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# Primordial Anti-Biasing & Galaxy Infall Kinematics

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*Part I*

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# The Effect of Primordial Anti-Biasing on the Local Measurements of the Key Cosmological Parameters

Lee 2014, MNRAS, 440,119

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# Introduction

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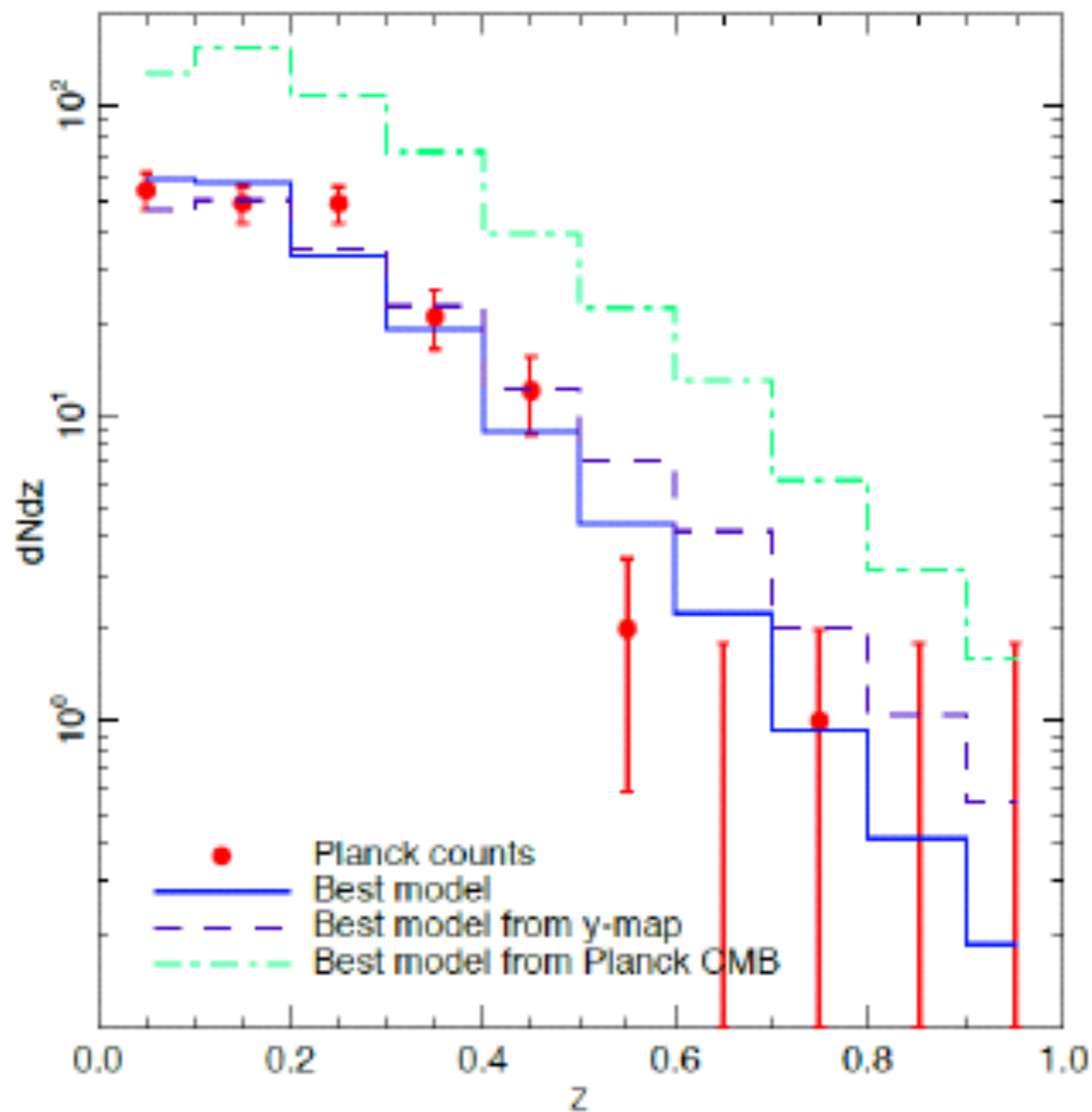
- ◎ To complete the simplest flat  $\Lambda$ CDM picture, it requires
  - precise determination of its key cosmological parameters
  - consistency between the local and the CMB measurements

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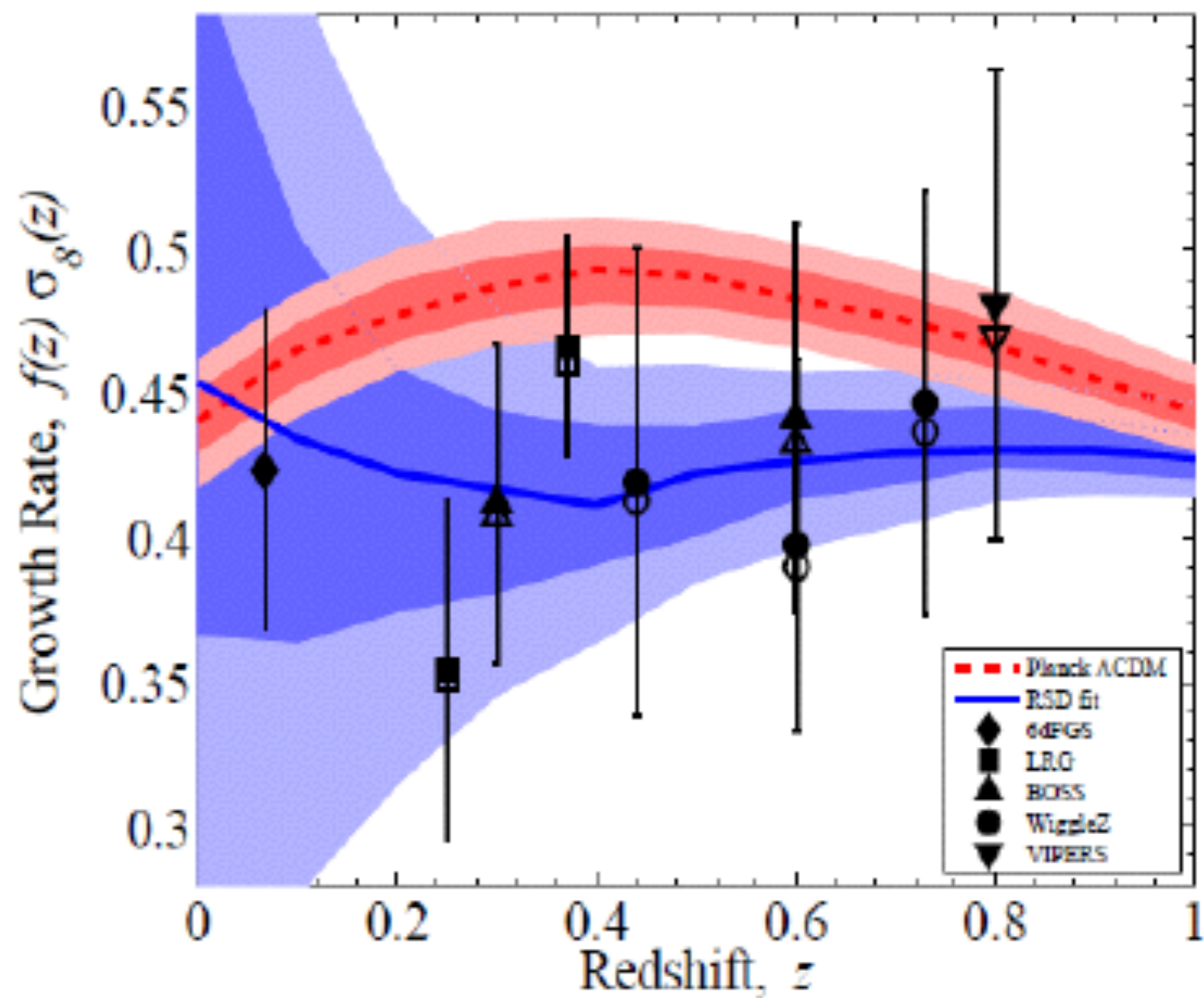
# Inconsistency between Local and Distant

