

Poly-instanton axion inflation

Shohei Uemura (MISC, Kyoto Sangyo University)

based on arXiv:1703.03402 [hep-ph]

With Tatsuo Kobayashi (Hokkaido University), SU, and Junji Yamamoto (Kyoto University),

July 13, 2017, @ KAIST, Daejeon

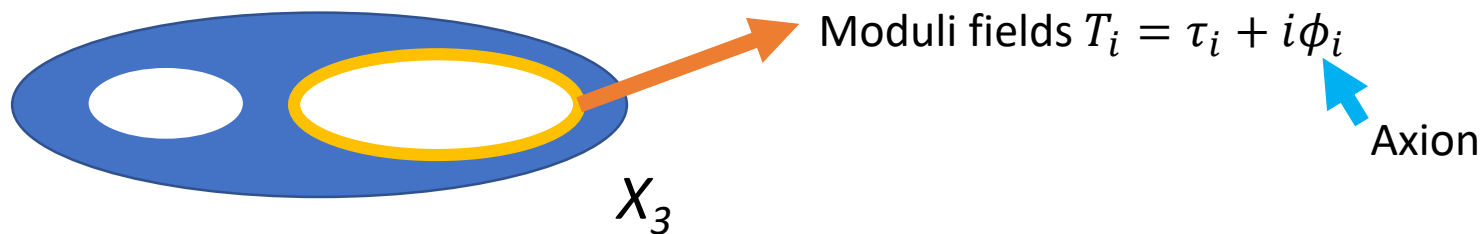
Axion-inflation

- Axion : fields having shift symmetry

$$\phi \sim \phi + \delta$$

- Axion is a good candidate of the inflaton.

1. $V(\phi) = V(\phi + \delta) \rightarrow$ flatness of the potential.
2. String compactifications provide many axions.



e.g. natural inflation

$$V = V_0 \left(\cos \left(\frac{\phi}{f} \right) + 1 \right) \rightarrow \text{We need modulation terms.}$$

e.g. Aligned inflation, Monodromy inflation

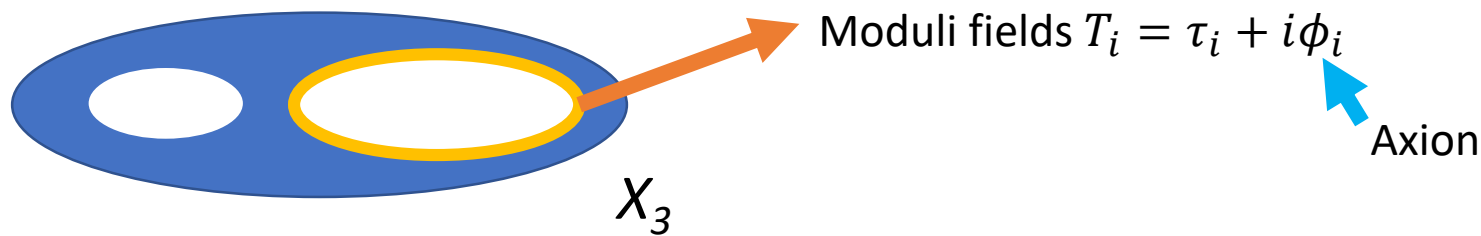
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$$V = V_0$$

Poly-instanton axion inflation

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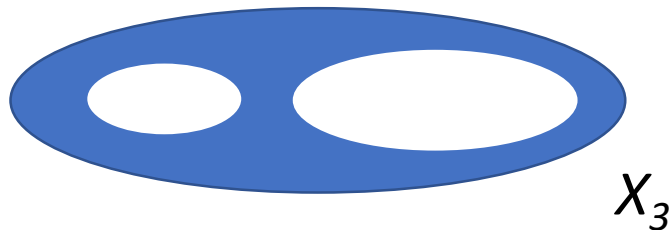
inflation

Before talking about poly-instanton, I'd like to talk about D-brane instanton

D-brane instanton effect

- Consider IIB orientifold on CY 3-fold X_3 , $\rightarrow$ SUGRA
- Dp-brane instanton : instanton like Dp-brane configuration,
non-perturbatively correct the EFT.

