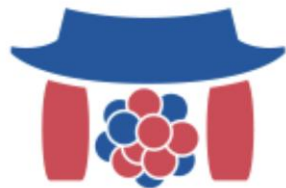


Heavy-ion induced single and double charge exchange reactions in a multi-channel approach: new results from the NUMEN project



Diana Carbone
on behalf of Francesco Cappuzzello
for the NUMEN collaboration



INPC 2025

May 25-30, 2025
DCC, Daejeon, Korea



- The problem of $0\nu\beta\beta$ -decay nuclear matrix elements (NMEs)
- The study of double charge exchange (DCE) @ INFN-LNS (NUMEN, NURE)
- The multichannel vision
- Recent results from SCE and DCE reactions
- Conclusions and perspectives

$0\nu\beta\beta$ decay

Open problem in modern physics:

Neutrino absolute mass scale

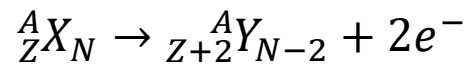
Neutrino nature



$0\nu\beta\beta$ is considered the **most promising approach**

^{75}Se	^{76}Se	^{77}Se	^{78}Se	^{79}Se
^{74}As	^{75}As	^{76}As	^{77}As	^{78}As
^{73}Ge	^{74}Ge	^{75}Ge	^{76}Ge	^{77}Ge

Still not observed



Isobaric nuclear transition where a parent nucleus spontaneously decays into a daughter nucleus changing by two units its charge and leaving the mass number unchanged

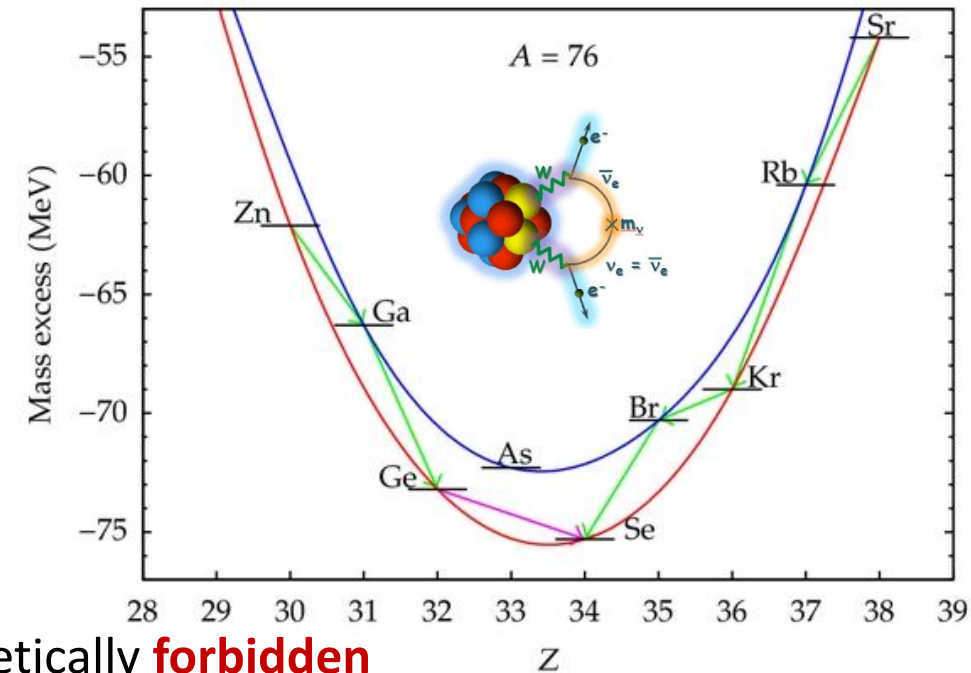
- ✓ Process mediated by the **weak interaction**
- ✓ Observable in even-even nuclei where the **single β -decay** is energetically **forbidden**

Beyond standard model:

- Violation of lepton number conservation
- CP violation in lepton sector



E. Majorana, Il Nuovo Cimento 14 (1937) 171
W. H. Furry, Phys. Rev. 56 (1939) 1184



Ejiri, H.; Suhonen, J.; Zuber, K., Physics Reports **2019**, 1, 797
Agostini, M.; Benato, G.; Detwiler J.A.; Menendez, J.; Vissani, F.;
Reviews of Modern Physics **2023**, 95, 025002

$0\nu\beta\beta$ decay

Intense activities in the searches for experimental evidence of this process

A worldwide challenge

$0\nu\beta\beta$ decay **half-life** $\downarrow$ Phase space factor $\downarrow$ contains the effective neutrino **mass** $\downarrow$

$$\left(T_{\frac{1}{2}}^{0\nu\beta\beta}(0^+ \rightarrow 0^+)\right)^{-1} = G_{0\nu\beta\beta} \left|M^{0\nu\beta\beta}\right|^2 \left|f(m_i, U_{ei})\right|^2$$

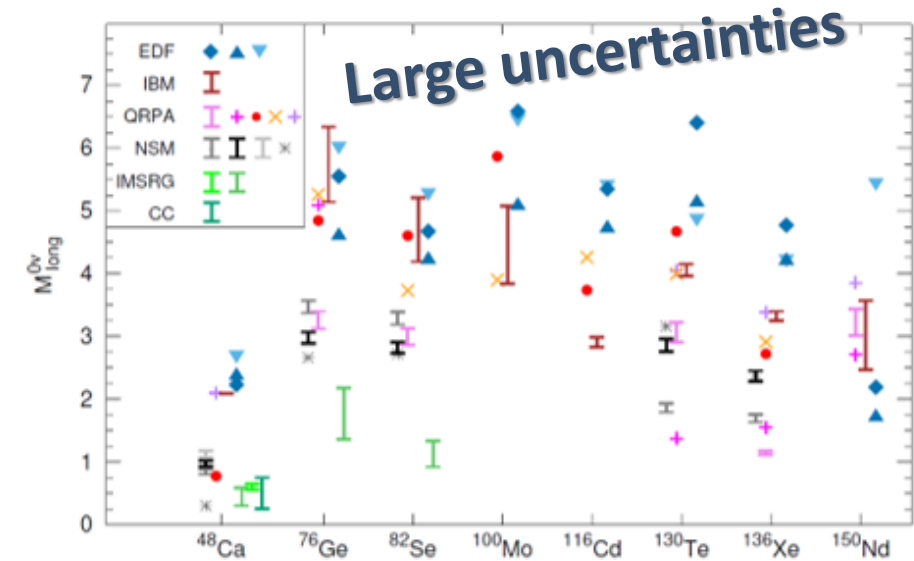
Nuclear Matrix Element (NME)

$$\left|M_{\varepsilon}^{0\nu\beta\beta}\right|^2 = \left|\left\langle\Psi_f\left|\hat{O}_{\varepsilon}^{0\nu\beta\beta}\right|\Psi_i\right\rangle\right|^2$$

Transition probability of a **nuclear** process

- ✓ NMEs are not physical observables
- ✓ The challenge is the description of the **nuclear many body states**
- ✓ Much work on the **transition operator**, now including all the known short-range weak interaction physics F.F. Deppisch et al., PRD 102, 095016 (2020)
- ✓ **Calculations** (still sizeable uncertainties): QRPA, Large scale shell model, IBM, EDF, ab-initio

State of the art NME calculations



M. Agostini et al., Rev. Mod. Phys. 95, 025002 (2023)

Support from the experiments

Measurements (not very strong constraining the $0\nu\beta\beta$ NME):

✓ β -decay and $2\nu\beta\beta$ decay

 1st order isospin probes
 2nd order isospin probes

✓ (π^+, π^-) , single charge exchange (SCE) ($^3\text{He}, t$), $(d, ^2\text{He})$, HI-SCE, electron capture, transfer reactions, μ -capture, γ -ray spectroscopy, double γ -decay etc.

✓ A recent promising tool: **Heavy-Ion Double Charge-Exchange (HI-DCE)**



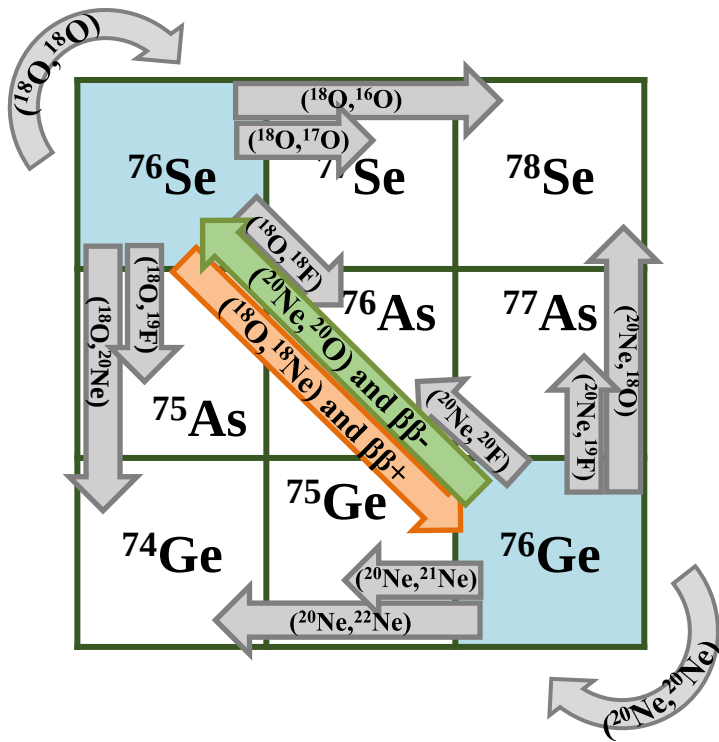
(**NU**clear **M**atrix **E**lements for **N**eutrinoless double beta decay)

Extraction from measured cross-sections of “*data-driven*”
information on NME for all the systems candidate for $0\nu\beta\beta$



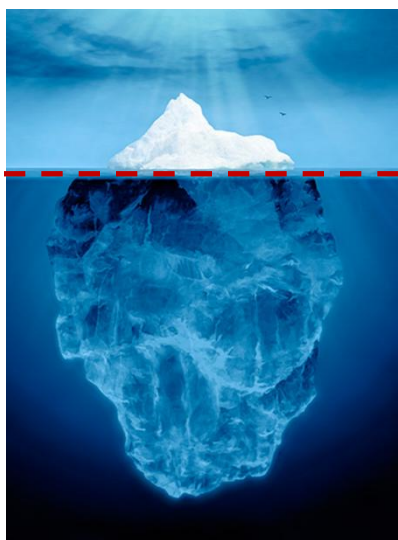
Heavy-ion DCE as surrogate processes of $\beta\beta$ -decay

- ✓ Induced by strong interaction
- ✓ Possibility to go in both directions
- ✓ Low but **measurable cross section in controlled laboratory conditions**



