



**Focus Workshop on Particle Physics and Cosmology**  
**IBS-CTPU, Dec. 2016**

# **TESTING NATURALNESS**

**Tao Liu**

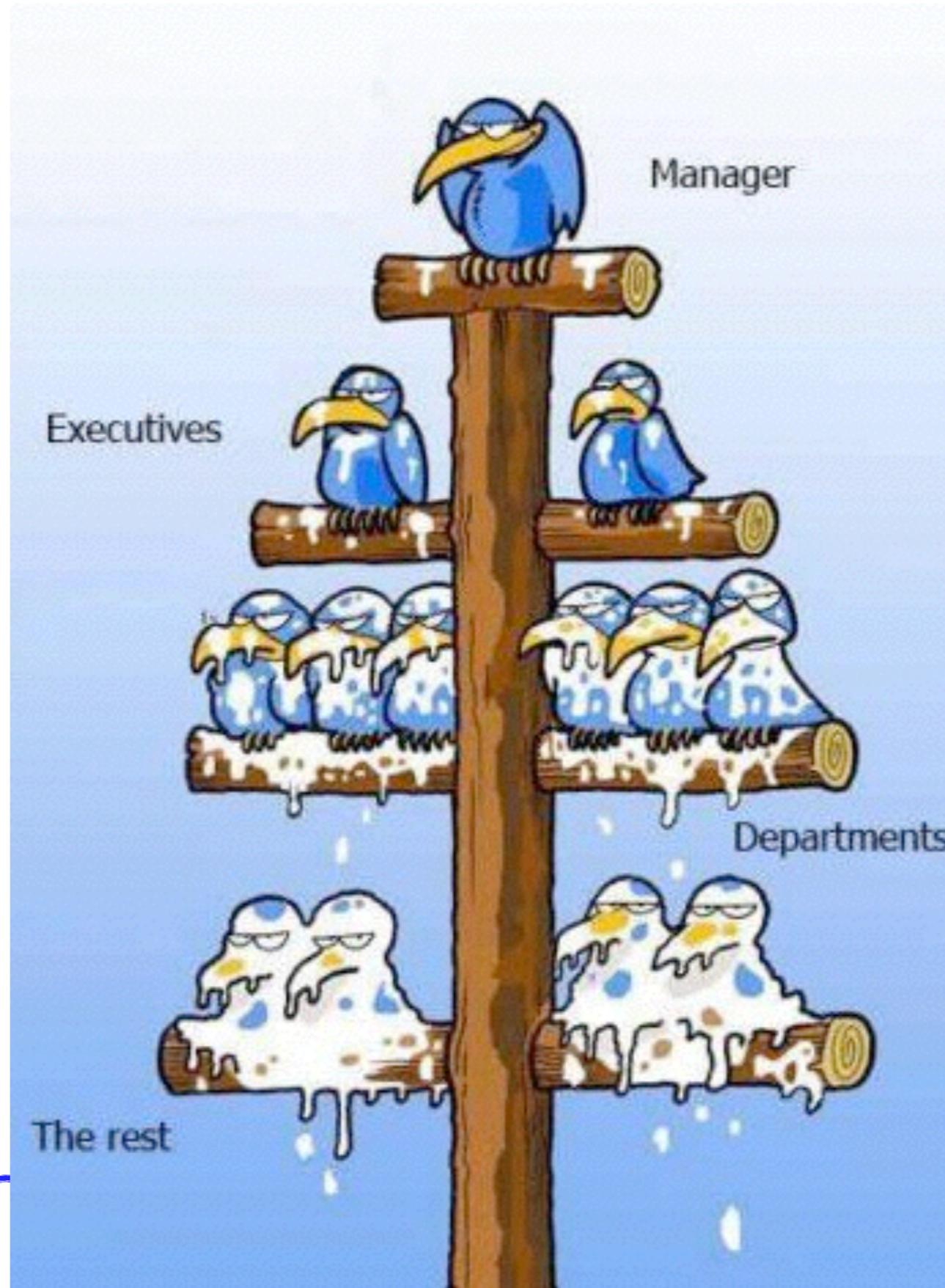
**The Hong Kong University of Science and Technology**

[C. Chen, J. Hajer, TL, I. Low and H. Zhang, arXiv: 1612.0xxxx]

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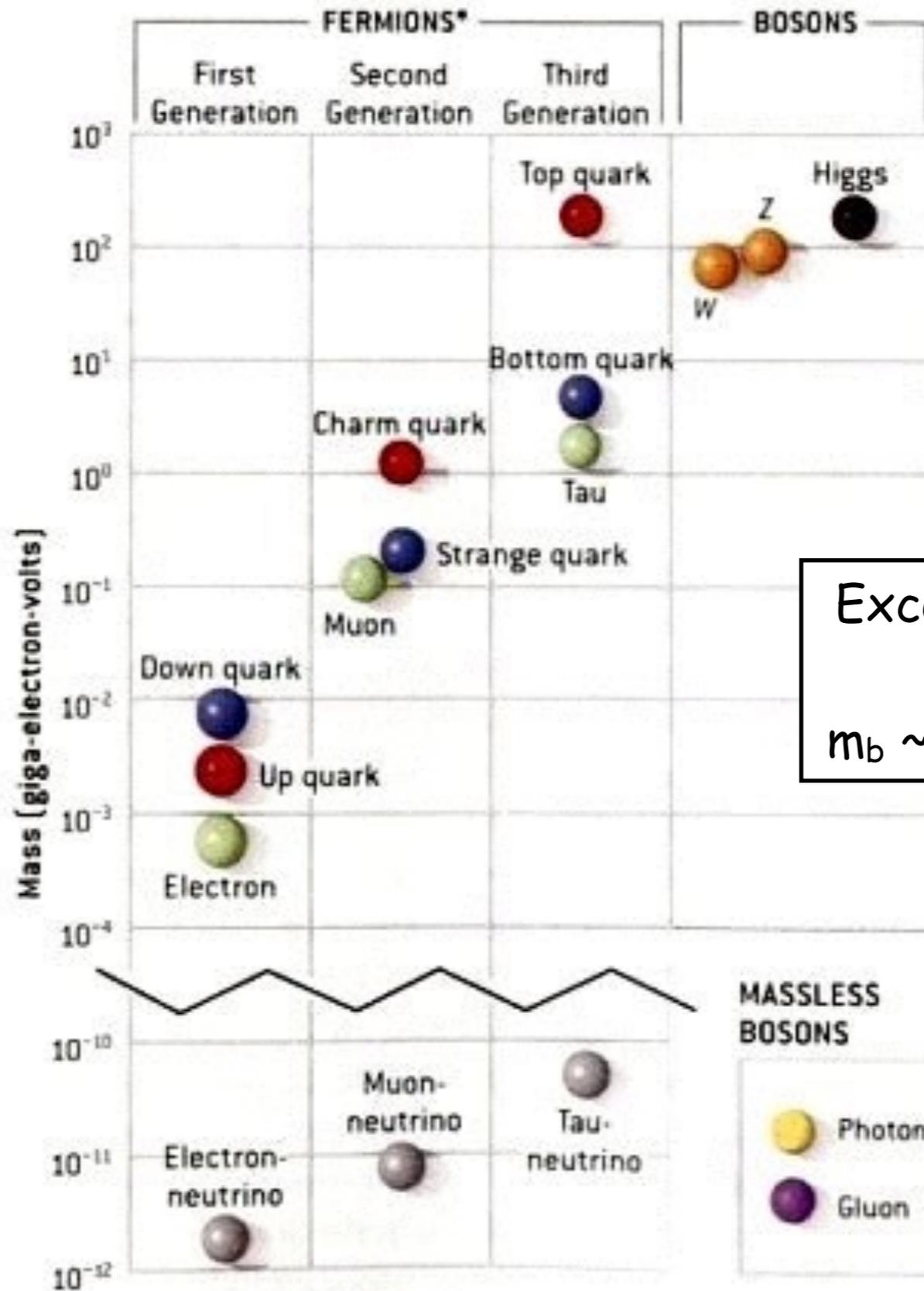


# Naturalness Problem





# Naturalness Problem



Except  $M_W, M_Z, M_H, m_t \sim g v$ , all others are unnaturally light:  
 $m_b \sim 5 \text{ GeV}, m_e \sim 0.5 \text{ MeV}, m_\nu < 0.2 \text{ eV} \dots$



## Naturalness Problem

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But, these particles share a nice property: chiral symmetry is restored, in the zero mass limit. The quantum corrections are merely logarithmically divergent

