

Heavy-quark suppression and anisotropic flow at intermediate momentum

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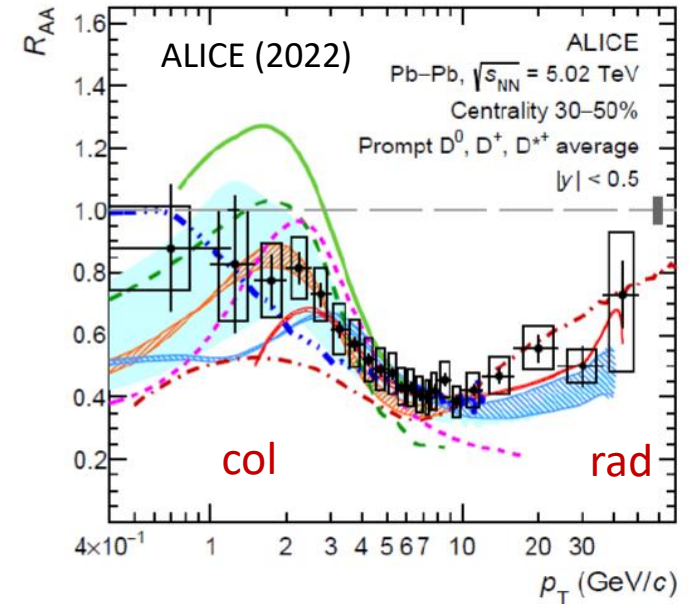


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Heavy quarks

- Important hard probes
- Large differences between transport models: describe experimental data with adjustment of model parameters
- Heavy quark energy loss
- Collisional/radiative dominant at low/high p_T
- At **intermediate momentum**, significant uncertainties: **transition between collisional and radiative energy loss**



Outline

- Boltzmann equation at **Intermediate momentum**:

$$\left(\frac{\partial}{\partial t} + \mathbf{v} \cdot \frac{\partial}{\partial \mathbf{x}} \right) f(\mathbf{p}) = C_{\text{col}}[f] + C_{\text{rad}}[f]$$

- **Collisional energy loss** in the Fokker-Planck approximation
- **Radiative energy loss** by gluon-bremsstrahlung from a single scattering:
radiative correction to the collision kernel for diffusion
- Single transport parameter:
heavy quark diffusion coefficient constrained by lattice QCD
- Consistently describe two energy losses and study the transition

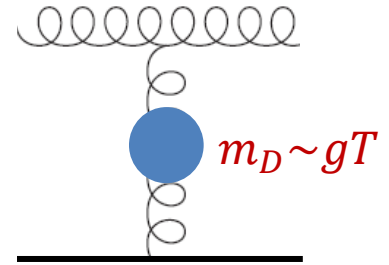
Collisional energy loss at low p

- Elastic scattering
- Brownian motion of heavy quarks

Collisional energy loss

- For soft gluon exchange: Fokker-Planck operator

$$C_{\text{col}}[f] = \frac{\partial}{\partial p^i} \underbrace{[\eta(\mathbf{p}) p^i f(\mathbf{p})]}_{\text{drag}} + \frac{1}{2} \frac{\partial^2}{\partial p^i \partial p^j} \underbrace{[\kappa^{ij}(\mathbf{p}) f(\mathbf{p})]}_{\text{diffusion}} \quad \text{Svetitsky (1988)}$$



- Momentum diffusion coefficient: $\kappa^{ij}(\mathbf{p}) = \kappa_L(p) \hat{p}^i \hat{p}^j + \kappa_T(p) (\delta^{ij} - \hat{p}^i \hat{p}^j)$

$$\kappa_{L,T}(p) = \int d^3 \mathbf{q} \frac{d\Gamma(\mathbf{q})}{d^3 \mathbf{q}} q_{L,T}^2 \quad \kappa_L(p=0) = \kappa_T(p=0)$$

- Approach the thermal equilibrium $f(p) \propto e^{-E/T}$: $\eta(p) = \frac{\kappa_L(p)}{2TE} + O\left(\frac{T}{E}\right)$
- Collisional energy loss by $\kappa_{L,T}(p=0)$ and their momentum dependence

