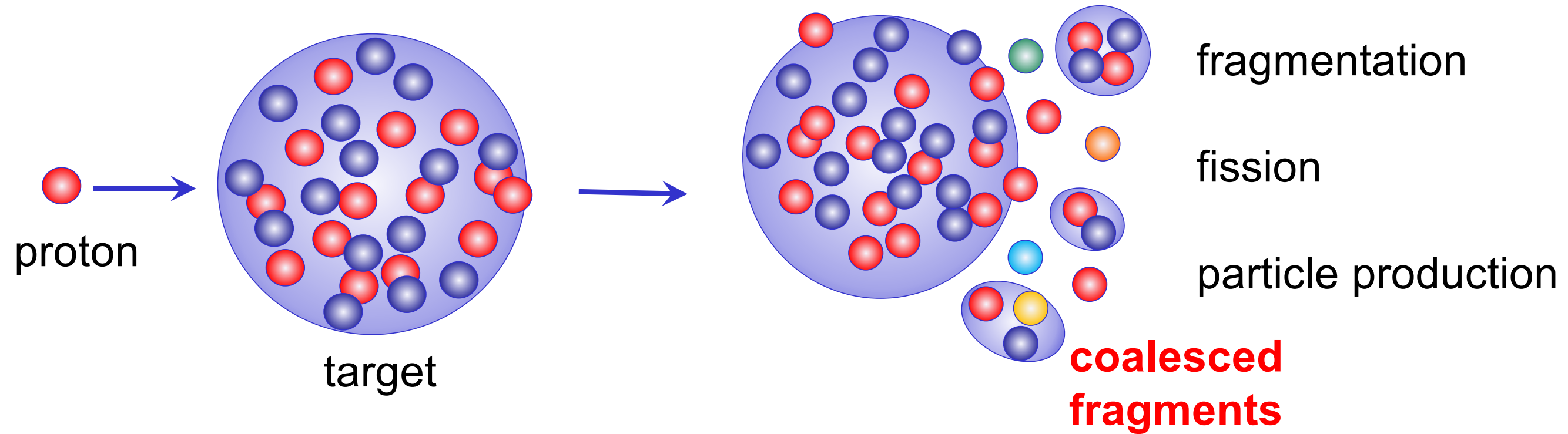
- High Luminosity: $L = 10^{33} - 10^{34} \text{cm}^{-2}\text{sec}^{-1}$, $10 - 100 \text{fb}^{-1}/\text{year}$
- Polarized beams: e, p, d, ^3He
- Large Center of Mass Energy Range:
 $E_{\text{cm}} = 29 - 140 \text{ GeV}$
- Large Ion Species Range: protons – Uranium

- **How does the mass of the nucleon arise?**
The Higgs mechanism accounts for only $\sim 1\%$ of the mass of the proton.
- **How does the spin of the nucleon arise?**
The spin of the quarks accounts for only one-third of the spin of the proton.
- **What are the emergent properties of dense system of gluons?**
The gluon saturation describes a new state of matter at extreme high density.

Fragment production: Cascade & coalescence & evaporation



Transport equations + coalescence

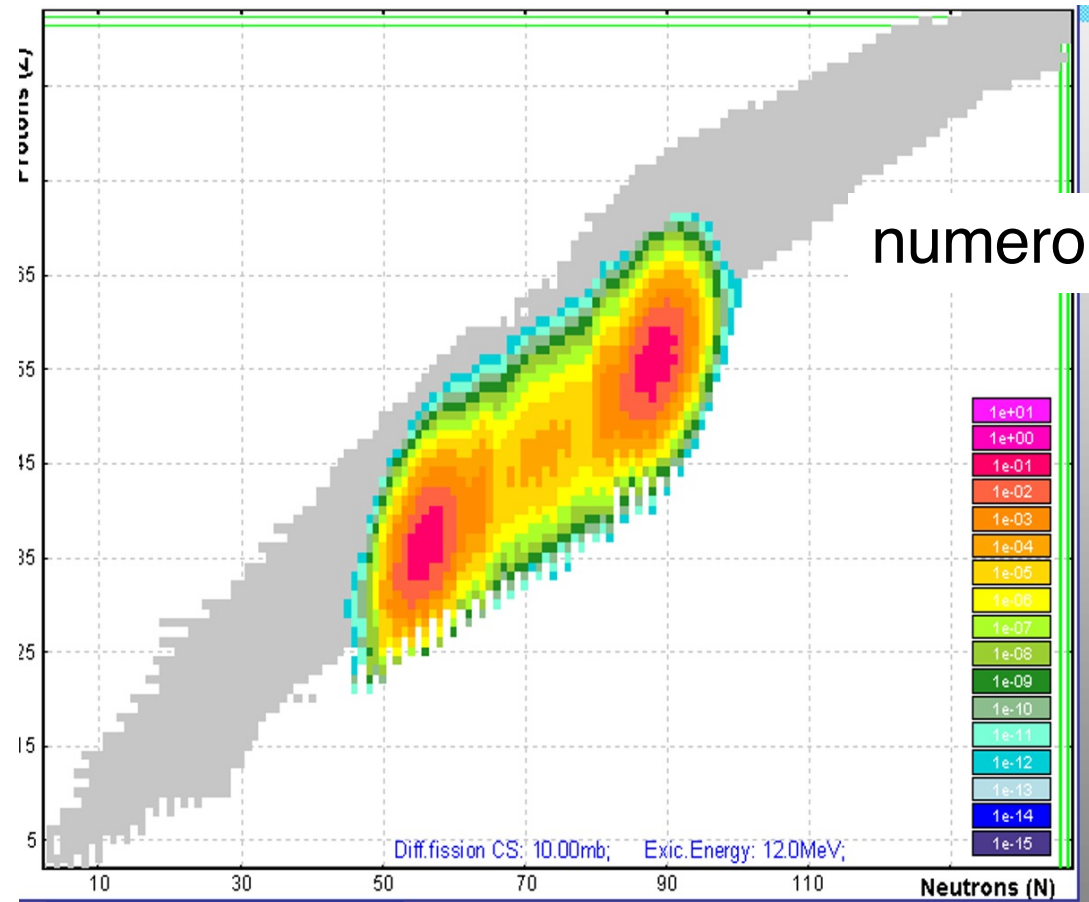


$$C_A = \frac{2J_A + 1}{2^A} \frac{1}{\sqrt{A} m_T^{A-1}} \left(\frac{2\pi}{R^2 + \left(\frac{r_A}{2}\right)^2} \right)^{\frac{3}{2}(A-1)}$$

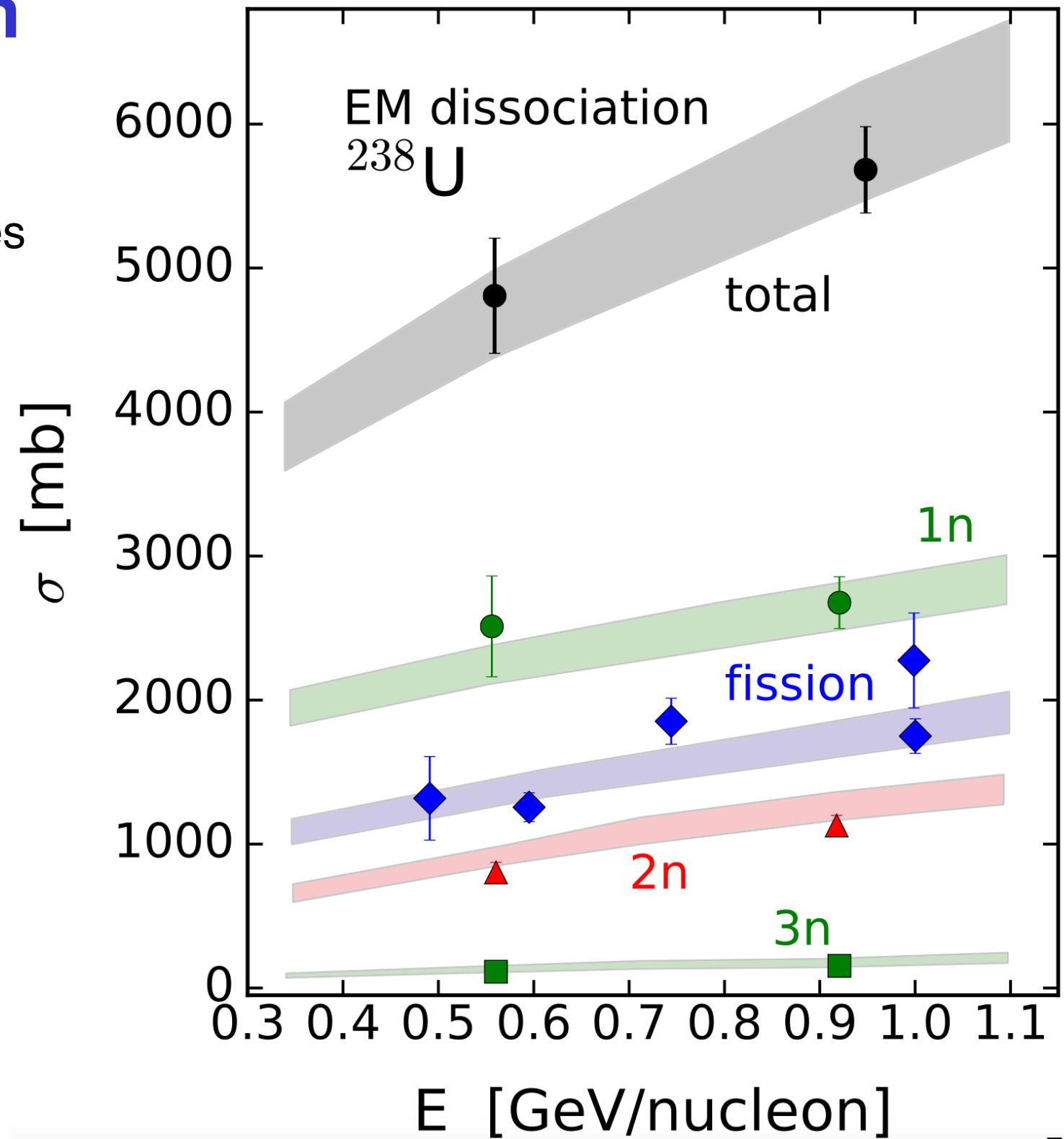
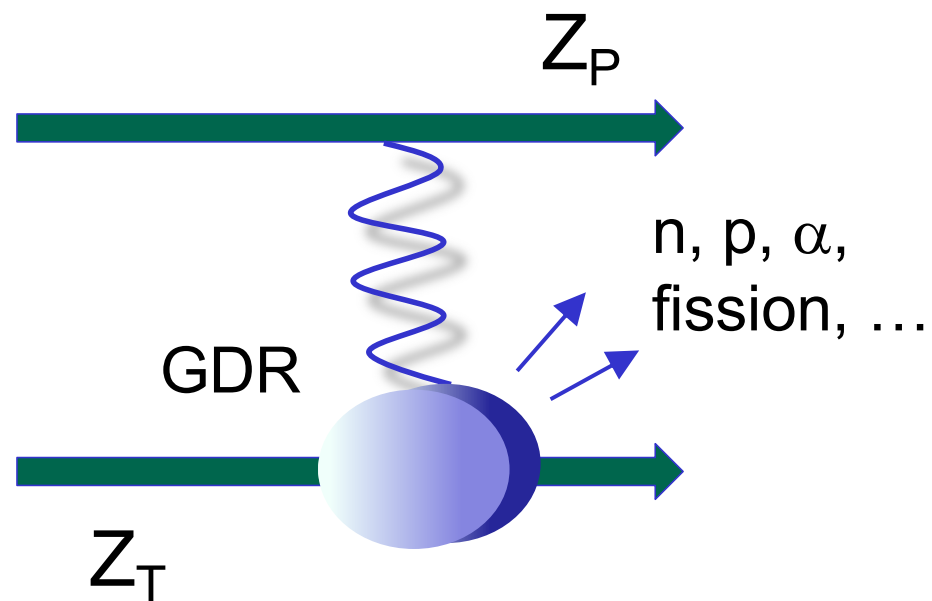
Particles produced coalesce into nuclei if they are close in space and momentum.

