

21cm line signals from minihalos as a probe of primordial fluctuations

Toyokazu Sekiguchi (IBS-CTPU)



In collaboration with:

Joe Silk (IAP), Naoshi Sugiyama (Nagoya), Tomo Takahashi (Saga),
Hiroyuki Tashiro (Nagoya) & Shuichiro Yokoyama (Rikkyo)

Plan of talk

- Introduction: minihalos in dark ages and its redshifted 21 cm line signal
- Application: a probe of primordial fluctuations
 - ▶ Spectral runnings of power spectrum
 - ▶ Primordial non-Gaussianity
- Summary

Refs:

- ❖ H. Tashiro, T. Sekiguchi & J. Silk, N. Sugiyama [arXiv:1311.3295]
- ❖ T. Sekiguchi, T. Takahashi, H. Tashiro & S. Yokoyama [arXiv: 1705.00405]
- ❖ T. Sekiguchi, T. Takahashi, H. Tashiro & S. Yokoyama [in prep.]

Introduction

CMB last scattering $z \sim 10^3$

ionization Era?
of the Cosmic History

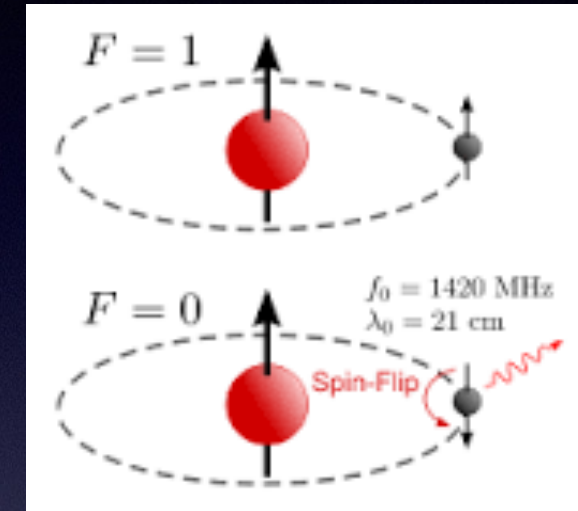
Dark ages (~cosmic dawn)

✓ neutral hydrogen

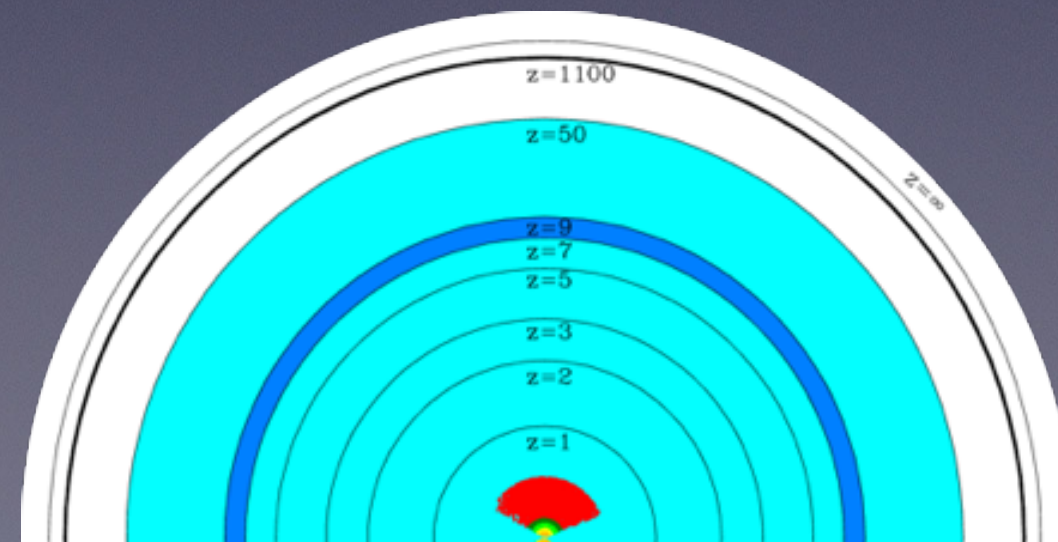
→ redshifted 21cm line

- tracer of matter fluctuations

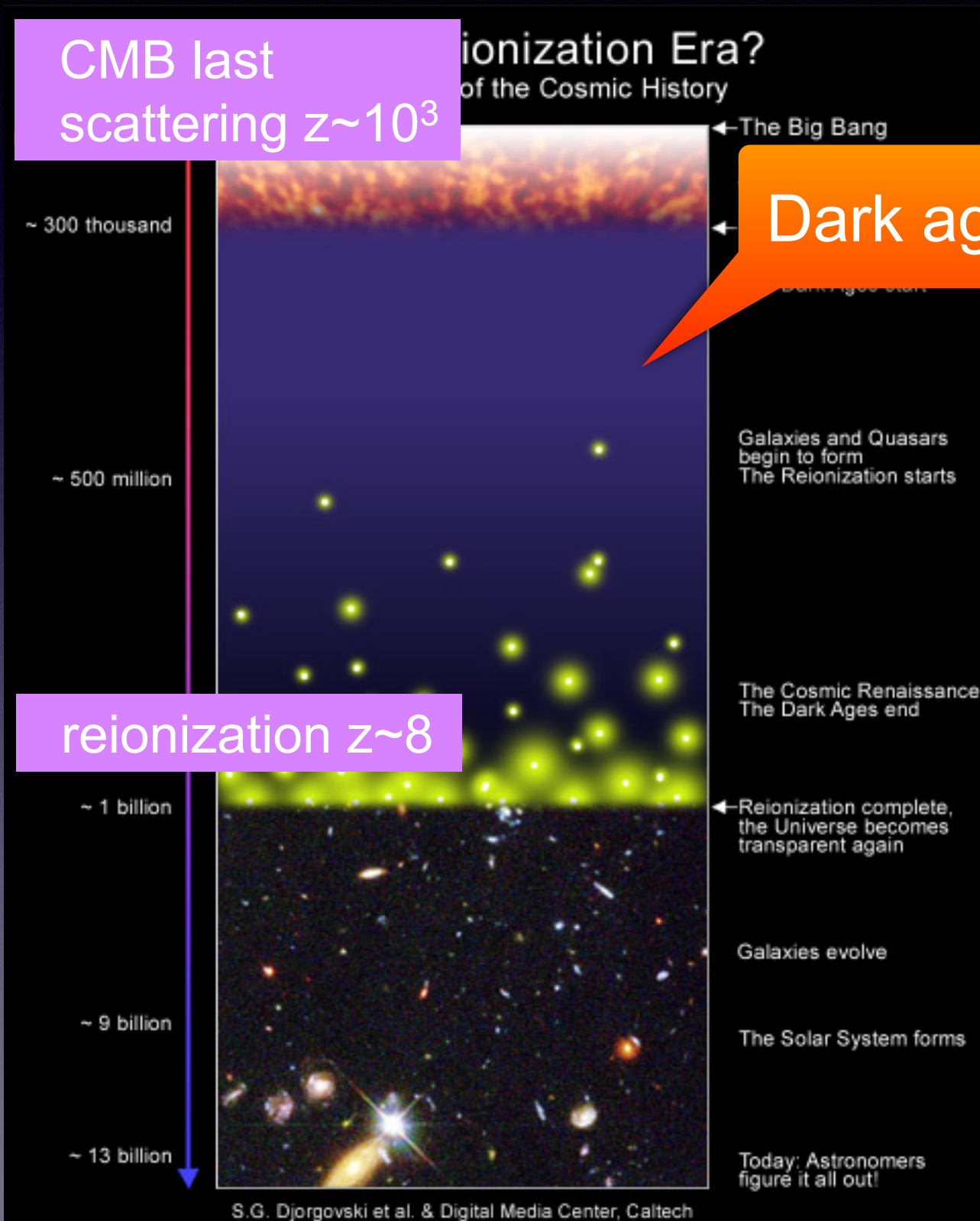
- tomography → 3D mapping



reionization $z \sim 8$



Mao+ 2008



S.G. Djorgovski et al. & Digital Media Center, Caltech

Redshifted 21cm line surveys

On-going:

LOFAR, MWA, PAPER, ...

Near future:

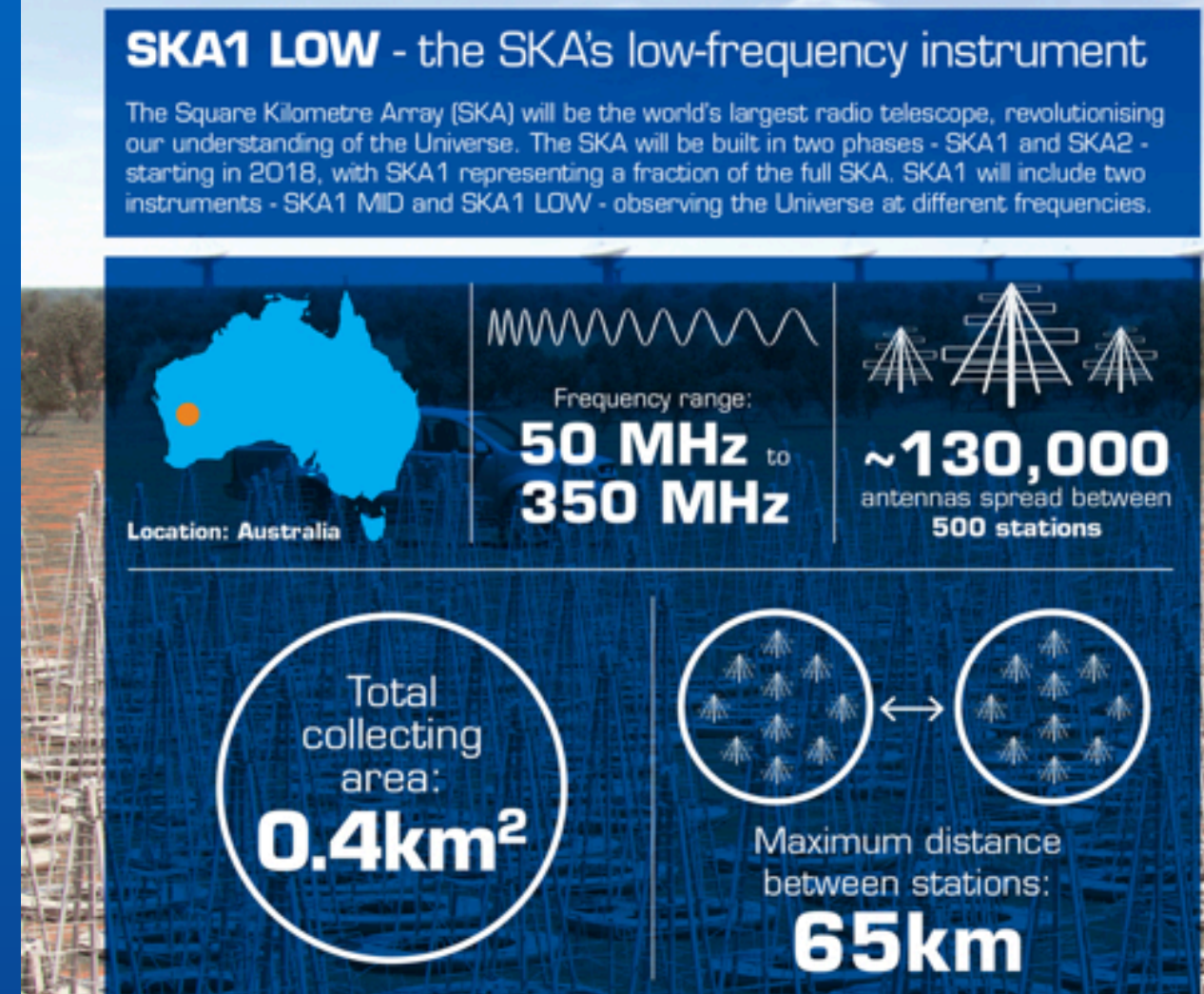
- Square Kilometer Array (SKA)

21cm line from $3 < z < 27$; SKA1-low will start from 2021

- Hydrogen Epoch Reionization Array (HERA)

main target: 21cm line from $7 < z < 12$

➡ Implications for cosmology and particle physics?



(c) www.skatelescope.org

Sources of 21cm line



Minihalos

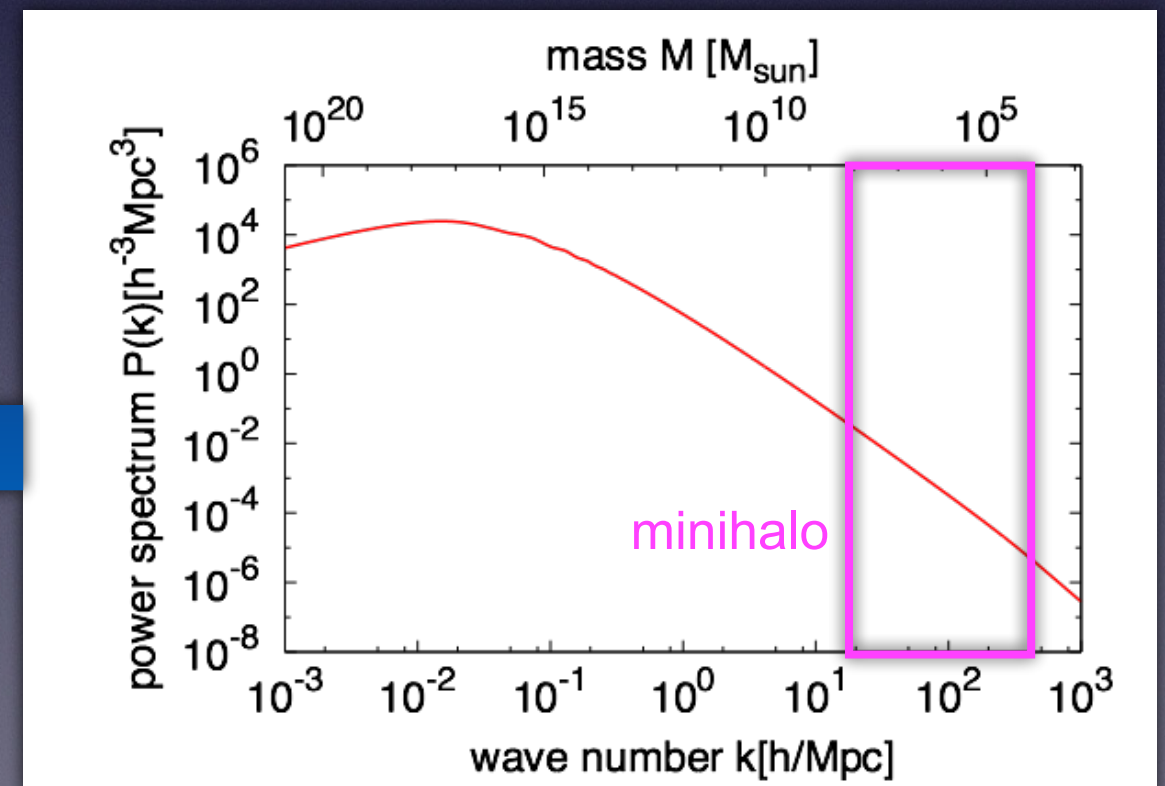
Halos too small to host galaxies

- No star formation: $T_{\text{gas}} < 10^4 \text{K}$ (inefficient radiative cooling)
→ dense neutral hydrogen inside; resistant to ionization

