

1ST IBS-HONAM FOCUS PROGRAM ON PARTICLE
PHYSICS PHENOMENOLOGY, CNBU, JEONJU

*Bound State via Higgs Exchanging
and resonant di-Higgs*

Based on arXiv:1606.01531, Zhaofeng Kang

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0. OUTLINE

◆ basics for bound state

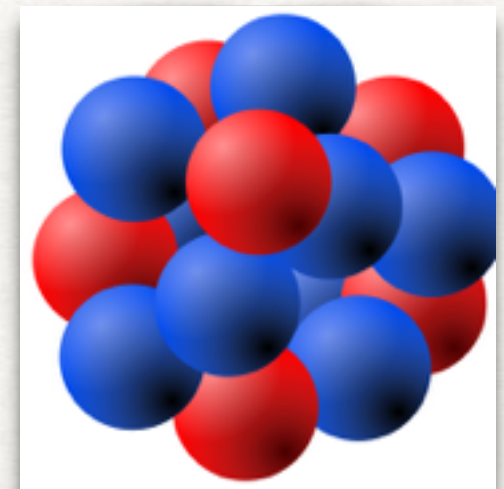
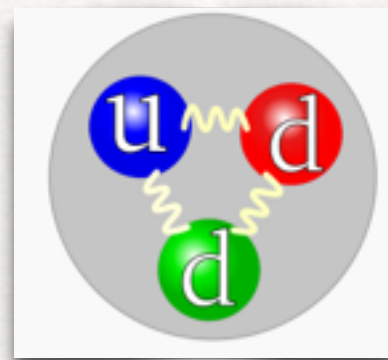
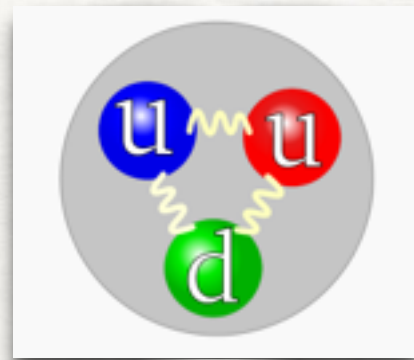
◆ bound state via higgs exchanging

◆ examples and conclusions

1. BASICS FOR BOUND STATE

- Bound states are everywhere in our known Universe

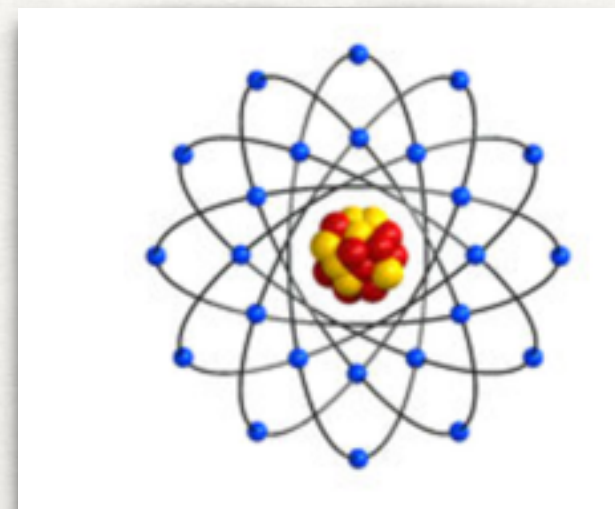
Proton & neutron due to confinement in QCD



Atomic nucleus due to the residual strong force
(**nuclear force**)

Atoms due to electromagnetic force/QED

what about in the
unknown universe? Ex,
dark atom dark matter?