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- ◎ The local universe seems to expand more rapidly than expected from Planck.
- ◎ There are less numbers of the galaxy clusters in the local universe than expected from the Planck cosmology.
- ◎ The number counts of massive clusters evolve less rapidly than expected from the Planck cosmology



$$f \equiv \frac{d \ln D}{d \ln a}$$



Macaulay et al. 2013, PRL, 111,161301

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# Distant vs. Local

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- ◉ From the Planck CMB analysis (Planck 2013 results XVI)

$$\Omega_m = 0.314 \pm 0.020, \sigma_8 = 0.834 \pm 0.027$$

- ◉ From the evolution of the number counts of the SZ clusters (Planck 2013 results XX)

$$\Omega_m = 0.29 \pm 0.02, \sigma_8 = 0.77 \pm 0.02$$

- ◉ From the mass function of the low- $z$  clusters (Vikhlinin et al. 2009)

$$\Omega_m = 0.255 \pm 0.043, \sigma_8 = 0.805 \pm 0.011$$

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# Previously Suggested Solutions

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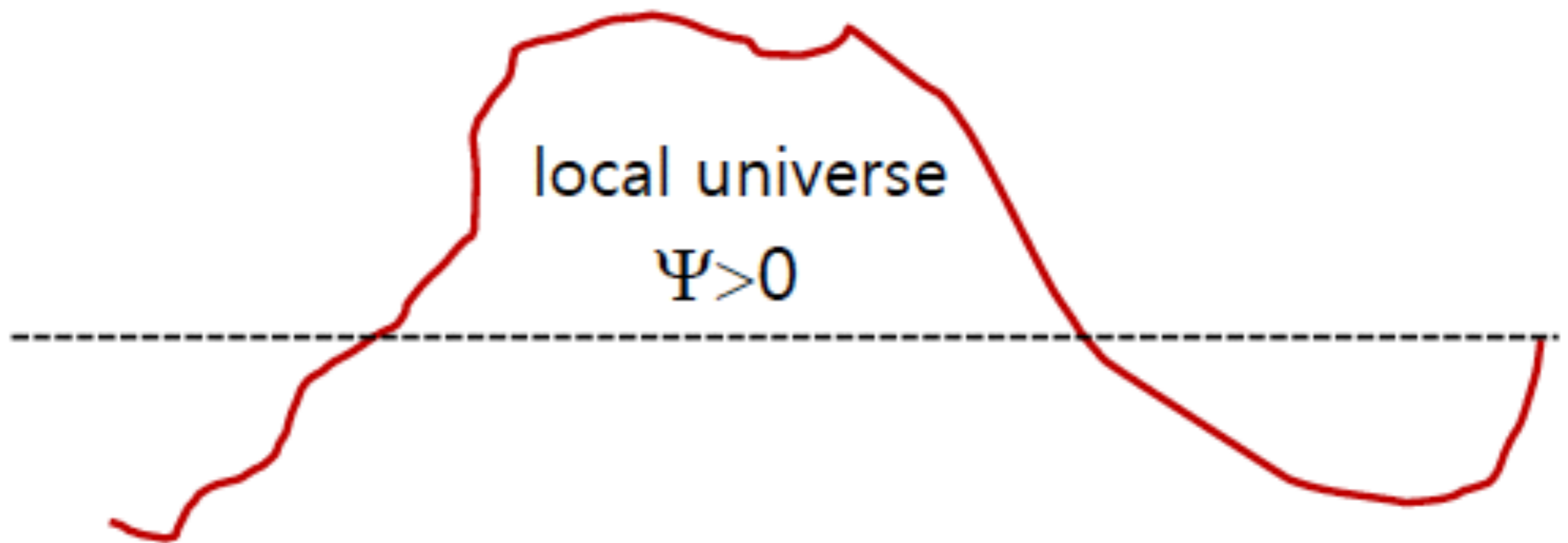
- ◉ The data might be wrong
  - unknown systematics must exist
- ◉ The model has to be improved by taking into account:
  - massive neutrinos (Wyman et al. 2013)
  - coupled dark energy model (Salvatelli et al. 2013)
  - inhomogeneous geometry (e.g., Fluery et al. 2013)

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# A New Approach

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- The local universe formed in the crest of the primordial peculiar potential field ( $\Psi$ )



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# Primordial Potential

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- Related to the linear density field as

$$\delta \propto \nabla^2 \Psi$$

- much smoother than the linear density field
- The nonlinear potential field resembles the smoothed version of the primordial potential (e.g., Pauls & Melott 1995)
- The characteristic scale:

$$R_\varphi = \sqrt{3} \sigma_\varphi / \sigma_\delta = \sqrt{3 \frac{\int_{k_l}^{\infty} dk k^{-2} P(k)}{\int_0^{\infty} dk P(k)}} \approx 120 h^{-1} \text{ Mpc}$$

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# The Press-Schechter Theory

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$$\frac{dN}{dM} = 2 \frac{\bar{\rho}}{M} \left| \frac{dF(\delta_c, M)}{dM} \right| ,$$

$$F(\delta_c; M) = \int_{\delta_c}^{\infty} d\delta \, p(\delta; \sigma_\delta) ,$$

$$\sigma_\delta^2(M) = \int_0^\infty dk \, k^2 P_\delta(k) W^2(k; M) ,$$

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# Modification of the PS Formalism

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$$F(\delta_c; M | \psi > 0) = \int_{\delta_c}^{\infty} d\delta p(\delta; \sigma_\delta, \sigma_c, \sigma_\psi | \psi > 0) ,$$

$$p(\delta, \sigma_\delta, \sigma_c, \sigma_\psi | \psi > 0) = \frac{\int_0^\infty d\psi p(\delta, \psi; \sigma_\delta, \sigma_c, \sigma_\psi)}{\int_0^\infty d\psi p(\psi; \sigma_\psi)} = 2 \int_0^\infty d\psi p(\delta, \psi; \sigma_\delta, \sigma_c, \sigma_\psi) ,$$

$$p(\delta, \psi; \sigma_\delta, \sigma_c, \sigma_\psi) = \frac{1}{[(2\pi)^2 \sigma_\delta^2 (\sigma_\psi^2 - \sigma_c^4 / \sigma_\delta^2)]^{1/2}} \exp\left(-\frac{\delta^2}{2\sigma_\delta^2}\right) \exp\left[-\frac{(\psi + \sigma_c^2 \delta / \sigma_\delta^2)^2}{2(\sigma_\psi^2 - \sigma_c^4 / \sigma_\delta^2)}\right] .$$

$$\sigma_c^2(M) = \int_0^\infty dk P_\delta(k) W(k; M) .$$

$$\sigma_\psi^2 = \int_{k_{nl}}^\infty dk k^{-2} P_\delta(k) ,$$

$$\nu \equiv \frac{\delta}{\sigma} \; , \qquad \mu \equiv \frac{(\psi + \sigma_c^2 \delta / \sigma_\delta^2)^2}{2(\sigma_\psi^2 - \sigma_c^4 / \sigma_\delta^2)} \; .$$

$$p(\nu, \mu) d\nu \, d\mu = \frac{1}{(2\pi)^{1/2}} \exp\left(-\frac{\nu^2}{2}\right) \frac{1}{(2\pi)^{1/2}} \exp\left(-\frac{\mu^2}{2}\right)$$

$$F(M; \nu_c, \mu_c) = \int_{\nu_c}^{\infty} d\nu \frac{1}{(2\pi)^{1/2}} \exp\left(-\frac{\nu^2}{2}\right) \int_{\mu_c}^{\infty} d\mu \frac{1}{(2\pi)^{1/2}} \exp\left(-\frac{\mu^2}{2}\right)$$