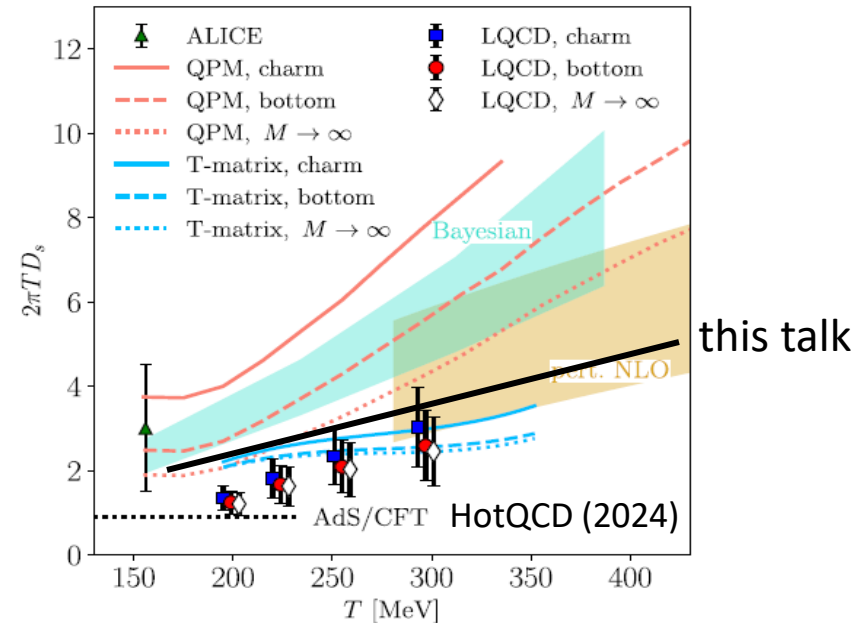
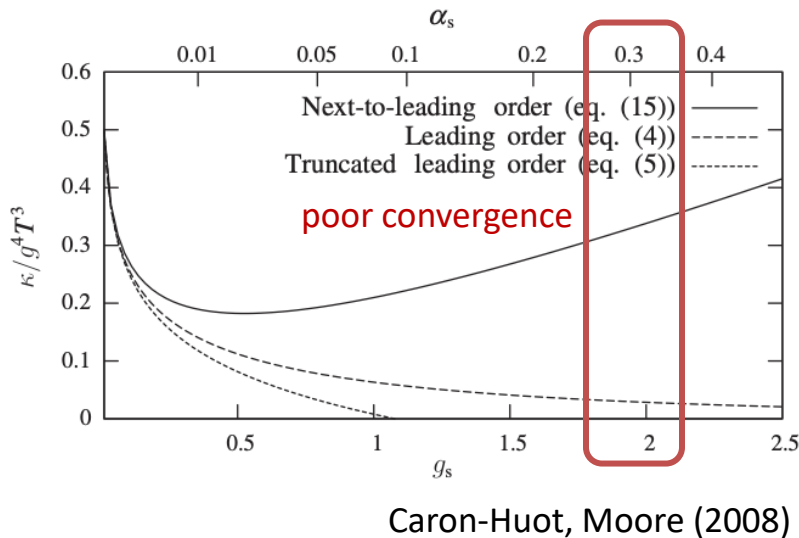
Heavy quark diffusion coefficient

At weak coupling

- LO: $\kappa_{LO} \sim \alpha_s^2 T^3$
- NLO: $\kappa_{NLO} \sim g \alpha_s^2 T^3$

Bose-enhancement with soft ($k \sim gT$) gluons

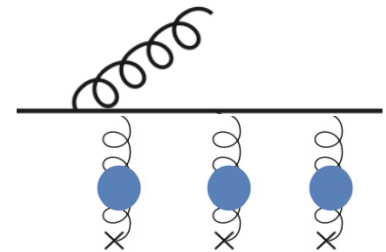
$$\alpha_s n_B(k) \sim \alpha_s \frac{1}{e^{k/T} - 1} \sim \frac{g^2}{4\pi} \frac{T}{k} \sim g$$



- **Nonperturbative lattice QCD** for spatial diffusion: $D_s = \frac{2T^2}{\kappa}$
- Temperature dependence by running coupling

Radiative energy loss at high p

- Medium-induced gluon emission
- Soft gluon exchange, collinear emission



Arnold, Moore, Yaffe (2001,2002)