R = source size, r_A = nuclear size
 m_T = transverse mass of coalesc. part.

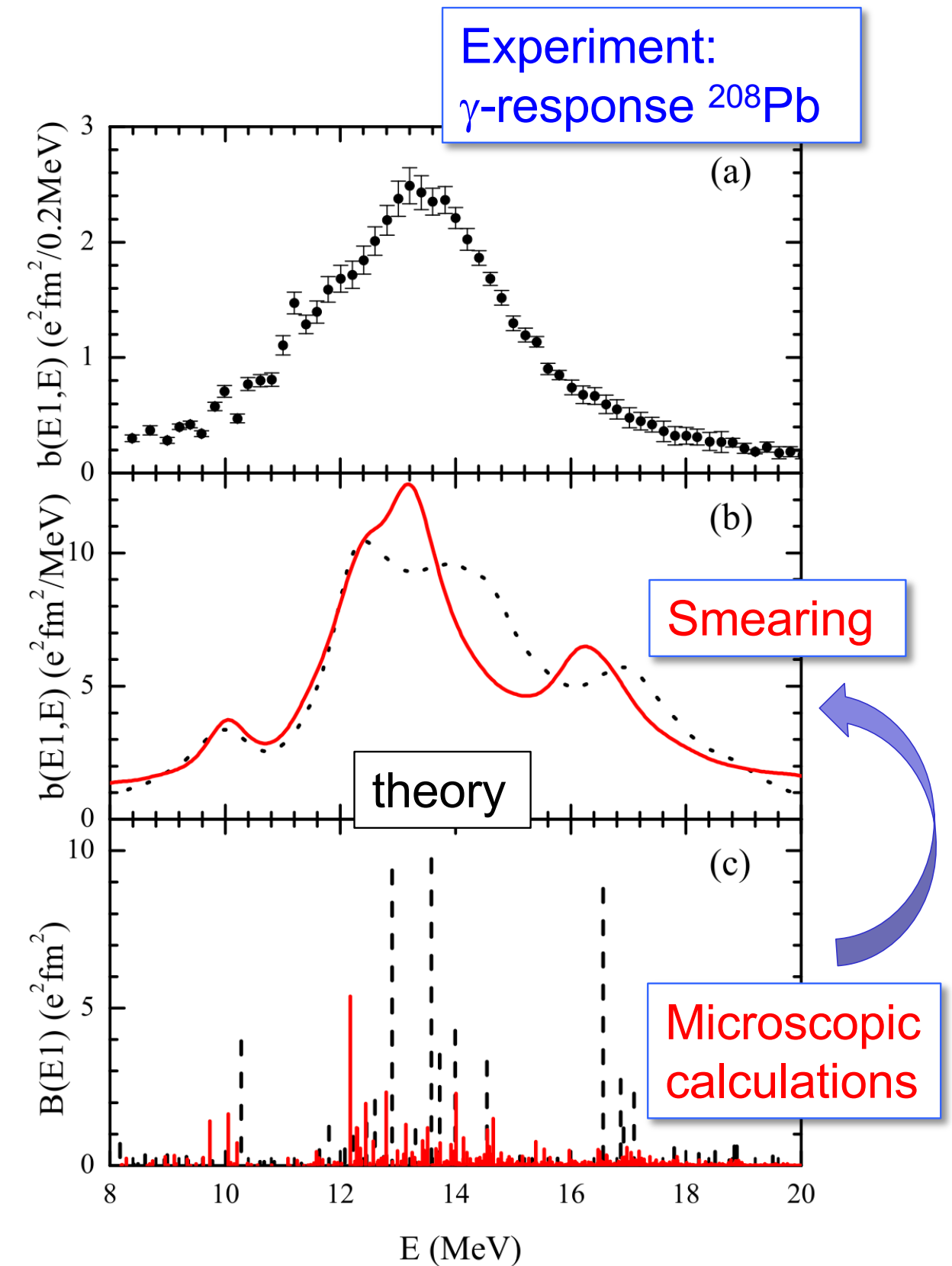
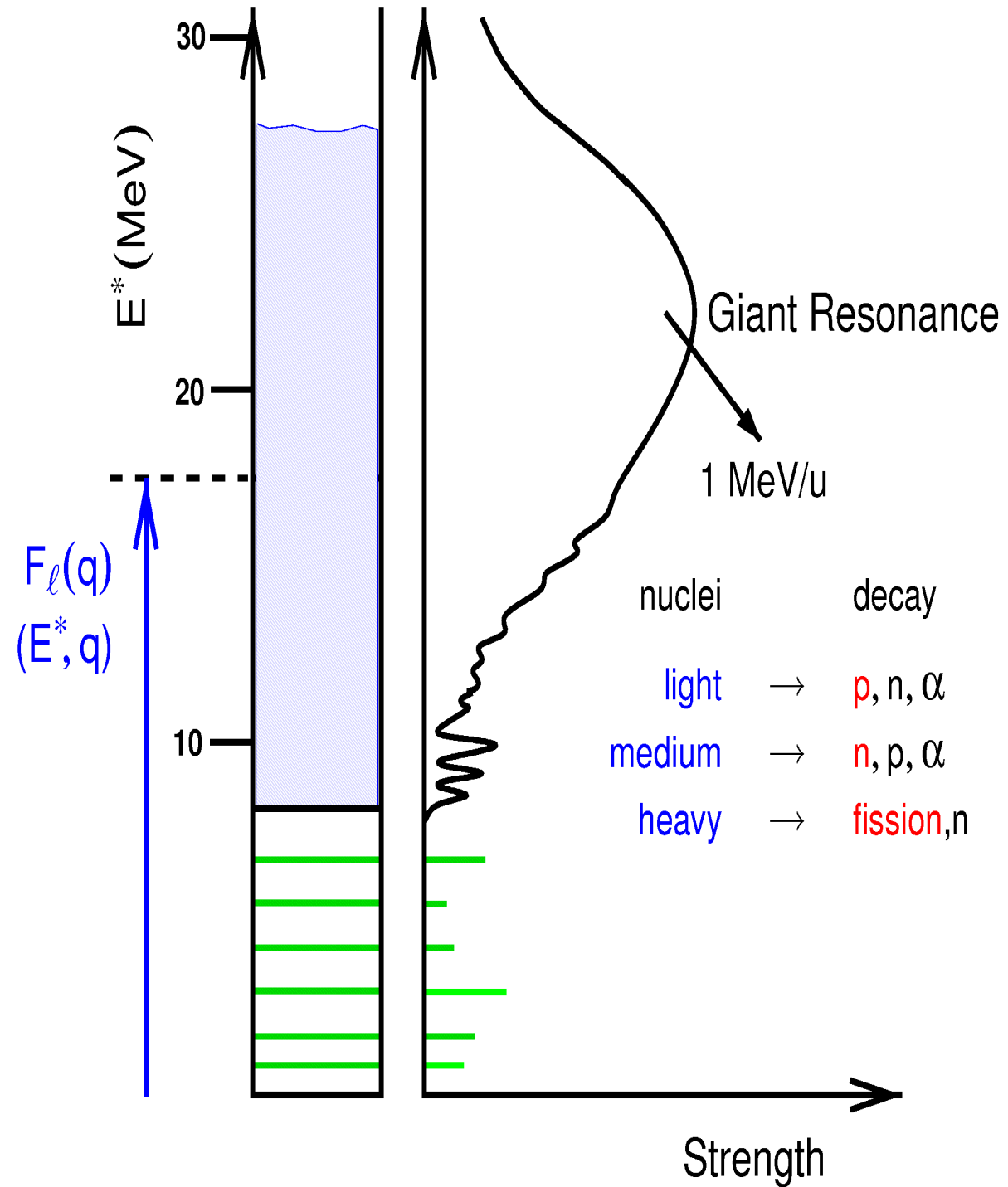
Electromagnetic fragmentation