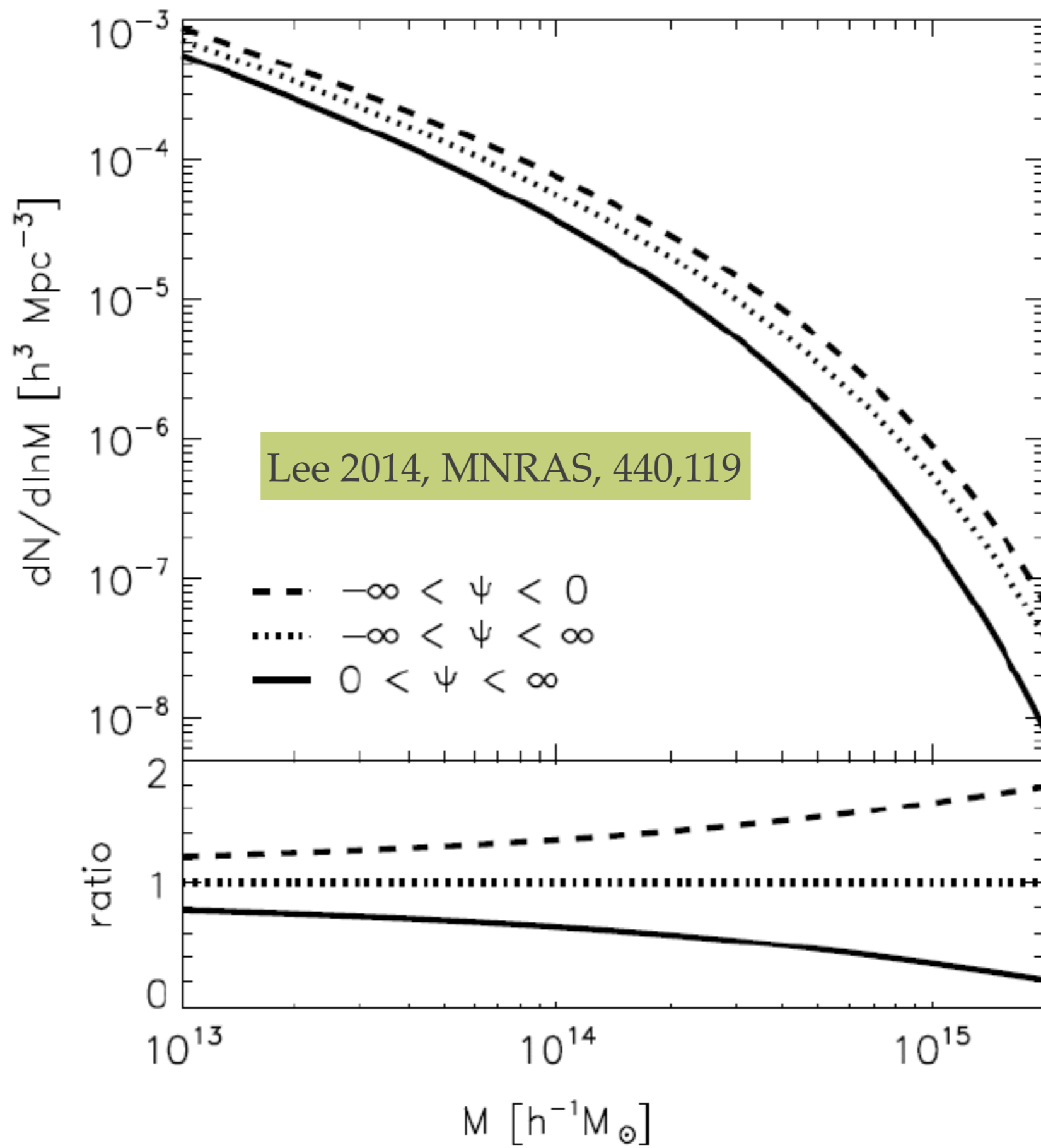
$$\frac{dN}{dM} = 4 \frac{\bar{\rho}}{M} \left| \frac{dF}{dM} \right| = 4 \frac{\bar{\rho}}{M} \left| \frac{d\nu_c}{dM} \frac{dF}{d\nu_c} + \frac{d\mu_c}{dM} \frac{dF}{d\mu_c} \right|$$

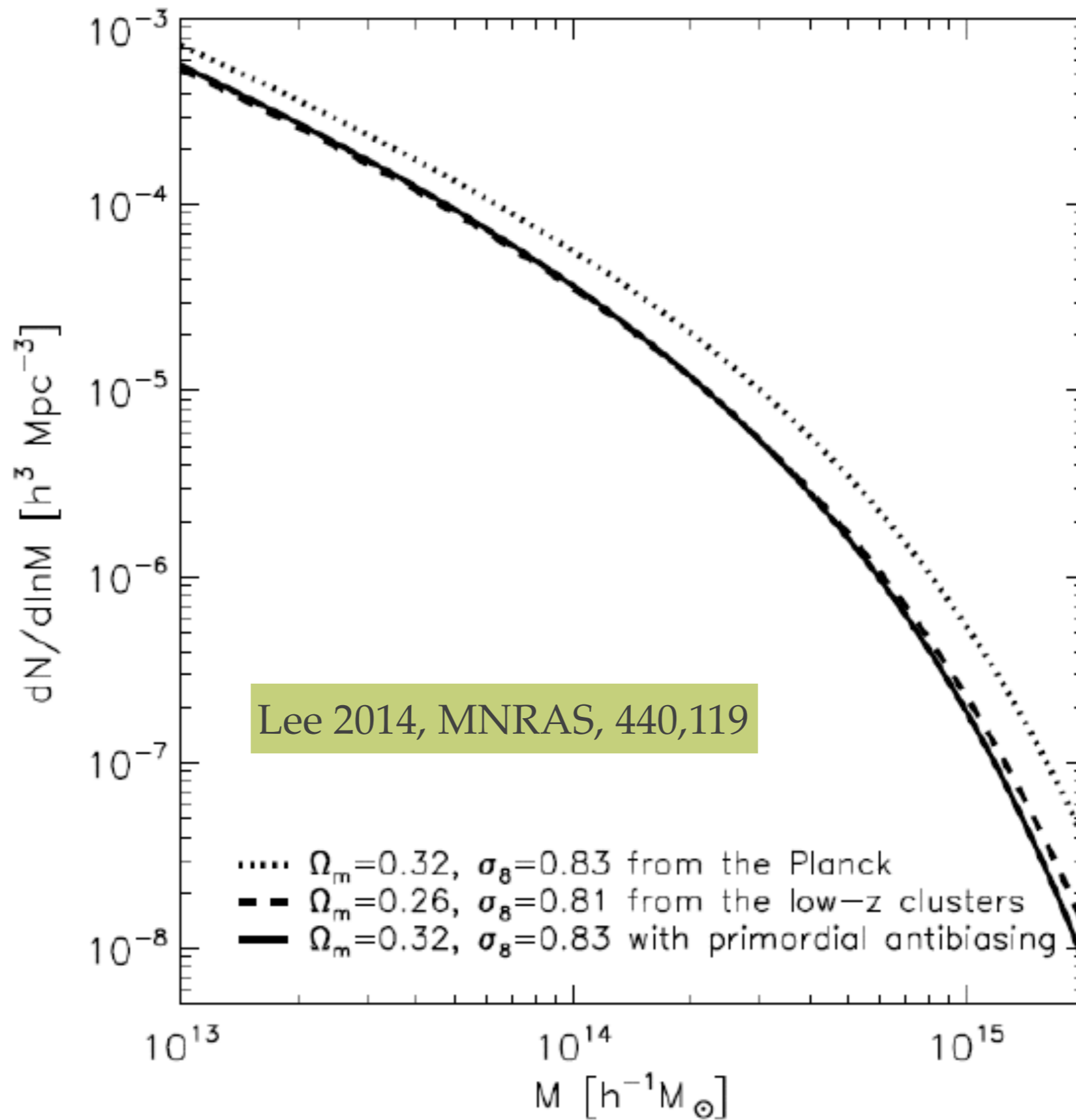
$$\frac{dF}{d\nu_c} = \frac{1}{(2\pi)^{1/2}} \exp\left(-\frac{\nu^2}{2}\right) \left[ \frac{1}{2} \text{erfc}\left(\frac{\nu_c}{2}\right) \right] ,$$