Medium-induced gluon emission

- Semi-collinear emission from a single scattering

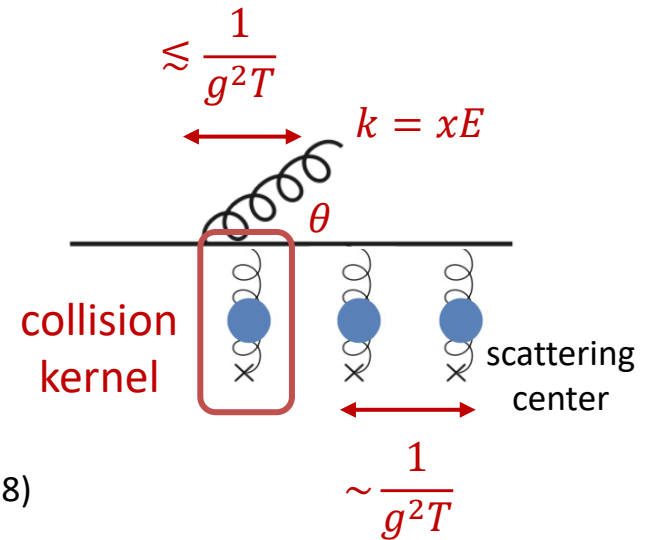
- Formation time: $t_f \sim \underbrace{\frac{k}{m^2 x^2 + k_T^2}} \lesssim mfp$

- Dead-cone for $\theta \sim \frac{k_T}{k} < \frac{m}{E}$ Dokshitzer, Kharzeev (1998)

- Smooth transition between low and high- p regimes

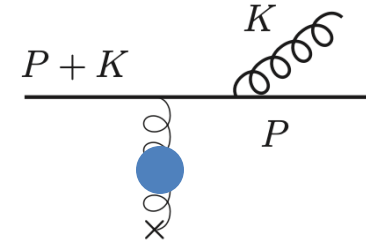
- With diffusion kernel: gluon emission rate with diffusion coefficient:

$$\frac{d\Gamma}{dk} = \frac{g^2 C_F \kappa_T}{\pi k} [1 + n_B(k)] [1 - n_F(E_{p-k})] [(1-x)^2 + 1] \int \frac{d^2 \mathbf{p}_T}{(2\pi)^2} \frac{1}{(\mathbf{p}_T^2 + m^2 x^2 + m_g^2)^2}$$



Radiative energy loss

- Eikonal approximation: $\mathbf{p} + \mathbf{k} = (p + k)\hat{\mathbf{p}}$



$$C_{\text{rad}}[f] = \underbrace{\int dk \left[f((p+k)\hat{\mathbf{p}}) \frac{d\Gamma(E_{(p+k)\hat{\mathbf{p}}}, k)}{dk} - f(\mathbf{p}) \frac{d\Gamma(E_{\mathbf{p}}, k)}{dk} \right]}_{\text{if } k < 0, \text{ gluon absorption for detailed balance}} + \underbrace{\frac{1}{2} \nabla_{\mathbf{p}T}^2 [\delta\kappa_T(p) f(\mathbf{p})]}_{\text{radiative correction}}$$

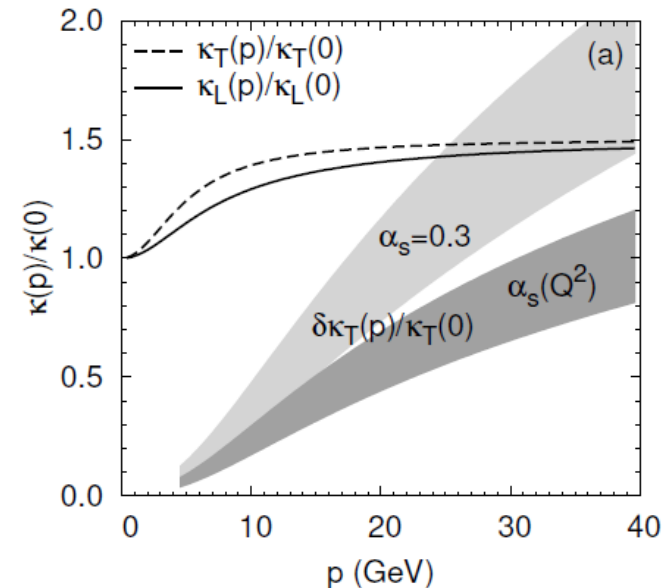
if $k < 0$, gluon absorption for detailed balance

radiative correction

- Radiative correction:

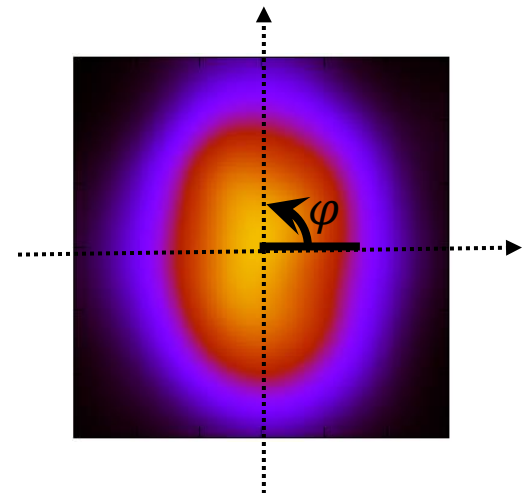
$$\delta\kappa_T = \int \frac{d^2\mathbf{k}_T}{(2\pi)^2} \mathbf{k}_T^2 \underbrace{\delta C(\mathbf{k}_T)}_{\propto \kappa_T} [1 + n_B(k)]$$

- Radiative energy loss with κ_T

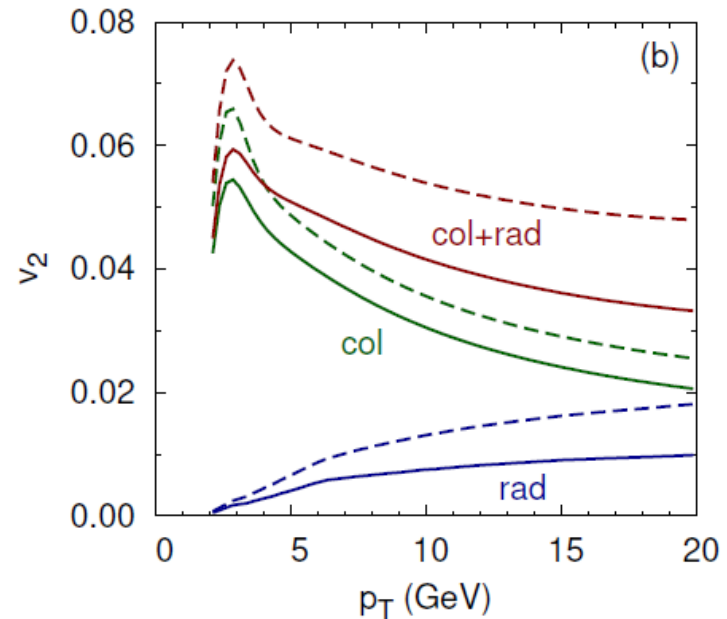
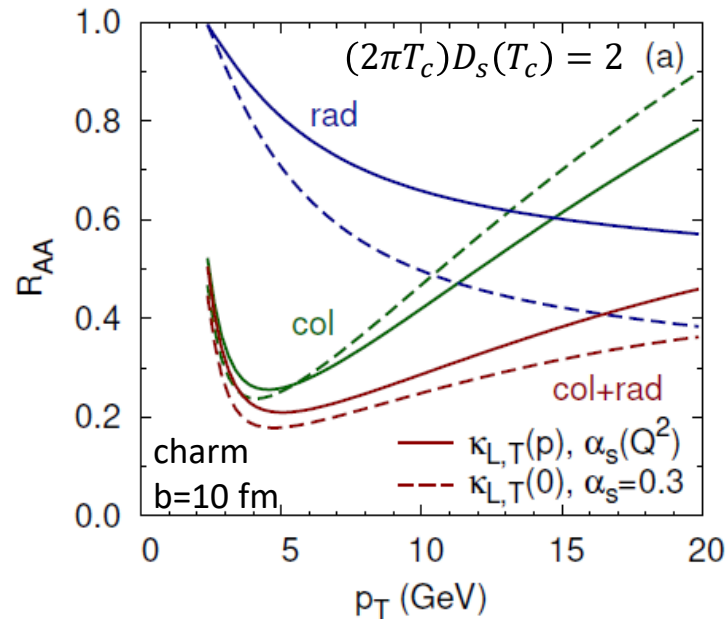


Numerical study

- Hydrodynamics with initial Glauber
- Nuclear modification factor
- Elliptic flow: asymmetric energy loss