Tiny amount of DGT
strenght for low lying states

Sum rule almost exhausted
by DGT Giant Mode, still not
firmly established. First
indications in [A. Sakaue et
al. Prog. Theor. Exp. Phys.
123D03 (2024)]






RIKEN
RCNP

Heavy-ion induced DCE

Heavy ion DCE can proceed via:

Mean field driven processes

1) 4th order sequential multi-nucleon transfer (TDCE) mediated by mean-field

J.L. Ferreira et al., PRC 105, 014630 (2022)

J.L. Ferreira et al., PRC 111, 014630 (2025)

Collisional processes

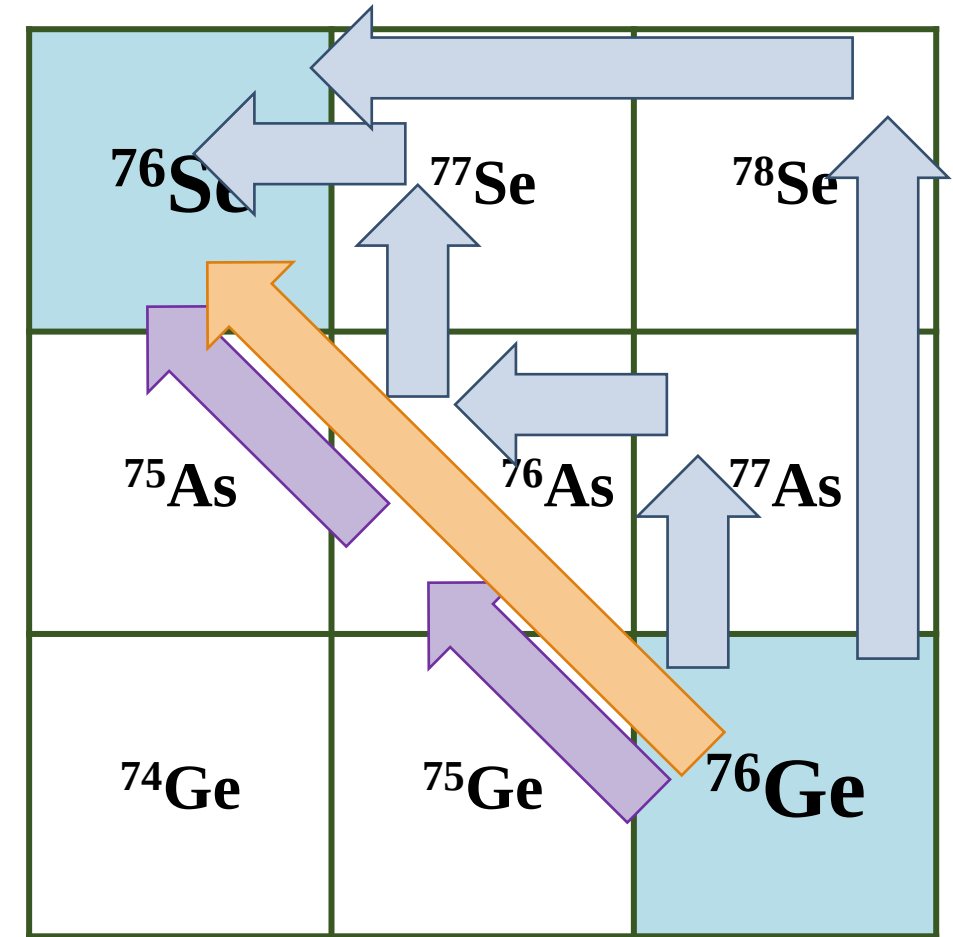
2) Two-step DCE - Double single charge exchange (DSCE): two consecutive single charge exchange processes, mediated by NN isovector interaction

H.Lenske et al., Universe (2024), 10, 93

3) One-step DCE - Two-nucleon mechanism (MDCE): relying on short range NN correlations, leading to the correlated exchange of two charged mesons between projectile and target

H. Lenske et al. Progr. Part. and Nucl. Physics 109 (2019) 103716

H. Lenske, Universe (2024) 10, 202



The DCE cross section combines the three different classes of reaction dynamics

F. Cappuzzello et al., Progr. Part. and Nucl. Physics 128, 103999 (2023)



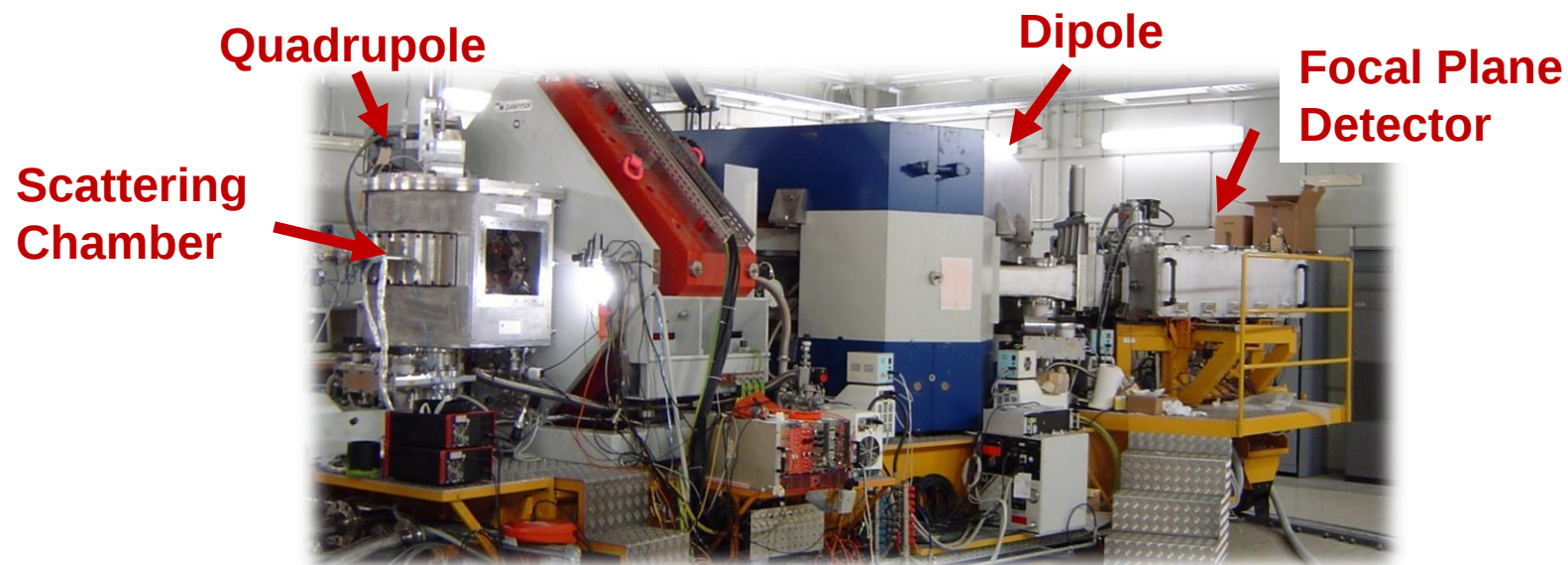
Crucial for the experimental challenges

K800 Superconducting Cyclotron

- In operation since 1996.
- Accelerates from H to U ions
- Maximum energy 80 MeV/u.



MAGNEX QD magnetic spectrometer



A **wide mass range** (from protons to medium-mass nuclei)

Optical characteristics	Current values	
Maximum magnetic rigidity (Tm)	1.8(*)	(*)presently being upgraded to 2.2 Tm
Angular acceptance (Solid angle) (msr)	50	
Momentum acceptance	-14%, +10%	
Momentum dispersion (cm/%)	3.68	

Measured resolutions:

- Energy $\Delta E/E \sim 1/1000$
- Angle $\Delta\theta \sim 0.2^\circ$
- Mass $\Delta m/m \sim 1/300$

F. Cappuzzello et al., Eur. Phys. J. A (2016) 52: 167
M. Cavallaro et al., NIM B 463 (2020) 334

The multichannel approach

Several scattering and reaction channels open in a heavy-ion collisions above Coulomb barrier

Although the main interest is for DCE reactions, all the other quasi-elastic processes are important sources of information, essential to **build a constrained analysis of the nuclear states of interest for DCE and $0\nu\beta\beta$**

Elastic scattering $\longrightarrow$ nucleus-nucleus optical potential

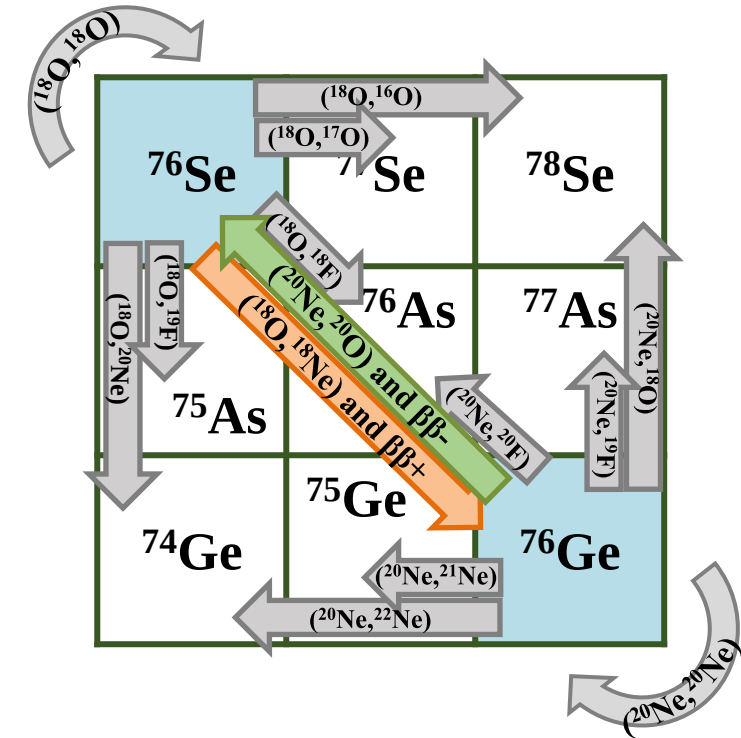
Inelastic scattering $\longrightarrow$ coupling strenght to low-lying states

One-nucleon transfer reactions $\longrightarrow$ single-particle spectroscopic amplitudes

Two-nucleon transfer reactions $\longrightarrow$ strenght of pairing correlations

Single charge exchange (**SCE**) $\longrightarrow$ nuclear response to 1st order isospin operators (One-Body Transition Densities)