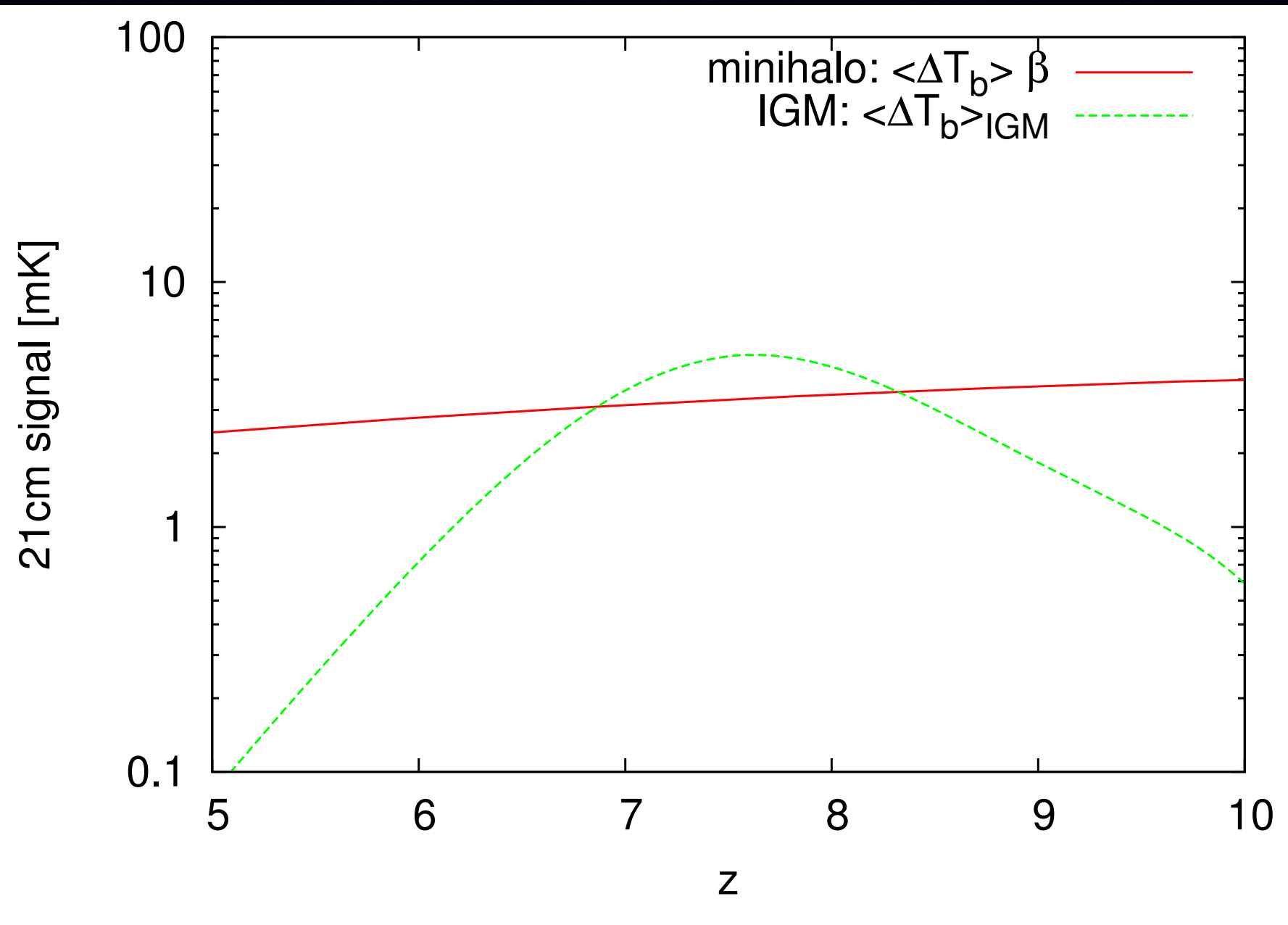
- Mass: $10^4 M_{\text{sun}} < M < 10^8 M_{\text{sun}}$

Sensitive to small-scale
($< 0.1 \text{Mpc}$) fluctuations

- Abundant, even at high- z



Minihalos vs IGM



Model of IGM consistent with
the recent Planck constraint
[Adam+1605:03507](#)

Minihalo contribution can dominate at a broad range of redshifts

frequency $\leftrightarrow$ redshift $\leftrightarrow$ radial distance

Observable

$$\nu = \frac{\nu_0}{1 + z_\nu} \quad r_\nu = r(z_\nu)$$

Redshifted 21cm line fluctuations from minihalos

$$\delta[\Delta T_b](\hat{n}, \nu) = \left[\int_{M_{\min}}^{M_{\max}} dM \Delta T_b(M, z_\nu) \frac{dN(M, z_\nu)}{dM} b(M, z) \right] \delta(\vec{x} = r_\nu \hat{n}, z_\nu)$$

strength of 21cm line
emission/absorption
from single minihalo

mass function

halo bias

sensitive to small-scale
($< \text{Mpc}$) matter fluctuations

matter fluctuations
at large scales
($> \text{Mpc}$)

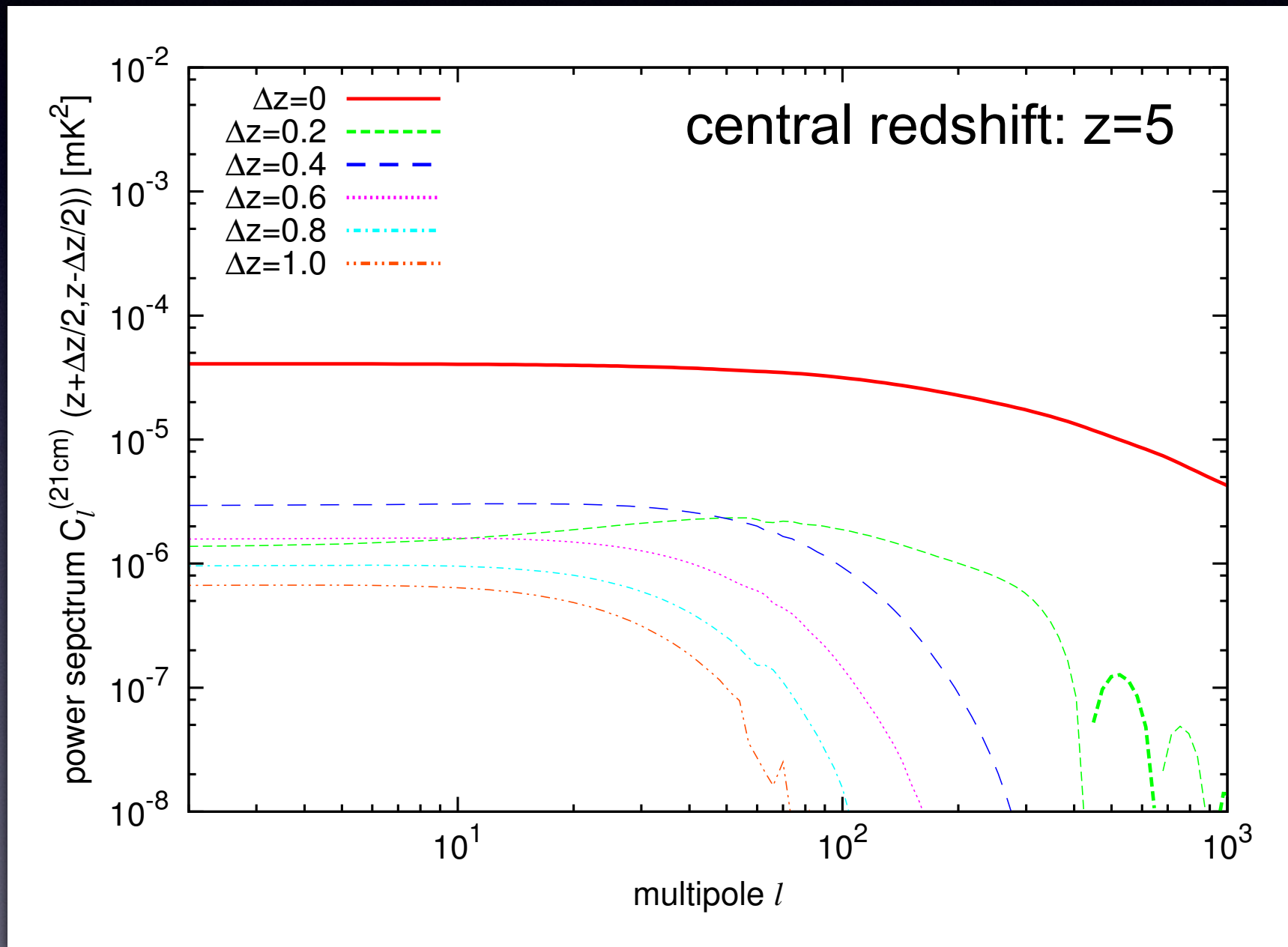
Tomographic angular power spectrum

TS, Takahashi, Tashiro & Yokoyama [arXiv:1705.00405]

$$C_l(z, z') = \frac{1}{2l + 1} \sum_m a_{lm}(z) a_{lm}^*(z')$$

with $a_{lm}(z_\nu) = \int d\hat{n} \delta[\Delta T_b](\hat{n}, \nu) Y_{lm}^*(\hat{n})$

Tomographic angular power spectrum



* Redshift space distortion is included

Application (1): Primordial spectral runnings

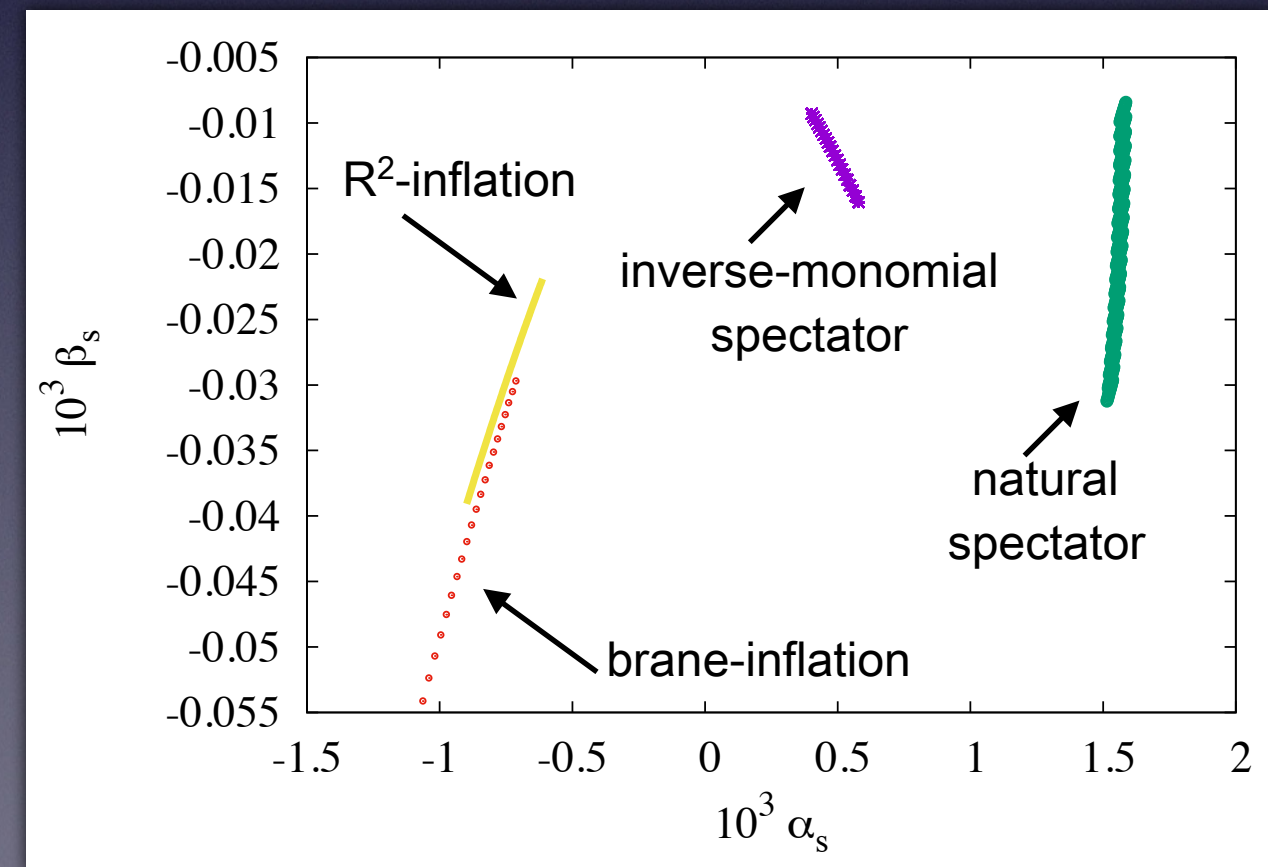
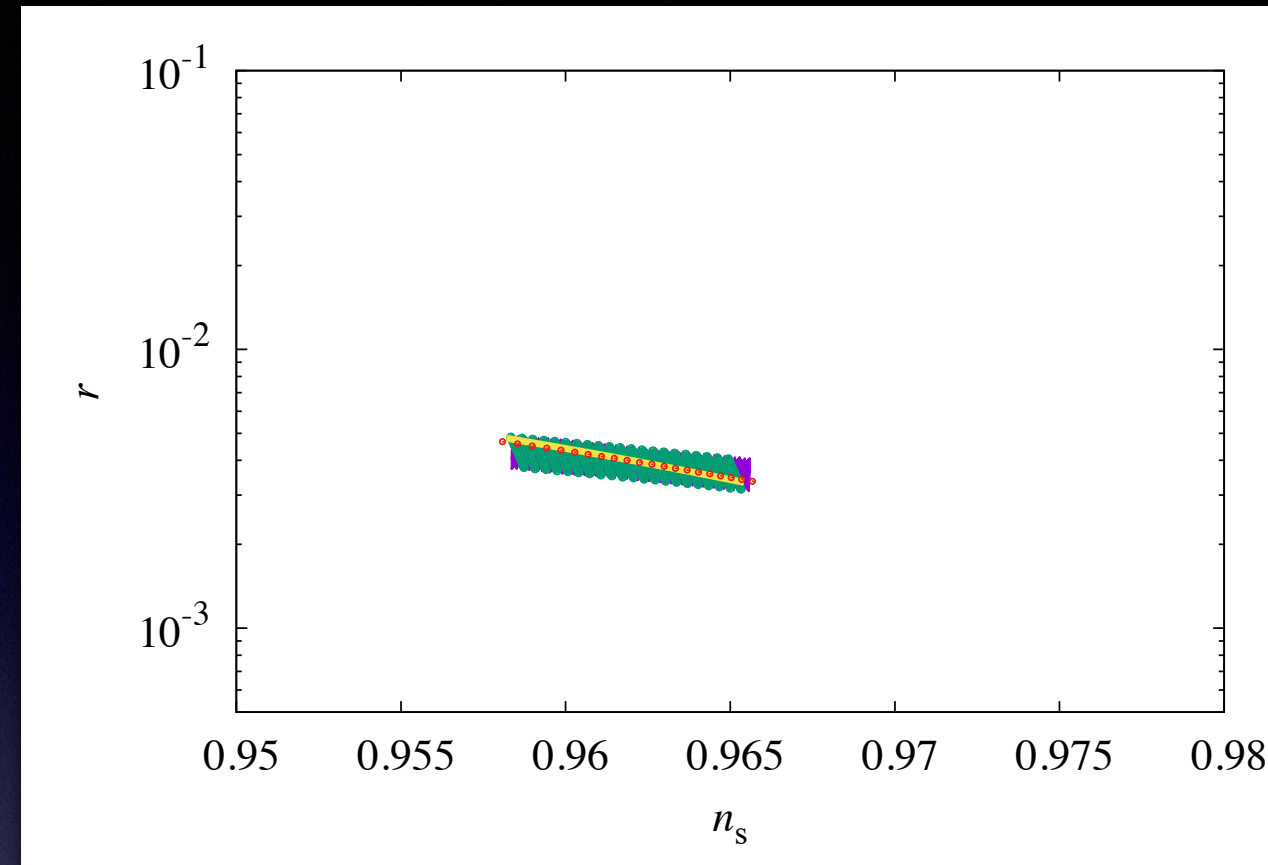
TS, Takahashi, Tashiro & Yokoyama [arXiv:1705.00405]

Spectrum of primordial fluctuations

$$\mathcal{P}(k) \propto k^{n_s - 1 + \frac{1}{2}\alpha_s \ln(k/k_*) + \frac{1}{6}\beta_s \ln^2(k/k_*) + \dots}$$