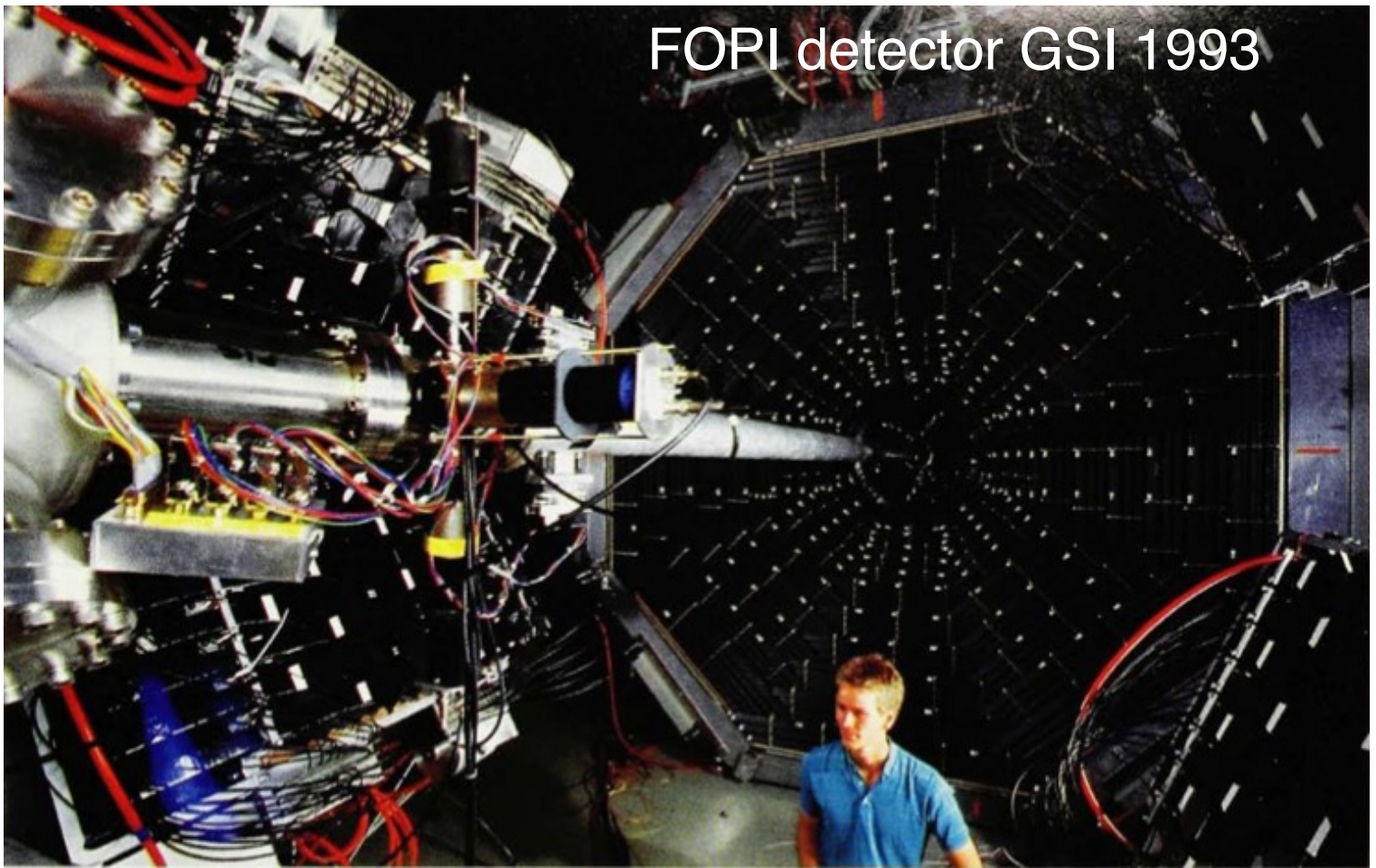
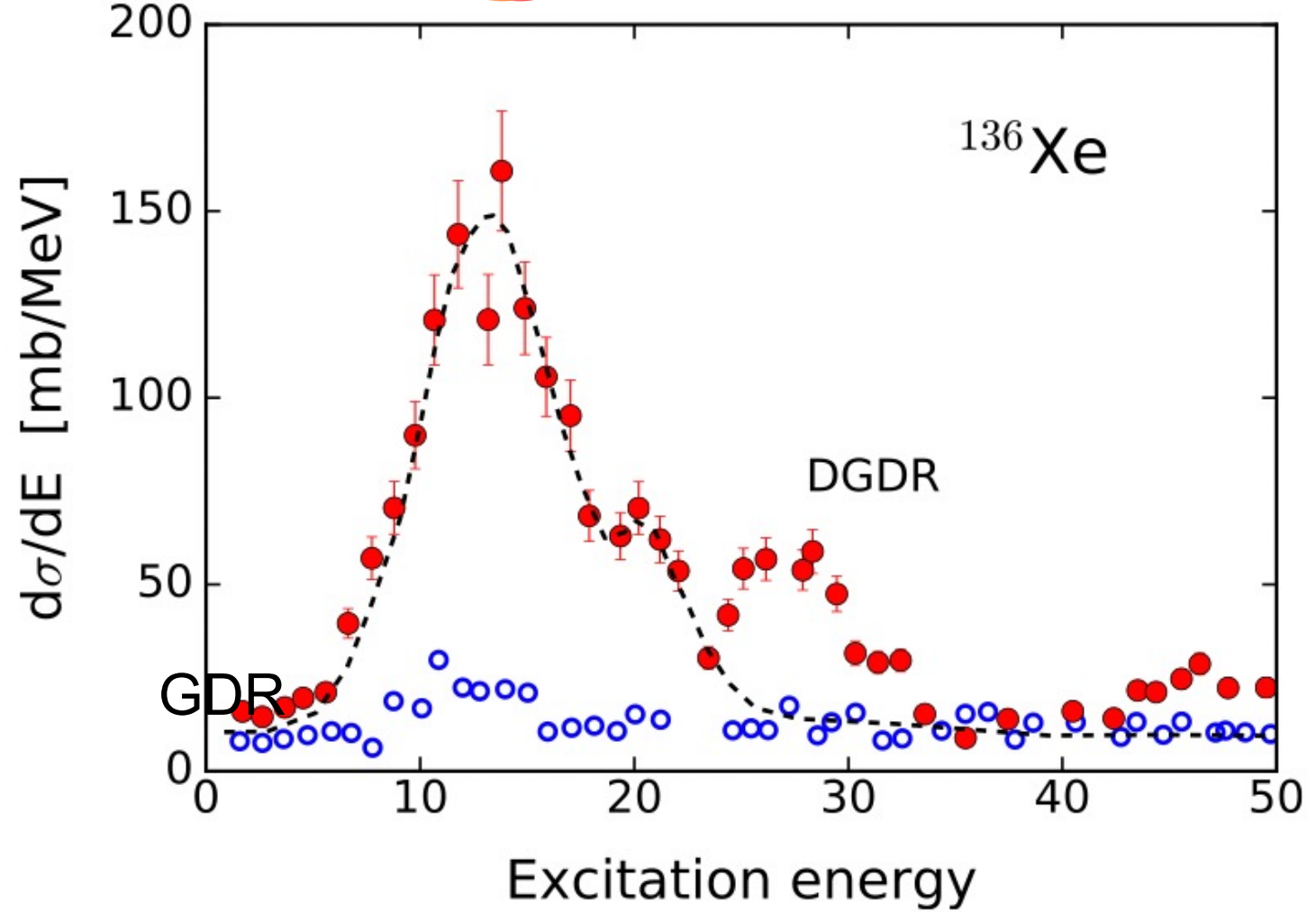
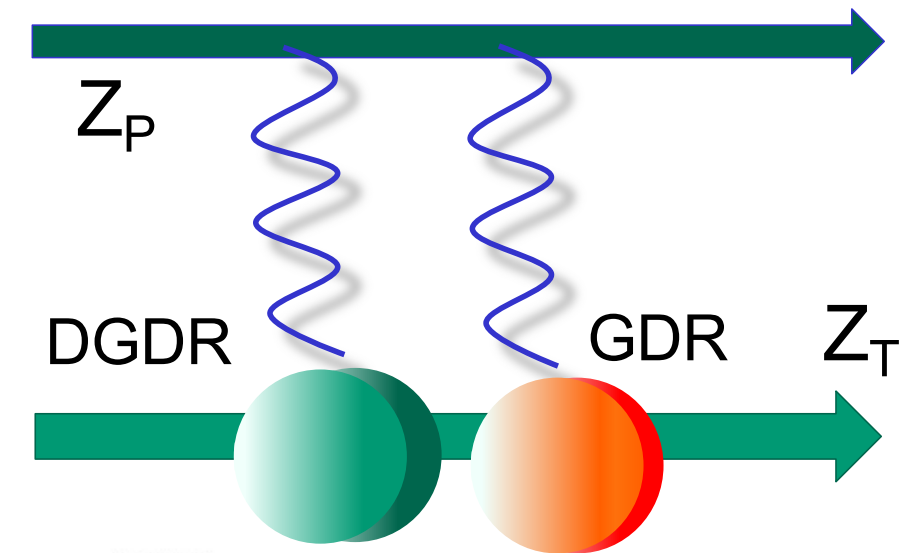
numerous new isotopes