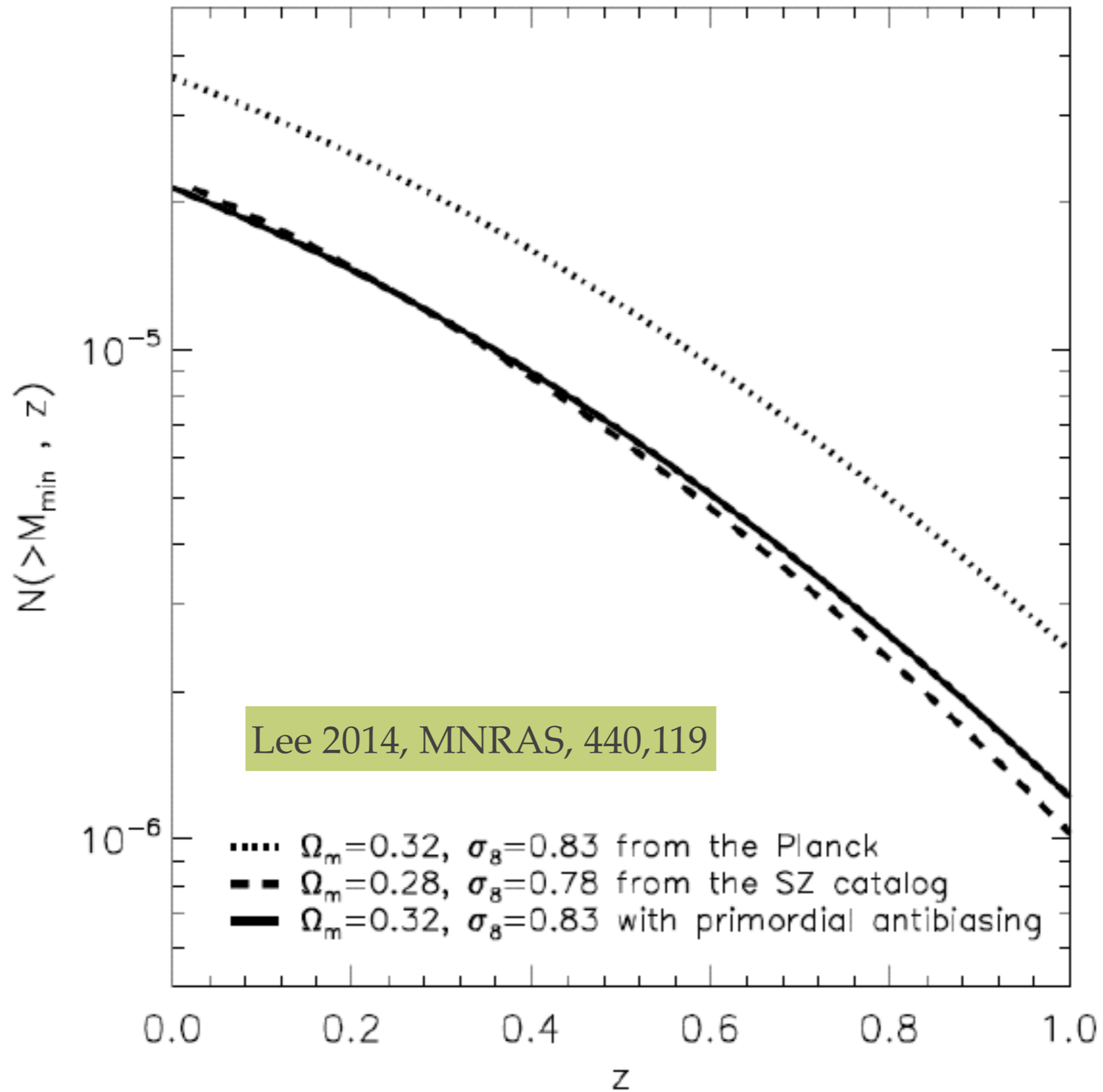
$$\frac{dF}{d\mu_c} = \frac{1}{(2\pi)^{1/2}} \exp\left(-\frac{\mu^2}{2}\right) \left[ \frac{1}{2} \text{erfc}\left(\frac{\mu_c}{2}\right) \right] ,$$

$$\frac{d\nu_c}{dM} = \frac{d\nu_c}{d\sigma_\delta} \frac{d\sigma_\delta}{dM} ,$$

$$\frac{d\mu_c}{dM} = \frac{d\mu_c}{d\sigma_\delta} \frac{d\sigma_\delta}{dM} + \frac{d\mu_c}{d\sigma_c} \frac{d\sigma_c}{dM} .$$







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# Summary and Future Works

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- ◎ The inconsistency between the local and the distant measurements of  $\Omega_m$  and  $\sigma_8$  can be explained away in the  $\Lambda$ CDM model if the local universe is assumed to have formed in the primordial potential crest.
- ◎ The characteristic scale of the primordial potential crest has to be empirically determined.
- ◎ To investigate the effect of primordial anti-biasing on the linear growth rate, halo merging rate, halo assembly bias and galaxy down-sizing phenomenon.

*Part II*

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# Galaxy Infall Kinematics around the Virgo Cluster as a Cosmological Probe

