

# Galactic Rotation Curves with Dark Matter Self-Interactions

Ayuki Kamada (IBS-CTPU)

**Based on**

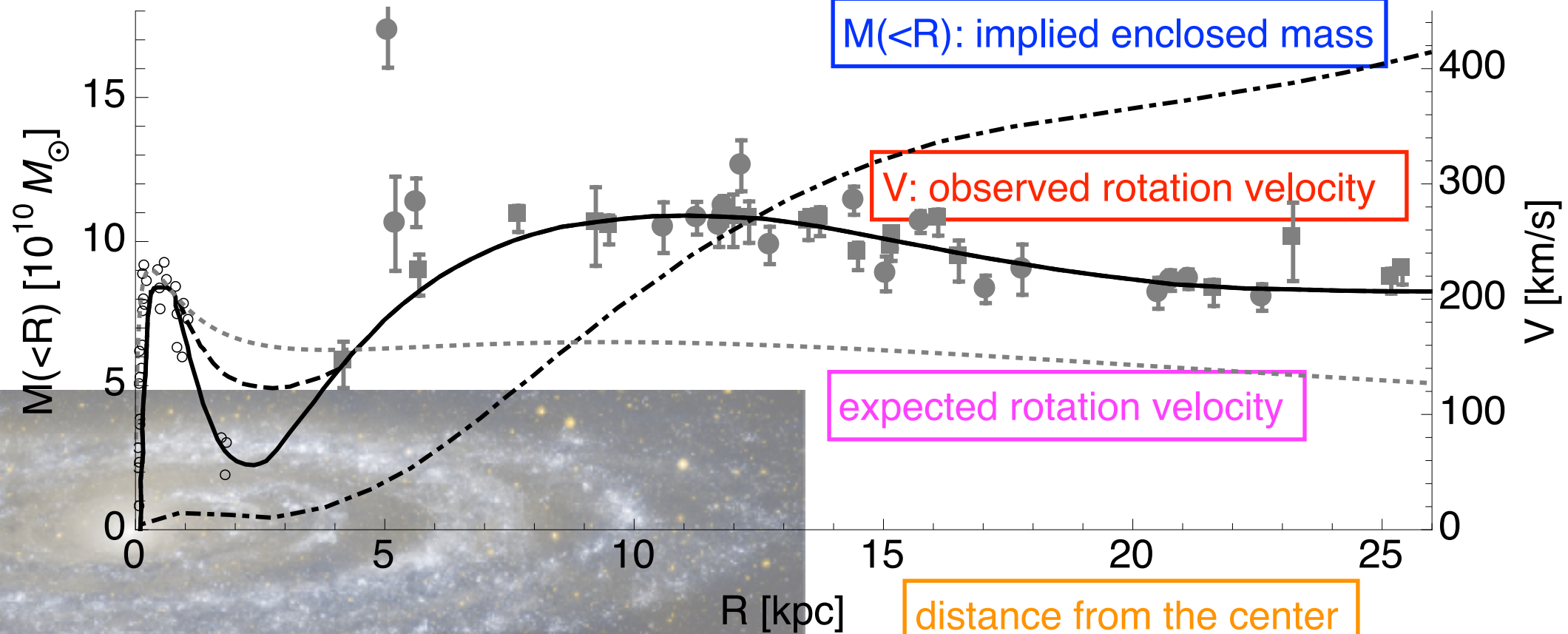
**AK, M. Kaplinghat, A. B. Pace, H.-B. Yu, arXiv:1611.02716**

Dec. 5, 2016 @ Focus Workshop on Particle Physics and Cosmology

# Evidence of Dark Matter

1970 Rubin and Ford  
Measurements of Rotation Curves

Andromeda



# Evidence of Dark Matter

1970 Rubi  
Measurem

Andromeda

Spergel *et al.*, PRL, 2000

dark mass  
supports  
the disk

total mass

rotation velocity

velocity

distance from the center

R [kpc]

V [km/s]

25

400

300

200

100

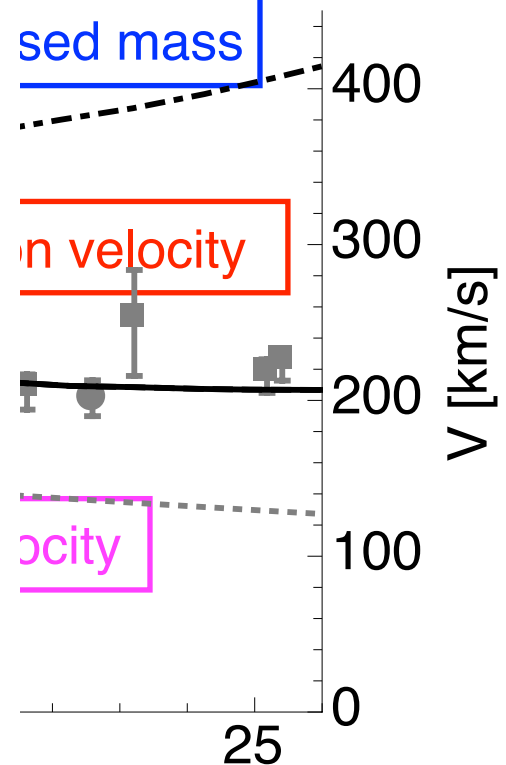
0

DM

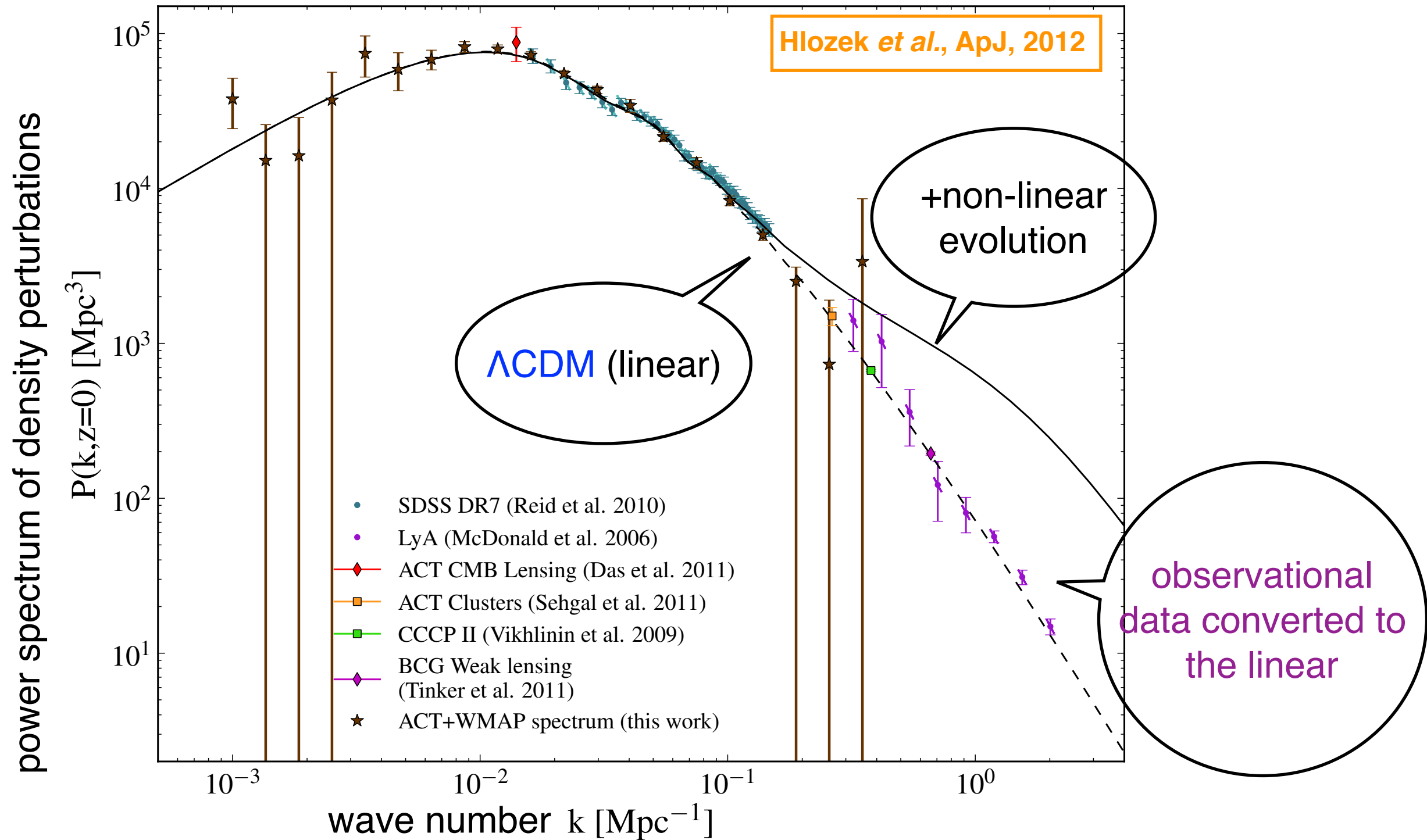
DM

DM

DM



# Large scale structure of the Universe



The  $\Lambda\text{CDM}$  model reproduces well the large scale ( $>\text{Mpc}$ ) structure of the Universe