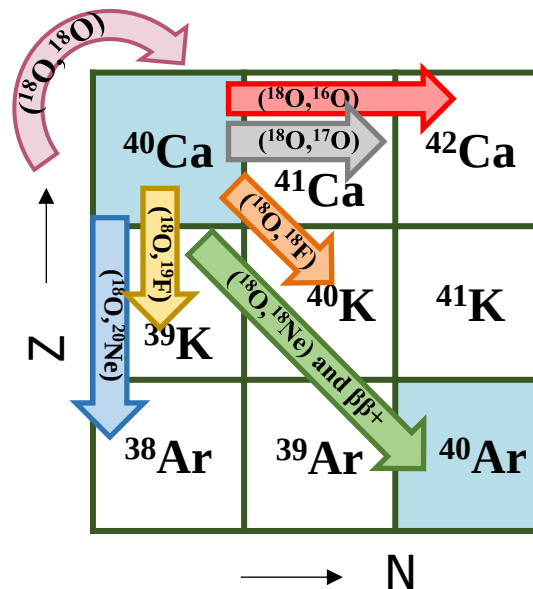
Double charge exchange (**DCE**) $\longrightarrow$ nuclear response to 2nd order isospin operators (Two-Body Transition Densities)



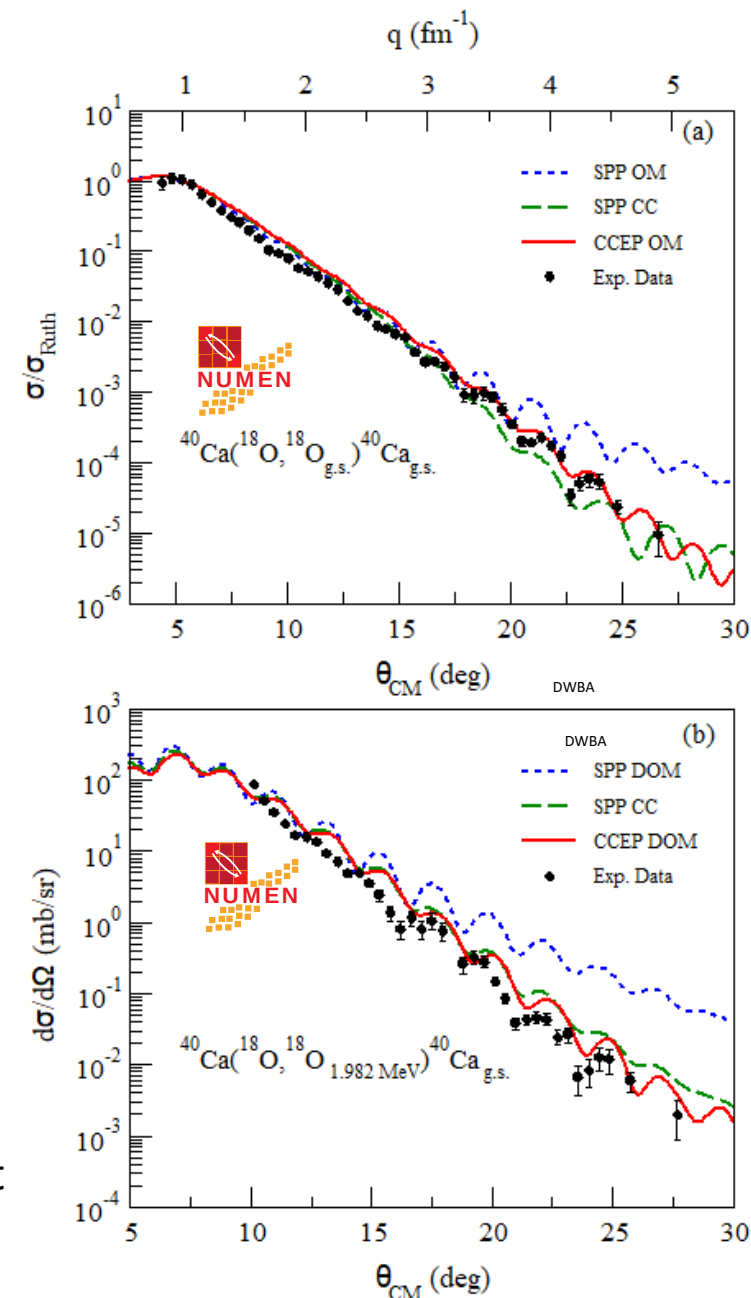
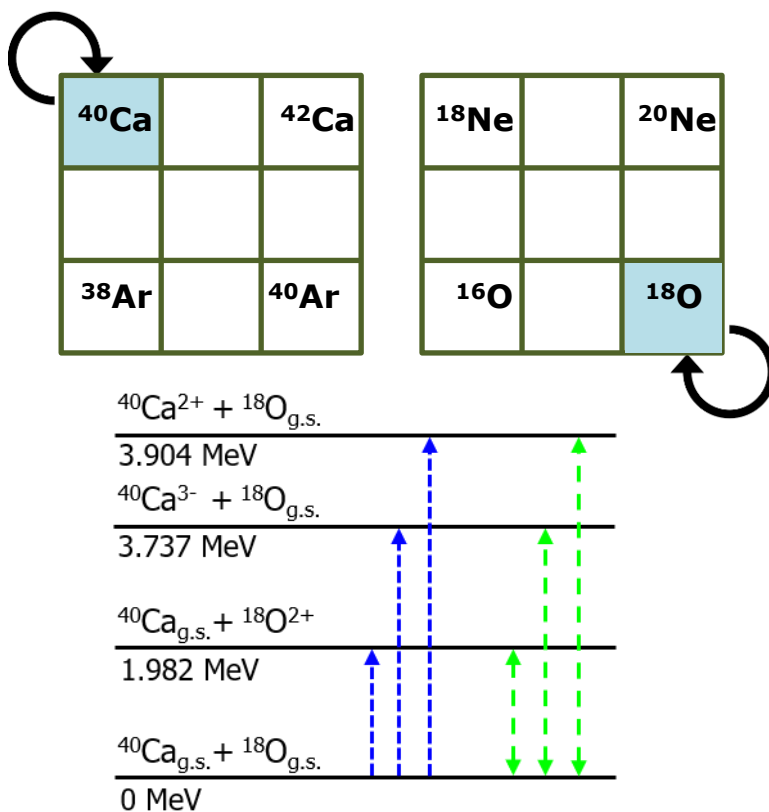
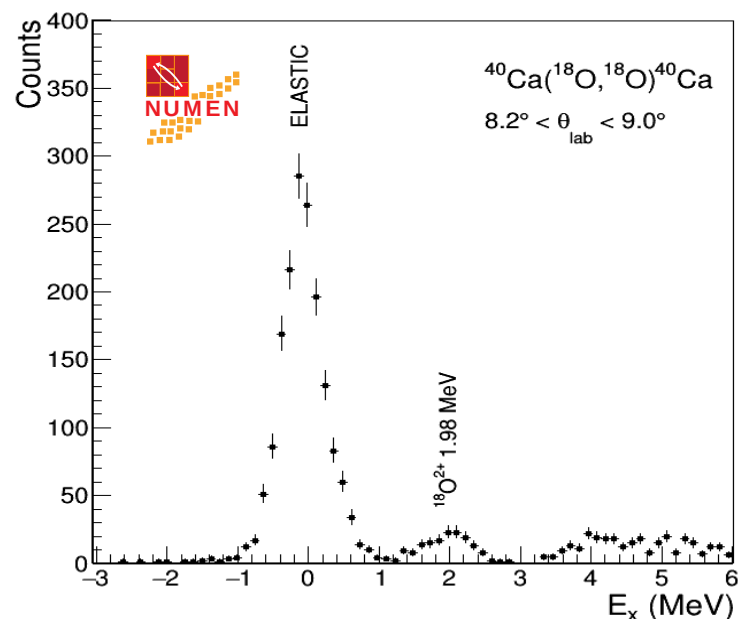
The multichannel approach

- Measuring all the accessible quasi-elastic channels **all at once** gives a **high reliability of the measured observables**, since systematic errors are largely cancelled, thanks to the many available cross checks in the data
- From the theory side, **constrained data analyses can be performed**, such as CC approaches, largely reducing the need of free parameters in both nuclear structure and reaction models

The $^{18}\text{O} + ^{40}\text{Ca}$ @ 275 MeV case



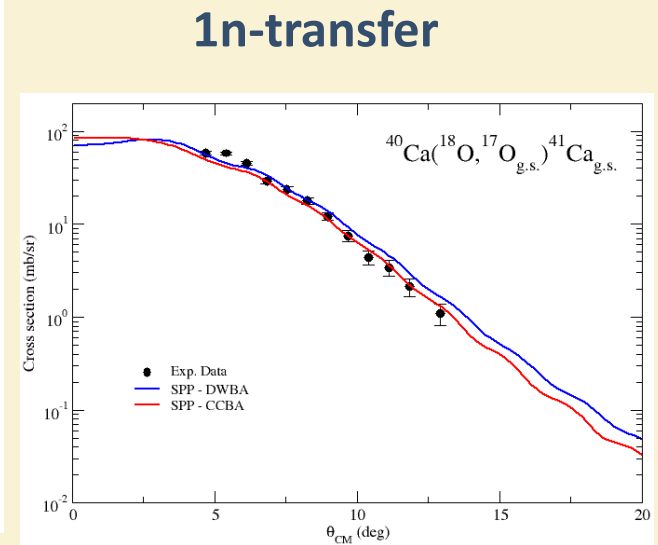
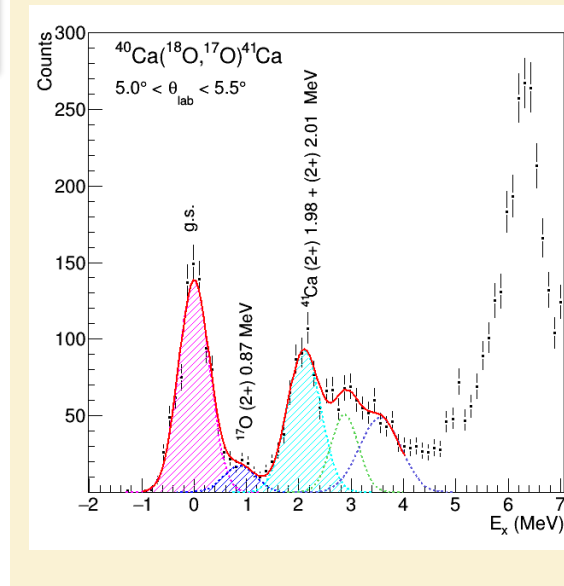
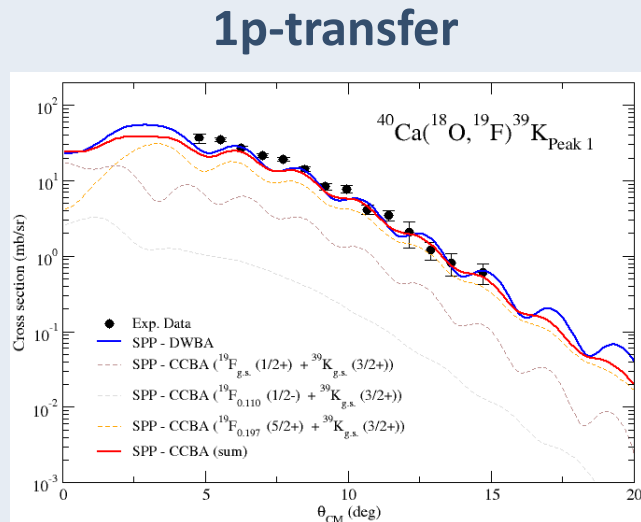
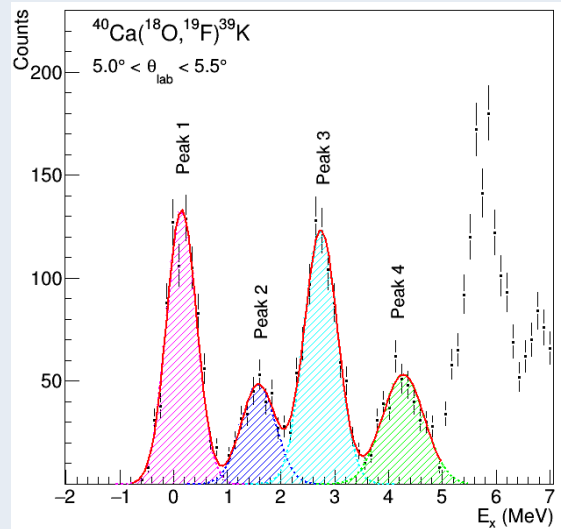
- ✓ F. Cappuzzello et al., EPJA 51, 145 (2015)
- ✓ M. Cavallaro et al., Front. Astr. Space Sci. (2021) 8:659815
- ✓ S. Calabrese et al., Phys. Rev. C (2021) 104, 064609
- ✓ J.L. Ferreira et al., Phys. Rev. C 103 (2021) 054604
- ✓ B.A. Urazbekov et al., PRC 108 (2023) 064609
- ✓ B.A. Urazbekov et al., PRC 111, 044603 (2025)
- ✓ J.L. Ferreira et al., PRC 111, 054609 (2025)