1. BASICS FOR BOUND STATE

- A complicated non-perturbative object in QFT

I) it does not appear in the conventional perturbative calculations
II) Bethe-Salpeter equation furnishes a powerful tool to study bound state in QFT

- Nonrelativistic (NR) limit simplification: Schrodinger equation

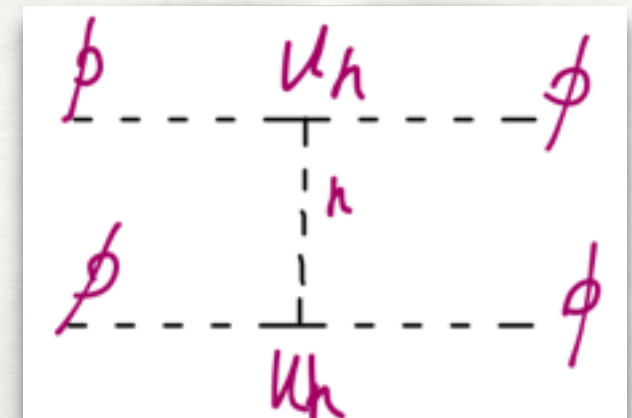
$$\left[-\frac{\nabla^2}{2\mu} + V(\mathbf{r}) \right] \psi_n(\mathbf{r}) = \mathcal{E}_n \psi_n(\mathbf{r})$$

1. i.e., we use NR quantum mechanism to describe the dynamics
2. it can be derived from the Bethe-Salpeter equation

the potential $V(r)$, by exchanging a massive scalar quantum ϕ , for instance the SM Higgs boson h , is the well-known Yukawa potential:

$$-\frac{\alpha_h}{r} e^{-m_h r} \text{ with } \alpha_h = u_h^2 / (16\pi m_\phi^2)$$

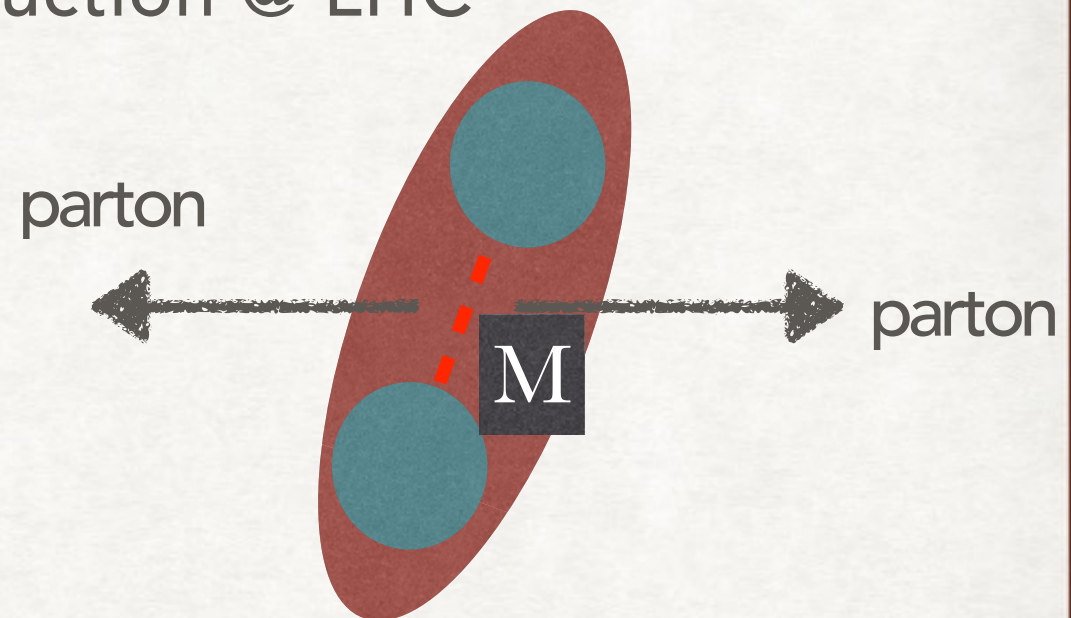
How to solve the equation? later——



1. BASICS FOR BOUND STATE

- Bound state (s-wave ground state) production @ LHC

I. the constitute pairly produced near M
 II. under the condition that the
 constitute is sufficiently long-lived
 III. observable for a sufficiently narrow
 width (assumed hereafter)



$$\hat{\sigma}_{ab \rightarrow M}(\hat{s}) \simeq \frac{2\pi (2J+1) D_M}{D_a D_b} \frac{\Gamma_{M \rightarrow ab}}{M} 2\pi \delta(\hat{s} - M^2) \quad [\times 2 \text{ if } a = b]$$

