

Hunting for New physics in Large Scale Structure of the Universe

Salvatore Bottaro



Let there be (light) particles Workshop - IBS-CTPU-PTC, Daejeon, Korea, 4/12/2024

The relevance of LSS today...

Parameter	TT+lowE 68% limits	TE+lowE 68% limits	EE+lowE 68% limits	TT,TE,EE+lowE 68% limits	TT,TE,EE+lowE+lensing 68% limits	TT,TE,EE+lowE+lensing+BAO 68% limits
$\Omega_b h^2$	0.02212 ± 0.00022	0.02249 ± 0.00025	0.0240 ± 0.0012	0.02236 ± 0.00015	0.02237 ± 0.00015	0.02242 ± 0.00014
$\Omega_c h^2$	0.1206 ± 0.0021	0.1177 ± 0.0020	0.1158 ± 0.0046	0.1202 ± 0.0014	0.1200 ± 0.0012	0.11933 ± 0.00091
$100\theta_{\text{MC}}$	1.04077 ± 0.00047	1.04139 ± 0.00049	1.03999 ± 0.00089	1.04090 ± 0.00031	1.04092 ± 0.00031	1.04101 ± 0.00029
τ	0.0522 ± 0.0080	0.0496 ± 0.0085	0.0527 ± 0.0090	$0.0544^{+0.0070}_{-0.0081}$	0.0544 ± 0.0073	0.0561 ± 0.0071
$\ln(10^{10} A_s)$	3.040 ± 0.016	$3.018^{+0.020}_{-0.018}$	3.052 ± 0.022	3.045 ± 0.016	3.044 ± 0.014	3.047 ± 0.014
n_s	0.9626 ± 0.0057	0.967 ± 0.011	0.980 ± 0.015	0.9649 ± 0.0044	0.9649 ± 0.0042	0.9665 ± 0.0038
H_0 [km s ⁻¹ Mpc ⁻¹] . .	66.88 ± 0.92	68.44 ± 0.91	69.9 ± 2.7	67.27 ± 0.60	67.36 ± 0.54	67.66 ± 0.42
Ω_Λ	0.679 ± 0.013	0.699 ± 0.012	$0.711^{+0.033}_{-0.026}$	0.6834 ± 0.0084	0.6847 ± 0.0073	0.6889 ± 0.0056
Ω_m	0.321 ± 0.013	0.301 ± 0.012	$0.289^{+0.026}_{-0.033}$	0.3166 ± 0.0084	0.3153 ± 0.0073	0.3111 ± 0.0056

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CMB already measures the cosmological parameters
at the sub percent level

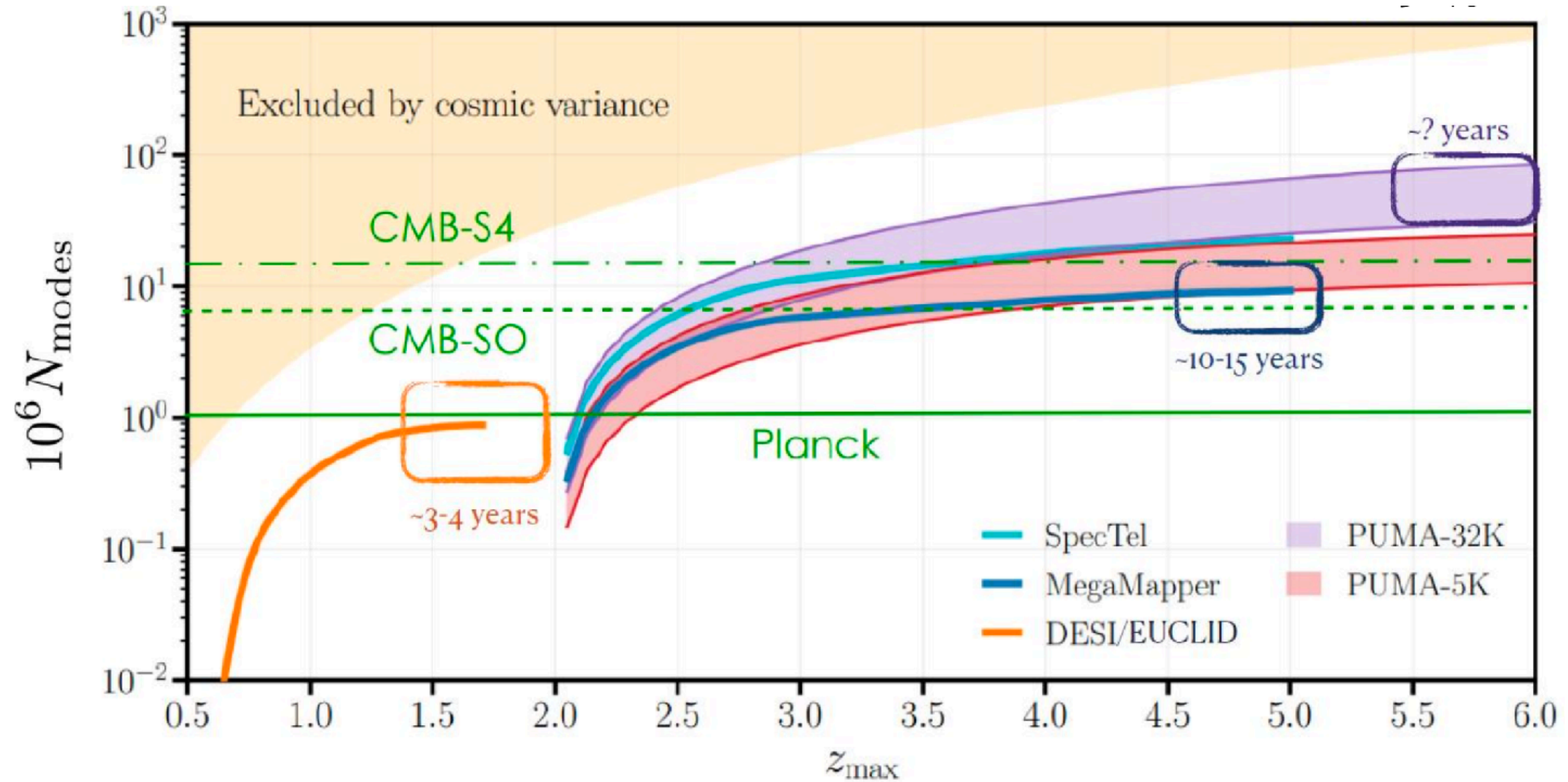
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Information from matter power spectrum
breaks degeneracies

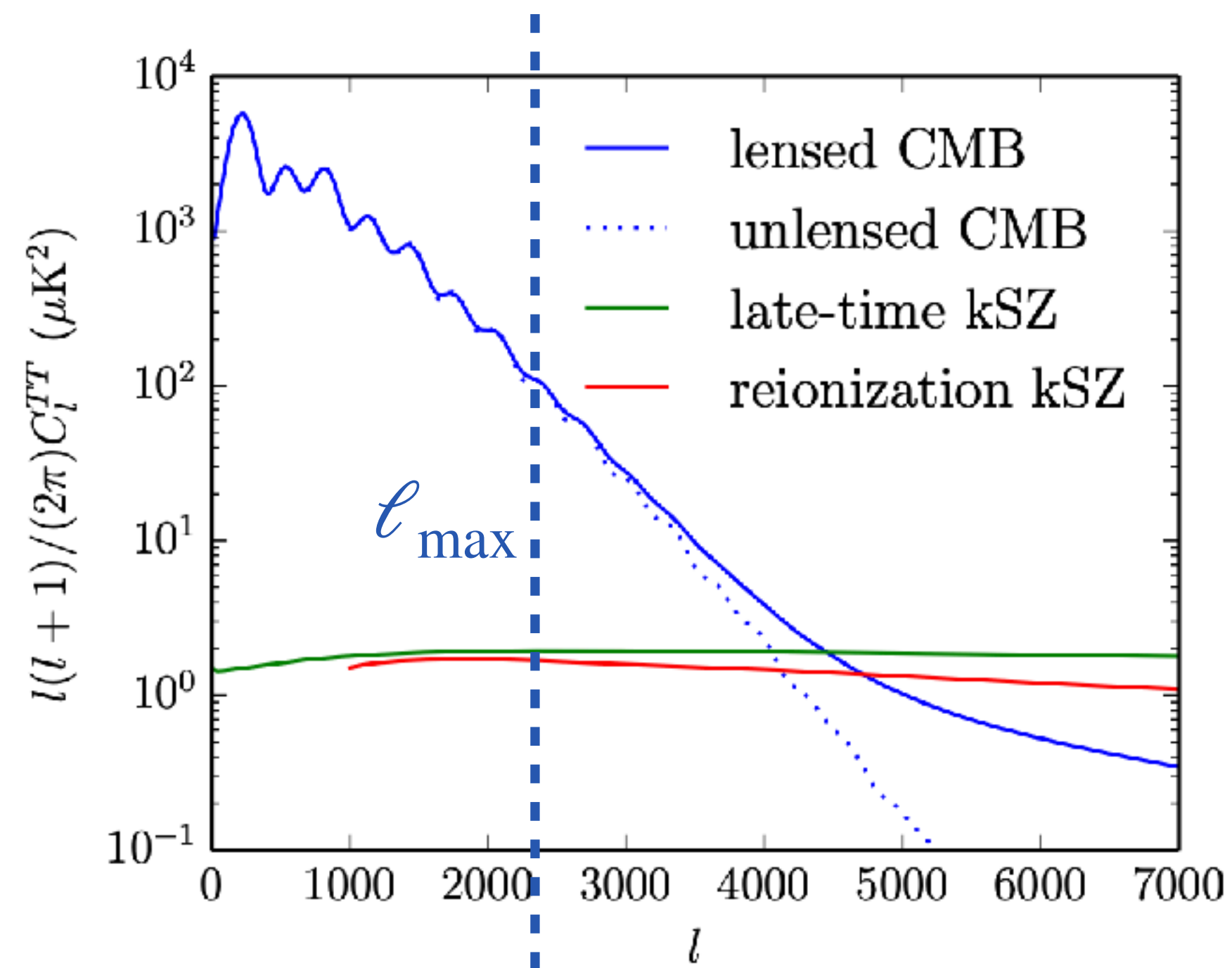
... and in the (very) near future!



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CMB is a 2D surface

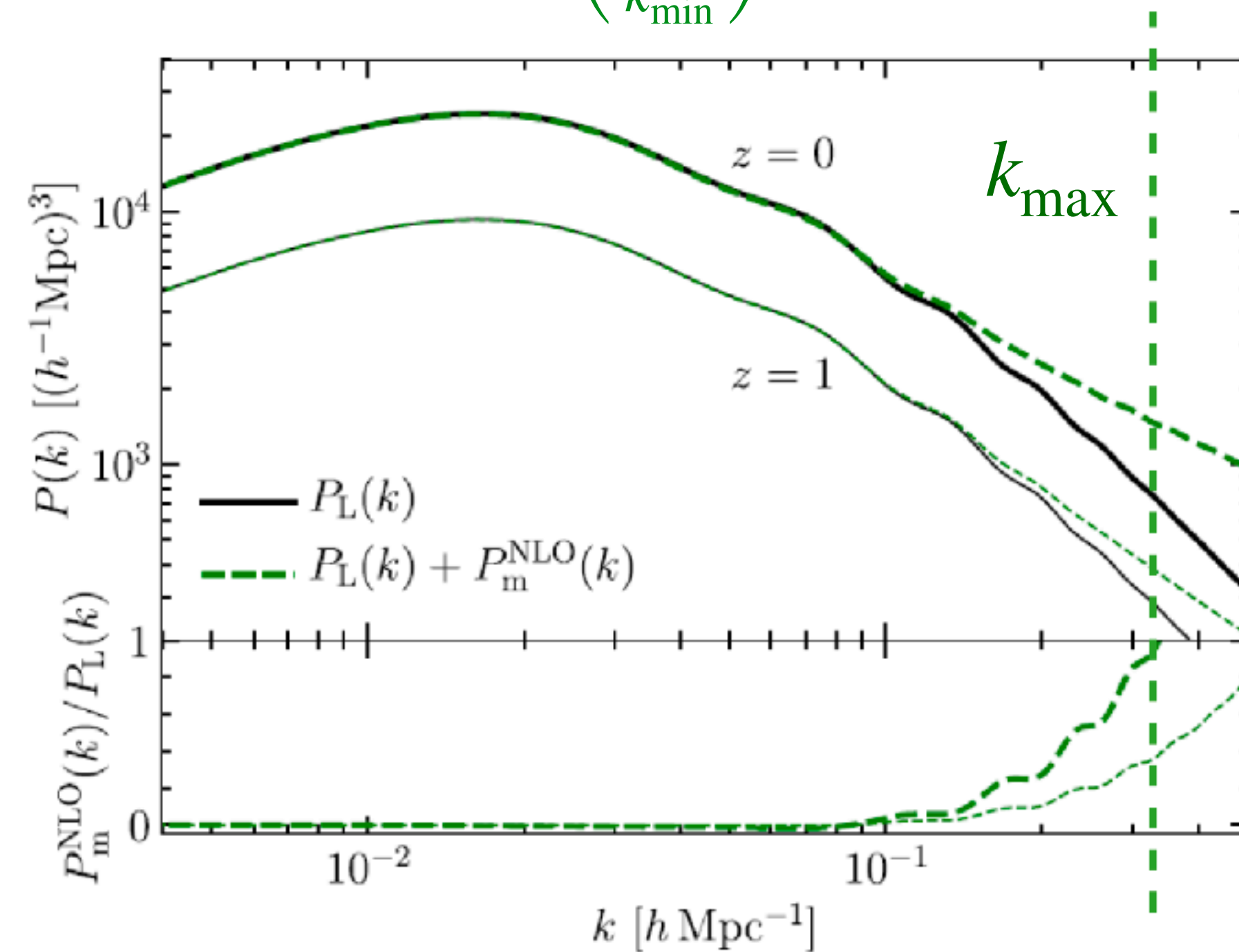
$$N_{\text{modes}}^{\text{CMB}} \approx \ell_{\text{max}}^2 \approx (2200)^2$$



Limited by small-scale
fluctuations

LSS probes a 3D volume

$$N_{\text{modes}}^{\text{LSS}} \approx \left(\frac{k_{\text{max}}}{k_{\text{min}}} \right)^3 \leq 10^9$$



Limited by convergence of
perturbative series

From theory to observations

Theory predicts $\delta_m = \frac{\delta\rho_m}{\bar{\rho}_m}$

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We observe galaxies $\delta_g = \frac{\delta n_g}{\bar{n}_g} = b_1\delta_m + \frac{b_2}{2}\delta_m^2 + b_K K_{ij}K^{ij} + \dots$

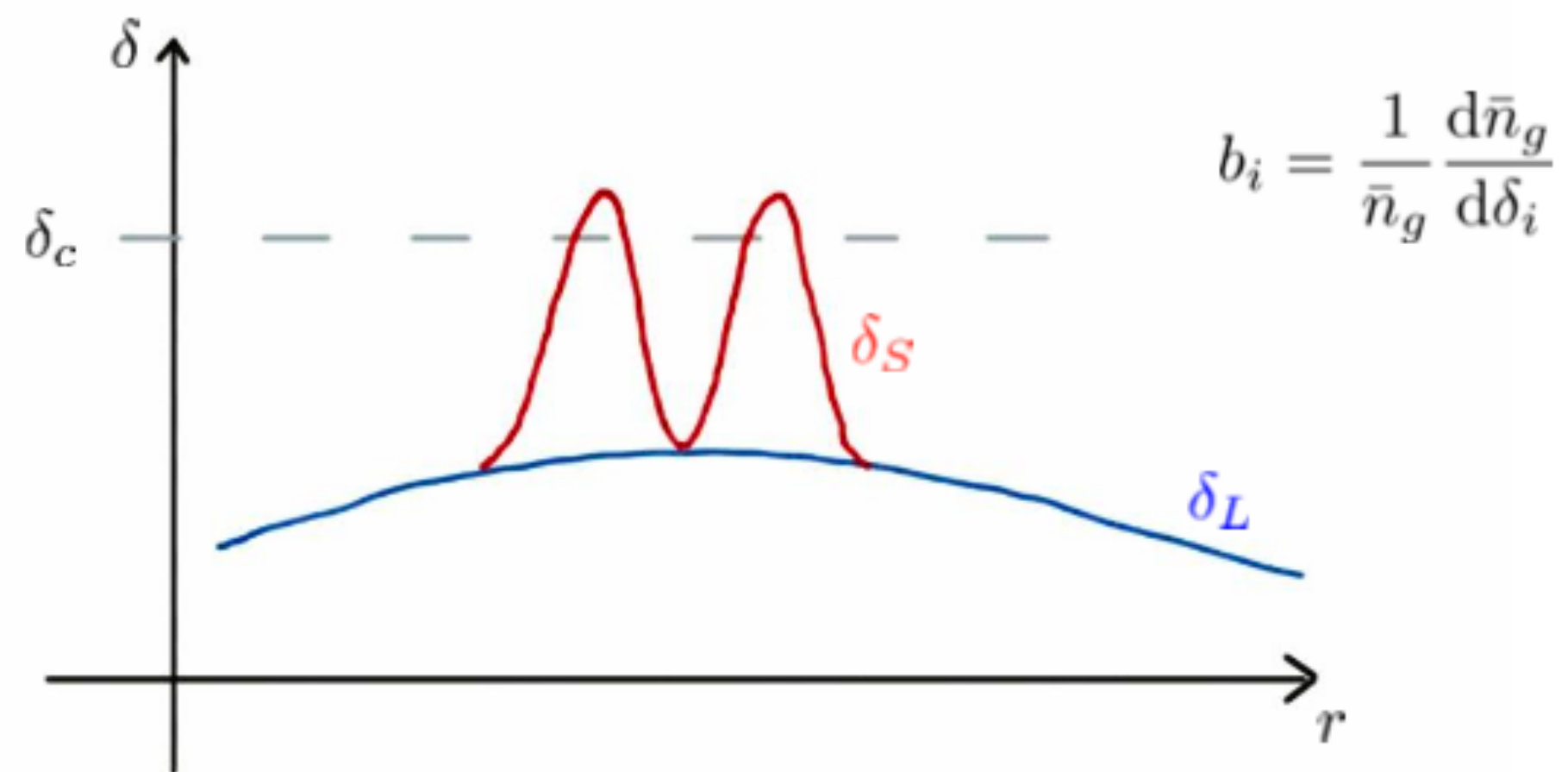
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Bias expansion



Long-range fluctuations
affect collapse

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Galaxies have proper motion $\delta_g^{\text{RSD}}(\vec{k}) = (b_1 + f\mu_k^2)\delta_m(\vec{k}) + \dots$

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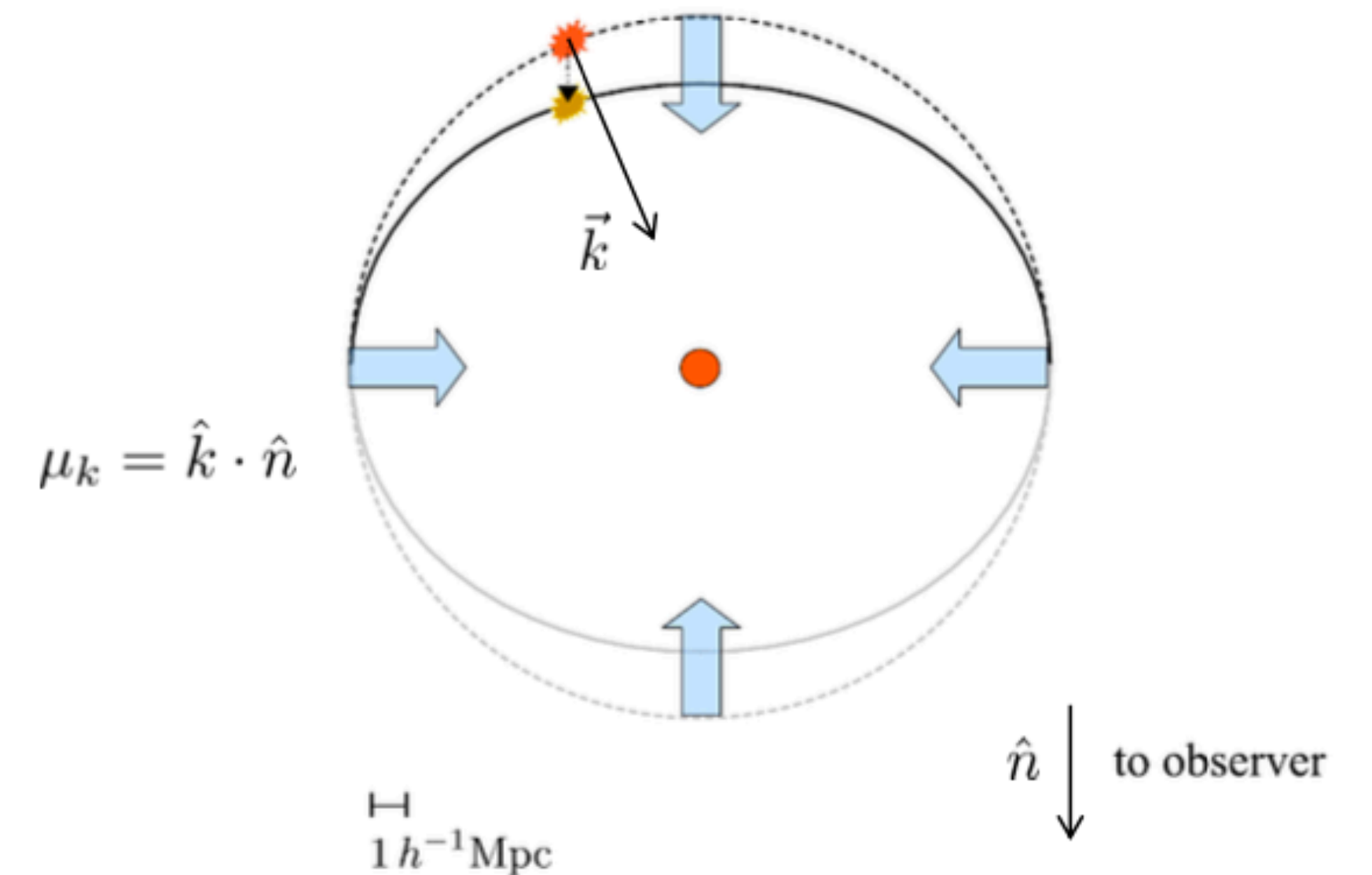
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Redshift-space distortions



From theory to observations

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We measure correlation functions of δ_g^{RSD} $\left\{ \begin{array}{l} \langle \delta_g^{\text{RSD}}(\vec{k}_1)\delta_g^{\text{RSD}}(\vec{k}_2) \rangle = (2\pi)^3\delta^{(3)}(\vec{k}_1 + \vec{k}_2)P_g^{\text{RSD}}(k_1) \\ \dots \end{array} \right.$

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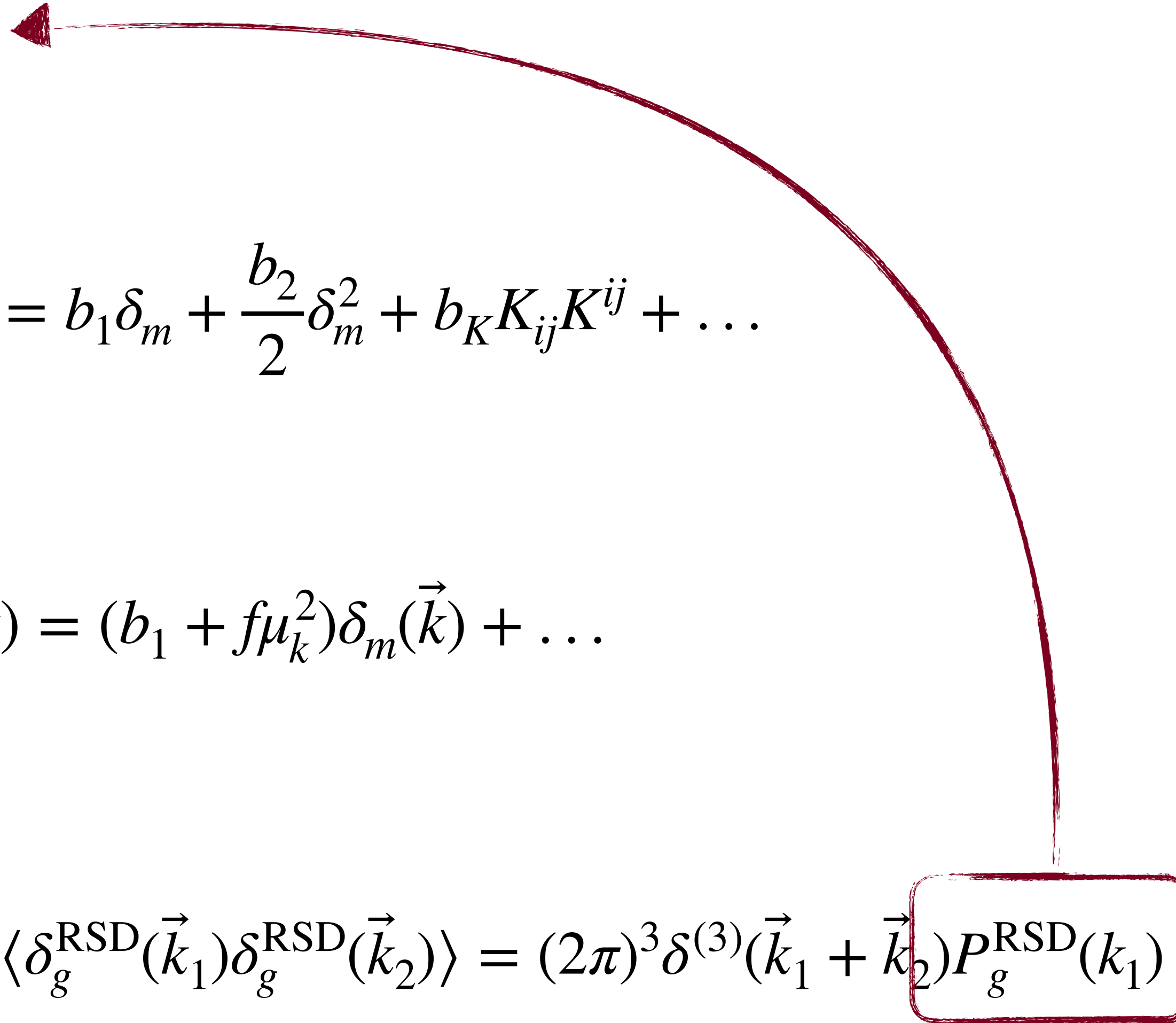
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How to make precise predictions?

$$\begin{array}{l} \text{Continuity} \\ \text{Euler} \end{array} \left\{ \begin{array}{l} \delta'_m + \theta_m + \vec{\nabla}(\delta_m \vec{v}_m) = 0, \quad \theta_m = \vec{\nabla} \vec{v}_m \\ \theta'_m + \mathcal{H} \theta_m + \frac{3}{2} \mathcal{H}^2 \delta_m + \partial_i (v_m^j \partial_j v_m^i) = 0 \end{array} \right.$$

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Solved iteratively, order by order

$$\delta_m(a, \vec{k}) = D_m(a) \delta_0(\vec{k}) + \sum_{n=2}^{\infty} D_m^n(a) \int \prod_{i=1}^n \frac{d^3 k_i}{(2\pi)^3} \delta_0(\vec{k}_i) \delta^{(3)} \left(\vec{k} + \sum_{i=1}^n \vec{k}_i \right) F_n(\vec{k}_1, \dots, \vec{k}_n)$$

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Linear growth
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$$\begin{array}{l} \text{Continuity} \\ \text{Euler} \end{array} \left\{ \begin{array}{l} \delta'_m + \theta_m + \vec{\nabla} \cdot (\delta_m \vec{v}_m) = 0, \quad \theta_m = \vec{\nabla} \cdot \vec{v}_m \\ \theta'_m + \mathcal{H} \theta_m + \frac{3}{2} \mathcal{H}^2 \delta_m + \partial_i (v_m^j \partial_j v_m^i) = 0 \end{array} \right.$$



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Initial
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Non-linear
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Compute correlation functions at any order

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Compute correlation functions at any order \longrightarrow Wrong predictions!

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Wrong model!