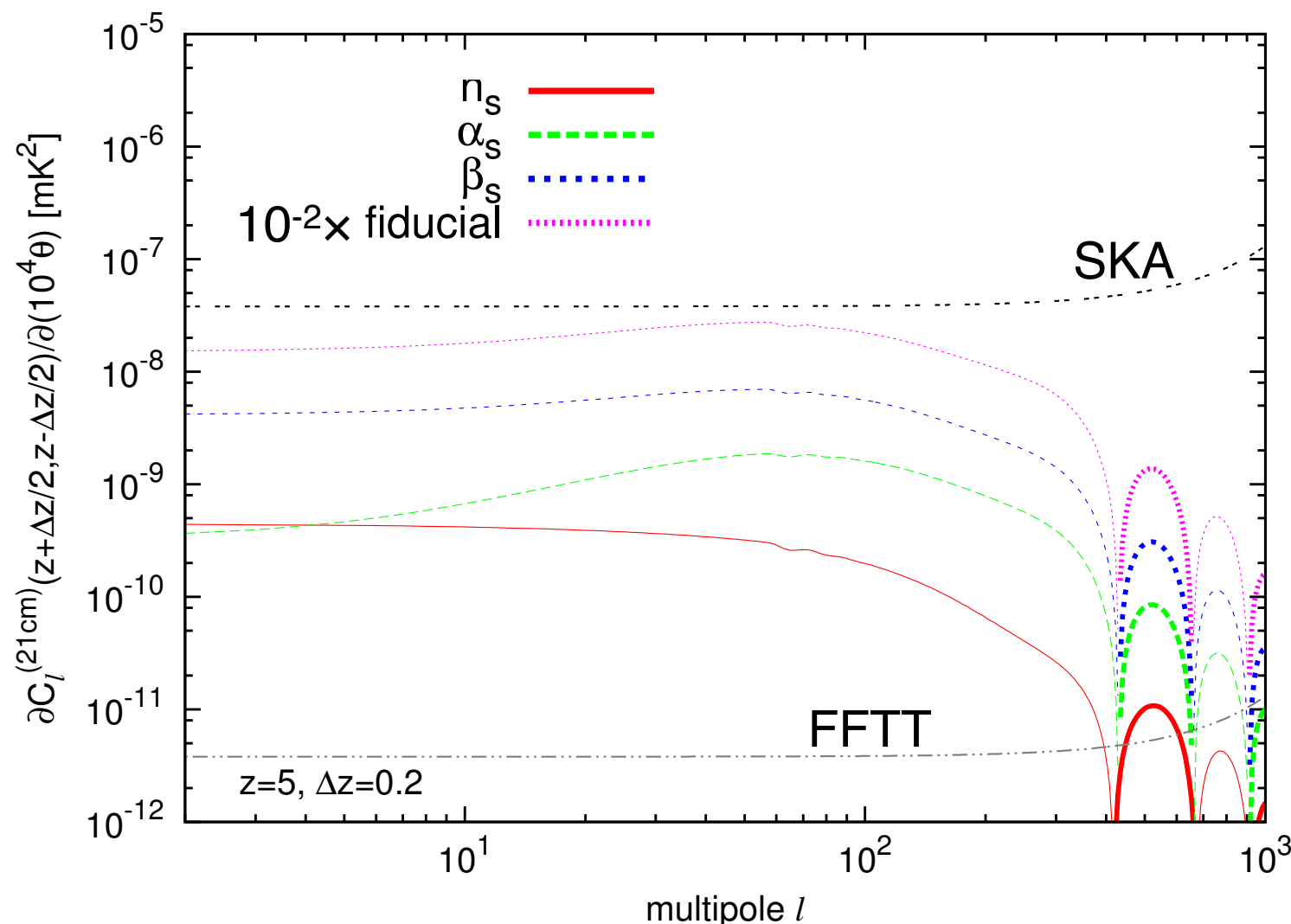
- Many models degenerate in the n_s - r plane
- However, they can be distinguished from the scale dependence of n_s

Spectral runnings: a key observable for discriminating inflation models



Application (1): Primordial spectral runnings (cont'd)

Parameter response



- Lower order spectral parameters (e.g. n_s or α_s) $\rightarrow$ spectral shapes
- Higher order parameters (e.g. β_s) $\rightarrow$ overall amplitudes
- $\rightarrow$ Solves parameter degeneracy
- Radial scale-dependence also enhances the discrimination

Application (1): Primordial spectral runnings (cont'd)

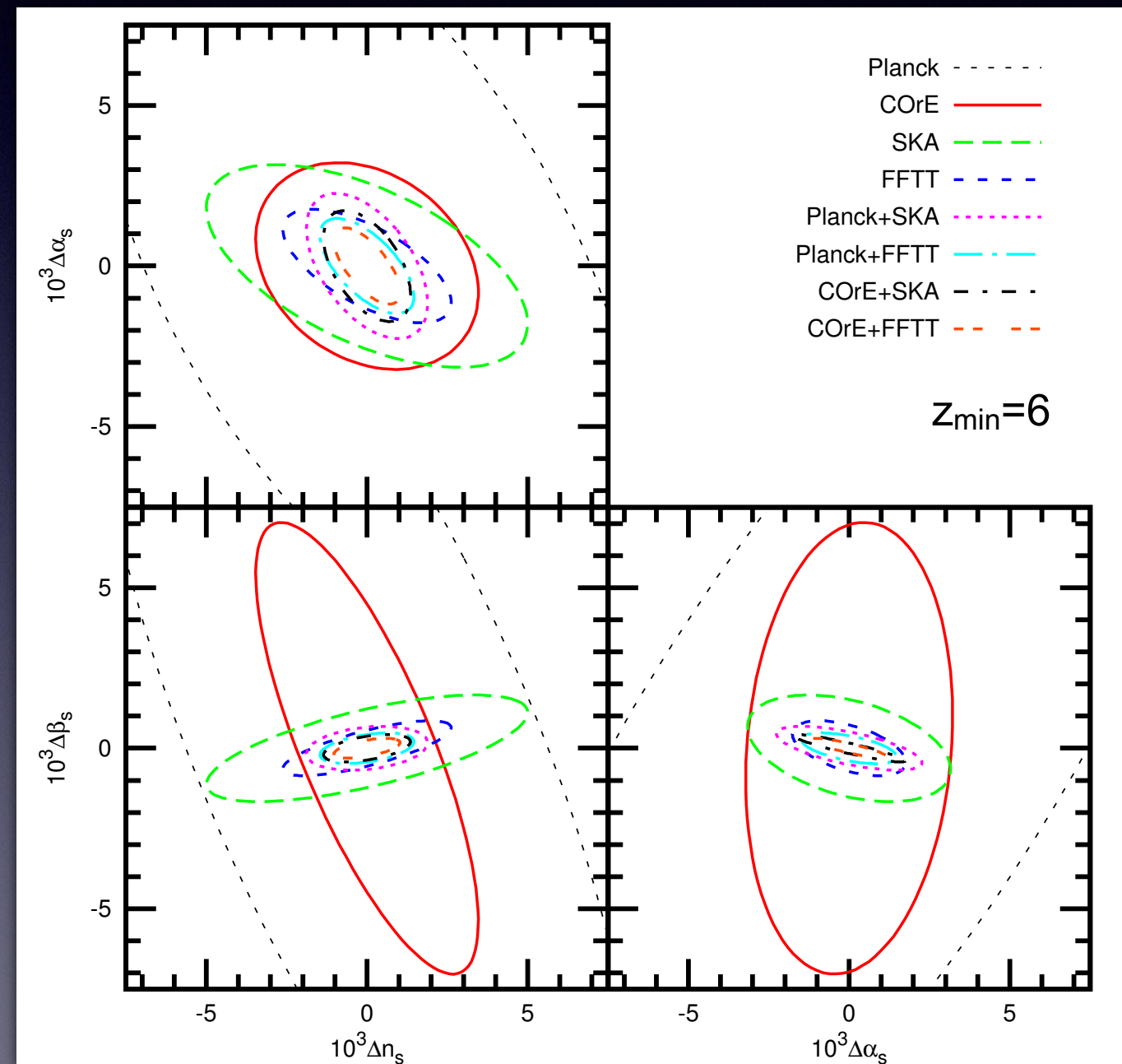
Forecasted constraints

Combination of CMB and 21cm is beneficial due to lever-arm effect.

$$\Delta\alpha_s=10^{-3}, \Delta\beta_s=10^{-4}$$

Constraints are dependent on $z_{\min}$ only mildly.

	$z_{\min}$	$10^{-3}\Delta n_s$	$10^{-3}\Delta\alpha_s$	$10^{-3}\Delta\beta_s$
Planck+SKA	4	1.4	1.4	0.40
	6	1.7	2.0	0.63
	8	2.3	3.0	0.85
	10	3.6	4.7	1.2
COrE+FFTT	4	0.85	0.96	0.24
	6	0.95	1.1	0.28
	8	1.0	1.2	0.31
	10	1.1	1.3	0.33



Application (2): Primordial non-Gaussianity

TS, Takahashi, Tashiro & Yokoyama, in prep.

Local type non-Gaussianity:

$$\Phi(\vec{x}) = \Phi_G(\vec{x}) + f_{\text{NL}}(\Phi_G(\vec{x})^2 - \langle \Phi_G \rangle^2) + g_{\text{NL}}\Phi_G(\vec{x})^3$$

- Small in single field inflation: $f_{\text{NL}} \sim \mathcal{O}(0.01)$, $g_{\text{NL}} < \mathcal{O}(10^{-3})$
- Large in multi-field models (e.g. curvaton, modulated reheating, etc.)

Current tightest bound (Planck 2015)

$$f_{\text{NL}} = 0.8 \pm 5.0, \quad g_{\text{NL}} = (9.0 \pm 7.7) \times 10^4$$

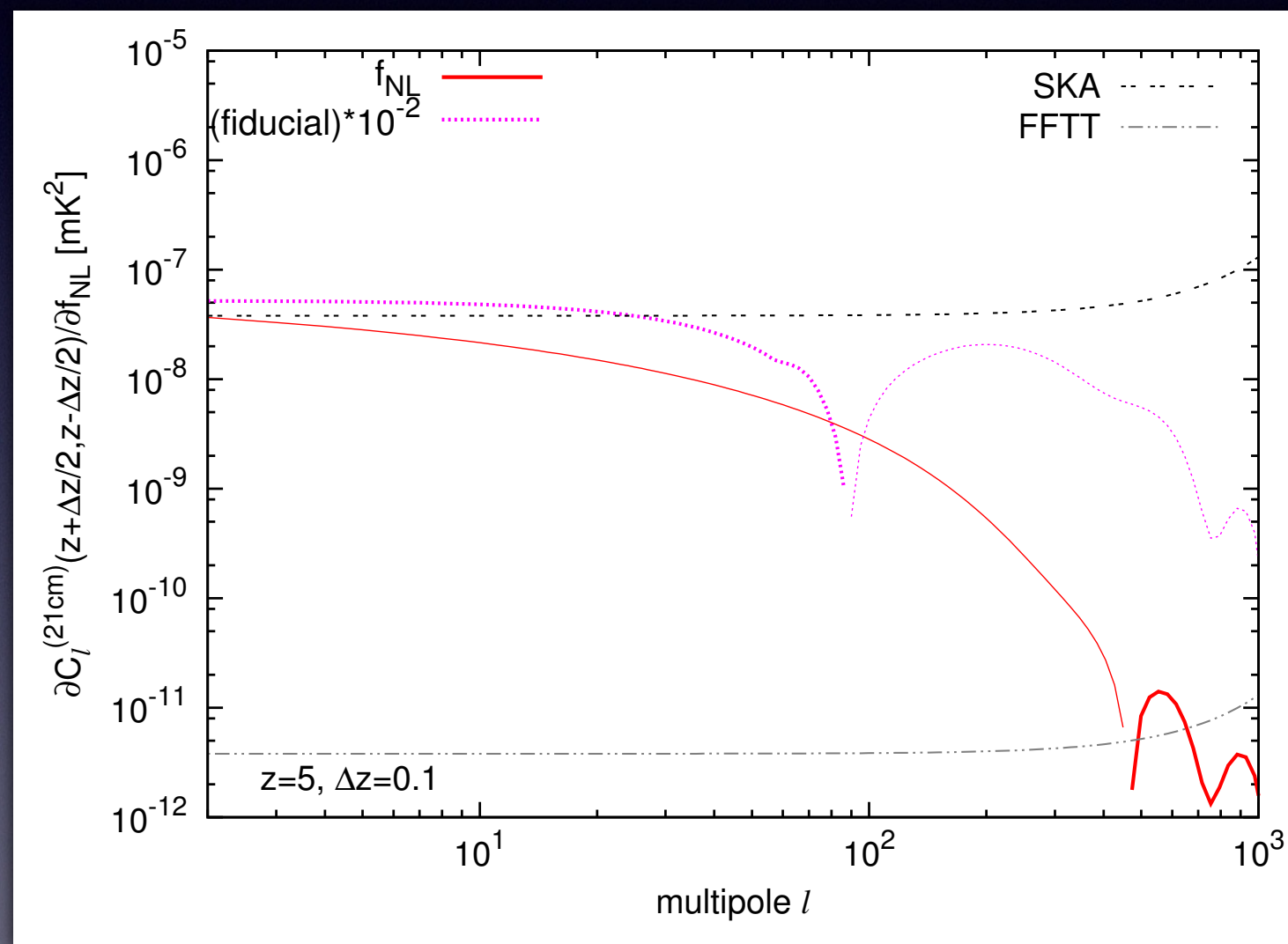
Application (2): Primordial non-Gaussianity (cont'd)

Effects on minihalo spectrum

- Coupling between large and small scale fluctuations
- Abundance of (mini)halos is modulated by large scale fluctuations

→ scale-dependent halo bias

Dalal+(2008); Slosar+(2008)



Application (2): Primordial non-Gaussianity (cont'd)

Forecasted constraints

- SKA

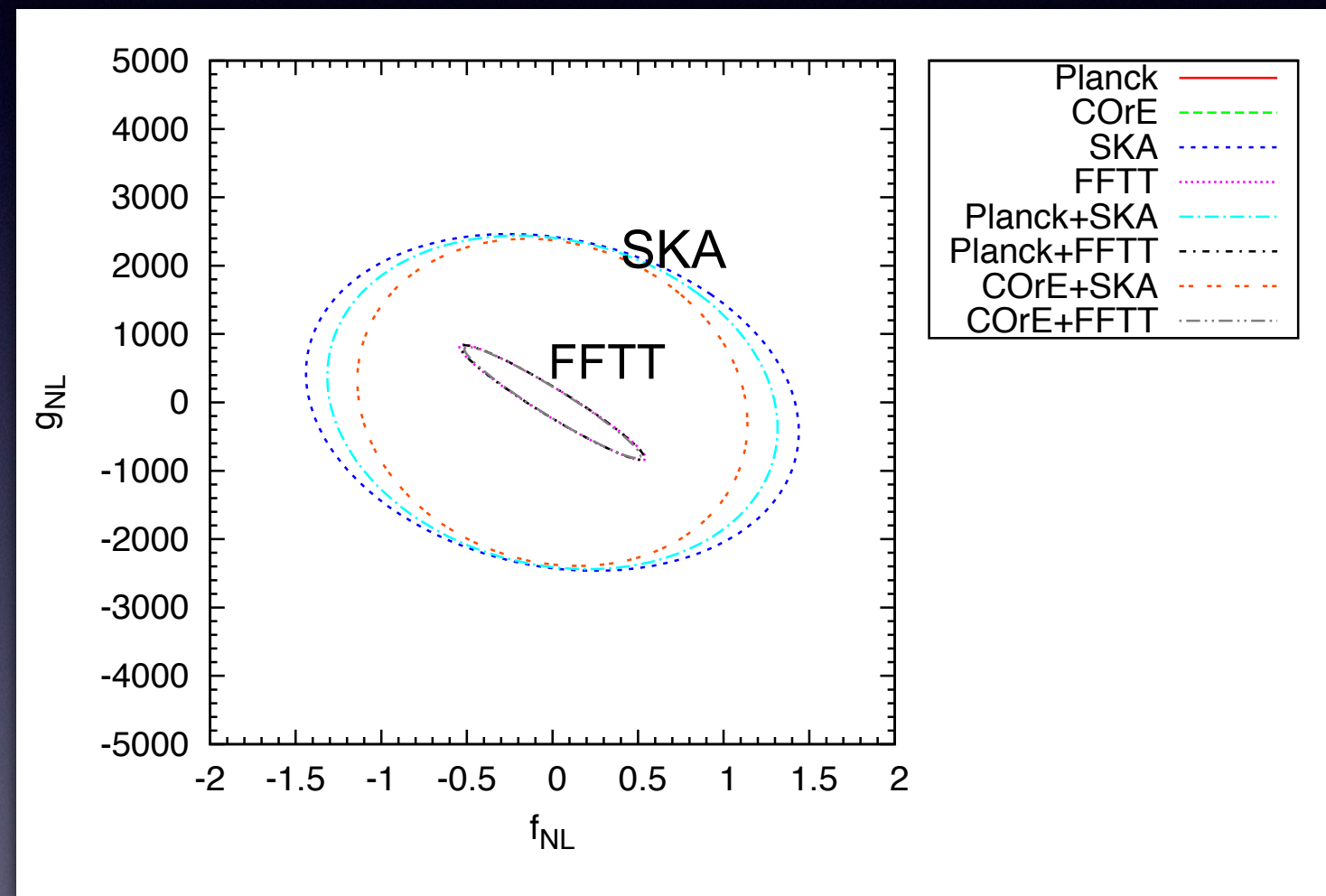
$$\Delta f_{\text{NL}}=0.7, \Delta g_{\text{NL}}=2 \times 10^3$$