Lee, Rey & Kim, 2014a, arXiv:  
1406.5250

Lee, Rey & Kim, 2014b, in  
preparation

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# Galaxy Infall Kinematics

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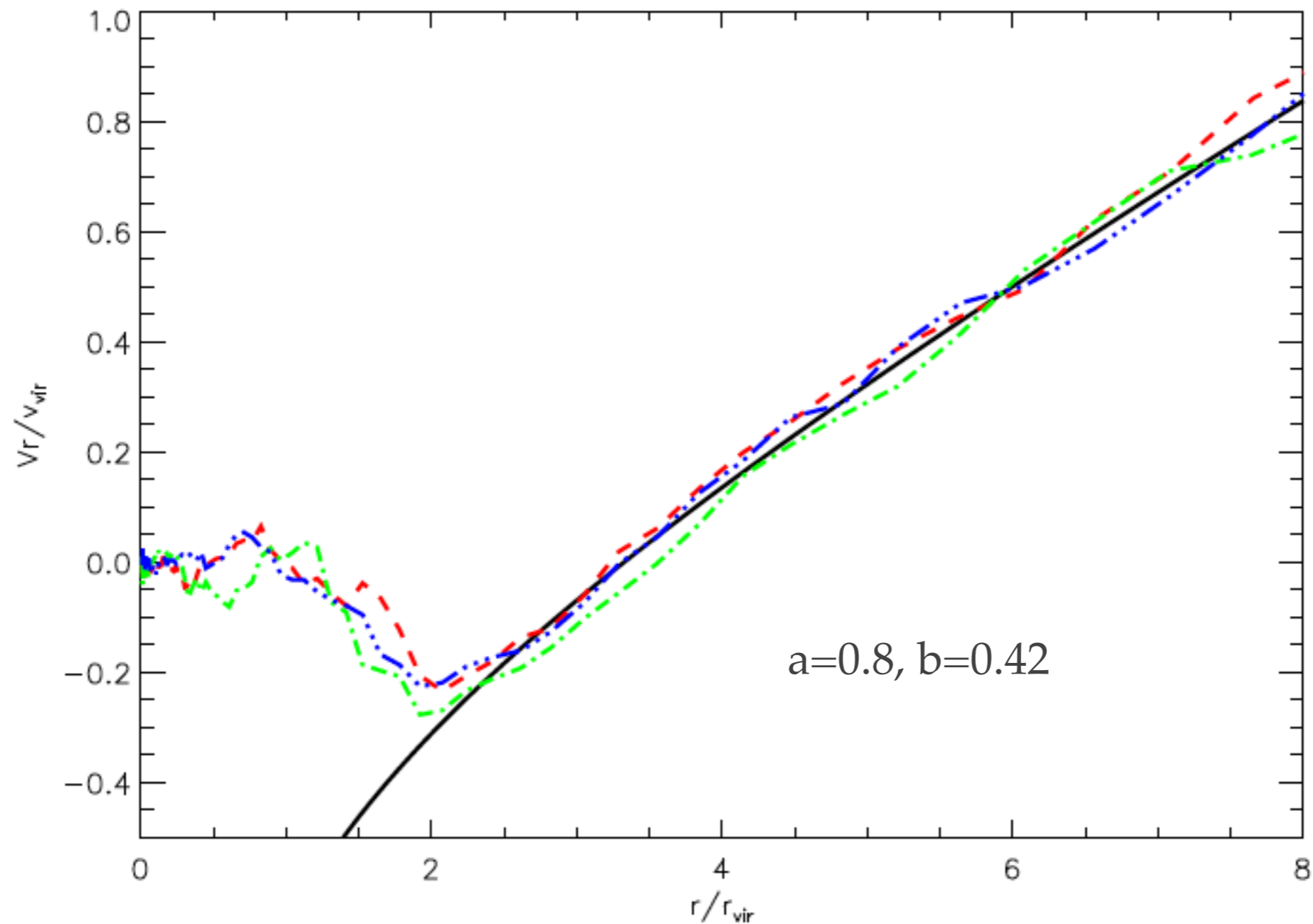
- The infall velocities of satellite galaxies located at (2-4) times the virial radii from the galaxy clusters can be used to determine the mass of galaxy clusters (Falco et al. 2014)

$$\bar{v}_r(r, M_v) = H r + \bar{v}_p(r, M_v) ,$$

- The peculiar velocity profile in the radial direction has been found by Falco et al. (2014) as

$$\bar{v}_p(r) \approx -v_0 \left( \frac{r}{r_v} \right)^{-b} \quad \text{with } v_0 = a V_v$$

# Radial Velocity Profiles



Falco et al. 2014, MNRAS, 442,1887

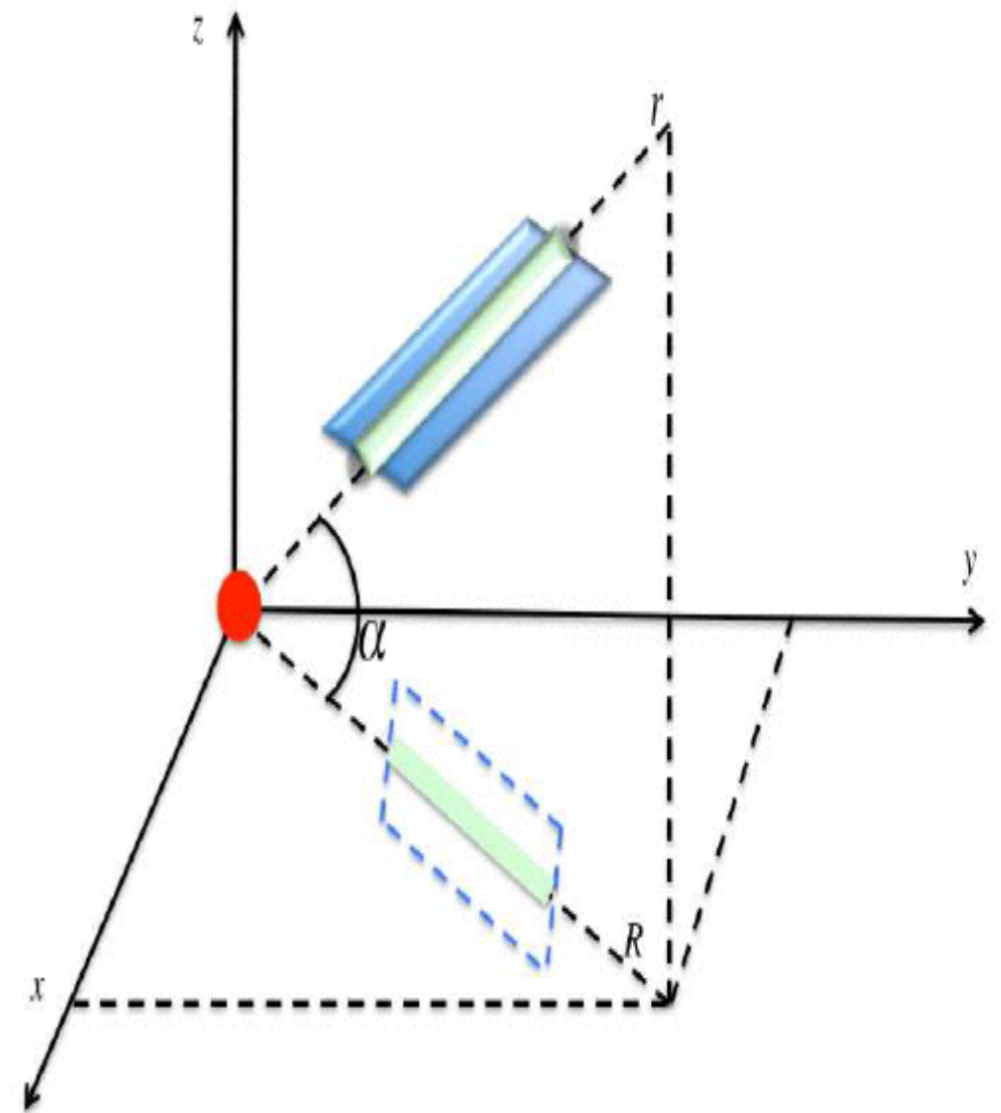
# Cosmic Web Environment

$$R = \cos \alpha r$$

$$v_{\text{los}}(R) = \sin \alpha v_r(r)$$

$$v_{\text{los}}(R, \alpha, M_v) = \sin \alpha \left[ H \frac{R}{\cos \alpha} + v_p \left( \frac{R}{\cos \alpha}, M_v \right) \right].$$

$$v_{\text{los}}(R, \alpha, M_v) = \sin \alpha \left[ H \frac{R}{\cos \alpha} - a V_v \left( \frac{R}{\cos \alpha r_v} \right)^{-b} \right].$$



Falco et al. 2014, MNRAS, 442,1887

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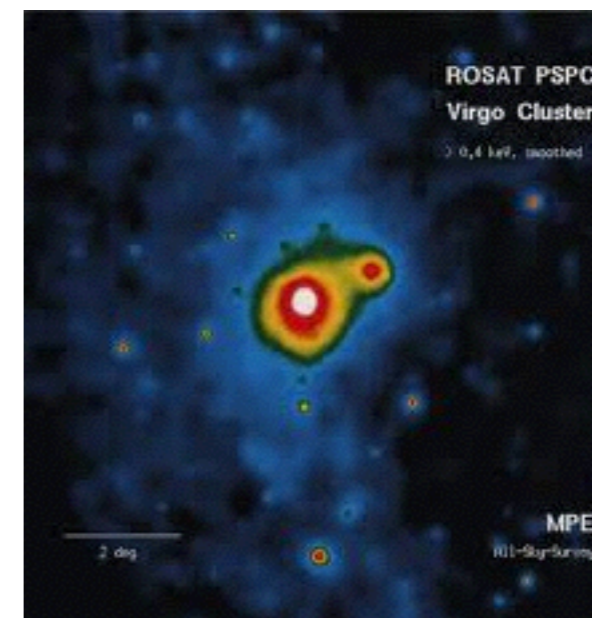
# Anisotropic Merging in the Cosmic Web