Key information from elastic and inelastic scattering data

- ✓ **Double folding** Sao Paulo Potential works well
- ✓ **Coupling to low-lying 2^+ and 3^- states** of ^{18}O and ^{40}Ca states is important
- ✓ Effects of coupling can be accounted for in average by Coupled Channel Equivalent Potential (**CCEP**) approach

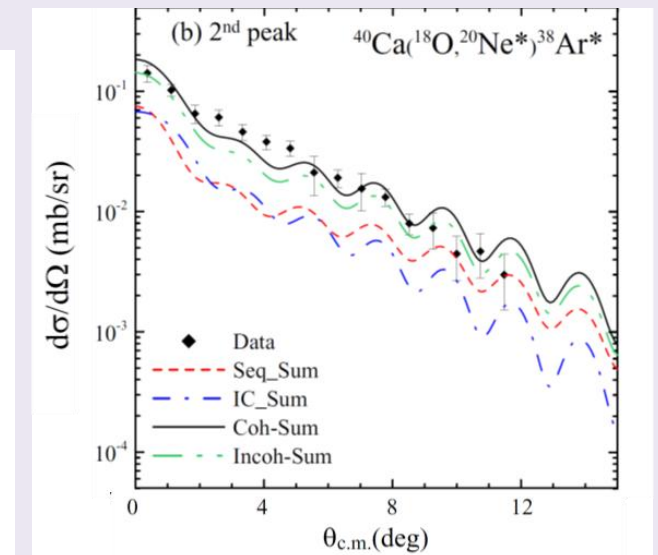
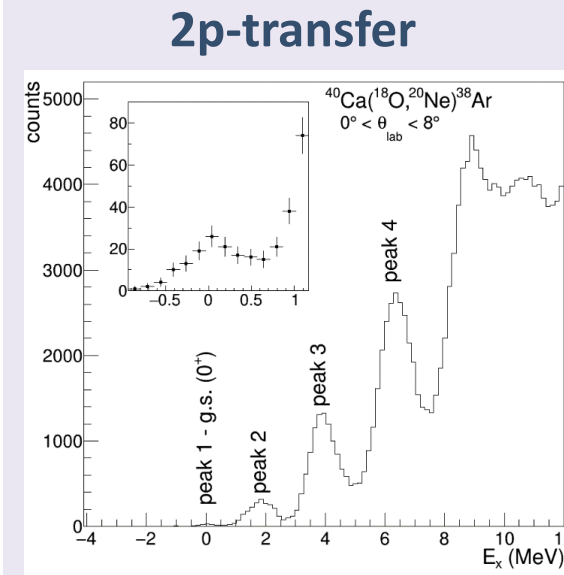
Transfer reactions



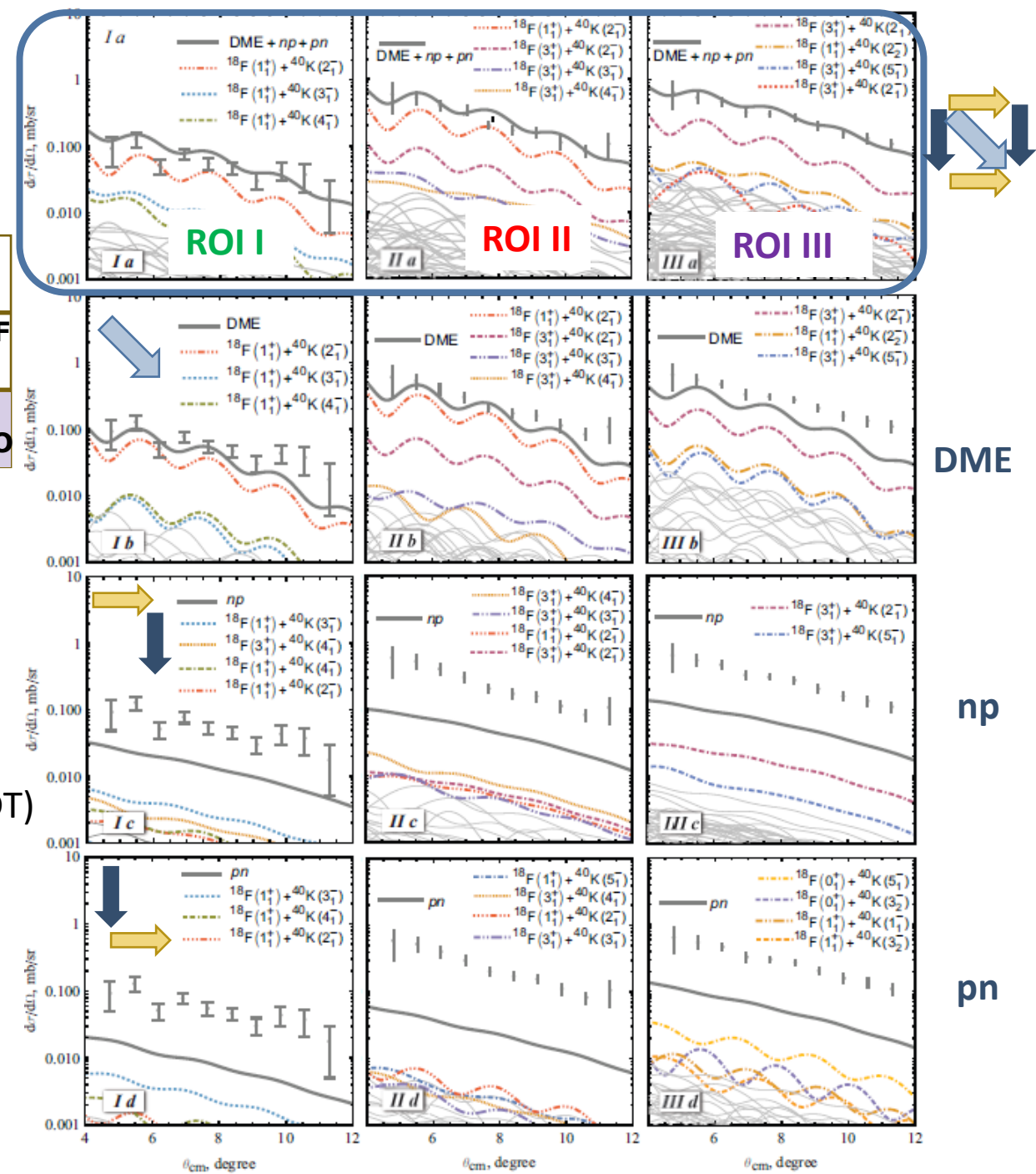
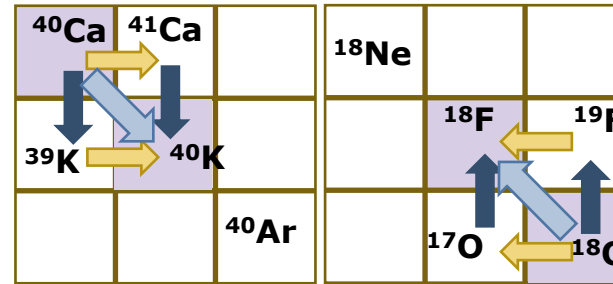
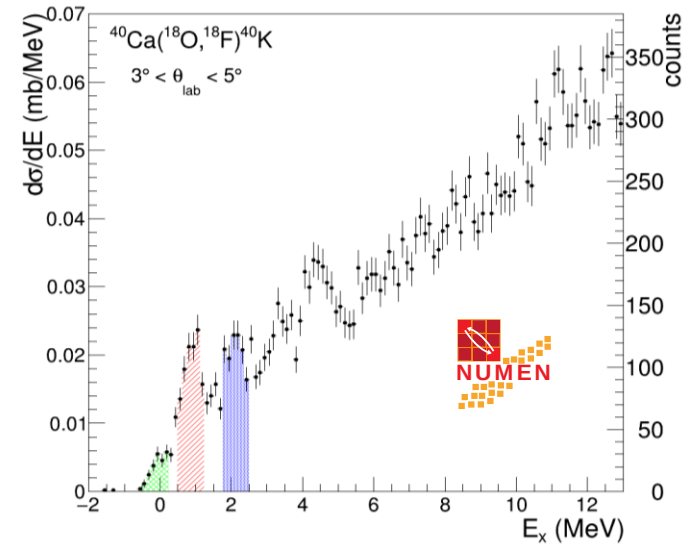
- OP extracted from elastic and inelastic scattering data
- **CCBA** analysis for direct and two-step transfer
- **Large scale shell model** spectroscopic amplitudes