- Bound state annihilation decay

the dimension of SU(3)_c representation of x

$$\Gamma_{M \rightarrow XY} = \frac{1}{2m_M} \frac{N_c}{1 + \delta_{XY}} \int d\Pi_2 \frac{2}{m_M} |\mathcal{M}_{\phi\phi^* \rightarrow XY}|^2 |\Psi(0)|^2,$$

amplitude of constitute
 pair annihilation into XY

2. B_h : BOUND STATE VIA HIGGS EXCHANGING

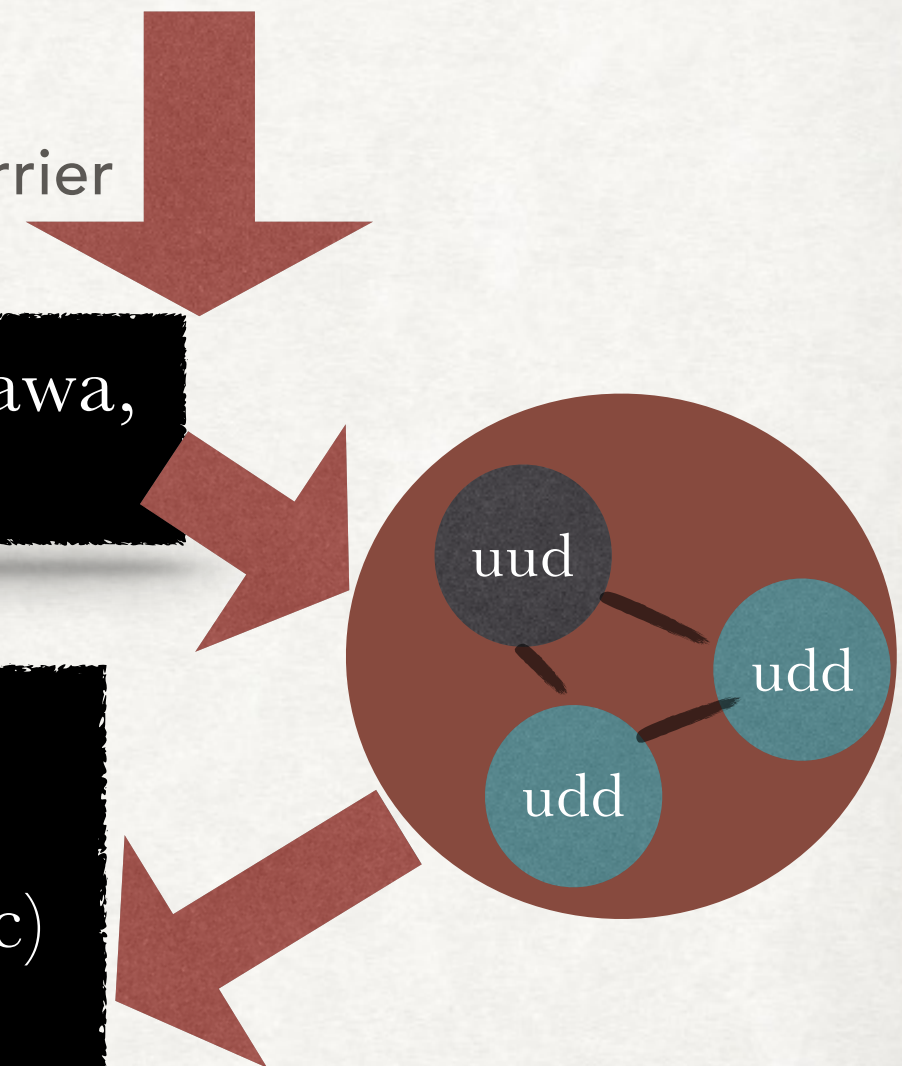
- An illustrating conjecture: Higgs force & bound state B_h

Higgs is just around the weak scale $\sim m_Z, m_W$, relatively light compared to the TeV scale, the hypothetic scale for new physics