- FFTT

$$\Delta f_{\text{NL}}=0.1, \Delta g_{\text{NL}}=7 \times 10^2$$

- cf. Future CMB (COrE)

$$\Delta f_{\text{NL}}=2, \Delta g_{\text{NL}}=2 \times 10^4$$



Minihalos potentially improve the (saturated) CMB bound
by orders of magnitude

Summary

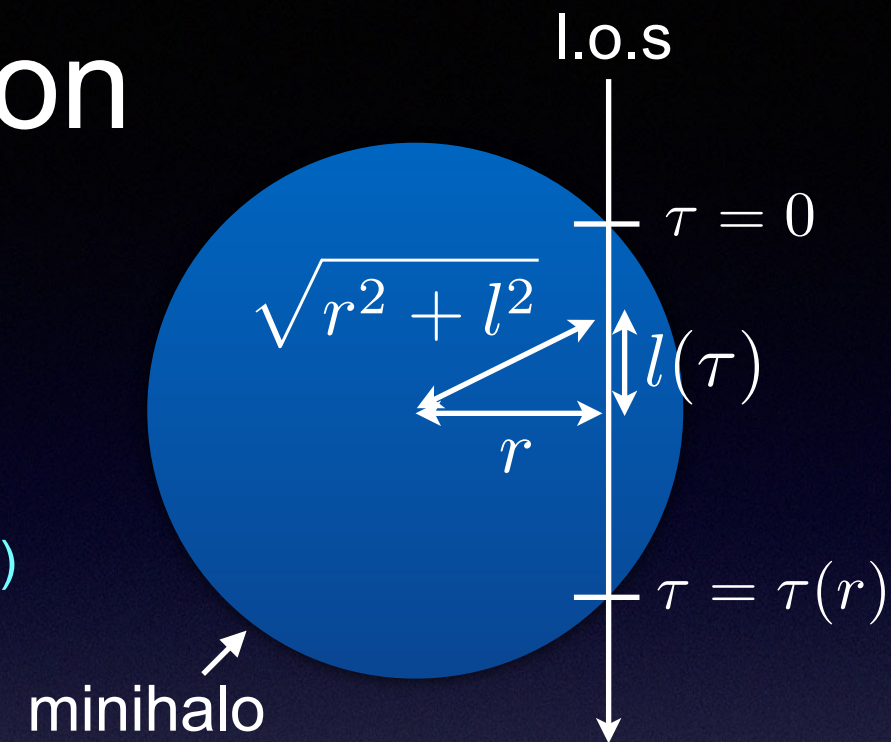
- Minihalos can probe primordial fluctuations at a wide range of scales, especially those at small scales ($\ll \text{Mpc}$), which are difficult to be probed by other observations.
- 21cm signal from can probe primordial fluctuations with increased statistics and enhanced range of scales. Our formulation of tomographic angular spectrum can maximally exploit such advantage in minihalos.
 - ▶ Spectral runnings of primordial spectrum
 - ▶ Non-Gaussianity
- Lots of other cosmological applications (e.g. WDM [TS & Tashiro arXiv: 1401.5563]) can be considered.

backup slides

Details of calculation

21cm line signals from single minihalo

based on Iliev+(2002)



- minihalo has an inner structure
→ line of sight integral + average over cross-section

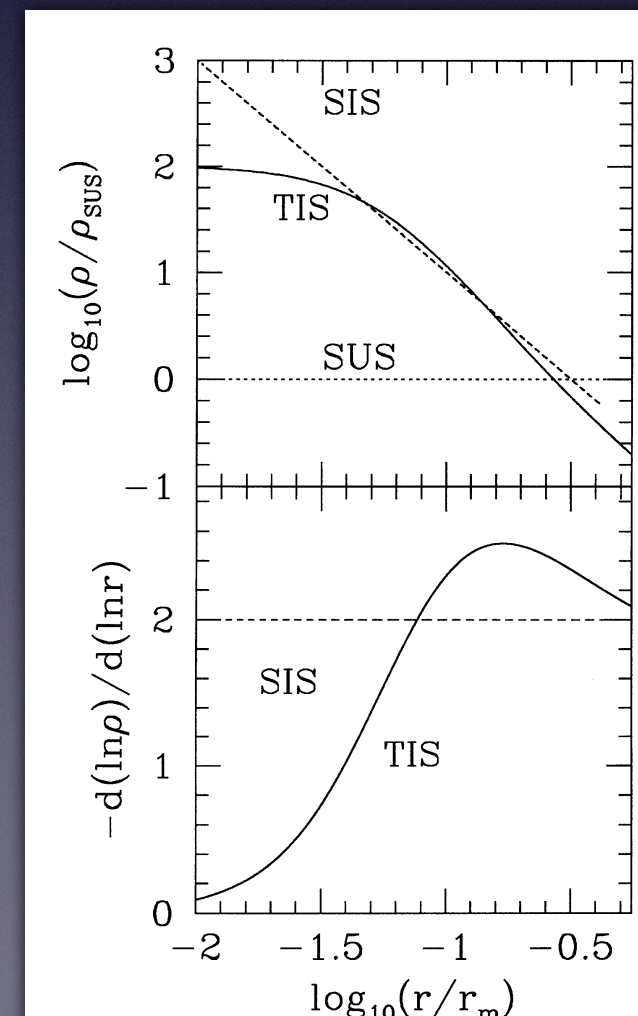
$$\Delta T_b(M, z) = A^{-1} \int dA \int_0^{\tau(r)} d\tau [T_S(\sqrt{r^2 + l(\tau)^2}) - T_{\text{CMB}}] e^{-\tau}$$

with $A = \pi r_{\text{halo}}^2$

- halo profile: truncated isothermal sphere (TIS)
Shapiro, Iliev & Raga (1999)

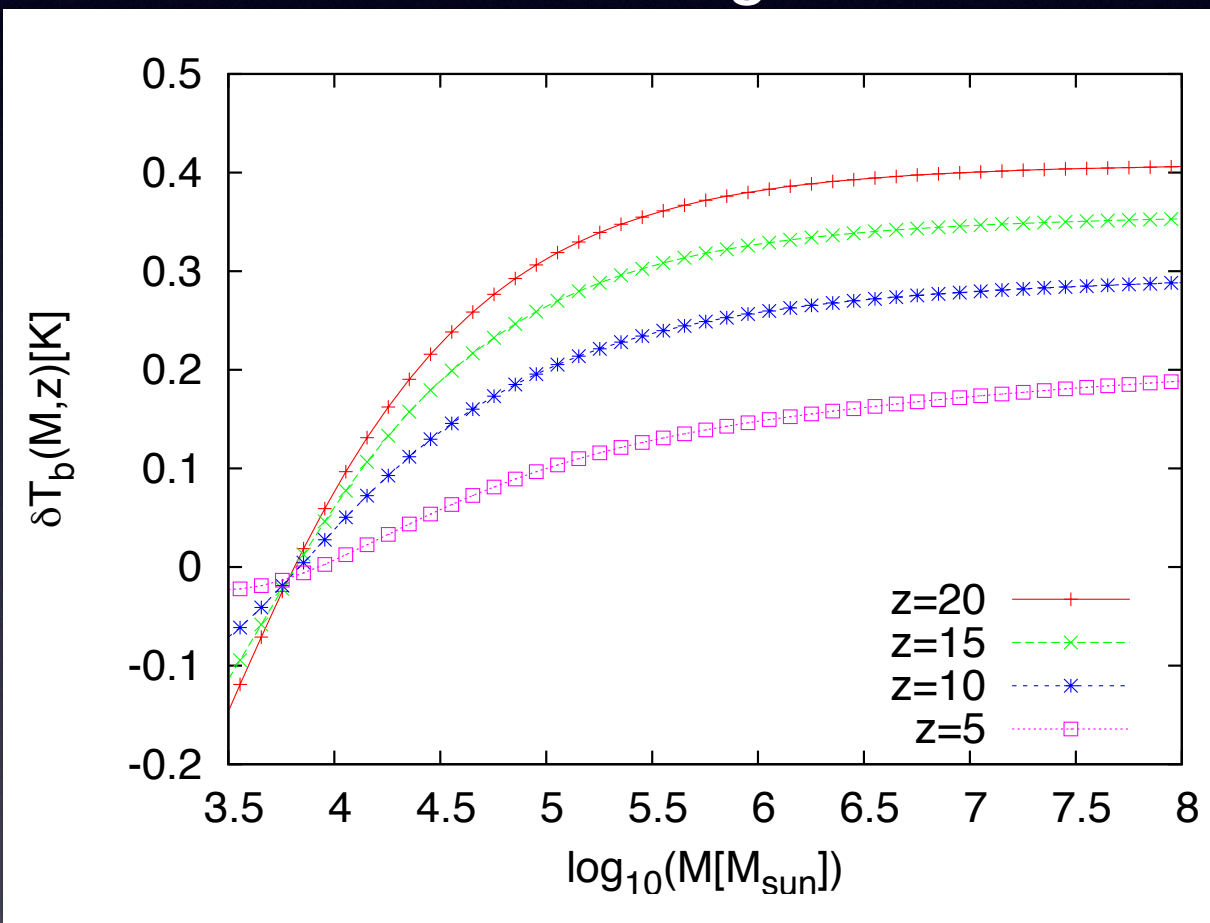
- spin temperature: strongly coupled with gas

$$T_S \approx T_{\text{gas}}$$

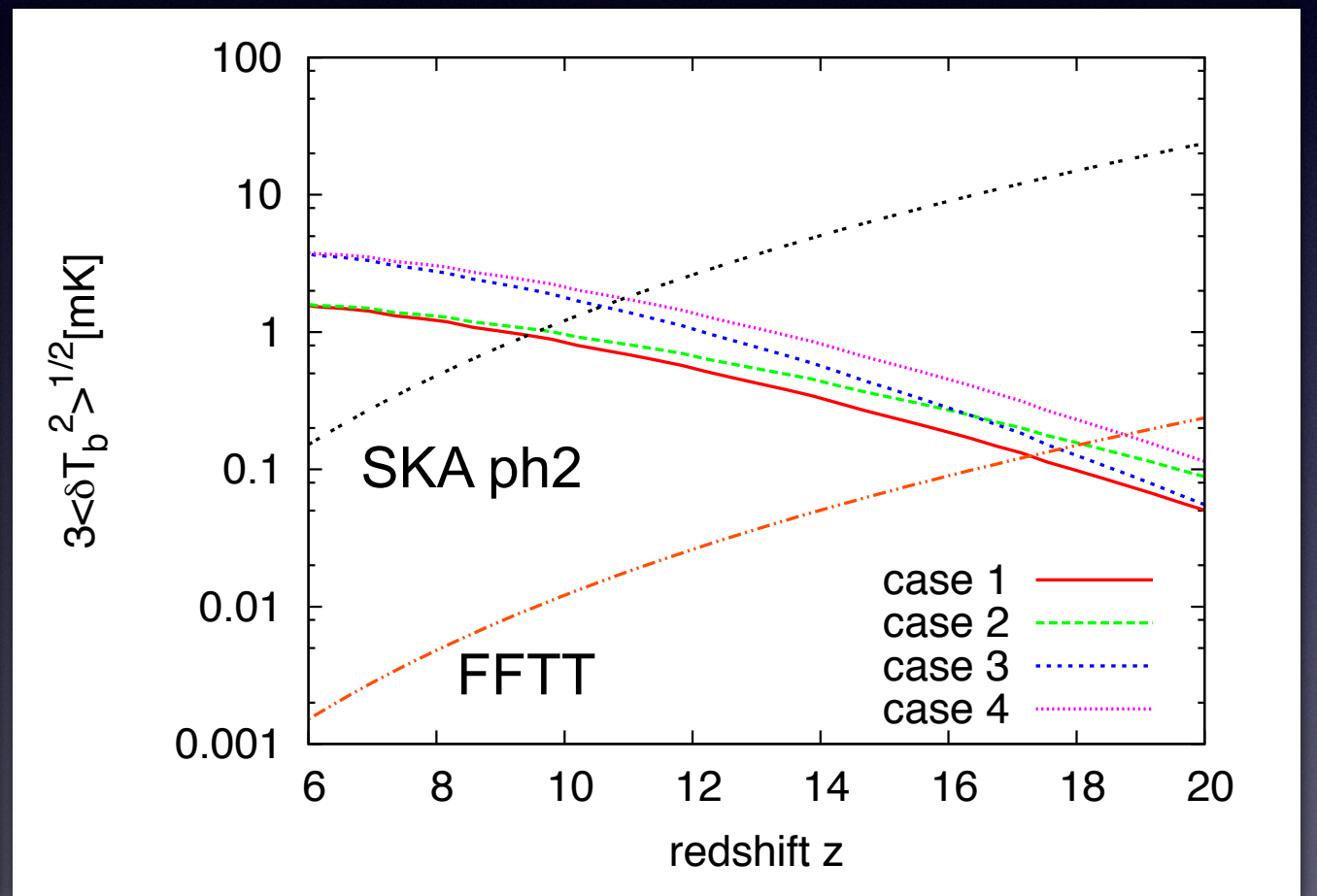


21cm signal

contributions from single halo



rms of 21cm fluctuations
(SKA-like survey with $\Delta\theta=9'$,
 $\Delta\nu=1\text{MHz}$)



21cm signal from minihalos
can be observed by SKA

case 1: PS & $\delta_c=1.67$
case 2: PS & $\delta_c=1.52$
case 3: ST & $\delta_c=1.67$
case 4: ST & $\delta_c=1.52$

Specification of surveys

	SKA	FFTT
total effective area A_{tot} [m ²]	10^5	10^7
bandwidth $\Delta\nu$ [MHz]		1
beam width $\Delta\theta$ [arcmin]		9
integration time t [hour]	1000	

Table 1. Specification of 21 cm surveys.

	Planck			COrE				
band frequency [GHz]	100	147	217	105	135	165	195	225
beam width $\Delta\theta$ [arcmin]	9.9	7.2	4.9	10.0	7.8	6.4	5.4	4.7
Temperature noise Δ_T [μ K arcmin]	31.3	20.1	28.5	2.68	2.63	2.67	2.63	2.64
Polarization noise Δ_P [μ K arcmin]	44.2	33.3	49.4	4.63	4.55	4.61	4.54	4.57

Table 2. Specification of CMB surveys.

Blue-tilted isocurvature power spectrum

Isocurvature perturbations

Relative perturbations between matter and radiation

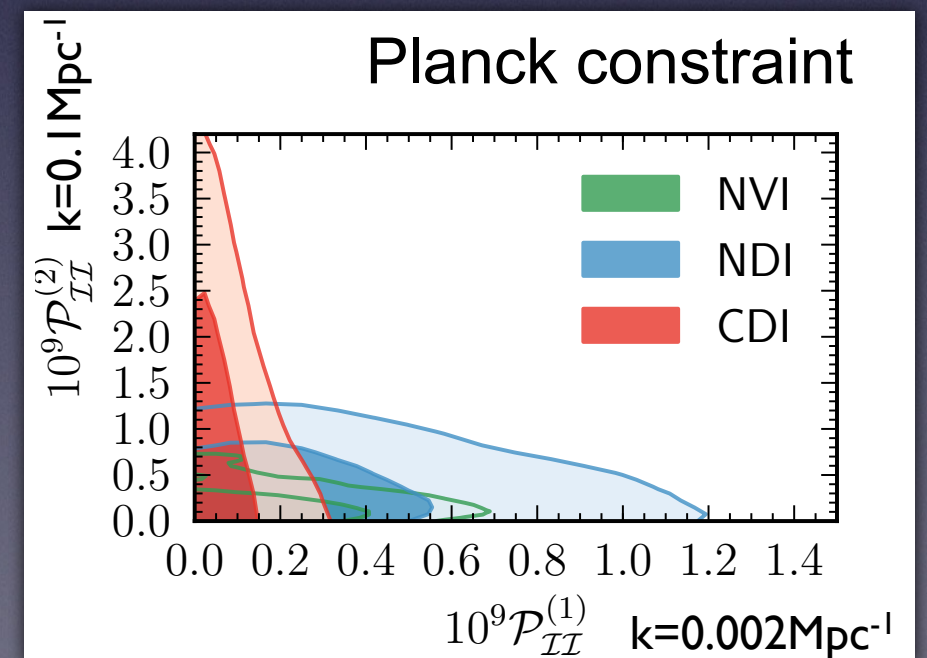
$$S(\vec{x}) = \delta \log \left(\frac{n_{\text{matter}}(\vec{x})}{n_{\text{rad}}(\vec{x})} \right)$$

Theoretical models: axion (uncorrelated), curvaton (correlated), ...