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DM is not collisionless at small scales!

$$\partial_i \partial_j \tau_{\text{eff}}^{ij} = c_s^2 \nabla^2 \delta_m + \dots$$

Encodes short-scale backreaction on long modes

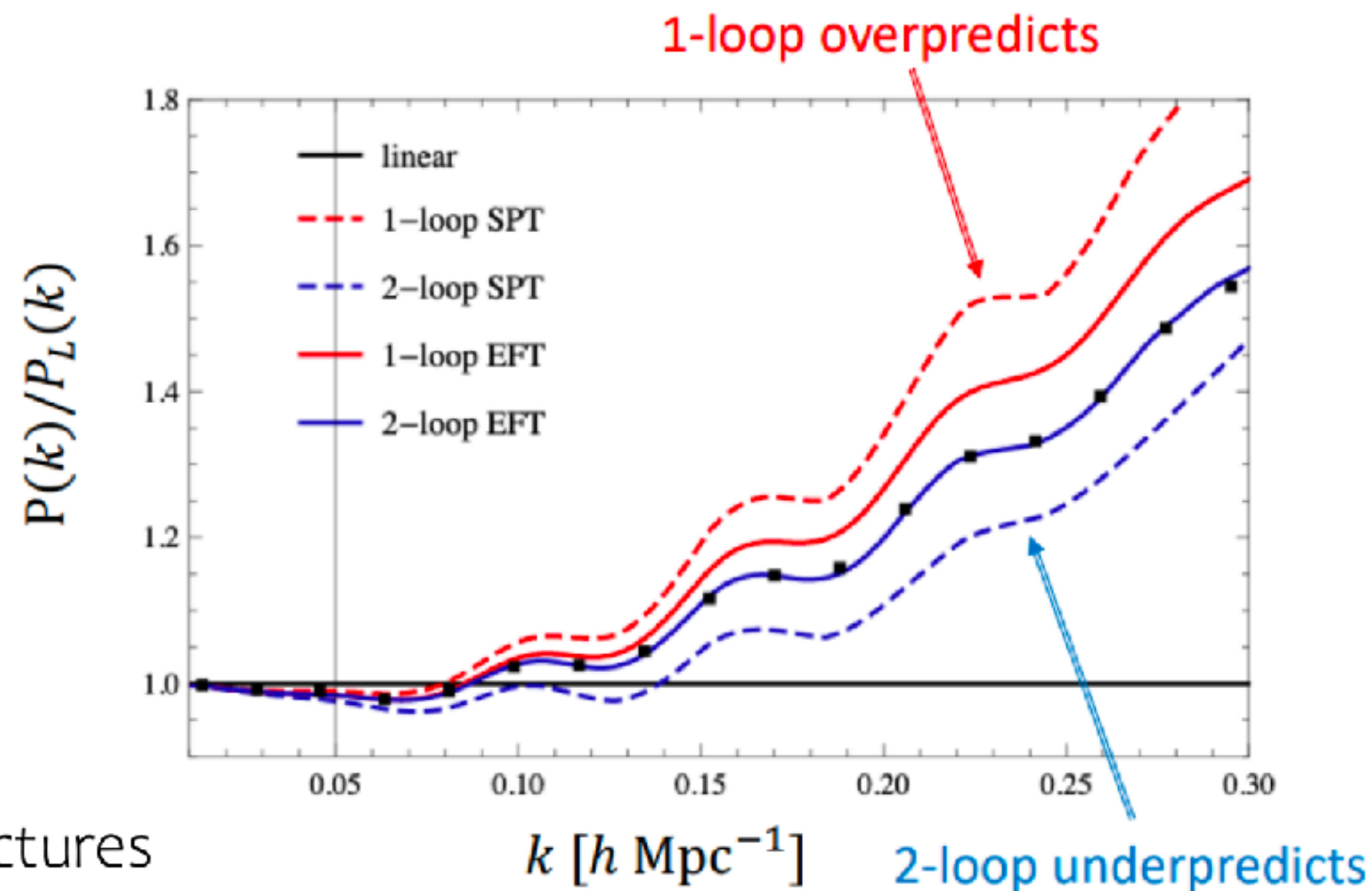
New expansion in powers of $\frac{k^2}{k_{\text{NL}}^2}$

Counterterms extracted from data

How to make precise predictions?

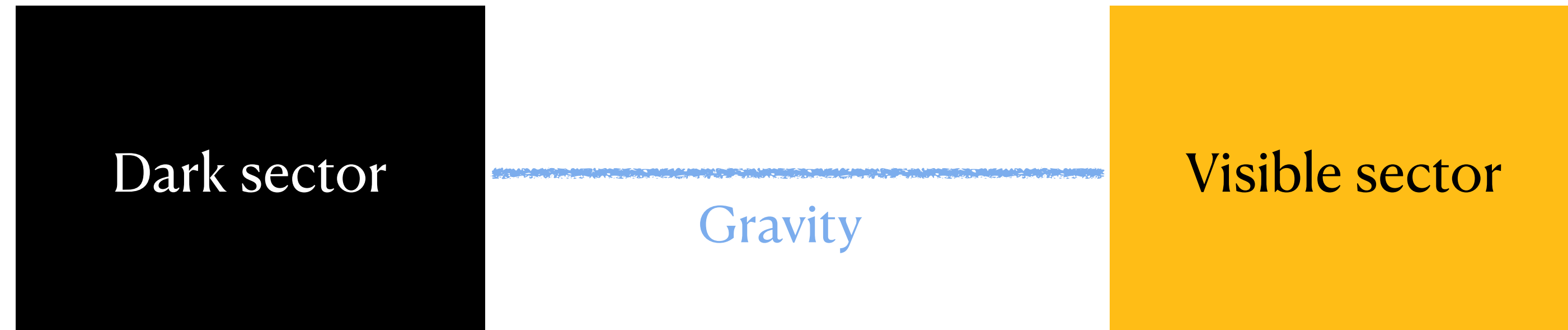
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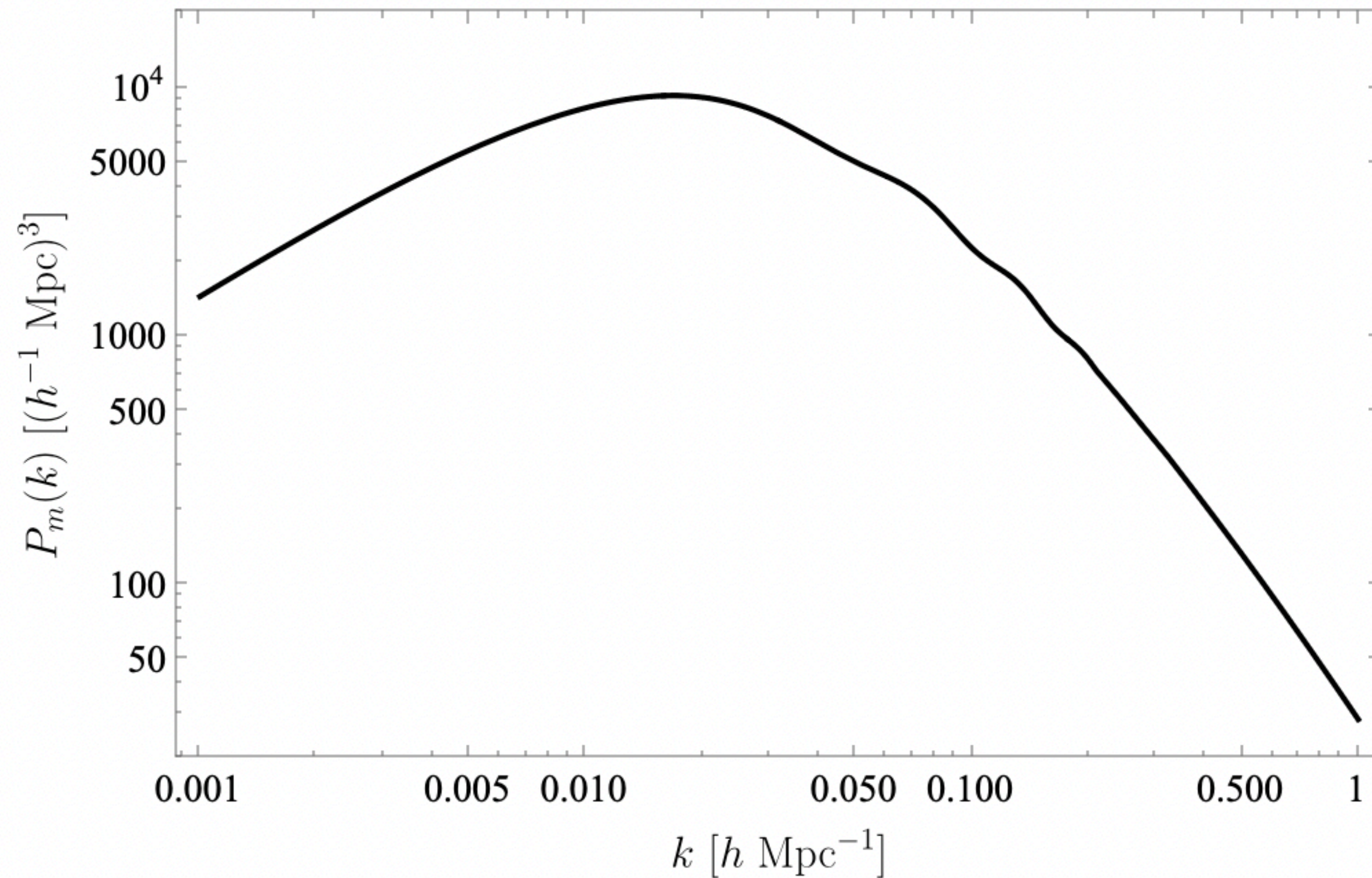
Baldauf lectures

Can we see in the dark?

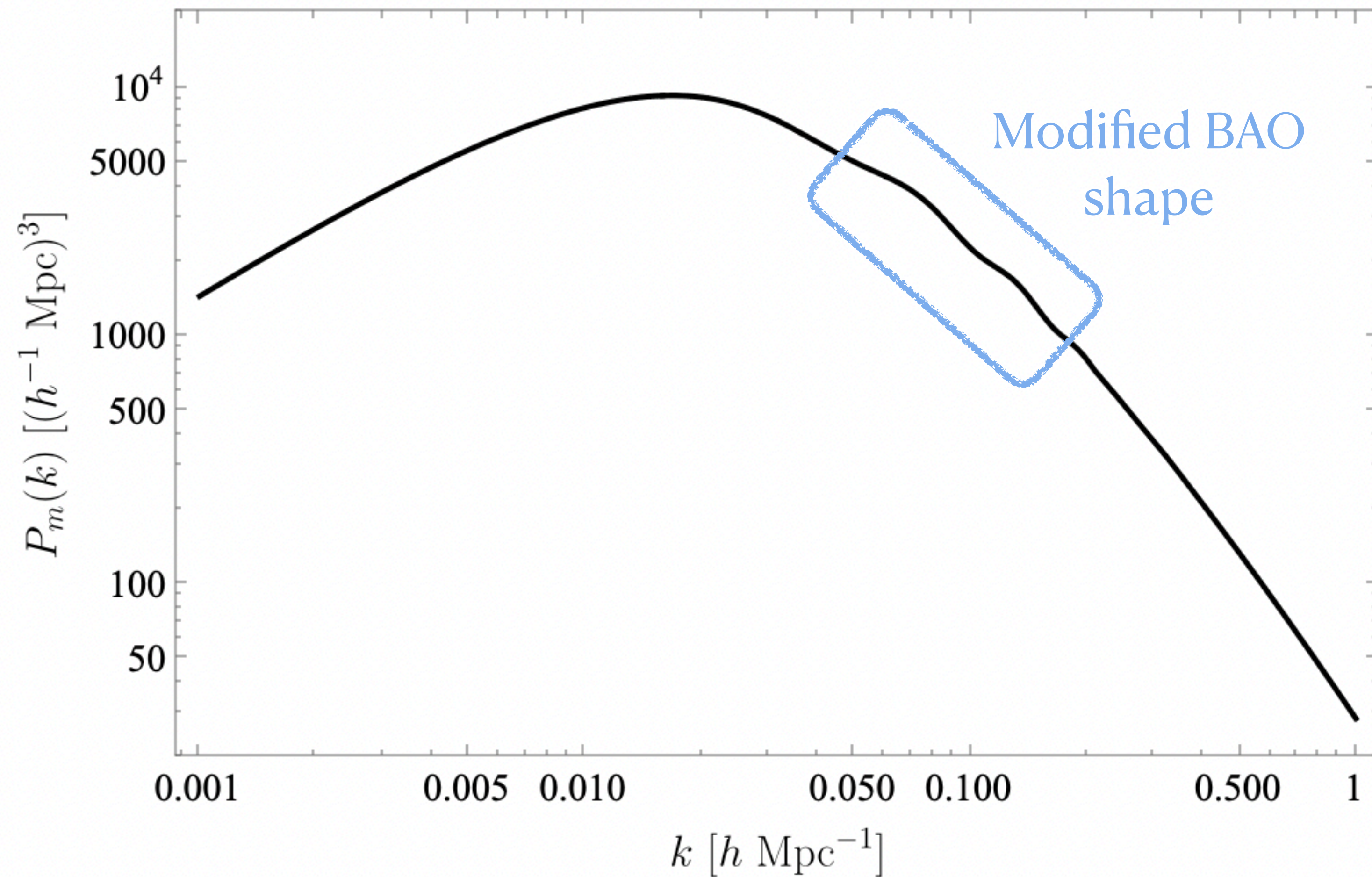


Cosmology is the only way to probe completely secluded dark sectors!

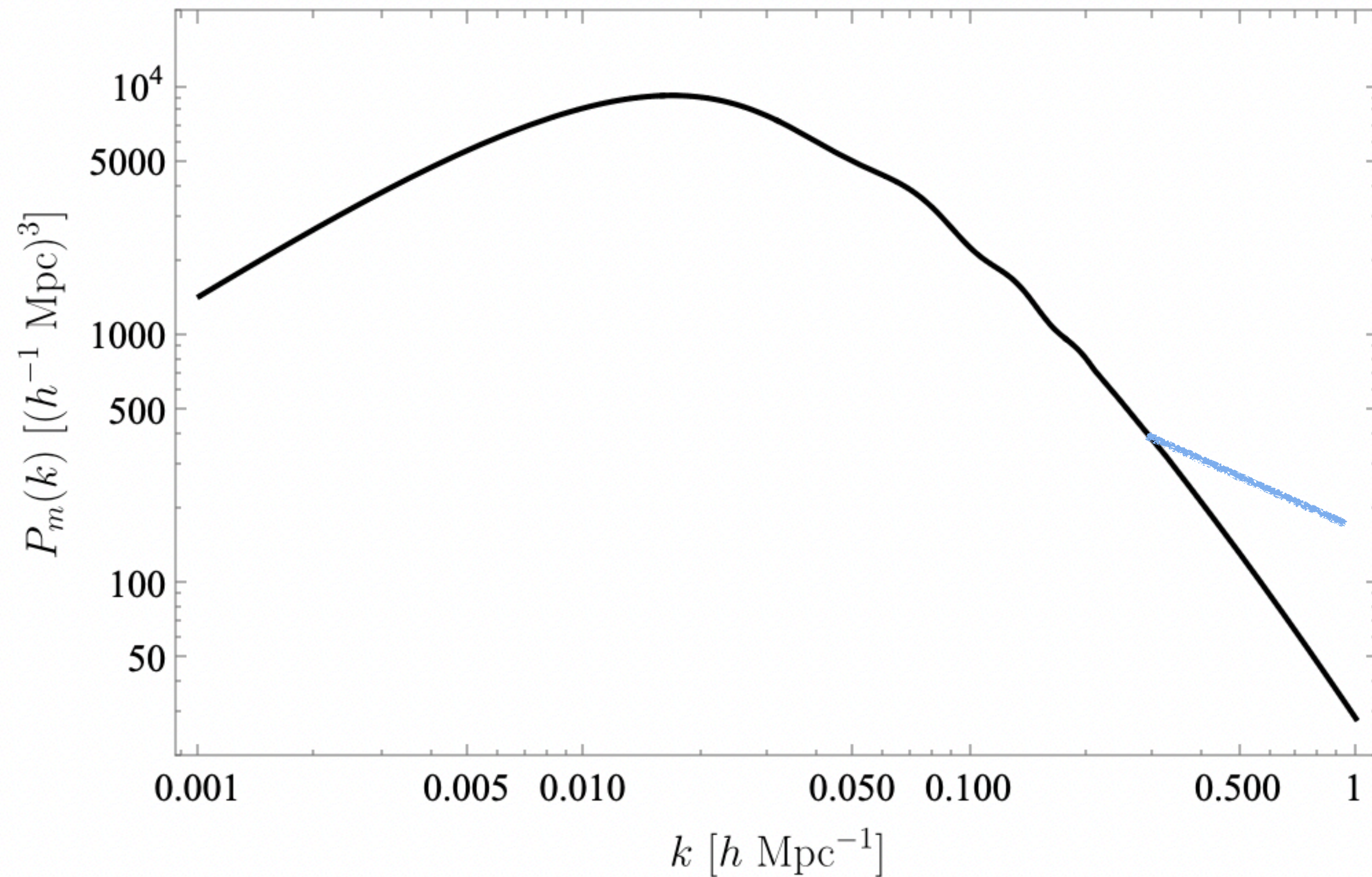
What can we find in the Power Spectrum?



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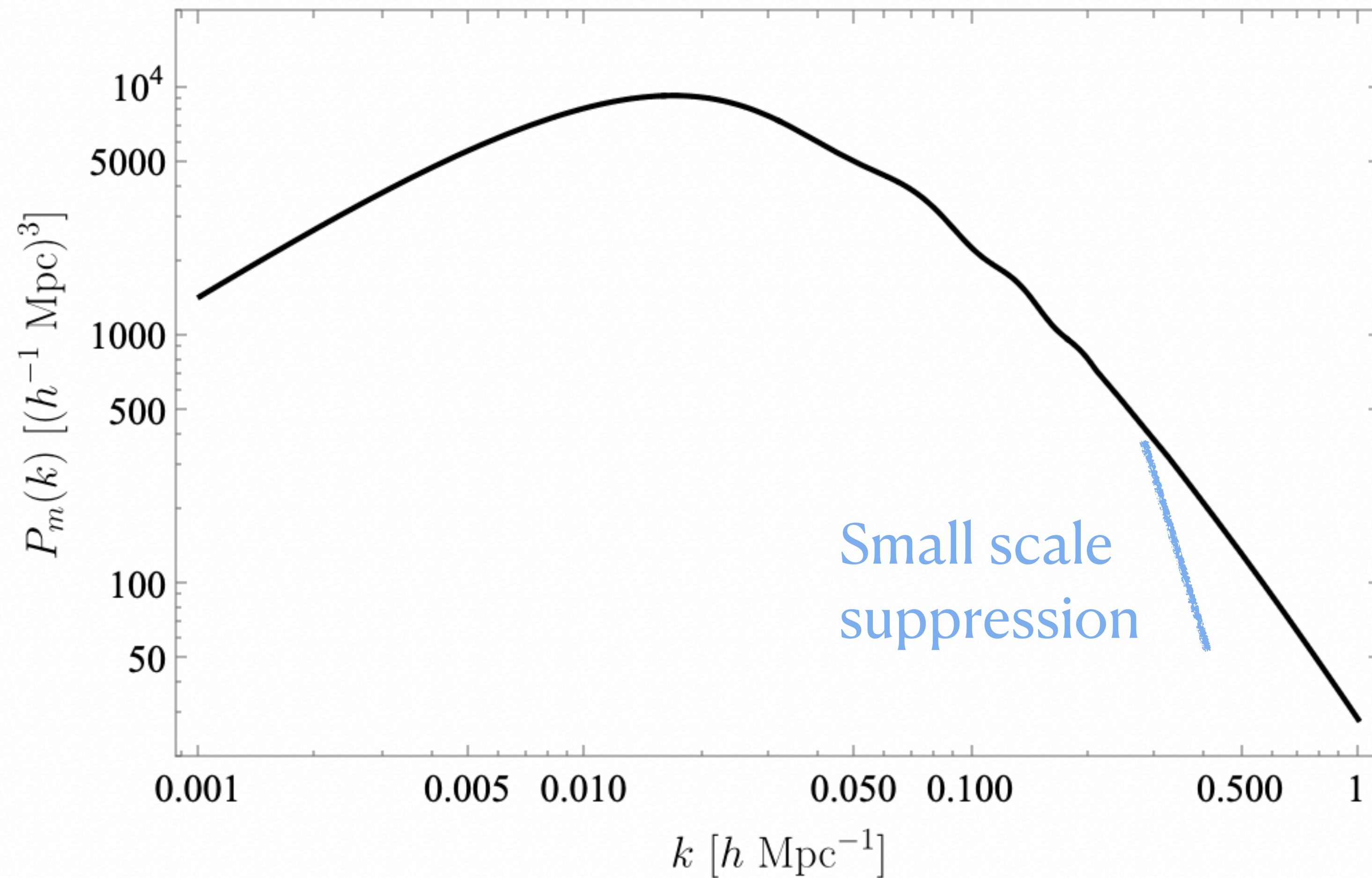


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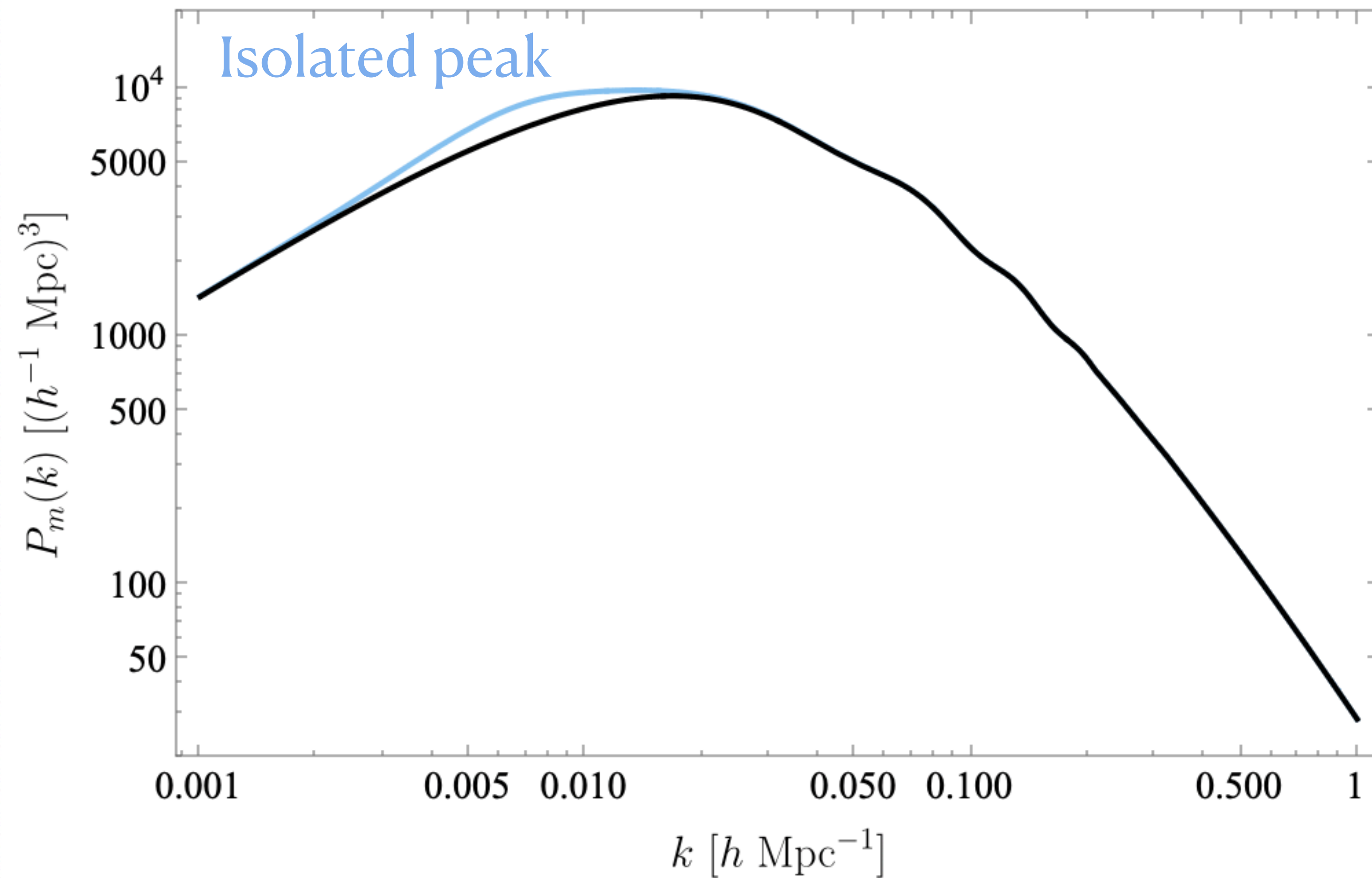