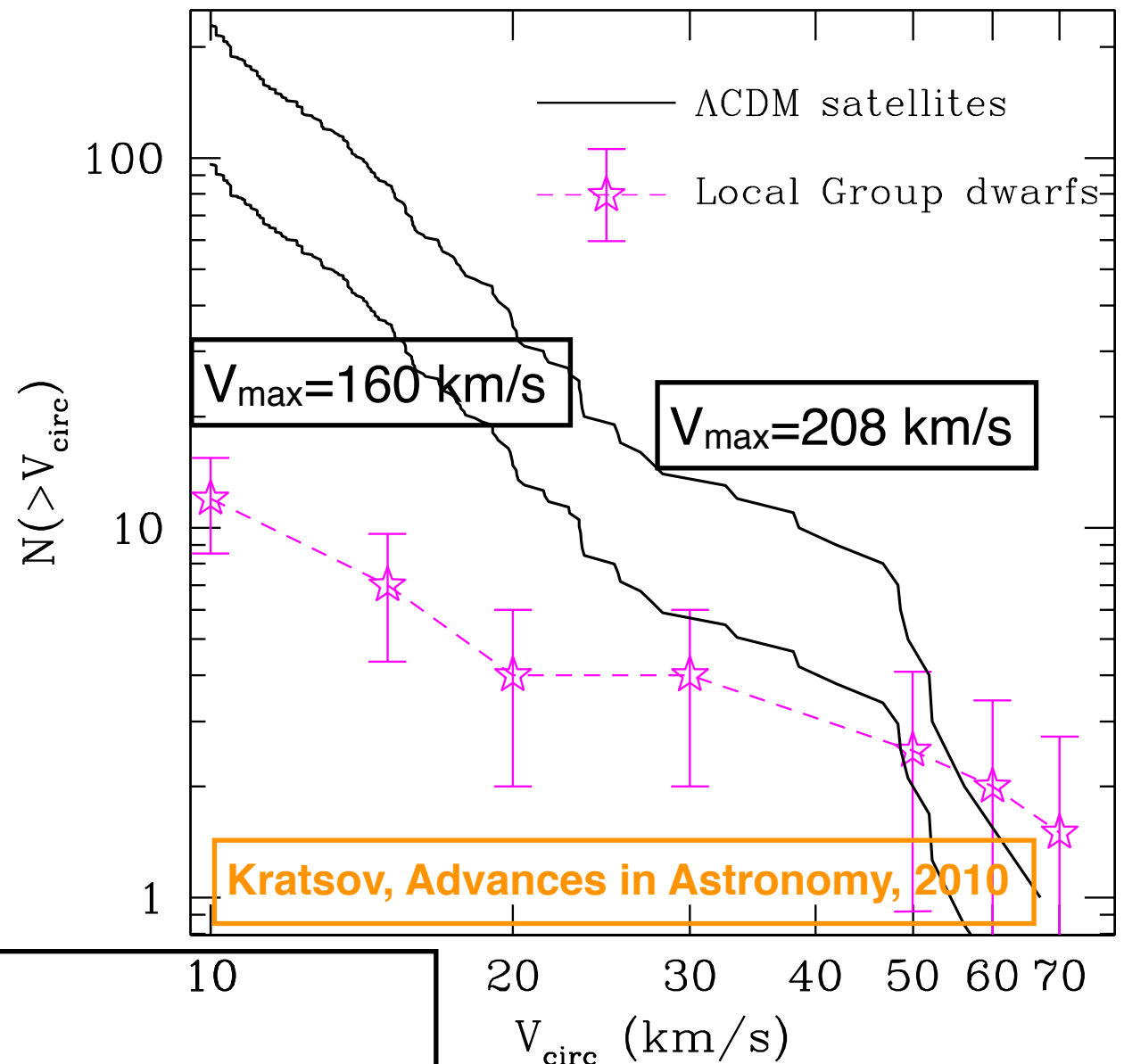
# Small scale crisis I

When  $N$ -body simulations in the  $\Lambda$ CDM model and observations are compared, problems appear at (sub-)galactic scales: **small scale crisis**

## missing satellite problem

$N$ -body (DM-only) simulations in the  $\Lambda$ CDM model  $\rightarrow$  Milky Way-size halos host **O(10)** times larger number of subhalos than that of observed dwarf spheroidal galaxies

cumulative number of subhalos



(maximum) circular velocity

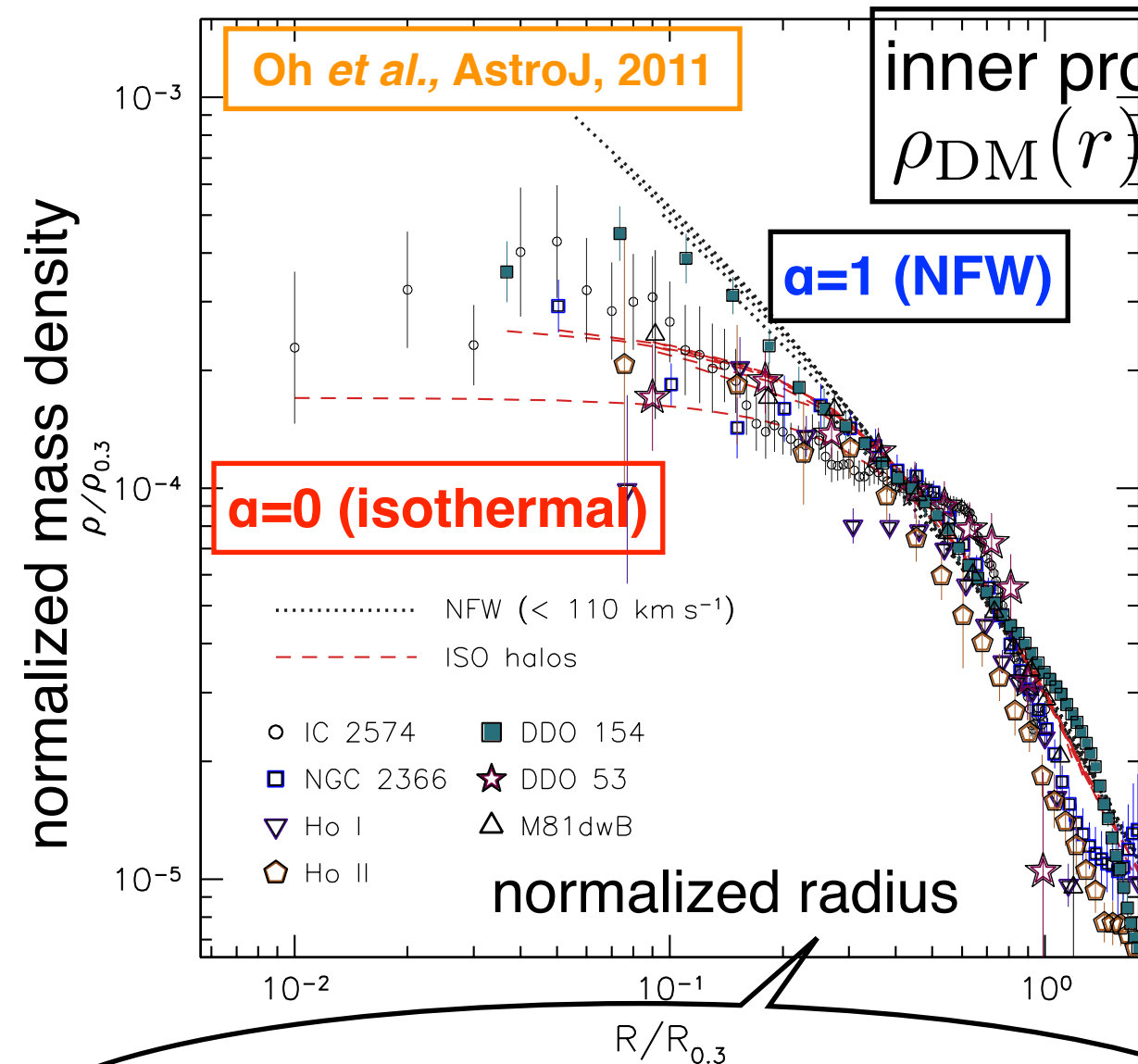
$$V_{\text{circ}}^2(r) = \frac{GM(< r)}{r} \quad V_{\max} = \max_r \{V_{\text{circ}}(r)\}$$

maximal circular velocity of subhalo

# Small scale crisis II

## cusp vs core problem

$N$ -body (DM-only) simulations in  $\Lambda$ CDM model  $\rightarrow$   
**UNIVERSAL** DM profile independent of halo size: **NFW profile**



field dwarf spheroidal galaxies  
 $\sim 10^9 \text{ Msun}$

Observations infer the **CORED** isothermal profile in the inner region rather than the **CUSPY** NFW profile

NFW profile:

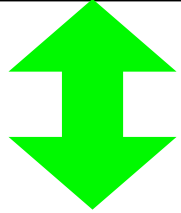
$$\rho_{\text{DM}}(r) = \frac{\rho_s}{r/r_s (1 + r/r_s)^2}$$

isothermal profile:

$$\rho_{\text{DM}}(r) = \rho_{\text{DM}}^0 \begin{cases} 1 & (r \ll r_0) \\ (r_0/r)^2 & (r \gg r_0) \end{cases}$$

# Possible solution I

The above discussions are based on  $N$ -body (**DM-only**) simulations in the  $\Lambda$ CDM model