Power spectrum

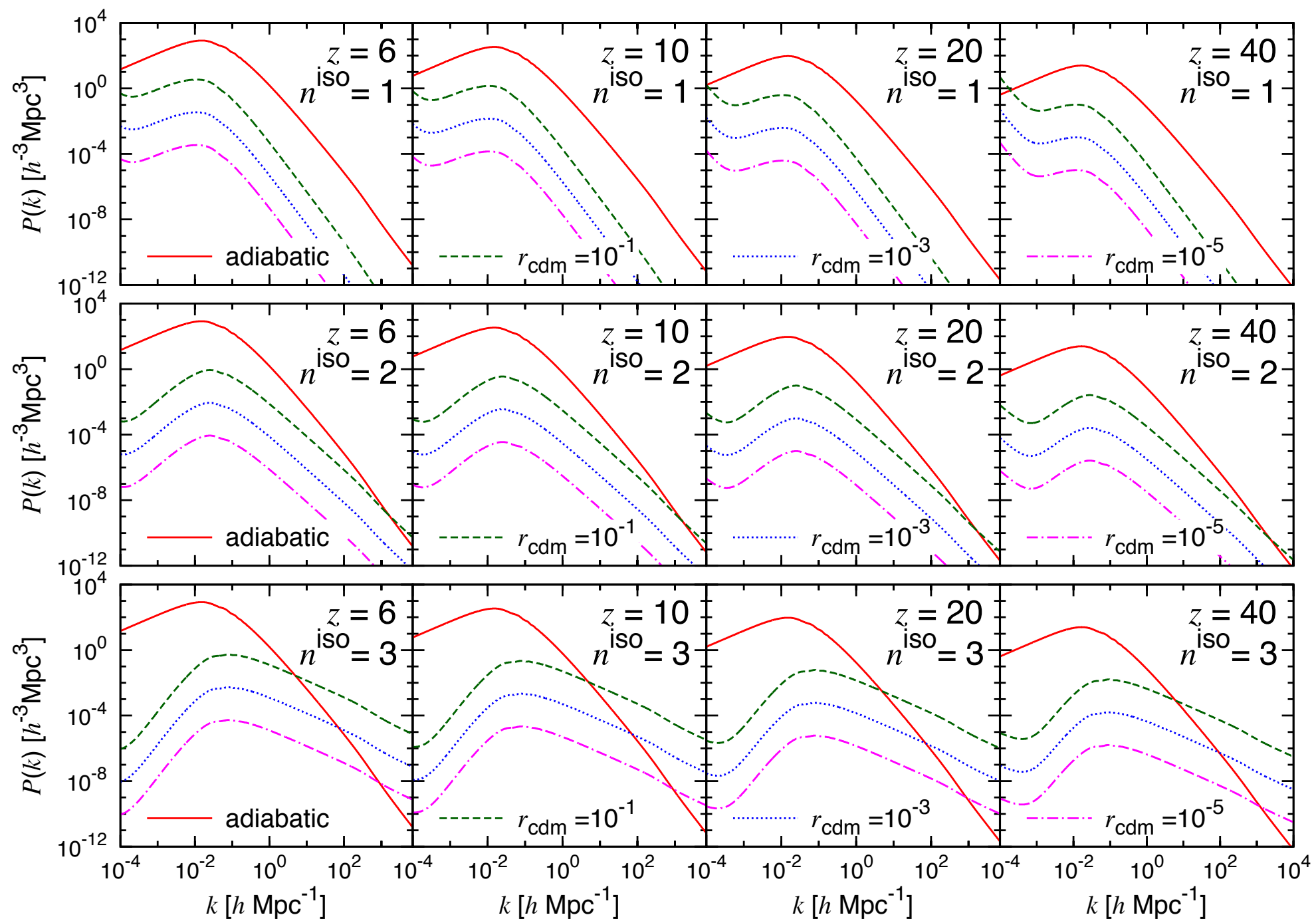
$$P_S(k) \propto \alpha k^{p-1}$$

$$\alpha = P_S(k_0)/P_\zeta(k_0) \quad \text{at } k_0=0.002\text{Mpc}^{-1}$$

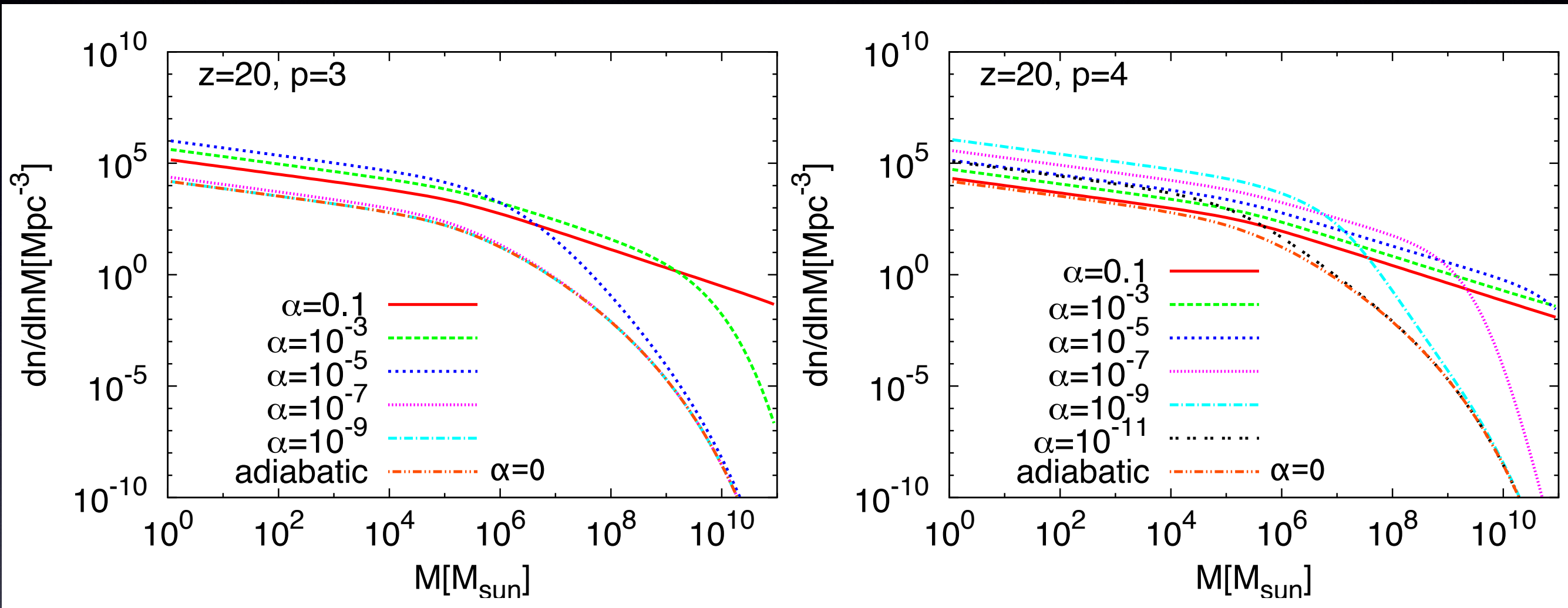


Blue spectrum (e.g, Kasuya & Kawasaki '09) is less constrained from CMB C_l

Matter power spectrum



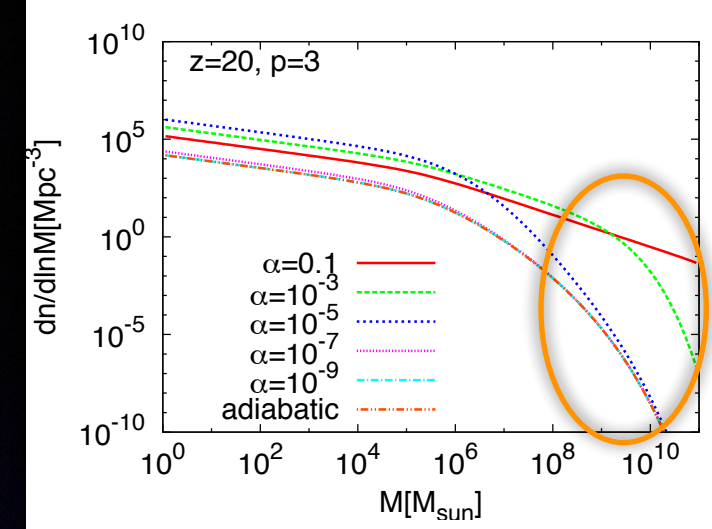
Effects on mass function



Mass function does not change monotonically:

- ▶ Small α : abundance of halos increases at all M as α increases
- ▶ Large α : abundance of small halos starts to decrease
← incorporation of smaller haloes into larger ones

Constraint from reionization



Isocurvature pert. with blue spectrum can promote reionization

Sugiyama, Zaroubi & Silk (2004)

- Simplified modeling of reionization Tegmark & Silk (1994)

excluded by
 $\tau_{\text{reion}} < 0.13$

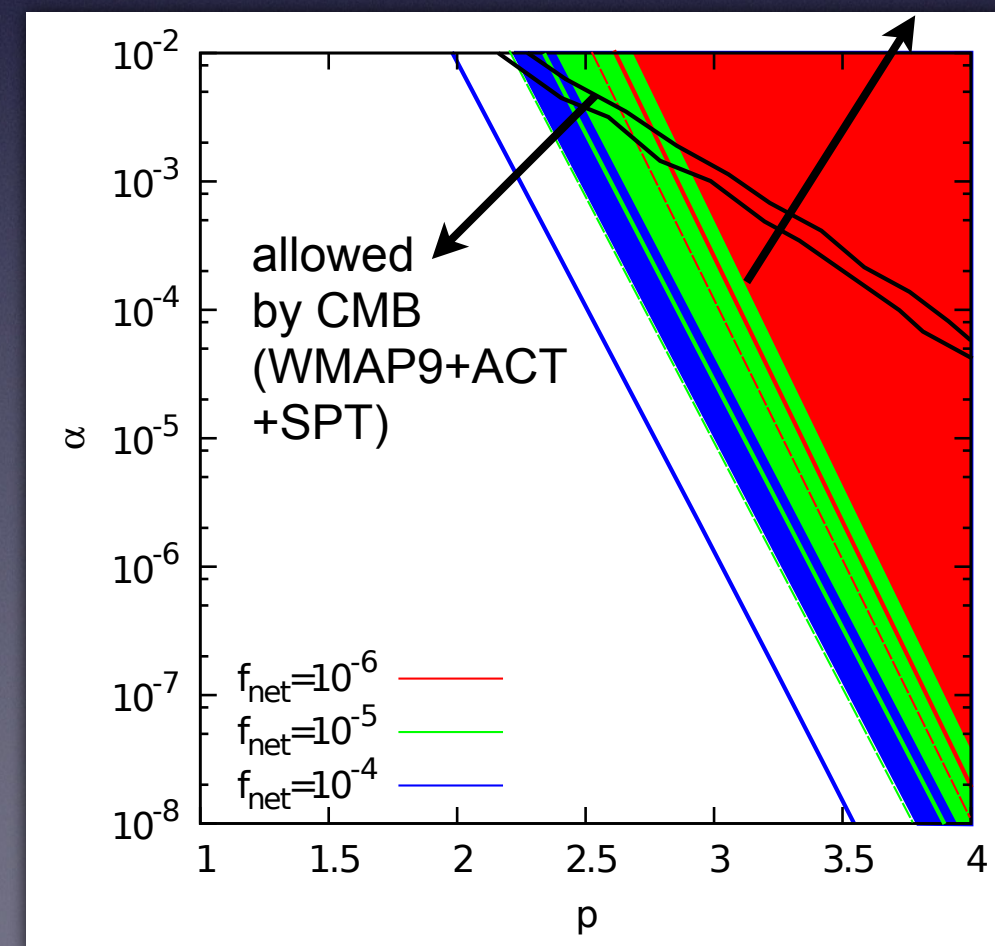
$$x_{\text{reion}} = f_{\text{coll}} \frac{\Delta m_p c^2}{13.6 \text{eV}} f_{\text{burn}} f_{\text{UV}} f_{\text{esc}} f_{\text{ion}} = f_{\text{net}} \sim 10^{-4}$$

collapsed baryon
fraction in massive
halos

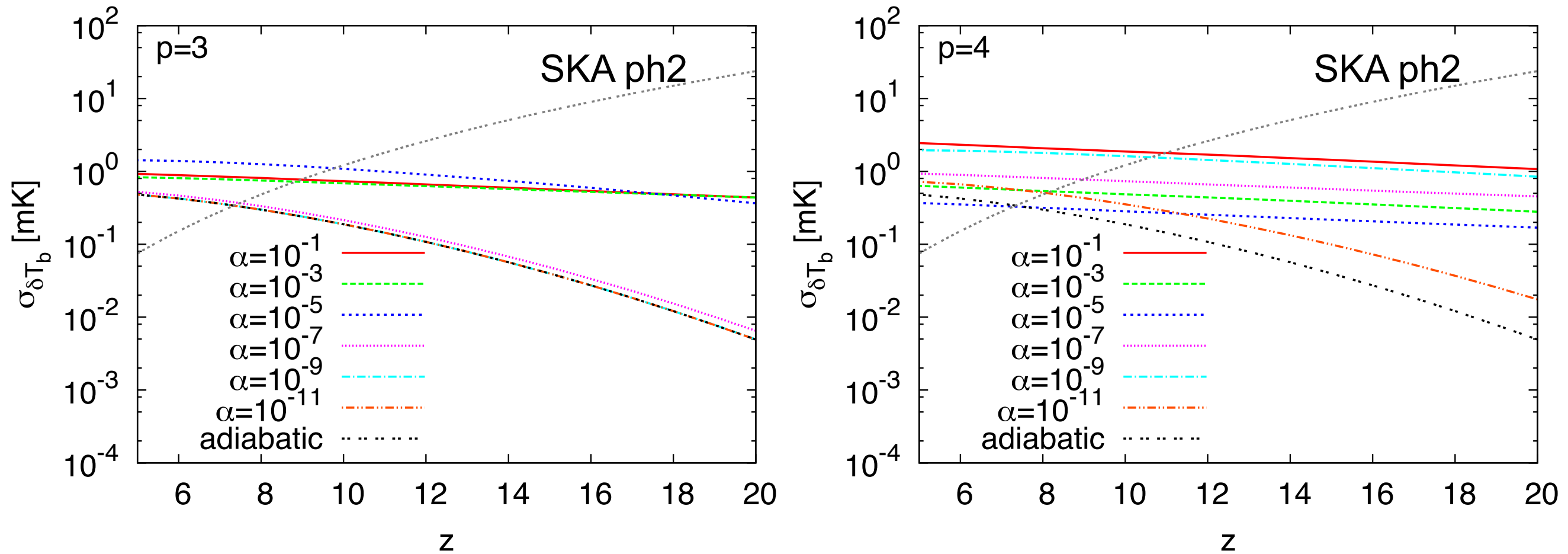
for Pop II model
(Sommerville & Lavio 2003)

- Constraints from τ_{reion}

→ Tighter constraints than from C_l^{TT}
(even with the large uncertainty in f_{net})



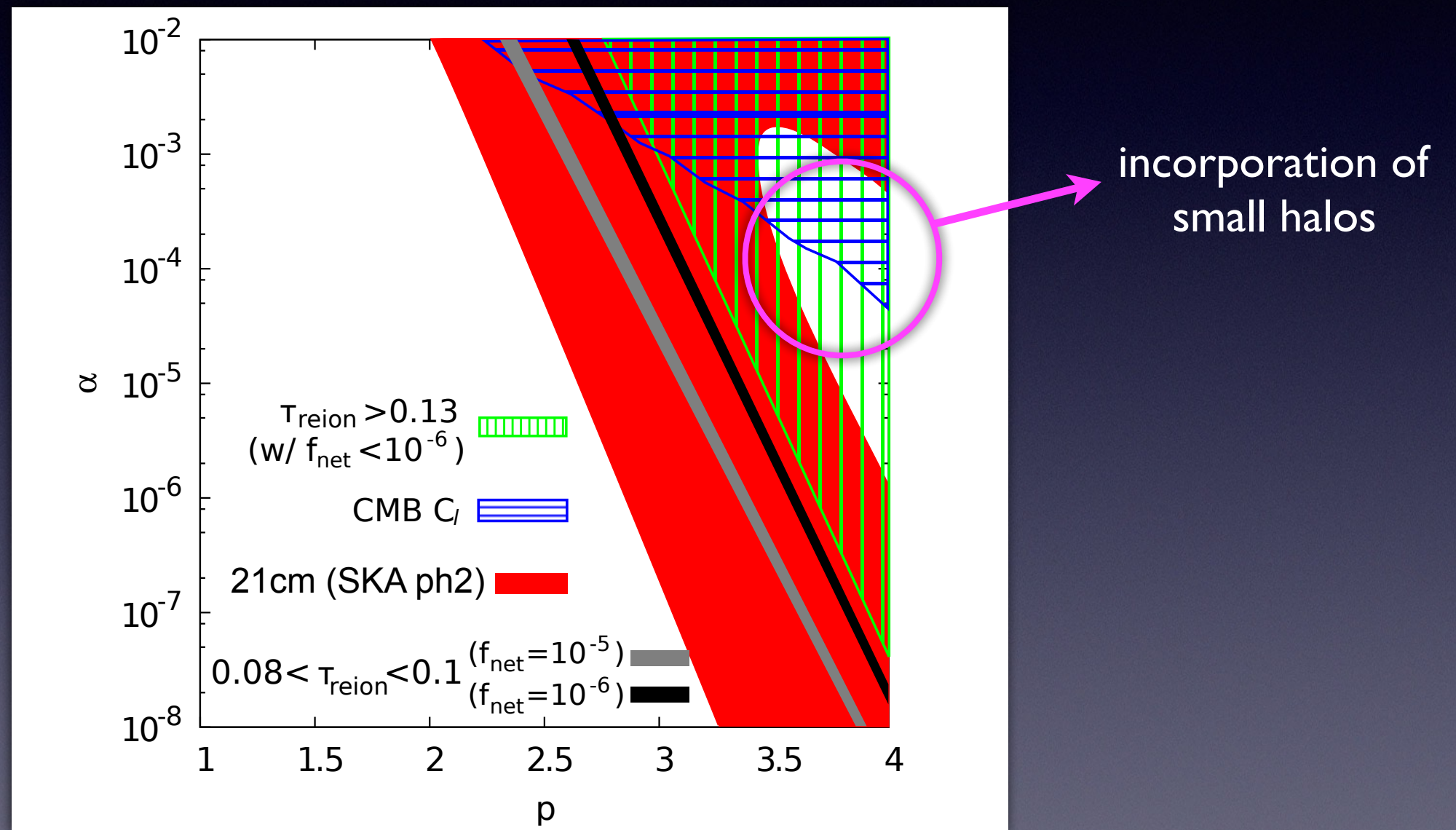
21cm fluctuations from minihalos



Complicated response to α :

- small $\alpha \rightarrow$ increase in mass function
- intermediate $\alpha \rightarrow$ decrease in mass function at $M < 10^8 M_{\text{sun}}$
- large $\alpha \rightarrow$ increase in matter fluctuations at resolved scales ($\sim \text{Mpc}$)

(Forecasted) constraint



21cm line fluctuations & reionization optical depth can complementarily constrain isocurvature perturbations

Warm dark matter

Warm dark matter?