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- Galaxies merge into the clusters preferentially along the cosmic filaments and sheets.
- The principal directions of the velocity shear field have been found to trace the anisotropic merging very well (Libeskind et al. 2013, 2014a, 2014b, 2014c)
- The spatial positions and velocity vectors of satellite galaxies are expected to align with the principal axes of the local velocity shears (e.g., Lee, Rey & Kim 2014a)

# Virgo Cluster as a Target

- ◉ proximity
  - 16.5 Mpc away
- ◉ not completely relaxed
  - presence of subgroups
- ◉ triaxial shapes
  - elongated along LoS (e.g., Mei et al. 2007)
- ◉ located in the filamentary environment
  - the Local Supercluster (Tully 1982)



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# Reconstruction of the Velocity Shear Field

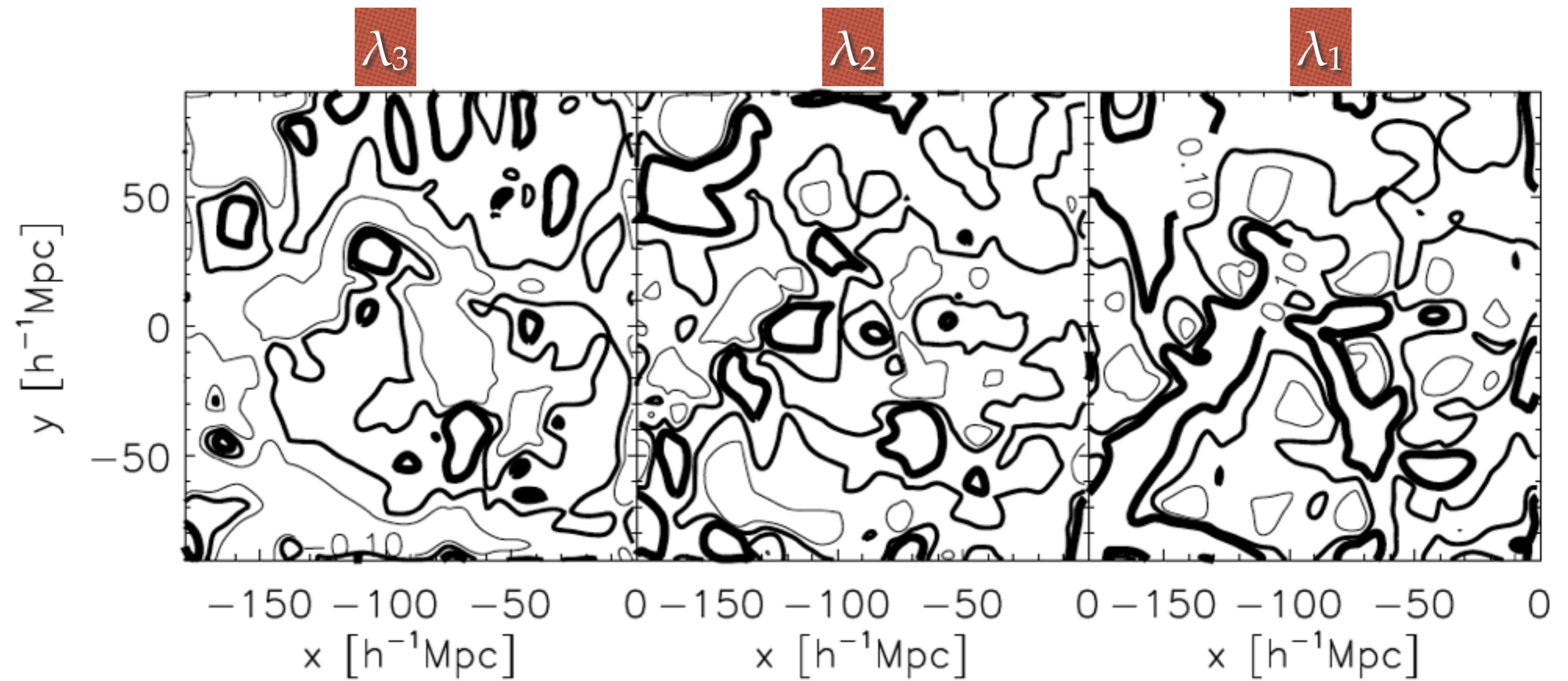
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- Construct the velocity shear field in the  $180^3 \text{ (Mpc/h)}^3$  sub volume consisting of  $256^3$  grids
  - by using the velocity field reconstructed by Wang et al. (2012) from the Sloan Digital Sky Survey,

$$\Sigma_{ij} = -\frac{1}{2H_0} (\partial_j v_i + \partial_i v_j) ,$$

$$\tilde{\Sigma}_{ij} = -\frac{1}{2H_0} (k_j \tilde{v}_i + k_i \tilde{v}_j) \exp \left( -\frac{R_f \tilde{v}^2}{2} \right) .$$

- where  $R_f$  is the filtering radius.