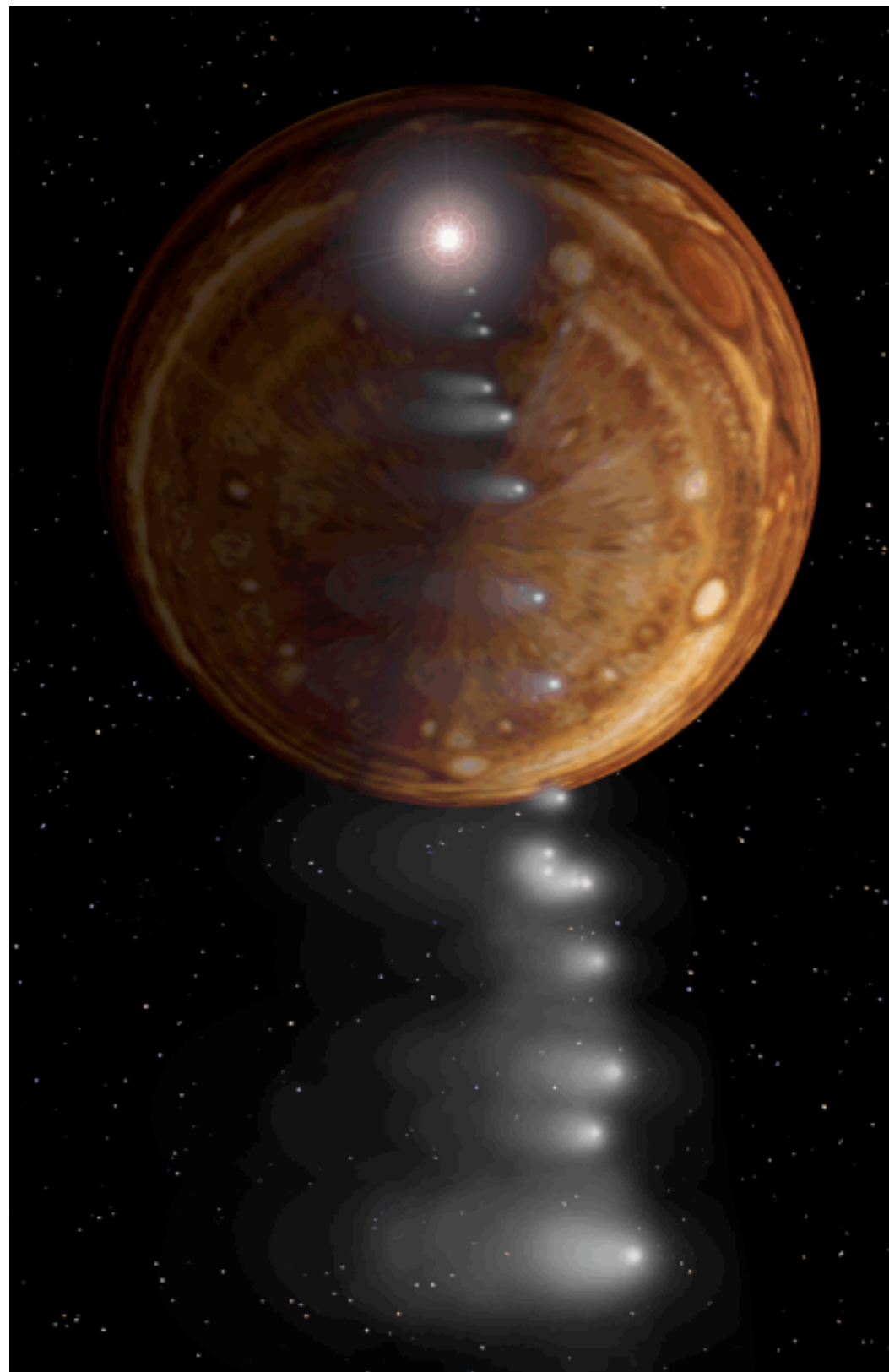


Giant resonances in nuclei



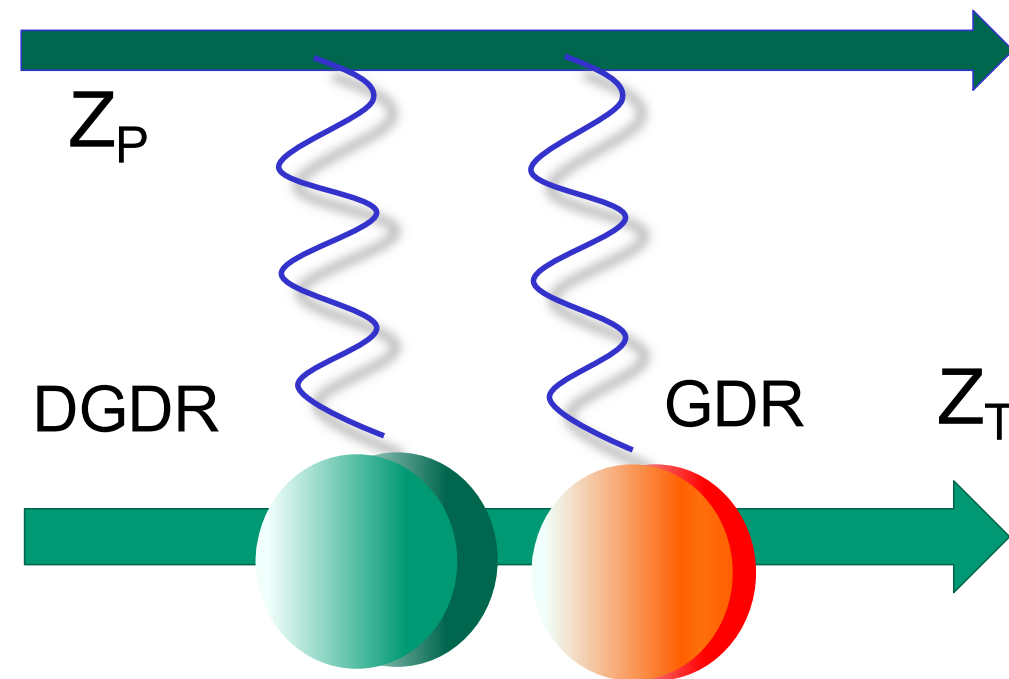
Double giant dipole resonance





Shoemaker-Levi comet (July 1992)

Fragmentation: **Classical and complicated**



Fragmentation: **Quantum and simpler**


Hauser-Feshbach theory

Include angular momentum conservation in the Ewing-Weisskopf theory

CN ang. mom. transmission probability

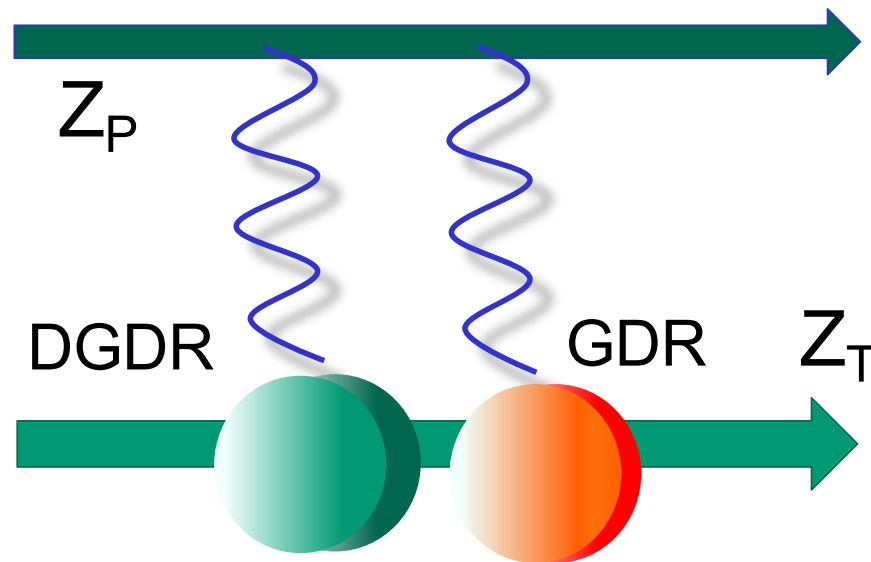
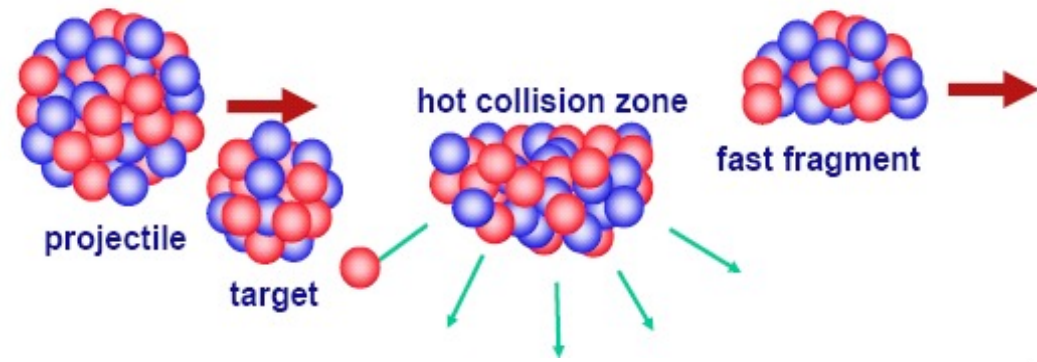
$$\sigma_{CN}(\alpha) = \frac{\pi}{k^2} \sum_J \frac{2J + 1}{(2j_a + 1)(2j_b + 1)} \frac{T_{l,s}(\alpha)}{\prod_{l,s,\alpha'} T_{l,s}(\alpha')}$$