$$m_e \sim m_e^0 [1 + 3\alpha/4\pi \ln(\Lambda/m_e)]$$

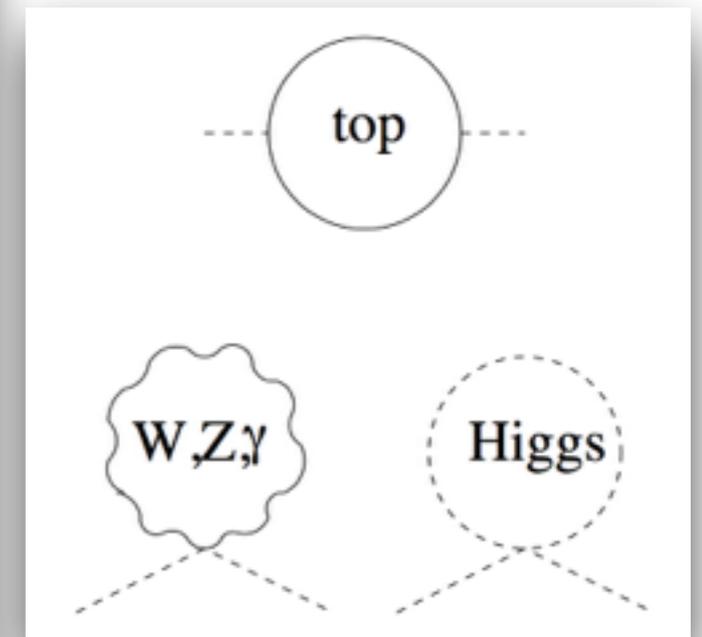
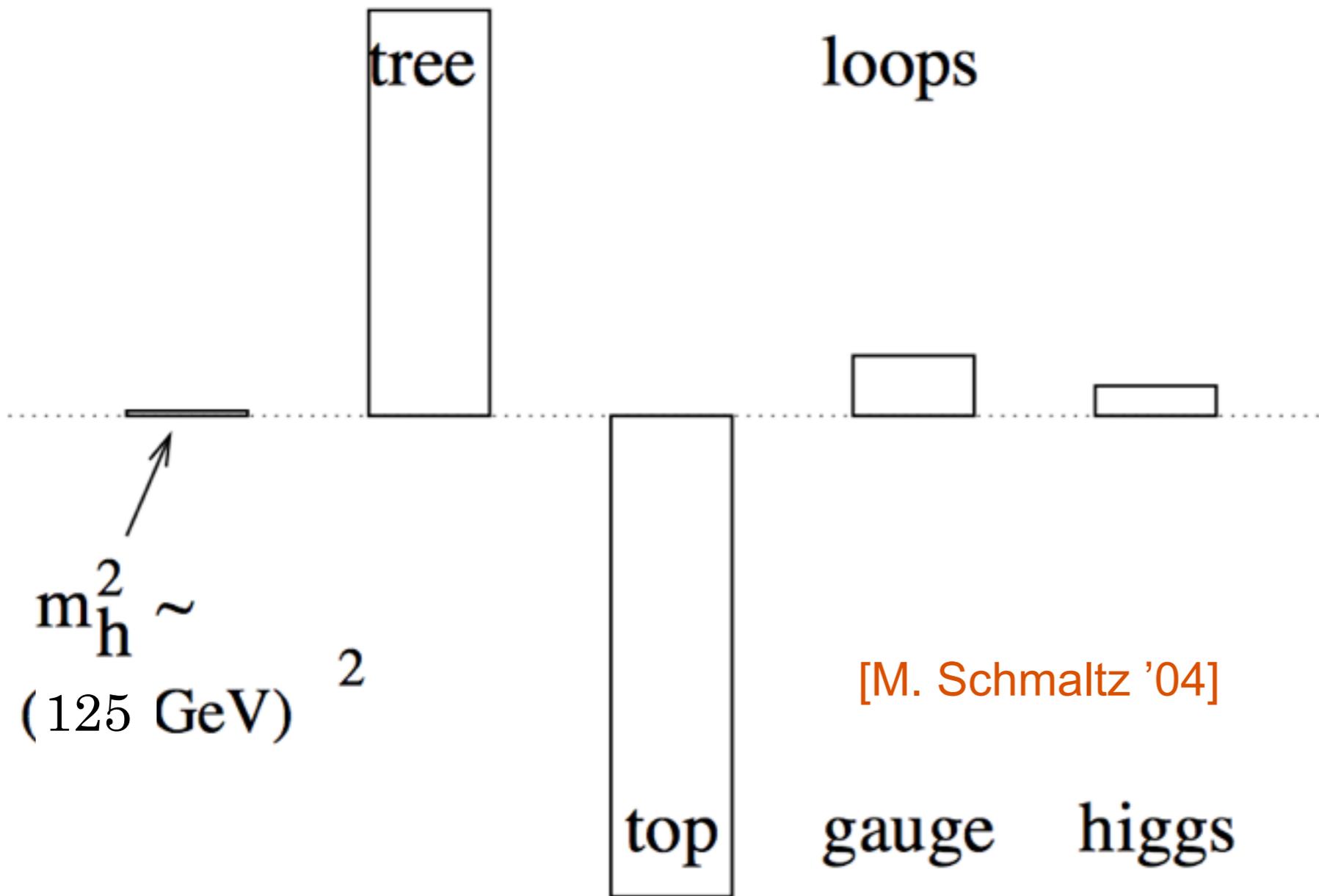
t'Hooft statement for "technical naturalness": **If a parameter is turned off (set to 0), the system results in an enlarged symmetry, then this parameter must be technically natural.**

=> The smallness of fermion (except top) mass is technically natural

**However, not all particle masses are technically natural in the SM**



# Naturalness Problem





## A Large Bulk of Ideas of Naturalness

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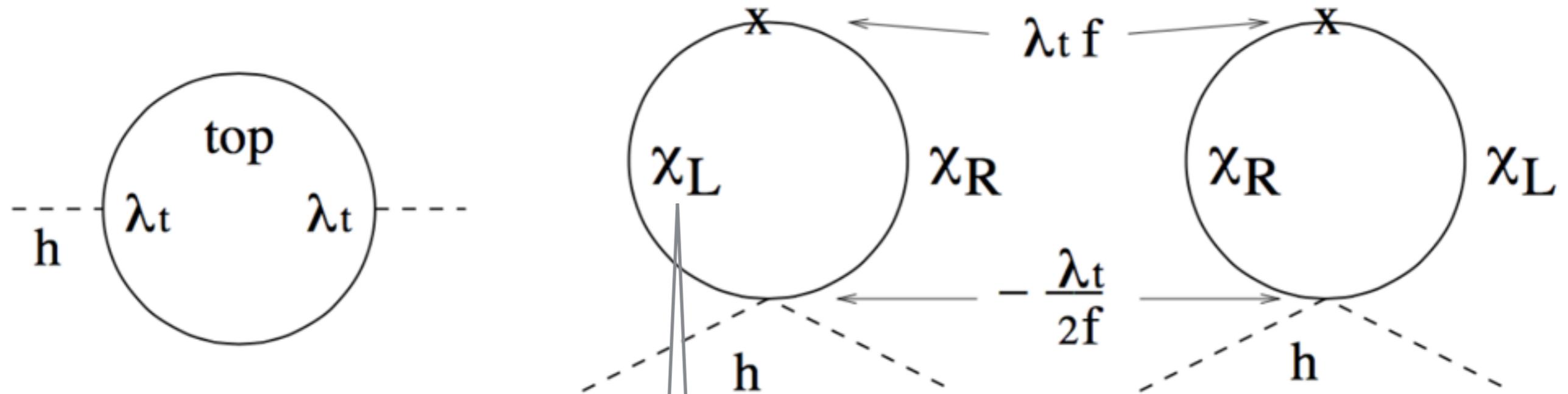
Introduce partners to the SM fields which couple with the Higgs boson. These couplings contribute to the squared Higgs mass, yielding a cancellation of quadratic divergence ensured by the underlying symmetries which are broken softly or collectively.

- ☒ supersymmetric models
- ☒ Composite Higgs models/ little Higgs models
- ☒ Twin Higgs models
- ☒ ... ..

To test these ideas, we need to ensure that the newly found partner-like particle is not an impostor, but a particle with the right properties to cancel the quadratic divergence.



# Focus - Fermionic Top Partners



Vector-like fermions  
are requested



## Simplified Model

SM + one pair of vector-like top partners

$$\mathcal{L}_U = u_3^c \left( c_0 f U + c_1 H q_3 + \frac{c_2}{f} H^2 U + \dots \right) \\ + U^c \left( \hat{c}_0 f U + \hat{c}_1 H q_3 + \frac{\hat{c}_2}{f} H^2 U + \dots \right) + \text{h.c. .}$$

Model		$c_0$	$c_1$	$c_2$	$\hat{c}_0$	$\hat{c}_1$	$\hat{c}_2$
$\left(\frac{\text{SU}(3)}{\text{SU}(2)}\right)^2$ simplest Higgs	[11]	$\lambda$	$-\lambda$	$-\lambda$	$\lambda$	$\lambda$	$-\lambda$
$\frac{\text{SU}(5)}{\text{SO}(5)}$ littlest Higgs	[7]	$\lambda_1$	$-\sqrt{2}i\lambda_1$	$-2\lambda_1$	$\lambda_2$	0	0
T-parity invariant $\frac{\text{SU}(3)}{\text{SU}(2)}$	[8]	$\lambda$	$-\lambda$	$-\lambda$	$-\lambda$	$-\lambda$	$\lambda$



## Simplified Model - Mass Basis Before EWSB

$$\begin{aligned} t'^c &= \frac{\hat{c}_0 u_3^c - c_0 U^c}{c} & t' &= q_3 \\ T'^c &= \frac{\hat{c}_0 U^c + c_0 u_3^c}{c} & T' &= U \end{aligned}$$

$$\begin{aligned} \mathcal{L}_{T'} &= m_{T'} T'^c T' + \lambda_{t'} H t'^c t' + \lambda_{T'} H T'^c t' + \frac{\alpha_{t'}}{2m_{T'}} H^2 t'^c T' + \frac{\alpha_{T'}}{2m_{T'}} H^2 T'^c T' \\ &\quad + \frac{\beta_{t'}}{6m_{T'}^2} H^3 t'^c t' + \frac{\beta_{T'}}{6m_{T'}^2} H^3 T'^c t' + \mathcal{O}(H^4) + \text{h.c.} \end{aligned}$$

$$m_{T'} = f c ,$$

$$c = \sqrt{c_0^2 + \hat{c}_0^2}$$

$$\lambda_{t'} = \frac{\hat{c}_0 c_1 - c_0 \hat{c}_1}{c} ,$$

$$\lambda_{T'} = \frac{c_0 c_1 + \hat{c}_0 \hat{c}_1}{c} ,$$

$$\alpha_{t'} = \hat{c}_0 c_2 - c_0 \hat{c}_2 ,$$

$$\alpha_{T'} = c_0 c_2 + \hat{c}_0 \hat{c}_2 ,$$

$$\beta_{t'} = (\hat{c}_0 c_3 - c_0 \hat{c}_3) c ,$$

$$\beta_{T'} = (c_0 c_3 + \hat{c}_0 \hat{c}_3) c$$



## Naturalness Condition - Mass Basis Before EWSB

The contribution of the top sector to the Higgs potential can be calculated using C-W potential, with the quadratically divergent contribution given by