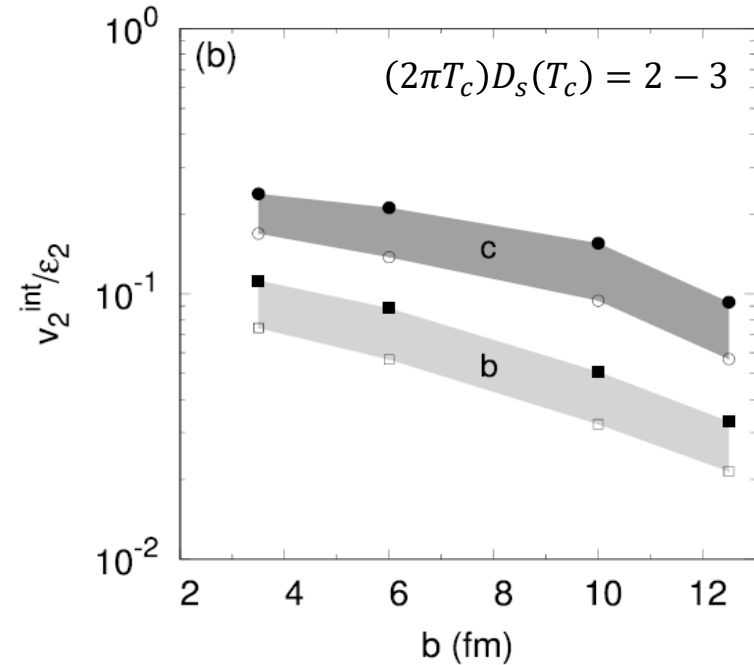
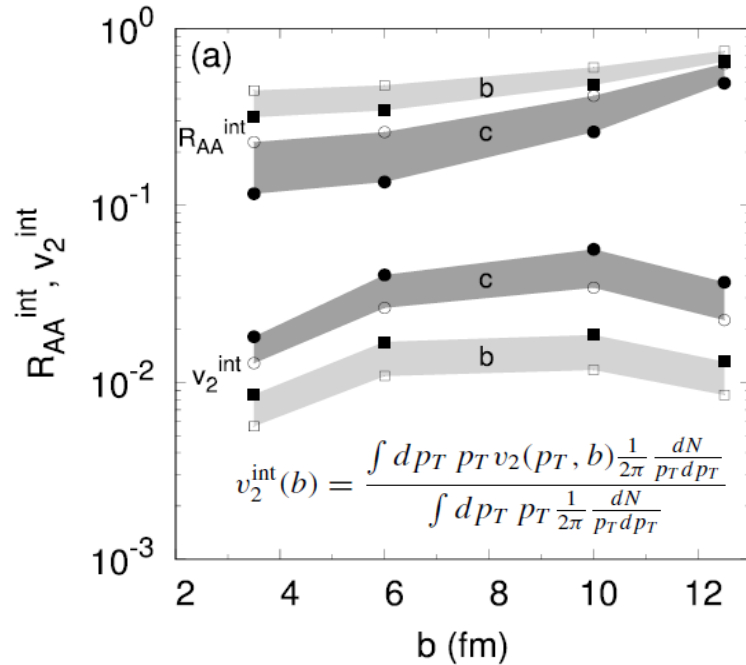


Heavy quark R_{AA} and v_2



- $\kappa_{L,T}(p)$ increase with p at leading-log Moore, Teaney (2005)
- Temperature dependence by running coupling: $\kappa_{L,T} \propto \alpha_s(ET) \alpha_s(m_D^2)$
Peigne, Peshier (2008)
- **Collisional/radiative** energy loss dominant at low/high momentum:
qualitatively different
- p, T -dependent $\kappa_{L,T}$: transition at higher momentum

b, m -dependence



- R_{AA} : larger energy loss in more central collisions
- v_2 : energy loss $\leftrightarrow$ geometric deformation
- $m_b \approx 3 m_c$: $R_{AA}^b > R_{AA}^c$, $v_2^b < v_2^c$

Summary

- Heavy quark transport at **intermediate momentum**
- Boltzmann equation with a single transport parameter:
heavy quark diffusion coefficient constrained by **nonperturbative** lattice QCD
- **Collisional/radiative** energy loss dominant at low/high momentum:
qualitatively different momentum dependence
- **Transition** between collisional and radiative effect
- **Significance of radiative effect** depends on $\kappa_{L,T}(p, T)$

Thank you for your attention!