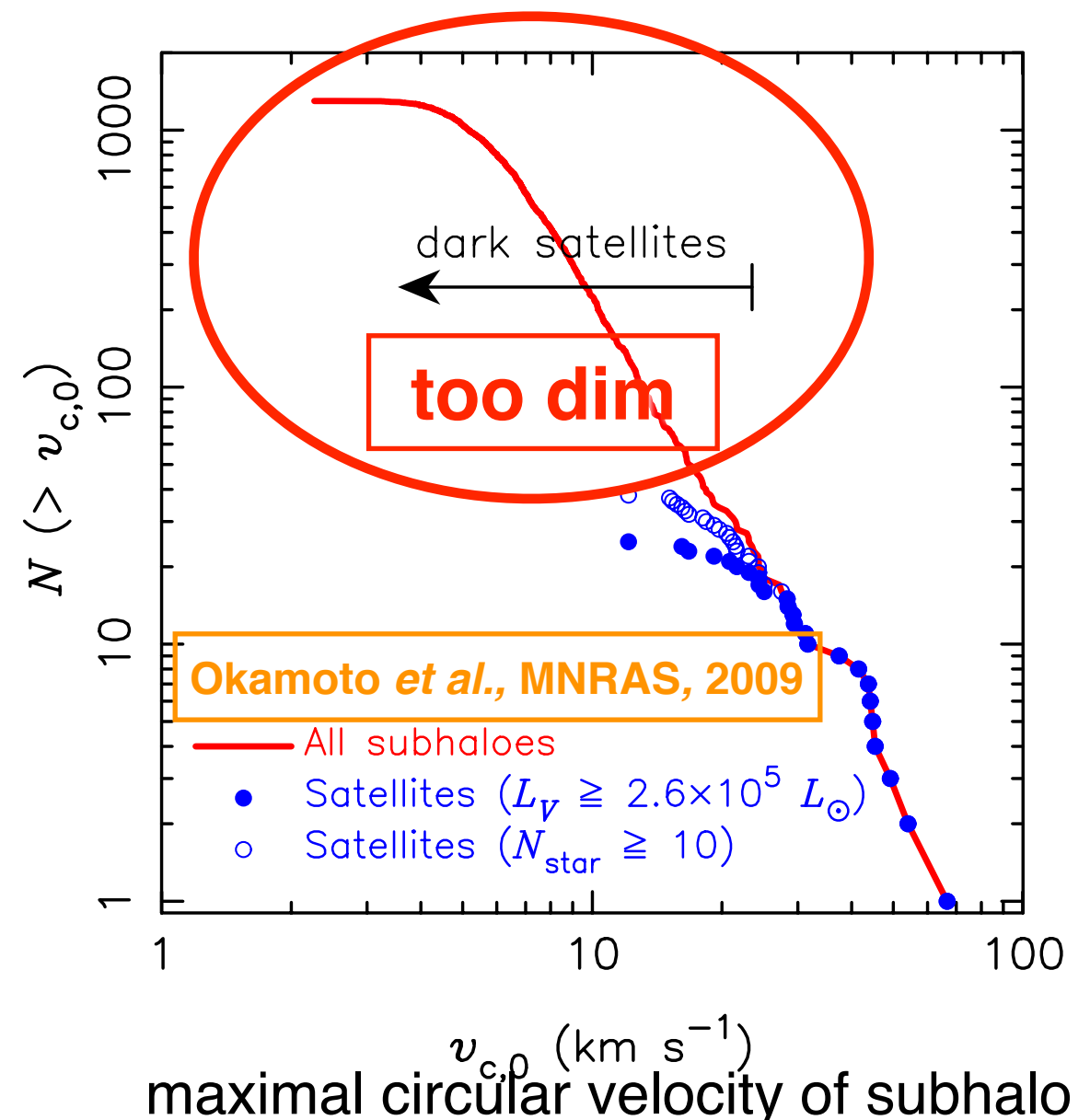


Gravitational potentials are shallower at smaller scales → **BARYONIC HEATING** and **COOLING** processes may be important

## Baryonic processes

- **heating from ionizing photons** - ionizing photons emitted and spread around reionization of the Universe heat and evaporate gases
- **mass loss by supernova explosions** - supernova explosions blow gases from inner region → DM redistribute along shallower potential

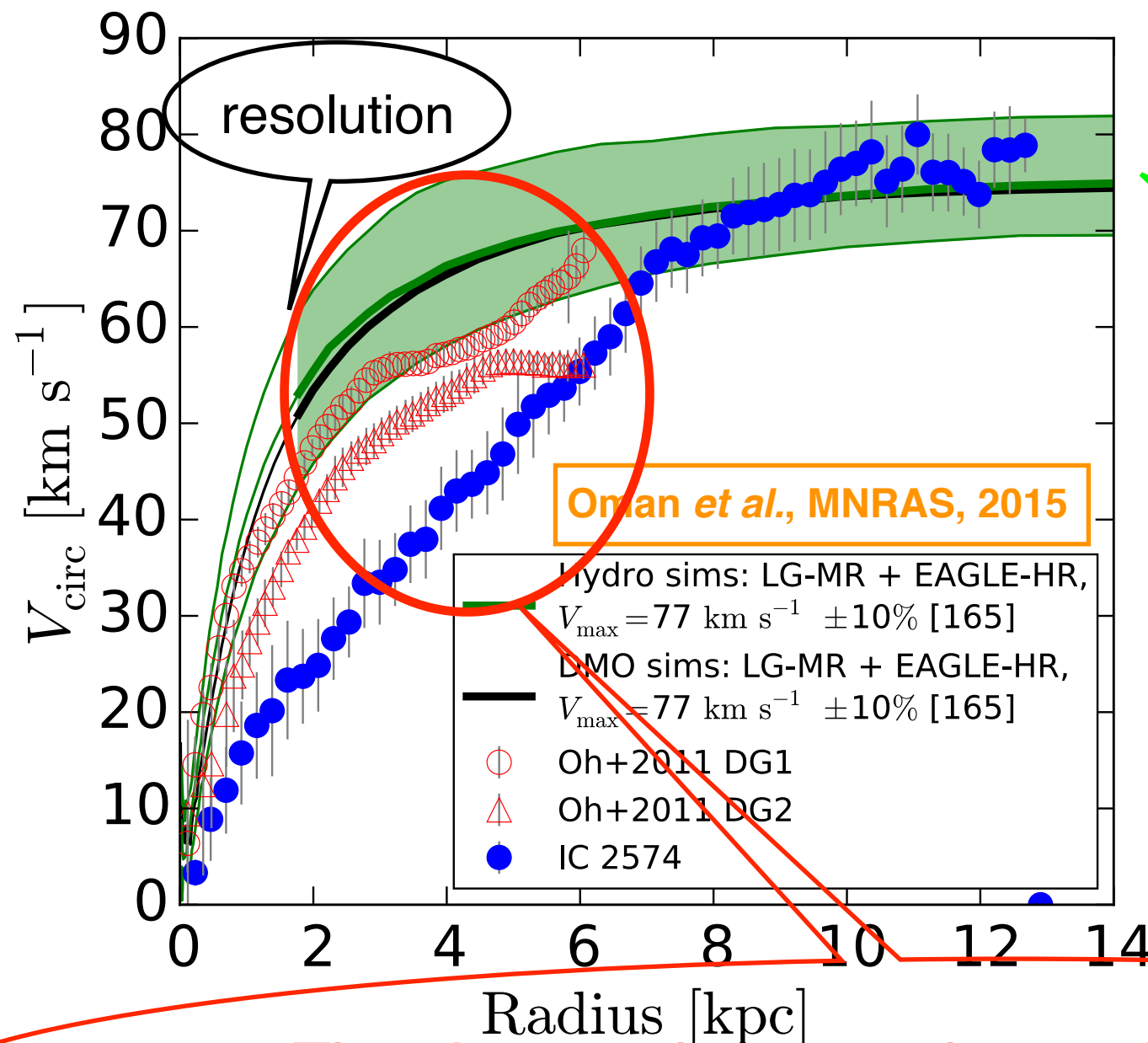
cumulative number of subhalos





# Inner mass deficit problem

Rephrasing cusp vs core problem to emphasize that not only the slope but also the **WHOLE MASS DISTRIBUTION** should be examined



10<sup>th</sup>-90<sup>th</sup> percentile range from the state-of-the-art hydrodynamical simulations in the  $\Lambda$ CDM model (*EAGLE*, *Local GROUPS*) with modeled subgrid baryonic physics (radiative cooling, star formation, stellar and chemical enrichment, energetic stellar feedback, black hole accretion and mergers, and AGN feedback)

The simulated enclosed mass is about **FOUR** times higher than the observed!