$$\frac{1}{16\pi^2} \Lambda^2 \text{tr } \mathcal{M}(H)^\dagger \mathcal{M}(H)$$

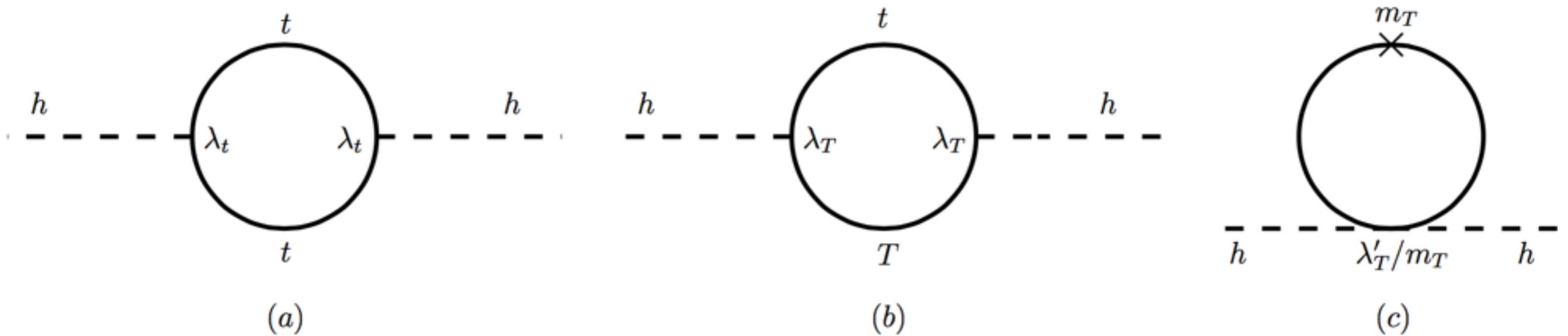
$$\mathcal{M}(H) = \begin{pmatrix} 0 & 0 \\ 0 & m_{T'} \end{pmatrix} + \begin{pmatrix} \lambda_{t'} & 0 \\ \lambda_{T'} & 0 \end{pmatrix} H + \begin{pmatrix} 0 & \alpha_{t'} \\ 0 & \alpha_{T'} \end{pmatrix} \frac{H^2}{2m_{T'}} + \mathcal{O}(H^3)$$

The requirement for the coefficient of  $H^2$  to vanish =>

$$\alpha_{T'} = -|\lambda_{T'}|^2 - |\lambda_{t'}|^2$$



## Naturalness Condition - Familiar to Us?



$$\alpha_{T'} = -|\lambda_{T'}|^2 - |\lambda_{t'}|^2$$



## Naturalness Condition - General Efforts

### Top quarks and electroweak symmetry breaking in little Higgs models

Maxim Perelstein, Michael E. Peskin, and Aaron Pierce  
Phys. Rev. D **69**, 075002 – Published 8 April 2004

$$\alpha_{T'} = -|\lambda_{T'}|^2 - |\lambda_{t'}|^2$$

☒ Convert the measurement of  $\alpha_{T'}$  as the measurements of  $\lambda_{T'}$  and  $f$

$$\alpha_{T'} = \lambda_{T'} \frac{m_T}{f}$$

☒ Measure the total decay width  $\Rightarrow \lambda_{T'}$   $\Gamma_T = \frac{m_T \lambda_{T'}^2}{16\pi}$

☒ Measure the vector boson sector  $\Rightarrow f$   $M_{Z_H} = \sqrt{\frac{g_L^2 + g_R^2}{2}} f = \frac{\sqrt{2}g}{\sin 2\psi} f.$



## Simplified Model - Mass Basis After EWSB

$$t^c = t'^c + \mathcal{O}\left(\frac{v^2}{m_{T'}^2}\right), \quad t = t' - T' \frac{v}{m_{T'}} \lambda_{T'}^* + \mathcal{O}\left(\frac{v^2}{m_{T'}^2}\right)$$
$$T^c = T'^c + \mathcal{O}\left(\frac{v^2}{m_{T'}^2}\right), \quad T = T' + t' \frac{v}{m_{T'}} \lambda_{T'} + \mathcal{O}\left(\frac{v^2}{m_{T'}^2}\right)$$

$$\mathcal{L}_T = m_T T^c T + \lambda_t v t^c t + \frac{\lambda_t}{\sqrt{2}} h t^c t + \frac{\lambda_T}{\sqrt{2}} h T^c t + \frac{a_t v}{\sqrt{2} m_T} h t^c T + \frac{a_T v}{\sqrt{2} m_T} h T^c T$$
$$+ \frac{\alpha_t}{4 m_T} h^2 t^c T + \frac{\alpha_T}{4 m_T} h^2 T^c T + \frac{b_t v}{4 m_T^2} h^2 t^c t + \frac{b_T v}{4 m_T^2} h^2 T^c t + \mathcal{O}\left(h^3, \frac{v^2}{m_T^2}\right) + \text{h.c.}$$

$$a_t = \alpha_{t'} + \lambda_{T'}^* \lambda_{t'},$$

$$b_t = \beta_{t'} - \alpha_{t'} \lambda_{T'},$$

$$a_T = \alpha_{T'} + |\lambda_{T'}|^2$$

$$b_T = \beta_{T'} - \alpha_{T'} \lambda_{T'}$$



## Naturalness Condition - Mass Basis After EWSB

$$a_T = -|\lambda_t|^2 + \mathcal{O}\left(\frac{v^2}{m_T^2}\right)$$

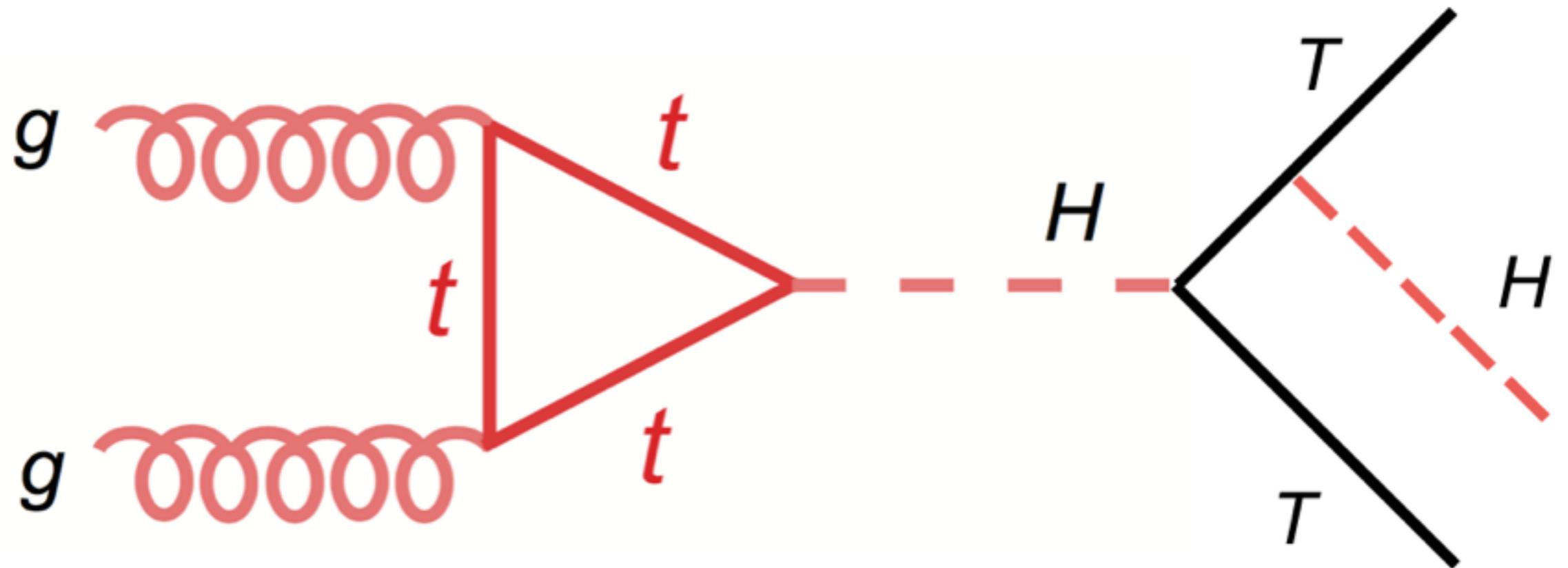
This suggests:

To test the naturalness condition (up to the order of  $v^2/m_T^2$ ), we only need to measure the Yukawa couplings of top quark pair and top partner pair

- ☒ More model-independent: with or without T-parity
- ☒ Irrelevant to the measurement of the decay constant



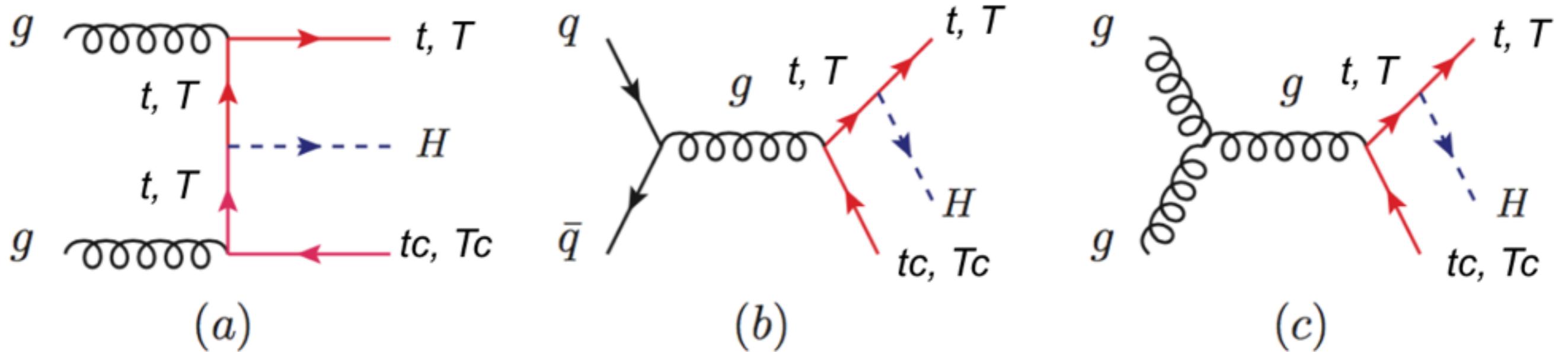
## Collider Strategy - Colorless Top Partners