Small scale
enhancement

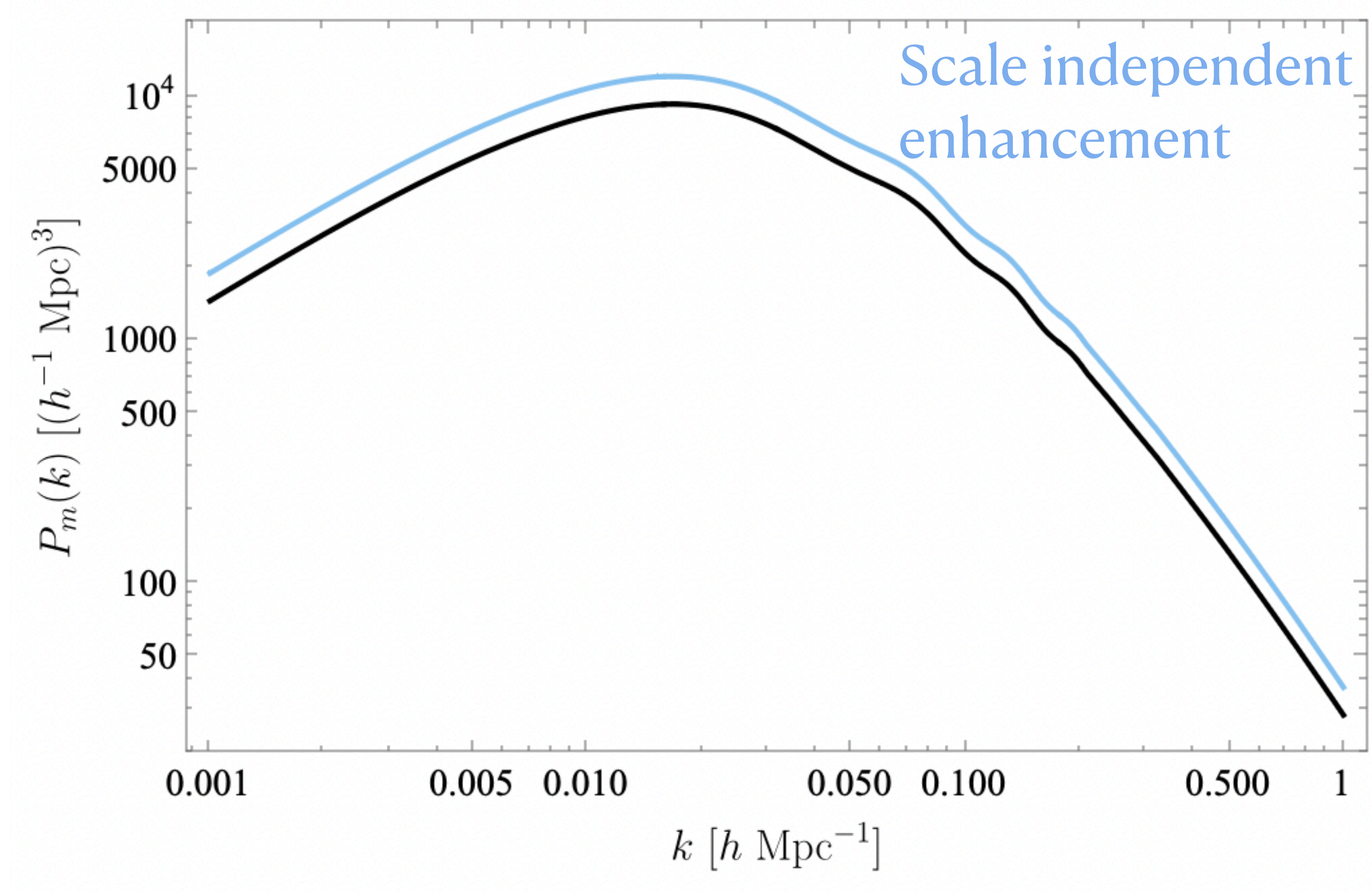
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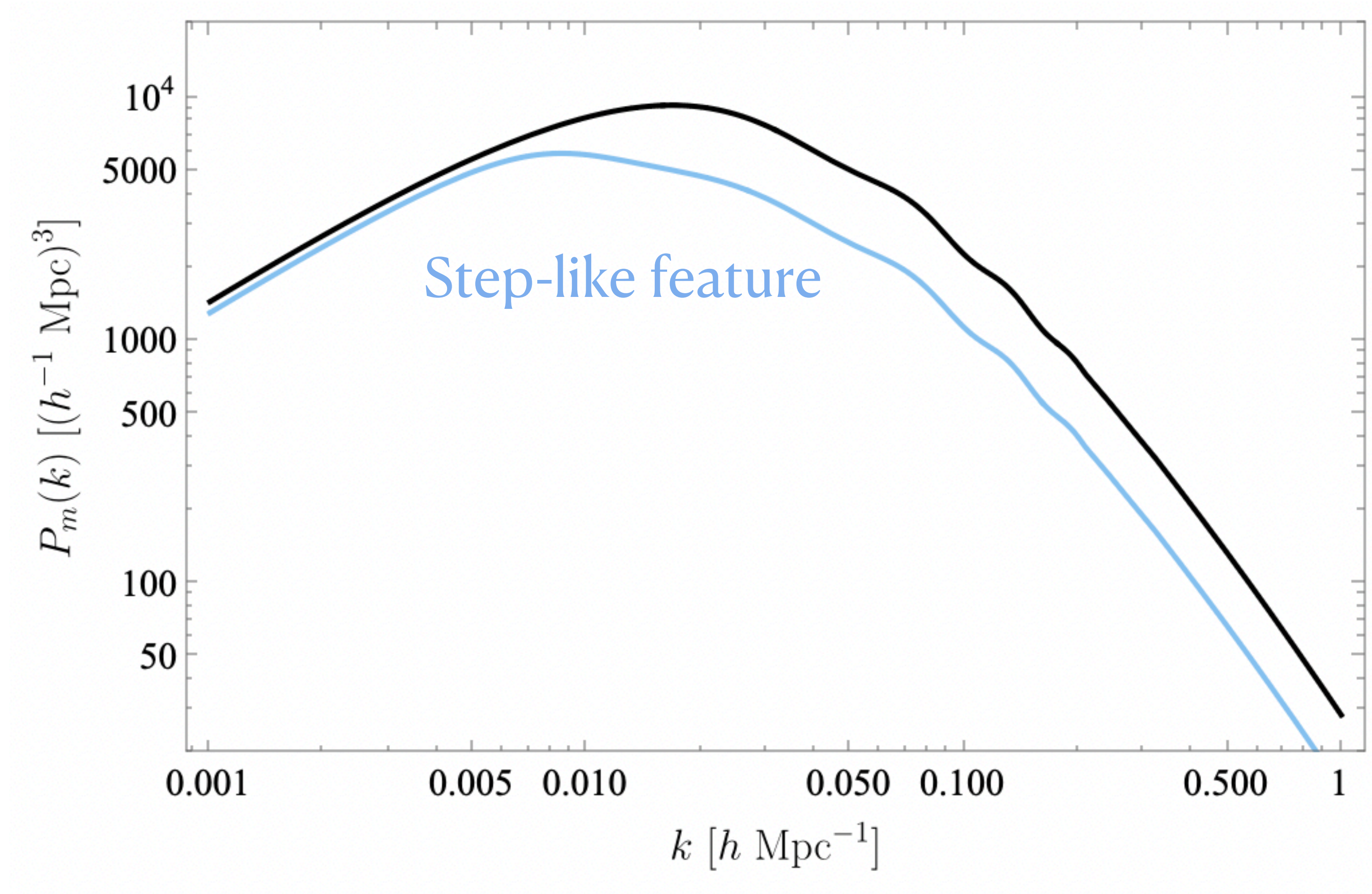
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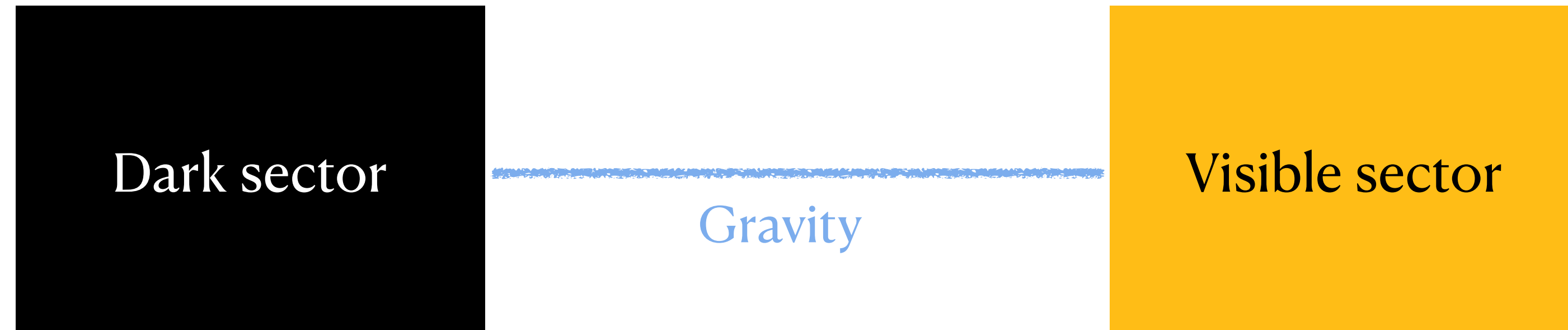
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Can we see in the dark?



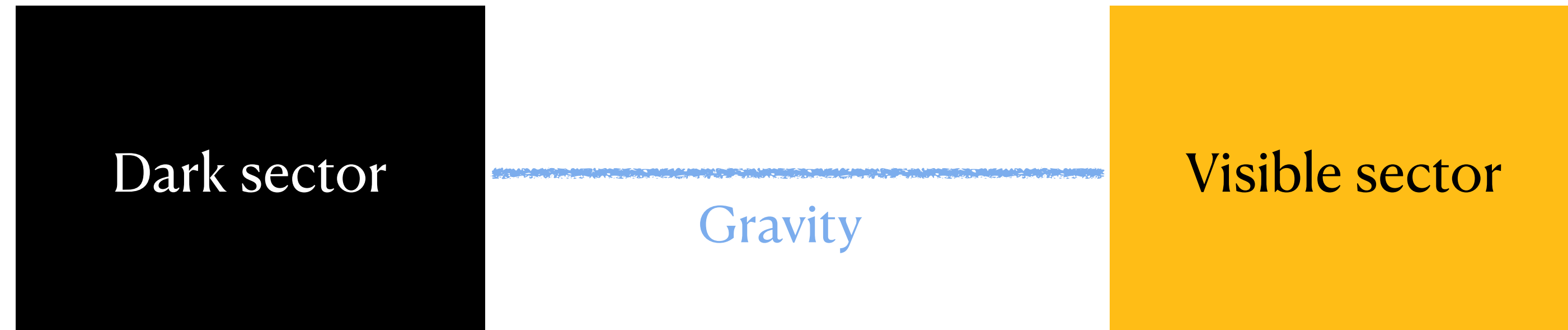
Cosmology is the only way to probe completely secluded dark sectors!

Examples in this talk

Long-range dark forces

Late-time dark phase transitions

Can we see in the dark?



Cosmology is the only way to probe completely secluded dark sectors!

SB et al. 2309.11496
SB et al. 2407.18252
Just al. 2204.08484

Examples in this talk

Long-range dark forces

Late-time dark phase transitions

A simple model

$$\mathcal{L} = \boxed{\frac{1}{2}(\partial_\mu \chi)^2} + \boxed{\frac{1}{2G_s}(\partial_\mu s)^2 + \frac{1}{2G_s}m_s^2 s^2} + \boxed{\frac{1}{2}m_\chi^2(1 + 2s)\chi^2}, \quad G_s = \frac{\kappa^2}{m_\chi^4}$$

Dark matter

Scalar dark force mediator

Interaction term: s-
dependent DM mass

A simple model

$$\mathcal{L} = \underbrace{\frac{1}{2}(\partial_\mu \chi)^2}_{\text{Dark matter}} + \underbrace{\frac{1}{2G_s}(\partial_\mu s)^2 + \frac{1}{2G_s}m_s^2 s^2}_{\text{Scalar dark force mediator}} + \underbrace{\frac{1}{2}m_\chi^2(1 + 2s)\chi^2}_{\text{Interaction term: s-dependent DM mass}}, \quad G_s = \frac{\kappa^2}{m_\chi^4}$$

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Dynamics determined by three parameters

1. Scalar mass m_s
2. Dark Matter fraction f_χ
3. Strength of the dark force $\beta = \frac{G_s}{4\pi G_N}$

Upper bound on m_χ from naturalness $m_\chi \lesssim 0.02 \text{ eV} \left(\frac{0.01}{\beta} \right)^{\frac{1}{4}} \left(\frac{m_s}{H_0} \right)^{\frac{1}{2}}$

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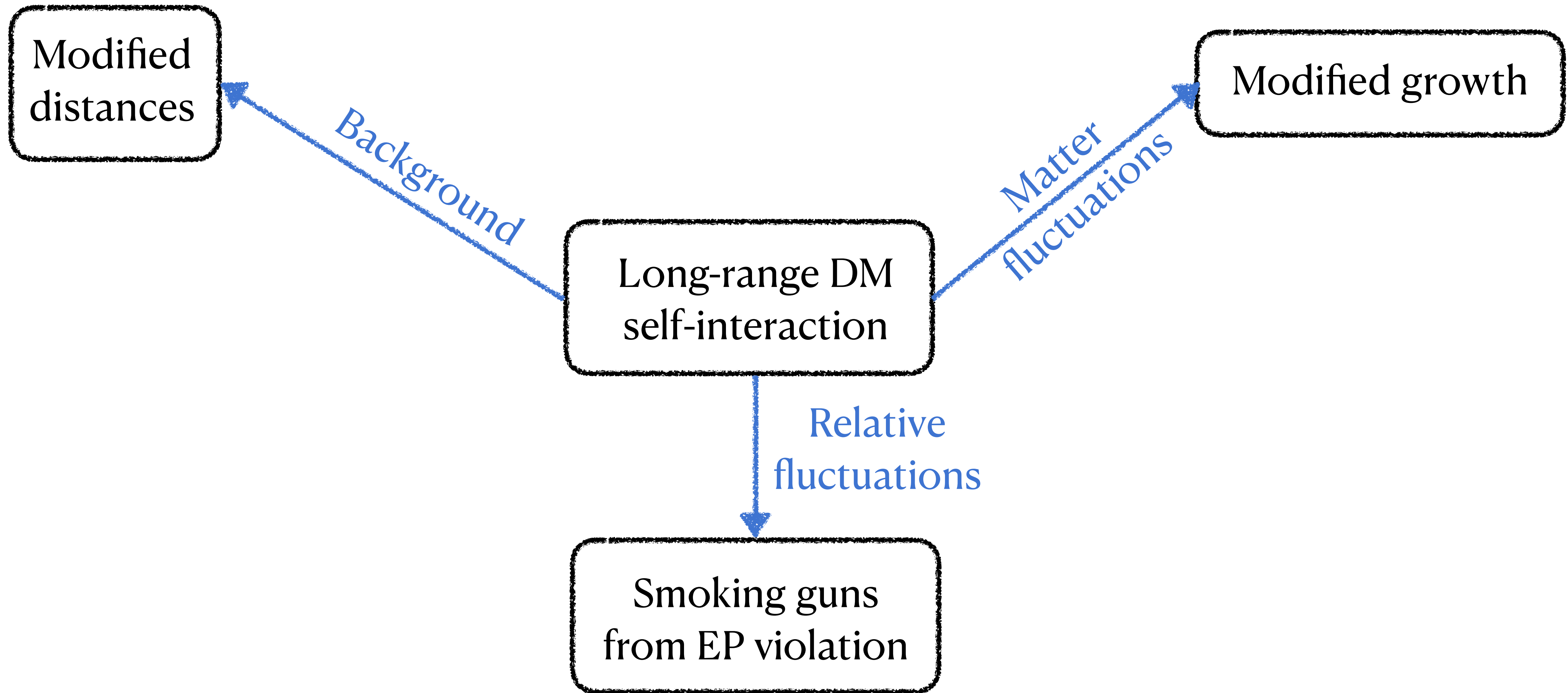
Working
assumptions

$$m_s \leq H_{\text{eq}} \approx 10^{-28} \text{ eV}$$

$$f_\chi \approx f_{\text{cdm}}$$

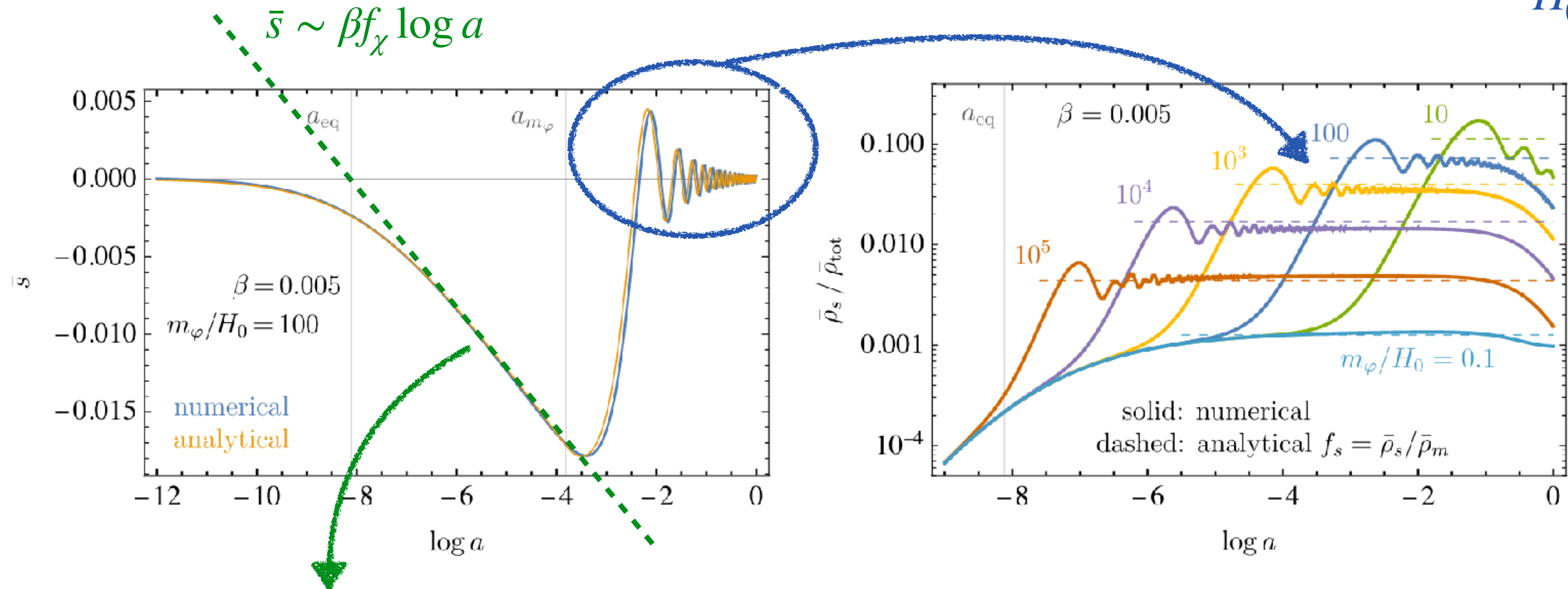
Upper bound on m_χ from naturalness $m_\chi \lesssim 0.02 \text{ eV} \left(\frac{0.01}{\beta} \right)^{\frac{1}{4}} \left(\frac{m_s}{H_0} \right)^{\frac{1}{2}}$

Dark force dynamics



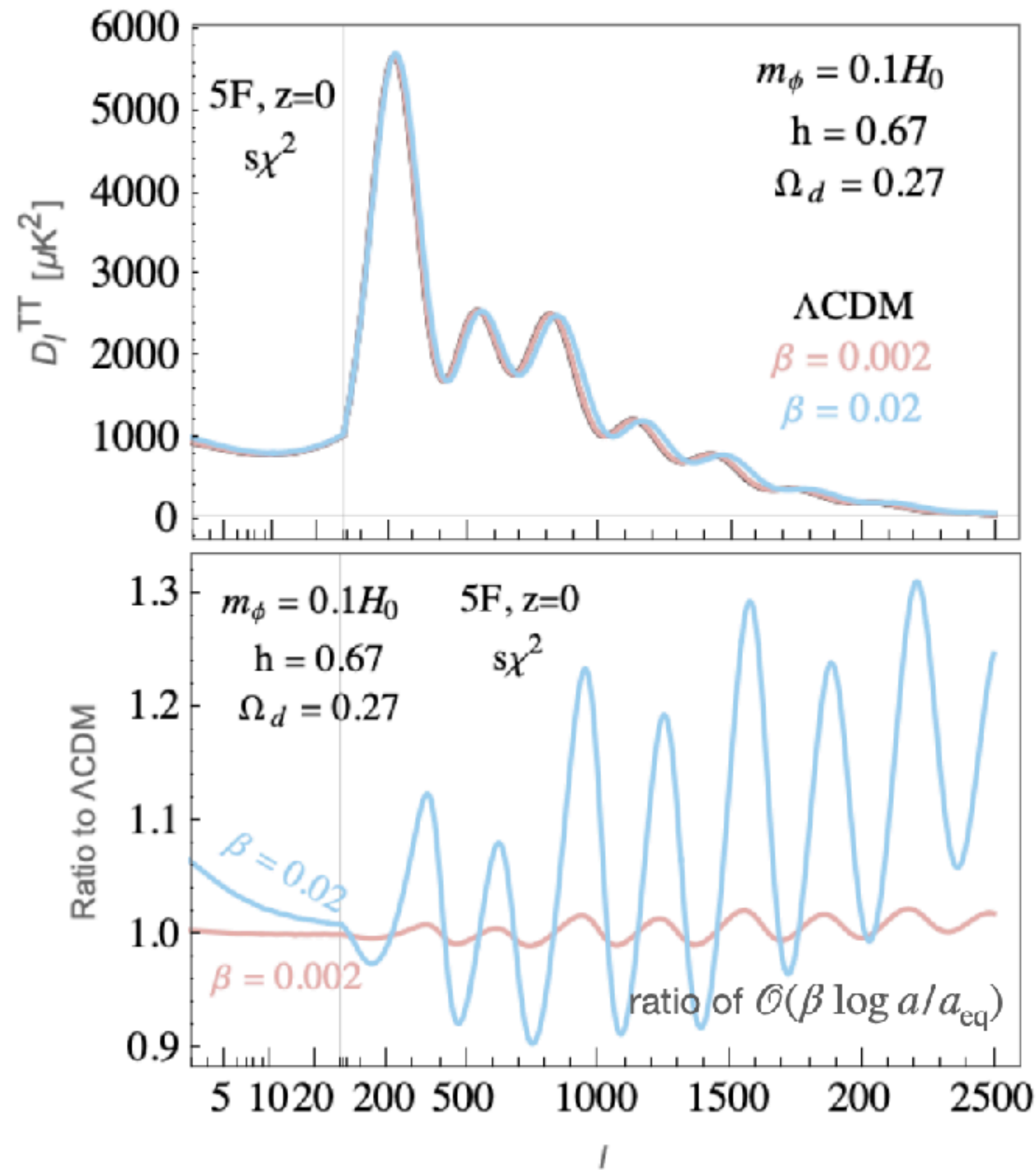
Background dynamics

Behaves as CDM with fraction $f_s \sim \beta f_\chi^2 \log \frac{m_s^2}{H_0^2}$



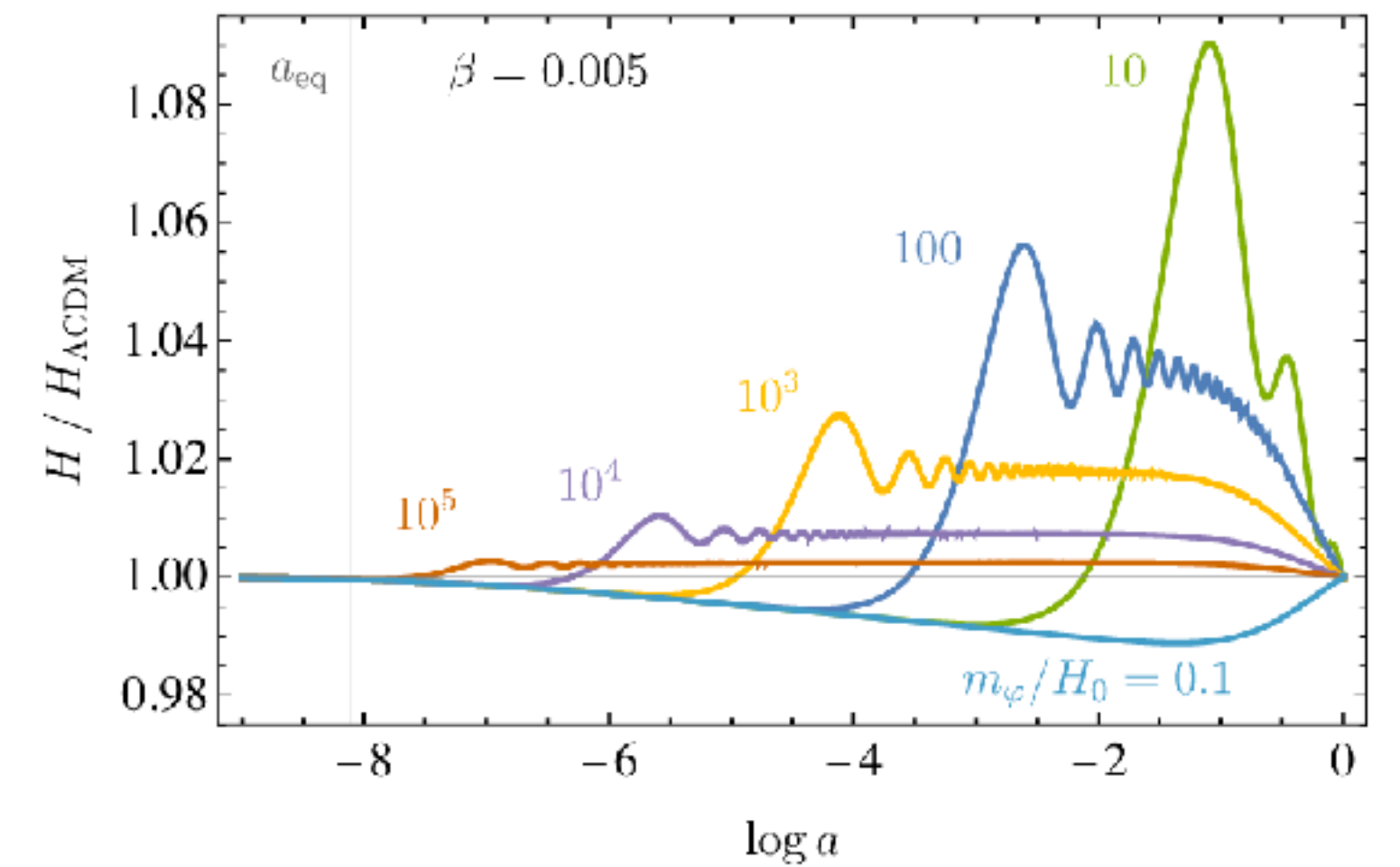
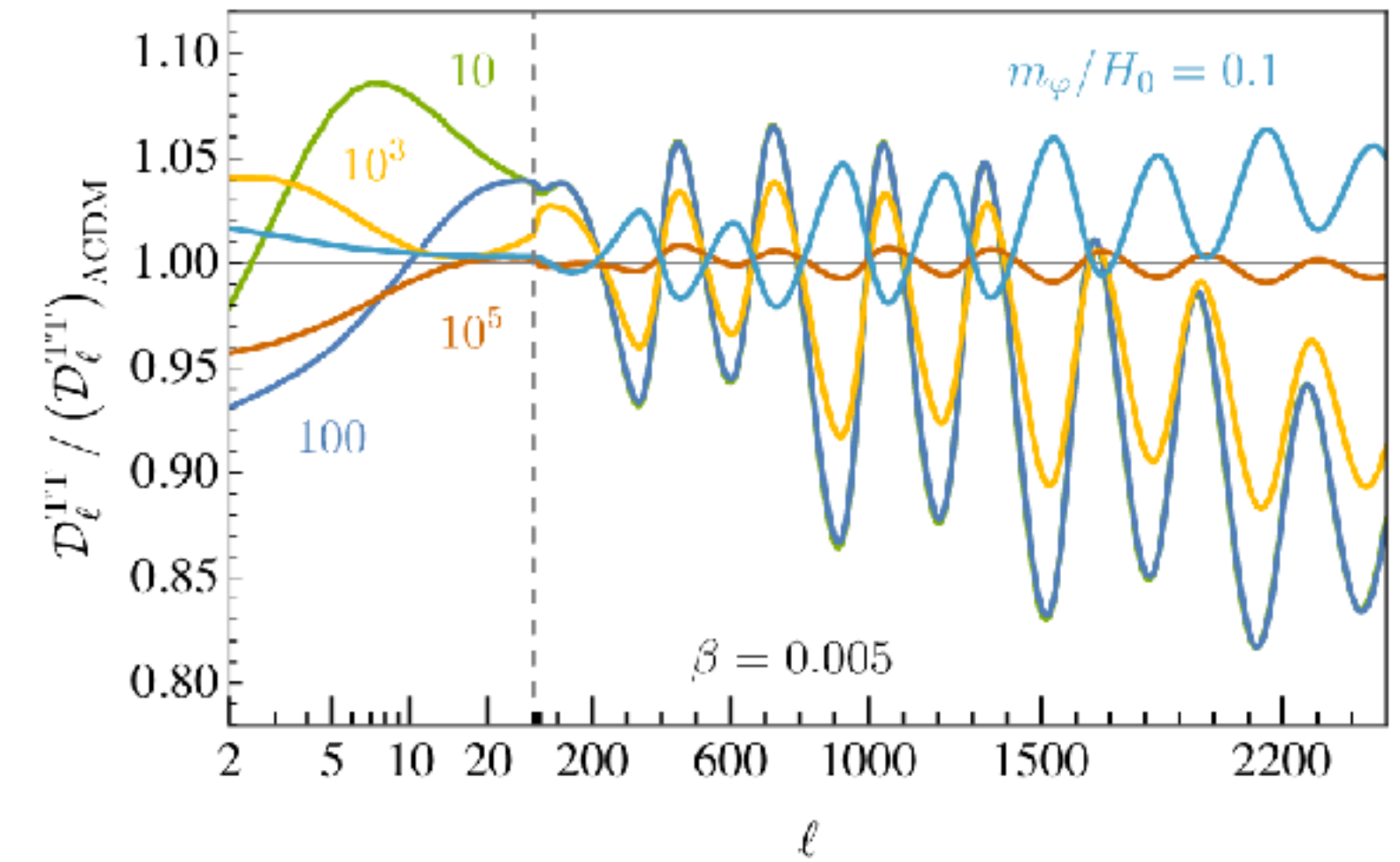
DM redshifts faster $\Omega_\chi \simeq a^{-3} \left(1 - \beta f_\chi \log \frac{a}{a_{\text{eq}}} \right)$

Effects on CMB



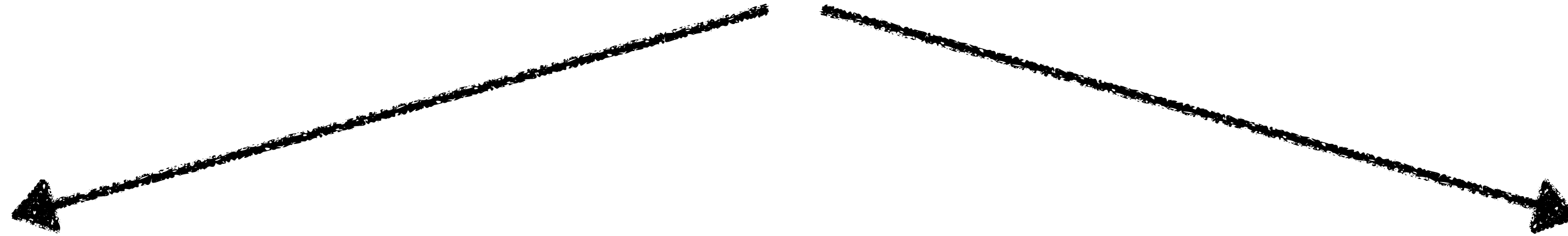
Pure shift from
bkg evolution

$$\ell_n \approx \frac{n\pi}{c_s \chi_{rec}} \propto \int_0^{rec} dz \frac{1}{H_{\Lambda CDM}(z) + \Delta H(z)}$$



Effects on Matter Power Spectrum

Two contrasting effects



Enhancement from
new attractive force

Suppression from
mediator Jeans scale

$$k_{Js} \approx 5 \times 10^{-4} \left(\frac{m_s}{H_0} \right)^{\frac{1}{2}} h \text{ Mpc}^{-1}$$

Effects on Matter Power Spectrum

Two contrasting effects

Enhancement from
new attractive force

Suppression from
mediator Jeans scale

$$m_s \leq H_0$$

$$k_{Js} \approx 5 \times 10^{-4} \left(\frac{m_s}{H_0} \right)^{\frac{1}{2}} h \text{ Mpc}^{-1}$$