# Concentration-mass relation

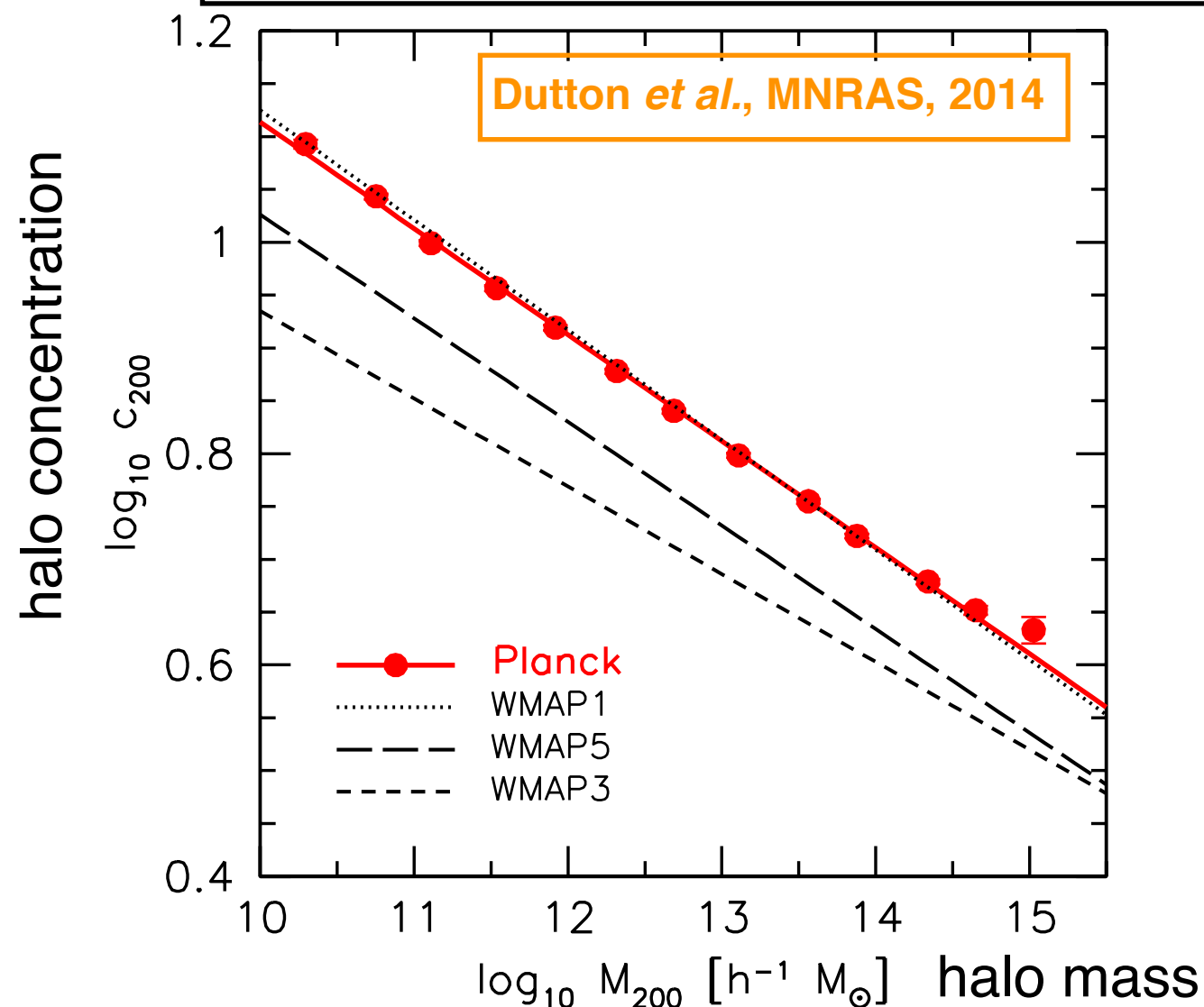
Why is a simulated rotation curve (almost) **DEFINITE** for a given  $V_{\max}$ ?

Two parameters for the NFW profile

$$\rho_{\text{DM}}(r) = \frac{\rho_s}{r/r_s (1 + r/r_s)^2}$$

A relation between two parameters usually given as the **CONCENTRATION-MASS RELATION**

$$c_{200} = 10^{0.905 \pm 0.11} (M_{200}/10^{12} h^{-1} M_{\odot})$$



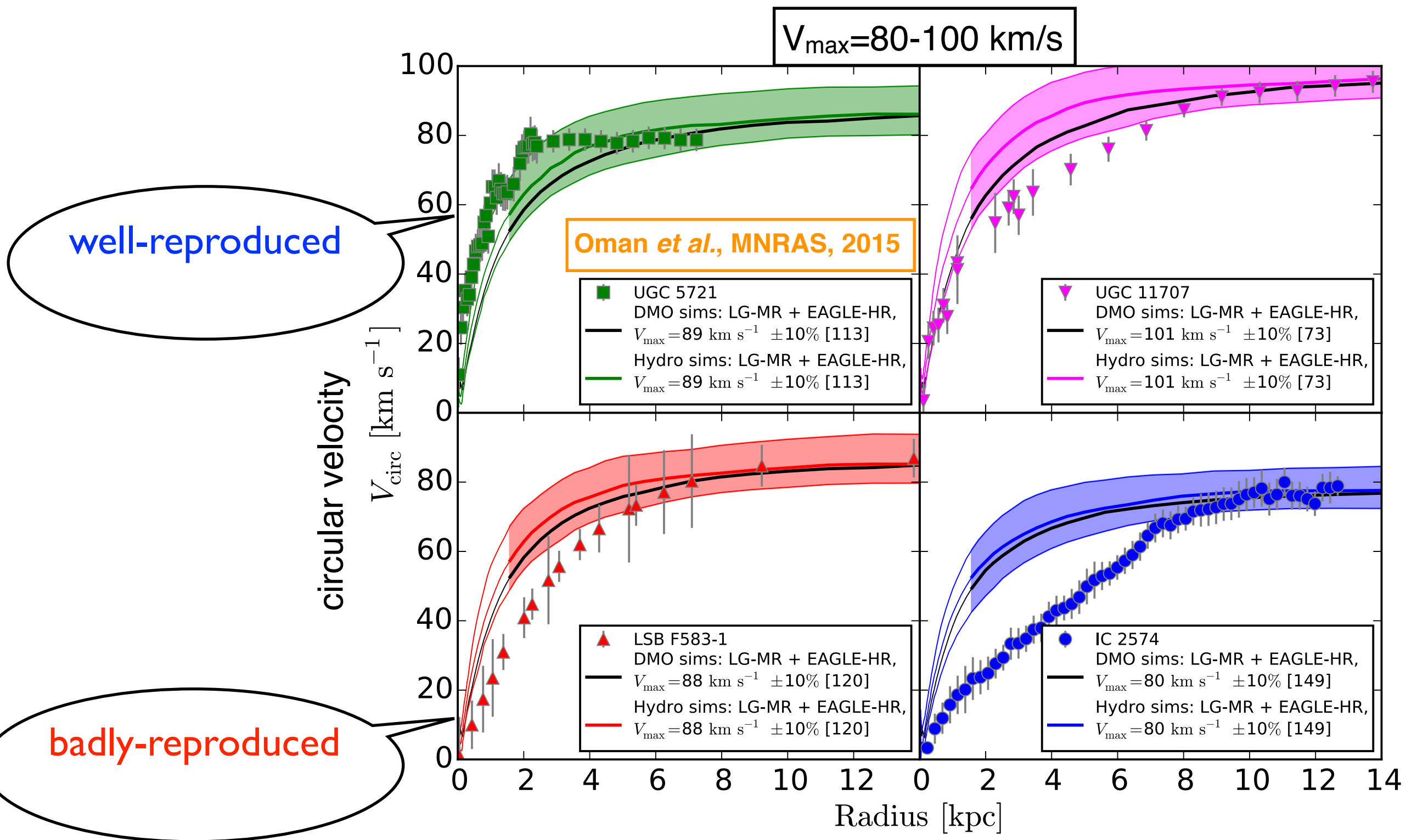
small  
intrinsic scatter

$$c_{200} = r_{200}/r_s$$

$$M_{200}(< r_{200}) = \frac{4\pi}{3} \bar{\rho}_M r_{200}^3$$

# Unexpected diversity problem

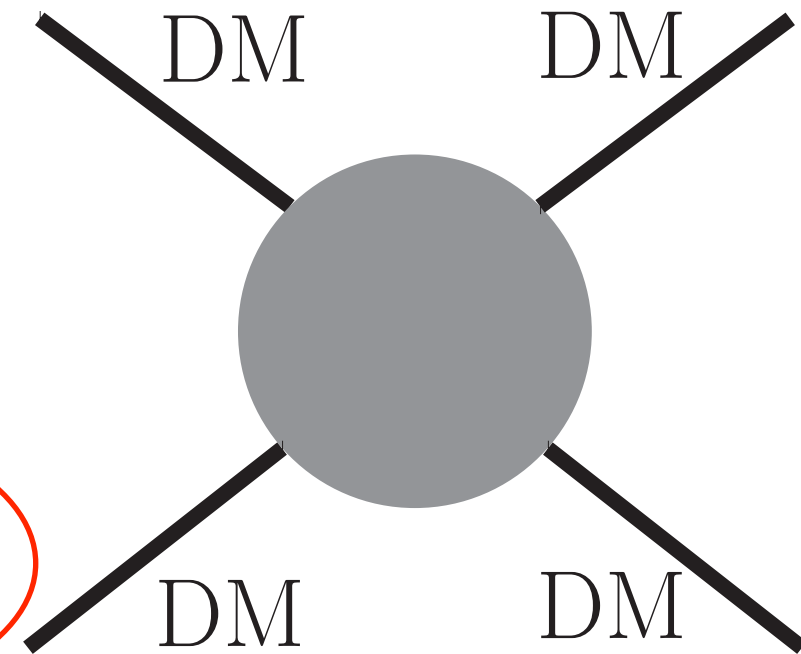
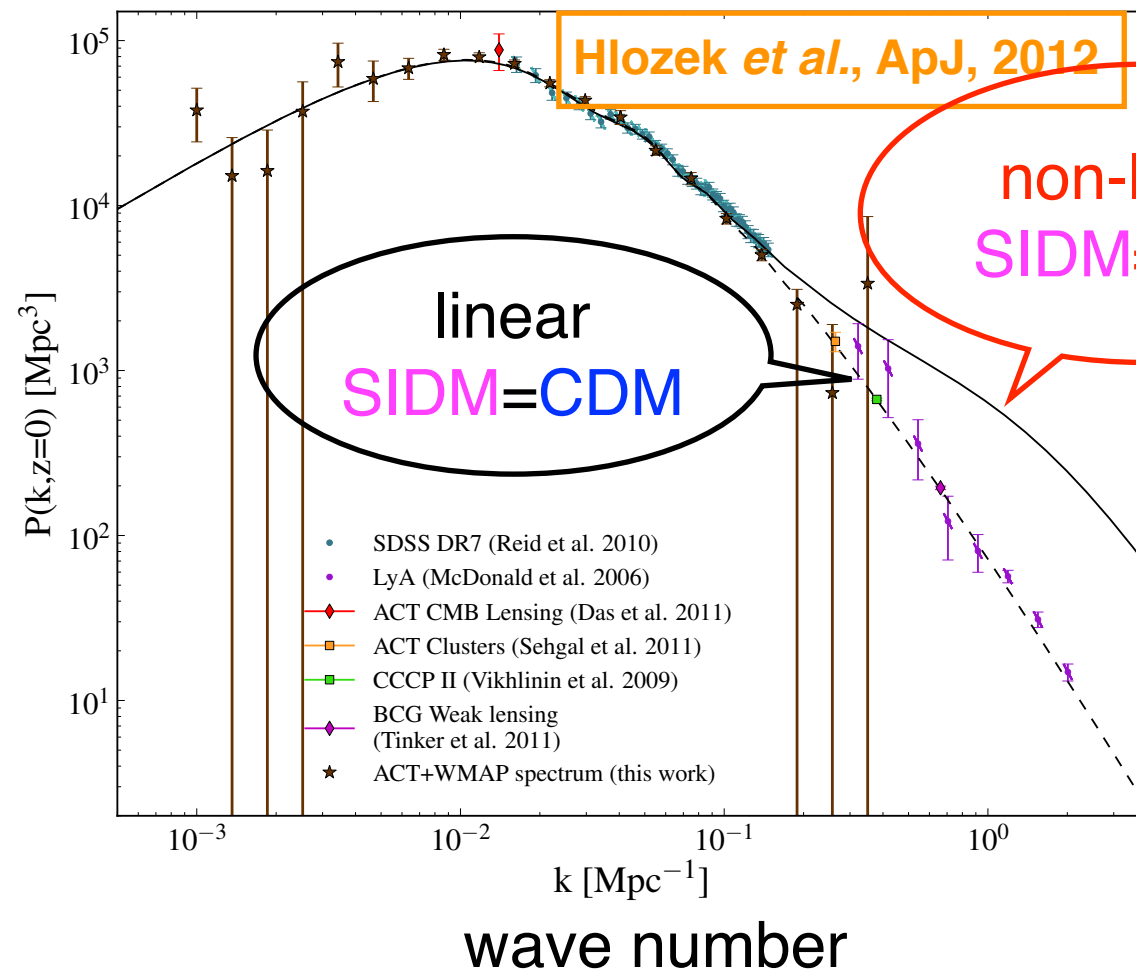
The inner mass deficit is **NOT UNIVERSAL**, but should be elaborated in a **GALAXY-BY-GALAXY** manner even with  $V_{\text{max}}$  fixed