Maybe mono-Higgs search can help if  $T$  is stable



# Collider Strategy - Colored Top Partners



☞ TTh production at 100 TeV, with

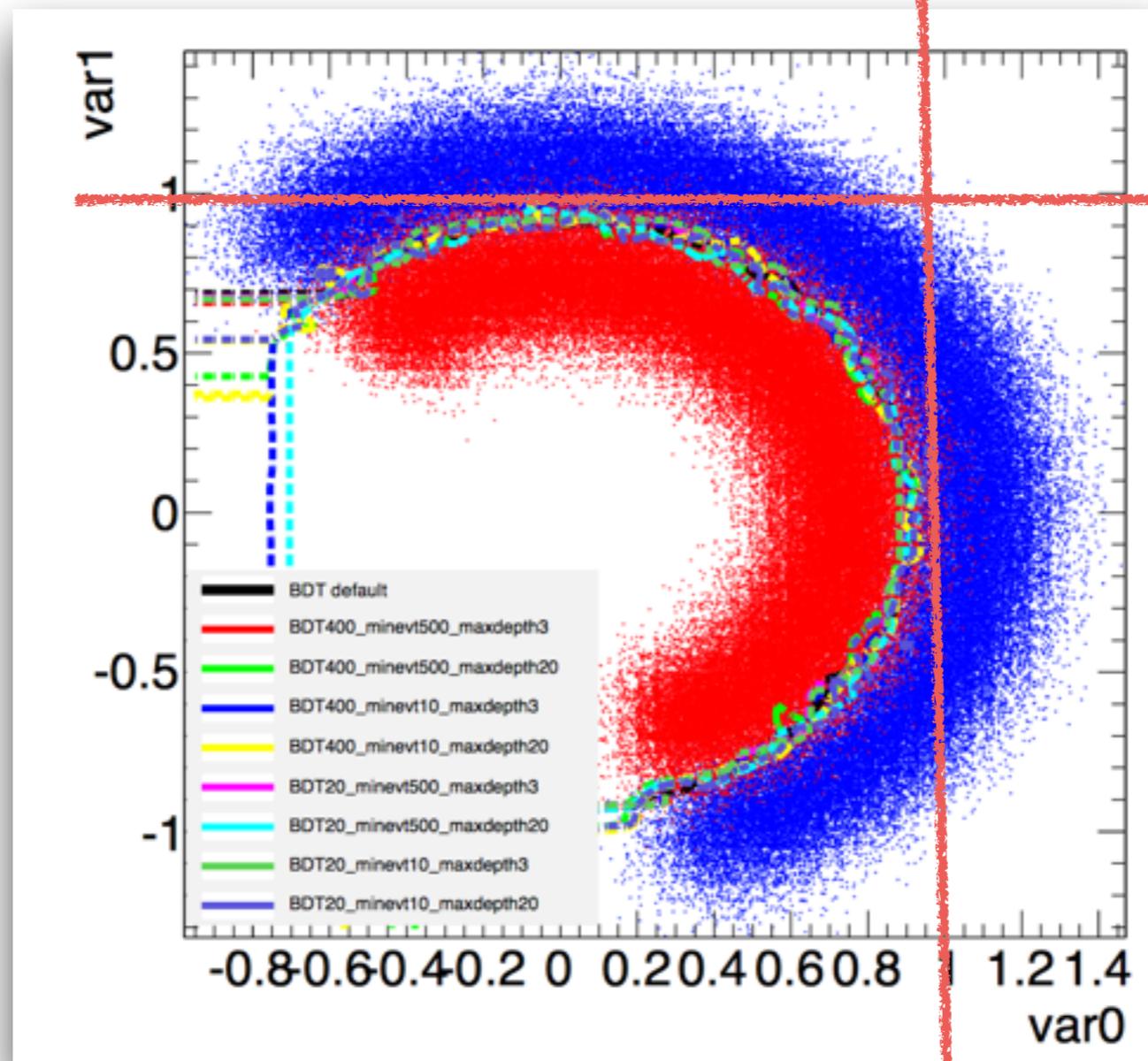
$$\text{BR}(T \rightarrow th) \simeq \text{BR}(T \rightarrow tZ) \simeq \frac{1}{2} \text{BR}(T \rightarrow Wb) \simeq 25\%$$

☞ For convenience of interpretation, introduce the naturalness parameter

$$\mu = -\frac{\Delta m_H^2|_{\text{NP}}}{\Delta m_H^2|_{\text{SM}}} \Rightarrow \mu = -\frac{a_T}{\lambda_t^2} + \mathcal{O}\left(\frac{v^2}{m_T^2}\right) \quad \mu|_{\text{nat}} \equiv 1$$



# The Tool - Boosted Decision Tree



[Yann COADOU '13]

(a) Circular correlation example

BDT: allow us to incorporate the correlation of variables to optimize the analysis. Particularly useful for suppressing combinatorial background



# The Tool - BDT Top Tagger



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## Heavy Higgs bosons at 14 TeV and 100 TeV

Jan Hajer,<sup>a,b</sup> Ying-Ying Li,<sup>a</sup> Tao Liu<sup>a</sup> and John F.H. Shiu<sup>a</sup>

[arXiv.org](#) > [hep-ph](#) > [arXiv:1605.08744](#)

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High Energy Physics – Phenomenology

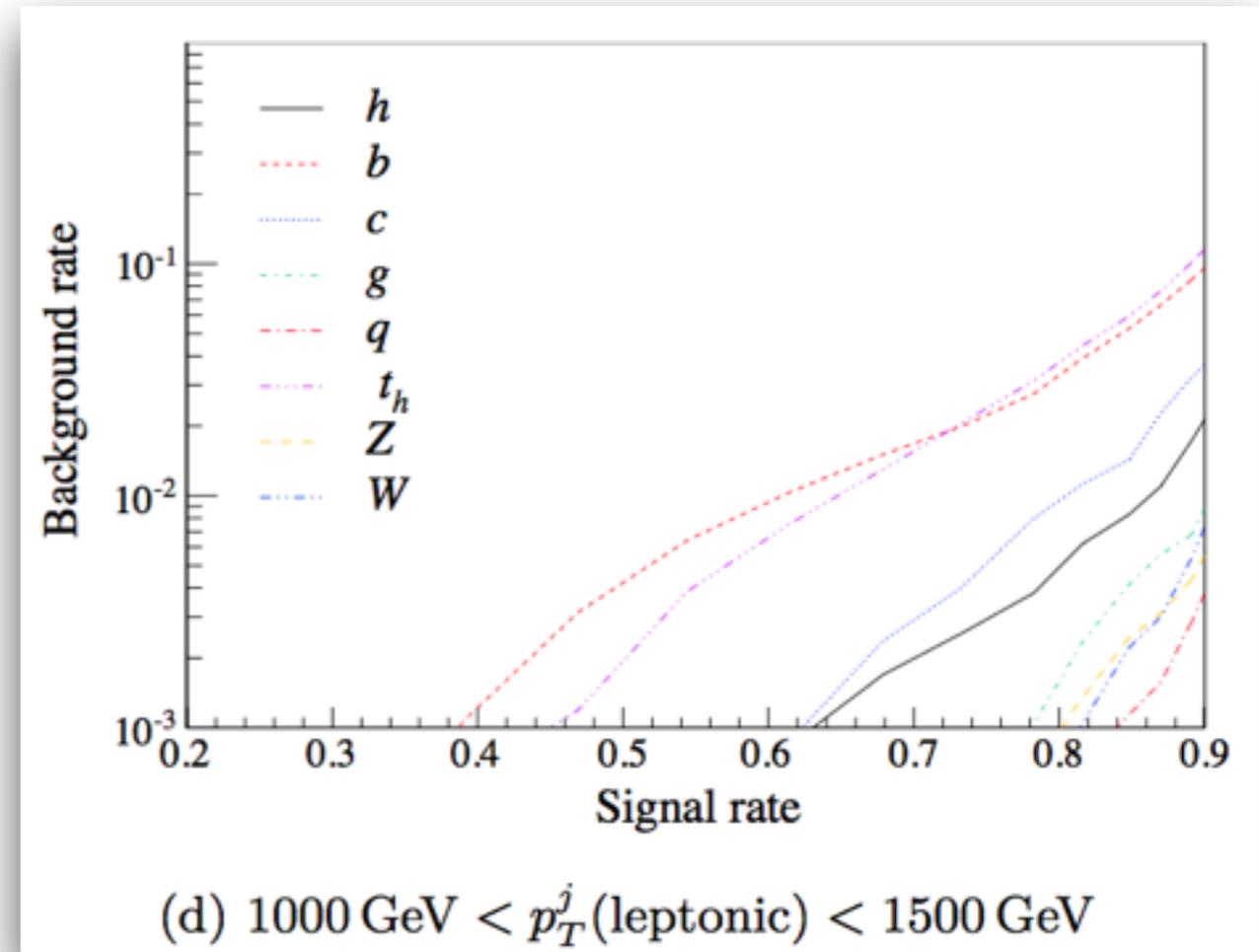
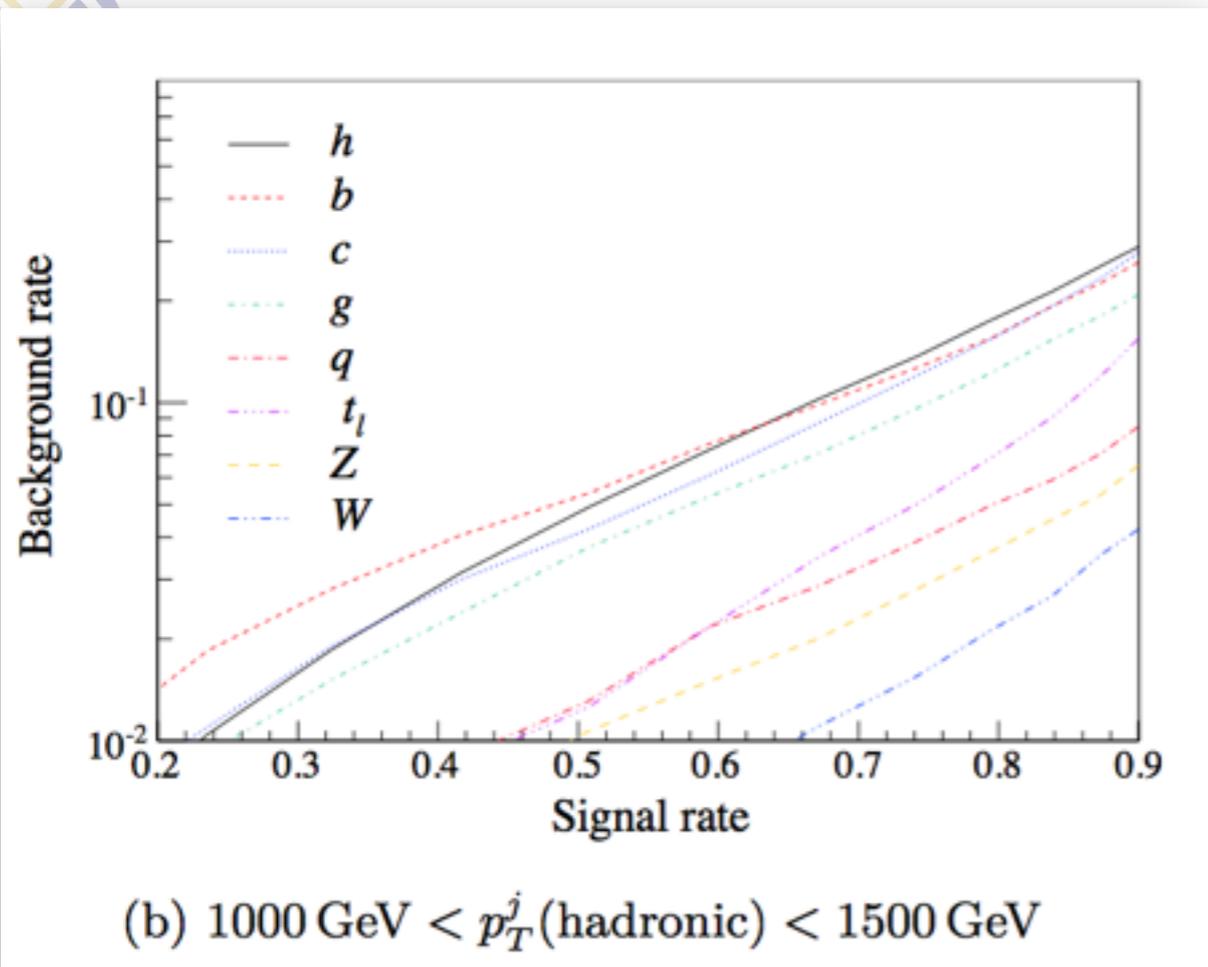
## Heavy Higgs Bosons at Low $\tan \beta$ : from the LHC to 100 TeV