projectile spin target spin

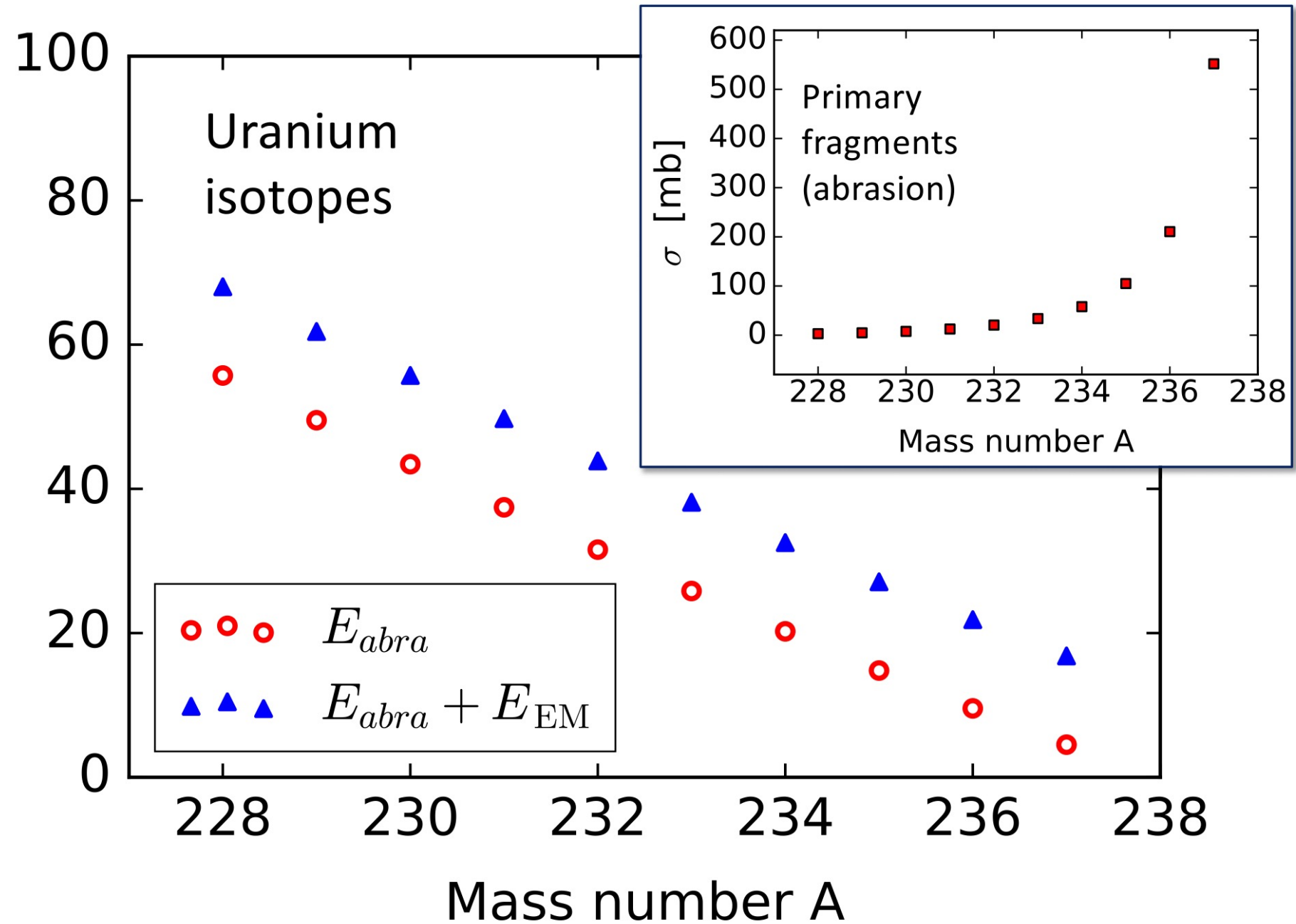


Optical potentials

Fragmentation in heavy ion collisions

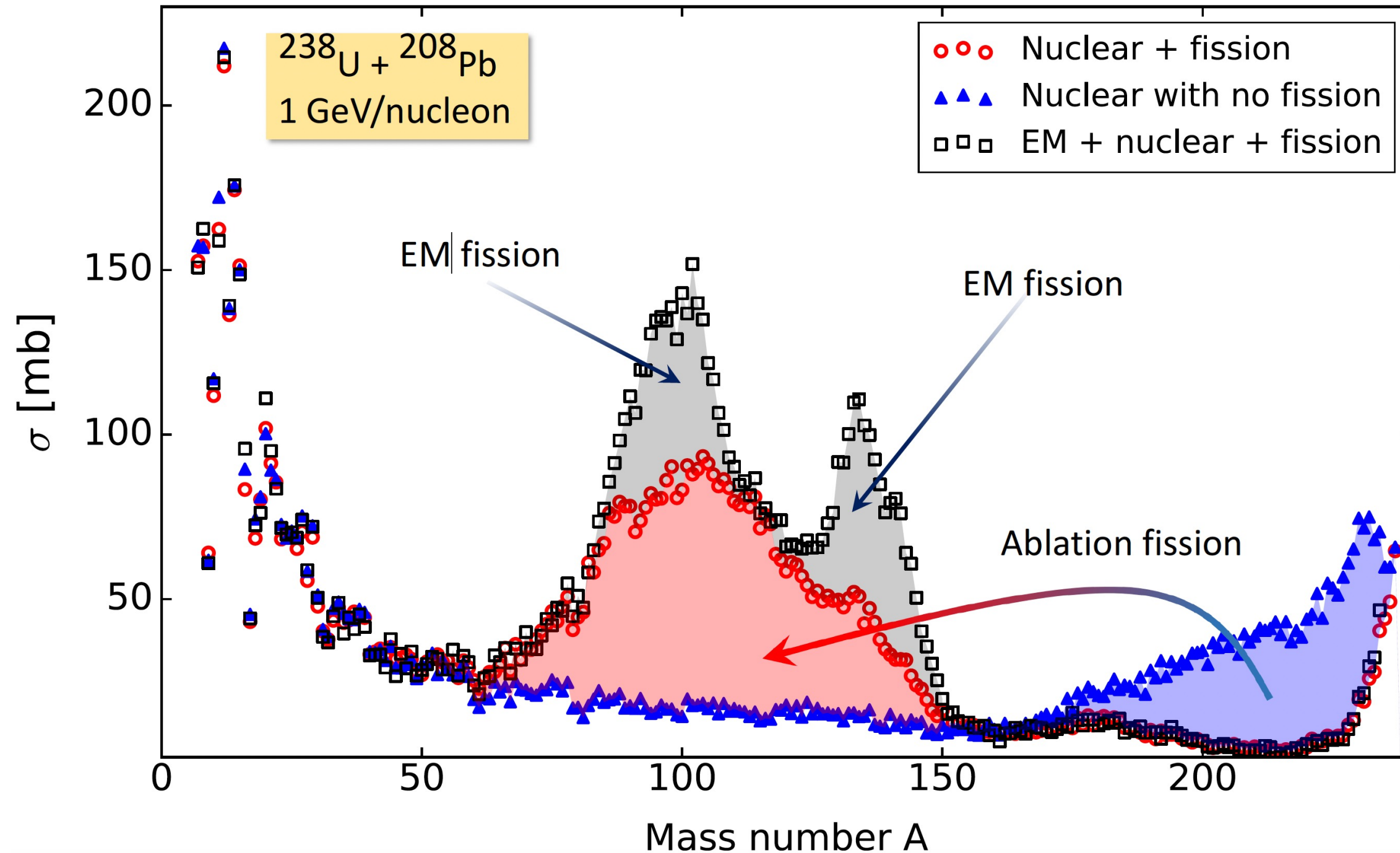


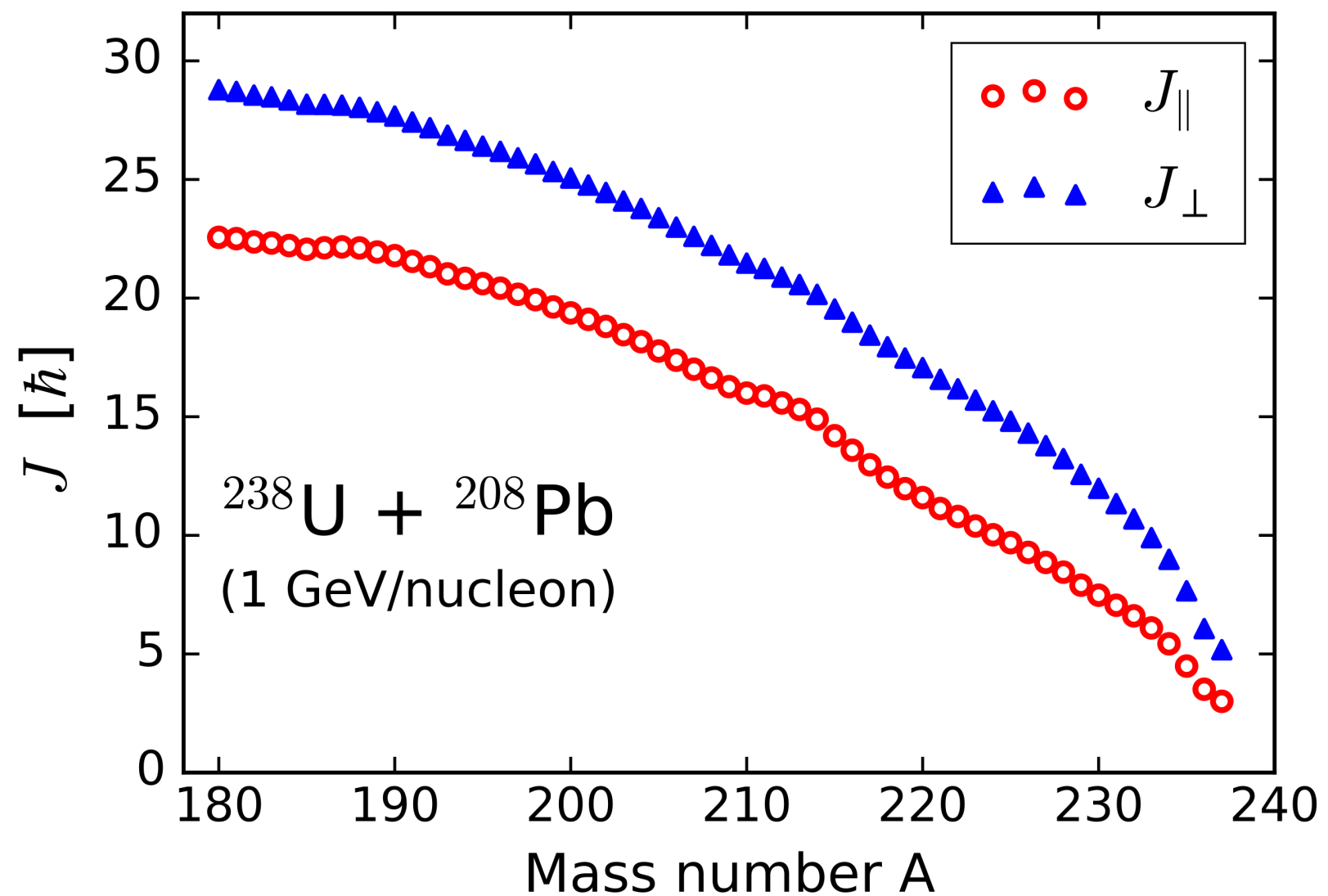
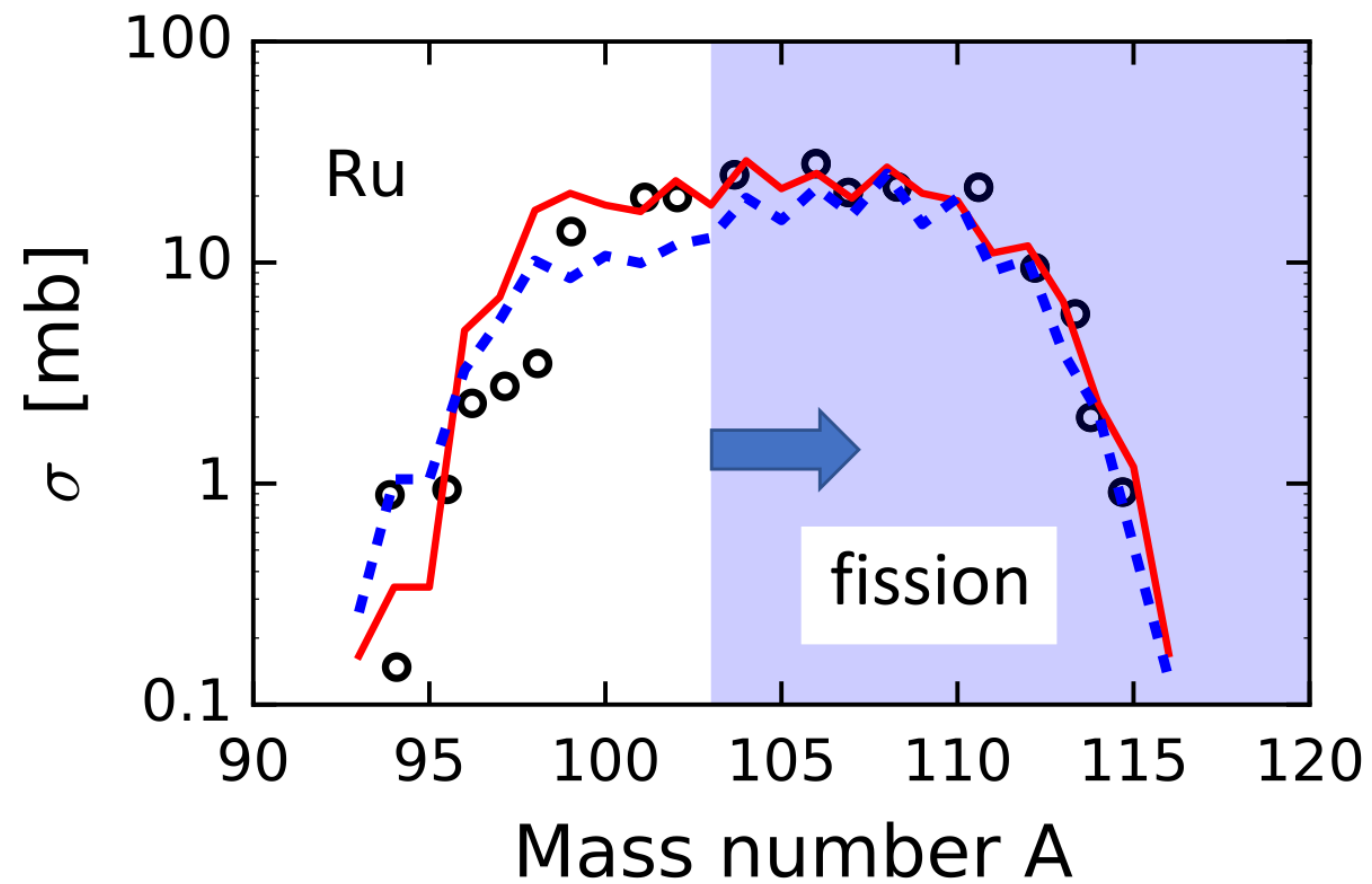
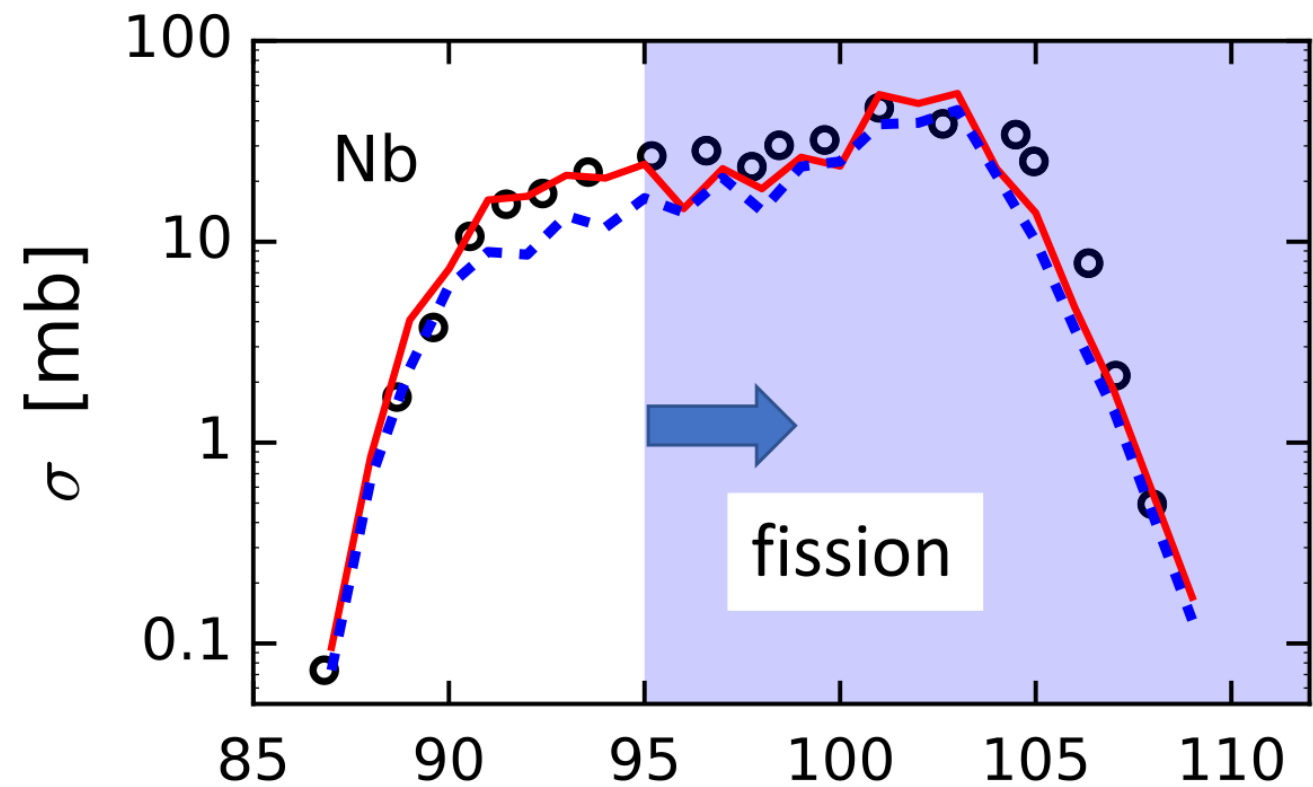
$\langle E \rangle$ [MeV]