In addition, it has spin-0, potential to be a force carrier

it is reminiscent of the π meson of Yukawa, to bound nucleons inside a nucleus

This is exactly the picture in the framework of composite Higgs where the Higgs is a PGSB, and the SM fermions (or other exotic) may be composite at least partially



2. B_h : BOUND STATE VIA HIGGS EXCHANGING

- An illustrating conjecture: Higgs force & bound state B_h

A general study on B_h in new physics, based on the simplified model

$$-\mathcal{L}_h = u_h \phi \phi h |\phi|^2 + m_\phi |\phi|^2$$

- I) a scalar field ϕ for simplicity
- II) discussions can be generalized to constitute with other spins

$$-\frac{\alpha_h}{r} e^{-m_h r} \text{ with } \alpha_h = u_h^2 / (16\pi m_\phi^2)$$

The existence of bound state $D_h = (1/m_h)/a_0 > 0.84$ with $a_0 = 1/(\alpha_h m_\phi/2)$ requires a heavy constitute field ϕ & large α_h ,

$$m_\phi \gtrsim 0.84 \times \frac{2}{\alpha_h} m_h \approx 0.7 \times \left(\frac{0.3}{\alpha_h} \right) \text{ TeV}$$

2. B_h : BOUND STATE VIA HIGGS EXCHANGING

- B_h close to the critical point $D_h \sim 1$

Far from the Column limit, so the previous approximation may be invalid

A new approximation: Yukawa potential \sim scaled Hulthen potential; the later admits analytical solution

$$V_{SH}(r) = -\alpha_h \frac{R_s m_h e^{-R_s m_h r}}{1 - e^{-R_s m_h r}}, \quad R_s \approx 1.75$$

$$|\Psi_n(0)|^2 \approx \frac{\epsilon(R_s/D_h)}{n^3} \frac{1}{\pi a_0^3} = \frac{\left(1 - \frac{R_s^2}{4D_h^2}\right)^{\frac{3}{2}}}{n^3} \frac{\alpha_h^3 m_B^3}{64\pi}$$

R. Dutt, K. Chowdhury, and Y. P. Varshni,
Journal of Physics A 18.9 (1985).

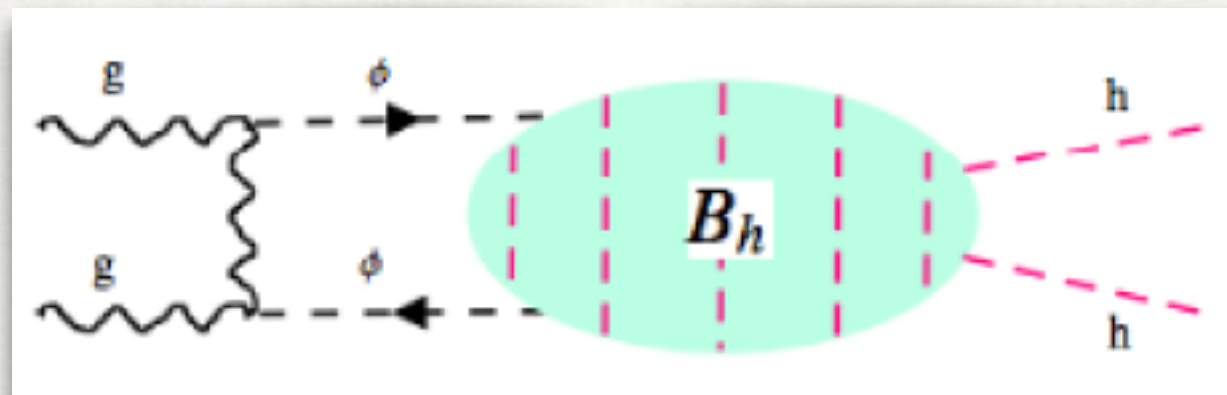
- I) For $D_h \gg 1$, one recovers the well-known Coulomb limit
- II) as $D_h \sim 1$, there is a sizable reduction of wave function at the origin