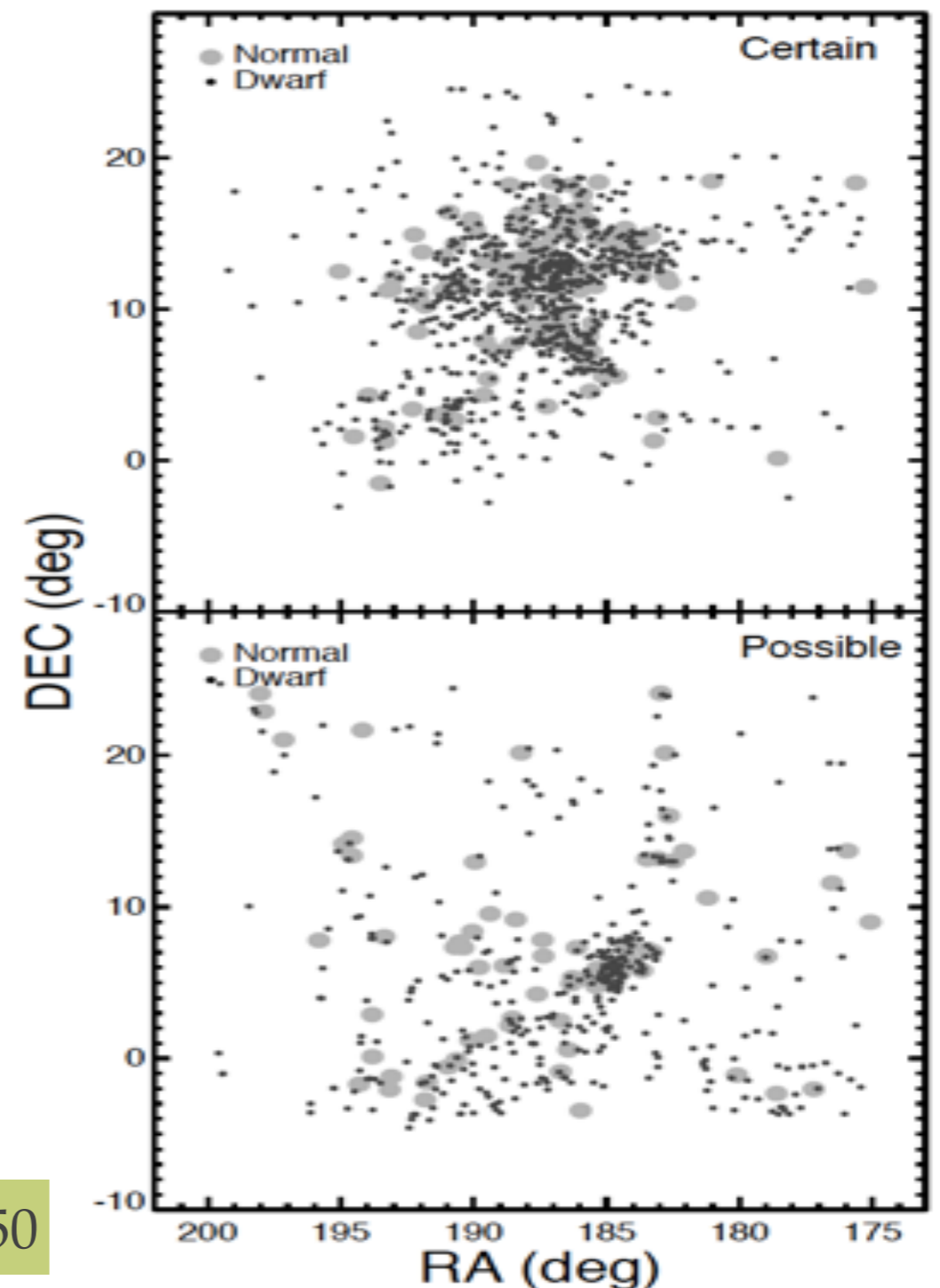


Lee, Rey & Kim 2014, arXiv:1406.5250

# Extended Virgo Cluster Catalog

- ◉ Kim et al. (2014, submitted to ApJS) constructed the EVCC
  - a total 1589 galaxies
  - $m_r < 17.77$  [mag]
  - spectroscopic information from the SDSS DR7 and NED
  - within 3.5 times virial radius from the Virgo cluster.

Lee, Rey & Kim 2014a, arXiv:1406.5250



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# Centrals vs. Satellite

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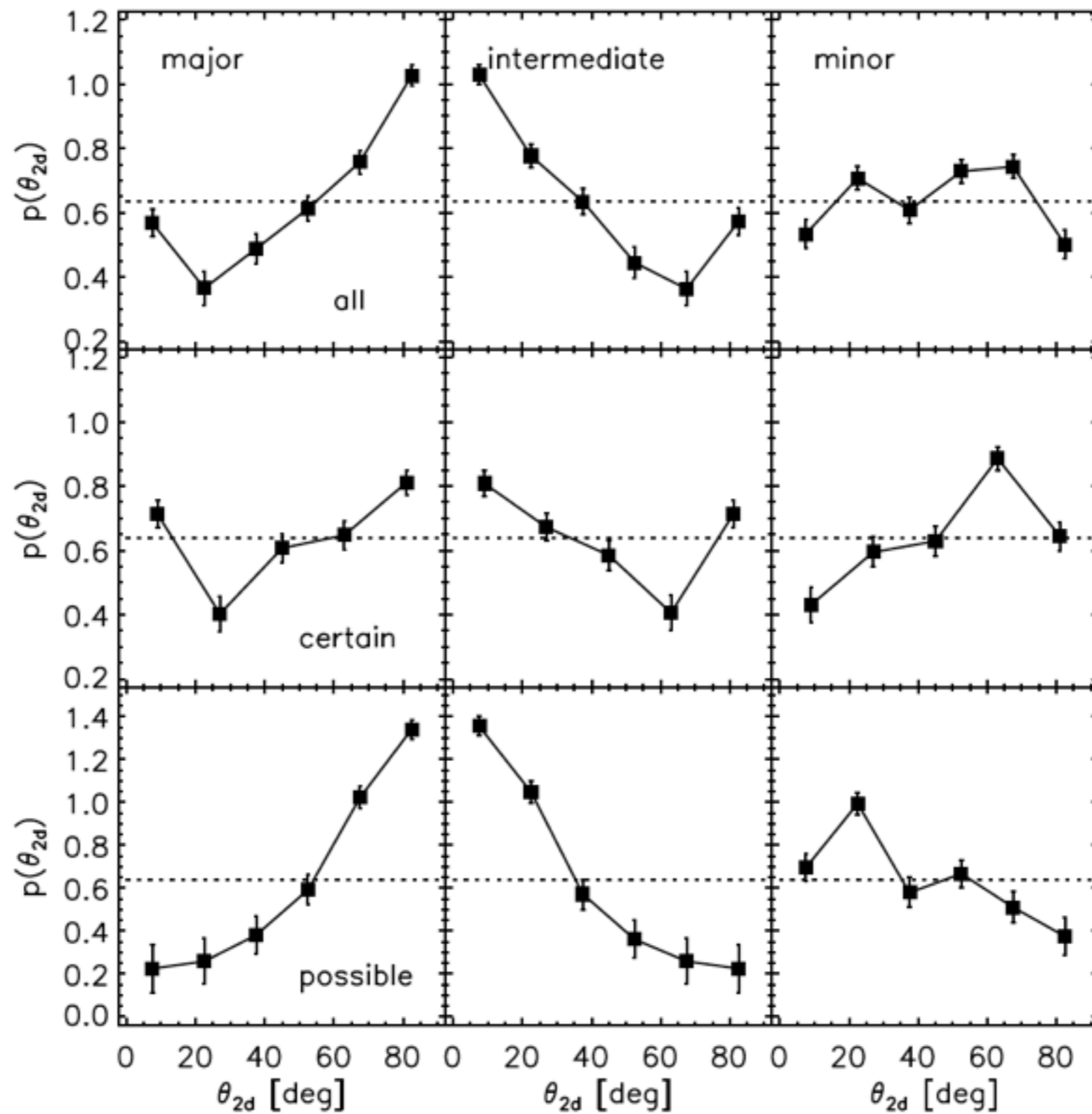
- ◉ Central galaxies (a total of 1028)
  - members of the Virgo cluster
  - gravitational bound, located within the virial radius
  - the magnitudes of their heliocentric radial velocities less than a given threshold (Praton & Schneider 1994)
- ◉ Satellite galaxies (a total of 561)
  - possible members of the Virgo cluster
  - still merging located beyond the virial radius
  - the magnitudes of their heliocentric radial velocities higher than a given threshold (Praton & Schneider 1994)