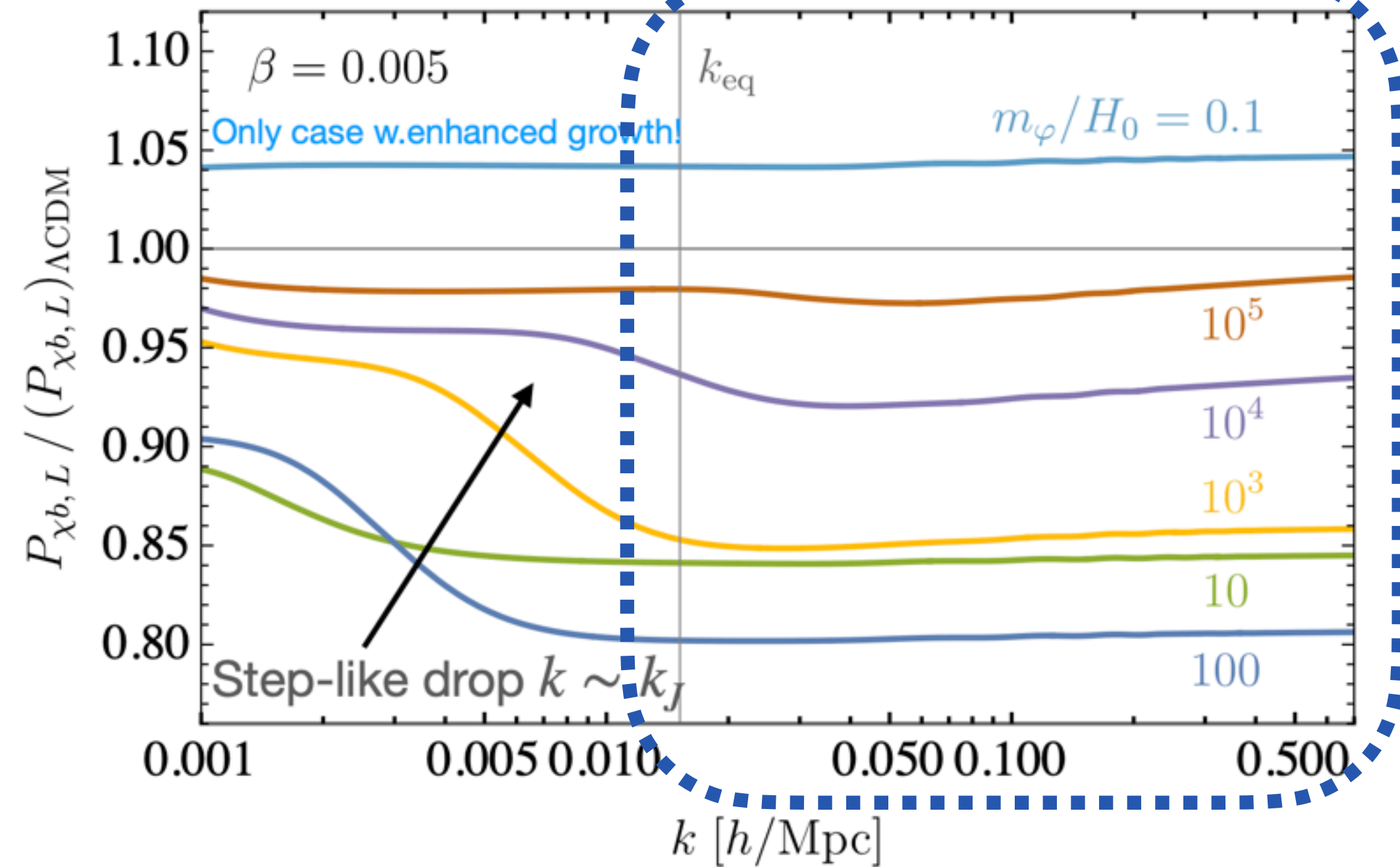
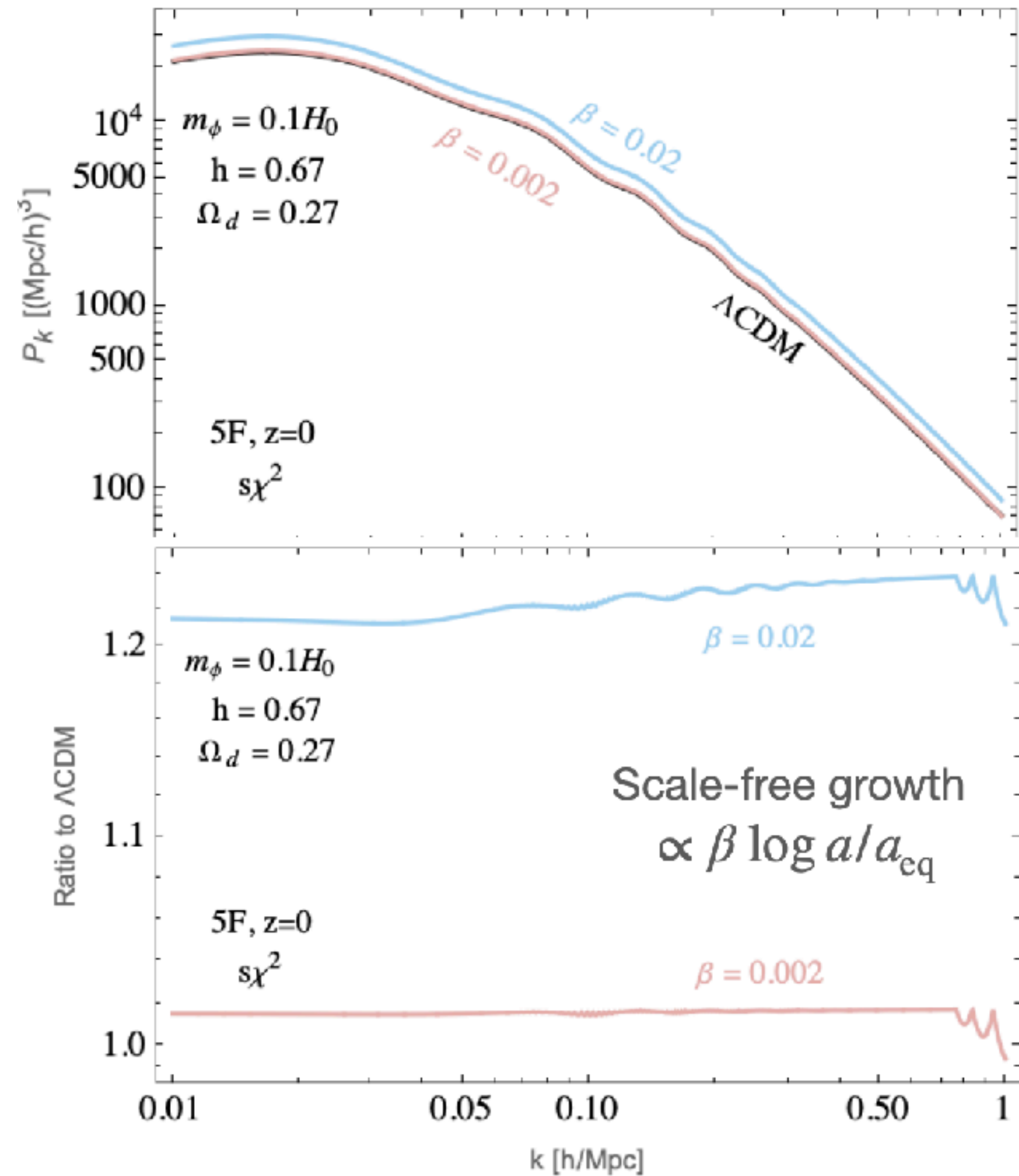
$$\begin{cases} \delta'_m + \theta_m + \vec{\nabla}(\delta_m \vec{v}_m) = 0, & \theta_m = \vec{\nabla} \vec{v}_m \\ \theta'_m + \mathcal{H}(1 - \beta f_\chi^2) \theta_m + \frac{3}{2} \mathcal{H}^2 (1 + \beta f_\chi^2) \delta_m + \partial_i (v_m^j \partial_j v_m^i) = - \frac{1}{\bar{\rho}_m} \partial_i \partial_j \tau_{\text{eff}}^{ij} \end{cases}$$

$$k_{Js} \leq k_{\text{eq}} \quad \text{if} \quad m_s \leq H_{\text{eq}}$$

Scale independent growth factor at
the scales relevant for LSS

Effects on Matter Power Spectrum

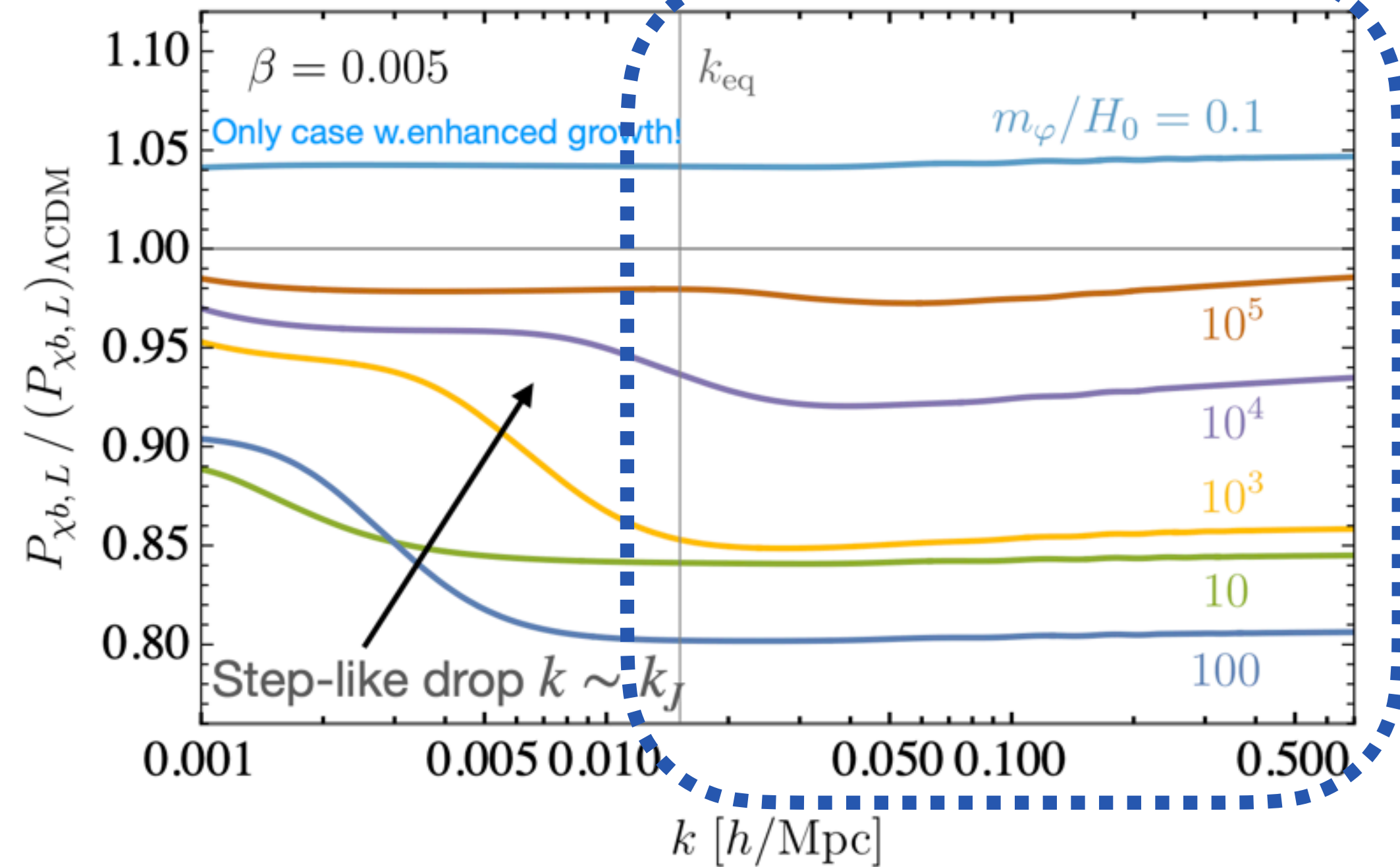
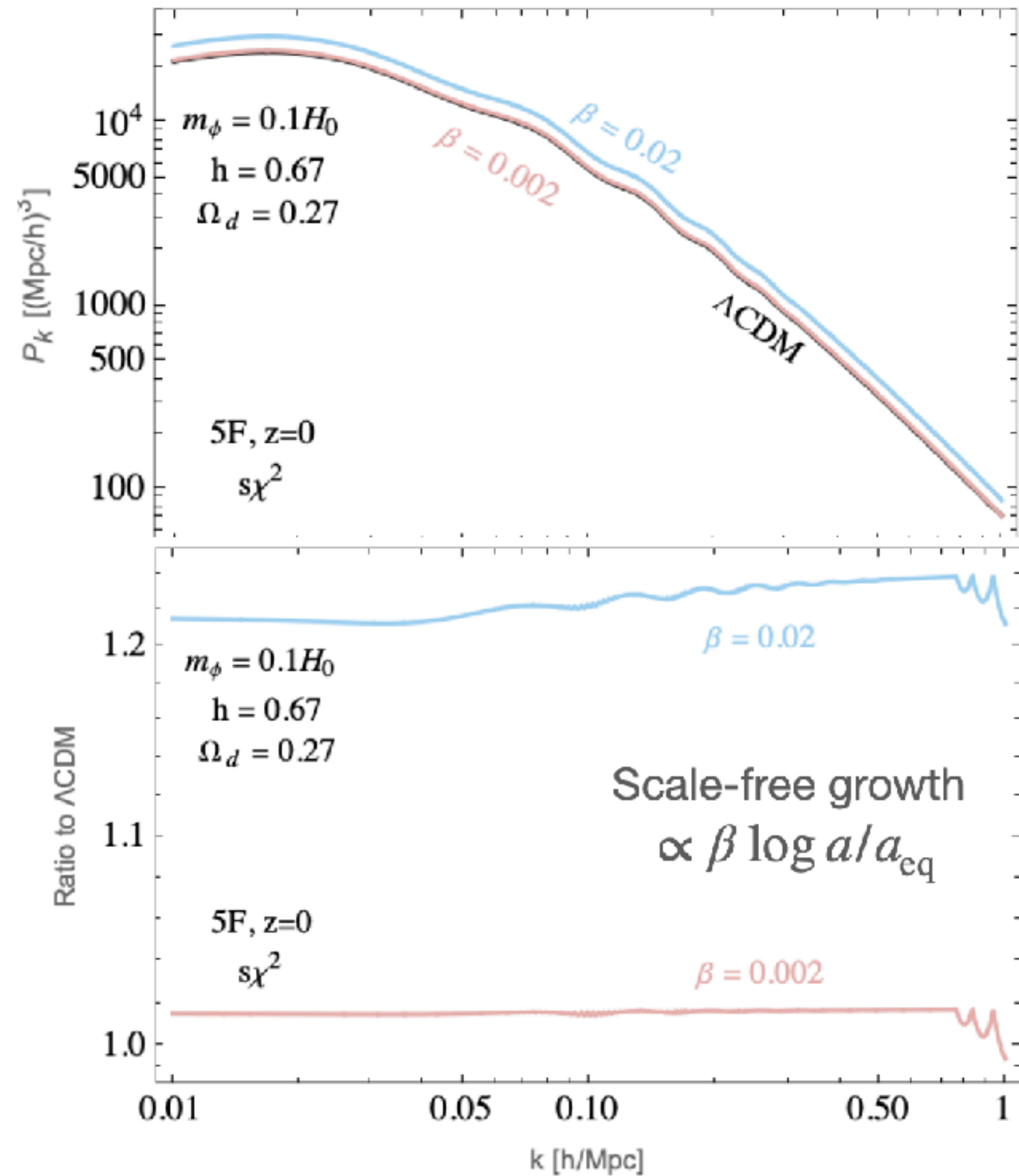
Scale-free growth factor at
scales relevant for LSS



$$\frac{\delta_m(a)}{\delta_m^{\text{CDM}}(a)} - 1 \simeq \frac{6}{5} \beta \tilde{m}_s^2 f_\chi^2 \log \frac{a_{m_\phi}}{a_{\text{eq}}} - f_s - \frac{3}{5} f_s \log \frac{a}{a_{m_\phi}}$$

Effects on Matter Power Spectrum

Scale-free growth factor at
scales relevant for LSS

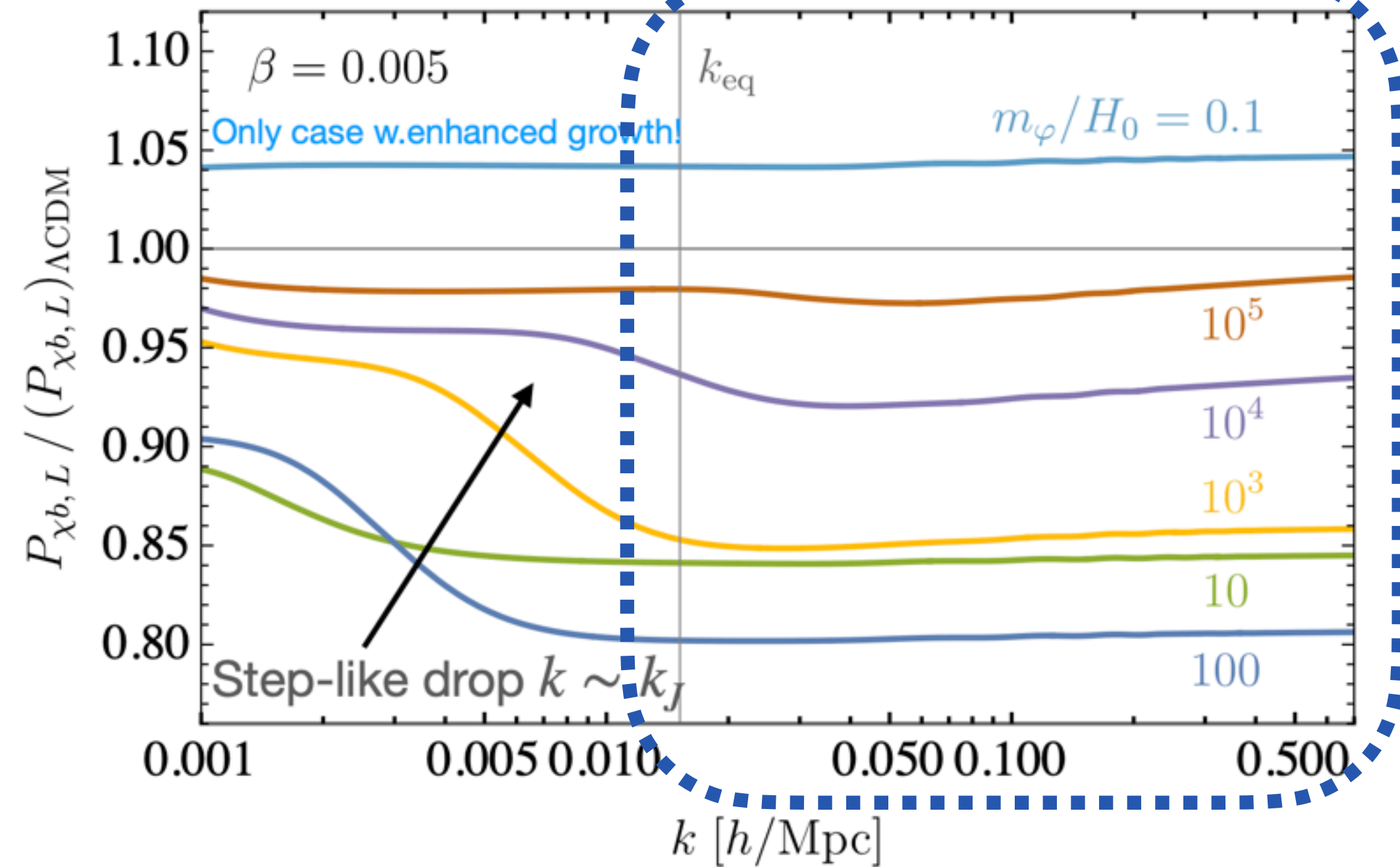
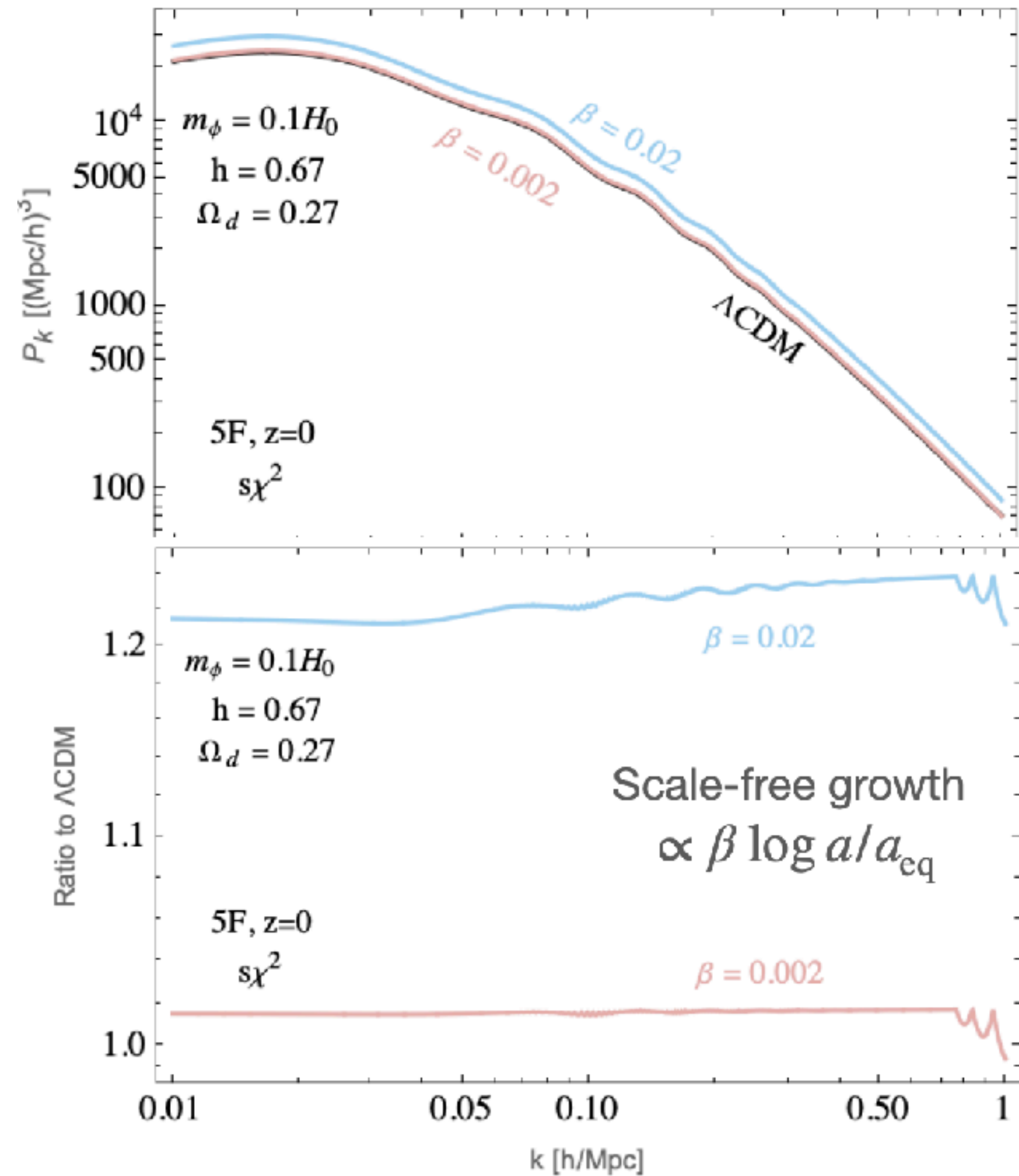


$$\frac{\delta_m(a)}{\delta_m^{\Lambda\text{CDM}}(a)} - 1 \approx \frac{6}{5} \beta \tilde{m}_s^2 f_\chi^2 \log \frac{a_{m_\phi}}{a_{\text{eq}}} - f_s - \frac{3}{5} f_s \log \frac{a}{a_{m_\phi}}$$

Enhanced
growth

Effects on Matter Power Spectrum

Scale-free growth factor at
scales relevant for LSS

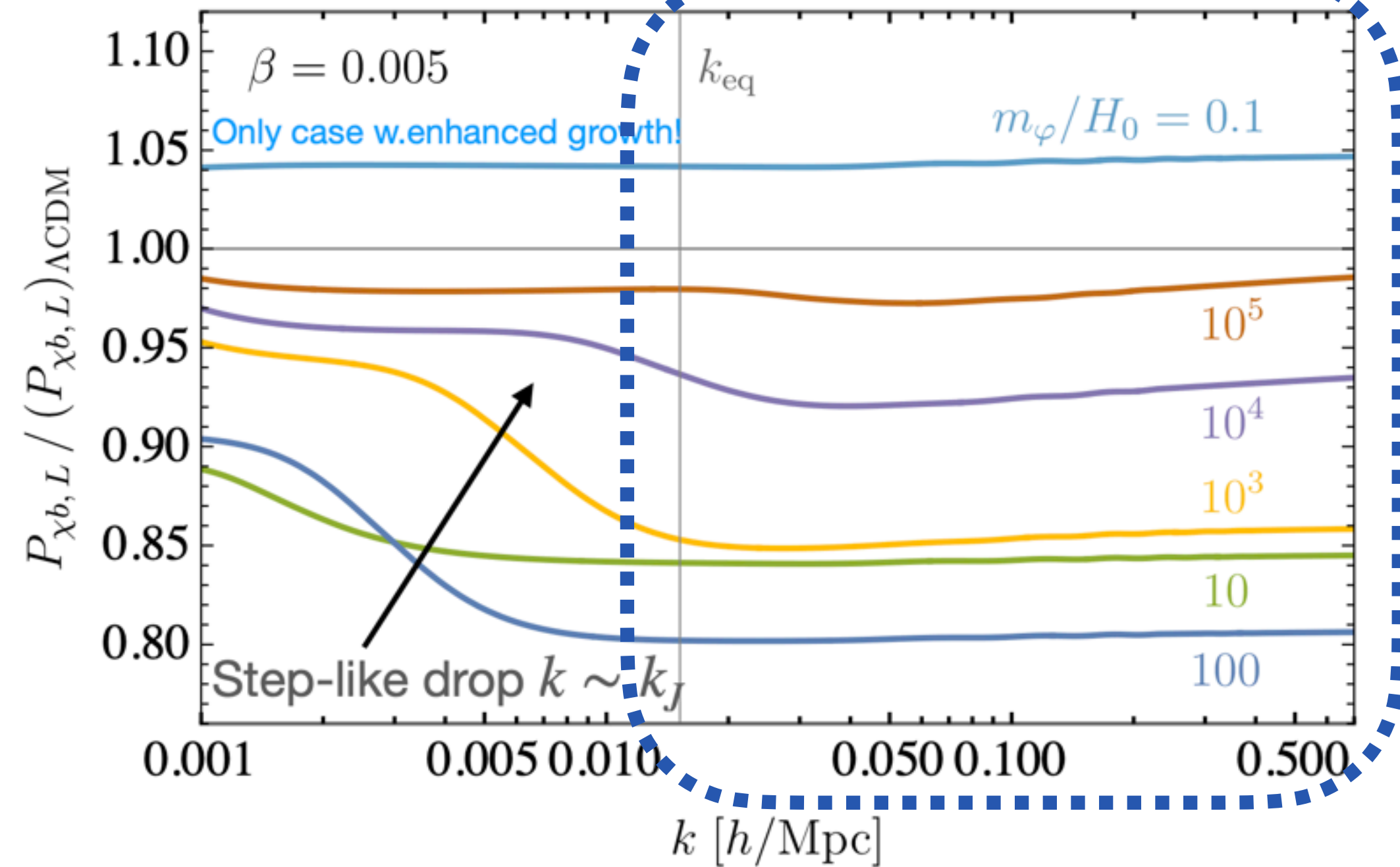
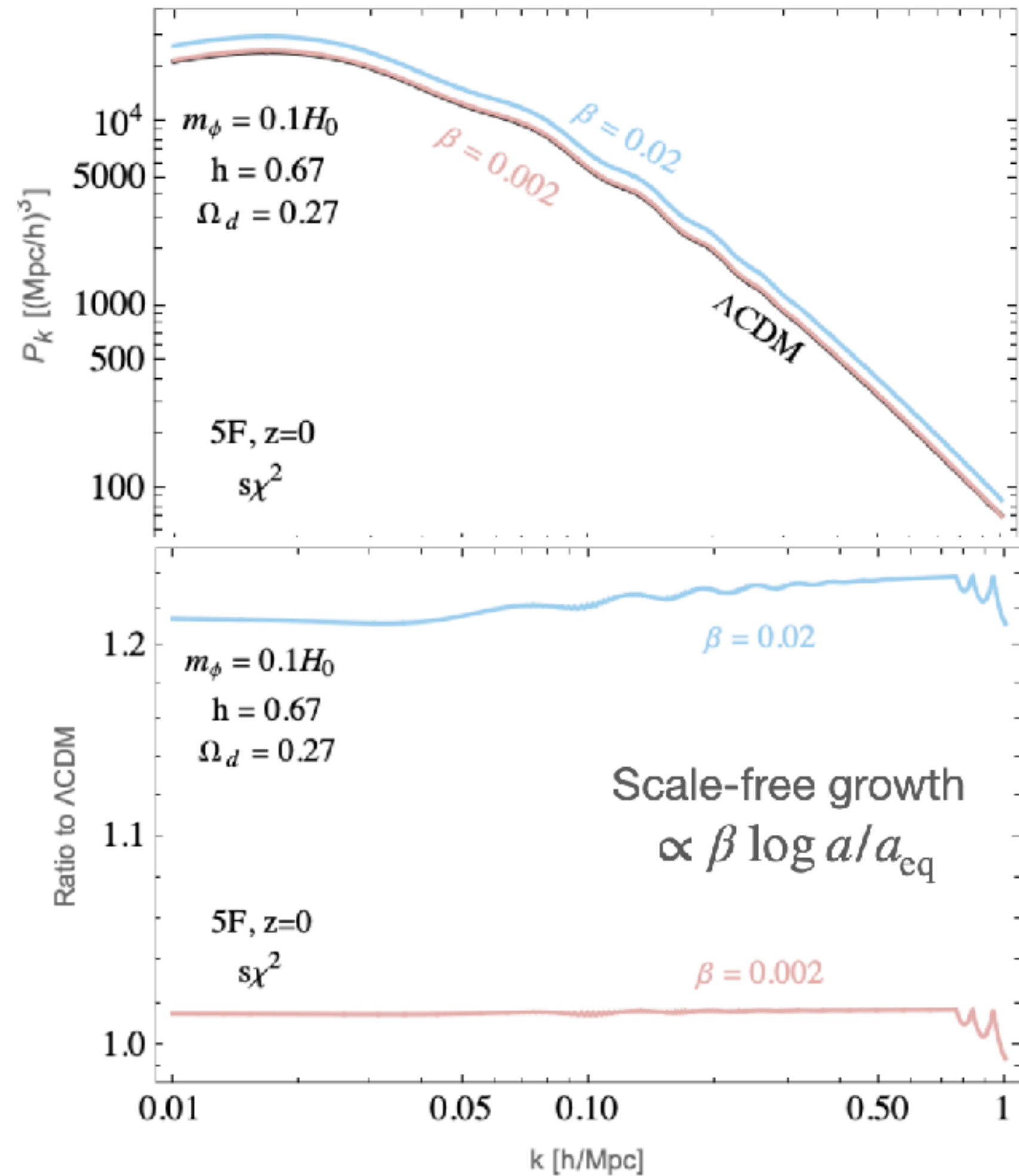


$$\frac{\delta_m(a)}{\delta_m^{\text{CDM}}(a)} - 1 \simeq \frac{6}{5} \beta \tilde{m}_s^2 f_\chi^2 \log \frac{a_{m_\phi}}{a_{\text{eq}}} \left[f_s - \frac{3}{5} f_s \log \frac{a}{a_{m_\phi}} \right]$$