Motivation: small-scale problems

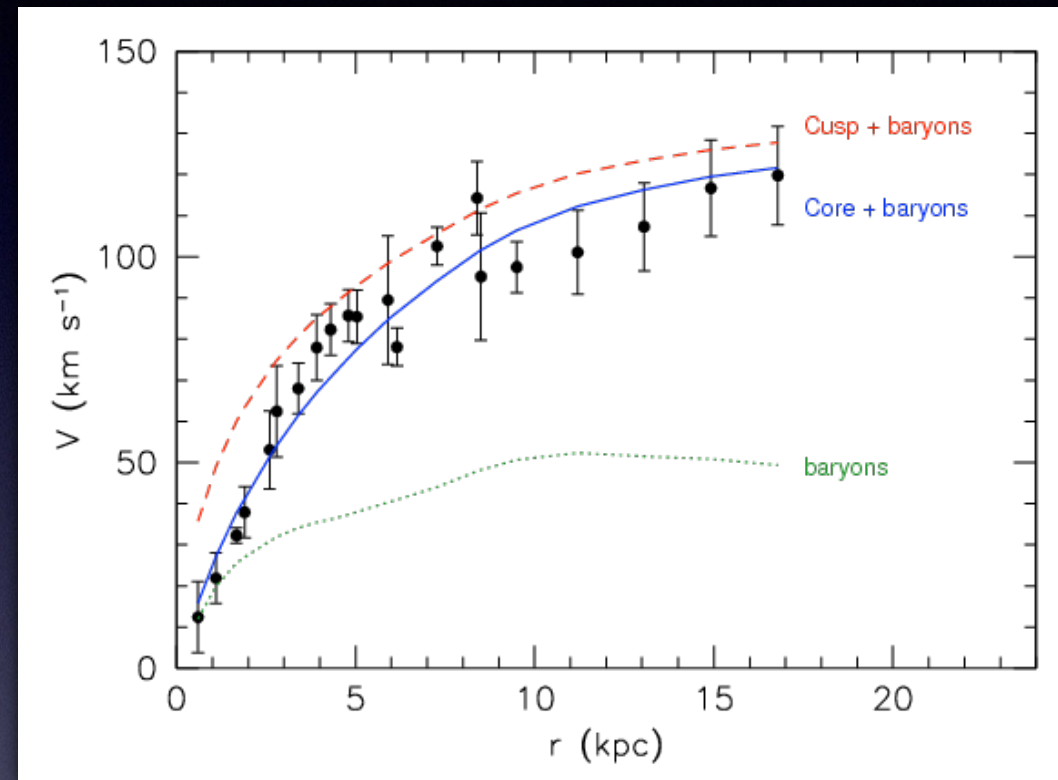
- missing satellites
- cusp-core profile
- ...

Models: thermal/non-thermal relics

ex) sterile neutrino, gravitino, ...

- solution to small scale problems?

$$m_{\text{WDM}} = \mathcal{O}(1)\text{keV}$$



D.H.Weinberg+(2013)

Effects on structure formation

Matter power spectrum

suppressed within free-streaming scale

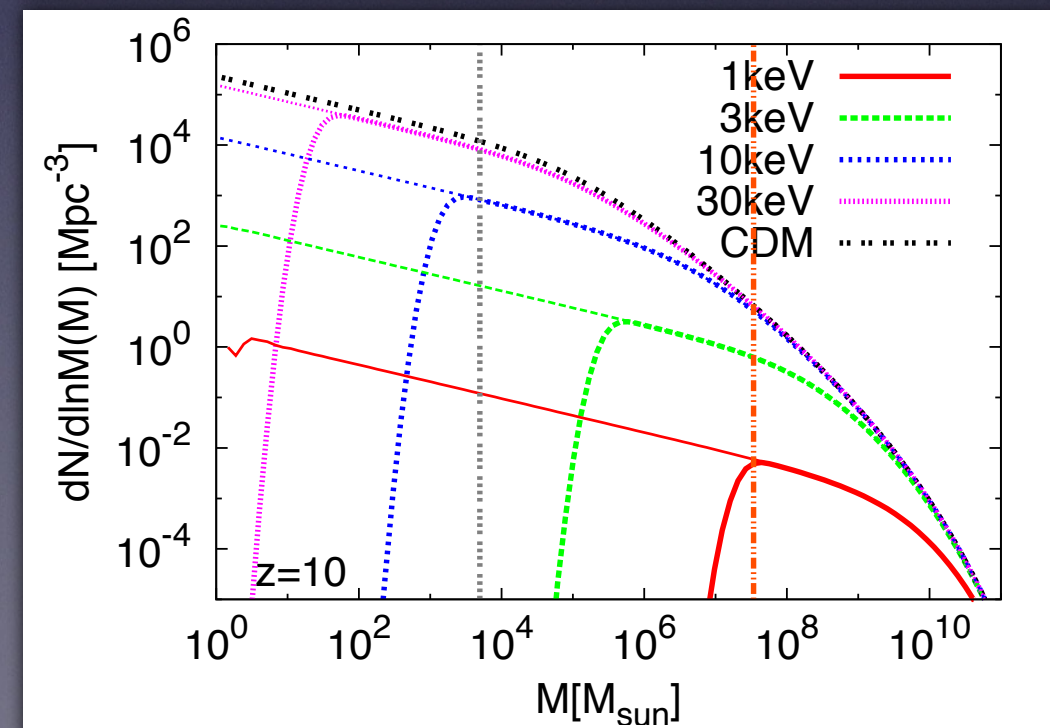
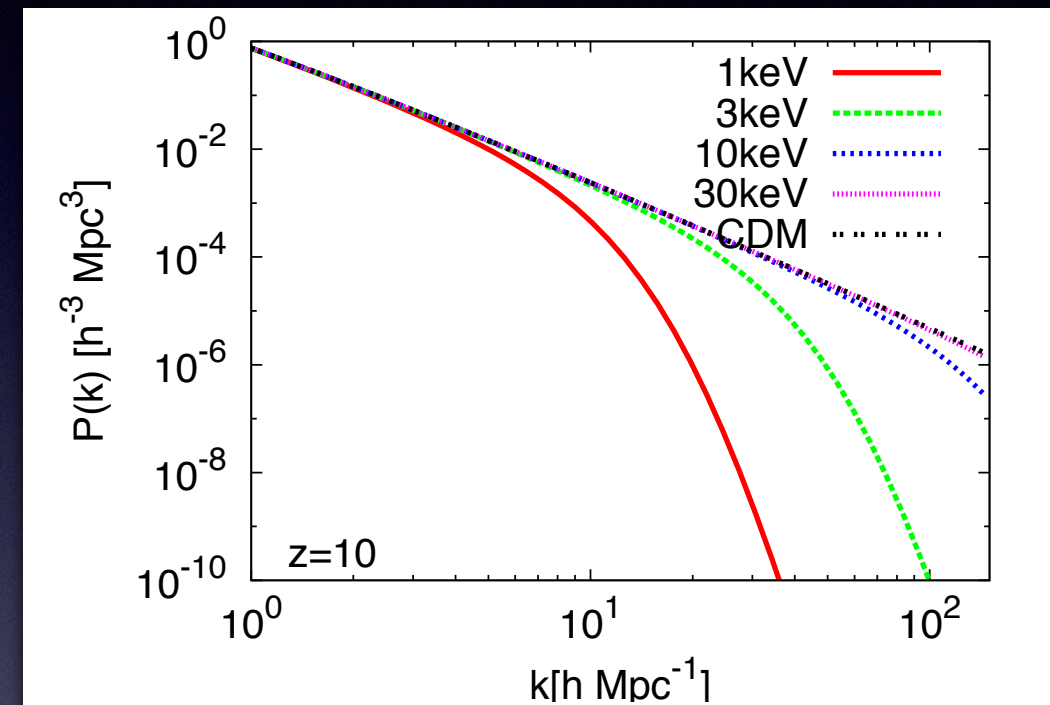
$$\lambda_{\text{FS}} \simeq 0.1 \left(\frac{m_{\text{WDM}}}{1\text{keV}} \right)^{-4/3} \text{Mpc}$$

Mass function

- suppressed formation of small halos
- additional cut-off at $\sim M(\lambda_{\text{FS}})$?

Zavala+(2009), Polisensky & Ricotti (2011)

← break down of hierarchical formation



Current & Future constraint

Lyman-alpha forest

Narayanan+ (2000), Viel+ (2005),
Seljak+ (2006), ...

- recent constraint: $O(1)$ keV

Iršič+ (2013): $m_{\text{WDM}} > 5.3 \text{ keV}$ (2σ)

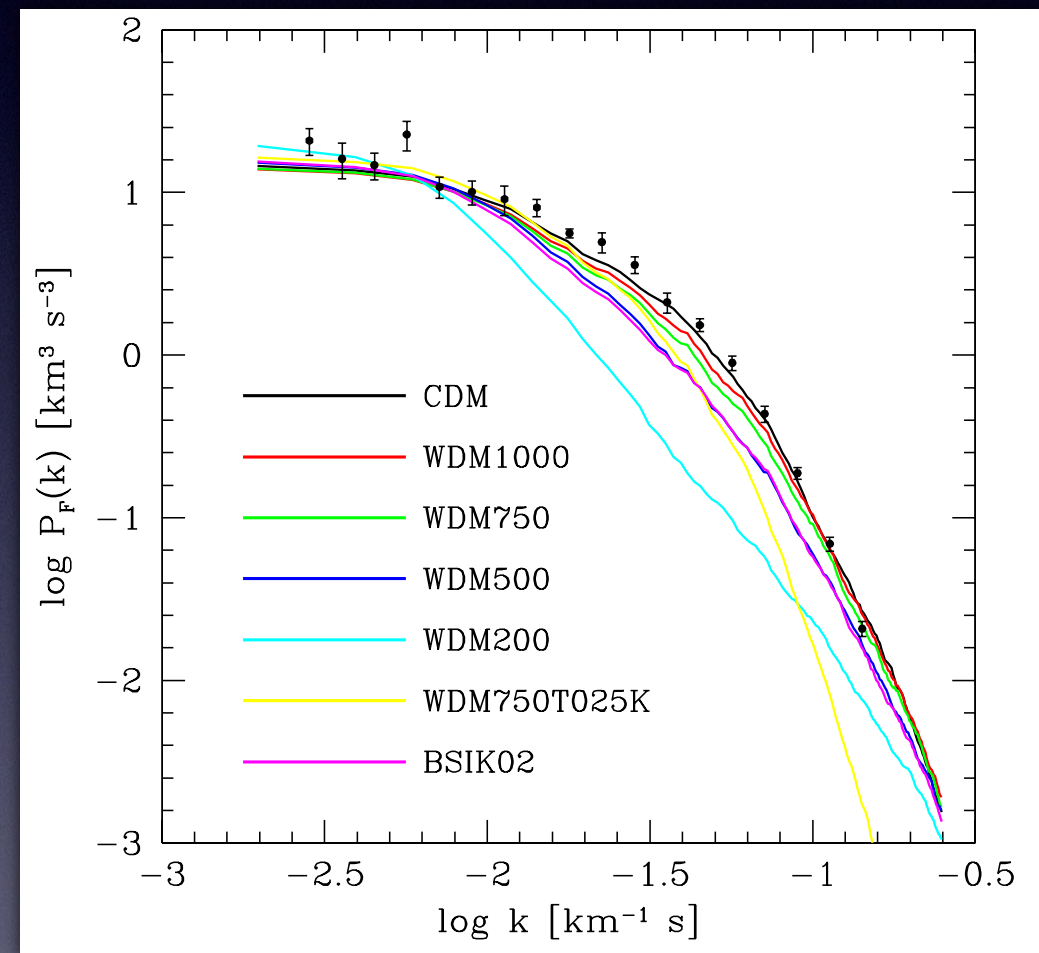
Abundances of GRB

de Souza+ (2013): $m_{\text{WDM}} > 1.6 \text{ keV}$ (2σ)

Weak lensing

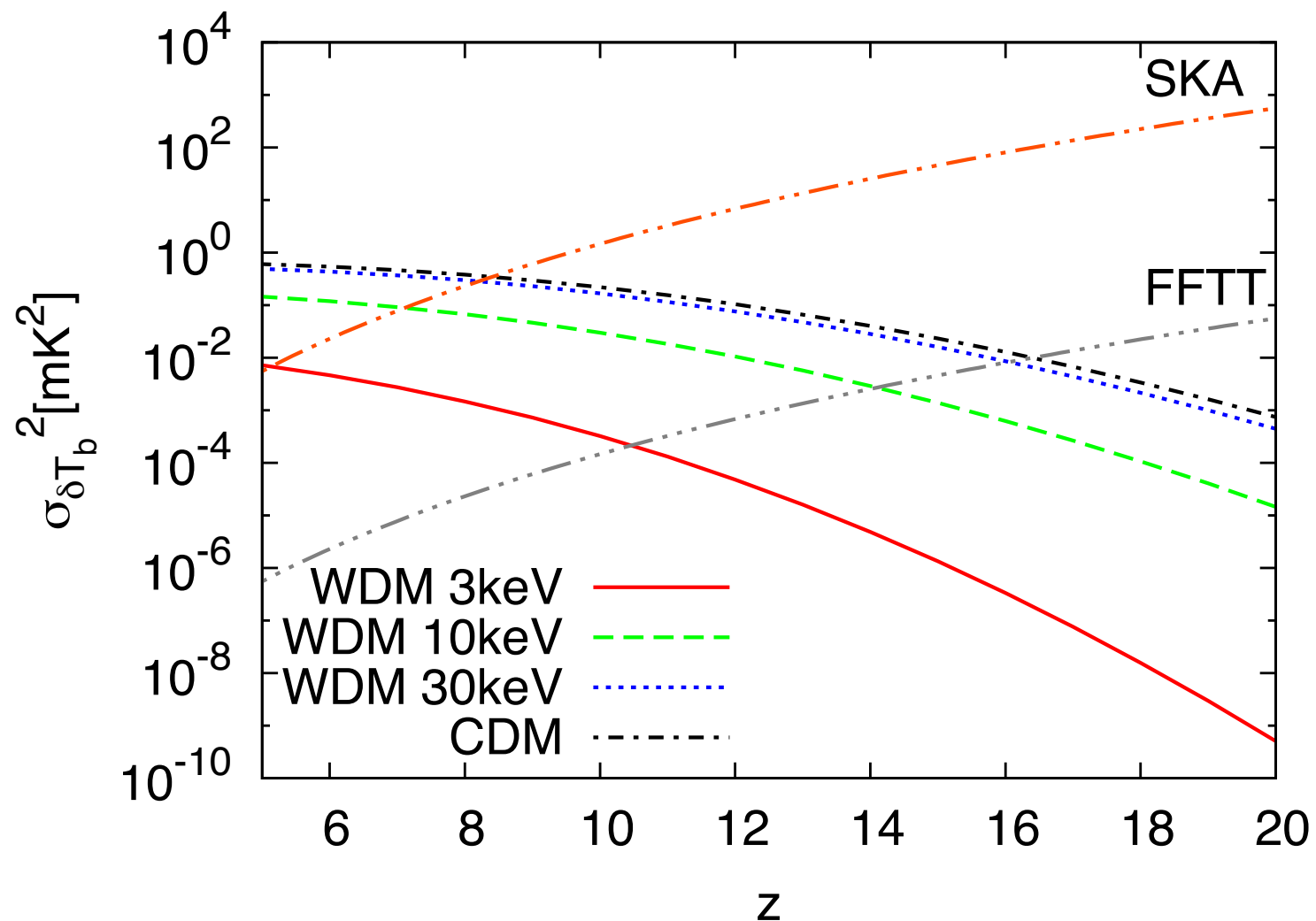
Euclid (forecast): $m_{\text{WDM}} > 2.6 \text{ keV}$ (2σ)

Smith & Markovic (2011)



Narayanan+(2000)

21cm fluctuations



- ▶ As WDM deviates from CDM ($m_{\text{WDM}} \rightarrow 0$), 21cm line fluctuations are suppressed
- ▶ Sensitive to $m_{\text{WDM}} > 10\text{keV}$