# Dark matter self-interaction

Self-Interacting Dark Matter: **SIDM**

power spectrum of density perturbations



Reaction rate  $\Gamma = \sigma v \rho / m$   
 $\sigma$ : cross section  
 $v$ : relative velocity  
 $\rho$ : dark matter mass density  
 $m$ : dark matter mass

**SIDM structure formation starts with the same linear (initial) matter power spectra as  $\Lambda\text{CDM}$ , but self-interactions become important as structure formation proceeds  $\leftrightarrow \rho$  increases**

# SIDM halo - mass density

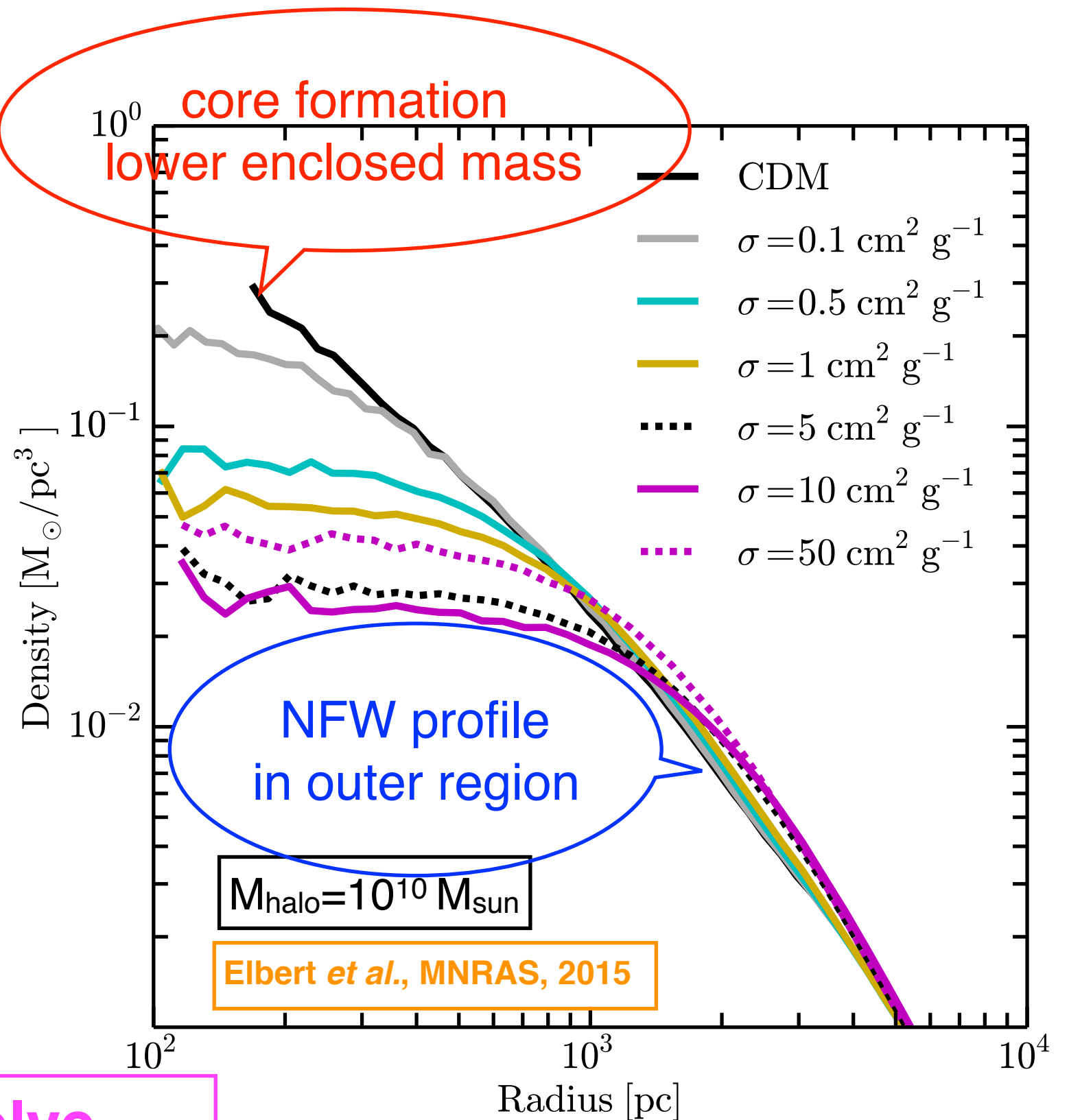
SIDM-only simulation

As  $\sigma/m$  increases,  
central density decreases

Inverted at some point  
← gravo-thermo instability  
↔ core-collapse

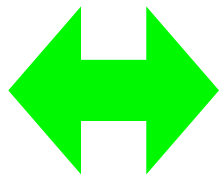


$\sigma/m=0.5-5 \text{ cm}^2/\text{g}$  may solve  
the inner mass deficit problem



# Origin of the diversity

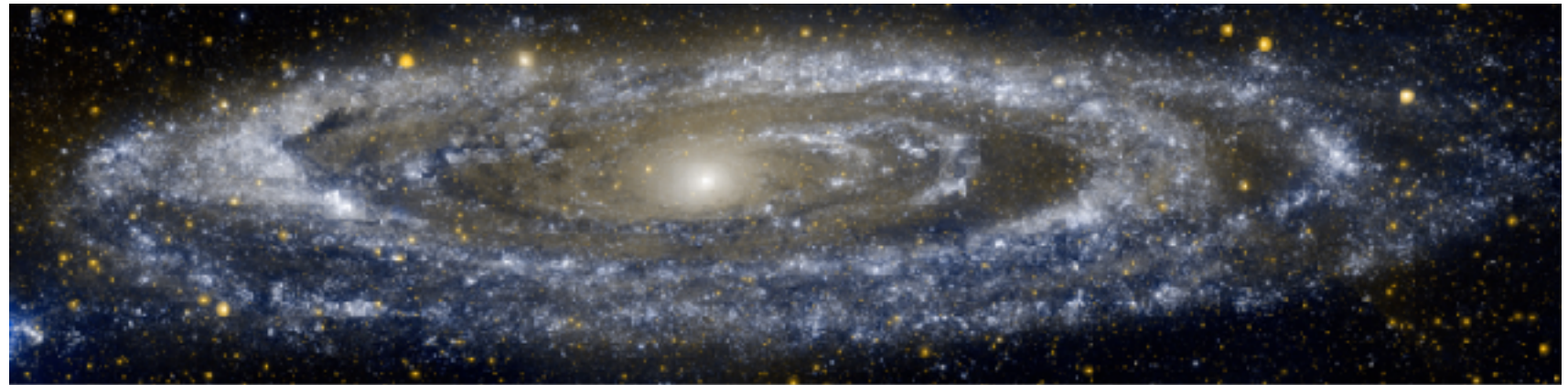
## Unexpected diversity problem??