Key information from transfer data

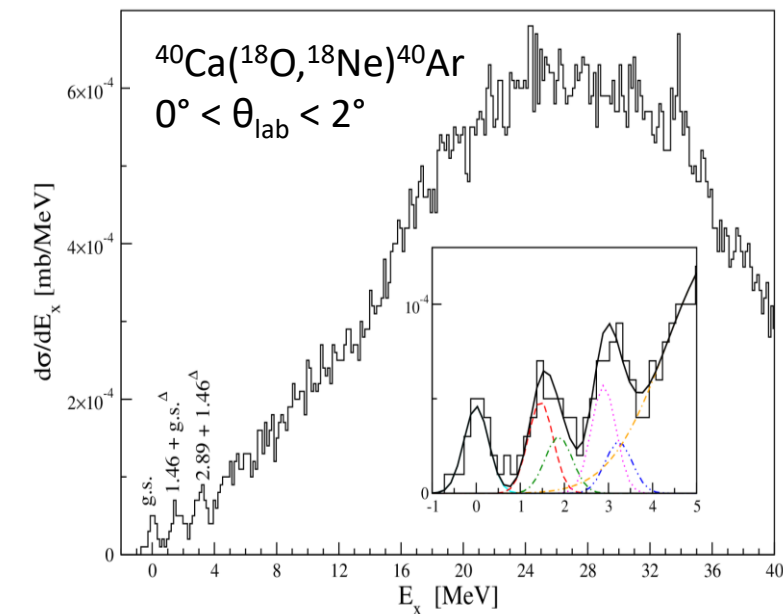
- ✓ Very good description of the data from constrained CCBA
- ✓ Mixing of single particle and core polarization configurations
- ✓ Competition between one-step and two-step mechanisms



Single charge exchange reaction



Double charge exchange reaction

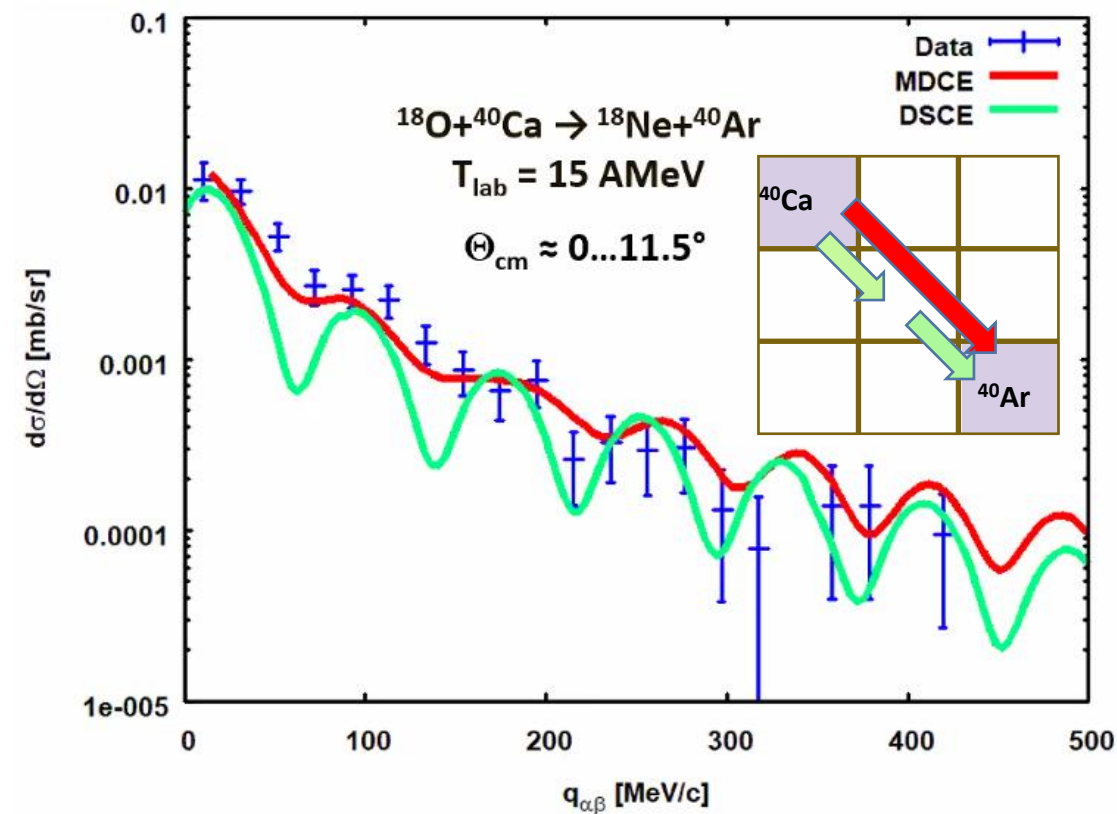


$$\sigma_{\text{g.s.} \rightarrow \text{g.s.}} = 35 \pm 2 \text{ nb}$$

- ISI and FSI ion-ion interaction from double folding (constrained by elastic and inelastic data)
- QRPA transition densities for microscopic form factors
- **One-step DWBA for MDCE** and **two-step DWBA for DSCE**

Caveat:

- Only $N\pi$ -correlations included
- Off-shell momentum structure approximated with on-shell component (T-matrix instead of G-matrix)



2-step DSCE: intermediate states with $J^\pi \leq 5^\pm$
 1-step MDCE: $^{40}\text{Ca}(0^+) \rightarrow ^{40}\text{Ar}([n^{-2}p^2]0^+)$: $J=0^+$ with $L=S=0$ & $[L=2 \times S=2]_{0^+}$

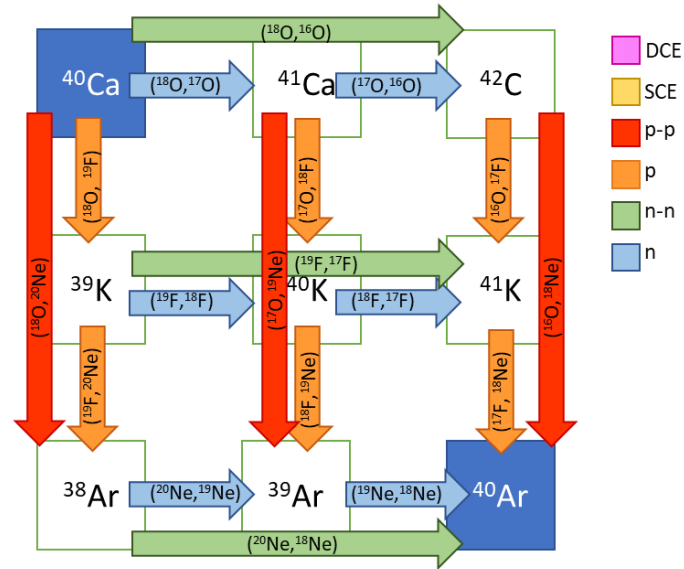
H. Lenske et al., Universe 10, 93 (2024)

Key information from DCE data

- ✓ G.s. to g.s. transition isolated
- ✓ Good description of the data

Double charge exchange reaction

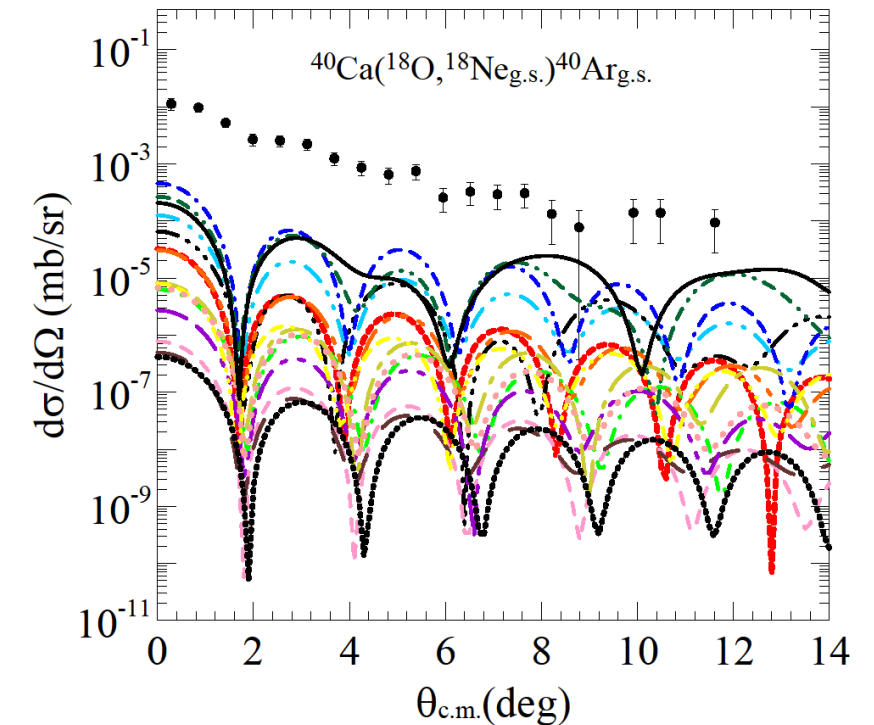
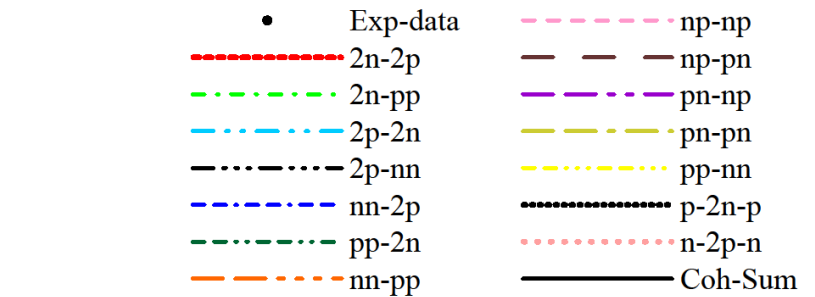
J.L. Ferreira et al., PRC 111, 014630 (2025)



The TDCE multi-nucleon transfer mechanisms

- ✓ ISI and FSI ion-ion interaction extracted from elastic and inelastic data
- ✓ Shell model amplitudes and deformations as for transfer calculations
- ✓ Four-step DWBA and CCBA calculations in large model spaces

TDCE contribution is negligible!