[Nathaniel Craig](#), [Jan Hajer](#), [Ying-Ying Li](#), [Tao Liu](#), [Hao Zhang](#)

(Submitted on 27 May 2016)



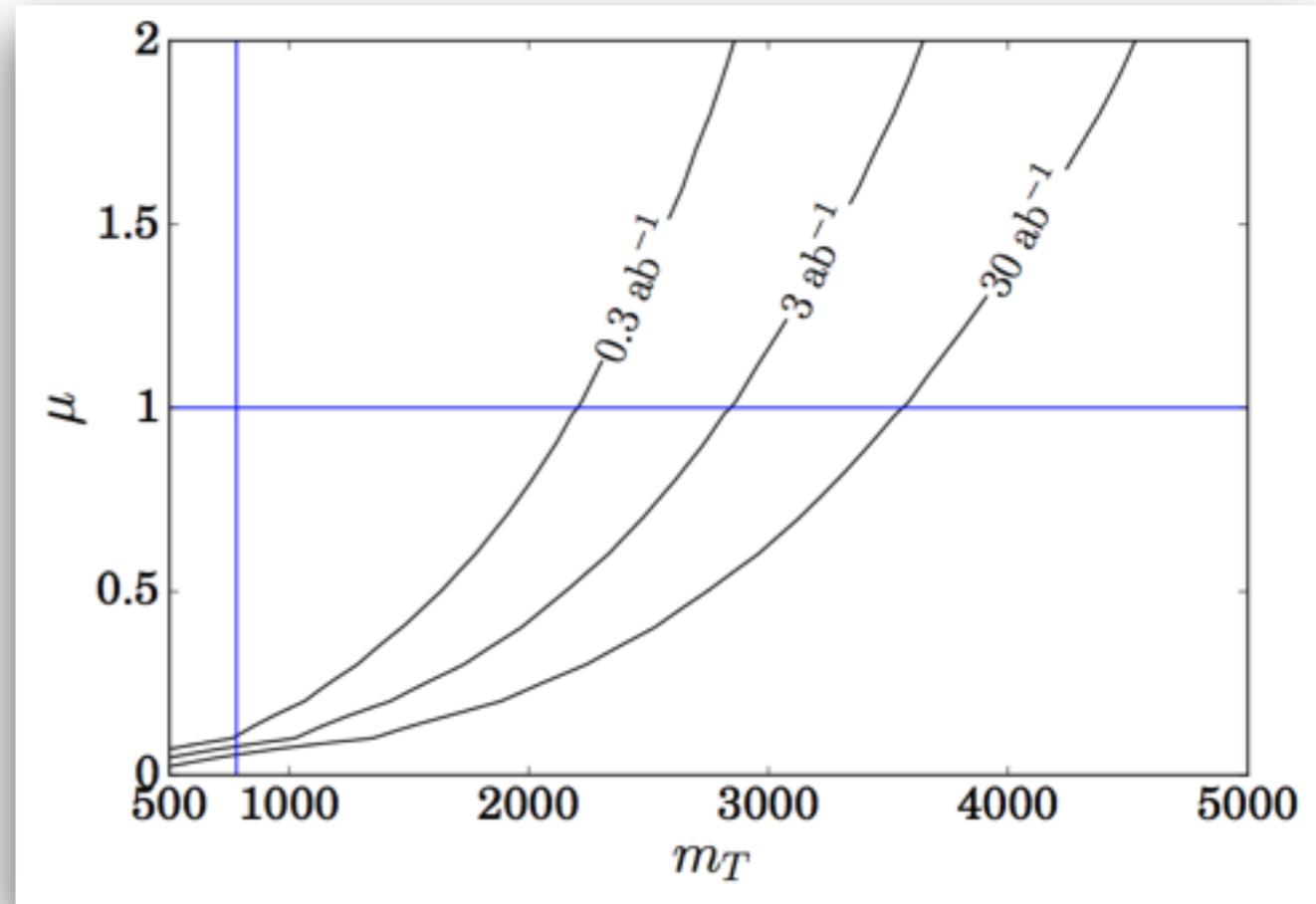
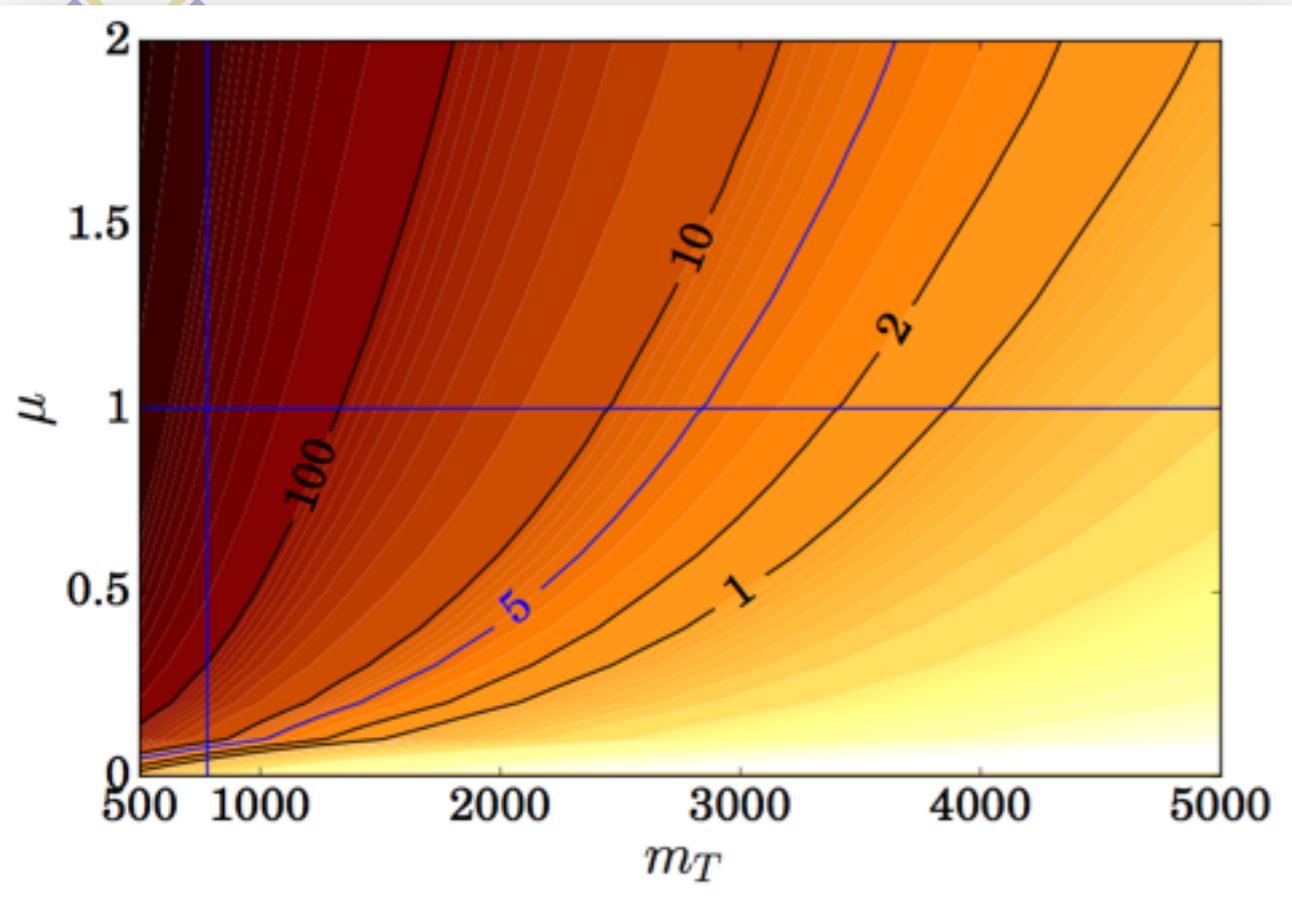
## The Tool - BDT Top Tagger