Fragmentation in heavy ion collisions

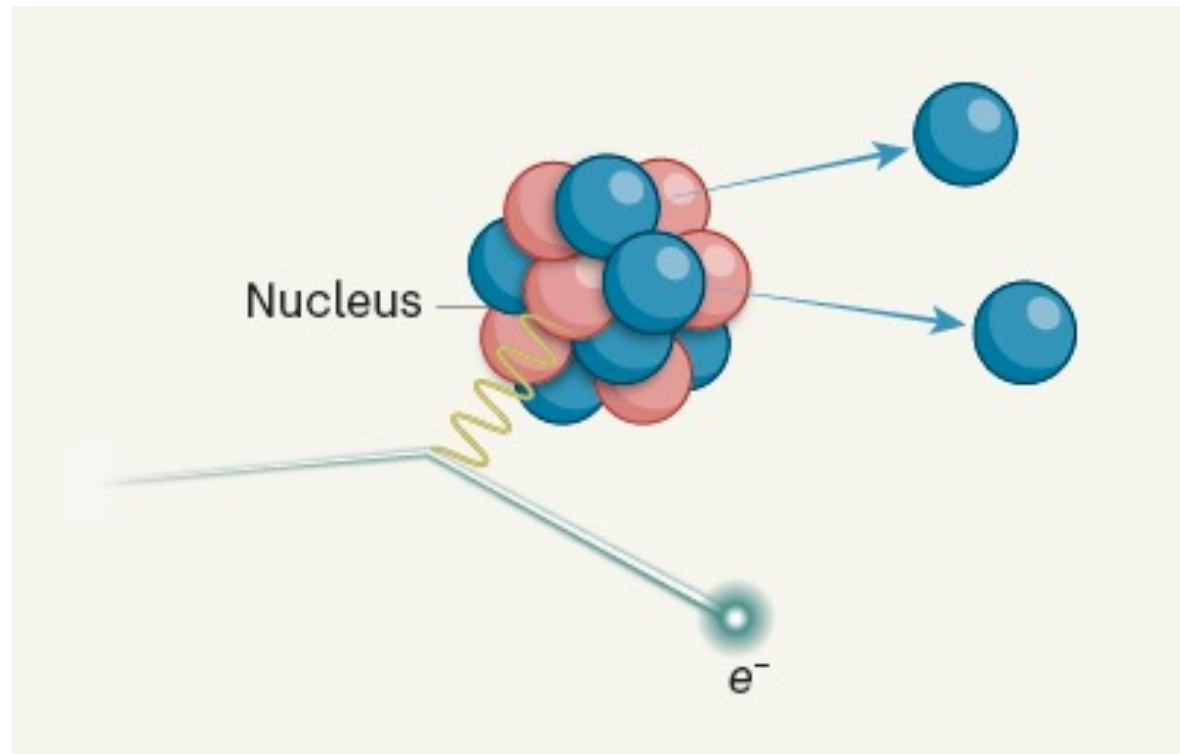
CB, Kucuk, Lozeva, PRL 124, 132301 (2020)





Five previously unknown isotopes
(182;183Tm, 186;187Yb, 190Lu)
[PRL 132, 072501 \(2024\)](#)

Zero degree physics at the EIC



No zero degree detector has been commissioned for the EIC, yet.