2. B_h : BOUND STATE VIA HIGGS EXCHANGING

- B_h and resonant di-Higgs signature

B_h can be produced at LHC via GGF if ϕ carries color or ϕ mixes with h

Due to the strong coupling between h and ϕ , B_h dominantly annihilation decays into a pair of Higgs boson



$$\Gamma_{B \rightarrow hh} \approx \frac{N_c}{16\pi} \frac{|\Psi(0)|^2}{m_B^2} \left[\frac{4u_h^4}{\left(\frac{1}{2}m_B^2 - m_h^2\right)^2} \right]$$

- B_h and Higgs signature shifts

$$\delta r_\gamma \approx r_{\text{SM},\gamma} + \text{sign}(u_h) \frac{d(\phi) Q_\phi^2}{12} \sqrt{2\pi\alpha_h} \frac{v}{m_\phi},$$

$$\delta r_g \approx r_{\text{SM},g} + \text{sign}(u_h) C(\phi) \sqrt{2\pi\alpha_h} \frac{v}{m_\phi},$$

3. STOPONIUM: BOUND STATE OF STOP

- A large soft trilinear term and a large stop mixing angle....

$$m_{stop}^2 \approx \begin{pmatrix} m_{RR}^2 & m_t X_t \\ m_t X_t & m_{LL}^2 \end{pmatrix} \quad X_t = A_t - \mu \cot \beta \approx A_t$$

$$-\mathcal{L}_{soft} \supset y_t A_t \tilde{t}_L \left(v_u + \frac{h}{\sqrt{2}} \right) \tilde{t}_R^* + h.c.,$$

- I. large A_t term is good for radiatively lifting m_h
- II. also good for large left-right stop mixing

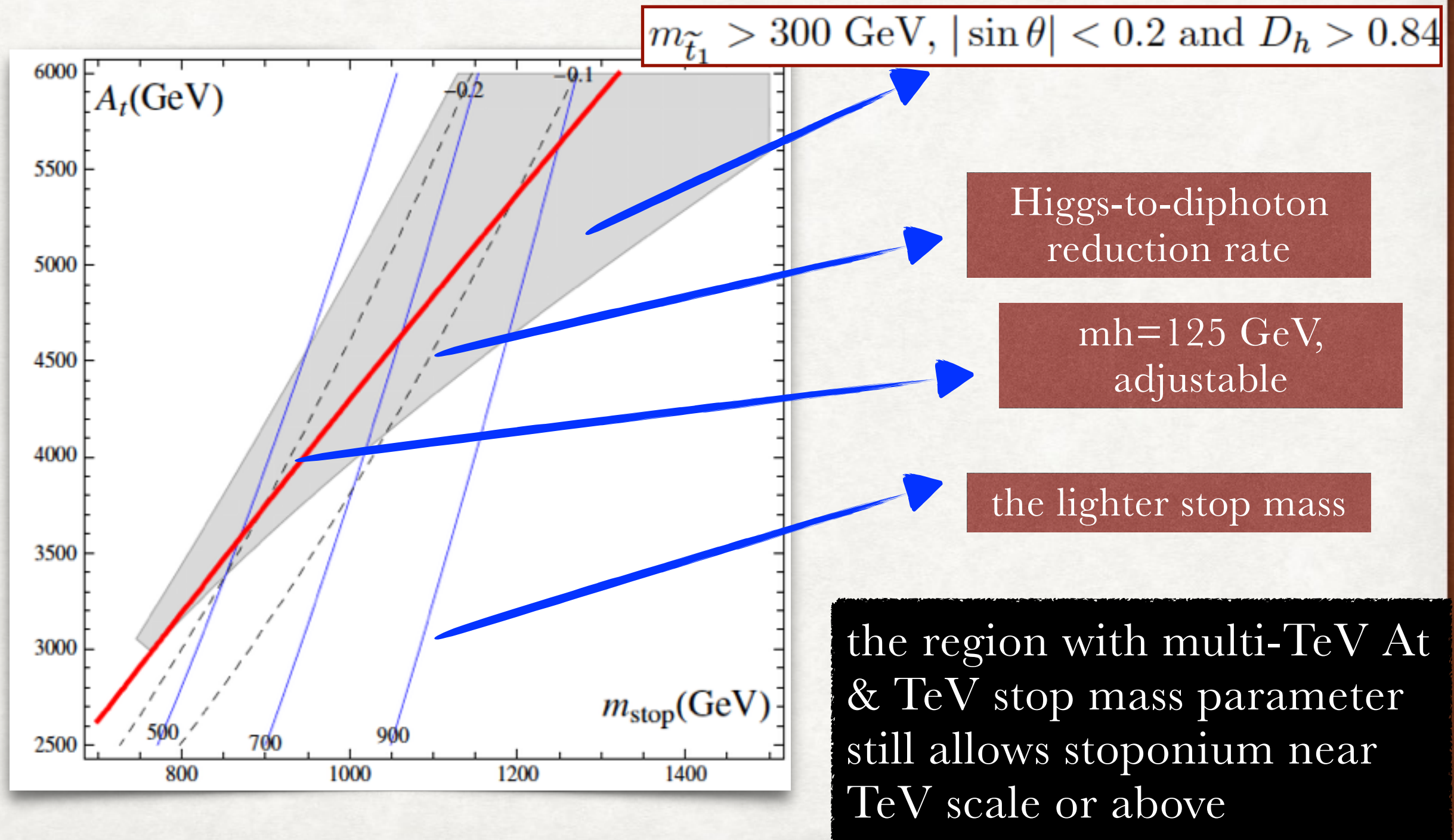
$$-\mathcal{L}_{h\tilde{t}_1\tilde{t}_1} = u_{h\tilde{t}_1\tilde{t}_1} h |\tilde{t}_1|^2 \quad \text{with} \quad u_{h\tilde{t}_1\tilde{t}_1} \approx \frac{m_t A_t}{\sqrt{2}v} \sin 2\theta_t$$