- Hadronic top tagger:  $b$  secondary vertex and jet mass information, veto hard lepton, etc.
- Leptonic top tagger:  $b$  secondary vertex and lepton information, jet mass requirement, etc.



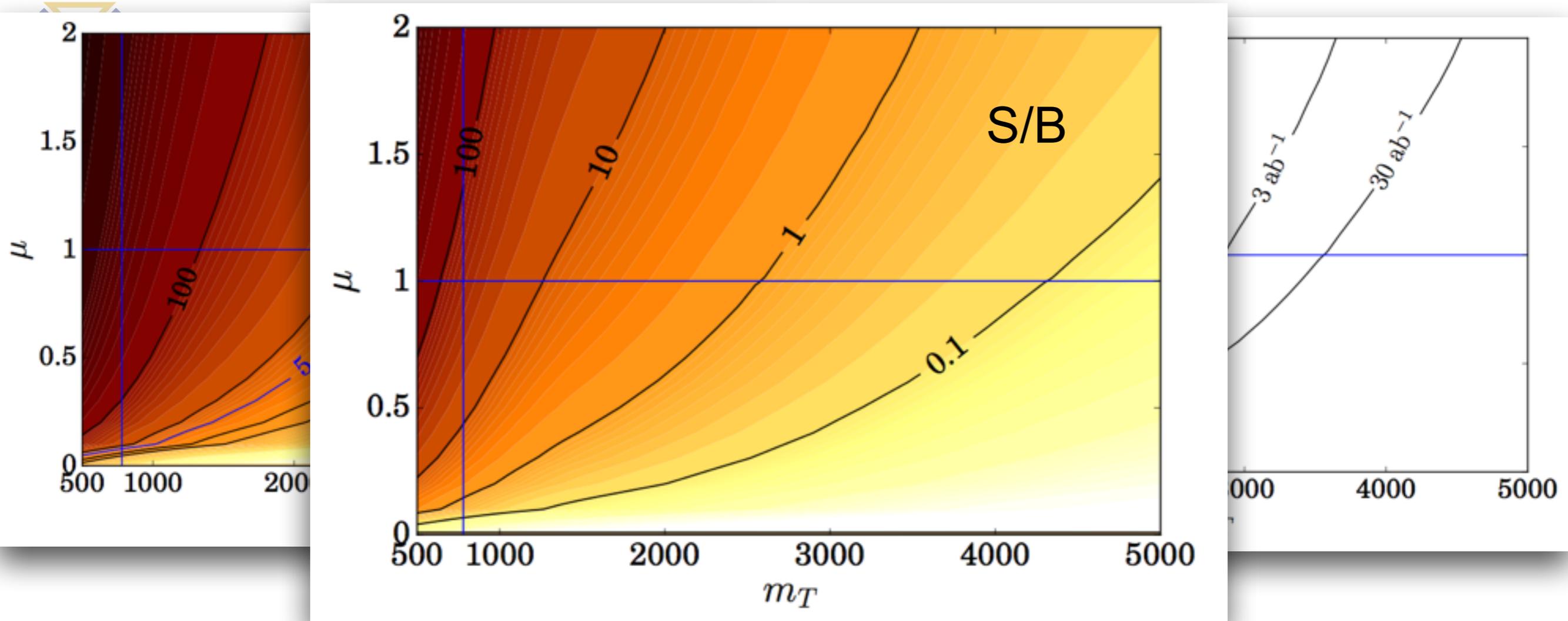
# Discovery Potential of Top Partner



- May not be the most sensitive search channel for top partners  
- to show the effectiveness of the analysis



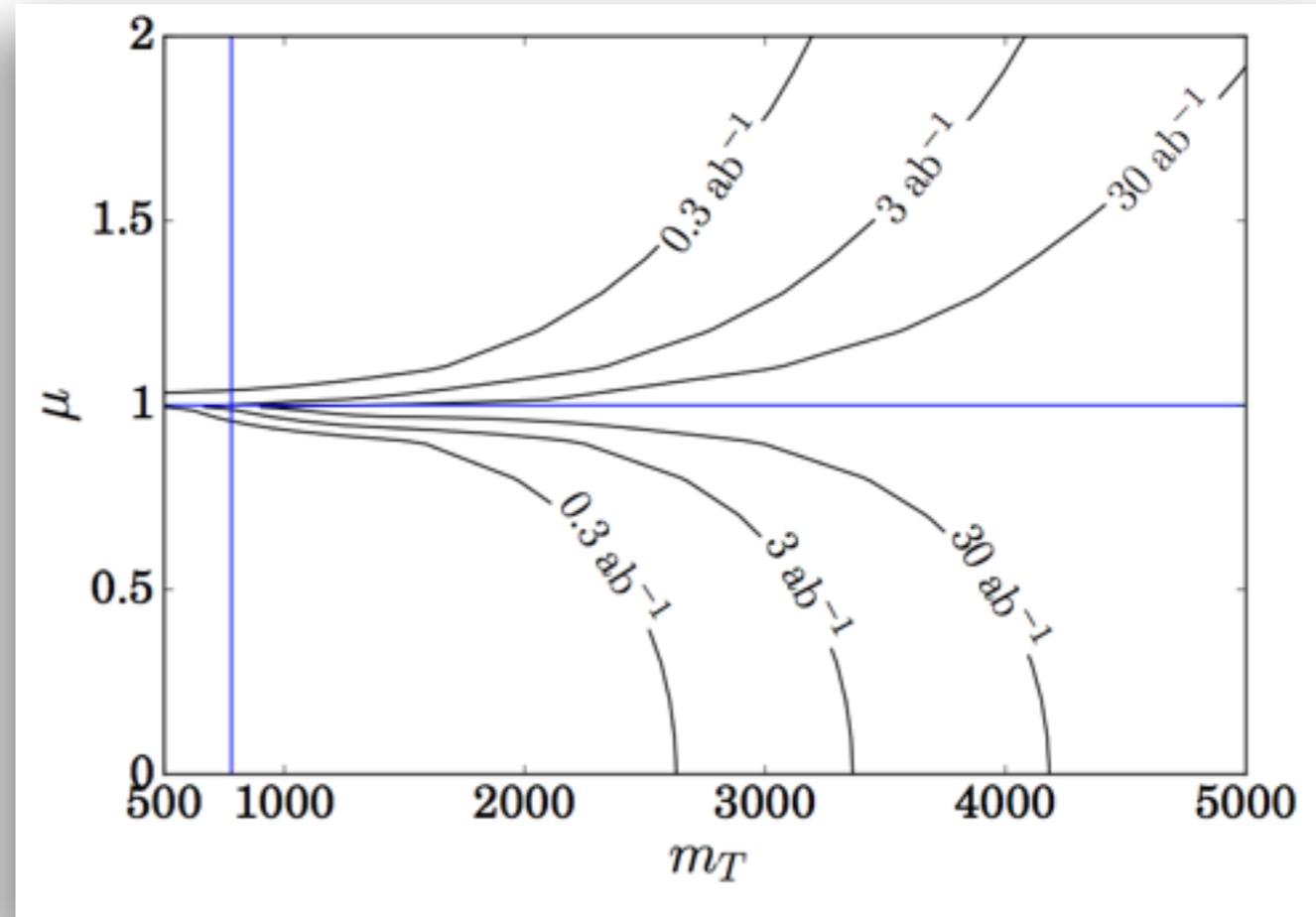
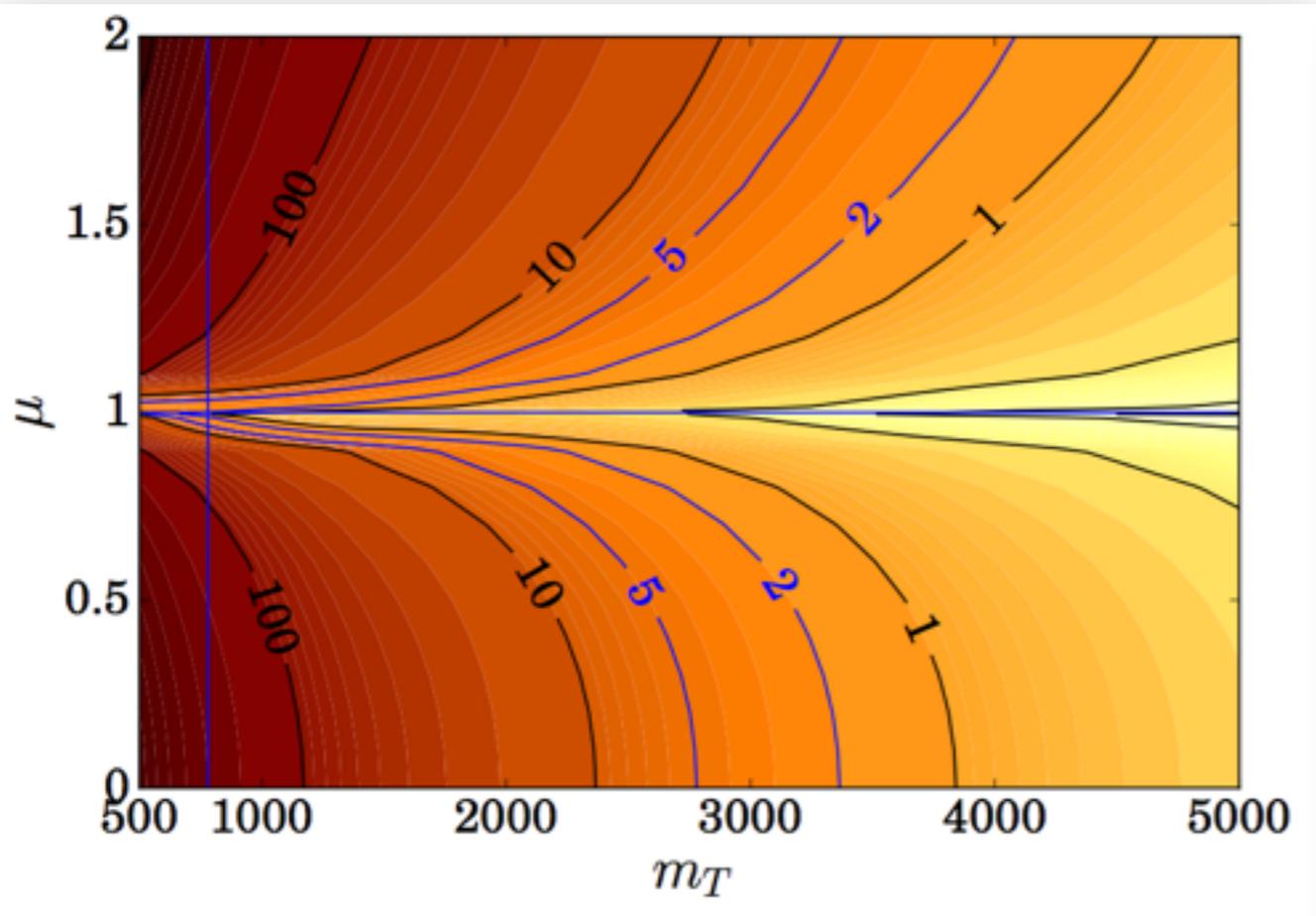
# Discovery Potential of Top Partner