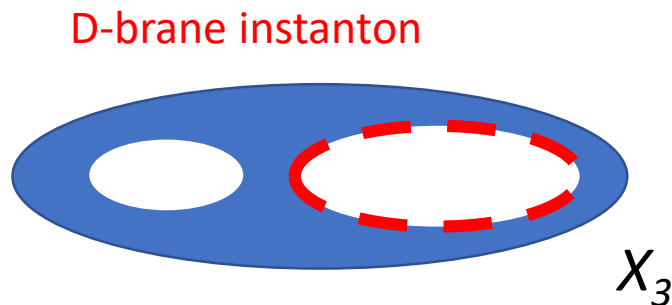
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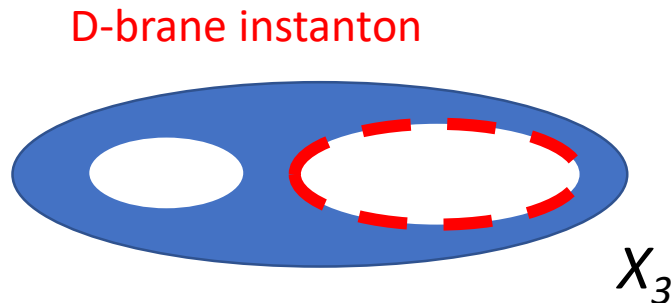


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$$W = W_0 + A_1 e^{-S}$$

Single instanton effect

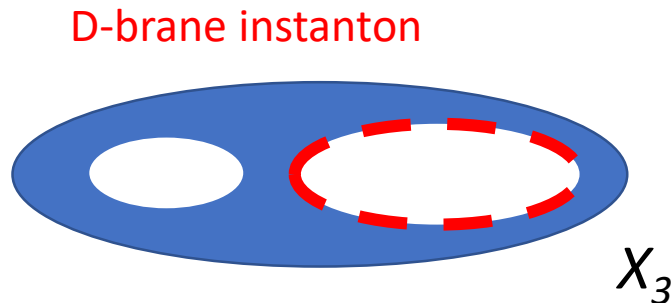


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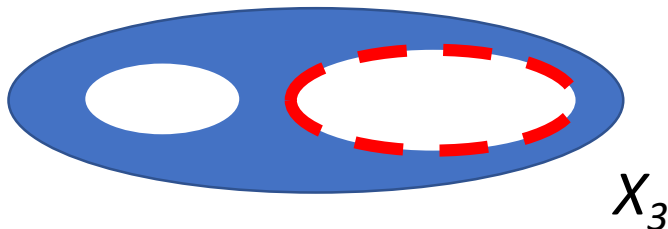
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Single instanton effect

- Poly-instanton : instanton corrected by another (D-brane) instanton.

D-brane instanton



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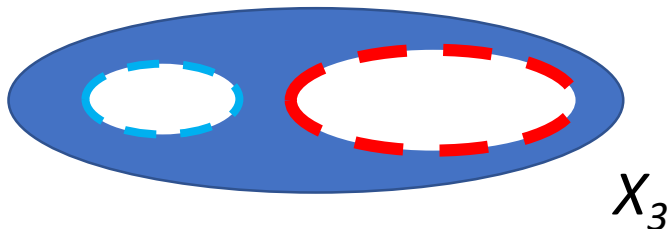
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X_3

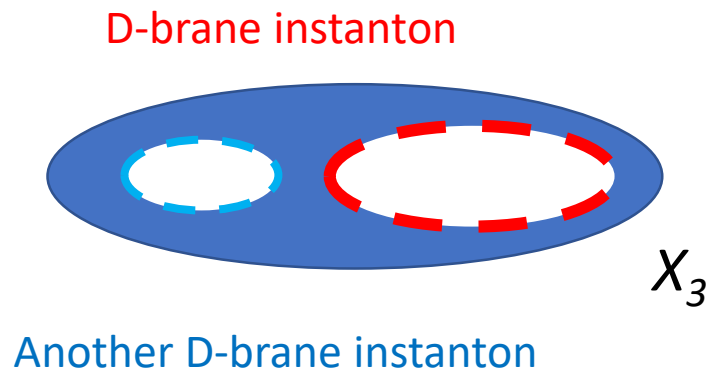
Another D-brane instanton

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Single instanton effect another instanton effect