Mediator not
clustering

Effects on Matter Power Spectrum

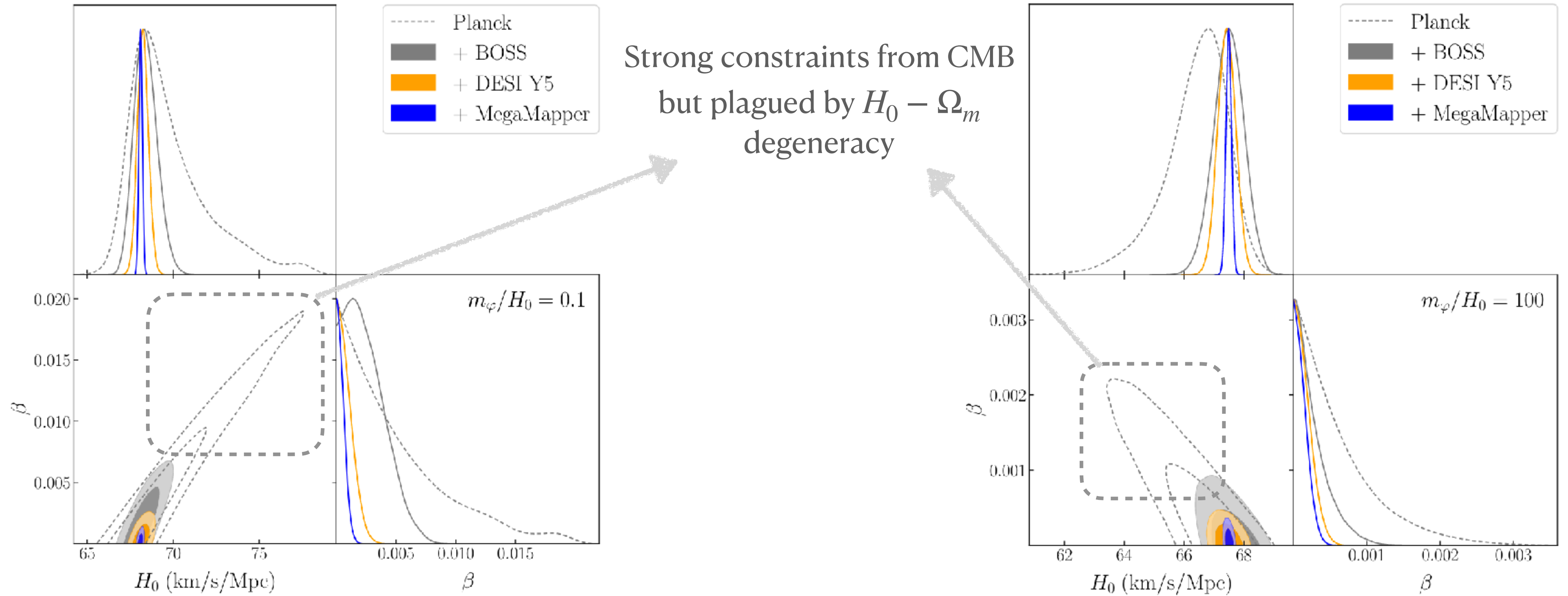
Scale-free growth factor at
scales relevant for LSS



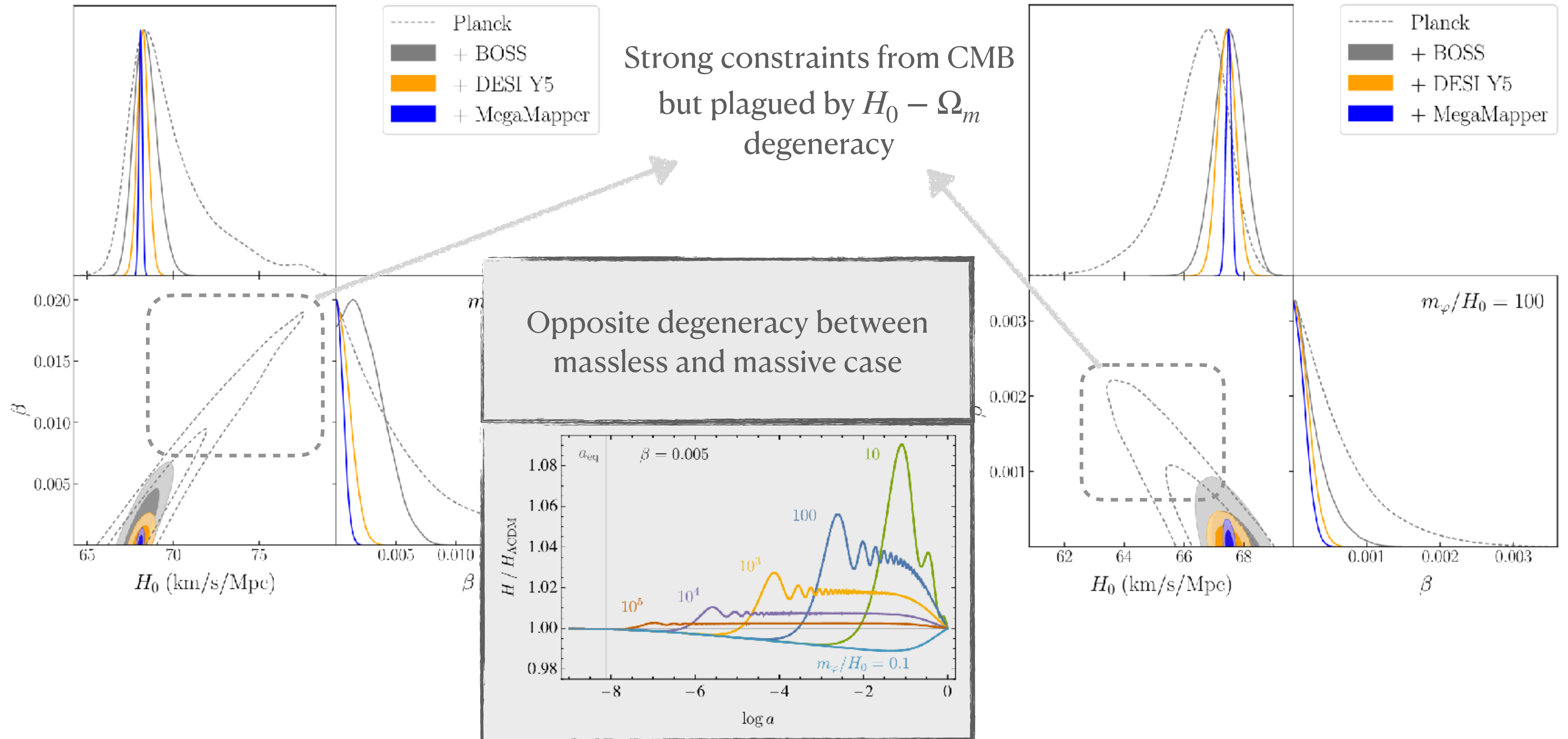
$$\frac{\delta_m(a)}{\delta_m^{\text{CDM}}(a)} - 1 \simeq \frac{6}{5} \beta \tilde{m}_s^2 f_\chi^2 \log \frac{a_{m_\phi}}{a_{\text{eq}}} - f_s \left[\frac{3}{5} f_s \log \frac{a}{a_{m_\phi}} \right]$$

Reduced gravitational
potential

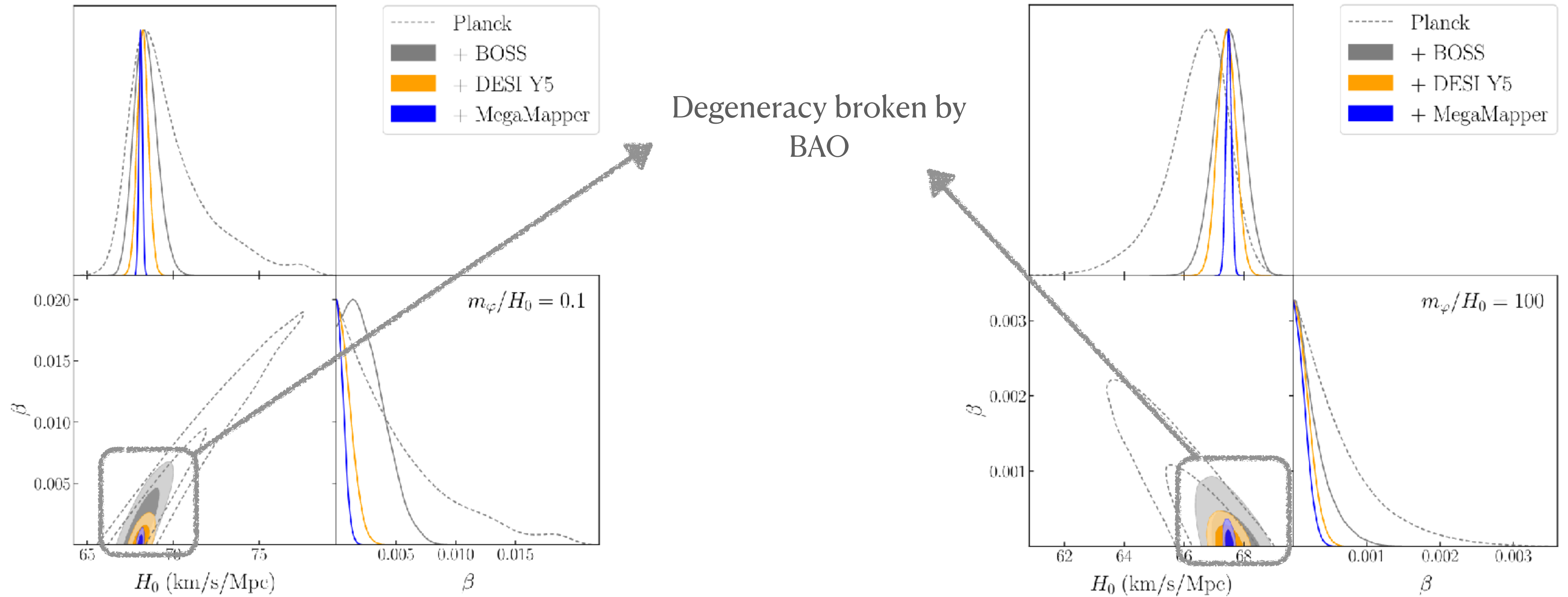
Results



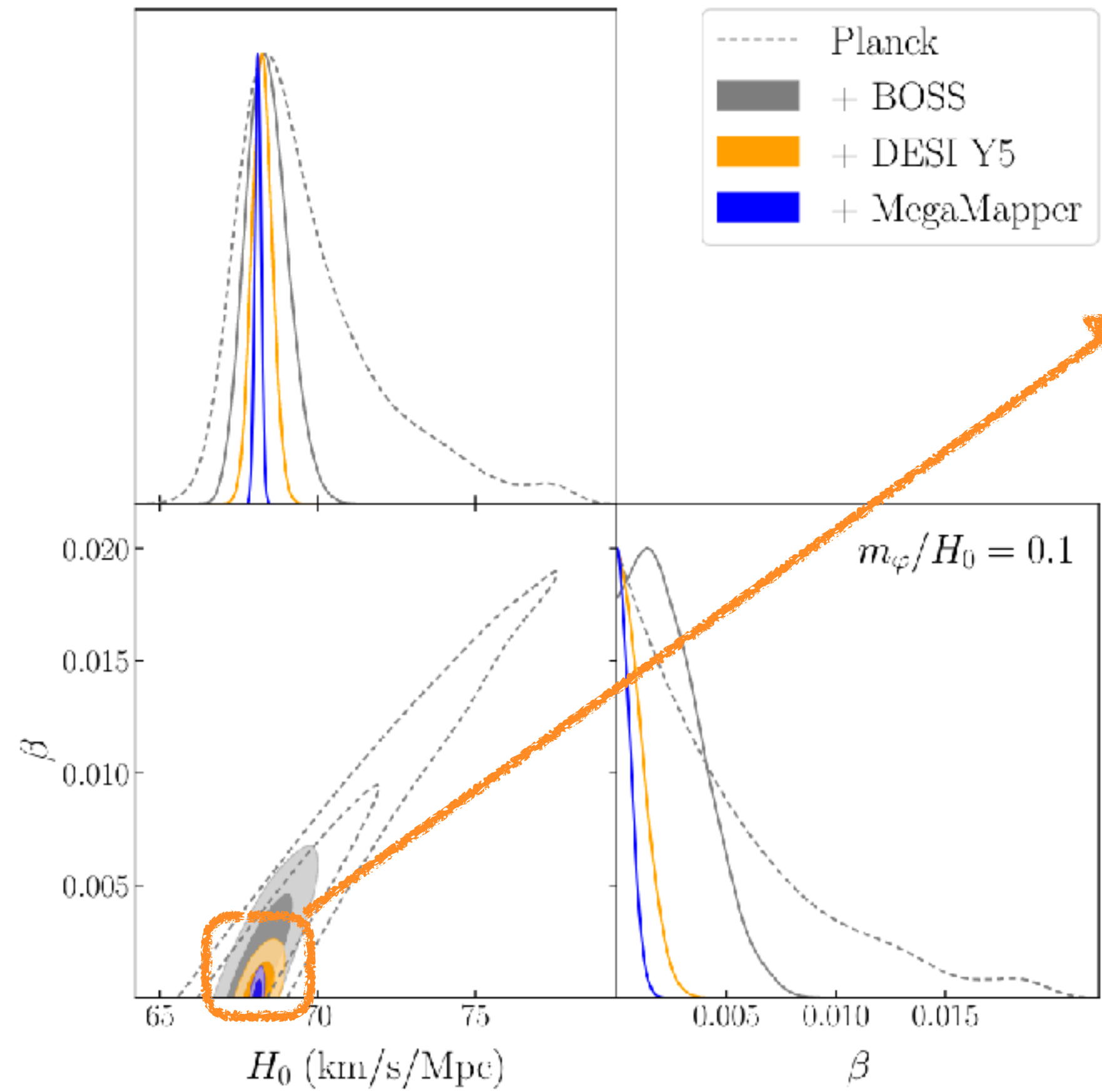
Results



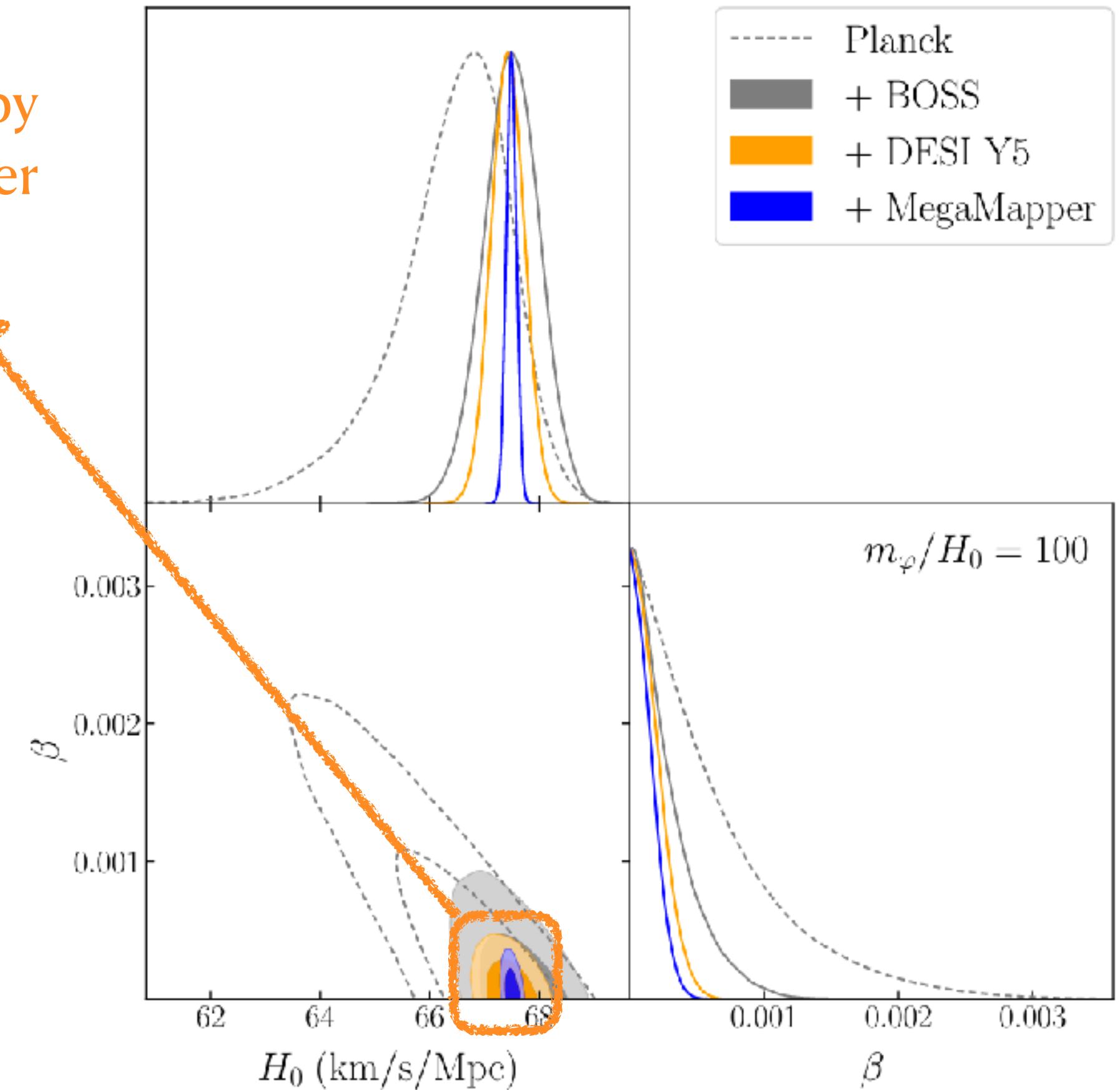
Results



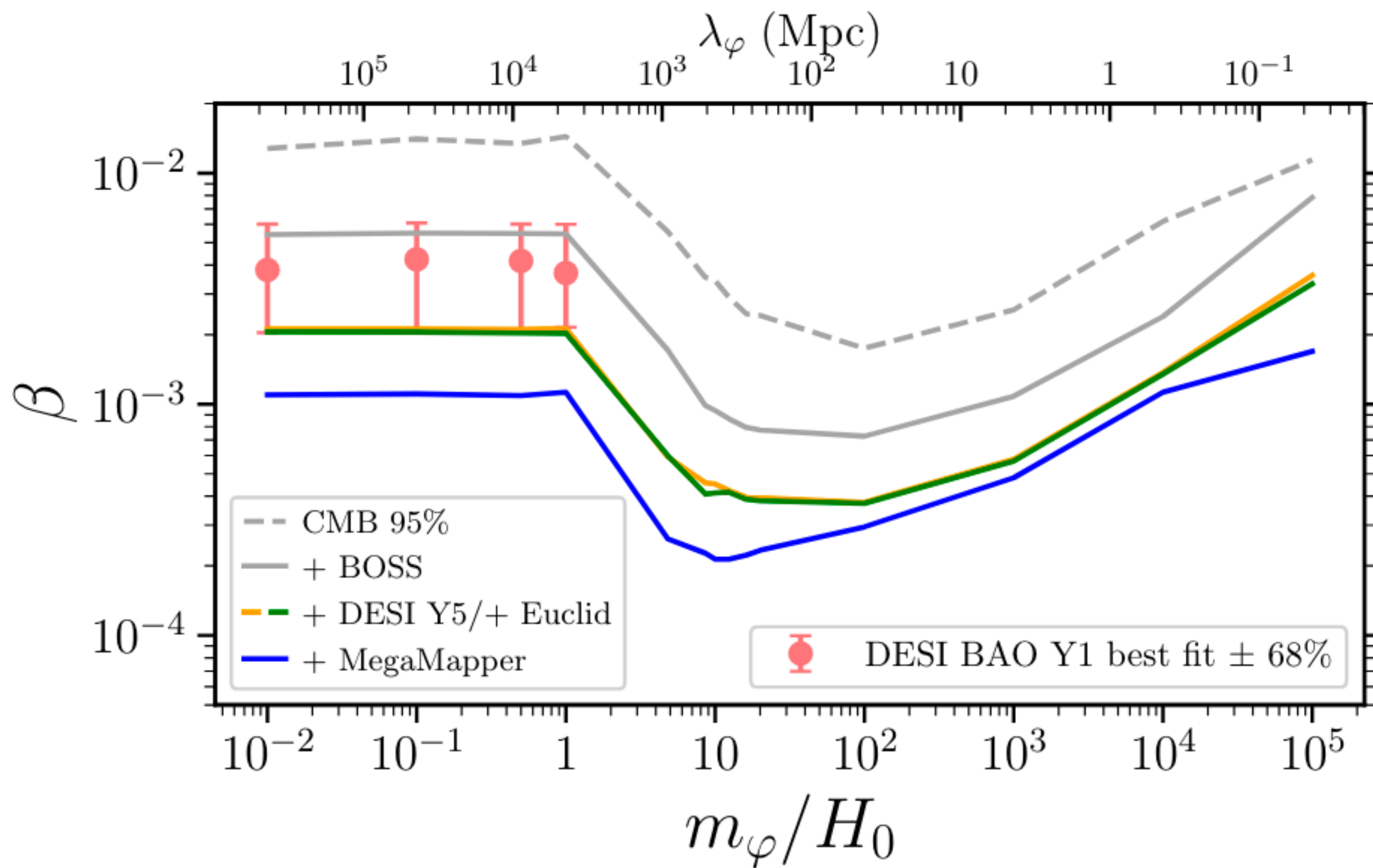
Results



DESI improves bounds by
a factor 2 thanks to better
determination of b_1



Results

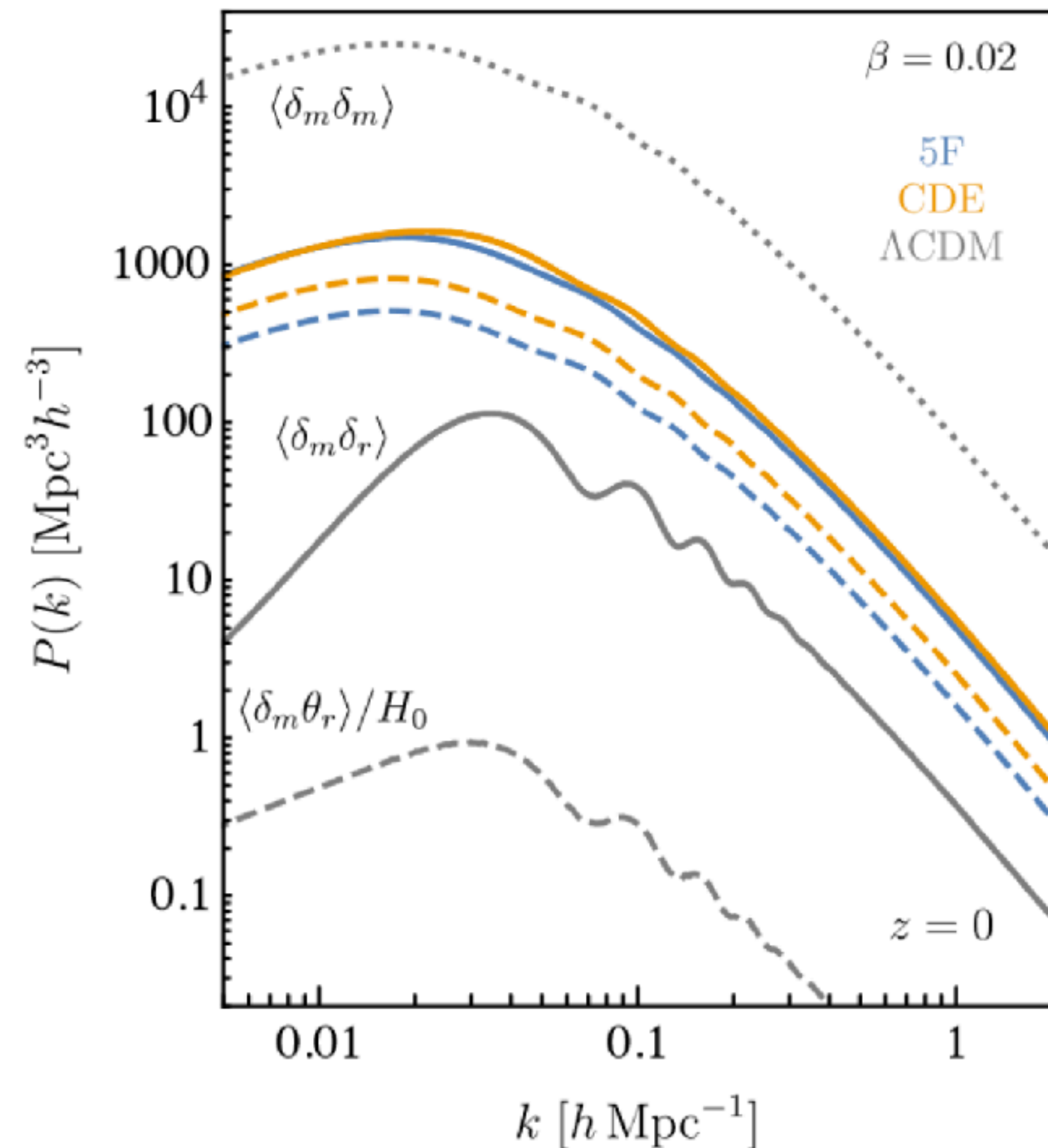


When are relative fluctuations important?

Relative fluctuations $\delta_r \equiv \delta_\chi - \delta_b$

Grow with
scale factor

$$\delta_r(a) = \frac{5}{3} \beta f_\chi \delta_m^{\Lambda\text{CDM}}(a)$$



When are relative fluctuations important?