- ❏ May not be the most sensitive search channel for top partners  
- to show the effectiveness of the analysis
- ❏ Sys error is not included. relatively large S/B indicates that it is not out of control



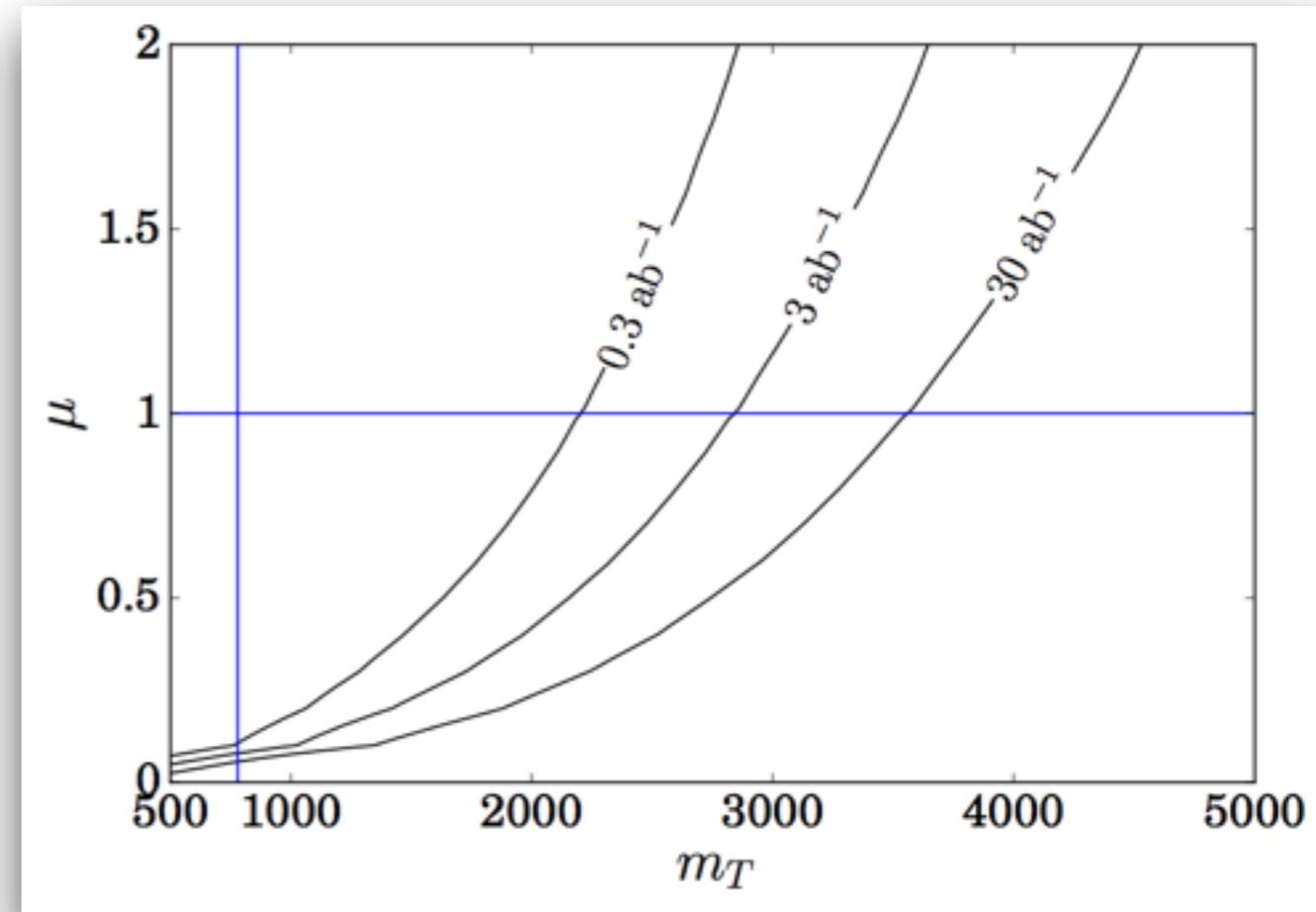
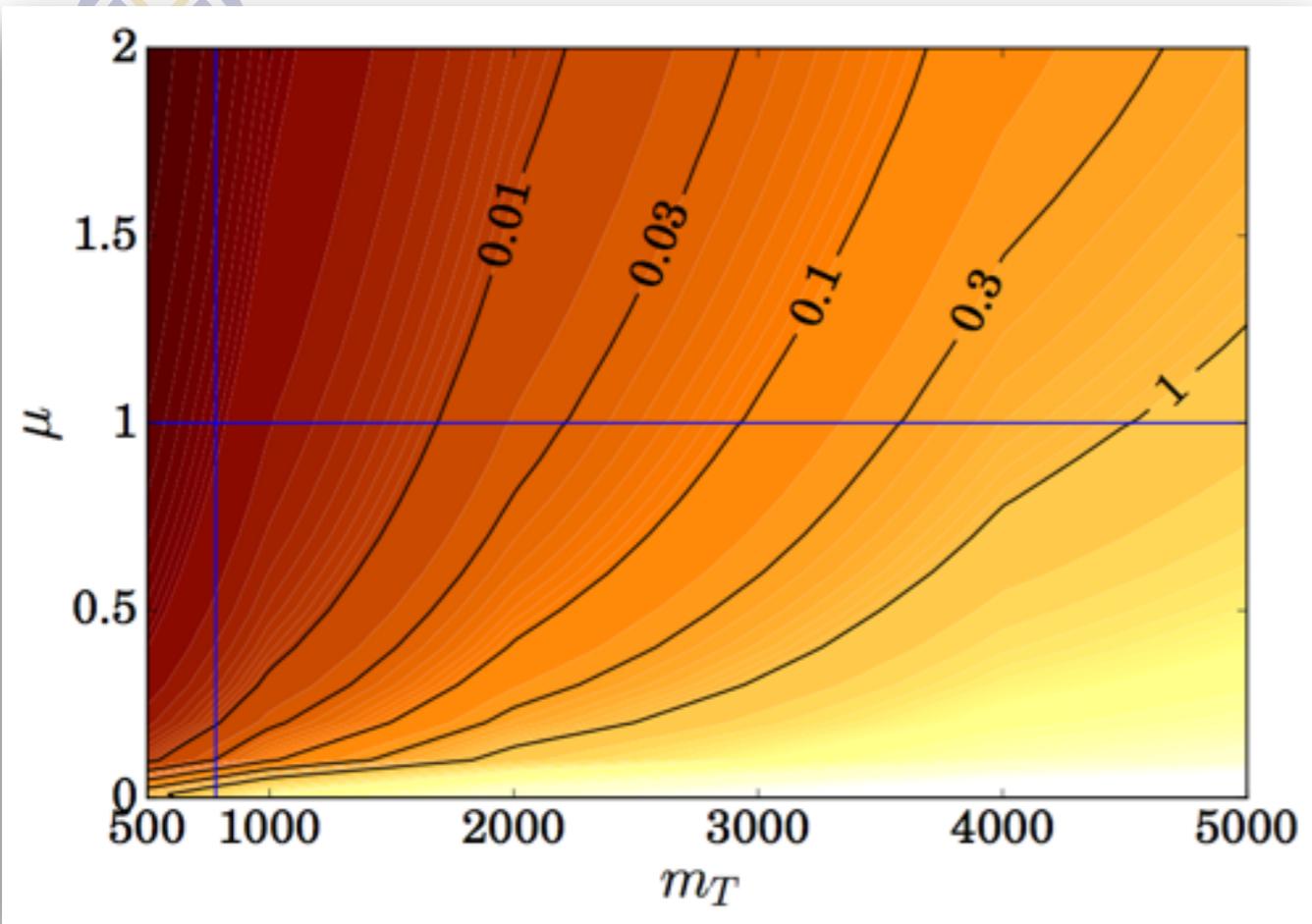
# Exclusion of Unnatural Theories