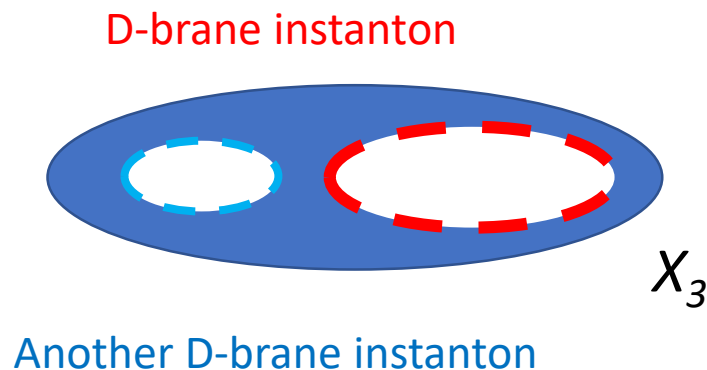


D-brane instanton effect

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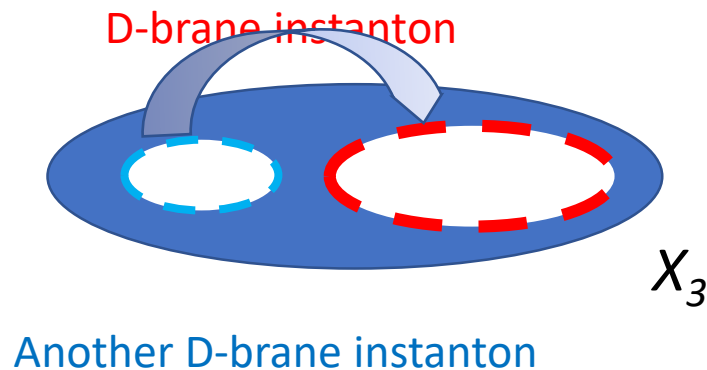
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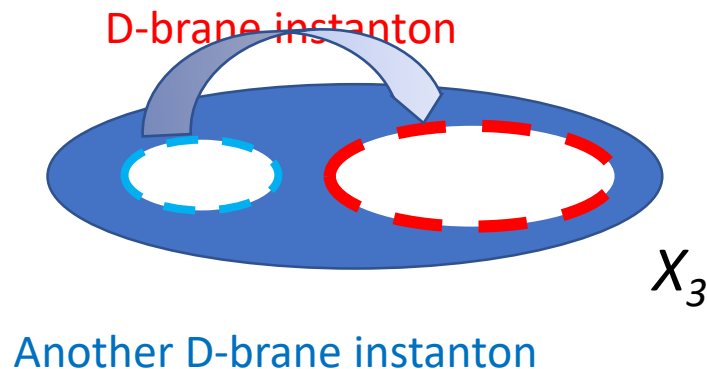
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Single instanton effect

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R.Blumenhagen and M.Schmidt-Sommerfeld, [2008]



This potential is highly suppressed...

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-> flat potential?

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-> Inflation

Poly-instanton potential

- Divide superpotential to two parts,

$$W = W_{pert+single} + W_{poly}$$

- Suppose, there is a one moduli T^0 , which appears only in poly-instanton superpotential, i.e.

$$W = W(T_i)|_{i \neq 0} + A_0 \exp[-a(T_i + C e^{-a_0 T_0})]|_{i \neq 0}$$

- $A_0 = 0$,  $\text{Im } T_0$ is massless, although $\text{Re } T_0$ can be massive.

$$\because \text{Re } T_0 \in K = -2 \log V = K(T + \bar{T})$$

- When $A_0 \ll W(\langle T_i \rangle)|_{i \neq 0}$, mass of $\text{Im } T_0$ can be the lightest scalar.

Q *Is the axion potential flat enough to satisfy the slow roll conditions?*

Poly-instanton axion potential

- All heavier modes are integrated out, we obtain the superpotential

$$W = W'_0 + A'_0 \exp[-aC e^{-a_0 T_0}]$$

- Assuming $A'_0 \ll 1$,

$$V_F = e^K (\sum_{i,j=\text{moduli}} K^{i\bar{j}} D_i W D_{\bar{j}} \bar{W} - 3|W|^2)$$

$$-3e^K |W|^2 = -3e^K (|W'_0|^2 + \bar{W}'_0 A'_0 \exp[-aC e^{-a_0 T_0}] + h.c.) + \mathcal{O}(A'^2_0)$$