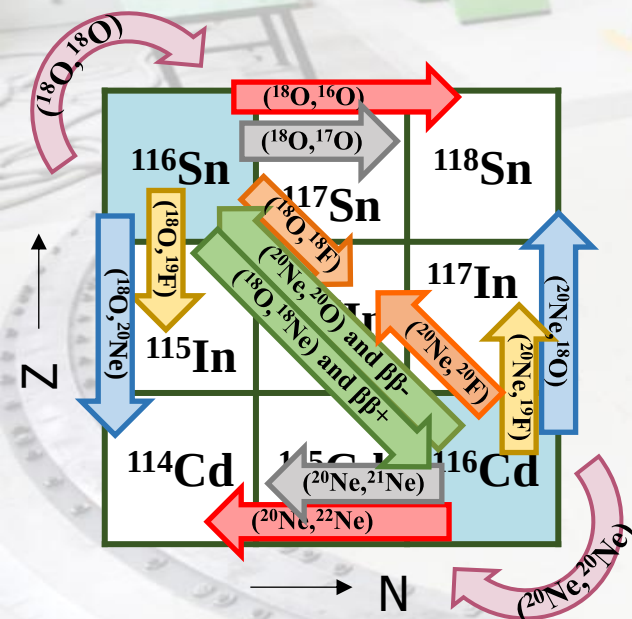
DCE on $0\nu\beta\beta$ candidates

NUMEN experimental runs

$^{116}\text{Cd} - ^{116}\text{Sn}$ case

@ 15 AMeV

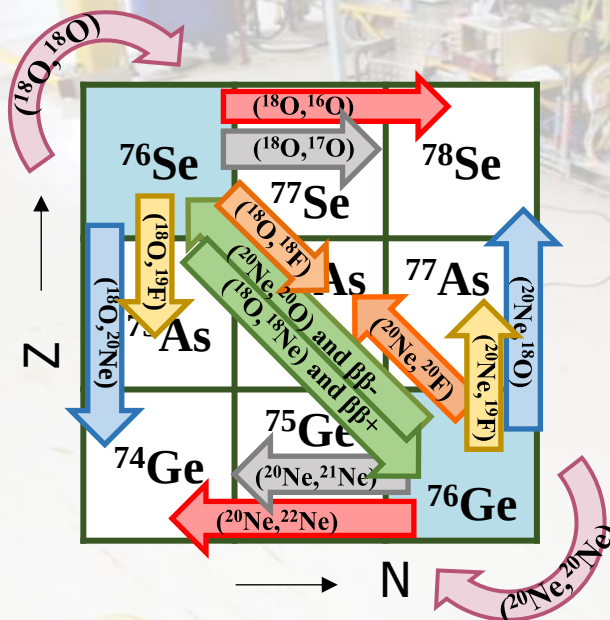
- $^{18}\text{O} + ^{116}\text{Sn}$
- $^{20}\text{Ne} + ^{116}\text{Cd}$



$^{76}\text{Ge} - ^{76}\text{Se}$ case

@ 15 AMeV

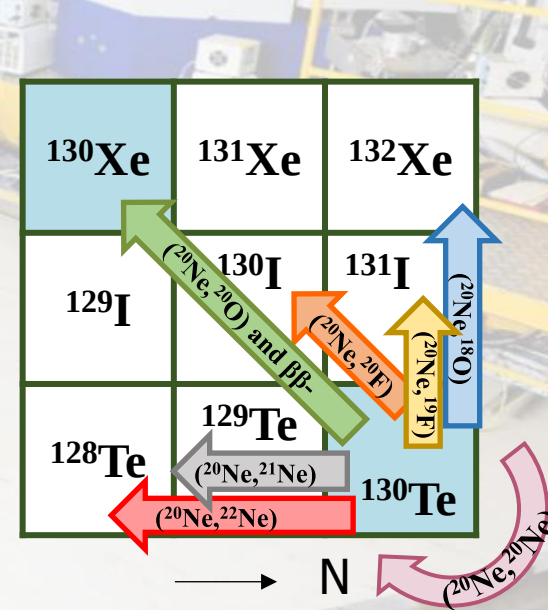
- $^{20}\text{Ne} + ^{76}\text{Ge}$
- $^{18}\text{O} + ^{76}\text{Se}$



$^{130}\text{Te} - ^{130}\text{Xe}$ case

@ 15 AMeV

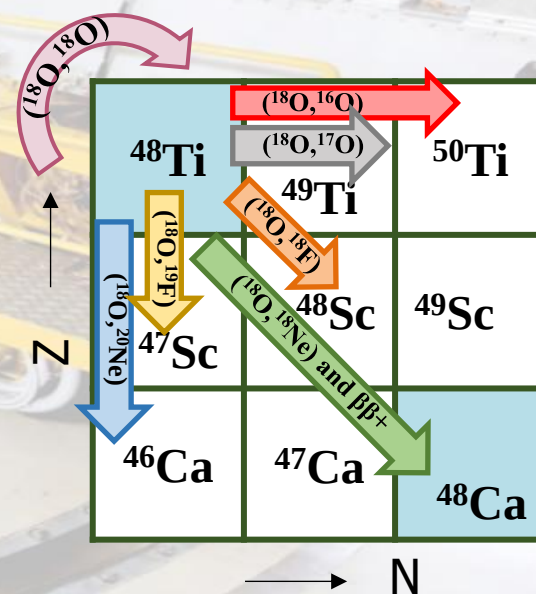
- $^{20}\text{Ne} + ^{130}\text{Te}$



$^{48}\text{Ca} - ^{48}\text{Ti}$ case

@ 15 AMeV

- $^{18}\text{O} + ^{48}\text{Ti}$

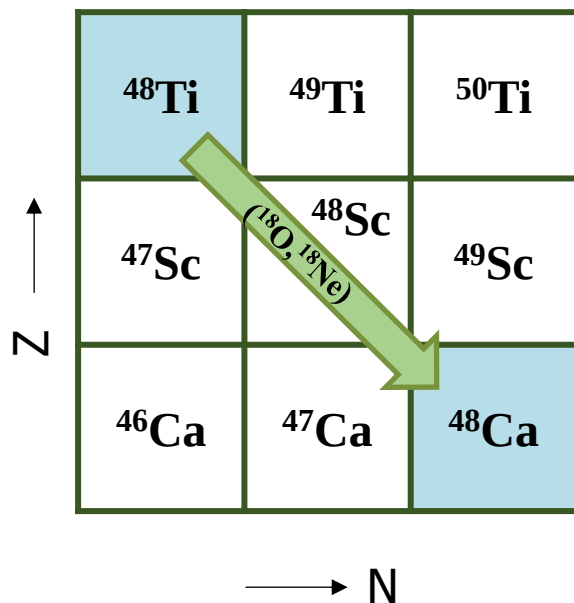


D. Carbone et al., PRC 102, 044606 (2020)
S. Calabrese et al., NIMA 980, 164500 (2020)
D. Carbone et al., Universe 07, 58 (2021)
S. Burrello et al. PRC 105, 024616 (2022)
J. Ferreira et al., PRC 105, 014630 (2022)
C.Eke et al. Res. In Phys. 67, 108037 (2024)

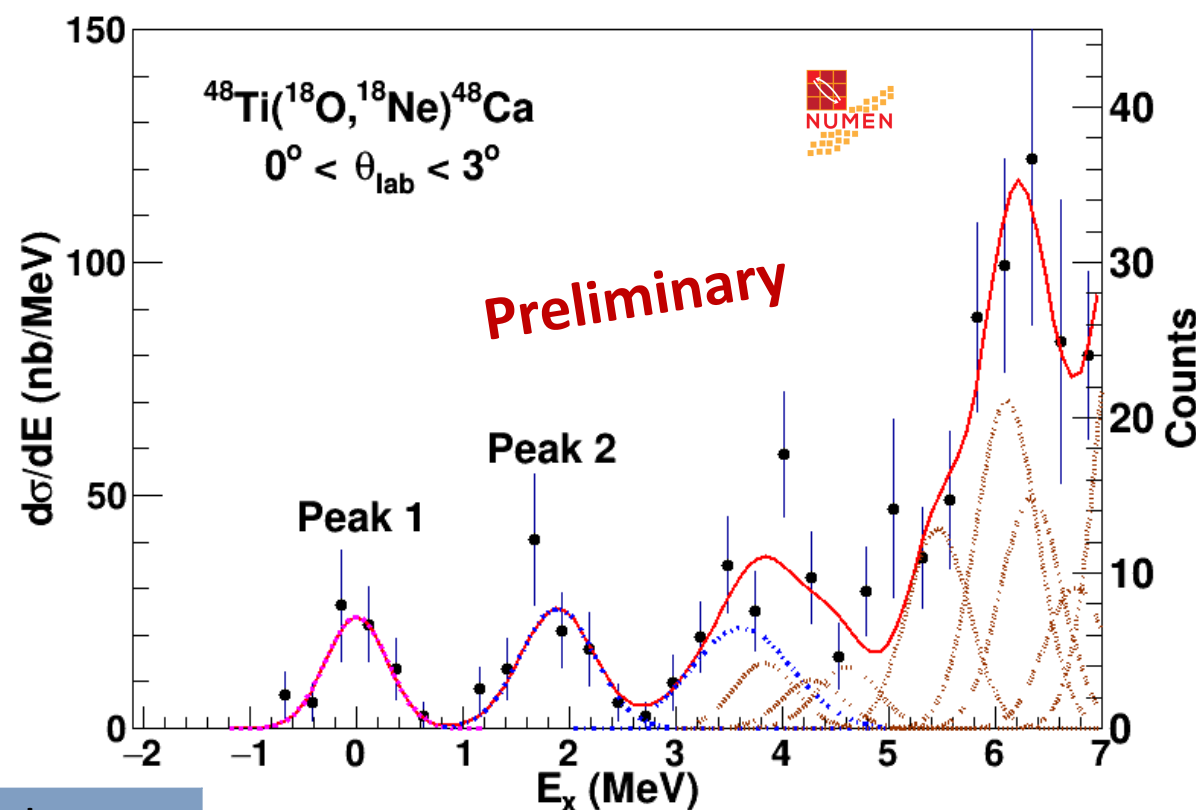
A. Spatafora et al., PRC 100, 034620 (2019)
L. La Fauci et al., PRC 104, 054610 (2021)
I. Cirialdo et al., PRC 105 (2022) 044607
I. Cirialdo et al., PRC 109, 024615 (2024)

M. Cavallaro et al., Res. Phys. 13, 102191 (2019)
V. Soukeras et al., Res. Phys. 28, 104691 (2021)
D. Carbone et al., Universe 07, 58 (2021)

O. Sgouros et al., PRC 104, 034617 (2021)
O.- Sgouros et al., PRC 108, 044611 (2023)
G.A. Brischetto et al., PRC 109, 014604 (2024)



DCE reaction $^{48}\text{Ti}(^{18}\text{O}, ^{18}\text{Ne})^{48}\text{Ca}$



State (MeV)	Counts	Absolute cross section (nb)
$^{48}\text{Ca}_{\text{gs}}(0^+) + ^{18}\text{Ne}_{\text{gs}}(0^+)$	24	20 ± 4
$^{48}\text{Ca}_{\text{gs}}(0^+) + ^{18}\text{Ne}_{1.89}(2^+)$	33	28 ± 5

- g.s. $\rightarrow$ g.s. transition isolated (resolution ~ 680 keV FWHM)
- Absolute cross section measured
- Zero-degree measurement