Relative fluctuations $\delta_r \equiv \delta_\chi - \delta_b$

Grow with
scale factor

$$\delta_r(a) = \frac{5}{3} \beta f_\chi \delta_m^{\Lambda\text{CDM}}(a)$$

New bias

$$\delta_g \supset b_r \delta_r + b_{\theta r} \theta_r + \dots$$

When are relative fluctuations important?

Relative fluctuations $\delta_r \equiv \delta_\chi - \delta_b$

Grow with
scale factor

$$\delta_r(a) = \frac{5}{3} \beta f_\chi \delta_m^{\Lambda\text{CDM}}(a)$$

New bias

$$\delta_g \supset b_r \delta_r + b_{\theta r} \theta_r + \dots$$

New non-linear
structures

$$\delta_r(a, \vec{k}) = \beta f_\chi \left(\frac{5}{3} D_m^{\Lambda\text{CDM}}(a) \delta_0(\vec{k}) + \sum_{n=2}^{\infty} D_m^{\Lambda\text{CDM},n}(a) \int \prod_{i=1}^n \frac{d^3 k_i}{(2\pi)^3} \delta_0(\vec{k}_i) \delta^{(3)} \left(\vec{k} + \sum_{i=1}^n \vec{k}_i \right) F_n^{(r)}(\vec{k}_1, \dots, \vec{k}_n) \right)$$

Crucial features: no log enhancement, only linear scaling with f_χ

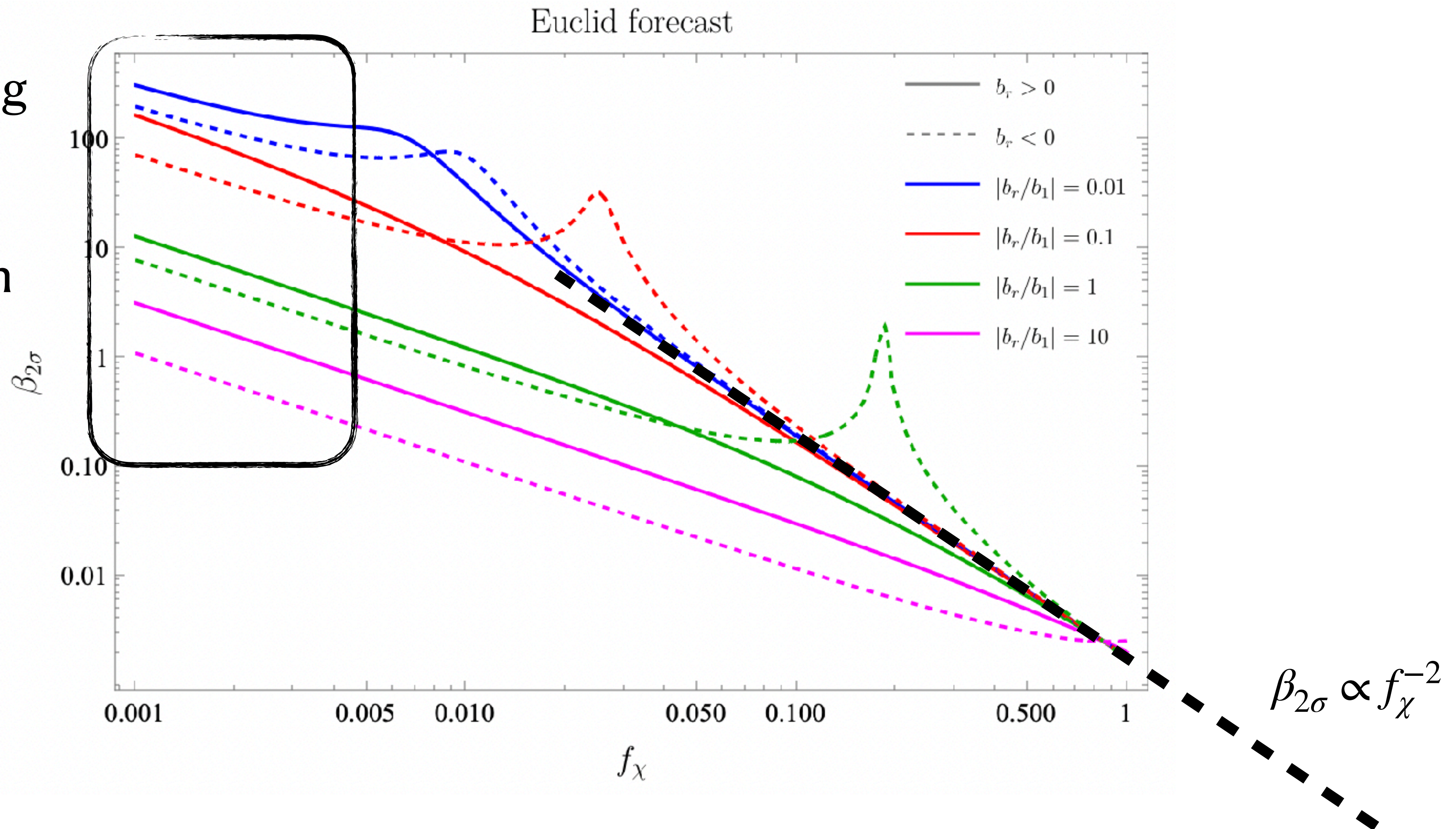
When are relative fluctuations important?

Different scaling

$$\beta_{2\sigma} \propto f_\chi^{-1}$$

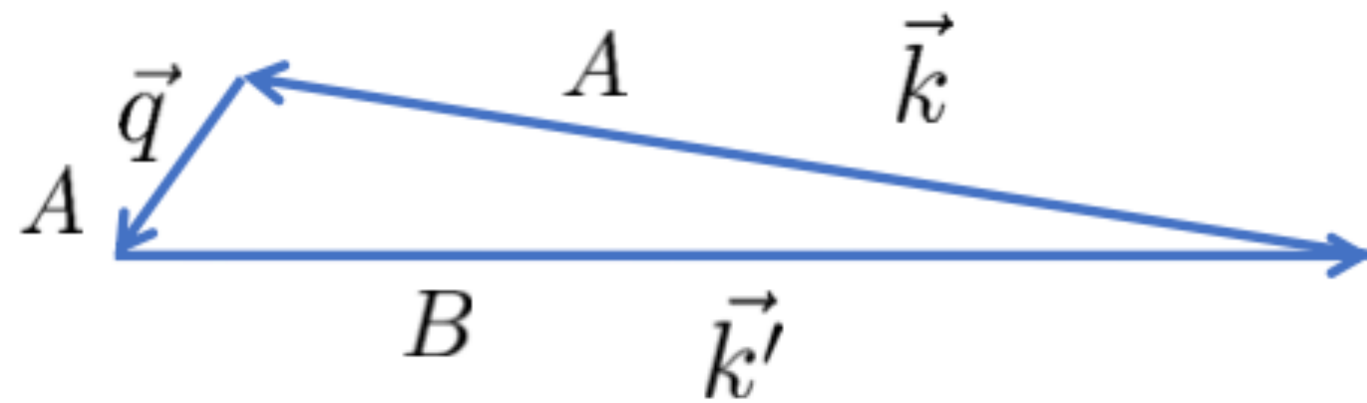
expected when

$$f_\chi \lesssim \frac{b_r}{b_1} \frac{1}{\log}$$



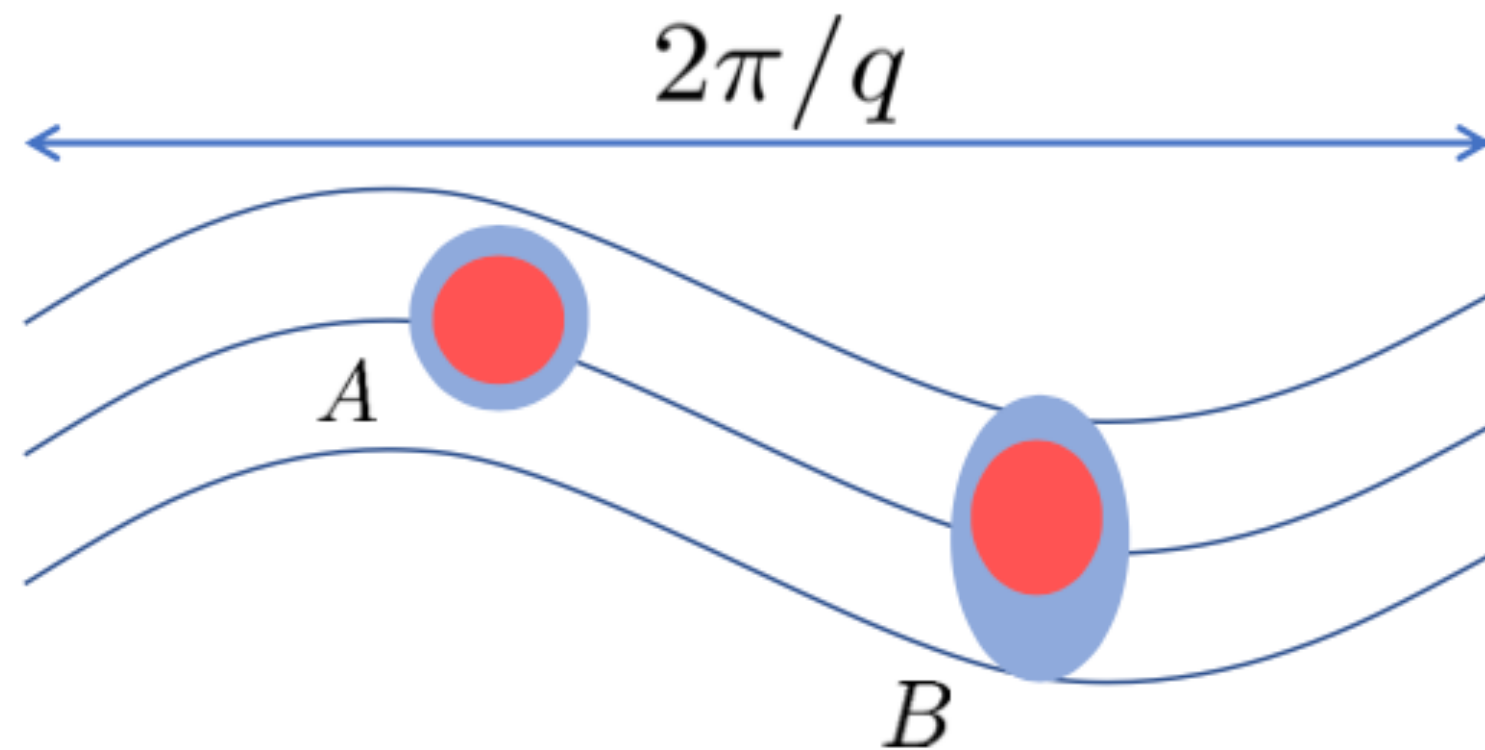
Smoking guns: Pole of the bispectrum

Pole emerging in the squeezed limit of the bispectrum for two different tracers



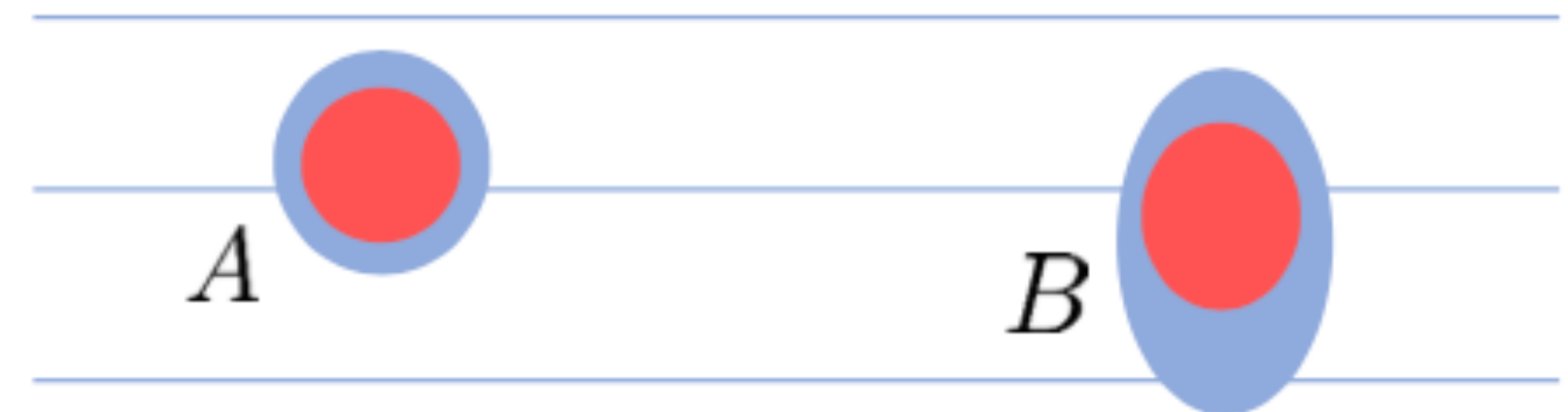
$$\lim_{q \rightarrow 0} \Delta B(q, k, k') \propto \Delta_{AB} \frac{\vec{q} \cdot \vec{k}}{q^2} P^{\text{lin}}(k) P^{\text{lin}}(q)$$

$$\Delta_{AB} = b_1^A (b_1^A b_r^B - b_1^B b_r^A)$$

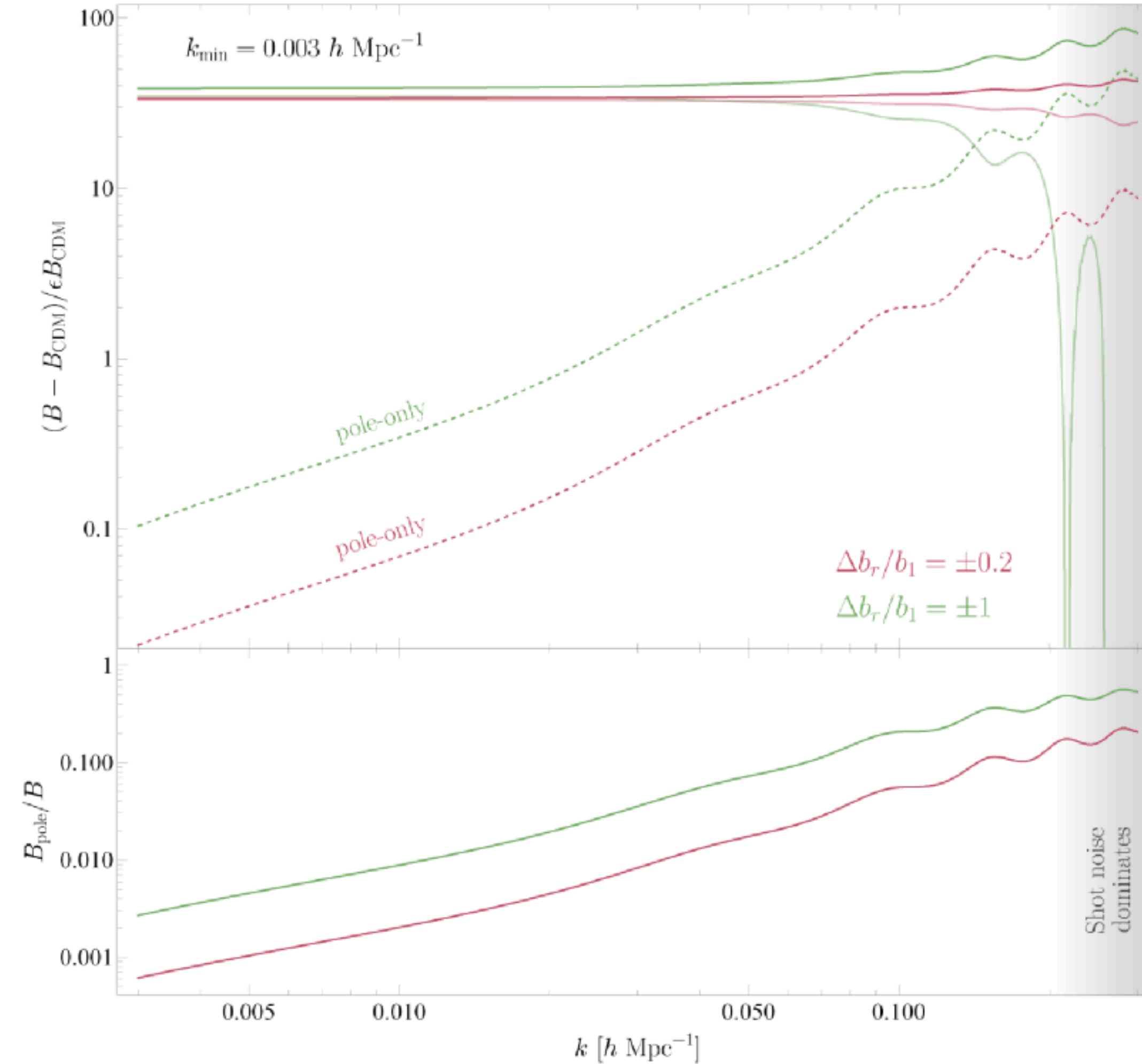


Boost to free-fall system

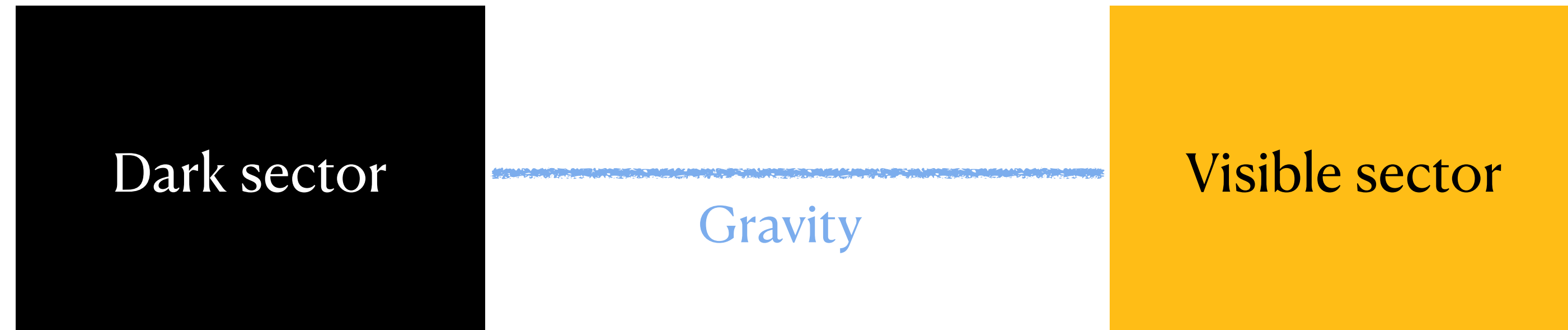
Still feel a non-zero potential!



Smoking guns: Pole of the bispectrum



Can we see in the dark?



Cosmology is the only way to probe completely secluded dark sectors!

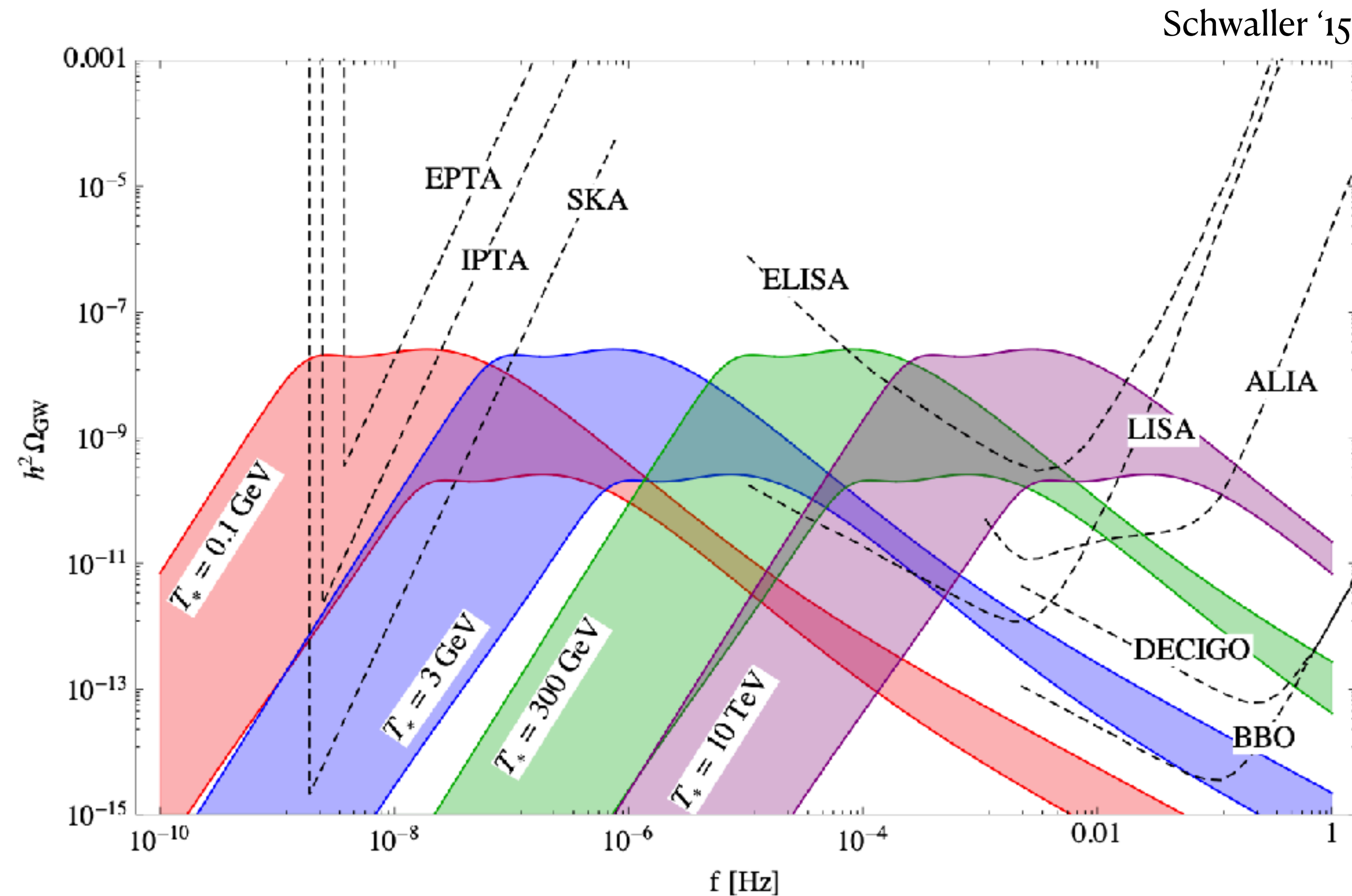
Examples in this talk

Long-range dark forces

Late-time dark phase transitions

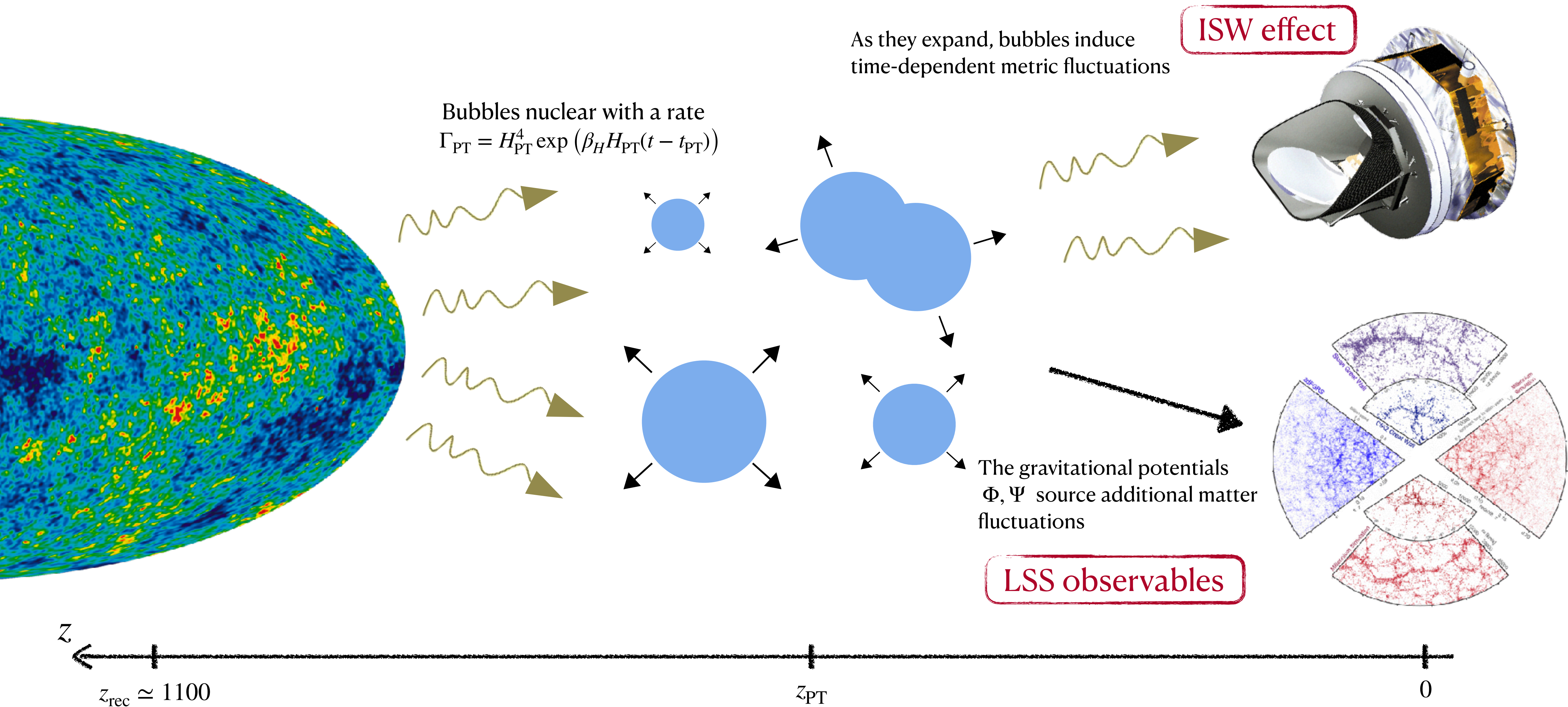
Can we test late-time PT?

PT happening at $T \gtrsim 1$ eV produce GWs in the sensitivity range of future interferometers



What about later PT? Imprints left on cosmological observables!