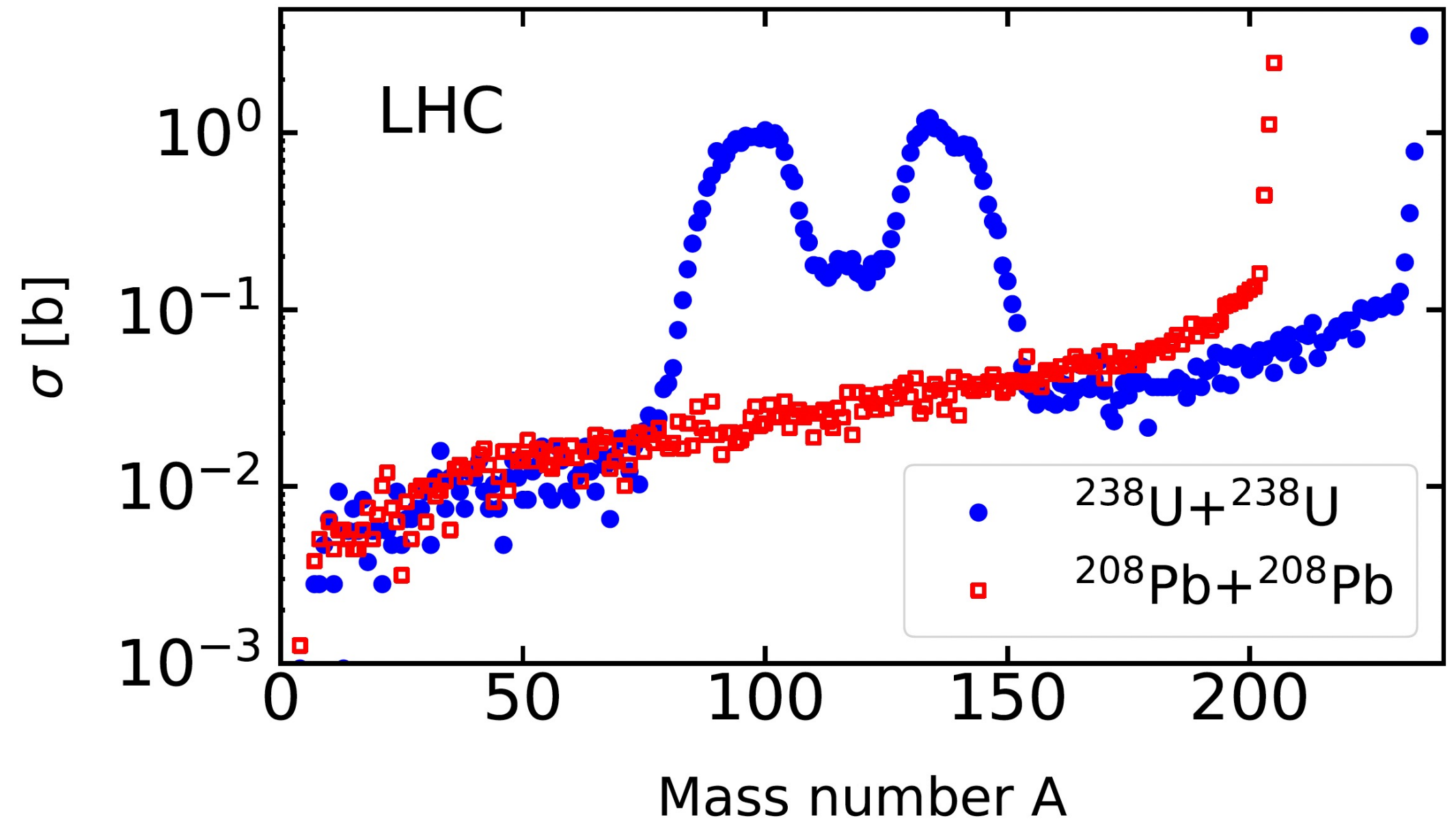
- Fragments move at high energies (> 100 GeV/nucleon). Time dilation allows detection for lifetimes > 1 ns.
- De-excitation photons are boosted to energies much larger than background photons

➡ Possible study of low energy physics of the isotopes.

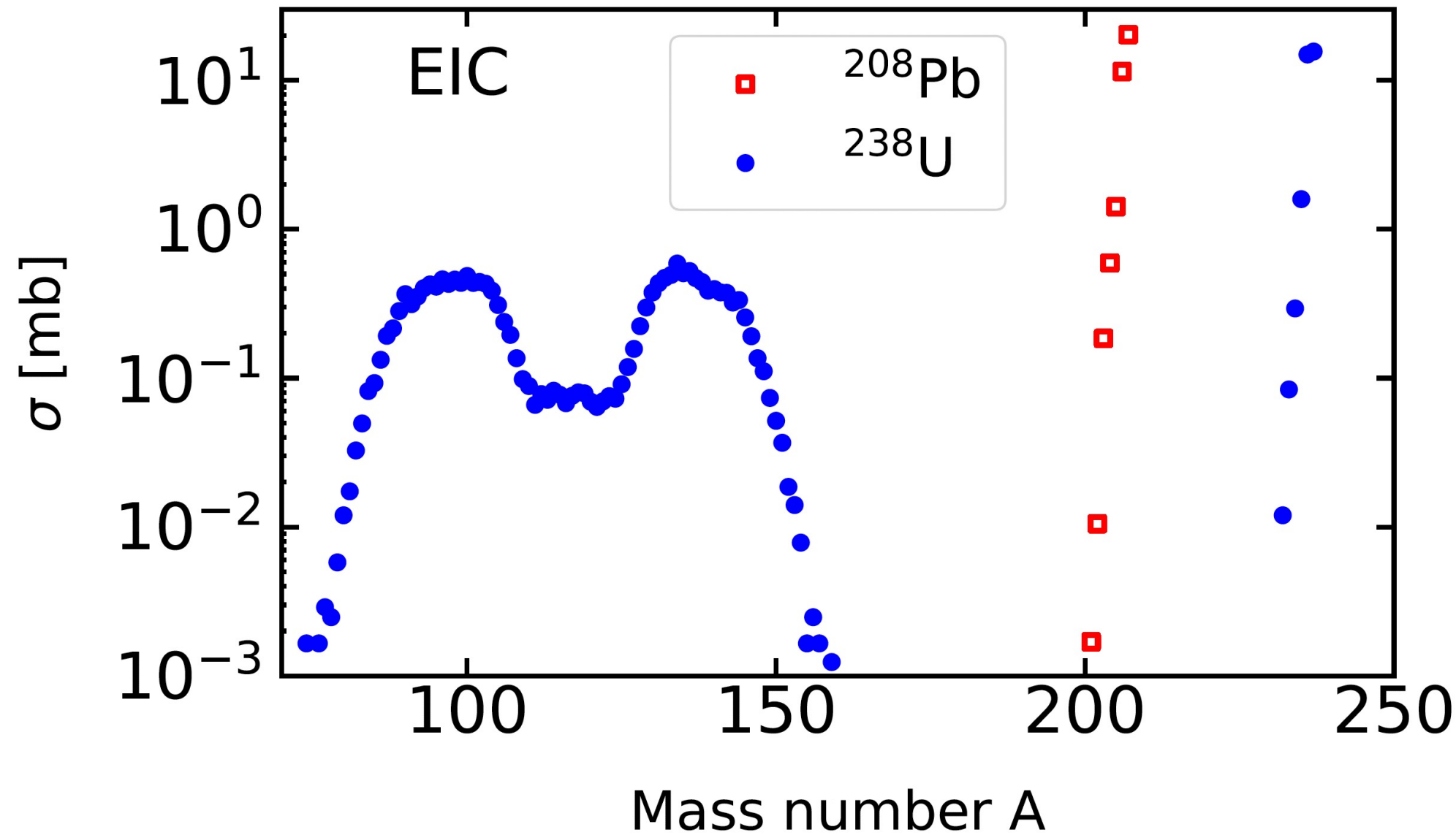
Nuclear fragmentation at the LHC

Excitation of GRs
+
evaporation

CB, Kucuk, Navarra,
[arXiv:2408.10157](https://arxiv.org/abs/2408.10157) (2024)



Nuclear fragmentation at the EIC



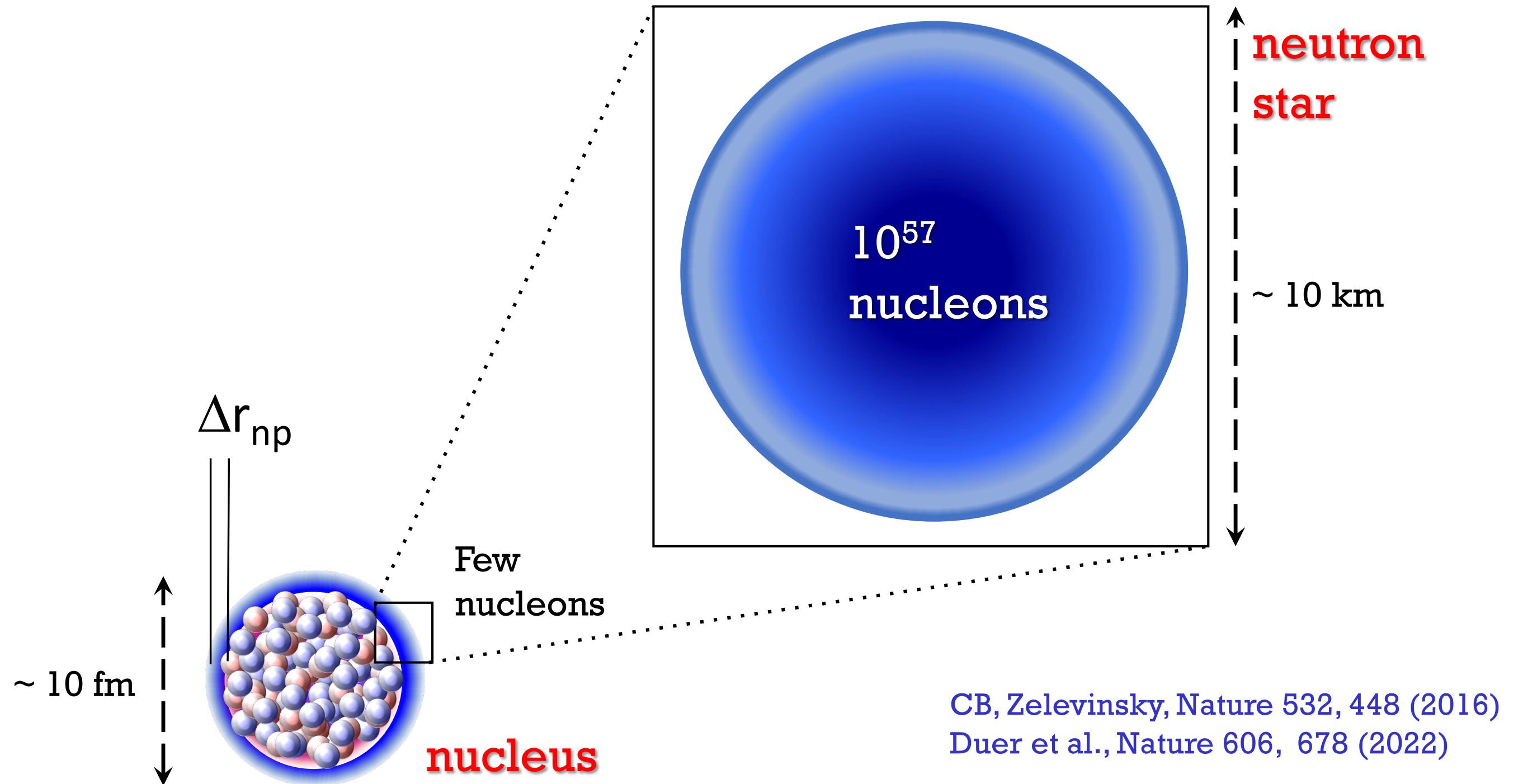
$$\frac{d\sigma}{d\omega dQ^2} = \sum_{\lambda} \frac{dN_{\lambda}}{d\omega dQ^2} \sigma_{\gamma}^{\lambda}(\omega)$$