O. Sgouros et al.

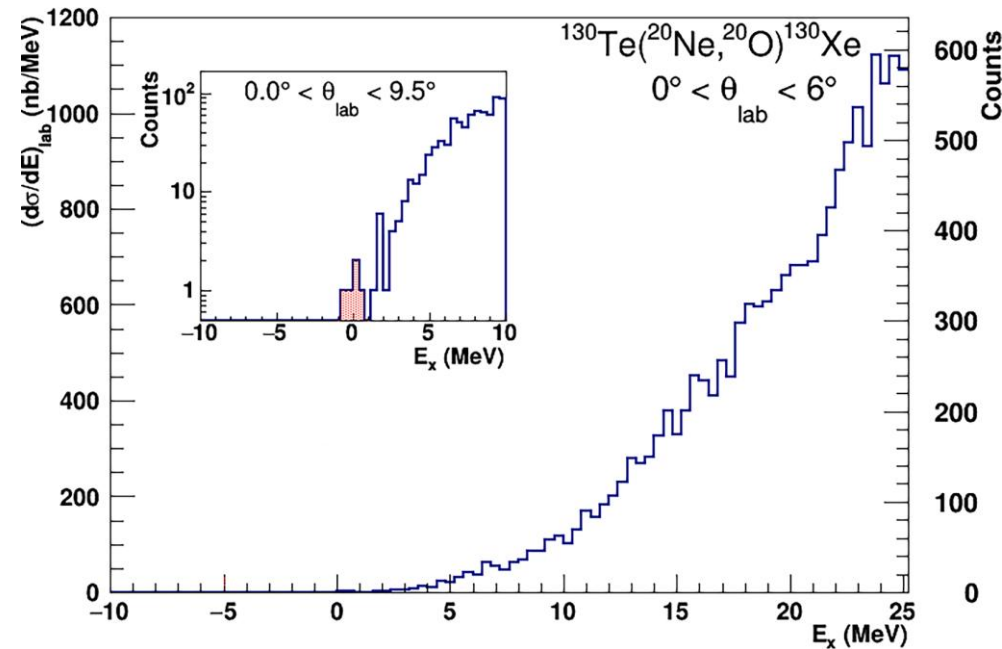
^{130}Xe	^{131}Xe	^{132}Xe
^{129}I	^{130}I	^{131}I
^{128}Te	^{129}Te	^{130}Te

($^{20}\text{Ne}, ^{20}\text{O}$) and $p\bar{p}$

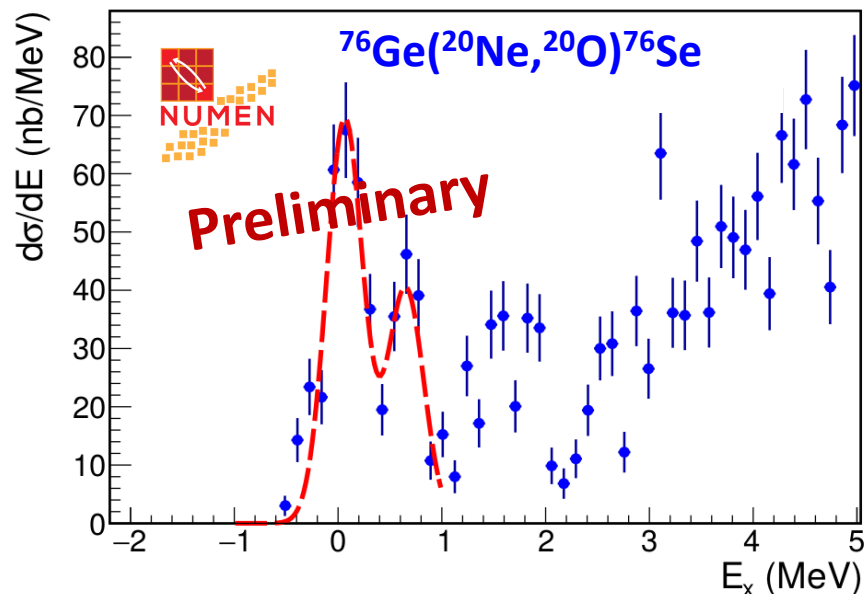
$^{130}\text{Te}(^{20}\text{Ne}, ^{20}\text{O})^{130}\text{Xe}$

- Resolution ~ 500 keV FWHM
- No spurious counts at $-10 < E_x < -2$ MeV

$\sigma_{-1 \text{ MeV} \rightarrow 1 \text{ MeV}} = \mathbf{13 \text{ nb}}$ ([3,18] nb at 95% CL)



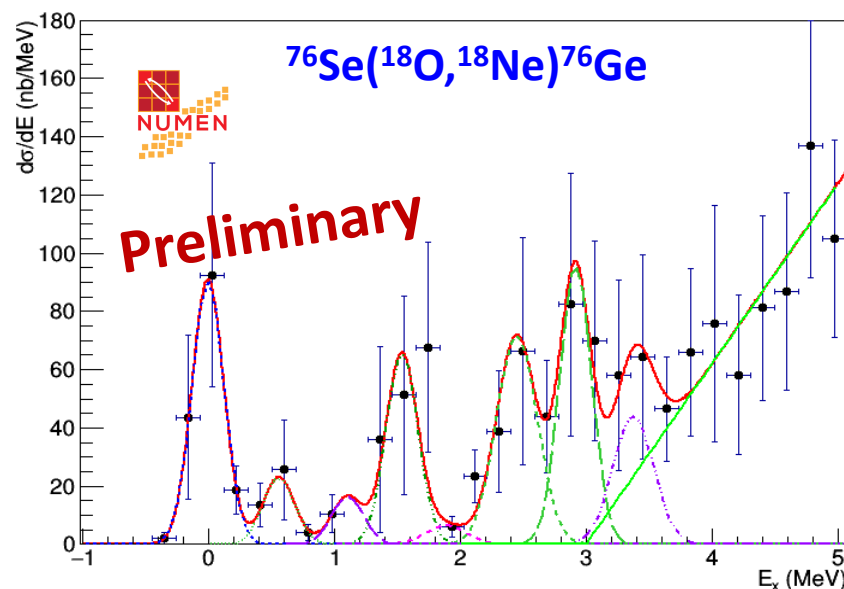
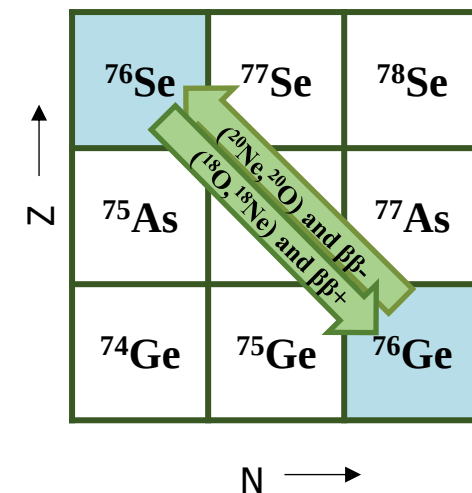
V. Soukeras et al., Results in Physics 28, 104691 (2021)



$$0^\circ < \theta_{\text{lab}} < 8^\circ$$

$$\sigma_{\text{g.s.} \rightarrow \text{g.s.}} = 30 \pm 4 \text{ nb}$$

- Same cross sections for different directions
 - Similar distortion factors
- Same NME (encouraging test of time invariance!)



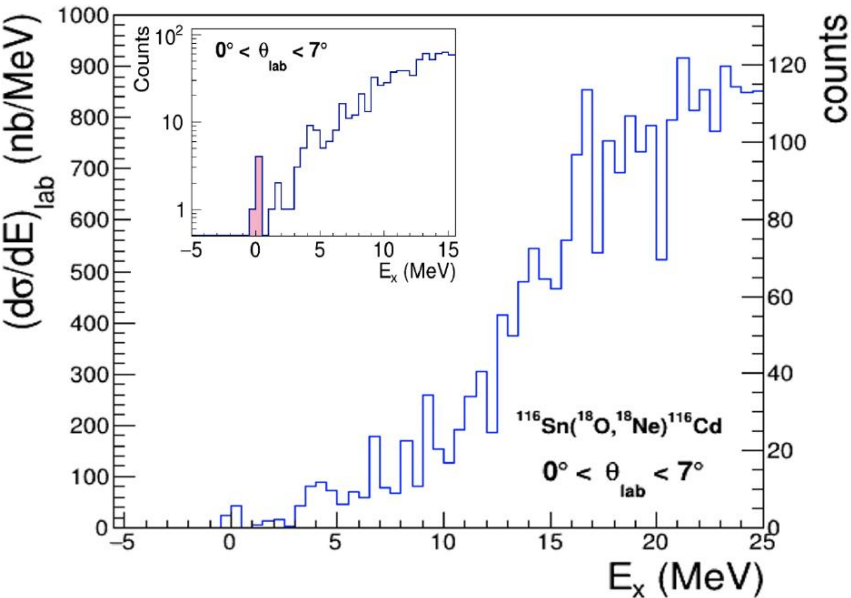
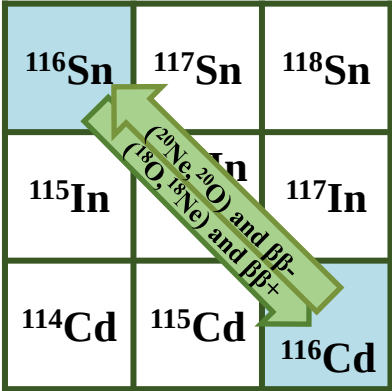
$$\sigma_{\text{g.s.} \rightarrow \text{g.s.}} = 29 \pm 6 \text{ nb}$$

Warning:

- Only one case?
- Reaction calculations in progress

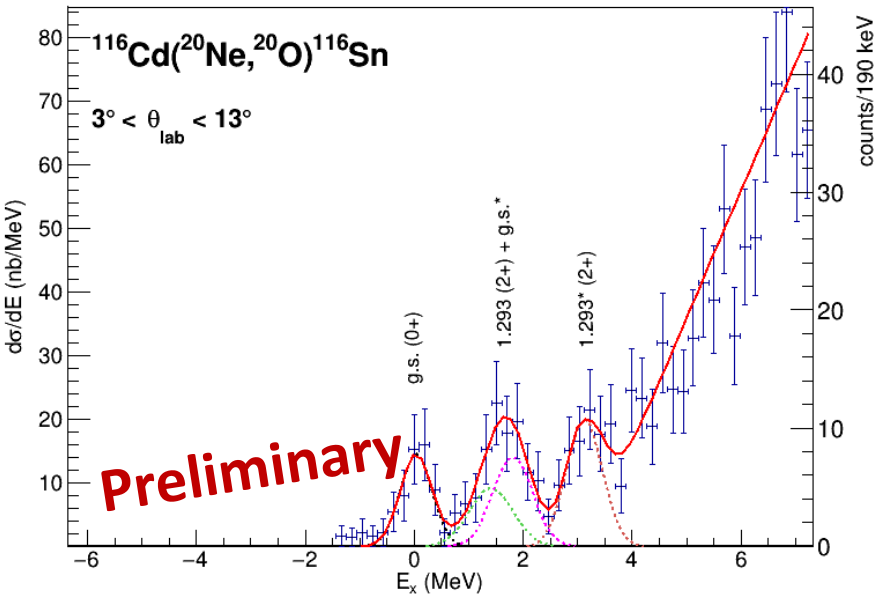
DCE experimental results

$^{116}\text{Cd} - ^{116}\text{Sn}$ case

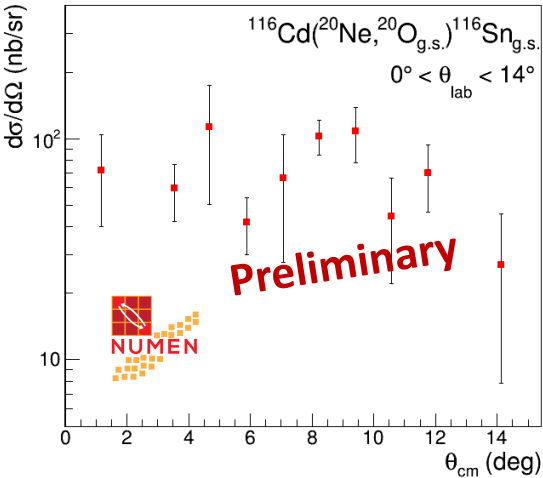


$$\sigma_{-1 \text{ MeV} \rightarrow 1 \text{ MeV}} = \mathbf{36 \text{ nb}} \text{ ([4,46] nb at 95\% CL)}$$

C. Eke et al. Res. In Phys. 67, 108037 (2024)



State (MeV)	Counts	Absolute cross section (nb)
$^{116}\text{Sn}_{\text{gs}}(0^+) + ^{20}\text{O}_{\text{gs}}(0^+)$	31	12 ± 2
$^{116}\text{Sn}_{1.293}(2^+) + ^{20}\text{O}_{\text{gs}}(0^+)$ $^{116}\text{Sn}_{\text{gs}}(0^+) + ^{20}\text{O}_{1.673}(2^+)$	67	24 ± 3

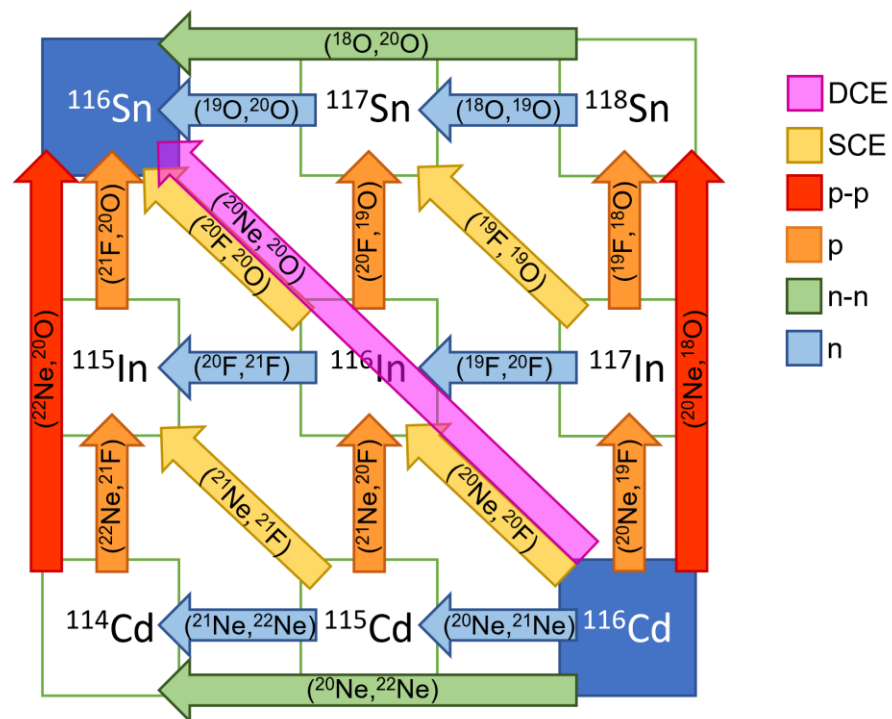


S. Calabrese et al., NIM A 980 (2020) 164500

Similar to the $^{76}\text{Ge} - ^{76}\text{Se}$ case

TDCE mechanism

- **DWBA** and **CRC calculations** of all the multi-nucleon transfer routes competing with meson-exchange processes.
- Coherent (and constrained) approach



J. Ferreira et al., Phys. Rev. C 105, 014630 (2022)

Mechanism	Int. cross section (nb)
	$^{20}\text{O}_{\text{g.s.}}(0^+) + ^{116}\text{Sn}_{\text{g.s.}}(0^+)$
$2p - 2n$	$1,28 \times 10^{-4}$
$2n - 2p$	$3,13 \times 10^{-4}$
$p - p - n - n$	$6,63 \times 10^{-5}$
$n - n - p - p$	$1,00 \times 10^{-5}$
$p - p - 2n$	$4,15 \times 10^{-5}$
$n - n - 2p$	$1,72 \times 10^{-6}$
$2p - n - n$	$9,26 \times 10^{-5}$
$2n - p - p$	$2,66 \times 10^{-4}$
$p - n - p - n$	$1,38 \times 10^{-7}$
$p - n - n - p$	$1,15 \times 10^{-6}$
$n - p - n - p$	$2,53 \times 10^{-7}$
$n - p - p - n$	$1,69 \times 10^{-7}$
$p - 2n - p$	$2,51 \times 10^{-7}$
$n - 2p - n$	$5,71 \times 10^{-6}$

Incoh. Sum 9.60×10^{-4}

Exp. DCE cross section $12 \pm 2 \text{ nb}$

Negligible contribution of TDCE on the diagonal DCE process

Present limitations and perspectives

DCE reactions are characterized by very **low cross-sections**

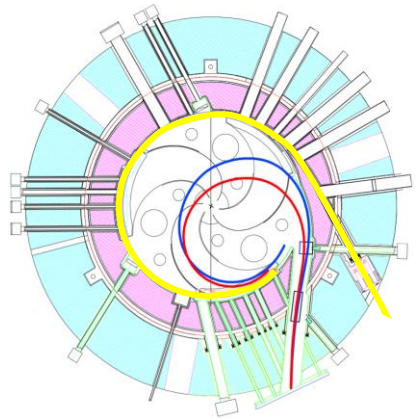


In the last years NUMEN studied only few systems

Much higher beam current is needed



Project of **upgrade of the LNS Cyclotron (from 100 W to 5-10 kW) and infrastructures** (triggered by NUMEN physics case) funded by national grant (PON)

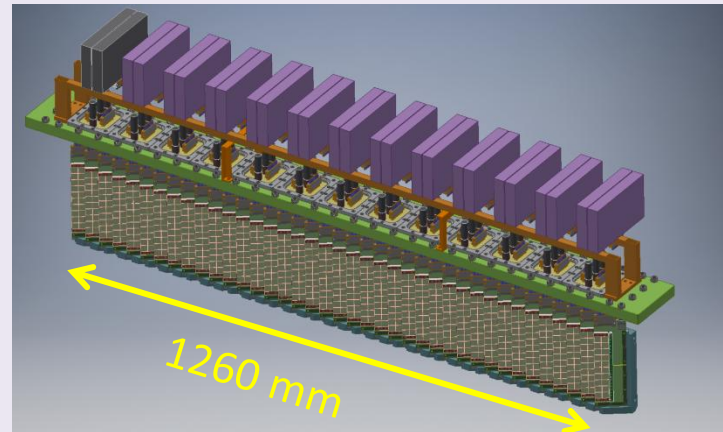


CS extraction by stripping

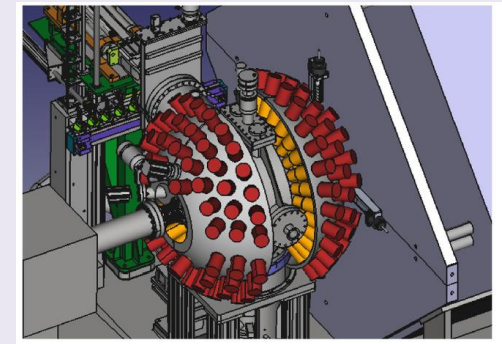
NUMEN TDR *F. Cappuzzello et al., Intern. Journ. of Mod. Phys. A 36 (2021) 2130018*



New tracker for the FPD
(**THGEM** technology)



New PID-wall for the FPD
(720 **SiC + CsI** telescopes)



New gamma-ray calorimeter
(110 **LaBr3** scintillators)

Conclusions and Outlooks

Use of HI-DCE reaction for $0\nu\beta\beta$ decay

- Second order isospin excitations of nuclei bridge the gap between nuclear and neutrino physics
- Heavy-ion DCE reactions can significantly contribute to this research field, providing that nuclear structure and reaction aspects are accurately and consistently addressed
- Multichannel approach for the data analysis
- **DCE reactions on ^{116}Cd , ^{76}Ge , ^{76}Se , ^{130}Te and ^{116}Sn measured for the first time**
 - ✓ Good energy resolution to isolate the g.s. $\rightarrow$ g.s. transition
 - ✓ Absolute cross section measured
- Role of **multi-nucleon transfer** routes **negligible** with respect to the diagonal DCE

Outlooks

- **MAGNEX FPD @ iThemba LABS**
- New measurements at iThemba LABS on $^{18}\text{O} + ^{76}\text{Se}$



- CS and MAGNEX FPD **upgrade** ongoing for reaching high intensity
- Extensive exploration of all the nuclei candidate for $0\nu\beta\beta$ decay with the **high intensity beams**

The NUMEN collaboration

(NUclear Matrix Elements for Neutrinoless double beta decay)



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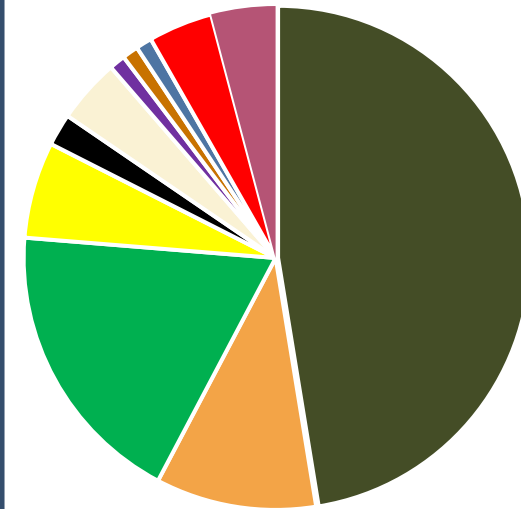
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