$$e^K K^{T_0 \bar{T}_0} |D_{T_0} W|^2 = e^K K^{T_0 \bar{T}_0} \{ |K_{T_0}|^2 (|W'_0|^2 + \bar{W}'_0 A'_0 \exp[-aC e^{-a_0 T_0}] + h.c.) \\ + K_{T_0} \bar{W}'_0 A'_0 a_0 aC e^{-a_0 T_0} \exp[-aC e^{-a_0 T_0}] + h.c. \} + \mathcal{O}(A'^2_0)$$



$$V_F = 2e^K |\bar{W}'_0 A'_0|^2 \exp[-\delta \cos(a_0 \phi_0)] \{ (K^{T_0 \bar{T}_0} K_{T_0})^2 - 3 \} \cos[\delta \sin(a_0 \phi_0) + \theta] \\ + K^{T_0 \bar{T}_0} K_{T_0} a_0 \delta \cos[-a_0 \phi_0 + \delta \sin(a_0 \phi_0) + \theta] \} + (const)$$

$\delta = aC \exp[-a_0 \langle \tau_0 \rangle]$: magnitude of a Poly instanton effect

Poly-instanton axion potential

$$V_F = 2e^K |\overline{W'_0} A'_0|^2 \exp[-\delta \cos(a_0 \phi_0)] \{ (|K^{T_0 \overline{T}_0} K_{T_0}|^2 - 3) \cos[\delta \sin(a_0 \phi_0) + \theta] \\ + K^{T_0 \overline{T}_0} K_{T_0} a_0 \delta \cos[-a_0 \phi_0 + \delta \sin(a_0 \phi_0) + \theta] \} + (const)$$

- When $a_0 \delta \gg 1$,

Poly-instanton axion potential

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- When $a_0 \delta \gg 1$,

$$V = A(e^{-\delta \cos(a \phi)} \cos[\delta \sin(a \phi) - a \phi + \theta] + V_0)$$

ϕ : canonically normalized field

- Sinusoidal function of a sinusoidal function

Poly-instanton axion potential

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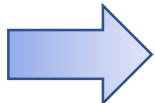
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- When $a_0 \delta \ll 1$,

$$V = A_1 \cos \theta + V_0 - \delta(A_1 - A_2) \cos[a \phi - \theta] + \frac{1}{2} \delta^2 (A_1 - 2A_2) \cos(2a \phi - \theta) + \dots$$



Natural inflation + modulation terms

Poly-instanton axion potential

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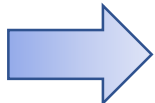
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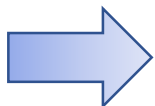
$$V = A(e^{-\delta \cos(a \phi)} \cos[\delta \sin(a \phi) - a \phi + \theta] + V_0)$$

ϕ : canonically normalized field

- Sinusoidal function of a sinusoidal function  Flat potential!

- When $a_0 \delta \ll 1$,

$$V = A_1 \cos \theta + V_0 - \delta(A_1 - A_2) \cos[a \phi - \theta] + \frac{1}{2} \delta^2 (A_1 - 2A_2) \cos(2a \phi - \theta) + \dots$$



Natural inflation + modulation terms

Numerical analysis

- Slow roll parameters,

$$\varepsilon = \frac{1}{2} \left(\frac{V_\phi}{V} \right)^2, \eta = \frac{V_{\phi\phi}}{V}, \xi = \frac{V_\phi V_{\phi\phi}}{V^2} \ll 1 \text{ during inflation.}$$

- And the observed values are given by

$$P_\xi = \frac{V}{24\pi^2 \epsilon} = 2.20 \pm 0.10 \times 10^{-9}, n_s = 1 + 2\eta - 6\epsilon = 0.9655 \pm 0.0062,$$

$$r = 16\epsilon < 0.12,$$

$$V = A(e^{-\delta \cos(a\phi)} \cos[\delta \sin(a\phi) - a\phi + \theta] + V_0)$$

δ	θ	A	n_s	r	N_e	α_s	m_ϕ^2
8.0	4.13	3.29×10^{-16}	0.953	6.02×10^{-7}	61.9	-3.66×10^{-4}	6.70×10^{-11}
9.0	3.16	3.46×10^{-16}	0.959	9.30×10^{-7}	58.6	-4.66×10^{-4}	1.27×10^{-10}
10.0	2.11	2.18×10^{-16}	0.963	7.65×10^{-7}	56.8	-4.70×10^{-4}	1.26×10^{-10}
11.0	7.25	1.08×10^{-16}	0.966	4.24×10^{-7}	61.7	-3.98×10^{-4}	8.31×10^{-11}
12.0	6.28	8.89×10^{-17}	0.966	4.89×10^{-7}	55.7	-4.61×10^{-4}	1.12×10^{-10}

Table 1: Examples of parameters and observables.