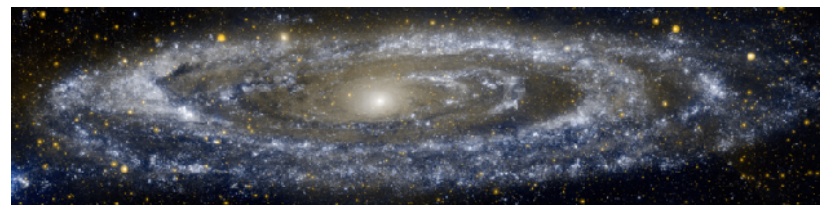
For a given cross section ( $\sigma/m=3 \text{ cm}^2/\text{g}$  in the following), the SIDM halo profile is still **DEFINITE** and characterized by only one parameter  $V_{\text{max}}$

Scatter in distributions of the baryons even in similar-size halos!!

Extended  
stellar disk



Compact  
stellar disk



# Influence of the baryons

SIDM static distribution with a thin exponential disk potential from the Poisson equation

$$\Delta\phi = 4\pi G\rho_{\text{DM}}^0 \exp(-\phi/\sigma^2)$$

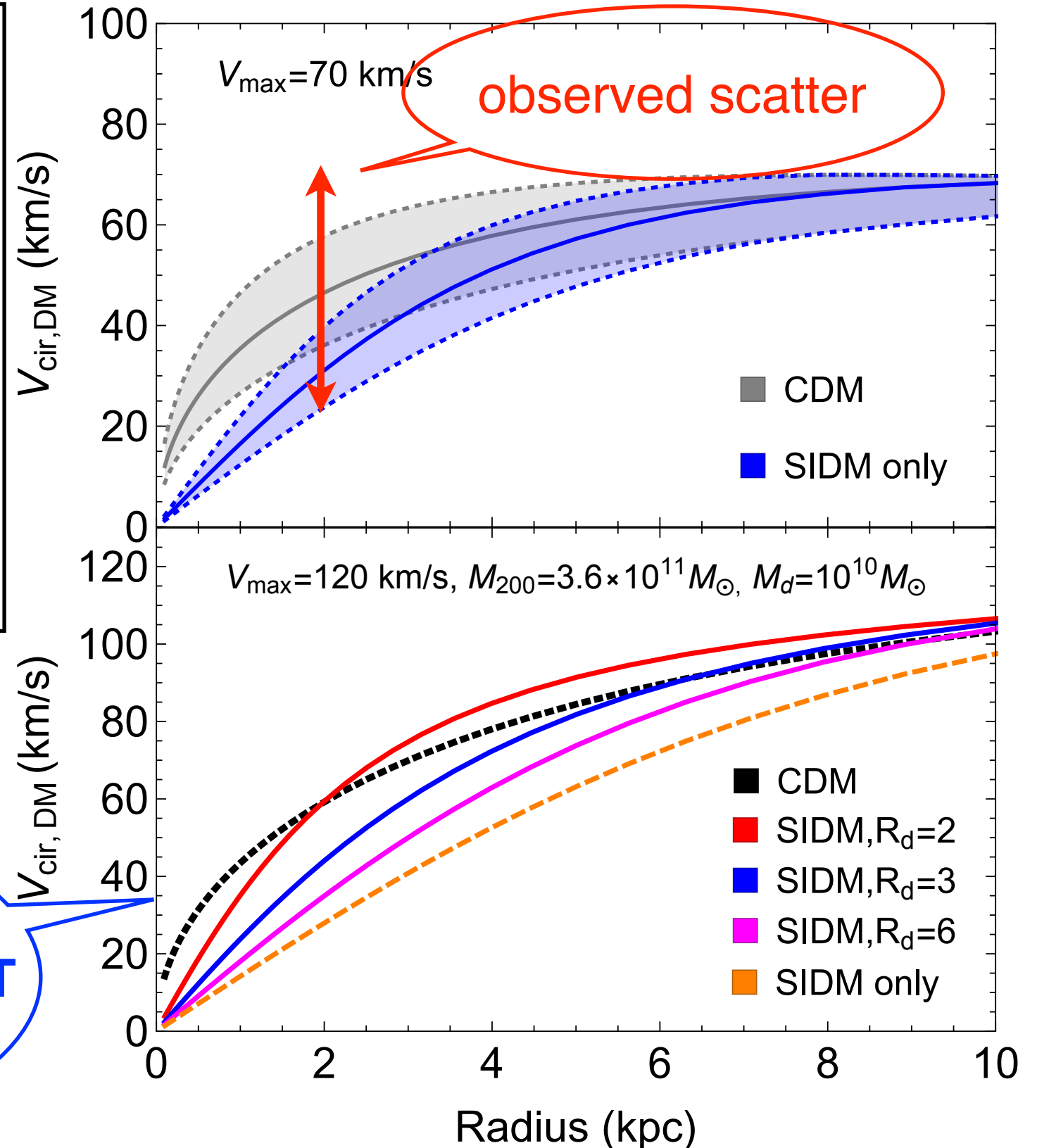
$$\phi(0) = 0$$

$$\phi(\vec{x}) \rightarrow V_\infty^2 \ln(r/r_0)$$

$$(r = |\vec{x}| \rightarrow \infty)$$

$$V_\infty^2 = 2\sigma^2 = 4\pi G\rho_{\text{DM}}^0 r_0^2$$

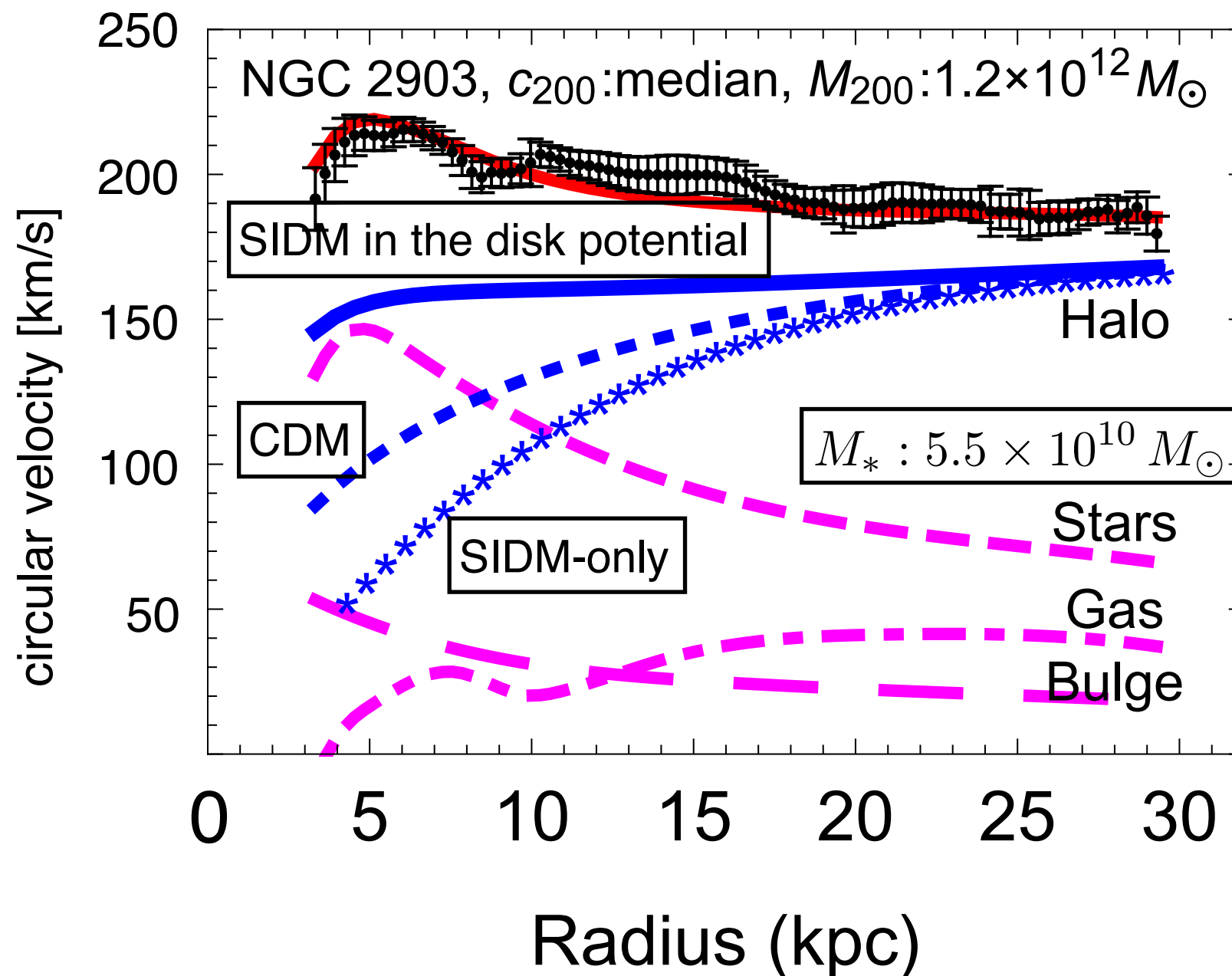
SIDM profile **CONTRACTS**  
under the presence of a **COMPACT**  
stellar disk