Forecast constraint

2 σ lower bounds ($z_{\min}=5$)

- SKA-low

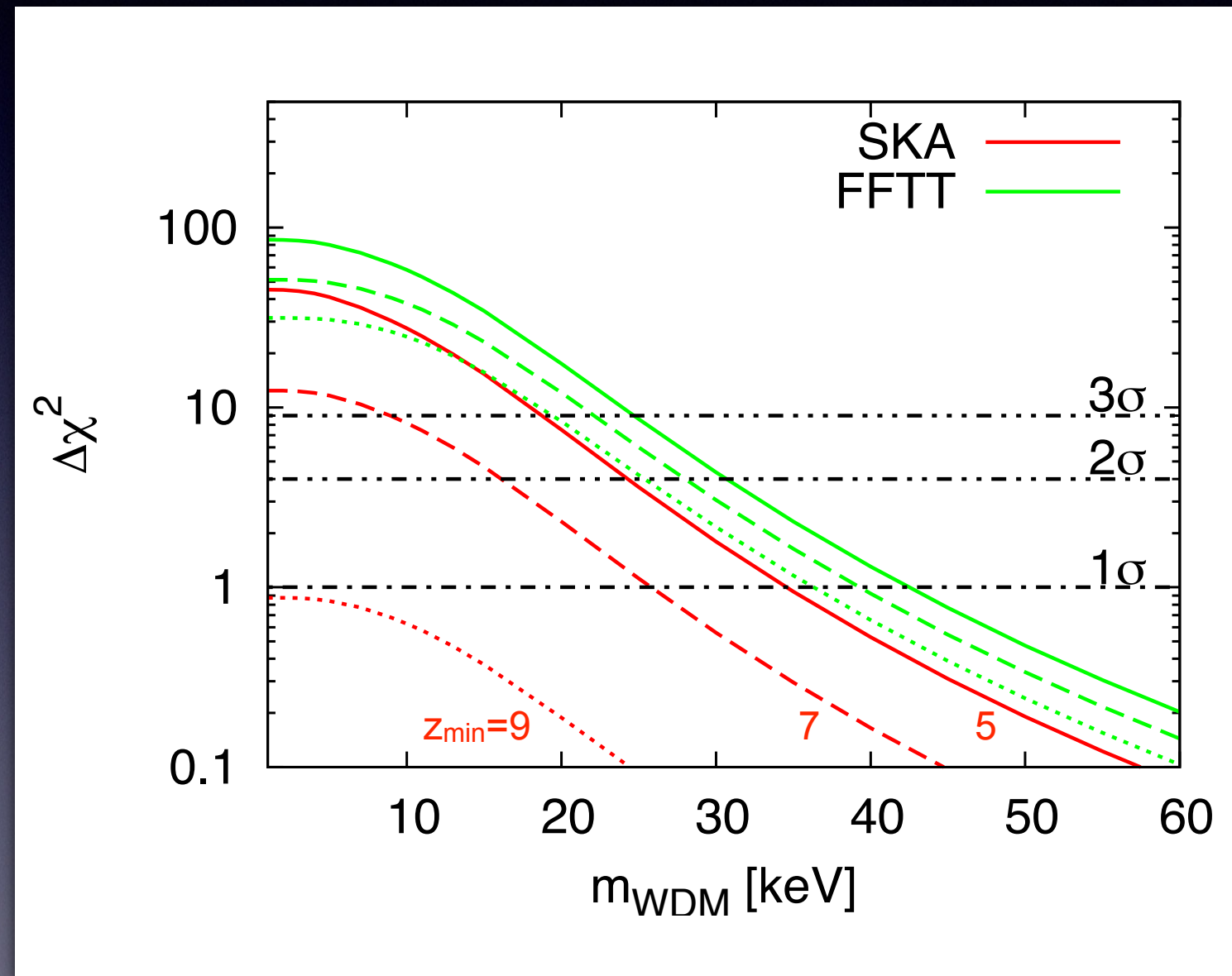
$$m_{\text{WDM}} > 22\text{keV}$$

- FFTT

$$m_{\text{WDM}} > 30\text{keV}$$

cf. current constraint

$m_{\text{WDM}} > 3\text{keV}$ (Ly α forest)



→ WDM of O(10)keV may be probed and precluded from the solution of small-scale crisis

Further suppression effects?

Modification of halo profile

- Formation of small halos delays

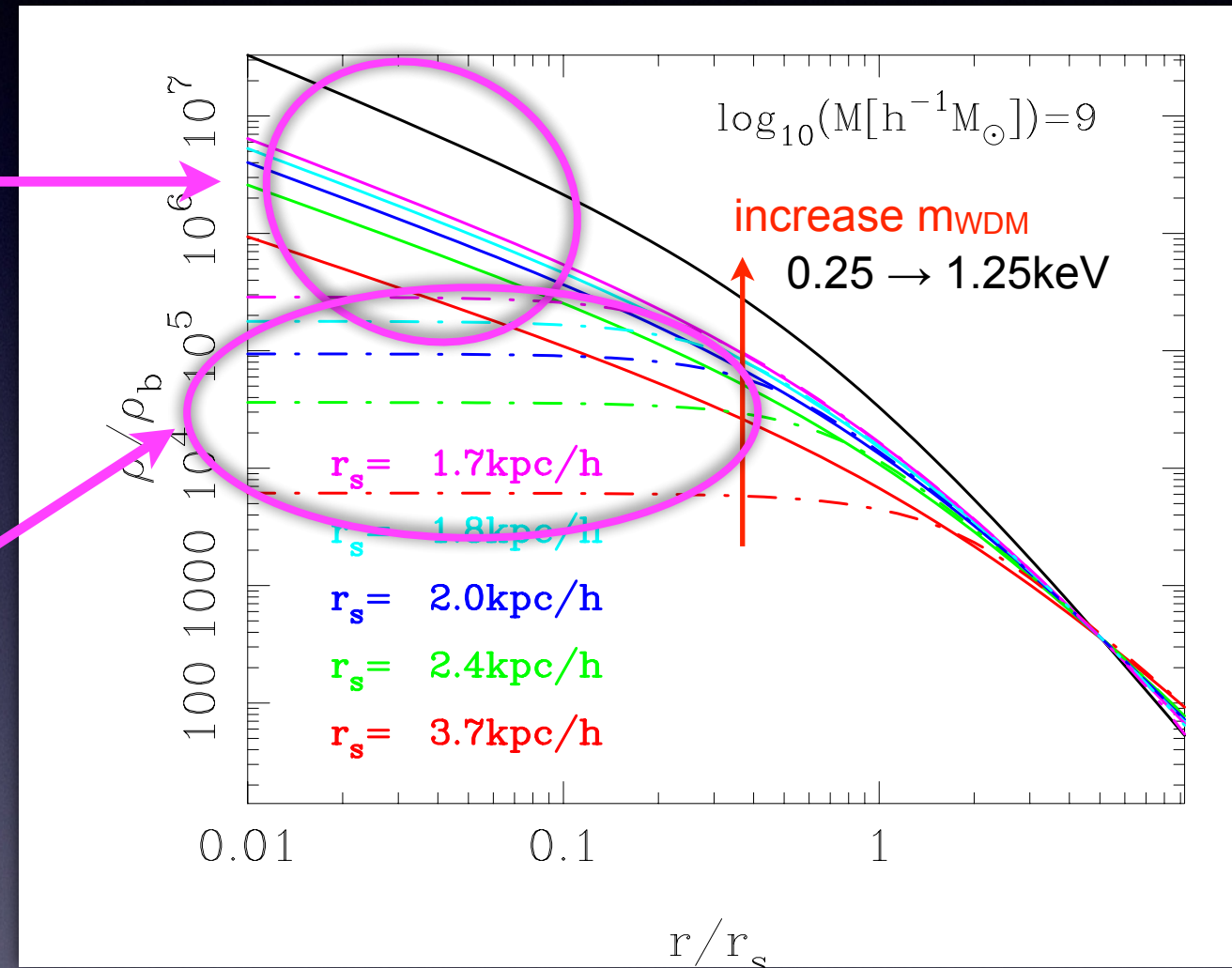
$$\langle 1 + z_{\text{coll}} \rangle(M) = \sigma_M / \delta_c$$

→ less concentration

- Thermal velocity

$$vt \sim 0.5(1+z)^{-1/2} \left(\frac{m_{\text{WDM}}}{1\text{keV}} \right)^{-4/3} \text{kpc}$$

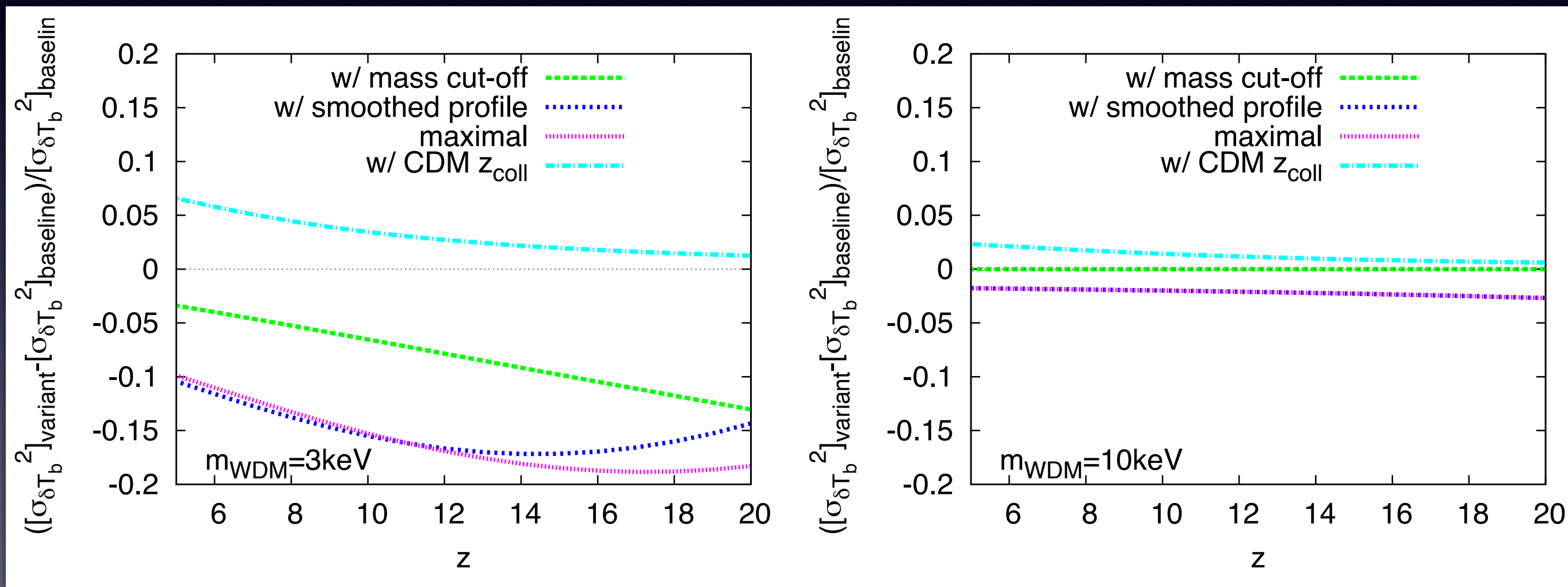
→ cored profile



Smith & Markovic (2011)

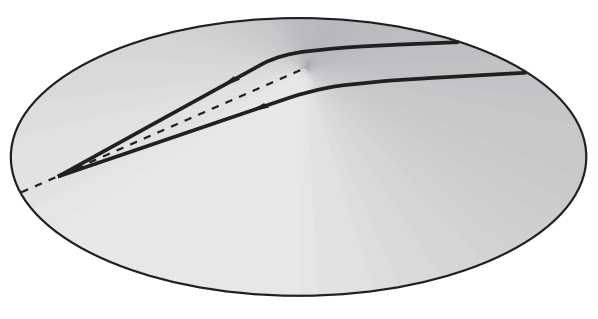
Further suppression effects? (cont'd)

Relative difference from the baseline case



Additional effects unique to WDM are important only for $m_{\text{WDM}} < \text{a few keV}$ and negligible for $m_{\text{WDM}} > 10 \text{ keV}$

String wakes



(c) Vilenkin & Shellard

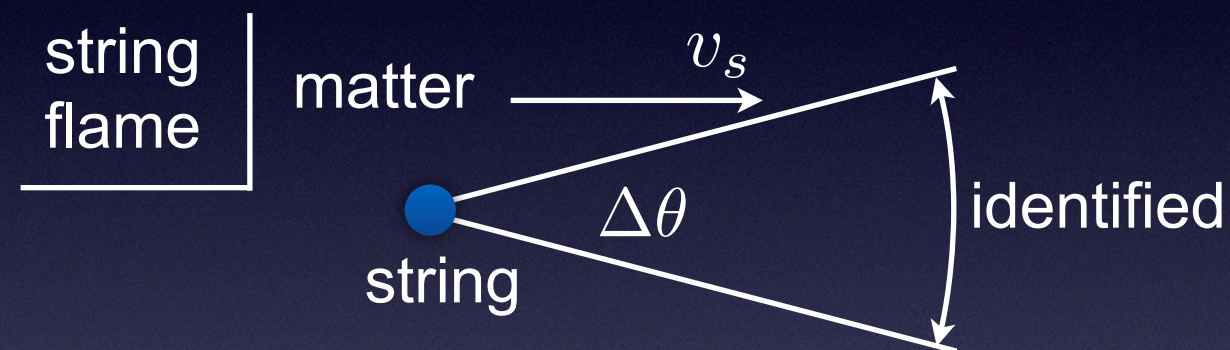
String wakes: overview

- Conical spacetime around a string

- deficit angle: $\Delta\theta = 8\pi G\mu$
 μ : string tension

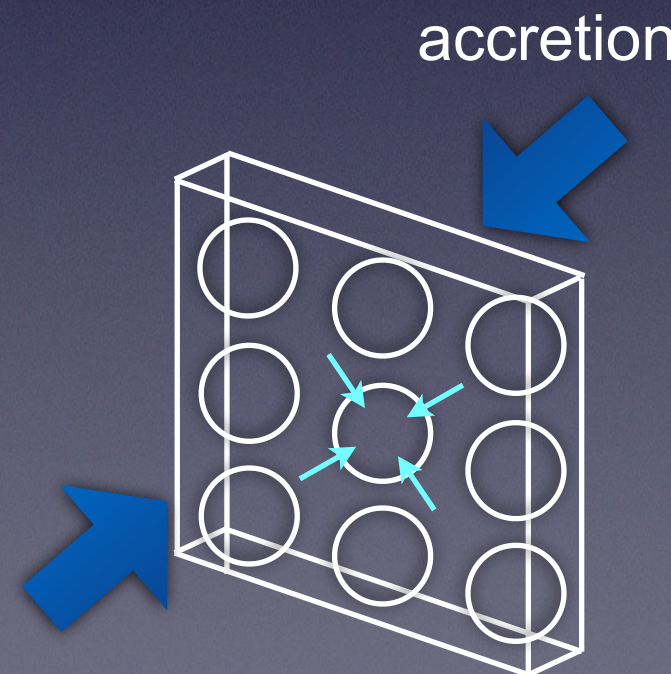
→ **Matter gets velocity kick**

$$v_{\text{kick}} = 4\pi G\mu v_s \gamma_s$$



- Formation of string wakes and minihalos

- Matter accretes around trace of strings
 → sheet-like structure=*wake*
- Shock front on wake surface → thermalization
- Instability of planar structure
 → fragmentation into minihalos (size ~ wake thickness)



Formation wakes

based on Duplessis & Brandenberger (2013)

- Zel'dovich approximation (in MD)

physical distance from wake $r_{\text{phys}}(x_{\text{ini}}, t) = a(t)(x_{\text{ini}} + \psi(x_{\text{ini}}, t))$

$$\frac{d^2\psi}{dt^2} + \frac{3}{4t} \frac{d\psi}{dt} - \frac{2}{3t^2} \psi = 0 \quad \rightarrow \quad \psi \simeq -\frac{5}{3} v_{\text{kick}} t_{\text{ini}} \left(\frac{t}{t_{\text{ini}}} \right)^{3/2}$$

- Decoupling from global expansion $\rightarrow$ virialization

physical wake size $\sim 1/2$ turn around scale ($\dot{r}_{\text{phys}} = 0$)

$$w(t) = \frac{5}{3} v_{\text{kick}} t_{\text{ini}} \left(\frac{t}{t_{\text{ini}}} \right)^{4/3} \propto a(t)^2$$

Baryon is thermalized at shock on wake surface

$$\frac{3}{2} k_B T = \frac{m_p}{2} v_{\text{surface}}^2 \rightarrow T = 10 \text{ K} \left(\frac{G\mu}{10^{-6}} \right)^2 (v_s \gamma_s)^2 \frac{z_{\text{ini}} + 1}{z + 1}$$