$$\sigma_x^{GR}(\omega) = b_x(\omega) \sum_{GR} \sigma_{\gamma}^{GR}(\omega)$$

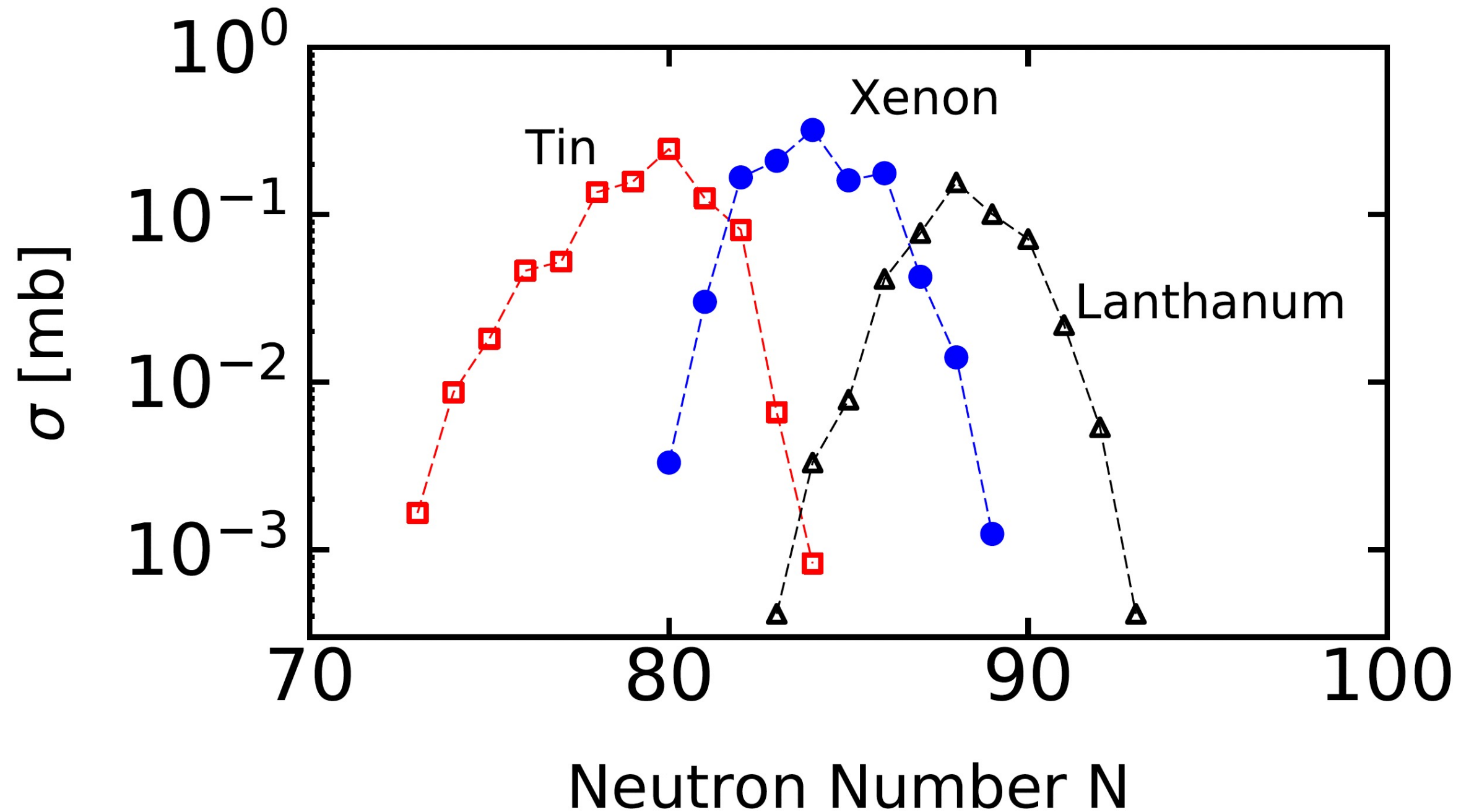
$$b_x(\omega) = \frac{\Gamma_x(\omega)}{\Gamma_{tot}(\omega)}$$

x = fragment

EM nuclear response and neutron stars



Nuclear fragmentation at the EIC



Nuclear fragmentation at the EIC

Cross sections	LHC	LHC	EIC	EIC
	Pb + Pb [b]	U + U [b]	e-Pb [mb]	e-U [mb]
σ_{-1n}	33.93	33.20	20.24	15.58
σ_{-2n}	18.89	30.59	11.45	14.88
σ_{-3n}	2.546	3.537	1.416	1.591
σ_{-4n}	1.091	0.784	0.5933	0.2934
$\sigma_{fission}$	0	18.24	0	8.867
σ_{total}	55.74	85.48	33.90	41.32
Fission b.r.	0%	19.54%	0%	21.45%

Summary

Physics at EIC

- Origin of nucleon mass and spin
- 3D structure of the nucleon and nucleus
- Gluon saturation
- Hadronization

Physics at zero degree of EIC

- EIC is a cleaner probe
- EIC has the potential to produce new nuclear isotopes
- Fragments can be detected and identified using particle ID, ZDC, and other yet to be proposed detectors
- Level structure of produced isotopes would be assessed through the detection of the de-excitation photons

Evaporation

Compound nucleus theory

Heisenberg relation: \rightarrow for a state with width Γ

$$\Delta E \Delta t \sim \hbar$$

\rightarrow decay time:

$$\Delta t \sim \frac{\hbar}{\Gamma_{\alpha}}$$

If many decay channels \rightarrow decay probability =

$$\frac{\Gamma_{\alpha}}{\sum_{\alpha} \Gamma_{\alpha}} = \frac{\Gamma_{\alpha}}{\Gamma}$$

Bohr hypothesis: formation independent of decay

$$\sigma_{\alpha\alpha'} = \sigma_{CN}(\alpha) \frac{\Gamma_{\alpha'}}{\Gamma}$$

$a + b$

or

$c + d$

or ...

α

formation

\times

α'

decay

Ewing-Weisskopf theory

detailed balance:

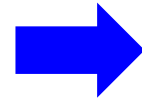
$$g_{\alpha} k_{\alpha}^2 \sigma_{\alpha\alpha'} = g_{\alpha'} k_{\alpha'}^2 \sigma_{\alpha'\alpha}$$

spin counting

for CN:

$$g_{\alpha} k_{\alpha}^2 \sigma_{CN}(\alpha) \Gamma_{\alpha'} = g_{\alpha'} k_{\alpha'}^2 \sigma_{CN}(\alpha') \Gamma_{\alpha}$$

$$\frac{\Gamma_{\alpha'}}{g_{\alpha'} k_{\alpha'}^2 \sigma_{CN}(\alpha')} = \frac{\Gamma_{\alpha}}{g_{\alpha} k_{\alpha}^2 \sigma_{CN}(\alpha)}$$



$$\Gamma_{\alpha} = g_{\alpha} k_{\alpha}^2 \sigma_{CN}(\alpha)$$

introducing density of levels ρ of final states:

$$\sigma_{\alpha\alpha'} = \sigma_{CN}(\alpha) \frac{\mu_{\alpha'} E_{\alpha'} \sigma_{CN}(\alpha') \rho(E_{\alpha'})}{\sum_{\alpha} \int \mu_{\alpha} E_{\alpha} \sigma_{CN}(\alpha) \rho(E_{\alpha}) dE_{\alpha}}$$

Hauser-Feshbach formula & resonances

$$\langle \sigma \rangle = 2\pi^2 \omega \frac{\Gamma_a \Gamma_b}{\Gamma D} = \pi D^2 \omega \frac{T_a T_b}{T_{tot}}$$

where

$$T_a = 2\pi \left\langle \frac{\Gamma_a}{D} \right\rangle$$

- T_a = dimensionless number between 0 and 1 = probability that a particle of type a crosses the nuclear surface (with angular momentum l)
- T_a is related to the “**strength function**”, $\langle \Gamma/D \rangle$, describing how width is distributed smoothly in the nucleus.
- These functions still contain the barrier penetration functions.
- This yields the Hauser-Feshbach formula for estimating cross sections where the density of resonances is high.

$$\bar{\sigma}_{ab} = \frac{\pi/k^2}{(2J_a + 1)(2J_b + 1)} \sum_{J^\pi} (2J^\pi + 1) \frac{T_a^{l,s}(J^\pi, E) T_b^{l,s}(J^\pi, E)}{T_{tot}(J^\pi, E)}$$