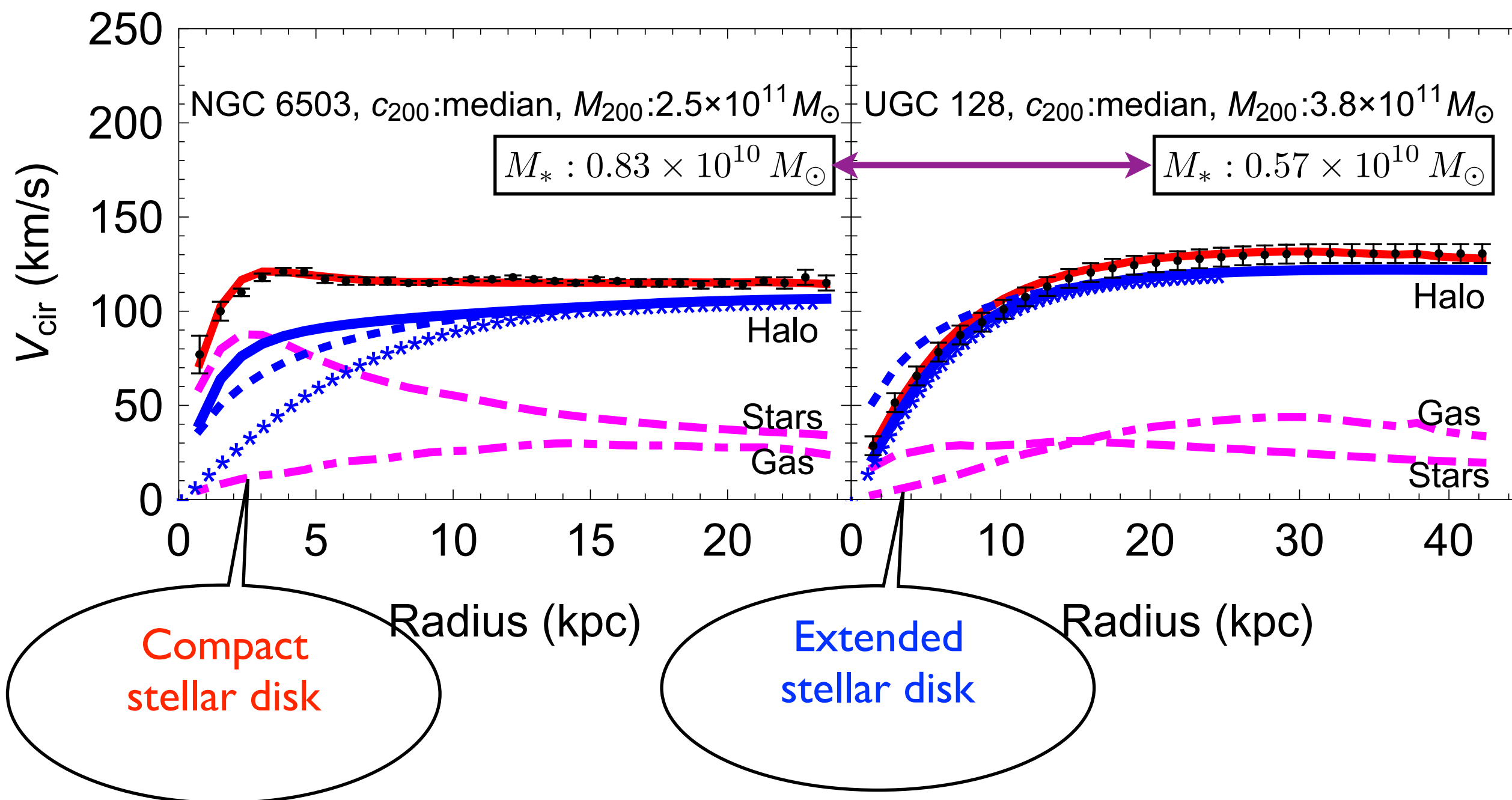
# Case study I

In **MASSIVE** spiral galaxies,  
stellar disks can change **WHOLE SIDM MASS DISTRIBUTIONS**



# Case study II

SIDM halo profile reflects **HOW COMPACT** the hosted stellar disk is even with similar  **$V_{\max}$  AND  $M_*$**



# Constraints from galaxy clusters

Halo shape - ellipticity  
- galaxy cluster MS 2137-23  
( $e=0.18$  @  $r=70$  kpc)

(estimate)  $\sigma/m < 0.02 \text{ cm}^2/\text{g}$

Miralda-Escudé *et al.*, ApJ, 2002

(simulation/l.o.s. effect)

$\sigma/m < 1 \text{ cm}^2/\text{g}$

Peter *et al.*, MNRAS, 2013

Bullet cluster - transparency  
- 1E0657-558

(offset)  $\sigma/m < 1.25 \text{ cm}^2/\text{g}$

(massloss)  $\sigma/m < 0.7 \text{ cm}^2/\text{g}$

Randall *et al.*, ApJ, 2008

- an ensemble (72)

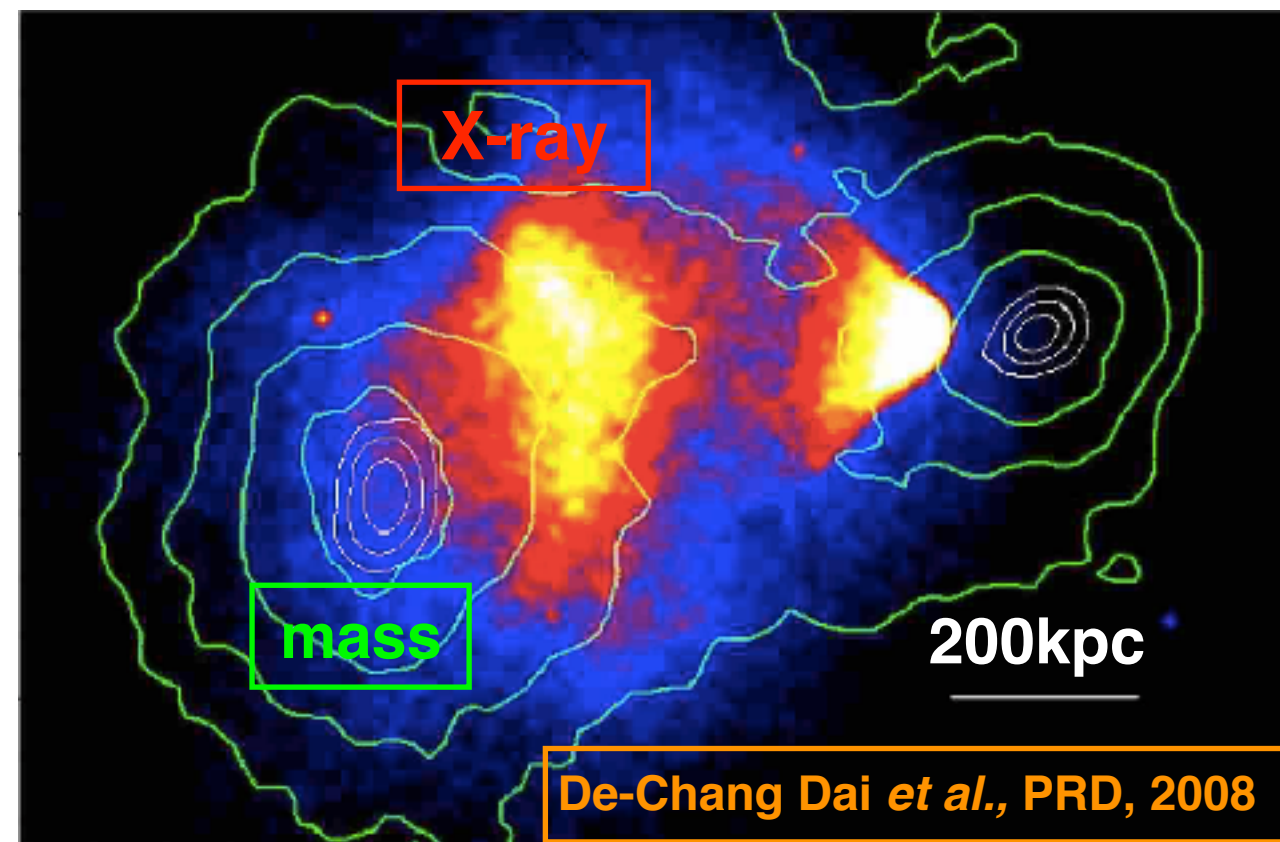
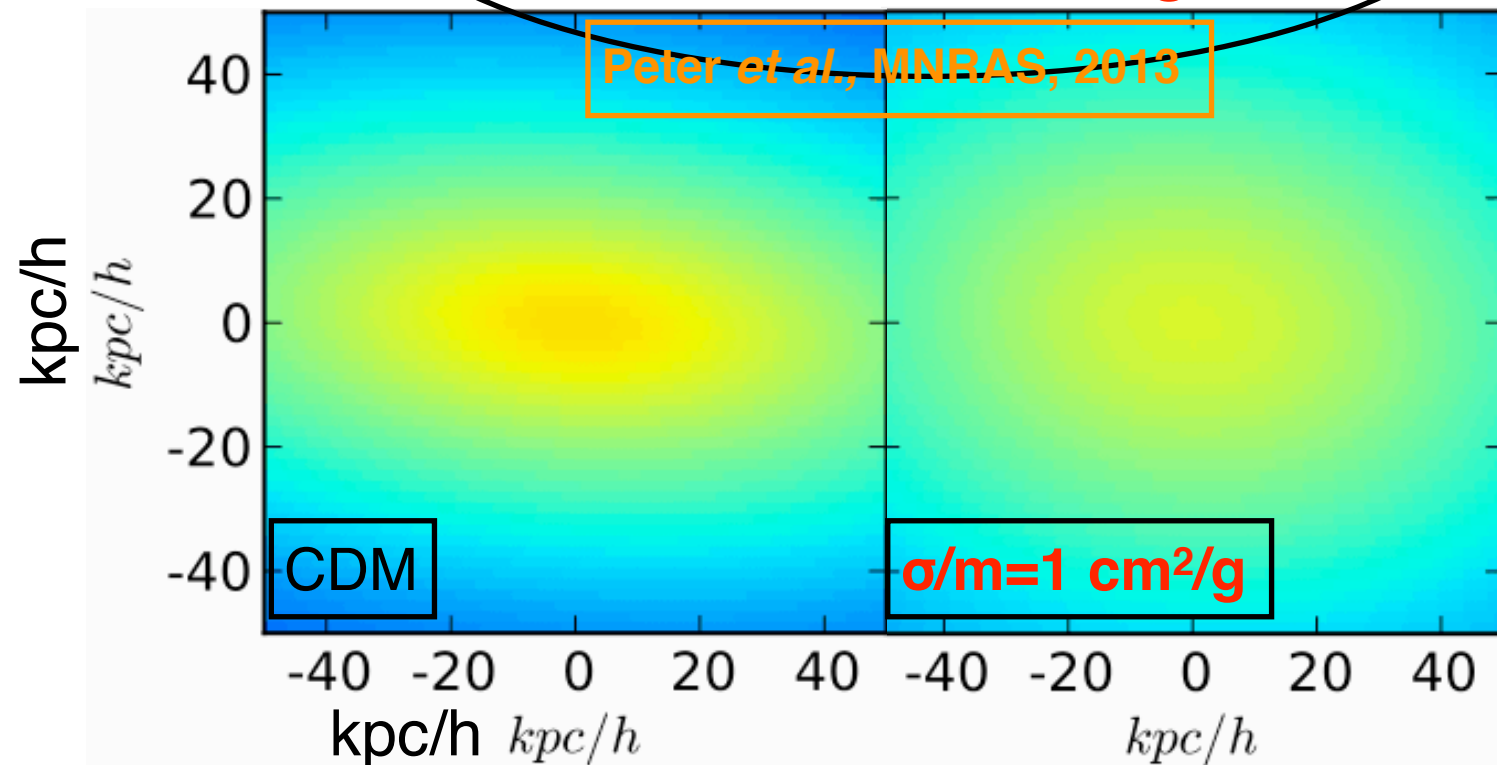
(offset)  $\sigma/m < 0.47 \text{ cm}^2/\text{g}$