Formation of minihalos

based on Duplessis & Brandenberger (2013)

- Wake volume in horizon

fractional volume of wakes generated in Δt_i at t_i

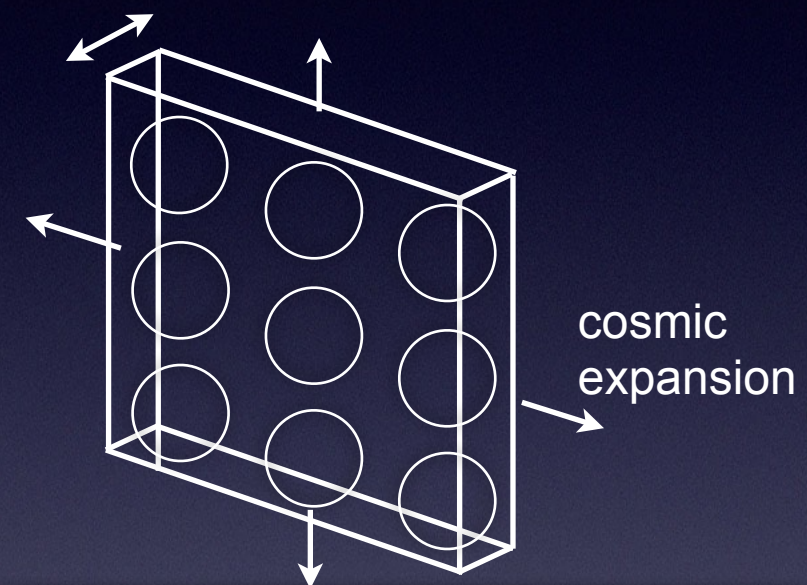
$$\Delta f_i(t) = \frac{\gamma t_i \times v_s \gamma_s \Delta t_i \times w_i(t) a(t)^2 / a_i^2}{t_i^3 a(t)^3 / a_i^3}$$

scaling solution: # of strings in horizon

$$= \gamma \sim \mathcal{O}(1)$$

width $\sim$ minihalo size

$$w \propto a^2$$



- Fragmentation into minihalo

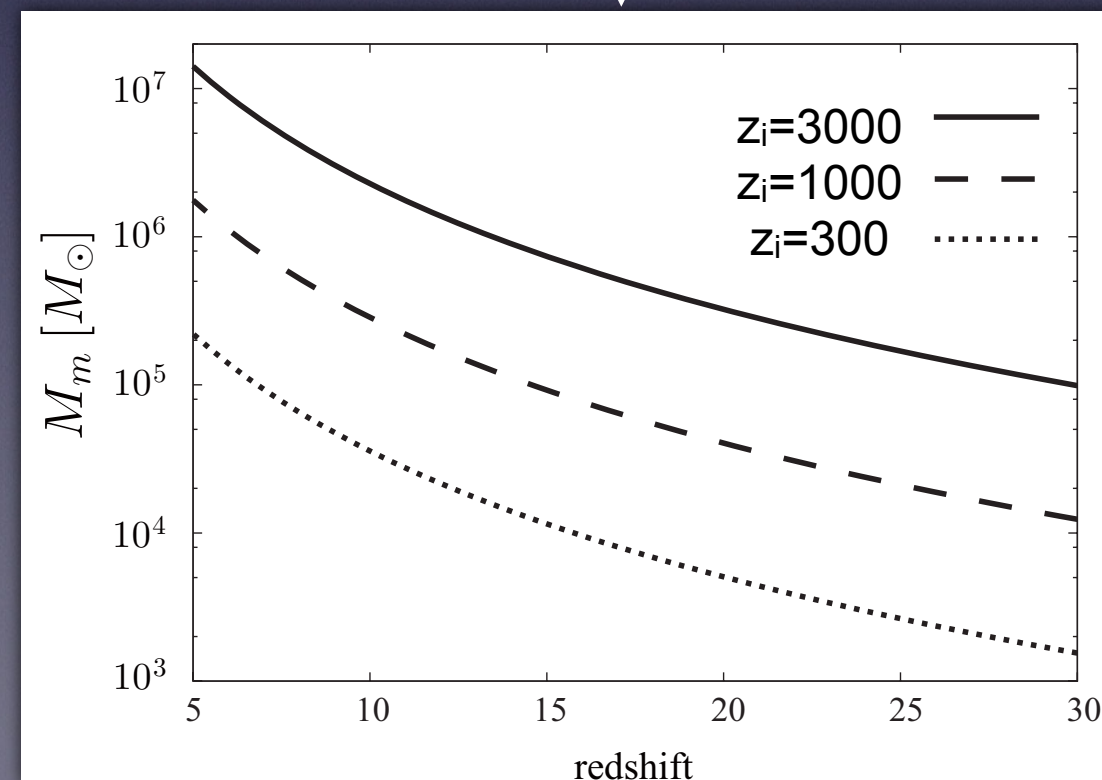
time scale $\sim w_i(t)$ (Zel'dovich pancakes)

$$\rightarrow V_i(t) = \frac{4\pi}{3} w_i(t)^3$$

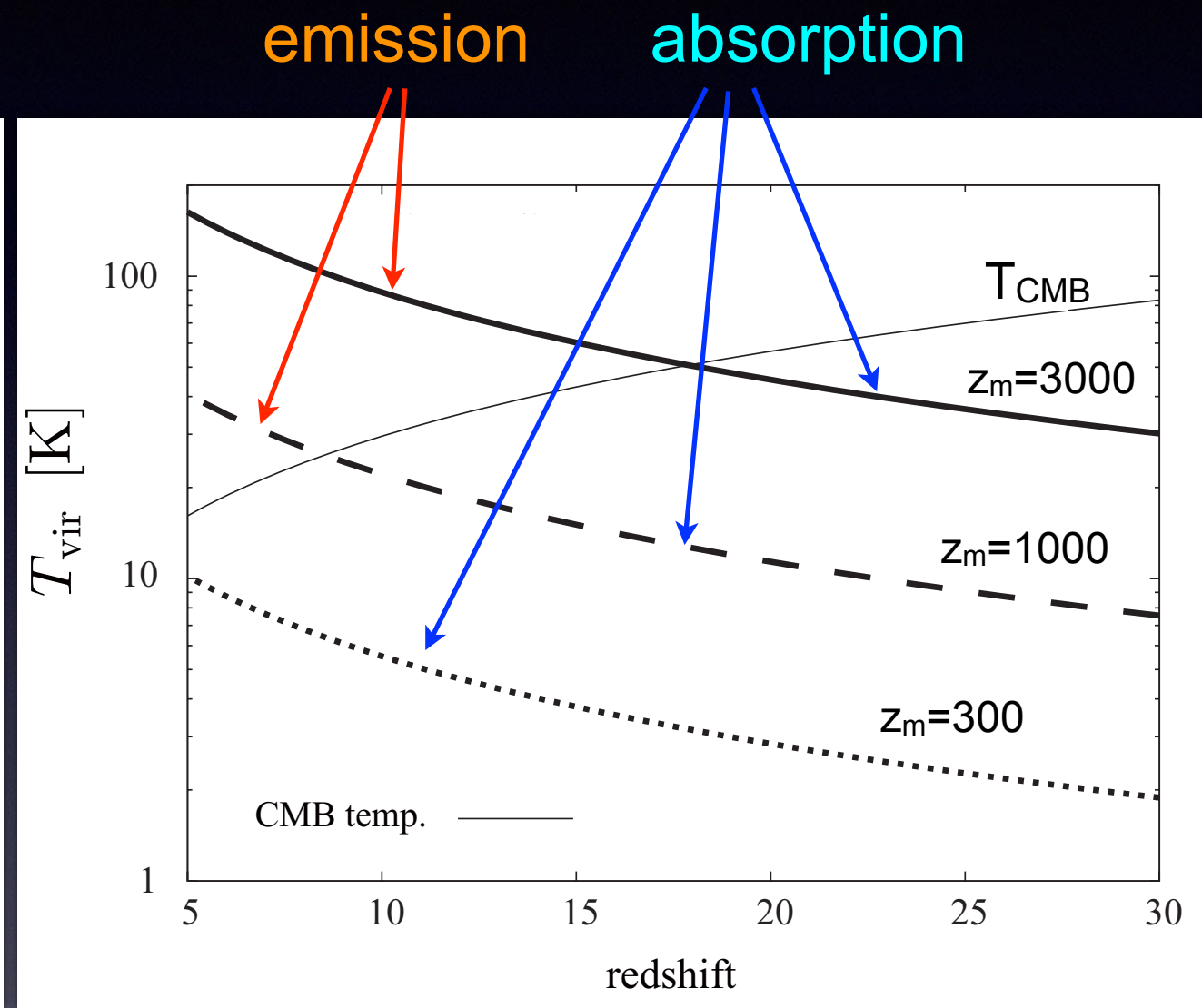
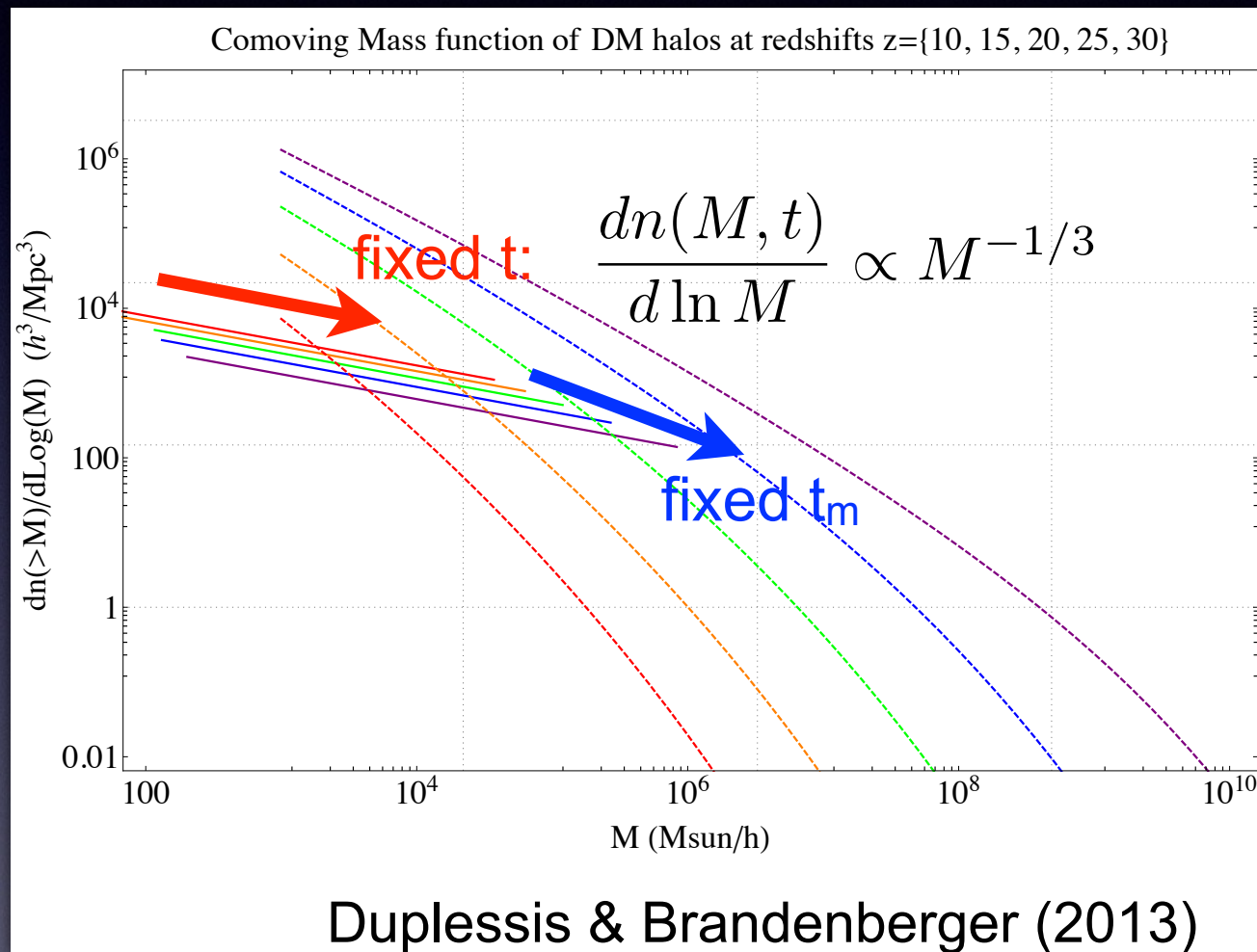
$$M_i(t) = 4\bar{\rho}(t) V_i(t)$$

- Mass function

$$\frac{dn(M, t)}{dM} = \frac{a(t)^3}{V_i(t)} \frac{df_i(t)/dt_i}{dM_i(t)/dt_i}$$



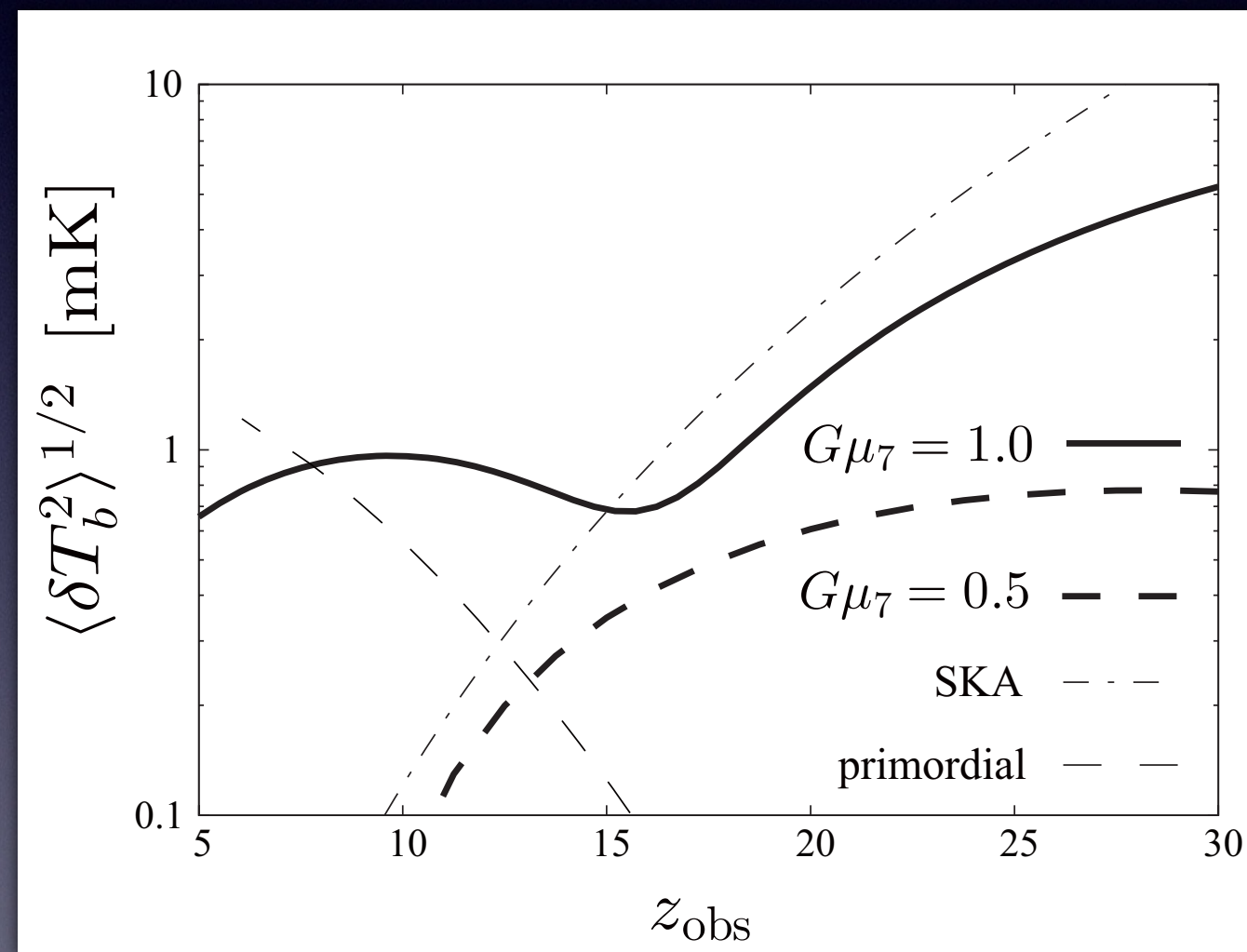
mass function & gas temperature



- Mass of minihalos increases: absorption $\rightarrow$ emission in 21cm line
- Atomic cooling is ineffective
 $\rightarrow$ can be observed by 21cm line fluctuations

21cm fluctuations

- string distributions
→ 21cm line fluctuations
- Upper bound on string tension
SKA: $G\mu < 4 \times 10^{-8}$ (2sigma)



➡ Strings with $G\mu=10^{-7}$ (Planck upper bound) can be observed with SKA