- The lighter stop two-body decay can be suppressed either by the degenerate with LSP or gravitino being the LSP (says in GMSB)
- Sbottom sector with a large μ -term from unnatural SUSY

$$\mu H_u H_d + y_b Q_3 H_d U_3^c \Rightarrow \frac{m_b \tan \beta}{\sqrt{2}v} \mu \sin 2\theta_b h |\tilde{b}_1|^2.$$

3. STOPONIUM: BOUND STATE OF STOP

- Is stoponium still possible?



3. INERT HIGGS DOUBLET FROM RADIATIVE SEESAW

- Higgs portal term with a large dimensionless coupling $\lambda|X|^2|\Phi_2|^2$

Can X be dark matter? No! direct detection rules it out!

$$\sigma_{\text{SI}}^n \approx \frac{4\alpha_h}{v^2} \frac{m_n^4}{m_h^4} \left(\sum_q f_{T_q}^{(n)} \right)^2 = 3.6 \times 10^{-6} \times \left(\frac{\alpha_h}{0.3} \right) \text{pb},$$

- But scalar X with $\lambda \gg 1$ are well motivated for triggering strong first order phase transition (SF OPT) or classical scale symmetry breaking
- Consider a celebrated model with X=quasi inert Higgs doublet Φ_1 ,

$$-\mathcal{L}_{\text{Ma}} = \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + \frac{\lambda_5}{2} \left[(\Phi_1^\dagger \Phi_2)^2 + h.c. \right] + (y_N \bar{l} \Phi_1 P_R N + c.c.)$$