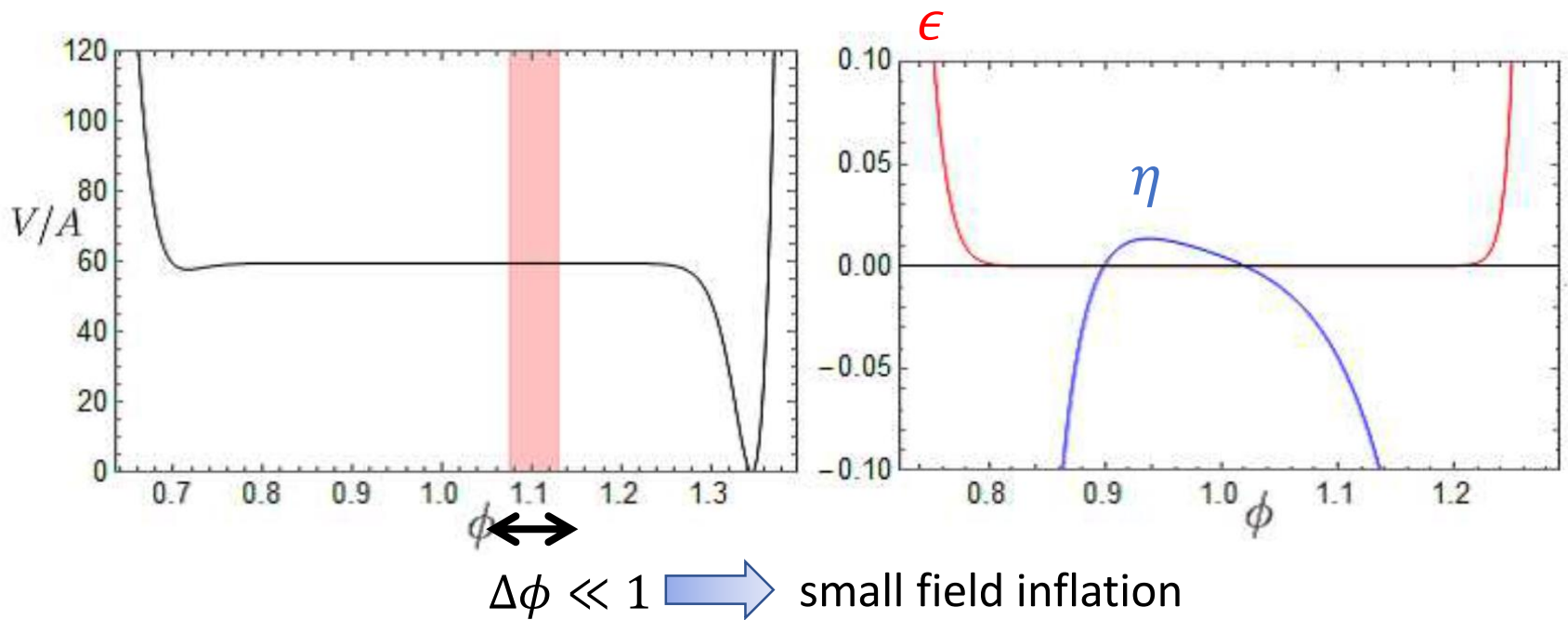


Figure 1: The inflation potential with $\delta = 8.0$. The red and blue curves correspond to ϵ and η , respectively.