Dynamics of a Late PT

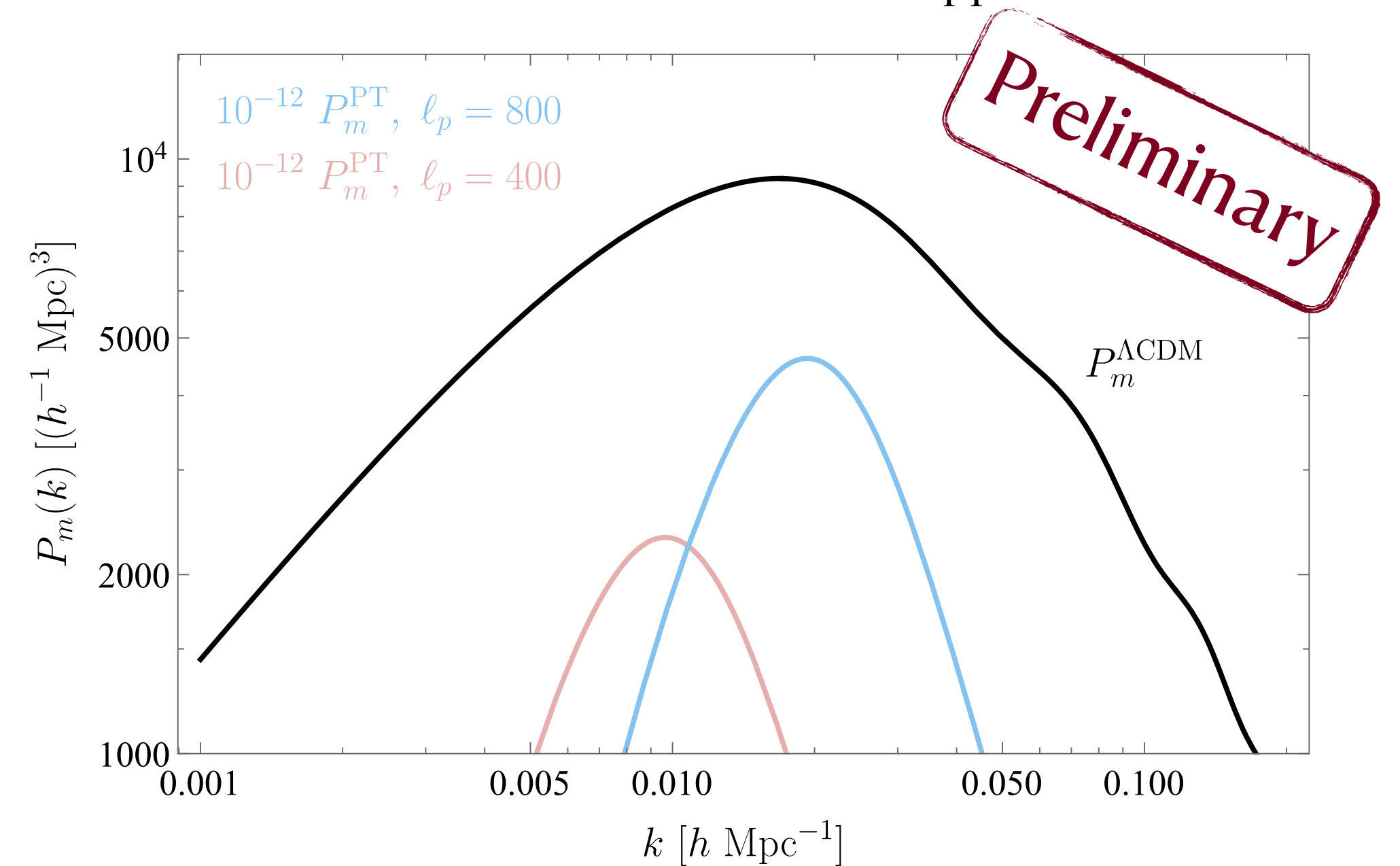
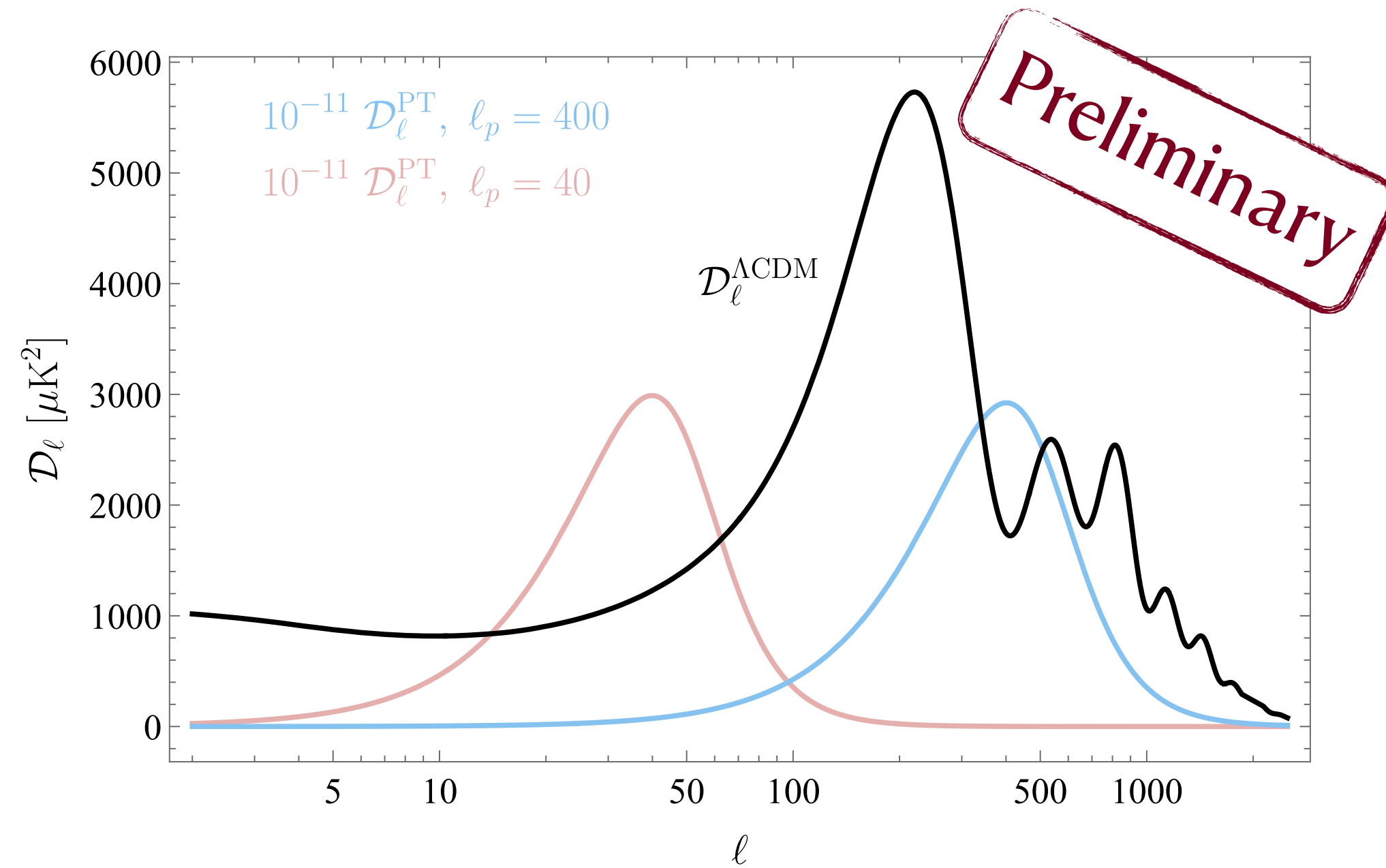


Features of the Signal

Both ISW and matter
power peak at a scale
set by β_H and z_{PT}

$$\ell_p \simeq 4.3 \sqrt{z_{\text{PT}}} \beta_H \sim \frac{\chi_{\text{PT}} H_{\text{PT}} \beta_H}{1 + z_{\text{PT}}}$$

$$k_p \simeq \frac{H_0 \ell_p}{13} \sim \frac{H_{\text{PT}} \beta_H}{1 + z_{\text{PT}}}$$



➡ Negligible degeneracies with cosmological parameters

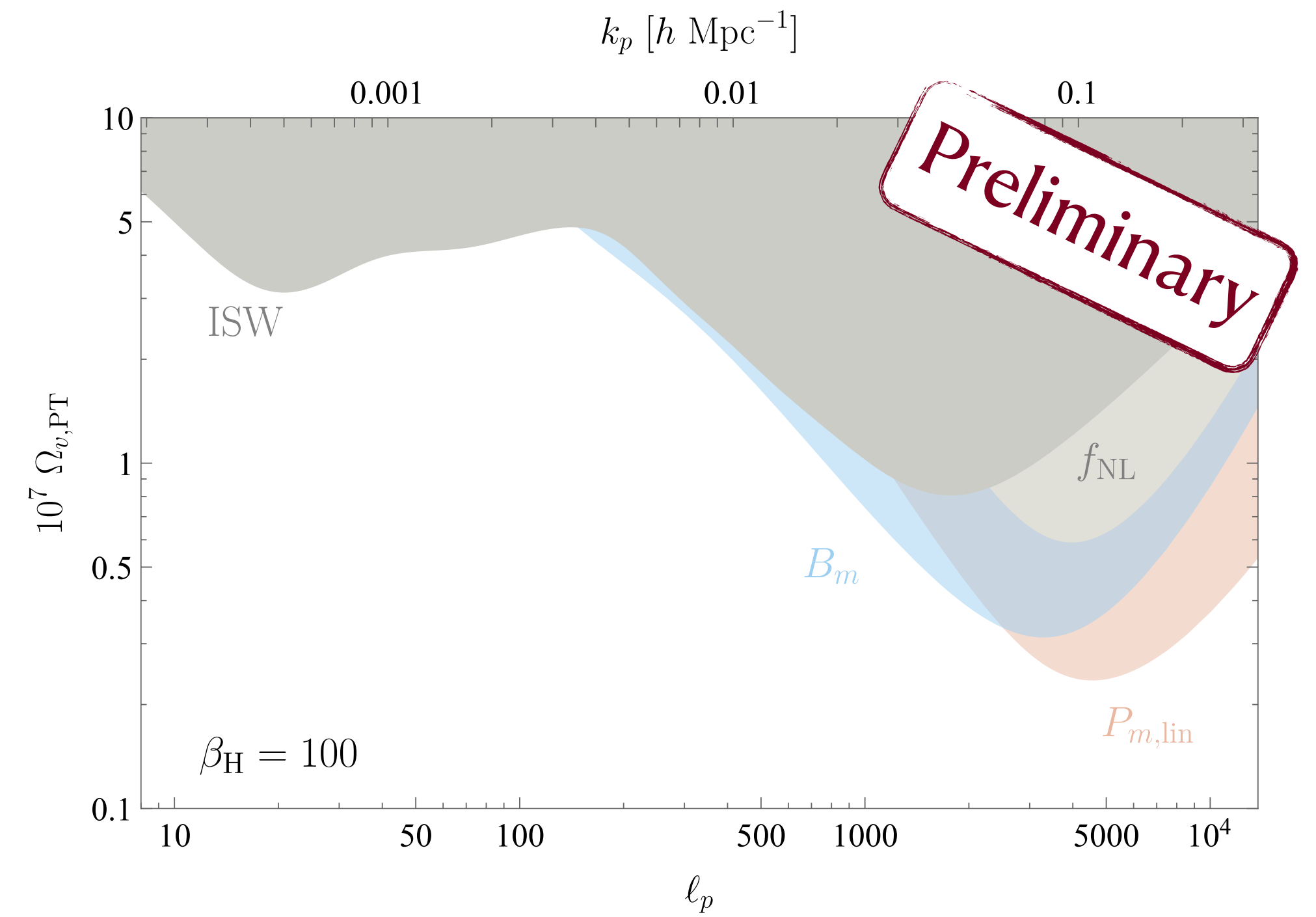
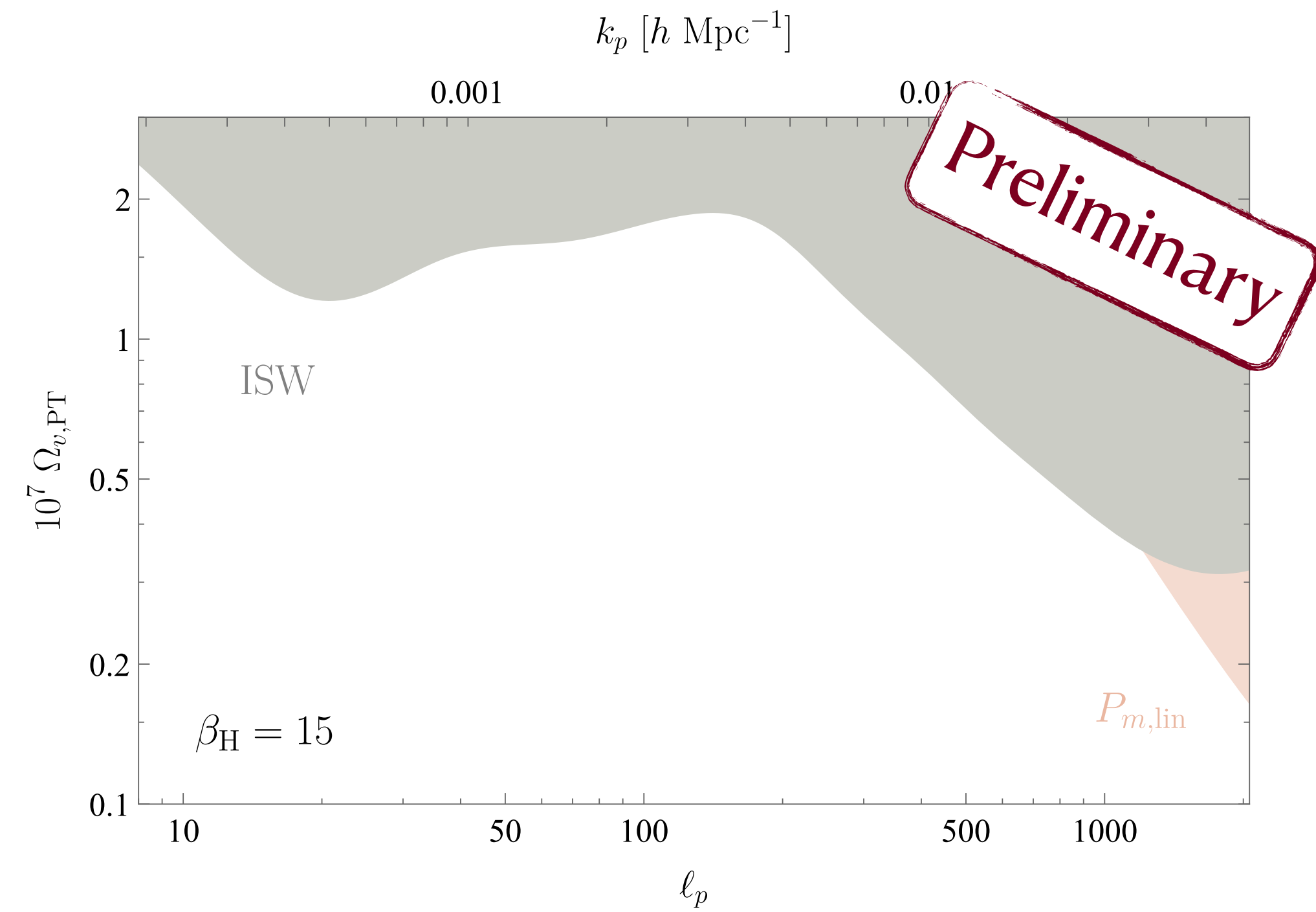
Significant non-Gaussianities
are produced

$$\langle \Phi \Phi \Phi \rangle^2 \approx \langle \Phi \Phi \rangle^3$$

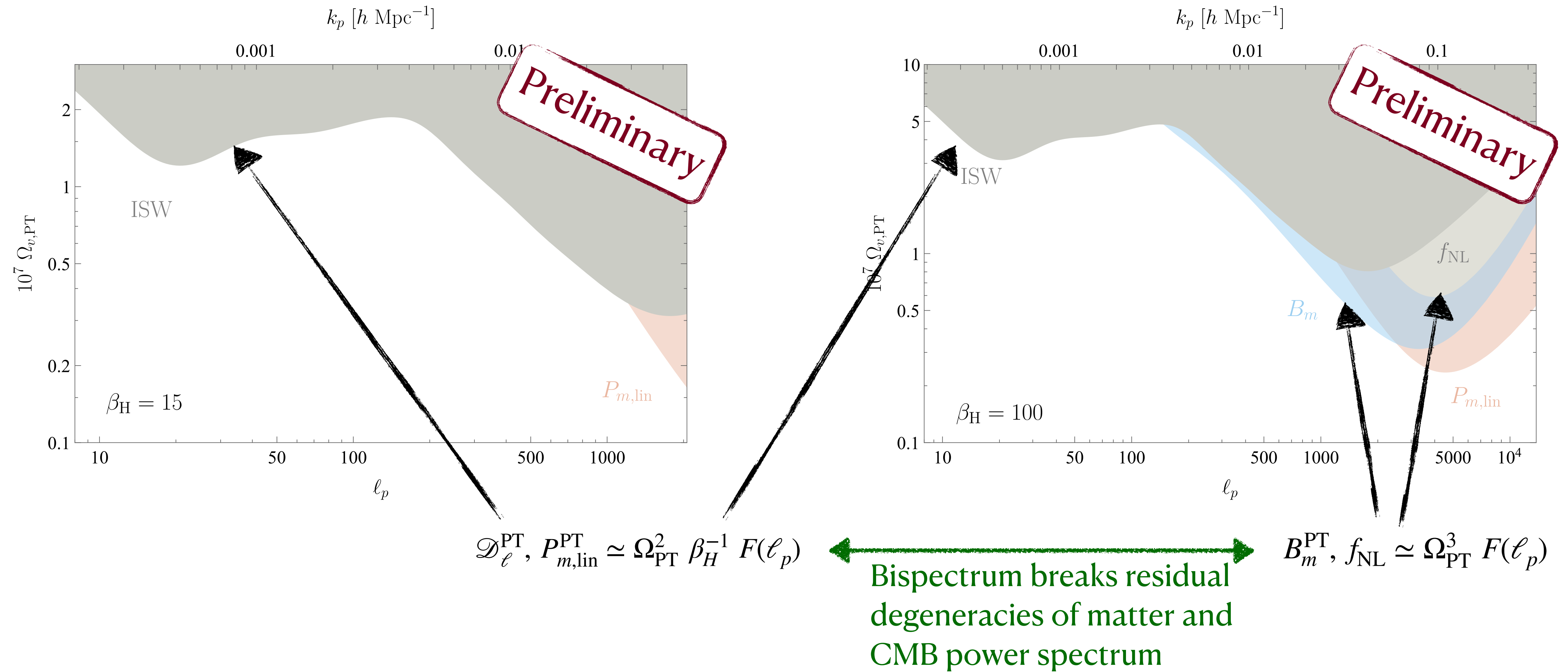


Constraints from bispectrum and f_{NL}

Bounds and Projections

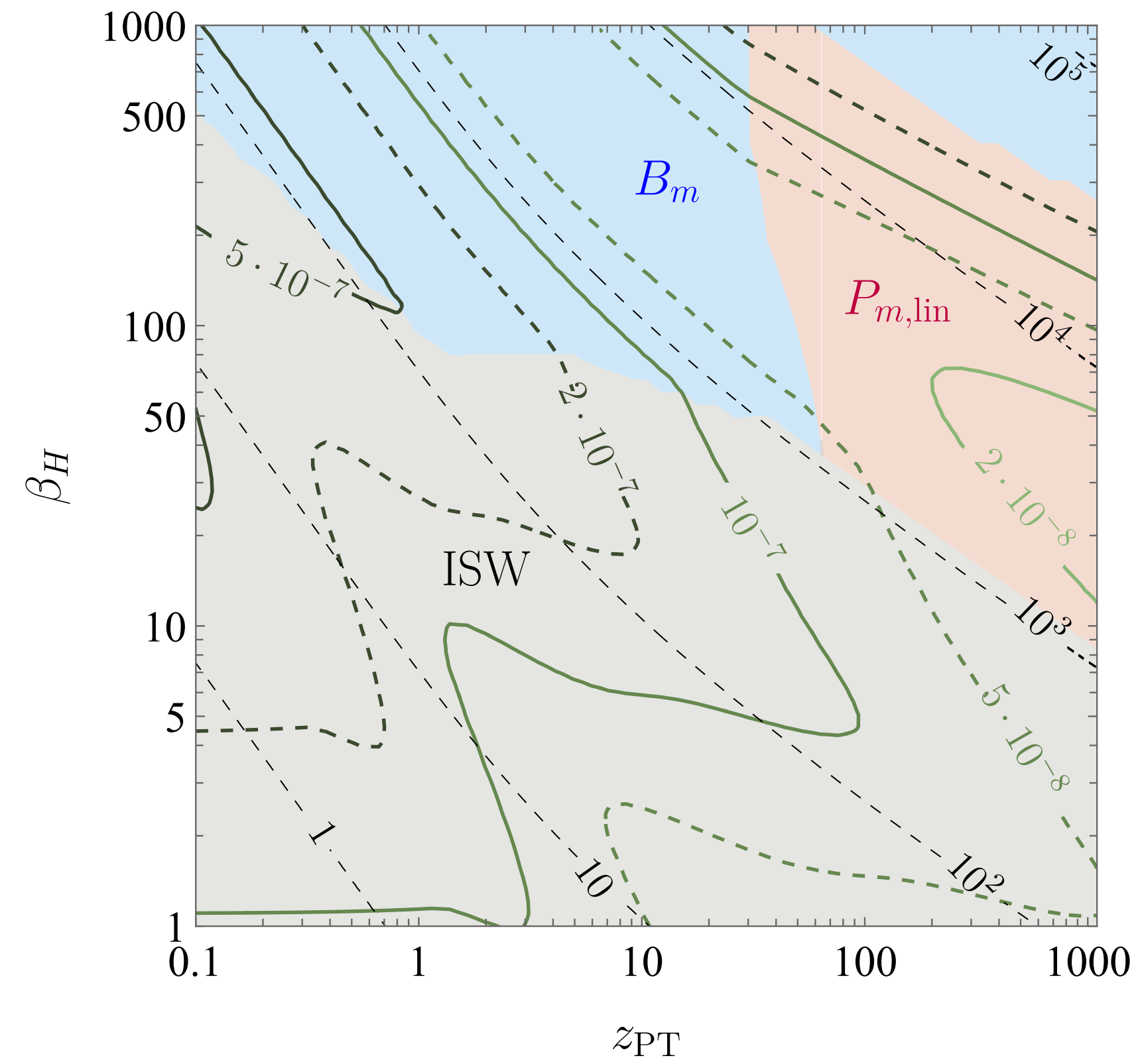


Bounds and Projections

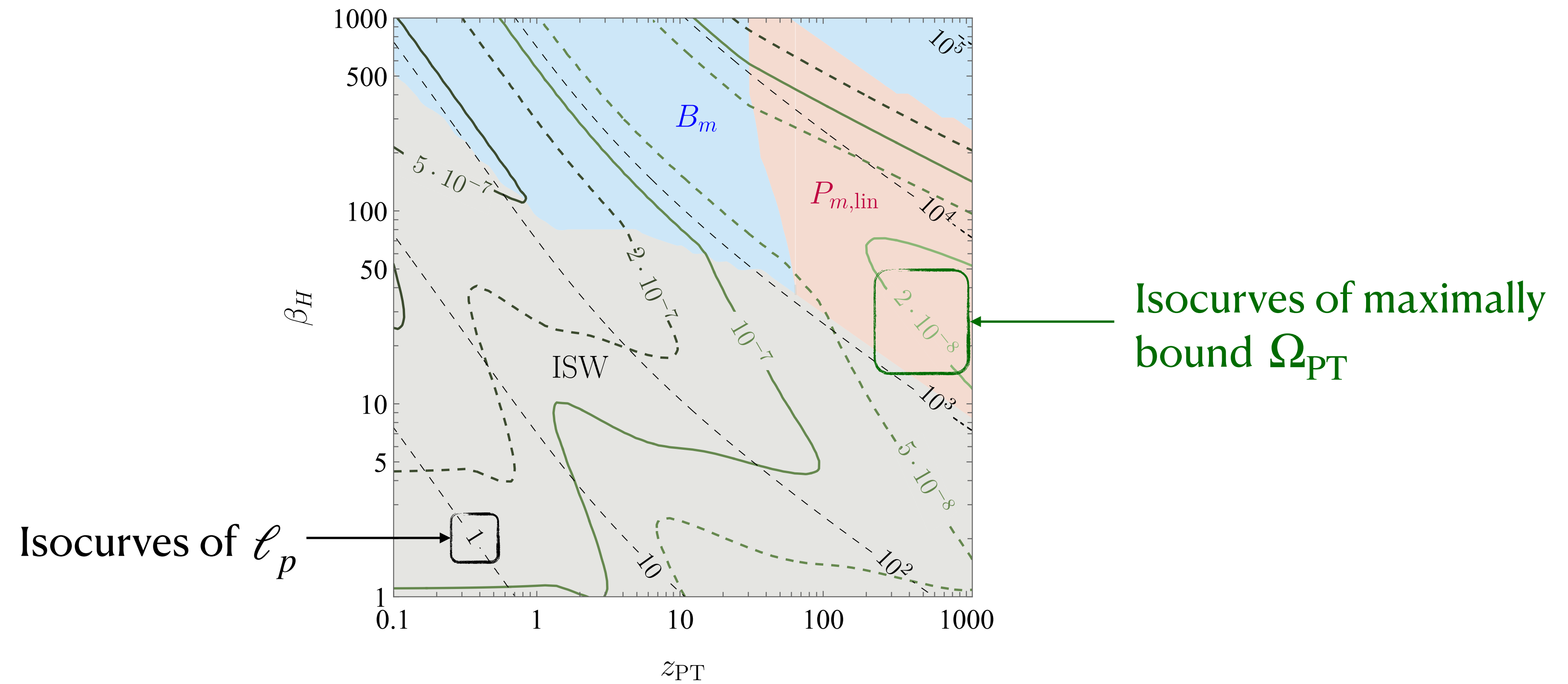


Phase transition can be fully characterized and $\Omega_{PT} \equiv \frac{\Delta \rho_{PT}}{\rho_{cr,PT}}$ can be probed at $\mathcal{O}(10^{-7})$