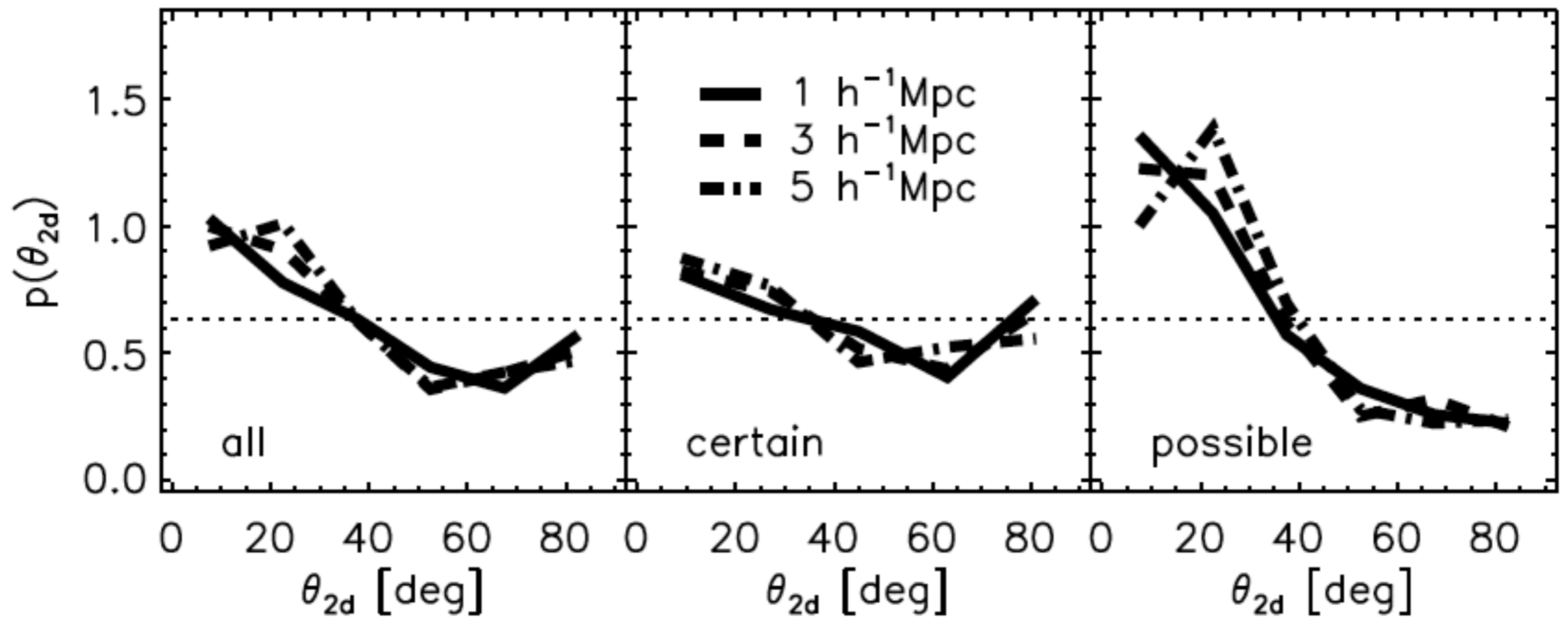
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# Alignments of the Virgo Satellites with the Velocity Shear

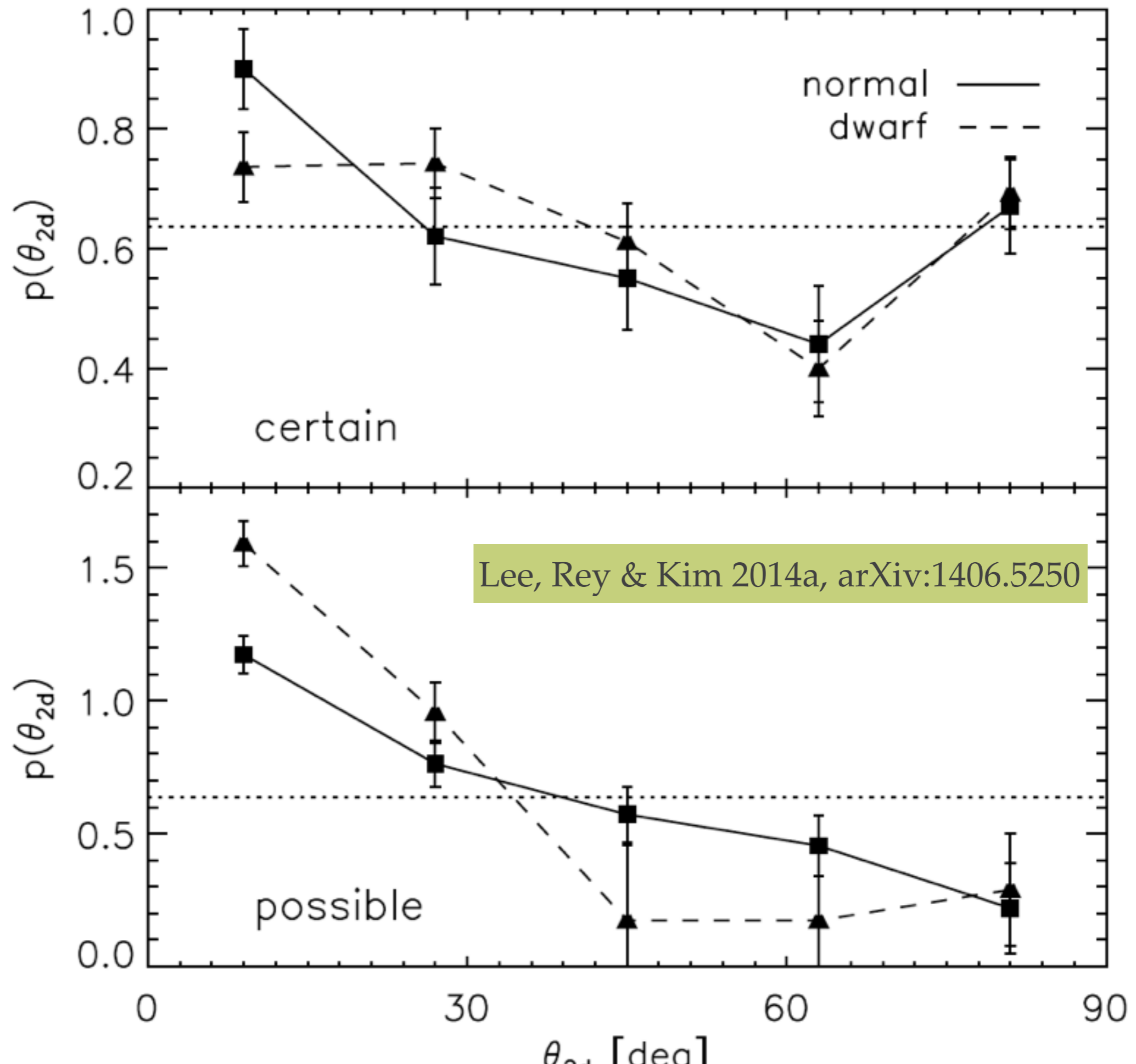
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- ◉ The minor principal axis of the velocity shear field is found to be almost perfectly aligned with the line of sight direction.
  - The angles of the major, intermediate and minor principal axes with the LoS are 94.7, 98.7, 9.9 in unit of degree, respectively.
- ◉ Measuring the alignments between the projected positions of the Virgo satellites and principal axes of the local velocity shear tensor in the plane of the sky





Lee, Rey & Kim 2014a, arXiv:1406.5250



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# Interpretation

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- ◉ The giant satellites merge into the Virgo cluster along the filament in the direction of the minor principal axis of the local velocity shear.
- ◉ The dwarf satellites merge into the Virgo cluster along the sheet spanned by the minor and intermediate principal axes.
- ◉ The 2D project diminishes the strength of the alignment of the giant satellites
  - since the minor principal axis of the local velocity shear is almost perfectly aligned with the line of sight direction.
  - But, the intermediate principal axis of the local velocity shear is almost perfectly lying in the plane of the sky, so that the alignment of the dwarf satellites is not diminished.

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# Follow-up Work

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- ◉ From the giant satellites located in  $(2-4)r_{\text{vir}}$  from the Virgo cluster,
  - determining  $H_0$  and  $M_{\text{vir}}$  of the Virgo cluster with the help of the GIK method
    - as the value of  $\alpha$  has been determined
  - understanding how the galaxies are distributed in the environment surrounding the Virgo cluster
    - difference between the giants and the dwarfs
  - testing modified gravity models which
    - requires a formula for the radial velocity profiles

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# Summary and Future Works

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- ◉ The velocity shear field in the local universe was reconstructed.
- ◉ The projected principal axes of the local velocity shear at the Virgo cluster are found to be aligned with the projected positions of the Virgo satellites.
- ◉ It will allow us to determine the mass of the Virgo cluster without assuming hydrostatic equilibrium as well as the Hubble constant independently.
- ◉ Comparison with the results from modified gravity theory is on going.