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Analytical analysis

- Derivations of the potential

$$V_\phi = A\delta a e^{-\delta \cos a\phi} \left[-\sin(\delta \sin a\phi - 2a\phi + \theta) + \frac{1}{\delta} \sin(\delta \sin a\phi - a\phi + \theta) \right]$$

$$\sim A\delta a e^{-\delta \cos a\phi} [-\sin(\delta \sin a\phi - 2a\phi + \theta)]$$

$$V_{\phi\phi} \sim A\delta^2 a^2 e^{-\delta \cos a\phi} [-\cos(\delta \sin a\phi - 3a\phi + \theta)]$$

$$V_{\phi\phi\phi} \sim A\delta^3 a^3 e^{-\delta \cos a\phi} [-\sin(\delta \sin a\phi - 4a\phi + \theta)]$$



$$\frac{\epsilon}{\eta} \sim e^{-\delta \cos a\phi}$$

$$|\eta| \sim \frac{|V_{\phi\phi\phi}| \Delta\phi}{V} \sim \frac{A\delta^3 a^3 e^{-\delta \cos a\phi} [-\sin(\delta \sin a\phi - 4a\phi + \theta)]}{A V_0} \sim \delta^2 a^2 \sqrt{\epsilon} \Delta\phi$$

+ Lyth relation : $r \sim 10^{-2} (\Delta\phi)^2$



$$r \sim \frac{10^{-2} \eta^2}{\delta^4 a^4 \epsilon} \quad \text{To realize } \eta \sim -0.1, \quad \epsilon^2 \sim \frac{10^{-7}}{\delta^4 a^4} \quad \begin{array}{l} \text{e.g. } \delta = 10, a = 2\pi \\ \rightarrow \epsilon = 10^{-7}, r \sim 10^{-6} \end{array}$$

Without fine tunings, large δa realize the inflation!

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$$V_{\phi\phi} \sim A\delta^2 a^2 e^{-\delta \cos a\phi} [-\cos(\delta \sin a\phi - 3a\phi + \theta)]$$

$$V_{\phi\phi\phi} \sim A\delta^3 a^3 e^{-\delta \cos a\phi} [-\sin(\delta \sin a\phi - 4a\phi + \theta)]$$

$$m_\phi^2 \sim V_{\phi\phi} \sim A V_0 \delta^2 a^2 \sim 10^{-10}$$

$$\alpha_s = \frac{\text{dlog } n_s}{\text{dlog } k} \sim -2\xi \sim -10^{-3}$$



$$\frac{\epsilon}{\eta} \sim e^{-\delta \cos a\phi}$$

$$|\eta| \sim \frac{|V_{\phi\phi\phi}| \Delta\phi}{V} \sim \frac{A\delta^3 a^3 e^{-\delta \cos a\phi} [-\sin(\delta \sin a\phi - 4a\phi + \theta)]}{A V_0} \sim \delta^2 a^2 \sqrt{\epsilon} \Delta\phi$$

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Without fine tunings, large δa realize the inflation!

Summery of my talk

- Here, we introduce new type of axion inflation model, poly-instanton axion inflation.
- Poly-instanton is a non-perturbative effect in string theory, which induce superpotential like,

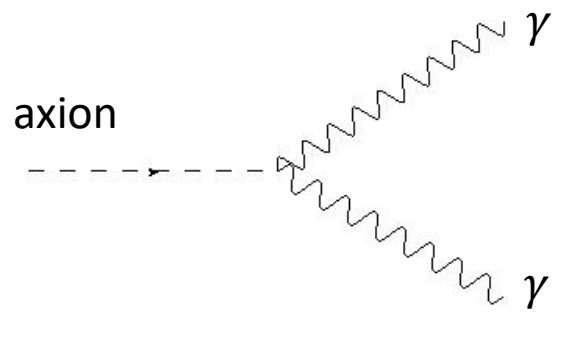
$$\delta W = A e^{-a(T_i + B e^{-2\pi T_j})}$$

- And it can realize a small field inflation.

Thank you!

Test : cosmological history

- Inflaton may decay to photon as,



$$f_{vis} = f_0 + B_{vis} e^{-b_{vis} T_0}.$$

$$\Gamma \sim \gamma^2 \left(\frac{m_\phi}{10^{13} \text{GeV}} \right)^3 \text{GeV},$$

where $\gamma = B_{vis} b_{vis} e^{-b_{vis} \tau_0}.$

when this is dominant decay mode,

$$T_r = \left(\frac{\pi^2 g_*}{90} \right)^{-1/4} \sqrt{\Gamma M_{Pl}} \sim 10^9 \gamma \left(\frac{m_\phi}{10^{13} \text{GeV}} \right)^{3/2} \text{GeV},$$

Reheating temperature is rather low.