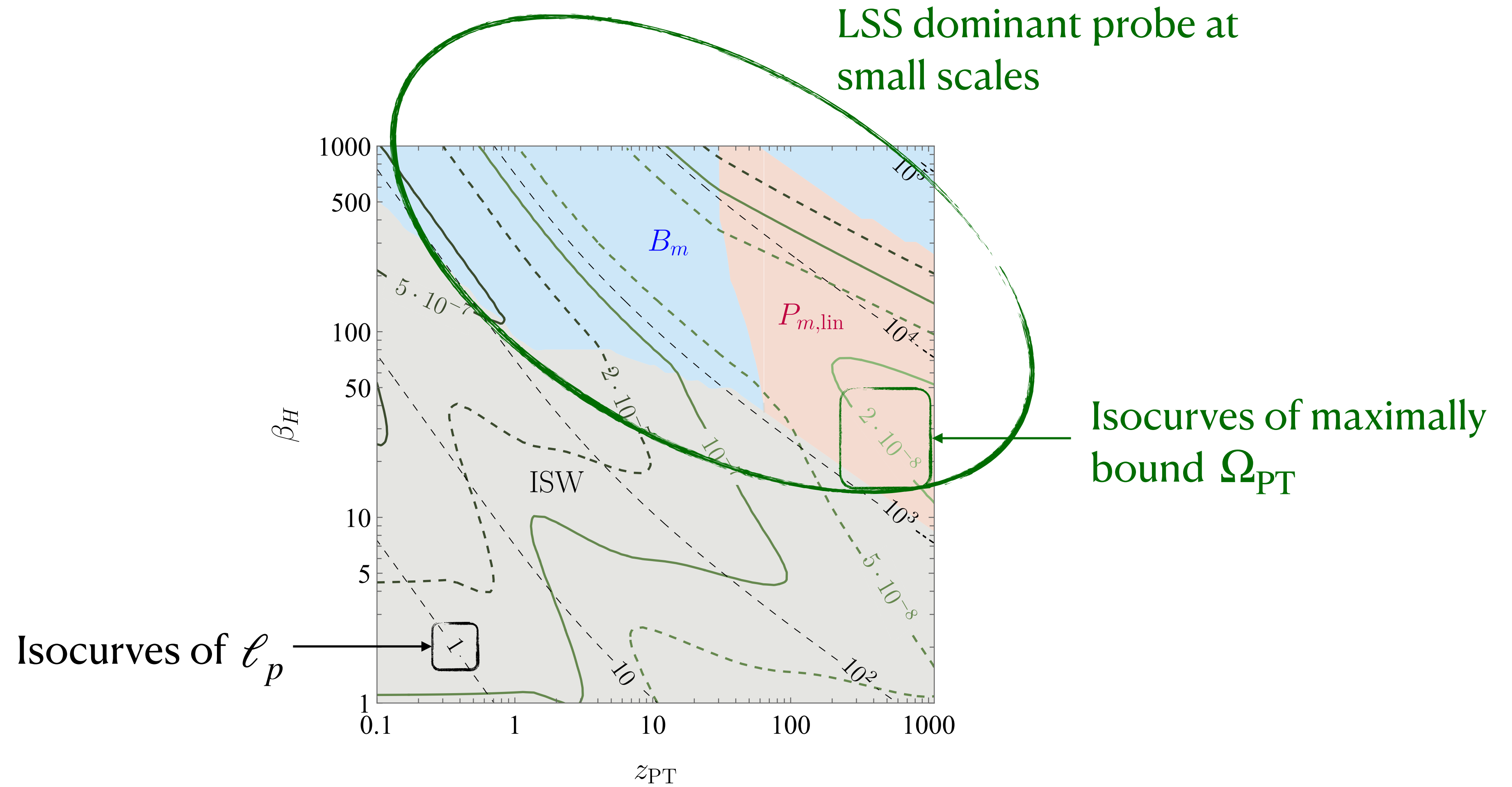
Bounds and Projections



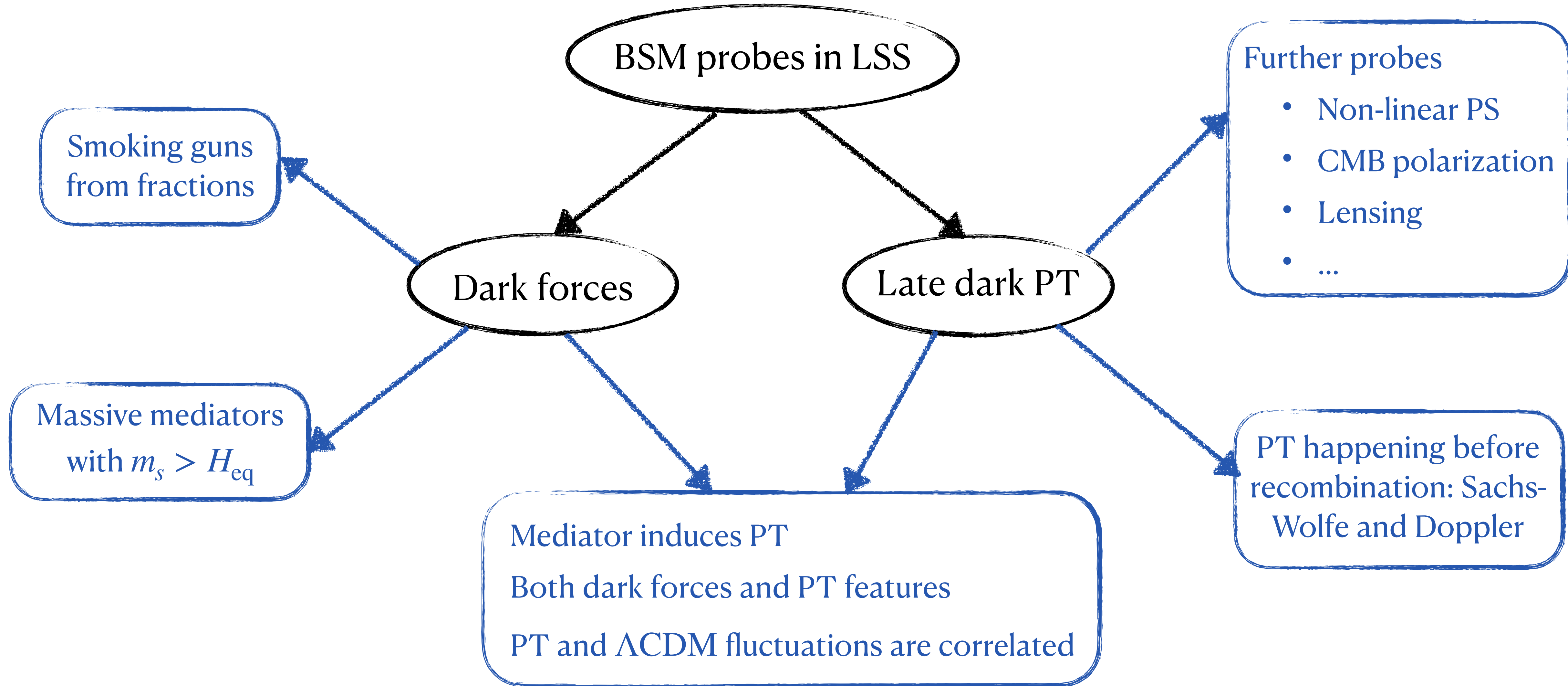
Bounds and Projections



Bounds and Projections

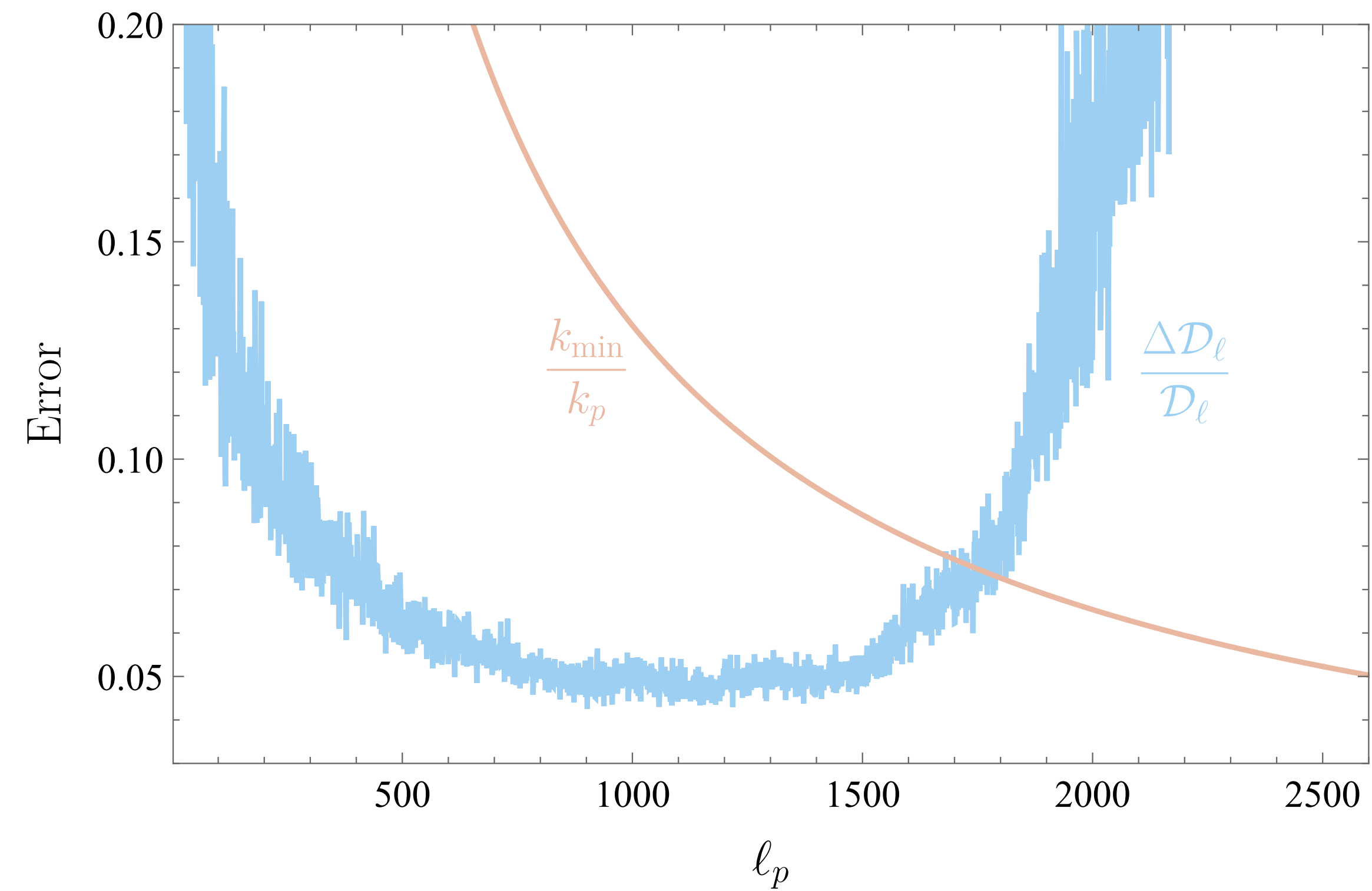


Outlook

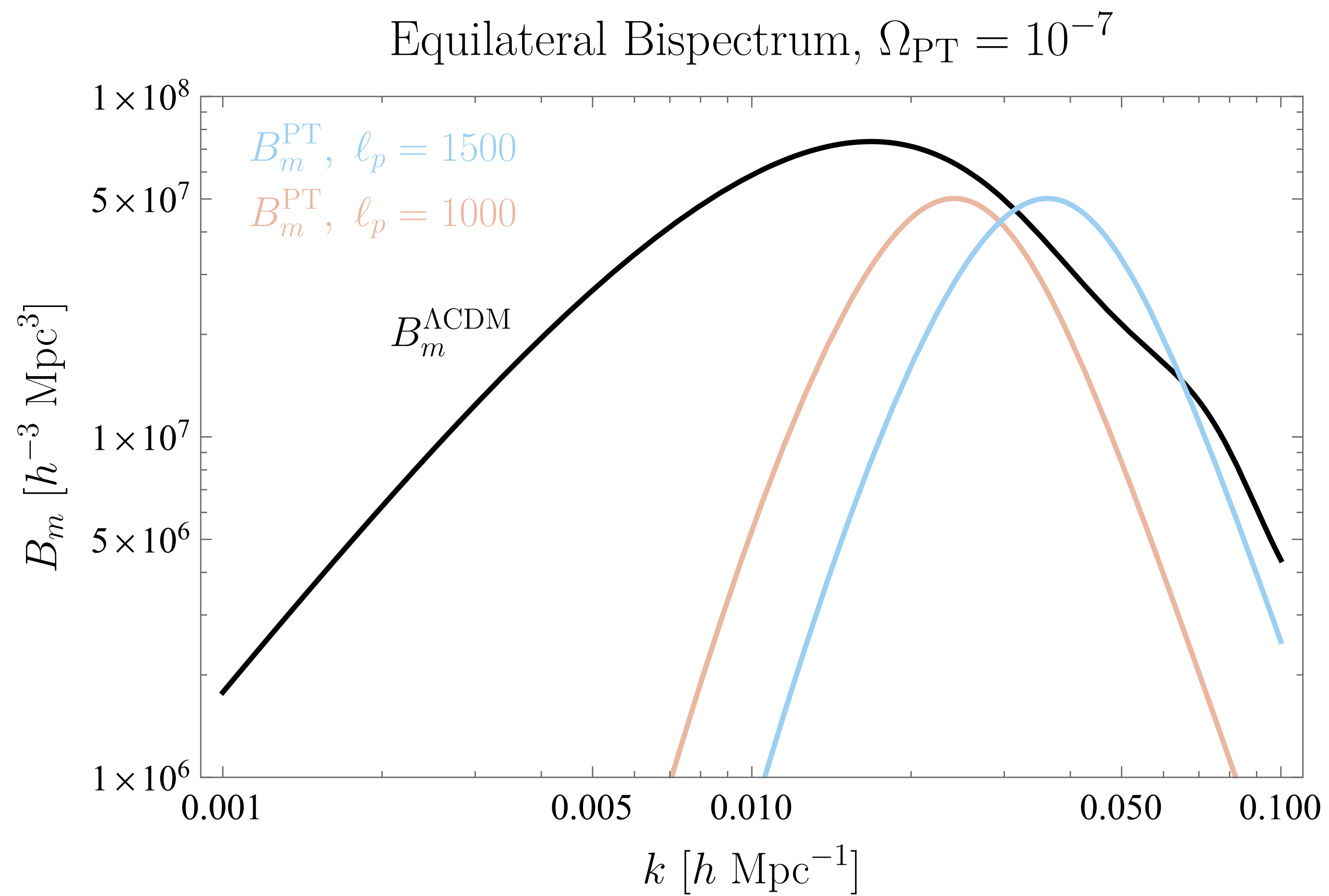


Back-up

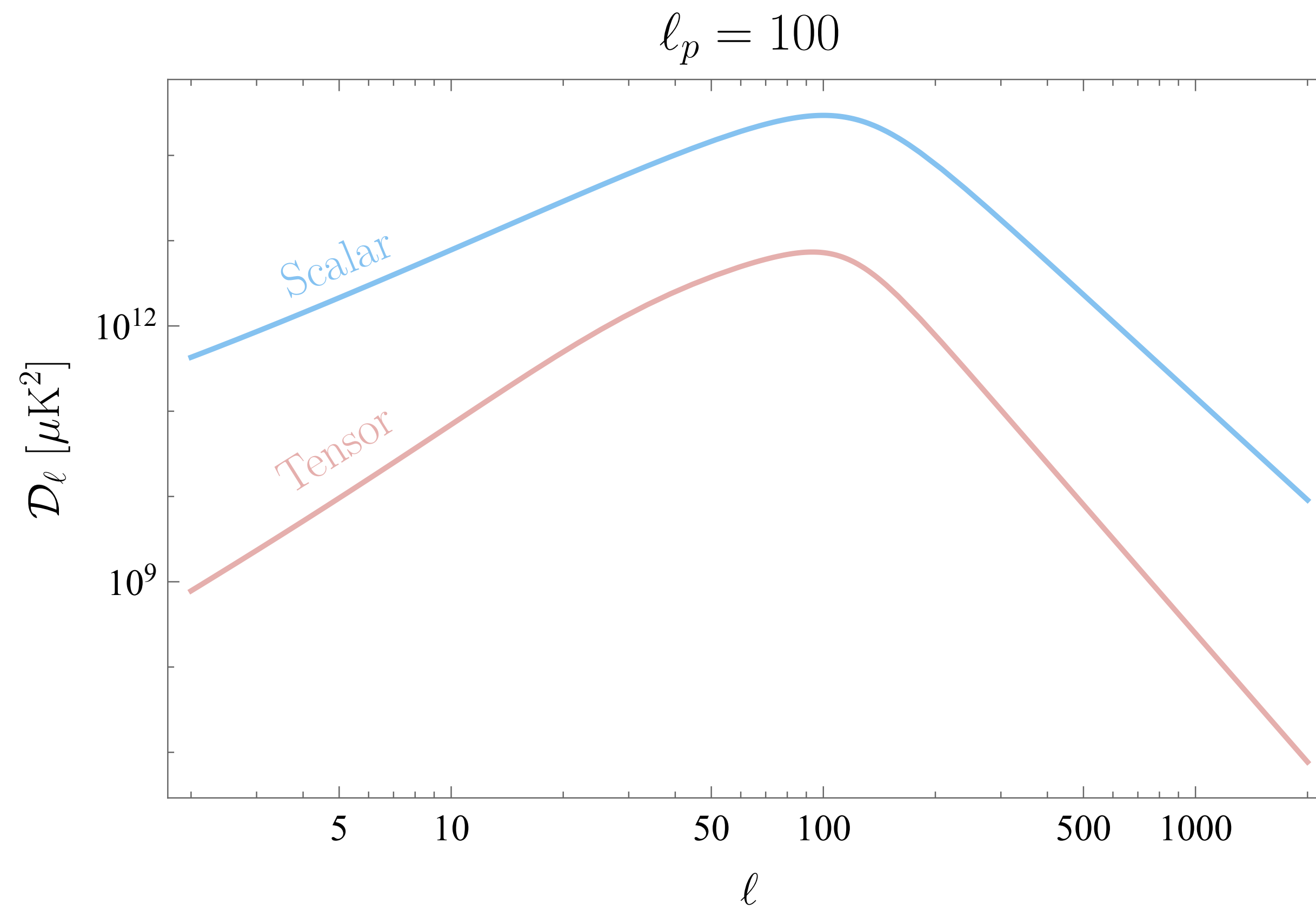
CMB vs. Power spectrum



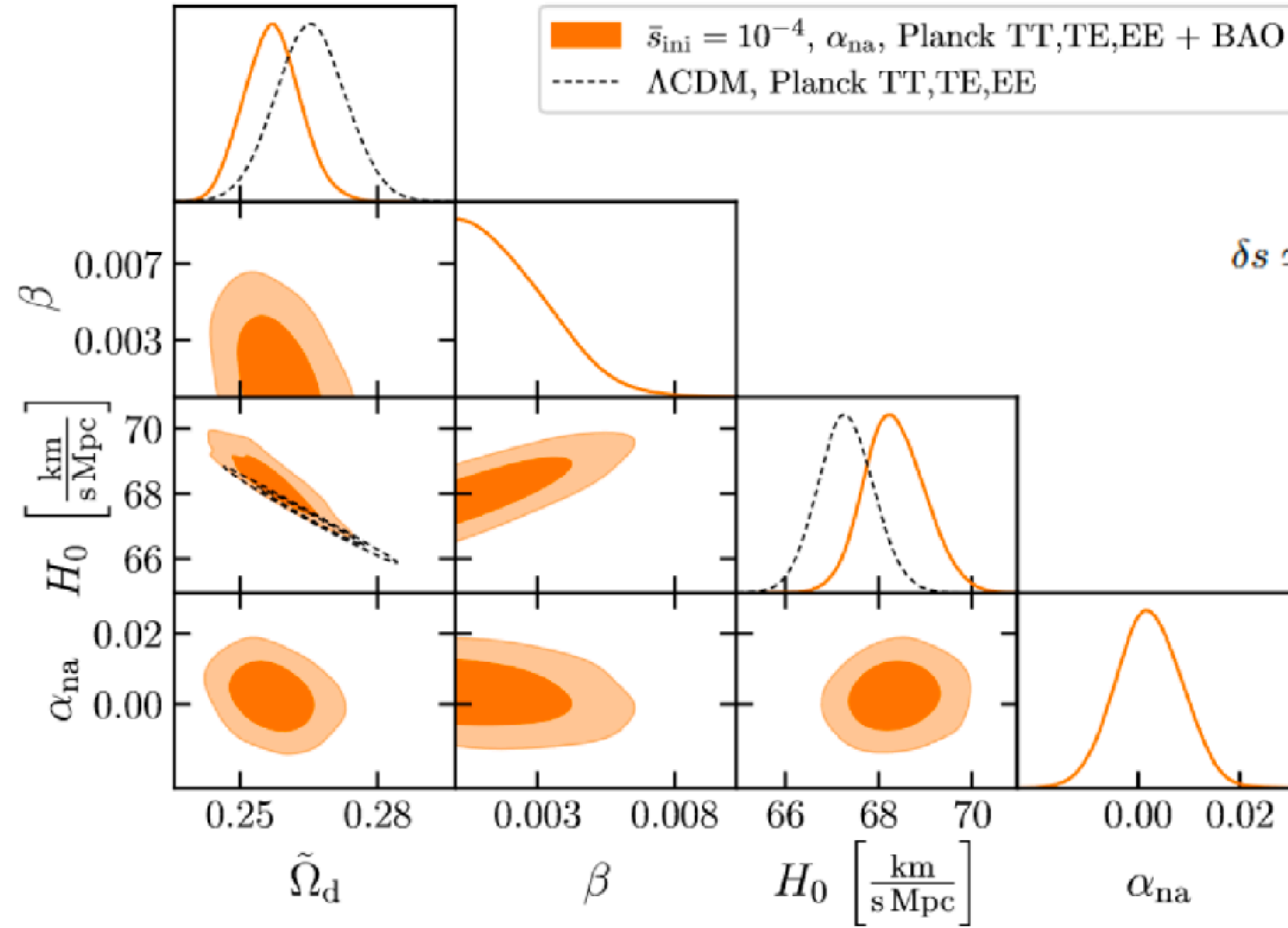
Bispectrum



ISW from GWs



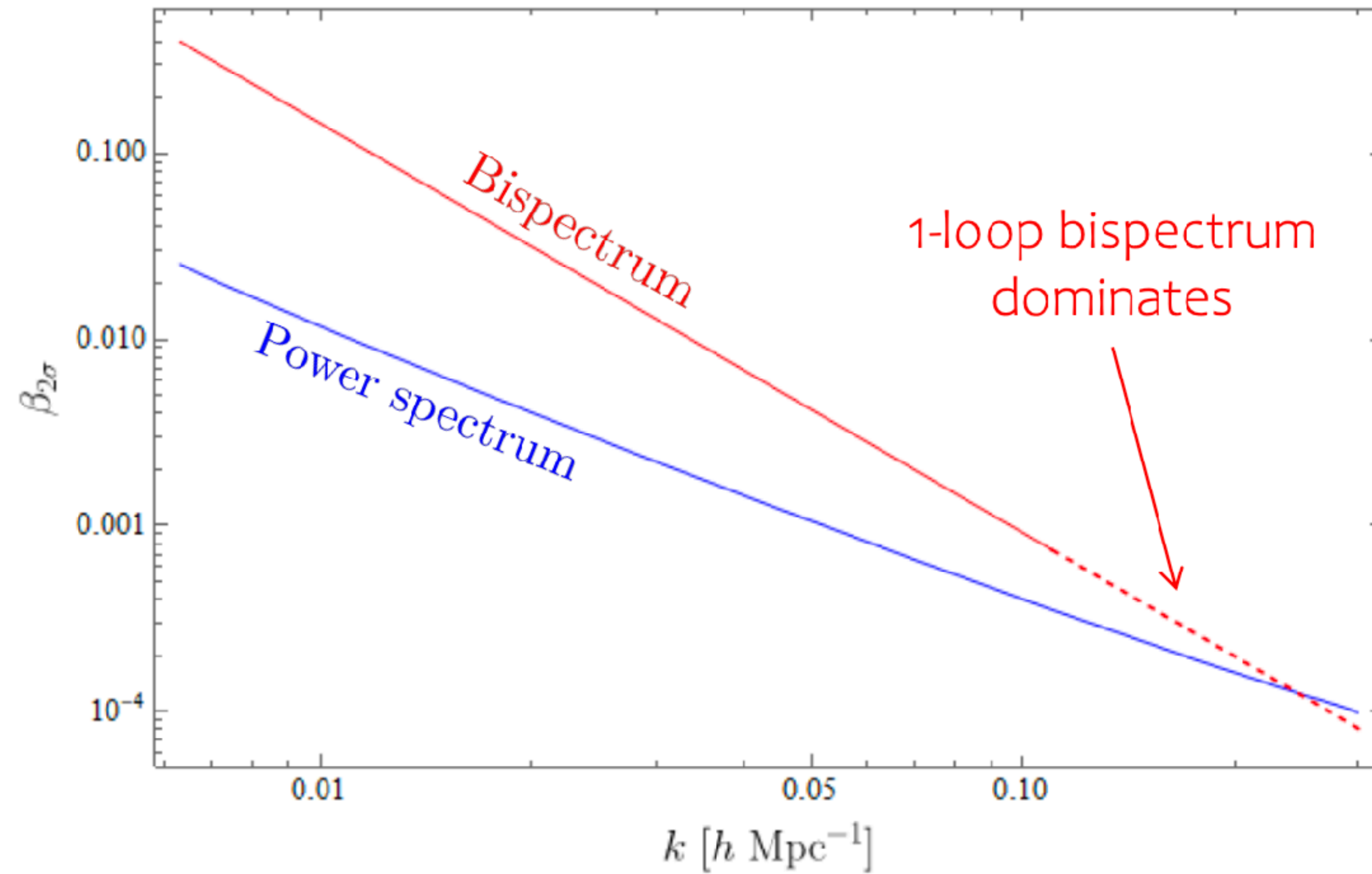
Non-adiabatic ICs



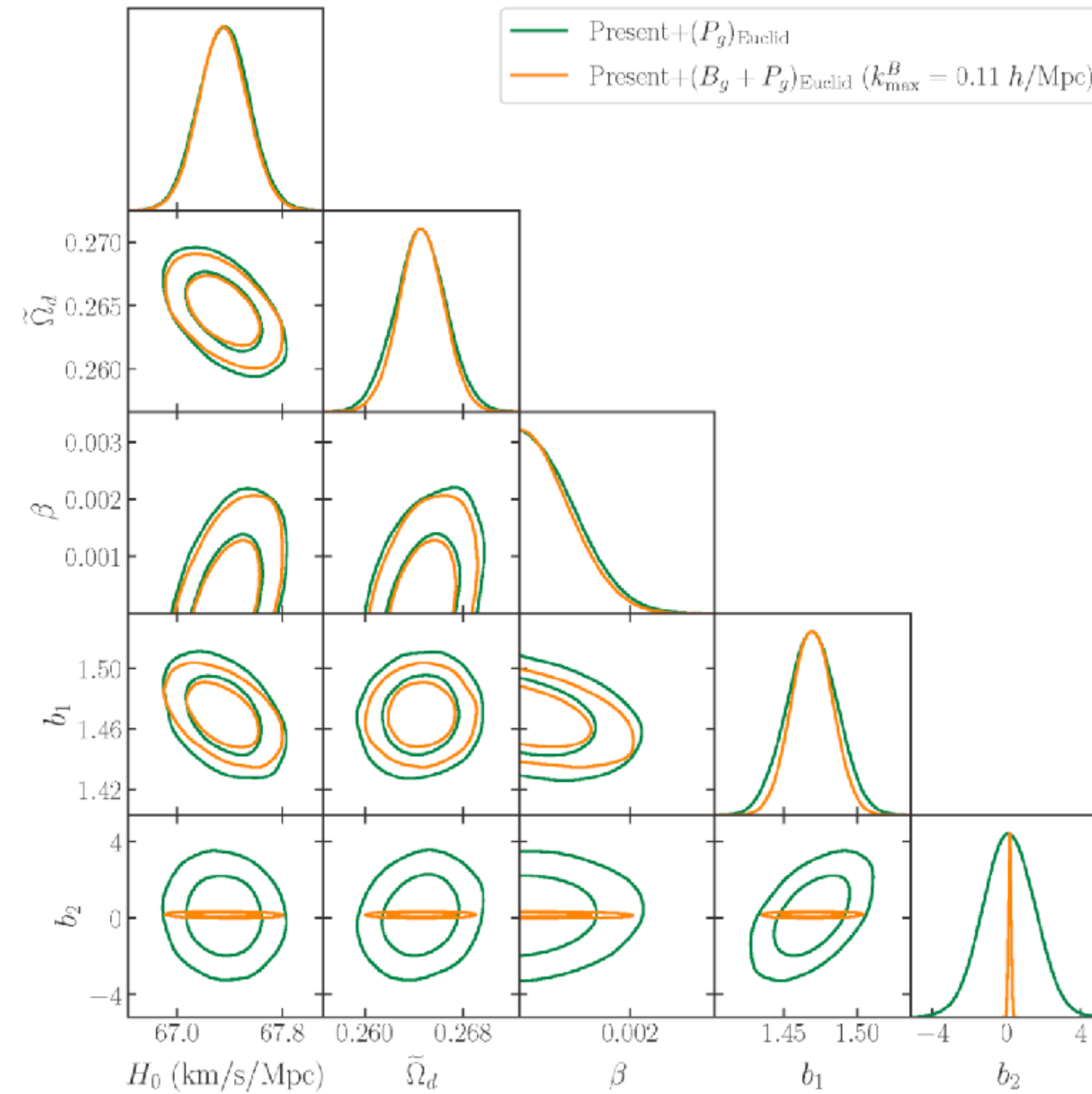
$$\delta s \simeq (\delta s)_{\text{ad}} + \alpha_{\text{na}} \left(1 + \frac{\partial^2 \log m_\chi(s)/\partial s^2}{\partial \log m_\chi(s)/\partial s} \bar{s}' \tau + \mathcal{O}(\bar{s}'^2 \tau^2) \right)$$

$$\theta_\chi \simeq (\theta_\chi)_{\text{ad}} + \frac{\alpha_{\text{na}}}{2} \frac{\partial \log m_\chi(s)}{\partial s} k(k\tau)$$

Bispectrum vs. Power spectrum



Bispectrum vs. Power spectrum

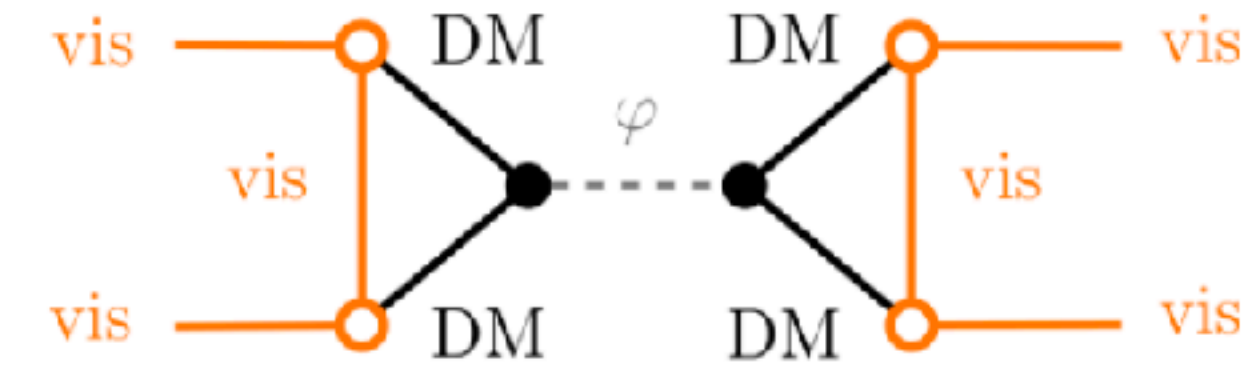


Relations with 5th force experiments

The scalar mediator can couple to the SM if DM does, e.g. the axion

$$\mathcal{L} = \frac{\alpha}{8\pi} \frac{E}{N} \frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu} + \frac{\alpha_3}{8\pi} \frac{a}{f_a} G_{\mu\nu}^a \tilde{G}^{\mu\nu a} - g_D m_a s a^2$$

$$\mathcal{L} = \sqrt{4\pi G_N s} \left(\frac{d_e}{4} F_{\mu\nu} F^{\mu\nu} + \frac{d_g b_3 \alpha_3}{8\pi} G_{\mu\nu}^a G^{\mu\nu a} + \dots \right)$$



$$\left. \begin{aligned} d_e &\simeq \sqrt{\beta} \left(\frac{m_a}{4\pi f_a} \right)^2 \frac{\alpha^2}{16\pi^2} \simeq 2 \times 10^{-10} \sqrt{\frac{\beta}{0.01}} \left(\frac{m_a}{f_a} \right)^2 \leq 2.1 \times 10^{-4} \\ d_g &\simeq \sqrt{\beta} \left(\frac{m_a}{4\pi f_a} \right)^2 \frac{\alpha_3}{8\pi b_3} \simeq 3 \times 10^{-6} \sqrt{\frac{\beta}{0.01}} \left(\frac{m_a}{f_a} \right)^2 \leq 2.9 \times 10^{-6} \end{aligned} \right\} \text{MICROSCOPE (1712.01176)}$$