Harvey *et al.*, Science, 2015

$V_{\text{max}} \sim 1000 \text{ km/s}$   
 $\leftrightarrow$  galaxy:  $V_{\text{max}} \sim 100 \text{ km/s}$

$\sigma/m = 0.5-5 \text{ cm}^2/\text{g}$

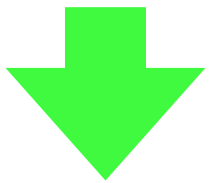
Peter *et al.*, MNRAS, 2013



# Particle physics models I

The constraints from galaxy clusters likely imply that dark matter self-interaction should **DIMINISH WITH INCREASING VELOCITY**, even though not necessarily so far

+ interestingly strong lensing of galaxy clusters may support SIDM with a smaller cross section  **$\sigma/m=0.1 \text{ cm}^2/\text{g}$**

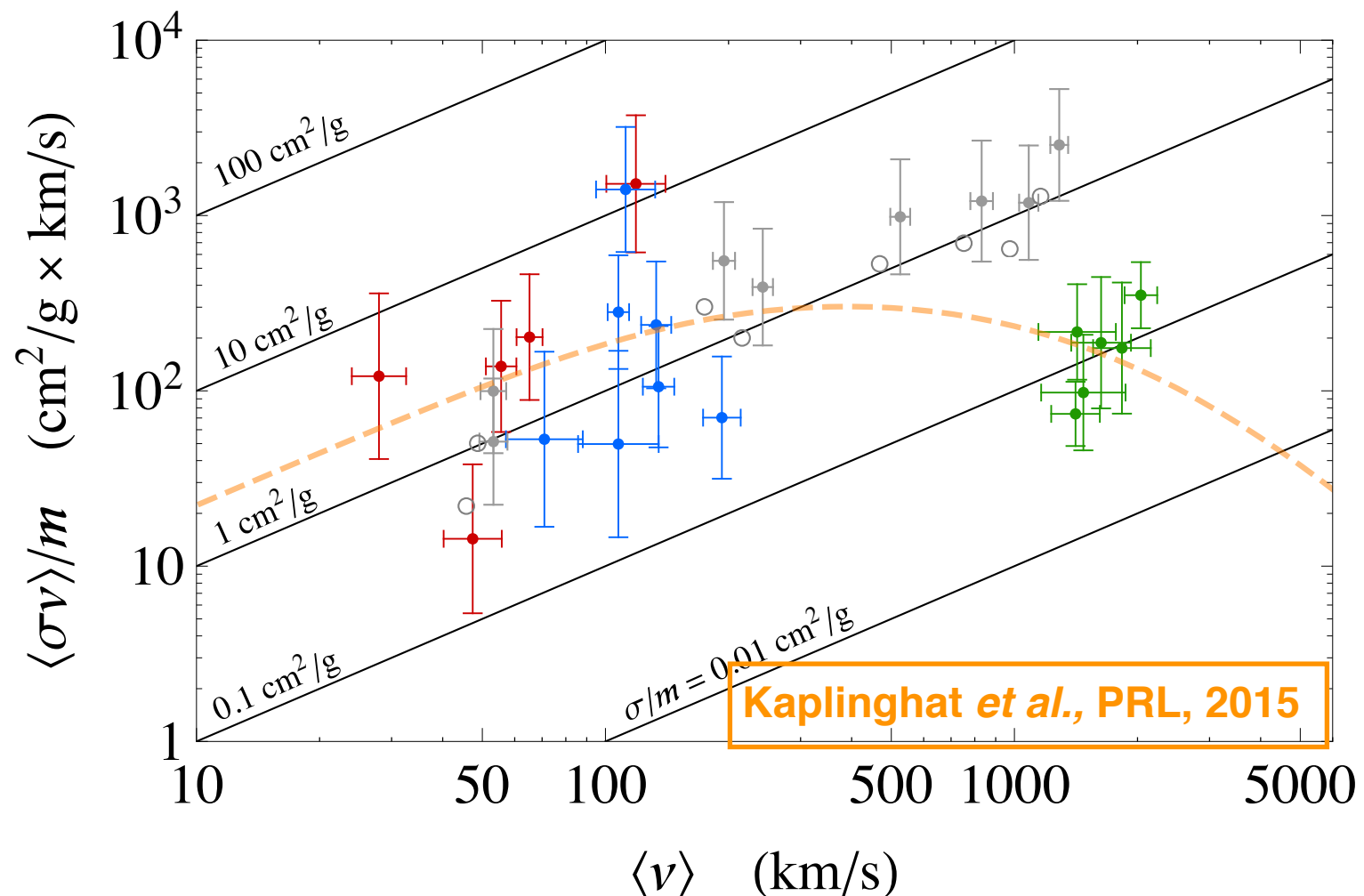


Tulin *et al.*, PRL, 2012

**velocity-DEPENDENT cross section:**

WIMP dark matter  
+ light mediator with

➔  **$m_{\text{med}} \sim m_{\text{DM}} v_{\text{gal}}/c$**   
 **$\sigma \sim 1/m_{\text{med}}^2$ : const.**  
**@(dwarf)galaxies**  
**( $V_{\text{max}} \sim 10\text{-}100 \text{ km/s}$ )**  
 **$\sigma \sim 1/v^4$ : suppressed**  
**@galaxy cluster**  
**( $V_{\text{max}} \sim 1000 \text{ km/s}$ )**

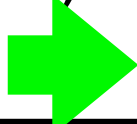


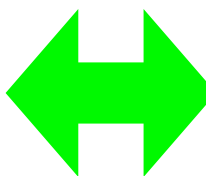
# Particle physics models II

If a **velocity-INDEPENDENT** cross section is concordant at both galaxy cluster and galaxy scales, self-interaction may originate from a **HIDDEN STRONG** interaction (geometrical cross section of strongly-interacting massive particle: **SIMP**)



Hochberg *et al.*, PRL, 2015

A simple hidden pion theory of  $m_\pi \sim f_\pi \sim 100\text{-}300$  MeV (non-linear sigma model with  $CP$  symmetry) works well: Wess-Zumino-Witten term (coefficient may be quantized and/or determined once a UV theory is specified)  $\mathcal{L}_{\text{WZW}} \supset \epsilon^{\mu\nu\rho\sigma} \text{Tr}[\pi \partial_\mu \pi \partial_\nu \pi \partial_\rho \pi \partial_\sigma \pi]$  freeze-out of  $3 \rightarrow 2$  reaction  correct relic abundance

 If the hidden sector is completely decoupled from the SM sector, the hidden sector is **HEATED UP** by the rest mass energy of SIMP through the  $3 \rightarrow 2$  reaction Carlson *et al.*, ApJ, 1992 comoving entropy density conservation  $\rightarrow T_h \propto 1/\ln(a)$  ( $T \propto 1/a$ )

 **KINETIC DECOUPLING** from the SM sector Kuflik *et al.*, PRL, 2016 has a big impact on the relic density of dark matter!! (cannibalism)

# Summary

- The long-standing cusp vs core problem is now highlighted as an **inner mass deficit problem** by state-of-the-art hydrodynamical simulations

- The inner mass deficit should be elaborated in a galaxy-by-galaxy basis, in contrast to the **concentration-mass relation**, which is hold even under the baryonic processes (**diversity problem**)

- Dark matter self-interaction, which intrinsically makes a mass distribution shallower in inner region, can solve the **inner mass deficit problem**, and also solve the **diversity problem** with the help of **scatter in baryon distributions**