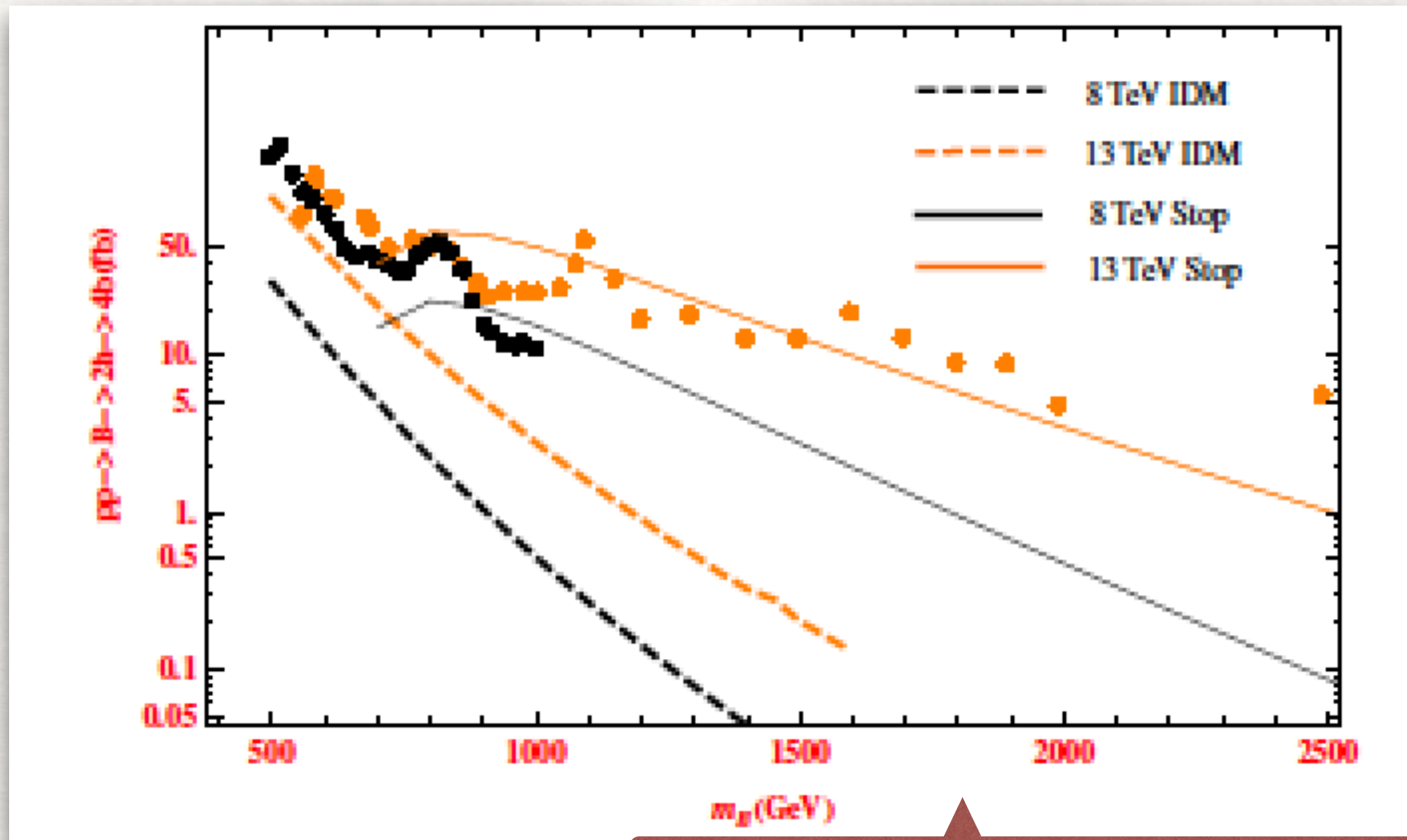
Ma's model for radiative neutrino masses

$$\lambda_3 = 8.5 \times \left(\frac{D_h}{0.84} \right) \left(\frac{0.5}{\alpha_h} \right)^{\frac{1}{2}}$$

$$-\mathcal{L}_h \supset \sqrt{2} \lambda_3 v h C^+ C^- + \frac{v}{\sqrt{2}} \left(\lambda_3 - \frac{m_C^2 - m_S^2}{v^2} \right) h S^2 + \frac{v}{\sqrt{2}} \left(\lambda_3 - \frac{m_C^2 - m_A^2}{v^2} \right) h A^2.$$

4. CURRENT B_h AT LHC VIA RESONANT DI-HIGGS

- The best sensitivity comes from the 4b channel @ 13 TeV



For IDM the production is via the bound state mixing with SM-Higgs boson

5. SUMMARY PART III

- Higgs boson may mediate a relatively strong new force, leading to bound state B_h
- A characteristic feature of B_h is producing resonant di-Higgs ($\sim \text{TeV}$) signature at LHC
- Stop/sbottom/inert Higgs doublet can be good candidates

Thank you!!!