- ☒ “Unnatural theory” hypothesis - defined wrt the natural theory
- ☒ A deviation from the natural theory larger than 0.1 can be excluded up to  $\sim 3\text{TeV}$



# Precision of Measuring the Naturalness Parameter

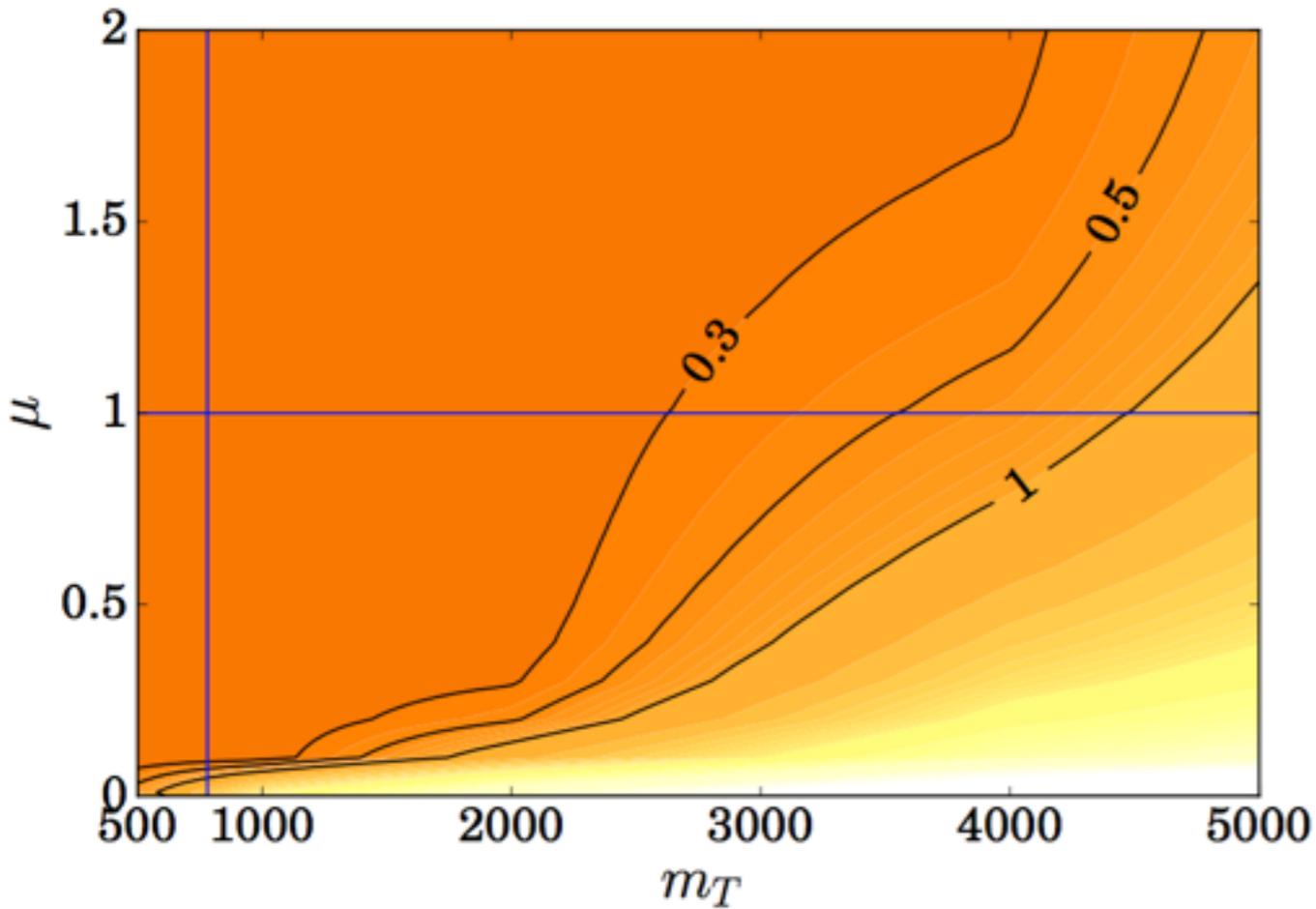


$$\delta\mu = \sqrt{\left(-\frac{1}{\lambda_t^2} \delta a_T\right)^2 + \left(2\frac{a_T}{\lambda_t^3} \delta\lambda_t\right)^2}$$

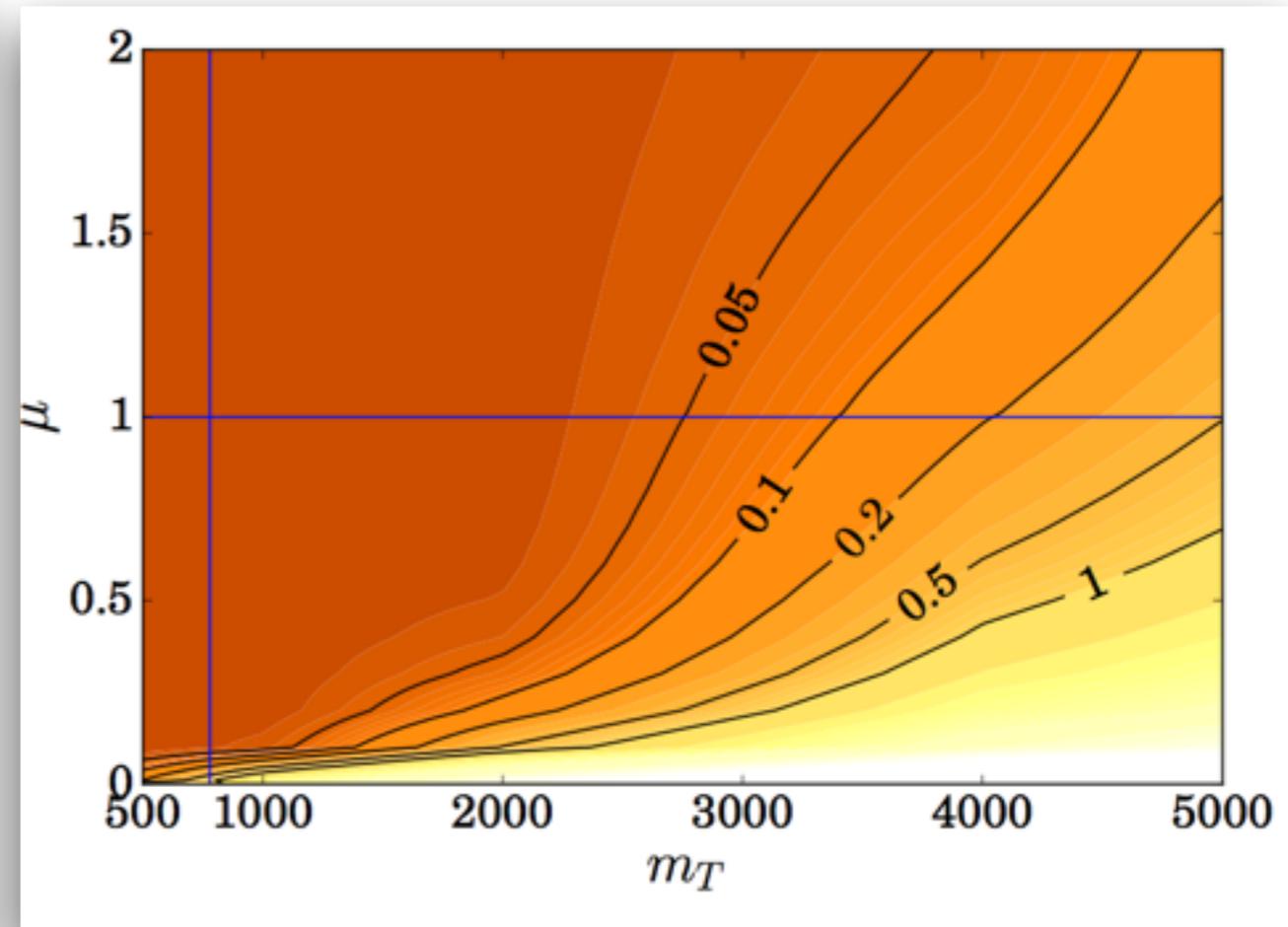
☞ If top Yukawa is perfectly measured, a precision of 10% could be pushed up to 3.5 TeV for a natural theory



# Precision of Measuring Naturalness Parameter



$\delta_{\lambda_t} \sim 10\%$  (HL-LHC)  
+  $\delta_{aT}$  (3/ab, 100TeV)



$\delta_{\lambda_t} \sim 1\%$  (100TeV)  
+  $\delta_{aT}$  (30/ab, 100TeV)

With a precision of 1% which might be achieved for the top Yukawa measurement at 100 TeV [M. Mangano et. al., '15], a precision of 10% could be still pushed up to  $>3$  TeV for a natural theory.



## Summary

- ☒ The naturalness problem drive particle physics for decades
- ☒ To test the theories of naturalness, it is extremely important to measure the naturalness condition
- ☒ The test of the naturalness condition for a top sector with fermionic top partners could be rather model-independent, without directly involving the measurement of the decay constant.
- ☒ At 100 TeV with 30/ab, a precision of 10% for the measurement of the naturalness parameter could be achieved for top partners up to 3 TeV
- ☒ Straightforward to generalize the discussions to the other sectors or the other theories of naturalness

*Thank you!*

